

Design of general-purpose assistive exoskeleton robot controller for upper limbs†

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Abstract

Though research and development on exoskeleton robots have been active recently, the results have limitations in terms of independence from robot platforms and capability for general purposes. This paper presents a novel control scheme named the general-purpose assistive exoskeleton controller (GAEC) for upper limb assistive exoskeleton robots. With only the joint position information used, GAEC is designed to be applicable to any type of upper limb exoskeleton robot platform assisting human worker's common activities. GAEC works in two modes: (1) An external force is neutralized by generation of force with the same magnitude and the opposite direction. (2) The control system complies with the user's own force while maintaining the force that compensates for the external force neutralized in the first mode. In addition to theoretical description of the controller, computer simulation was conducted for validation using a robot model adopted from related studies. Two exemplary working scenarios were considered in the simulation: lifting and moving an object, and tightening a bolt with a wrench.

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Keywords: Exoskeleton robot controller; General-purpose assistive exoskeleton; Terminal sliding mode control; Upper limb exoskeleton robot

1. Introduction

Various research studies for developing and applying assistive exoskeleton robots have been reported [1-33]. Exoskeleton robots are designed to improve the user's physical performance in many fields where human's physical labor is required, such as manufacturing, construction, rescue, and military operations. In particular, upper limb exoskeletons for supporting the user's upper body in various tasks are very useful.

Development of an upper limb exoskeleton involves two main issues. One is design of the mechanical structure. Biomechanics of humans, such as parameters of limb links, joint center of rotation, and body segment dimension, contains a large variance and is also difficult to capture [24]. Incompatibility between biomechanics of human arm and mechanical structure of exoskeletons causes misalignments, which leads to the user's discomfort and limits the user's natural movement [24].

The second issue is design of the controller. An assistive exoskeleton robot is supposed to follow the user's intended motion, while rejecting external disturbances. However, capturing the user's motion intention exactly is still at research level [25]. This paper is focused on the controller design issue.

Control schemes for upper limb exoskeletons can be categorized into two types: Biological signal-based and nonbiological signal-based [25]. Electro-myography (EMG) is often used in the first type. This type of control scheme estimates the user's motion intention by classifying the EMG signal using neuro-fuzzy, fuzzy logic, and neural network techniques, or muscle model-based methods [26]. However, the use of EMG signals involves difficulties in terms of sensor placement, signal processing, and controller implementation [27]. Instead of using EMG, some researchers attempted to capture the user's motion intention by observing changes in muscle density [2] or muscle volume [4].

Non-biological signal-based control schemes use force or torque signals. This type of control scheme estimates the user's motion intention by analyzing the user's force on the robot. To obtain the user's force information, force/torque sensors can be set on a handle that the user grasps for manipulating the robot [9, 11, 12]. Force/torque sensors can be used in a different form in Ref. [10] where the sensors were designed as a ring-shaped arm coupling covering the arm. The use of force/torque sensors causes difficulties in locating the sensor and disadvantage in cost and size [25]. Thus, control schemes that use an observer instead of force/torque sensors have been proposed [13].

With regard to applications of existing upper limb exoskeleton robots, another limitation can be found. Some research studies were focused on optimizing performance of the robot

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in a specific application field or task, rather than covering human worker's common activities [7, 8, 14]. Additional problem is found in exoskeleton devices that use passive elements only. Most of them compensate for the weight of the user's particular body parts and were developed for use in industry [28]. These exoskeletons are light weight and low price, but their usage is limited and their performance is optimized only for a specific weight [29]. Recently, studies about soft wearable assistive robots that replace rigid structures with soft materials were reported [30-33]. These robots have advantage in wearability and misalignment problem, however, assistive force is limited due to lack of rigid structures.

In this paper, a novel control scheme for an upper limb assistive exoskeleton robot, named the general-purpose assistive exoskeleton controller (GAEC), is proposed. The controller is designed to assist human worker's common activities and also designed to be independent of the type of exoskeleton robot platform. The term "human worker's common activities" refers to activities that humans often do repeatedly in a working environment, such as carrying, pushing/pulling an object, and maintaining a certain body posture. Many activities found in industry [34-36] can be categorized into those activities.

Rather than trying to estimate the user's motion intention, GAEC complies only with the user's own force while compensating for the other forces. Thus, sensor systems for observing and analyzing the user's motion intention are not needed. GAEC requires only the joint position information, where measurable joint positions are available.

system model and dynamic equation used in the design of GAEC are introduced. Sec. 3 presents the concept and design the point $p \in \mathbb{R}^{3 \times 1}$, and $F_e \in \mathbb{R}^{6 \times 1}$ is the external work space of GAEC. GAEC was implemented and simulated using a robot model adopted from a related study. In Sec. 4, the simulation results are provided and discussed. Finally, the conclusion is presented in Sec. 5.

2. System modeling

Fig. 1 depicts the typical *n*-degrees of freedom (DOFs) exoskeleton robot system. The robot is assumed to be fixed at the base, which can be a backpack or a spine module, etc. Kinematics of the user is not considered because of its uncertainty and variability. Instead, only the user's force through the coupling is considered. Point \hat{p} on the user's hand in Fig. 1 indicates where the external force F_e is expected to be applied. \qquad c If the robot is equipped with a specific tool, the tool position corresponds to \hat{p} . Point p in Fig. 1 indicates where the actual external force is applied. It may not coincide with \hat{p} and may not be a fixed point.

Note that the user's force τ_h is expressed as a joint space force like the robot's force τ_r . In fact, the user's force is a work space force transmitted through the coupling. However, because the user knows intuitively how to manipulate the robot through the user's body, the user's force that is converted into

Fig. 1. Typical exoskeleton robot system model.

joint space will eventually lead to the desired motion. Therefore, it is convenient to consider the user's force as a joint space force. The external force is an unknown and unpredictable force from an external environment, and therefore, is expressed as a work space force.

Dynamics of the exoskeleton system can be written as

$$
D(q)\ddot{q} + C(q,\dot{q})\dot{q} + g(q) = \tau_r + \tau_h + J^T(q)F_e
$$
 (1)

which makes it applicable to any exoskeleton robot platform tia matrix, $C(q, \dot{q}) \in \mathbb{R}^{n \times n}$ is the Corilolis force and centrifu-
where measurable joint positions are available. gal term, $g(q) \in \mathbb{R}^{n \times 1}$ is the g This paper is organized as follows. In Sec. 2, a human-robot $\tau_{\hat{n}} \in \mathbb{R}^{m}$ represents the generalized force exerted by the robot stem model and dynamic equation used in the design of and user, respectively, $J(q) \in \$ where $q \in \mathbb{R}^{m \times 1}$ is the joint position, $D(q) \in \mathbb{R}^{m \times n}$ is the iner-´ ^Î¡ is the joint position, () *n n D q* ´ ^Î¡ is the inerthe matrix, (*n* is the Corilolis force and centrifu-

The point pace will eventually lead to the desired motion. Therefore, it is convenient to consider the user's force as a joint

space force. The external force is a Fig. 1. Typical exoskeleton robot system model.

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Signal term and the gravity term. In the gravity of the exoskeleton system $\tau_{h} \in \mathbb{R}^{n \times 1}$ represents the generalized force exerted by the robot *n*-DOF frame hand

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space force. The exter Dynamics of the exosketeton system can be written as
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term, $g(q) \in \mathbb{R}^{n\alpha_1}$ is $(q)\ddot{q} + C(q, \dot{q})\dot{q} + g(q) = \tau_r + \tau_s + J^T(q)F_c$ (1)
 $\text{Re } q \in \mathbb{R}^{n \times 1}$ is the joint position, $D(q) \in \mathbb{R}^{n \times n}$ is the iner-
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ere $q \in \mathbb{R}^{n \times 1}$ is the joint position, $D(q) \in \mathbb{R}^{n \times n}$ is the iner-

matrix, $C(q, \dot{q}) \in \mathbb{R}^{n \times 1}$ is the Corillois

Total inertia of the system consists of inertia of the robot, user, and external source, if an object is being held. Thus,

$$
D(q) = D_r(q) + D_h(q) + D_e(q)
$$

\n
$$
C(q, \dot{q}) = C_r(q, \dot{q}) + C_h(q, \dot{q}) + C_e(q, \dot{q})
$$

\n
$$
g(q) = g_r(q) + g_h(q)
$$
\n(2)

where the subscripts *r*, *h* and *e* denote the robot, user, and external source, respectively. The gravity term does not include the gravity of the external source. This is because it is convenient to include it in the external force term. Note that the user terms may not be obtained exactly. Therefore, the system equation may contain uncertainty.

3. Controller design

GAEC is a high-level controller that generates a target force signal, which is realized by each actuator force controller. In the following subsections, the control method, the controller architecture, and the performance of GAEC are discussed.

3.1 Method

Exoskeleton robots are supposed to comply with the user's force, while resisting external forces, which can be implemented by position control. Application of position control enables the robot to resist external forces in order to maintain its certain position. Therefore, the robot can be made comply with the user's force by deactivating the position control. However, the problem of distinguishing the source of force using position information only has to be solved.

One approach for resolving this problem is to separate forces by time such that GAEC can work in two modes: (1) The force is assumed to be from an external source, and it is neutralized by the position control. (2) While compensating for the external force, the control system complies with the user's force. In fact, many physical activities are performed similarly to the two-mode process.

If we consider an example of lifting an object, a person first needs to produce force to overcome the weight of the object. Then, the person can move the object by producing an additional force while maintaining the force against the weight. Similarly, for pushing/pulling an object, a person first needs to apply force that can overcome resistive forces such as friction, and then can push/pull the object by producing an additional force.

A couple of things are noted with this approach. First, a discontinuity in the user's behavior is unavoidable. Because the external force is neutralized by the position control, the user $dU/dt = u$. To simplify the discussion, let us suppose that the cannot move until the neutralization process is over. Secondly, the external force should be given like a step so that the end of the weight of the user and the robot, so that $\tau \approx \tau$ and the neutralization process can be determined clearly. If magnitude or direction of the external force keeps changing like vibration, the neutralization process cannot be completed.

3.2 Architecture

Fig. 2 shows a block diagram of GAEC. The main components are the position controller, double integration loop, external force estimator, and signal switch.

3.2.1 Position controller

The purpose of the position controller is to neutralize extersignal of GAEC is the target force, the output of the position controller is the target force signal to maintain a certain position. It converges to neutralization force with the same magnitude and the opposite direction compared to the external force.

The performance of the position controller in terms of robustness to disturbance and position tracking is critical to performance of GAEC. If the controller works better, the neutralization process takes less time, which results in less discontinuity in behavior. Any type of position controller of the second order or less, linear or nonlinear, can be used. However, to guarantee the performance of the position controller against uncertainty in model parameters and various external forces, an adaptive or robust controller is recommended.

Fig. 2. Block diagram of the control system.

3.2.2 External force estimator

The external force estimator is a kind of proportional integral compensator. For the constant external force F_e , the output of the position controller $u \in \mathbb{R}^{m}$ is accumulated in the integrator until it reaches F_e . As shown in Fig. 2, the target force signal $\tau_d \in \mathbb{R}^{n \times 1}$ is written as

$$
\tau_d = u - \hat{J}^T(q)\hat{F}_e = u + \gamma \hat{J}^T(q)\hat{J}^{-T}(q)U = u + \gamma U \tag{3}
$$

Jacobian matrix of \hat{p} , γ is a positive constant, and **Example 19 Example 19 Example 19 Constant Conduct Constant Constant Constant Constant Constant external force estimator**
 Example 2. Block diagram of the control system.
 3.2.2 External force estimator
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 Example 2. Block diagram of the control system.
 3.2.2 External force estimator

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of the position controller $u \in \mathbb{R}^{n-1}$ *p* is accumulated in the hotegral of the position controller $u \in \mathbb{R}^{n \times 1}$ is written as $r_a = u - \hat{J}^{\tau}(q)\hat{F}_c = u + \gamma \hat{J}^{\tau}(q)\hat{J}^{-\tau}(q)U = u + \gamma U$ (3) where superscript *T* denotes the transpose, $\hat{J}(q) \in \mathbb{R}^{n$ $\tau_a = u - \hat{J}^T(q)\hat{F}_z = u + \gamma \hat{J}^T(q)\hat{J}^{-T}(q)U = u + \gamma U$ (3)

where superscript *T* denotes the transpose, $\hat{J}(q) \in \mathbb{R}^{p,6}$ is the

Jacobian matrix of \hat{p} , γ is a positive constant, and
 $dU/dt = u$. To simplify the

$$
D(q)\ddot{q} + C(q,\dot{q})\dot{q} = \dot{U} + \gamma U + J^{T}(q)F_{q}
$$
\n⁽⁴⁾

$$
\dot{U} + \gamma U = \{ D(q)\ddot{q} + C(q,\dot{q})\dot{q} \} - J^{T}(q)F_{\rho}.
$$
 (5)

Suppose the system is stable, so that $\dot{q} \rightarrow 0$ as $t \rightarrow \infty$. If

$$
\gamma U = -\hat{J}^T(q)\hat{F}_e \approx -J^T(q)\hat{F}_e = -J^T(q)F_e .
$$
 (6)

nal force with position information only. Because the output ∞ . As the system is more stable and γ is larger, this process takes less time.

Stability of the system can be guaranteed better by adding a dissipation term to the position controller. For a positive constant *K* and the output of the original position controller u_0 , let the weight of the user and the robot, so that $\tau_r \approx \tau_d$ and
 $\tau_k = g(q)$. Then, Eq. (1) becomes
 $D(q)\ddot{q} + C(q,\dot{q})\dot{q} = \dot{U} + \gamma U + J^T(q)F_c$ (4)
 $\dot{U} + \gamma U = \{D(q)\ddot{q} + C(q,\dot{q})\dot{q}\} - J^T(q)F_c$. (5)

Suppose the system is stabl $u = u_0 - K\dot{q}$. Then, τ_d becomes *D(q)* $\ddot{q} + C(q, \dot{q})\dot{q} = U + \gamma U + J^T(q)F_e$ (4)
 $\dot{U} + \gamma U = \{D(q)\ddot{q} + C(q, \dot{q})\dot{q}\} - J^T(q)F_e$. (5)

Suppose the system is stable, so that $\dot{q} \rightarrow 0$ as $t \rightarrow \infty$. If

is chosen such that $\hat{p} \approx p$, Eq. (5) becomes
 $\gamma U =$ $U + \gamma U = \{D(q)\ddot{q} + C(q, \dot{q})\dot{q}\} - J^T(q)F_c$. (5)

Suppose the system is stable, so that $\dot{q} \rightarrow 0$ as $t \rightarrow \infty$. If
 \dot{p} is chosen such that $\dot{p} \approx p$, Eq. (5) becomes
 $\gamma U = -\dot{J}^T(q)\dot{F}_c \approx -J^T(q)\dot{F}_c = -J^T(q)F_c$. (6)
 Suppose the system is stable, so that $\dot{q} \rightarrow 0$ as $t \rightarrow \infty$. If

is chosen such that $\hat{p} \approx p$, Eq. (5) becomes
 $\gamma U = -\hat{J}^T(q)\hat{F}_e \approx -J^T(q)\hat{F}_e = -J^T(q)F_e$. (6)

Thus, $\hat{F}_e \approx F$ and the external force is neutralized

$$
\tau_d = u_0 + \gamma U_0 - K\dot{q} - \gamma K e \tag{7}
$$

where $e = q - q_0$ for the desired steady-state position q_0 . Let us introduce Lyapunov function candidate as the mechanical energy of the system.

$$
V = \frac{1}{2} \left\{ \dot{q}^T D(q) \dot{q} + e^T \gamma K e \right\}.
$$
 (8)

According to the principle of the conservation of mechanical energy, the time derivative of *V* is equal to the power pro-3512 *H. Seo and S. Lee / Journal of Mechanical Science and Technology 33 (7) (2019) 3509-3519*

According to the principle of the conservation of mechani-

cal energy, the time derivative of *V* is equal to the power pro *H. Seo and S. Lee / Journal of Mechanical Science and Technology 33 (7) (2019) 35*

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 $(q) + J^T(q)F_e\frac{1}{2} + \dot{q}^T\gamma K\dot{e}$
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rding to the principle of the conservation of mechani-

rgy, the time derivative of *V* is equal to the power pro-

y the applied

$$
\dot{V} = \dot{q}^T \left\{ \tau_r - g(q) + J^T(q) F_e \right\} + \dot{q}^T \gamma K \dot{e}
$$
\n
$$
= \dot{q}^T \left\{ u_0 + \gamma U_0 - g(q) + J^T(q) F_e \right\} - \dot{q}^T K \dot{q} \ . \tag{9}
$$

Therefore, by choosing K such that an inequality

$$
\left\| \dot{q}^T \left\{ u_0 + \gamma U_0 - g(q) + J^T(q) F_\varepsilon \right\} \right\| \le K \left\| \dot{q} \right\|^2.
$$
 This logic may not we
trollers However, effect

to be satisfied, stability of the system is guaranteed.

3.2.3 Double integration

The double integration loop makes the robot comply with the user's force by deactivating the position controller, while maintaining \hat{F}_e . This part is inspired by the theory of impulse and momentum. A change in momentum is equal to the im pulse:

$$
\Delta(mv) = m\Delta v = \int Fdt \ . \tag{10}
$$

Accordingly, the desired velocity is set at $\dot{q}_d = \int \tau_h dt$.
However, because there is no way for measuring the user's force τ_h , it cannot be used directly. Instead, using the property b that the output of the position controller reacts to the user's force, *ρu* is used, where *ρ* is a positive constant. Therefore, the desired velocity is set as 1.3 **Double integration**

the robot comply with

is compensated.

the double integration loop makes the robot comply with

intaining \hat{F}_e . This part is inspired by the theory of impulse

the signal switch

to the do *d* **a d a d a a a d a d a a d a d a d a d a d a d a d a d a d a d a d a d a d a d a d a d a a a d a a a a a a a** Accordingly, the desired velocity is set at $\dot{q}_z = \int_{\tau_i} dt$. updated, the position controller starts function
wever, because there is no way for measuring the user's cannot be moved. Ibvoever, when the soutier
the expre

$$
\dot{q}_d = -\rho \left[u dt \right]. \tag{11}
$$

Note that the sign is negative since u is a reaction to τ_h . To guarantee stability of q_d , a dissipation term can be added, such as

$$
\ddot{q}_d = -\rho u - b\dot{q}_d \tag{12}
$$

where *b* is a positive constant.

$$
u \approx \lambda_j \ddot{q}_d + \lambda_j \dot{q}_d + \lambda_0 q_d + \omega(q, \dot{q}, \ddot{q})
$$
\n(13)

where λ_0 , λ_1 and λ_2 are positive constants or 0. For example, for a simple proportional derivative controller, $\lambda_2 = 0$ and $\omega = -\lambda_1 \dot{q} - \lambda_0 q$, so that $u = -\lambda_1 \dot{e} - \lambda_0 e$, where $e = q - q_d$. Substituting Eq. (12) into Eq. (13) and differentiating twice, we have der the following general expression of u
 $a_2\ddot{q}_d + \lambda_1\dot{q}_d + \lambda_0q_d + \omega(q,\dot{q},\ddot{q})$ (
 a_0 , λ_1 and λ_2 are positive constants or 0. For example

mple proportional derivative controller, $\lambda_2 = 0$ a
 $\dot{q} - \$ and λ_2 are positive constants or 0. For example,

e proportional derivative controller, $\lambda_2 = 0$ and
 $\lambda_0 q$, so that $u = -\lambda_1 e - \lambda_0 e$, where $e = q - q_d$. Sub-

(12) into Eq. (13) and differentiating twice, we
 $+\lambda_1 q_d$

$$
\begin{aligned}\n\ddot{u} &= \lambda_2 q_d^{(4)} + \lambda_1 q_d^{(3)} + \lambda_0 \ddot{q}_d + \ddot{\omega} \\
&= -\lambda_2 \left(\rho \ddot{u} + b q_d^{(3)} \right) - \lambda_1 \left(\rho \dot{u} + b \ddot{q}_d \right) - \lambda_0 (\rho u + b \dot{q}_d) + \ddot{\omega} \\
&= -\rho \left(\lambda_2 \ddot{u} + \lambda_1 \dot{u} + \lambda_0 u \right) - b \left(\lambda_2 q_d^{(3)} + \lambda_1 \ddot{q}_d + \lambda_0 \dot{q}_d \right) + \ddot{\omega} & \text{turne} \\
&= -\rho \left(\lambda_2 \ddot{u} + \lambda_1 \dot{u} + \lambda_0 u \right) - b(\dot{u} - \dot{\omega}) + \ddot{\omega} & \text{stopp}\n\end{aligned}
$$

or

$$
p(\lambda_2 \ddot{u} + \lambda_1 \dot{u} + \lambda_0 u) + (\ddot{u} + b\dot{u}) = \ddot{\omega} + b\dot{\omega}
$$
 (14)

(9) walue of ρ , Eq. (14) becomes r and Technology 33 (7) (2019) 3509-3519
 $\rho(\lambda_2 \ddot{u} + \lambda_1 \dot{u} + \lambda_0 u) + (\dot{u} + b\dot{u}) = \ddot{\omega} + b\dot{\omega}$ (14)

ere $q_a^{(n)}$ is *n*-th derivative of q_a . For a sufficiently large

ue of ρ , Eq. (14) becomes
 $\lambda_2 \ddot{u} + \lambda_$ ie and Technology 33 (7) (2019) 3509-3519

or
 $\rho(\lambda_2 \ddot{u} + \lambda_1 \dot{u} + \lambda_0 u) + (\ddot{u} + b\dot{u}) = \ddot{\omega} + b\dot{\omega}$

where $q_a^{(n)}$ is *n*-th derivative of q_a . For a sufficie

value of ρ , Eq. (14) becomes $q_d^{(n)}$ is *n*-th derivative of q_d . For a sufficiently large

$$
\lambda_2 \ddot{u} + \lambda_1 \dot{u} + \lambda_0 u = \frac{1}{\rho} \left((\ddot{\omega} + b\dot{\omega}) - (\ddot{u} + b\dot{u}) \right) \approx 0 \,. \tag{15}
$$

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ocrding to the principle of the conservation of mechani-

or

by the applied forces. If τ , $\approx \tau_a$,
 $\rho\left(\lambda_a \bar{u} + \lambda_i \dot{u} + \lambda$ *H. See and S. Lee / Journal of Mechanical Science and Technology 33 (7) (2019) 3509-3519*

ccording to the principle of the conservation of mechani-

or

or q^x , the time derivative of *V* is equal to the power pro-
 2 1 0 *u u u b u bu* 0 . ^l ^l ^l ^w ^w + + = + - + » ^r && & && & && & (15) This logic may not work for some nonlinear position controllers. However, effect of the double integration loop can be inferred. Eventually, *u* approaches 0 as λ_0 , λ_1 , $\lambda_2 \ge 0$, and \hat{F}_e is not updated, because it is the integration of *u*. This makes the robot comply with the user's force while the external force is compensated.

3.2.4 Signal switch

 $\vec{v} = \vec{q}^r \left\{ \vec{r}_c - g(q) + J^r(q) F_s \right\} + \vec{q}^r \gamma K \vec{e}$

= $\vec{q}^r \left\{ u_6 + \gamma U_0 - g(q) + J^r(q) F_s \right\} - \vec{q}^r K \vec{q}$. (9) where $q_a^{(n)}$ is *n*-th derivative c

= $\vec{q}^r \left\{ u_6 + \gamma U_0 - g(q) + J^r(q) F_s \right\} \le K \|\vec{q}\|^2$. This logic (10) cussion in Sec. 3.2.3, when the switch is turned off, q_d is not Therefore, by choosing *K* such that an inequality

Therefore, by choosing *K* such that an inequality
 $\lambda x^2 + \lambda y + \lambda y = \pm (\left(\delta t + b\dot{a}\right) - \left(\dot{u} + b\dot{u}\right)) \approx 0$. (15)

This logic may not work for some nonlinear position con- $\int \tau_n dt$ updated. When q_d is fixed in the position controller, the robot The signal switch determines whether u is to be connected to the double integration loop or not. In other words, when the signal switch is off, the signal through the switch is 0, and when the switch is on, it is *u*. Therefore, according to the disupdated, the position controller starts functioning, and \hat{F}_e is cannot be moved. However, when the switch is turned on, because of the double integration loop, the position controller stops functioning and \hat{F}_e is fixed. The robot can be moved in this state while \hat{F}_e is maintained. In summary, the control law of GAEC can be written as **h**
 h

ch determines whether *u* is to be connected

gration loop or not. In other words, when the

surfact the signal through the switch is 0, and

s on, it is *u*. Therefore, according to the dis-

2.3, when the swit by with the user's force while the external force
ated.
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 e integration loop or not. In other words, when the

le integration loop or not. In other words, when the

de integration couply the *mal switch*
mal switch
gnal switch determines whether *u* is to be connected
uble integration loop or not. In other words, when the
vitch is off, the signal through the switch is 0, and
switch is on, it is *u*

$$
\tau_d = \begin{cases} u + \gamma \int u dt & \text{if Switch Off} \\ u_{\text{deact}} - \hat{J}^T(q) \hat{F}_e & \text{if Switch On} \end{cases}
$$
 (16)

where u_{deact} denotes output of the position controller deactivated by the double integration loop, which is nearly 0.

Thus, when an external force is applied and needs to be neutralized, the switch should be turned off. When the neutralization process is complete and the user wants to move, the signal switch should be switched on. This is done automatically according to the control phases, which is discussed in the next subsection.

3.3 Phases

[orce, *pu* is used, where *p* is a positive constant. Therefore, the this state while F_x is maintained. In summar

lesired velocity is set as
 $\dot{q}_a = -\rho \int u dt$. (11)

Note that the sign is negative since *u* is a reac $(\lambda_2 \ddot{u} + \lambda_1 \dot{u} + \lambda_0 u) - b(\lambda_2 q_d^{(3)} + \lambda_1 \ddot{q}_d + \lambda_0 \dot{q}_d) + \ddot{\omega}$
III. The end of phase III is the moment when the motion is the sign is negative since u is a reaction to τ_b . To where u_{data} denotes output of the position controller deach
 $-\frac{b\dot{q}}{dt}$, $-\frac{b\dot{q}}{dt}$, $-\frac{b\dot{q}}{dt}$, $-\frac{b\dot{q}}{dt}$, $-\frac{b\dot{q}}{dt}$, $-\frac{b\dot{q}}{dt}$, $-\frac{$ vated by the double integration loop, which is r

(12) Thus, when an external force is applied and

neutralized, the switch should be turned off.

trailzation process is complete and the user was

scally according to the *T_a* = $\frac{d}{dt}$

Note that the sign is negative since *u* is a reaction to τ_b . To

arantee stability of q_a a dissipation term can be added, such
 $\ddot{q}_a = -\rho u - b\dot{q}_a$
 $\ddot{q}_a = -\rho u - b\dot{q}_a$

(12) Thus, when con **be sign is negative since u is a reaction to** τ_b **.** To the sign is negative since u is a reaction to τ_b . To the u_{dust} denotes output of the position controller derivative constant.
 u be due to the constructiv blity of q_{ab} a dissipation ferm can be added, such

where u_{dust} denotes output of the position controller de
 $b\dot{q}_a$
 $b\dot{q}_a$
 $b\dot{q}_b$
 $\dot{q}_a + \lambda_q q_a + \omega(q, \dot{q}, \ddot{q})$

(12) Thus, when and external force is *u* vated by the double integration loop, which the integration loop, which multiplated, the switch should be turned for transferse applied and the use signal switch should be universely and $\lambda_1 \dot{q}_d + \lambda_q q_d + \omega(q, \dot{q}, \ddot$ $\vec{r}_d = \begin{vmatrix} t_a & t_a \\ t_{\text{data}} & -\hat{J}'(q)\hat{F}_e & \text{if Switch On} \\ t_{\text{data}} & -\hat{J}'(q)\hat{F}_e & \text{if Switch On} \\ t_{\text{total}} & -\hat{J}'($ that the sign is negative since u is a reaction to τ_b . To

se stability of q_a a dissipation term can be added, such where u_{base} denotes output of the position controller descti-
 $-\rho u - b\dot{q}_s$ (12) Thus, when an ext exaltity of q_a a dissipation term can be added, such

where u_{exact} denotes output of the position controller deacti-
 $-\rho u - b\dot{q}_a$

(12) Thus, when an external force is applied and needs to be

is a positive constan $-\rho u - b\dot{q}_a$

is a positive constant.

is a positive constant.

is a positive constant.

is a positive constant.

der the following general expression of u

is a meteral for the switch should be turned off. When the surv $\lambda_4 \lambda_5$ and λ_2 and λ_3 and $\lambda_4 \lambda_5$ if λ_6 and differentiating twice we have λ_7 and λ_8 and λ_9 and the sign is negative since u is a reaction to τ_b . To where u_{dual} denotes output of the p bte that the sign is negative since u is a reaction to τ_b . To where u_{head} down ϵ the position controller deacti-
 $u_{\text{head}} = -\lambda u - b\dot{q}$,
 $\lambda_i \dot{q}_i + \lambda_i q_i + \lambda_i q_i + \alpha_i q_i$, and $\lambda_i \dot{q}_i + \lambda_i q_i + \lambda_i q_i + \alpha_i q_i$, and λ nitic stability of q_n a dissipation term can be added, such
 $= -\mu - b\dot{q}_n$
 $= -\mu - b\dot{q}_n$
 $= -\mu + b\dot{q}_n$ an extend by the double integration loop, which is n
 $\alpha \cdot b$ is a positive constant.

(12) Thus, when an external force is applied and

neutralized, the switch should be turned off. V

railization process is complete a $\tau_d = \begin{cases} \n\tau_d = \frac{1}{2} & \text{if } \lambda_d = \frac{1}{2} \lambda_d \\ \n\mu_{\text{data}} = \hat{J}^T(q) \hat{F}_e & \text{if Switch On} \n\end{cases}$

bility of q_{ds} a dissipation term can be added, such
 $-\hat{b}q_d$ (12) Thus, where μ_{data} denotes output of the position
 $-\hat{b}q$ the sign is negative since u is a reaction to τ_b . To

bility of q_a , a dissipation term can be added, such

where u_{data} denotes output of the position controller de-
 $b\dot{q}_a$
 $-\dot{b}\dot{q}_a$

(12) Thus, when an ex blitty of q_a , a dissipation term can be added, such

where u_{dual} denotes output of the position contra
 $\frac{1}{2}$ $\frac{1}{2}$ Thus, when an external force is applied and

reutralized, the southie integration loop, wh GAEC has three phases. In phase I, external forces are neutralized. When this process is complete, phase II is initiated. Phase II is an intermediate phase between phases I and III and the system waits for the user's force to be applied during phase II. Phase III is initiated when the user's force is applied. The signal switch is turned off in phases I and II but it is turned on in phase III. The robot's motion is allowed in phase stopped or changed abruptly, for example, because of envi-

Fig. 3. Cycle of phases.

ronmental constraints or change of the motion intention. In addition, when another external force is applied, it is also considered as the end of phase III. At the end of phase III, the system returns to phase I.

The cycle of phases and its shifting law are depicted in Fig. 3. The shifting law is implemented by evaluating the control signals. The shifting law of phases I and II uses *u*. If \hat{F}_e converges, *u* also converges to 0. Convergence of *u* can be determined by observing if the magnitude of *u* remains smaller than a threshold for a sufficiently long time span. Thus, the shifting law of phase I is defined as

where δ_1 and t_1 are positive constants. If δ_1 is too large and t_1 is set too short, the external force may not be neutralized successfully. If δ_1 is too small and t_1 is too large, the robot may not move for a much longer time than necessary. In phase II, considering the applied force is the user's force, the shifting law is defined as

where δ_2 represents a positive constant. If δ_2 is too large, too much force is required to initiate motion, or if δ_2 is too small, the shifting law becomes excessively sensitive.

The shifting law of phase III should be designed such that the end of motion can be determined. This can be achieved by where $I \in \mathbb{R}^{6\times6}$ is the identity matrix, $\hat{J} = \hat{J}(q)$, and using joint velocity \dot{q} . However, to avoid noise, \dot{q}_d can be $J = J(q)$. The magnitude of the residual force is determined used instead of \dot{q} . Furthermore, it may be more intuitive to by the matrix $\Delta \in \mathbb{R}$ used instead of \dot{q} . Furthermore, it may be more intuitive to use the work space velocity, $v_d = \hat{J}(q)\dot{q}_d$. In general, the ve-**10r** *t*₁ energy only when *P*= *P*. In pactice, *P* one
eide with *p* most of time. This results in incomple
eide with *p* most of time. This results in incomple
any not be neutralized success-
this paper. During ph locity reaches the maximum value during a certain motion, and then decreases to 0 as the motion is completed. If $\|v_{d}\|$ drops below a certain proportion of the maximum value observed, the motion can be considered to have been completed or stopped. A sudden change in the motion can be determined $\hat{p} = p$. mind by elsewing if the magnitude of a cannis smaller particular since as the plott particular stress
by the strength construction of the strength constrained by determining the constrained by the
magnitude plane of the s by observing $\dot{v}_d^T v_d = \frac{d}{dt} \left(\frac{1}{2} v_d^2 \right)$, which represents the change in plied force is the user's force, the shifting law is
 according to Eq. (6), where $\hat{J}_q = \sum_{i=1}^n J_{ij}^T J_{ij}^T$.
 SECUTE:
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 EVALUAT the velocity magnitude. A decrease in this value means force is being applied in the opposite direction to produce motion. If the value drops by a certain proportion in a sufficiently short Therefore, the shifting law of phase III is defined as

$$
\begin{aligned}\n\textbf{Shift to phase I if } & \|\mathbf{v}_d\| < \eta_m \|\mathbf{v}_d\|_{\max} \\
& \textbf{or} \quad \mathbf{v}_d^T \mathbf{v}_d < \eta_m \left(\mathbf{v}_d^T \mathbf{v}_d\right)_{\text{drop}} \quad \textbf{in } t_3\n\end{aligned}
$$

md Technology 33 (7) (2019) 3509-3519 3513
 Shift to phase I if $||v_a|| < \eta_m ||v_a||_{max}$
 or $v_a^T v_a < \eta_m (v_a^T v_a)_{drop}$ **in** t_3

are η_m and η_d are positive constants between 0 and 1, t_3 is a sitive constant, $||v_a||$ *md Technology 33 (7) (2019) 3509-3519* 3513
 Shift to phase I if $||v_d|| \le \eta_m ||v_d||_{max}$
 or $\dot{v}_d^T v_d < \eta_m (\dot{v}_d^T v_d)_{drop}$ **in** t_3

here η_m and η_d are positive constants between 0 and 1, t_3 is a

here η_m a *d d m d d drop v v v v* & & <^h **in** *^t*³ where *ηm* and *η^d* are positive constants between 0 and 1, t_3 is a **Shift to phase I if** $||v_a|| < \eta_m ||v_a||_{\text{max}}$
 Shift to phase I if $||v_a|| < \eta_m ||v_a||_{\text{max}}$
 or $\dot{v}_a^T v_a < \eta_m (\dot{v}_a^T v_a)_{\text{drop}}$ **in** t_3

where η_m and η_d are positive constants between 0 and 1, t_3 is a

positive *dian d* η_d **d** η_d *d d d* η_d *d d* η_d *d d* η_d *d d* ³⁵¹⁹
<sup>*v_d* $\left\| \sum_{\text{max}} \left(\dot{v}_d^T v_d \right) \right\|_{\text{drop}}$ **in** t_3

mstants between 0 and 1, t_3 is a

e maximum of observed $\left\| v_d \right\|$,
 $\dot{v}_d^T v_d$ when it starts to drop. If

is too small, the shifting law

ersa.
</sup> η_m and η_d are too large and t_3 is too small, the shifting law becomes too sensitive, or vice versa. *d* $\eta_m ||v_d||_{\text{max}}$
 $\eta_m ||v_d||_{\text{max}}$
 $\eta_m (v_d^T v_d)_{\text{drop}}$ in t_3
 e constants between 0 and 1, t_3 is a
 d to the maximum of observed $||v_d||$,

of $v_d^T v_d$ when it starts to drop. If
 d t_3 is too small, the sh

The values of δ_1 , t_1 , δ_2 , η_m , η_d and t_3 can be determined by observing $||u||$, $||v_d||$ and $\dot{v}_d^T v_d$. The discontinuity in behavior can be minimized by an appropriate choice of these values. They may have to be tuned or optimized by considering tradeoff. Additional conditions can be applied to the shifting law or a different design of the shifting law is possible.

3.4 Residual force

Shift to phase II if $||u|| < \delta$, for t_1 perfectly only when $\hat{p} = p$. In practice, \hat{p} does not coin-Although the external force is assumed static, each joint experiences a different force as the joint positions change. The external force estimator was designed to resolve this problem by estimating the external force in the workspace, and then converting it into the joint space force. However, this works and $(\hat{v}'_a v_a)_{\text{loop}}$ is the value of $\hat{v}'_a v_a$ when it starts to drop. If η_m and η_d are too large and t_3 is too small, the shifting law becomes too sensitive, or vice versa. The values of δ_1 , t_1 , δ_2 cide with *p* most of time. This results in incomplete compensation of the external force, which is called residual force in this paper. During phases I and II, with joint position $q = q_0$, \hat{F}_e converges to can be minimized by an appropriate choice of these values.

eye may have to be tuned or optimized by considering trade-
 Additional conditions can be applied to the shifting law or

ifferent design of the shifting law i ear co-trainmizate of y an explorate conce or entered interest.
The properation and complision contributed in the shifting law or
 Thesidual force
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 Residual forc 3.4. The system of the shifting law is possible.

3.4 **Residual force**

Although the external force is assumed static, each joint experiences a different force on the joint positions change. The external force estimator w Although the external force is assumed static, each joint ex-
periences a different force as the joint positions change. The
external force estimator was designed to resolve this problem
by estimating the external force i Although the external force is assumed static, each joint ex-

reinces a different force as the joint positions change. The

erand force estimator was designed to resolve this problem

estimating the external force in the orce estimator was designed to resolve this problem

tring the external force in the workspace, and then

i it in to the joint space force. However, this works

only when $\hat{p} = p$. In practice, \hat{p} does not coin-

p *J* sesumal true weaken in the works packet and the magnitude of the residual force is determined of the external force, this works berfectly only when $\hat{p} = p$. In practice, \hat{p} does not coincide with *p* most of ti converting it muon triguarity can be joint space tonce. However, this works
perfectly only when $\hat{p} = p$. In practice, \hat{p} does not coin-
cide with p most of time. This results in incomplete compen-
sation of the ext or we verter

or $\vec{v}_s \vec{b}_{n,m}$, $\vec{n}_{n,d}$ and t_3 can be determined by

and $\vec{v}_3^T \vec{v}_n$. The discontinuity in behav-

by an appropriate choice of these values.

by an appropriate choice of these values.

butured of the external force, which is called residual force in
of the external force, which is called residual force in
per. During phases I and II, with joint position $q = q_0$,
werges to
 $\hat{J}_0^{-T} J_0^T F_c$. (17)
ing to Eq. (6) ion of the external force, which is called residual force in

spaper. During phases I and II, with joint position $q = q_0$

converges to
 $\hat{F}_e = \hat{J}_0^{-T} J_0^T F_e$. (17)

ording to Eq. (6), where $\hat{J}_0 = \hat{J}(q_0)$ and $J_$

$$
\hat{F}_e = \hat{J}_0^{-T} J_0^{T} F_e \ . \tag{17}
$$

Shift to phase III if $||u|| > \delta_2$ according to Eq. (6), where $\hat{J}_0 = \hat{J}(q_0)$ and $J_0 = J(q_0)$.
When the system shifts to phase III, with a new joint position $\hat{F}_e = \hat{J}_0^{-T} J_0^{T} F_e$.

according to Eq. (6), where $\hat{J}_0 = \hat{J}(q_0)$ and $J_0 = J($

When the system shifts to phase III, with a new joint pos
 q, the residual force is
 $F_e - J^{-T} \hat{J}^T \hat{F}_e = (I - J^{-T} \hat{J}^T \hat{J}_0^{-T$

$$
F_e - J^{-T} \hat{J}^T \hat{F}_e = (I - J^{-T} \hat{J}^T \hat{J}_0^{-T} J_0^T) F_e = \Delta^T F_e
$$
 (18)

 $\int_{\gamma}^{1} f(x) dx$
 $\int_{\gamma}^{1} f(x) dx$ is the identity matrix, $\hat{J} = \hat{J}(q)$, and

magnitude of the residual force is determined
 $\Delta \in \mathbb{R}^{6\times6}$, and Δ can be rewritten as
 $\int_{1}^{1} f(x) dx$ $\int_{1}^{1} f(x) dx$ $\int_{1}^{1} f(x) dx$

$$
\Delta = I - J_0 \hat{J}_0^{-1} \hat{J} J^{-1} = \left(J \hat{J}^{-1} - J_0 \hat{J}_0^{-1} \right) \left(J \hat{J}^{-1} \right)^{-1} . \tag{19}
$$

time, a sudden change in the motion is supposed to occur. removed perfectly even if $\hat{p} = p$. However, this problem can Converges to
 $\hat{F}_e = \hat{J}_0^{-T} J_0^T F_e$. (17)

cording to Eq. (6), where $\hat{J}_0 = \hat{J}(q_0)$ and $J_0 = J(q_0)$.

then the system shifts to phase III, with a new joint position

the residual force is
 $F_e - J^{-T} \hat{J}^T \hat{F}_e =$ $\hat{F}_e = \hat{J}_0^{-T} J_0^T F_e$. (17)
 p according to Eq. (6), where $\hat{J}_0 = \hat{J}(q_0)$ and $J_0 = J(q_0)$.

When the system shifts to phase III, with a new joint position
 p, the residual force is
 $F_e - J^{-T} \hat{J}^T \hat{F}_e = (I - J^{$ is applied to each center of mass of the robot and the user's body parts. Therefore, because the external force estimator considers all forces applied to \hat{p} , the residual force cannot be *q*, the residual force is
 $F_e - J^{-T} \hat{J}^T \hat{F}_e = (I - J^{-T} \hat{J}^T \hat{J}_0^{-T} J_0^T) F_e = \Delta^T F_e$ (18)

where $I \in \mathbb{R}^{666}$ is the identity matrix, $\hat{J} = \hat{J}(q)$, and
 $J = J(q)$. The magnitude of the residual force is determin be solved by employing a gravity compensator.

4. Simulation study

Computer simulation was conducted using Matlab for validation of GAEC. Two exemplary working scenarios were examined. In each scenario torque required for the user with the robot's assistance was compared to that without it. The user's torque with the robot's assistance was designed such that desired motion can be accomplished. If there is no desired motion, the user's torque is zero and only the robot's torque works. This can be written as

er's torque with the robot's assistance was designed such
\nIt desired motion can be accomplished. If there is no desired
\nition, the user's torque is zero and only the robot's torque
\nrks. This can be written as
\n
$$
\tau_h =\begin{cases}\n0 & \text{if } \dot{q}_h = 0 \\
D(q)\{K_1(q_h - q) + K_2(\dot{q}_h - \dot{q})\} & (20) \\
+C(q, \dot{q})\dot{q} + g(q) & \text{if } \dot{q}_h \neq 0 \\
+J^T(q)F_e - \tau_r & (20) \\
\text{where } K_1, K_2 \text{ are positive constants and } q_h \text{ is the user's desired}\n\end{cases}
$$
\n
$$
\text{where } K_1, K_2 \text{ are positive constants and } q_h \text{ is the user's desired}\n\begin{cases}\n\frac{1}{2} & \text{if } \frac{1}{2}m_2 = 0 \\
\frac{1}{2} & \text{if } \frac{1}{2
$$

where K_1 , K_2 are positive constants and q_h is the user's desired position. Note that q_h is different from q_d in the controller. Without the robot's assistance, the user must overcome all the forces alone. The user's torque required to accomplish the same work without the robot's assistance can be written as

$$
\tau_n^* = D(q) \{ K_1(q_n - q) + K_2(\dot{q}_n - \dot{q}) \} + C(q, \dot{q}) \dot{q} + g(q) + J^T(q) F_e .
$$
\n(21)

Substituting Eq. (20) to Eq. (1), the robot joint position q is computed. And q_h and F_e are defined according to situation in α the scenario, and τ_r is obtained by GAEC. The following subsections present the robot model, implementation of the controller and simulation results. With the robot model, the sysand τ_r is defined by the implemented controller.

4.1 Models

To show that GAEC is independent of the type of exoskeleton robot platform, this simulation employs a robot model that is adopted from related studies: Ebrahimi's [7, 8, 14] and Schiele's [37] exoskeletons. Ebrahimi's one actively supports 3 DOFs in the arm: Shoulder abduction/adduction, flexion/extension, and elbow flexion/extension. The remaining DOFs are freely movable by passive joints. The arm coupling is placed on both upper and lower arms. The spinal module to which the arm part is attached is mounted on the torso.

Schiele's exoskeleton is a non-anthropomorphic one where its arm part is attached under the chest. It has 8 active joints that generate torque corresponding to every rotation of the shoulder and wrist and flexion/extension of the elbow. It also has 6 passive joints to resolve the alignment problem. Both defined as Ebrahimi's and Schiele's models have measurable joint positions required to obtain the Jacobian. Thus, GAEC can be applied to both models. However, simulation in this paper was carried out using Ebrahimi's model.

Fig. 4. Simulation model.

 (21) the work space. However, in order to show that the number of that are the system of the controller the system of the controller the results of the tem dividend the controller terms for these must overcome all the controller terms force showed the controller terms of the system of To simplify the problem, we made a few modifications and assumptions on the model of the robot and the user. First, the robot's active joints are sufficient to manage all the force in the active DOFs does not affect applicability of GAEC, the shoulder and elbow flexion/extension were assumed to be the only active DOFs. The orientation of the end-effector was assumed to be still measurable. Secondly, the shoulder was assumed as a ball joint with a fixed center of rotation. Finally, point *p* was set to coincide with \hat{p} , and properties of the user arm (mass, length, etc.) were assumed to be known.

Fig. 4 shows the robot model. As shown, only the right arm was considered in the simulation. The user's body is also depicted to help the reader understand the model. In the figure, the base coordinate of the robot is O_B , and the coordinates of the active joints are O_1 and O_2 . The coordinates of the passive joints are not included, because these DOFs depend completely on the user. omy active Dors. The onetation of the entereform was assumed to be still measurable. Secondly, the shoulder was assumed as a ball joint with a fixed center of rotation. Finally, point *p* was set to coincide with \hat{p} ,

4.2 Controller implementation

The robot torque τ_r in Eq. (1) for the simulation is obtained by Eq. (16) and dynamics of the actuator force control. It was assumed in the simulation that the actuator controller performs

tion controller. It is known to be robust to parameter uncertainty and insensitive to disturbance, and also guarantee finite time convergence [38-42]. The terminal sliding surface was picted to help the reader understand the model. In the figure,
the base coordinate of the robot is O_B , and the coordinates of
the active joints are O_I and O_2 . The coordinates of the passive
joints are not included, the active joints are O_1 and O_2 . The coordinates of the passive
joints are not included, because these DOFs depend com-
pletely on the user.
4.2 **Controller implementation**
The robot torque τ , in Eq. (1) for the

$$
S = \dot{e} + Ce^{p_1/p_2} \tag{22}
$$

Fig. 5. Simulation scenario 1: Lifting and moving an object.

constants c_1 and c_2 . And p_1 and p_2 are on and p_2 were chosen as 3 and 5, respectively. The terminal sliding mode controller consists of equivalent control and discontinuous control [39]. The equivalent control was defined as consists of equivalent control and discontinuous control [39]. The equivalent control was defined as And p_1 and p_2 are odd integers w
8]. The values of p_1 and p_2 were chosely. The terminal sliding mode control
11 control and discontinuous control [3]
10 was defined as
 $\frac{1}{2}Ce^{p_1/p_2-1}$ + $C_0(q,\dot{q}) + g_0(q)$

$$
u_{eq} = D_0(q) \left(\ddot{q}_d - \frac{p_1}{p_2} C e^{p_1/p_2 - 1} \right) + C_0(q, \dot{q}) + g_0(q) \tag{23}
$$

where $D_0 = D_r + D_h$, $C_0 = C_r + C_h$ and $g_0 = g_r + g_h$. For a positive constant *ψ*, the discontinuous control was defined as

$$
\Delta u = \begin{cases} -\frac{s}{\delta} \omega & \text{if } ||S|| < \psi \\ -\frac{s}{||s||} \omega & \text{if } ||S|| \ge \psi \end{cases}
$$
 (24)

where *ω* is

$$
\omega = ||S|| ||D_0^{-1}|| (b_0 + b_1 ||q|| + ||\dot{q}||^2).
$$
 (25)

and b_0 , b_1 and b_2 are positive constants. In addition, a dissipation term was added to guarantee convergence of the external force estimator. The total terminal sliding controller is

$$
u = u_{eq} + \Delta u - K\dot{e} \tag{26}
$$

The values of the shifting law parameters δ_1 , t_1 , δ_2 , η_m , η_d and t_3 were chosen by trial and error, which resulted in $\delta_1 = \delta_2$ $= 0.4, t_1 = 0.06, t_3 = 0.01, \eta_m = 0.1$ and $\eta_d = 0.01$. According to the value of t_1 , the robot cannot be moved for at least 0.06 s between motions.

4.3 Scenario 1

Scenario 1 involves lifting and moving a 5 kg object. The object is lifted and held for a little while, and then moved to a higher location, as shown in Fig. 5, where the red line represents the trajectory of \hat{p} . This scenario is designed for simulating weight handling activities, such as manipulating a heavy tool. Simulation of this scenario shows how GAEC works for such activities.

Fig. 6. The user's torque for scenario 1. τ_1 and τ_2 denote flexion/extension torque on the shoulder and elbow, respectively.

Fig. 7. The robot's torque for scenario 1. τ_1 and τ_2 denote the flexion/extension torque on the shoulder and elbow, respectively. In the phase plot, 1, 2 and 3 refer to phases I, II and III, respectively.

Fig. 6 shows τ_h and τ_h^* for the scenario. Fig. 7 shows the robot torque τ_r and the torque by the external forces, and the cycle of phase for the same work. Note that the torque by the external forces is shown in the opposite sign, because it is the target of τ_r . Initially, the weights of the human arm and the

Fig. 8. Simulation scenario 2: Tightening a bolt.

robot itself were compensated. The object is lifted from 0.3 to 0.6 s, for which the weight of the object is not on the robot because it is supported by the user only.

The object is held from 0.6 to 1.5 s. At 0.6 s, the user's Eque is relieved and the robot starts to neutralize the weight torque is relieved and the robot starts to neutralize the weight of the object. Because the weight of the object is compensated for by the robot, the object can be held without the user's effort for the period.

The object is moved to a higher target location from 1.5 to
s, for which less torque is required for the user. It is noted
at magnitude of τ_h is larger than that of τ_h^* from about 1.8
2.8. This is because force in 2 s, for which less torque is required for the user. It is noted that magnitude of τ_h is larger than that of τ_h^* from about 1.8 to 2 s. This is because force in the same direction as the external force (weight of the object) is required for the period. As the weight of the object is compensated for by the robot, the user has to apply force against the compensation force.

The moving motion ends at 2 s and the object is put down at 2.2 s. The external force neutralization process is repeated in case of a situation change. The user returns to the initial posture from 2.5 s to 3 s. The magnitude of τ_h is larger than that of τ_h^* for this period because the robot's compensatory force, which is the weight of the user and robot combined, remains same as that at 2.5 s.

Additional inertia by the object causes fluctuation of τ_r to start at 0.6 s in phase I. The problem is undesirable because it may delay completion of phase I and make the user unmovable during phase I. By improving robustness of the position controller, it is possible to prevent delay of completion of phase I.

4.4 Scenario 2

Scenario 2 involves fastening a bolt with a wrench, as shown in Fig. 8, where the red line represents the trajectory of \hat{p} . This scenario was inspired by the overhead work required in car assembly lines. In this scenario, a 50 N force is applied to the wrench handle and then the wrench is pushed to fasten the bolt. Then, the force is released, and the wrench is returned to its initial position. It is possible to apply force by pushing with the user's body weight while posture of the arm is fixed. manufacturing field. This scenario corresponds to general pushing/pulling activities. Various activities can be done in a similar fashion, for exam-

Fig. 9. The user's torque for scenario 2. τ_1 and τ_2 denote the flexion/extension torque on the shoulder and elbow, respectively.

Fig. 10. The robot's for scenario 2. τ_1 and τ_2 denote the flexion/extension torque on the shoulder and elbow, respectively. In the phase plot, 1, 2 and 3 refer to phases I, II and III, respectively.

ple, grinding, drilling, and punching with power tools in the

manufacturing field.
Fig. 9 shows the user's torque τ_h and τ_h^* . Fig. 10 shows τ_r , *torque by the external forces, and cycle of the phases for sce-* nario 2. For $0 - 0.5$ s, the user applies a 50 N force gradually to the wrench handle along the +y-direction. The force is applied by the body weight with the arm posture fixed. As the robot generates torque to maintain the arm posture in that process, the user's effort is not needed. For $0.5 - 0.9$ s, the wrench is turned by approximately 60° around the +z-axis. The only torque required for the user is the inertia and residual force, since the torque necessary to apply 50 N on the arm is maintained by the robot.

The 50 N force is released at 0.9 s and the neutralization process is repeated. It can be observed that the torque on the user's shoulder required by the overhead posture is compen sated by the robot. From 1.5 s to 1.8 s, the user's initial posture is recovered. Here in scenario 2 again, the user needs to overcome only the inertia and residual force. The wrenchturning process is restarted at 2 s.

5. Conclusion

In order to overcome limitations of existing exoskeleton robots in terms of independence from robot platforms and capa bility for general purposes, a control scheme named GAEC was designed for upper limb exoskeleton robots. GAEC can assist the human worker's common activities working in the two modes by neutralizing a step-like external force and com plying the user's own force. Performance of GAEC was validated by computer simulation of two scenarios featuring two of the most common working activities. On condition that the user understands the working process of GAEC and the robot's joint position information is available, GAEC can be used for general purposes without dependence on the type of robot platform.

One of the main advantages of GAEC is that it does not require a sensor system to estimate the user's motion intention. As it requires the joint position information only, the exoskeleton platform can include more active DOFs at a lower price without concerns on sensor location. In addition, the capability for general purposes of GAEC is expected to promote development of exoskeleton platforms that can be used in various fields and also specialized for a specific field by an add-on application.

Some practical issues with GAEC may be discussed. For robots with a complex joint mechanism or several joints, it may be difficult or expensive to measure all the joint positions. In this case, GAEC can be complemented by employing an acceleration measurement device, such as an inertia measurement unit (IMU). Another issue is that the phase shifting law may be affected by measurement noise of the position. In order to avoid the problem, noise filtering can be as important as determining the shifting law constants.

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