

# Vibration analysis of new drill string system with hydro-oscillator in horizontal well†

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# **Abstract**

With the growth of oil and gas resource demand, the hydro-oscillator is widely used to enhance the Rate of penetration (ROP) and improve the efficacy in drilling various wells. The vibration model is the key issue of dynamics analysis and optimization of downhole tools. For the vibration analysis of the new drill string system with hydro-oscillator in the horizontal well, based on the design of the new hydro-oscillator and its operation conditions, the kinematics expressions are presented. Combined with the vibration force calculation results of the hydro-oscillator, the dynamics model of the new drill string system is established. Furthermore, the important features of vibration frequency, displacement, velocity and acceleration are discussed in the numerical example calculation results. By comparing the results of the calculation and experiment test, we can verify the correctness of the analysis model. With the hydro-oscillator vibration effect, the static friction between the drill string and wellbore is changed to the dynamic friction, so it can result in a significant increase in run length. At the same time, the ROP can be enhanced with the vibration effect. Moreover, with the parameters' adjustment according to the operation conditions, the analysis method and model can also provide references to the study of similar downhole tools dynamics or mechanical properties.

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*Keywords*: Drilling; Hydro-oscillator; Drill string; Vibration; Horizontal well; ROP

### **1. Introduction**

With the growth of oil and gas resource demand, drilling engineering faces more complex operation conditions [1, 2]. For example, directional drilling or ERD (Extended reach drilling) is widely used in oil and gas mining field; with the increasing development of well drilling towards deep layers, high temperature and complex tracking, it produces some new challenges. To a directional or horizontal well, the friction between the drill string and wellbore has become the key factor of reducing the ROP, which makes the Weight on bit (WOB) loss and low rock-breaking efficiency [3]. To solve the above problem, scholars in related fields have done much research [4-7]. Compared with other methods and technologies, downhole vibration or shock tools [8-13] can make drill string produce certain frequency and amplitude of periodic vibration, which can obviously reduce frictional resistance, improve drilling ROP and shorten drilling time.

The hydro-oscillator is a typical downhole tool which uses self-generated vibration to improve WOB transfer and decreases friction between drill string and wellbore efficiently. Furthermore, it has good adaptability in different and complex

drilling patterns. For its simple and effective work model, the hydro-oscillator quickly attracts the oil industry's eyes and has been successfully applied in many field sites. Unfortunately, to the best of our knowledge, for the complexity of drilling parameters, the existing research has focused on experimental or field tests, and did not make a detailed study on the tool working mechanism, theory model or vibration characteristics [14-18].

Therefore, this paper is devoted to a novel hydro-oscillator introduction and its vibration analysis in a horizontal drill string system, which provides a deep insight into the engineering applications. The rest of this paper is organized as follows: In Sec. 2, the design of new hydro-oscillator is introduced and the vibration of the new drill string system with the hydrooscillator in the horizontal well is analyzed, including the kinematics expressions and dynamics model. The analysis method and models can also provide reference for the study of similar downhole tools dynamics or mechanical properties. Sec. 3 carries out the numerical calculation and analysis of the vibration system, including important parameters such as displacement, velocity and acceleration. In Sec. 4, the laboratory experiment is designed according to the example parameters, and the results from the example and experiment verifies the rationality of the vibration analysis model. Finally, some conclusions are summarized.

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① Stator; ② Rotor; ③ Adapter; ④ Dynamic valv%e plate; ⑤ Static valve plate

Fig. 1. Design of the hydro-oscillator.

# **2. Hydro-oscillator design and analysis model**

#### *2.1 Hydro-oscillator design*

Considering the drilling field conditions, the new hydrooscillator is designed as shown in Fig. 1, consisting of the Positive displacement motor (PDM) including the stator and rotor ②, adapter ③ with three branch holes, dynamic valve plate ④ and static valve plate ⑤, etc.

The hydro-oscillator is assembled with the shock absorber, and the oscillator is at the side of near the drill bit. Under the downhole operation conditions, the drilling fluid flows through the rotor and stator, and the rotor movement determines the motion of the adapter and dynamic valve plate. Therefore, the flow area between the dynamic and static valve plate produces periodic change, which results in a periodic change of drilling fluid pressure. Coupled with the Bottom hole assembly (BHA) including the drill bit, hydro-oscillator and absorber, the pressure energy of drilling fluid turns into the mechanical energy of drill string, which causes the vibration of downhole tools.

#### *2.2 Kinematic characteristics of hydro-oscillator*

To analyze the vibration characteristics of the hydrooscillator, the kinematic characteristics must be first determined. Rather, according to the working mechanism of this new tool, the change rule of the flow area between the dynamic and static valve plate is the key issue to solve the kinematic characteristics of the tool.

First, the study of the screw motor movement features is the foundation of the hydro-oscillator kinematic analysis. For the need of high speed and small torque, the lobe configuration is 1:2, which is different from the normal configuration in most drilling motors. Setting the conjugate profile of the motor as hypocycloidal curve, the expressions of flow quantity of per revolution  $q$ , the sectional area of stator  $A_s$ , and the sectional **2.2 Kinematic characteristics of hydro-oscillator**<br>
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lial described as a circle with centralization the kinematic characteristics must be first deter

$$
q = (As - Ar)NTs = 8eDrh
$$
 (1)

$$
A_{\rm s} = \pi R^2 + 8eR
$$

$$
A_{\rm r} = \pi R^2 \tag{3}
$$

where *N* is the rotor ends lobes and here  $N = 1$ ,  $T<sub>S</sub>$  is the stator lead,  $e$  is the rotor eccentricity value,  $D<sub>r</sub>$  is the external diame-



(a) Motion characteristics of the rotor  $O<sub>1</sub>$ 



(b) Sectional drawing of the rotor moved in the stator

Fig. 2. Kinematic relationship of the rotor and stator.

ter of the stator, *h* is the motor screw pitch, and *R* is the rotor radius.

Moreover, for the hydro-oscillator, the rotor motion can be described as a circle with center  $O_1$  and radius  $e$ , pure rolling in another circle with center  $O_0$  and radius 2*e*. The movement and position relationship is shown in Fig. 2(a). Defining  $\omega$ as the rotation angular velocity of the rotor around its center  $O_1$ ,  $\omega_0$  as the revolution angular velocity of the rotor center  $O_1$  around the stator center  $O_0$ ,  $\omega$  can be given as (b) Sectional drawing of the rotor moved in the stator<br>
2. Kinematic relationship of the rotor moved in the stator<br>
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position relationship is shown in Fig. 2(a). Defining  $\omega$ <br>
the rotation angular velocity of the rotor acnumal its center<br>  $\omega$ ,  $\omega_0$  as the revolution ang

$$
\omega = 2\pi \frac{Q\eta_v}{q} \tag{4}
$$

where  $Q$  is the total flow rate,  $\eta_v$  is the flow efficiency. The relationship between  $\omega$  and  $\omega_0$  can be obtained as

$$
\omega = -\omega_0 \,. \tag{5}
$$

As for the center  $O_1$ , its motion trajectory is a straight line in Fig. 2(b). After a certain time *t* and for Eq. (5), the rotation angle  $\theta$  of the rotor center  $O_1$  is

$$
\theta = \omega t \tag{6}
$$

Defining the point  $O_2$  as one point on the circle  $O_1$ , the coordinate equation of  $O_2$  can be described as



(a) Structural drawings of the dynamic valve plate



(b) Real photo of the dynamic valve plate

Fig. 3. Parameters relationship on the dynamic valve plate.

$$
\begin{cases}\n x_2 = 0 \\
 y_2 = 2e \cos \omega t\n\end{cases}
$$
\n(7)

where  $E$  is the rotor eccentricity, which equals to the displacement between  $O_0$  and  $O_1$ .

. For connecting with the adapter and rotor, the dynamic valve plate is the same movement features with the rotor. The position relationship of the two flow holes on the static and dynamic valve plates is shown in Fig. 3.  $O_3$  is the center of the t dynamic valve plate,  $O_4$  is the center of the eccentric hole on  $\qquad$ the dynamic valve plate,  $O_5$  is the center of the static valve s plate, the circle  $O_3$  share the same axis with the circle  $O_3$  and is internally tangent with the circle  $O_4$ . At the initial time, the i angle between the line  $O_4 O_3$  and the axis *Y* is 120°.  $\epsilon$  cos ω (7)<br>
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is the rotor eccentricity, which equals to the dis-<br>
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thectween  $O_0$  and  $O_1$ .<br>
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e is the same movement features *x<sub>2</sub>* = 0<br> *x*<sub>2</sub> = 2<br> *x* = cos *x* = *x* (*x*) and *Q*<sub>1</sub>.<br> *x* + *x* = *x*) (*x*<sub>1</sub> + *x* = *x*) (*x*<sub>1</sub> + *x* = *x*) (*x*<sub>1</sub> + *x*<br> *x* or connecting with t *y*<sub>2</sub> = 0<br> *y*<sub>2</sub> = 2<br> *y*<sub>2</sub> the rotor eccentricity, which equals to the dis-<br>
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tween  $O_0$  and  $O_1$ .<br>
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the same movement features with the rotor. The where the symbol  $r_2$  represe [ $x_2 = 0$ <br>  $\left(x_3 = 0\right)$  The length of intersecting chord L is described by<br>  $\left(x_2 = 2e \cos \omega t\right)$ <br>
cere E is the rotor eccentricity, which equals to the dis-<br>
cere E is the rotor expansion between  $O_0$  and  $O_1$ .<br>
Correct ere E is the rotor eccentricity, which equals to the dis-<br>
cerment between  $O_0$  and  $O_1$ .<br>
Corrections with the adapter and rotor, the dynamic<br>
cerment between  $O_0$  and  $O_1$ .<br>
For connecting with the adapter and rotor

According to the analysis above, the motion equations of *O*<sup>4</sup> are obtained by

$$
\begin{cases}\n x_4 = e \sin \omega t + e_m \sin \left( \omega t + \frac{\pi}{6} \right) & \neq 0 \\
 y_4 = e \cos \omega t - e_m \cos \left( \omega t + \frac{\pi}{6} \right) & \text{Acc}\n\end{cases}
$$
\n(8)

dynamic valve plate central axis, as the distance  $O_3O_4$ . Defin-



Fig. 4. Parameters relationship on the static valve plate.

ing  $r_0$  as the radius of dynamic valve plate,  $r_1$  as the radius of eccentric hole,  $r'_0$  as the radius of circle  $O_3$  and *s* as the difference between  $r_0$  and  $r'_0$ ,  $e_m$  can be described as

$$
e_{\rm m} = r_0 - r_1 - s \tag{9}
$$

To the static valve plate, the center of the flow hole and static valve plate is the same point. Defining  $O_5$  as the center of the flow hole on the static valve plate, the displacement between the eccentric hole  $O_4$  and  $O_5$  can be given by the radius of dynamic valve plate.<br>
the radius of dynamic valve plate.<br>
the radius of dynamic valve plate.  $r_1$  as the radius of<br>
hole,  $r_0'$  as the radius of circle  $O_3$  and  $s$  as the<br>
between  $r_0$  and  $r_0'$ ,  $e_m$  **Example 18**<br> **Example 18**<br> **Example 18**<br> **e** factorizationship on the static valve plate.<br> **e** the radius of dynamic valve plate,  $r_1$  as the radius of<br> **c** hole,  $r_0'$  as the radius of circle  $O$ ; and  $s$  as the<br> **e** Parameters relationship on the static valve plate,  $r_1$  as the radius of<br>
tic hole,  $r'_0$  as the radius of circle  $O'_t$  and s as the<br>
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Subset to relationship on the static valve plate.<br>
Subset in the radius of circle  $r_0$  and s as the radius of circle  $O_6$  and s as the<br>
note between  $r_0$  and  $r'_0$ , *r*<sub>0</sub> as the radius of dynamic valve plate,  $r_1$  as the radius of<br>entric hole,  $r_0'$  as the radius of circle  $O_2$  and s as the<br>ference between  $r_0$  and  $r_0'$ ,  $e_m$  can be described as<br> $e_m = r_0 - r_1 - s$ . (9)<br>Fo the stat  $_{0}$  as the radius of dynamic valve plate,  $r_{1}$  as the radius of<br>tric hole,  $r_{0}^{'}$  as the radius of circle  $O_{3}$  and s as the<br>rence between  $r_{0}$  and  $r_{0}^{'}$ ,  $e_{m}$  can be described as<br> $=r_{0} - r_{1} - s$ . (9)<br>the stat

$$
\delta = \left[ e^2 + e_{\rm m}^2 - 2e \cdot e_{\rm m} \cdot \cos \left( 2\omega t + \frac{\pi}{6} \right) \right]^{\frac{1}{2}}.
$$
 (10)

The length of intersecting chord  $L$  is described as

$$
L = \frac{1}{\delta} \Big[ \Big( r_1 + r_2 + \delta \Big) \Big( r_1 + r_2 - \delta \Big) \Big( r_1 + \delta - r_2 \Big) \Big( r_2 + \delta - r_1 \Big) \Big]^{1/2} \tag{11}
$$

the radius of dynamic valve plate,  $r_1$  as the radius of<br>thole,  $r'_0$  as the radius of circle  $O'$ , and s as the<br>between  $r_0$  and  $r'_0$ ,  $e_m$  can be described as<br> $r_1 - s$ . (9)<br>tatic valve plate, the center of the flow ho where the symbol  $r_2$  represents the radius of the flow hole on the static valve plate and the yellow lines represent the trajectory of the circle  $O_4$  on the static valve plate affected by the dynamic valve plate under the working conditions, as shown in Fig. 4.

Setting  $\theta_1$  and  $\theta_2$  as the central angles of *L* corresponding to  $O_4$  and  $O_5$ , its expressions are given by

$$
\delta = \left[ e^{2} + e_{m}^{2} - 2e \cdot e_{m} \cdot \cos \left[ 2\omega t + \frac{\pi}{6} \right] \right]
$$
\n(10)  
\nThe length of intersecting chord *L* is described as  
\n
$$
L = \frac{1}{\delta} \left[ \left( r_{1} + r_{2} + \delta \right) \left( r_{1} + r_{2} - \delta \right) \left( r_{1} + \delta - r_{2} \right) \left( r_{2} + \delta - r_{1} \right) \right]^{\frac{1}{2}}
$$
\n(11)  
\nwhere the symbol  $r_{2}$  represents the radius of the flow hole on  
\nthe static value plate and the yellow lines represent  
\nthe trajectory of the circle  $O_{4}$  on the static valve plate affected  
\nby the dynamic valve plate under the working conditions, as  
\nshown in Fig. 4.  
\nSetting  $\theta_{1}$  and  $\theta_{2}$  as the central angles of *L* correspond-  
\ning to  $O_{4}$  and  $O_{5}$ , its expressions are given by  
\n
$$
\begin{cases}\n\theta_{1} = 2 \arcsin \left( \frac{L}{2r_{1}} \right) \\
\theta_{2} = 2 \arcsin \left( \frac{L}{2r_{2}} \right)\n\end{cases}
$$
\n(12)  
\nAccording to the change of the intersecting chord *L* increasing  
\nfrom 0 to  $2r_{1}$ , then decreasing from  $2r_{1}$  to 0, the time  
\nsymbols are defined as  $t_{1} < t_{2} < t_{3} < t_{4}$ . Moreover, when  
\n $r_{1} \le r_{2}$ ,  $t_{1}$  and  $t_{4}$  refer to the time  $L = 2r_{2}$ ,  $t_{2}$  and  $t_{3}$ 

where  $e_m$  is the eccentricity of the eccentric hole relative to symbols are defined as  $t_1 < t_2 < t_3 < t_4$ . Moreover, when dynamic valve plate central axis, as the distance  $O_3O_4$ . Defin-  $r_1 \le r_2$ ,  $t_1$  and  $t_4$  refe According to the change of the intersecting chord *L* increasing from 0 to  $2r_1$ , then decreasing from  $2r_1$  to 0, the time



Fig. 5. Position changes of the circles *O*4 and *O*<sup>5</sup> .

refer to the time  $L = 0$ . The motion characteristics between the circles  $O_4$  and  $O_5$  are in Fig. 5.

To the flow area *A* of drilling fluid, which is also the intersecting area of the two flow holes on static and dynamic valve plates, it is the basis for analyzing the energy conversion and drill string system vibration, and its expressions are, respectively, given by following: and  $O_5$  are in Fig. 5.<br>
field situation, the parameter<br>
the basis for analyzing the energy conversion and<br>
subsets the basis for analyzing the energy conversion and<br>
g system vibration, and its expressions are, respec-<br>

$$
\sum_{i=1}^{n} \frac{1}{x_i^2} \cdot \frac{1}{x_i^2} \cdot \frac{1}{y_i^2} \cdot \frac{1}{z_i^2 \cdot \theta_i - \frac{1}{2} L \delta}
$$
\n
$$
= \begin{cases}\n\frac{1}{2} \pi_i^2 \cdot \frac{1}{2} \pi_i^2 \
$$

2 2 2 2 <sup>2</sup> 1 1 1 2 2 1 2 3 4 2 <sup>1</sup> 2 3 ' ' 1 1 1 r + r 0, , 2 2 2 1 1 1 = r + r , , 2 2 2 *A r L for t t t t t <sup>r</sup> for t t t* <sup>p</sup> <sup>q</sup> <sup>q</sup> <sup>d</sup> <sup>p</sup> ì ï - Î U formula is as the following: í - - Î ï Î î (14) where ' <sup>1</sup>*t* and ' <sup>4</sup>*t* refer to the time <sup>1</sup> *L r* <sup>=</sup> <sup>2</sup> , ' <sup>2</sup>*t* and ' <sup>3</sup>*<sup>t</sup>* area *A*, and ' ' ' ' 1 2 3 4 <sup>0</sup> < < < < < *t t t t <sup>T</sup>* . Besides when the PDM works in a circle, the flow area *<sup>A</sup>* <sup>1</sup> <sup>2</sup> = 2 <sup>w</sup> <sup>w</sup> <sup>=</sup> . (15)

refer to the time  $L = 0$ , *T* refers to the time cycle of the flow

will periodically change twice, just as shown in Fig. 5. So the angular velocity of the flow area *A* is

$$
\omega_1 = \frac{2\pi}{T} = 2\omega \,. \tag{15}
$$

#### *2.3 Vibration analysis of drill string system*

According to the drilling field conditions, with the analysis results of kinematic characteristics, the vibration model of the drill string system with the hydro-oscillator can be established. Setting the drilling well as horizontal, and the drill string and downhole tools (including hydro-oscillator) are elastic deformation in drilling process, the vibration model of the drill string system is established, as shown in Fig. 6.

results of kinematic characteristics, the vibration model of the<br>
drill string system with the hydro-oscillator can be established.<br>
Setting the drilling system with the hydro-oscillator can be established.<br>
Setting the d Setting the drilling well as botizontal, and the drill string and<br>
Setting the drilling well as botizontal, and the drill string and<br>
downhole cools (including hydro-oscillator) are elastic defor-<br>
mation in drilling proc (*order)*<br>
(ariable foot including hydro-oscillator) are desired ederi-<br>
mation in drilling process, the vibration model of the drill<br>
string system is established, as shown in Fig. 6.<br>
In the analysis model, the symbol **Example 1981**<br>
For dill stiring acting on BHA,  $F_{\text{non-ons}}$  is the axial harmonic<br>
frogenerated by the hydro-oscillators,  $F_{\text{in}}$  is the harmonic<br>
frogenerated by the hydro-oscillators,  $F_{\text{in}}$  is the harmonic<br>
strict The analysis model, the symbol  $r_{\rm in}$  for the dial string and the symbol  $r_{\rm in}$  the symbol  $r_{\rm in}$  for the symbol string and the hydro-excilence precented by the hydro-excilence force per actives the transic frequent Mathematical diality process, the wintinum procedure and  $\theta$  the nearby served by the particular material by the hydro-oscillator,  $F_{\text{tot}}$  is the baseline of the same state force opper drill alternal diality and contro Fin the analysis model, the symbol  $F_{\rm esc}$ , nearest the force up-<br>
per drill string aceing on BHA,  $F_{\rm re,max}$  is the axial barmonic<br>
frome generated by the hydro-residuator,  $F_{\rm esc}$  is the harmonic<br>
frome generated by th In the analysis model, the symbol  $F_{\text{sta}}$  means the force upper drill string acting on BHA,  $F_{\text{h-oscillator}}$  is the axial harmonic force generated by the hydro-oscillator,  $F_{\text{har}1}$  is the harmonic force of drilling fluid acting on bit,  $F_{\text{har2}}$  is the axial force generated by the absorber,  $F_{\text{bit}}$  is the bit-rock interaction force, and  $m_i$  is the mass element of drill string,  $F_{\text{fric}}$  is the friction force between the drill string and borehole well,  $G_0$ is the BHA gravity,  $F_N$  is the support of the BHA. resulus of xenematic canceleristics, the vibration model of the dirlil string system with the hydro-oscillator can be established.<br>Setting the drilling well as horizontal, and the drill string and downhole tools (includin gy system while the intervolucional can be established.<br>
the drilling well as horizontal, and the drill string and<br>
le tools (including hydro-oscillator) are elastic defor-<br>
in drilling process, the vibration model of the *t* studenture characteristics, the vibration model of the hydro-oscillator can be established.<br>
the drilling well as horizontal, and the drill string and<br>
the drilling well as horizontal, and the drill string and<br>
to too g system win in enguro-oscillator, the directions can be established.<br>
the drilling well as horizontal, and the drill string and<br>
te tools (including hydro-oscillator) are elastic defor-<br>
n drilling process, the vibration In so knematic characteristics, the vivation model on the hand of the hail siting system with the hydro-oscillator can be established.<br>In string system with the hydro-oscillator can be established.<br>In the drilling well as **Example 2016** and we have observed and the diffusion can be concernanced and the drilli string and whilole tools (including hydro-oscillator) are elastic defortion in drilling process, the vibration model of the drill st ording to the drilling field conditions, with the analysis<br>of kinematic characteristics, the vibration model of the<br>ting system with the hydro-oscillator can be established.<br>the drilling well as horizontal, and the drill mation in drilling process, the vibration model of the drill<br>string system is established, as shown in Fig. 6.<br>In the analysis model, the symbol  $F_{\text{na}}$  means the force up-<br>per drill string acting on BHA,  $F_{\text{non-linear}}$  is string system is established, as shown in Fig. 6.<br>In the analysis model, the symbol  $F_{\text{na}}$  means the force up-<br>per drill string acting on BHA,  $F_{\text{h}}$  is the axial harmonic<br>force generated by the hydro-oscillator,  $F$ **i i c**

With the symbol definitions above, according to the drilling field situation, the parameters relationship can be analyzed.

$$
[\mathbf{M}]\ddot{\mathbf{u}}(t) + [\mathbf{C}]\dot{\mathbf{u}}(t) + [\mathbf{K}]\mathbf{u}(t) = \mathbf{F}_{\text{sta}} + \mathbf{F}_{\text{h-oscillator}}(t)
$$
  
+
$$
\mathbf{F}_{\text{har}1}(t) + \mathbf{F}_{\text{har}2}(t) + \mathbf{F}_{\text{bir}}(t) + \mathbf{F}_{\text{fric}}
$$
 (16)

of the drill string. [M] $\mathbf{u}(t) + [\mathbf{C}]\mathbf{u}(t) + [\mathbf{K}]\mathbf{u}(t) = \mathbf{F}_{sta} + \mathbf{F}_{\text{h-oscillator}}(t)$ <br>  $+ \mathbf{F}_{\text{hart}}(t) + \mathbf{F}_{\text{har2}}(t) + \mathbf{F}_{\text{bit}}(t) + \mathbf{F}_{\text{fric}}$ <br>
where [M] is the mass matrix, [C] is the dampin<br>
[K] is the stiffness matrix, and *u*

$$
\in (t_2, t_3). \qquad k_i = \frac{E_i A_i}{l_i} \tag{17}
$$

where  $E_i$  is Young's modulus,  $A_i$  is the element crosssectional area, and *l* is the element length.

where [M] is the mass matrix, [C] is the da<br>
[K] is the stiffness matrix, and  $u$  is the axia<br>
of the drill string.<br>
For the element  $k_i$  of the stiffness matrix, it<br>
lated by following<br>  $\bigcup (t_3, t_4)$ <br>  $\bigcup (t_3, t_4)$ <br>  $\$ (*t<sub>a</sub>, T*) of the drill string.<br>
For the element  $k_i$  of the stiffness matrix, it can lated by following<br>  $t_2$ )  $\cup (t_3, t_4)$ <br>  $k_i = \frac{E_i A_i}{l_i}$ <br>
(13)<br>
where  $E_i$  is Young's modulus,  $A_i$  is the element length.<br>
For the For the damping matrix, in drilling condition, it can be regarded as proportional to the mass matrix, and its calculation

$$
\bigcup (t_s, t_4) \qquad \qquad [C] = \alpha[M] + \beta[K] \qquad (18)
$$

 $+ \mathbf{F}_{\text{bar}}(t) + \mathbf{F}_{\text{bar}}(t) + \mathbf{F}_{\text{int}}(t) + \mathbf{F}_{\text{int}}(t) + \mathbf{F}_{\text{int}}(t)$ <br>
ere [M] is the mass matrix, and *u* is the axial displacement<br>
the drill string.<br>
[C] is the stiffness matrix, and *u* is the axial displaceme where  $\alpha$  and  $\beta$  are the scale factors,  $\alpha = 0.1$ ,  $\beta = 0.001$ .<br>According to the meaning of the symbols in the model above, the right-hand side of Eq. (16) represents the forces acting on the whole system, which can be obtained as the following.  $k_i = \frac{E_i A_i}{l_i}$  (17)<br>
nere  $E_i$  is Young's modulus,  $A_i$  is the element cross-<br>
trional area, and  $l_i$  is the element length.<br>
For the damping matrix, in drilling condition, it can be re-<br>
rded as proportional to the mas **Example 10** For the damping matrix, in drilling condition, it can be re-<br>
For the damping matrix, in drilling condition, it can be re-<br>
graded as proportional to the mass matrix, and its calculation<br>
formula is as the f

$$
F_{\text{harl}}(t) = F_0 \sin(\omega_{\text{h}} \cdot t) \tag{19}
$$

where  $F_0$  and  $\omega_{\rm h}$  are the amplitude and frequency of the



Fig. 6. Vibration analysis model of the hydro-oscillator.



Fig. 7. Analysis of the axial harmonic force generated by the hydro-oscillator.

hydro-oscillator transmitting in two directions along the axis, the upward transmission of vibration will be translated into the downward vibration from the disc spring in the upper. The force generated by the tensile disc spring is

$$
F_{\text{bar2}}(t) = -K \cdot u(t) \tag{20}
$$

ment of the hydro-oscillator.

calculated by

$$
\begin{cases}\nF_{\text{bit}}(\dot{u}(t)) = c_1 \exp(-c_2 \dot{u}(t)) - c_1 & \text{for } \dot{u}(t) > 0 \\
F_{\text{bit}}(\dot{u}(t)) = 0 & \text{for } \dot{u}(t) \le 0\n\end{cases}
$$
\ntwo flow holes on the static and dynamo

\nThe axial force of the PDM rotor is

where  $c_1$  and  $c_2$  are the constants of interaction between the bit and rock.

Among the parameters of the vibration model, the friction force between the drill string and borehole well is given by

$$
F_{\text{fric}} = -\mu mg \cdot \text{sgn}(\dot{u}(t)) \tag{22}
$$

where  $\mu$  is the friction coefficient,  $m$  is the BHA gravity quality, *g* is the gravitational constant.

Besides the above forces, there is still a very important force  $F_{\text{h-oscillator}}$  that should be taken into account in detail. As shown in Fig. 7, the analysis is presented about the axial harmonic force generated by the hydro-oscillator. where  $\mu$  is the friction coefficient, *m* is the BHA gravity<br>quality, *g* is the gravitational constant.<br>Besides the above forces, there is still a very important force<br> $F_{\text{h-oscillator}}$  that should be taken into account in

n n+1 n n+1 j(n+1) <sup>2</sup> <sup>2</sup> j(n+1) <sup>n</sup> n+1 <sup>1</sup> 2 1 2 <sup>é</sup> <sup>ù</sup> = - <sup>ê</sup> <sup>ú</sup> ë û (23)

where  $P_n$  is the average pressure in section *n*,  $\rho$  is the drilling fluid density,  $v_n$  is the average flow velocity in section *n*,  $A_n$  is the flow area of section *n*,  $h_{j(n+1)}$  is the lo-

$$
F_{\text{bar}}(t) = P_4 S = P_4 (A_5 - A)
$$
\n(24)

Analysis of the axial harmonic force generated by the hydro-oscillator.<br>
Socillator transmitting in two directions along the axis, where  $\overline{P}_n$  is the average pressure in section  $n$ ,  $\rho$  is the average flux transmiss **F** Analysis of the axial harmonic force generated by the hydro-oscillator.<br> **F** as the axial harmonic force generated by the hydro-oscillator.<br> **For up** to the stress of the variable control of the stress of the control where  $P_4$  is the average pressure in the eccentric hole of the hole on the static valve plate; *A* is the intersecting area of the two flow holes on the static and dynamic valve plates. ere  $\overline{P}_n$  is the average pressure in section  $n$ ,  $\rho$  is the alling fluid density,  $\overline{v}_n$  is the average flow velocity in section  $n$ ,  $A_n$  is the flow area of section  $n$ ,  $h_{n=0}$  is the lohead loss from section

$$
G = G_3 + G_1 - G_2 = \xi G_3 = \xi \Delta p (\pi R^2 + 16ER) \tag{25}
$$

Figure 10 and the distance of the ring of the signal contained the selection of the theorem is the distantial of the parameters of the distantial of the BHA gravity is the distantial force generated by the selection of th  $G = G_3 + G_1 - G_2 = \xi G_3 = \xi \Delta p(\pi R^2)$ <br>
arameters of the vibration model, the friction<br>
arameters of the vibration model, the friction<br>  $G = G_3 + G_1 - G_2 = \xi G_3 = \xi \Delta p(\pi R^2)$ <br>
and intensity only the part of the axial force acting<br> and  $c_2$  are all expansion of metadeon ocerved int<br>  $c_k$  the parameters of the vibration model, the friction<br>  $\mu mg \cdot \text{sgn}(\hat{u}(t))$ <br>  $\mu mg \cdot \text{sgn}(\hat{u}(t))$ <br>
(22) screw (rotor) and fixed liming (state<br>  $\mu mg \cdot \text{sgn}(\hat{u}(t))$ <br> *P*  $F_{\text{int}} = -\mu mg \cdot \text{sgn}(\hat{u}(t))$ <br>
and  $\phi$ , are the constants of interaction between the<br>
and  $\phi$ , are the constants of interaction between the<br>
and  $\phi$ , are the constants of interaction between the<br>  $F_{\text{int}} = -\mu mg \cdot \text{$ and  $c_2$  are the constants of interaction between the<br>  $G = G_1 + G_1 - G_2 = \zeta G_3 = \zeta G_1$ <br>  $Q_1 + G_2 = \zeta G_2$ <br>  $Q_2$  are the vibration model, the friction<br>  $Q_3$  is the axial force as<br>  $\zeta$  is the axial force axis<br>  $\zeta$  is th For  $u_{\text{rad}}(t) = 0$ <br>
Final and C<sub>2</sub> are the constants of interaction between the<br>  $G = G_1 + G_1 - G_2 = \xi G_1 = \xi \Delta p(\pi R^2 +$ <br>
and constants of interaction between the<br>
mong the parameters of the vibration model, the friction<br>
wher where  $G_1$  is the axial force acting on the rotor when the liquid in the high pressure cavity leaks to the low pressure cavity,  $G<sub>2</sub>$  is the part of the axial force caused when the eccentric screw (rotor) and fixed lining (stator) contact with friction, according to their helicoid along the axial movement,  $G_3$  is the part of the axial force caused by pressure drop  $\Delta p$  of the liquid between the high pressure port and the low pressure port,  $\xi$  is the axial force coefficient, taking  $\xi = 1$ , R is the rotor radius. The axial force of the PDM rotor is<br>  $G = G_3 + G_1 - G_2 = \xi G_3 = \xi \Delta p (\pi R^2 + 16ER)$  (25)<br>
where  $G_1$  is the axial force acting on the rotor when the liq-<br>
uid in the high pressure cavity leaks to the low pressure cavity,<br>  $G_2$  nere *G*<sub>1</sub> is the axial force acting on the rotor when the liq-<br>i in the high pressure cavity leaks to the low pressure cavity,<br>i is the part of the axial force caused when the eccentric<br>cevering (rotor) and fixed lining

By the Bernoulli equation, the function of the pressure drop considered; it can be obtained by approximate calculation Besides the two axial forces mentioned above, the axial force caused by the system pressure difference should also be

$$
F_{\!_{\Delta}} = (\bar{P}_{\!1} - \bar{P}_{\!6})A_{\!6} \,. \tag{26}
$$

$$
F_{\text{h-oscillator}} = F_{\text{har}}(t) + G + F_{\text{A}} \tag{27}
$$

Parameter name	Result
Diameter of dynamic valve plate (mm)	55.32
Diameter of hole on rotor valve plate (mm)	27.94
Eccentricity of hole to rotor (mm)	10.084
Diameter of hole on static valve plate (mm)	30.48
Absorber stiffness (kN/mm)	4.5
Volumetric efficiency	0.95
Drilling fluid density $(kg/m3)$	1100
Pressure drop of the motor (MPa)	3.2
Rotor radius (mm)	40.589
Volumetric flow rate of drilling fluid $(L/s)$	22
Inputting pressure of drilling fluid (MPa)	20
Outer diameter of stator (mm)	80.594
Pitch of hydro-oscillator motor (mm)	530

Table 1. The example parameters of hydro-oscillator.

Numerical calculation and analysis

Depending on the analysis model and calculation formulas presented above, the numerical example can be discussed. With inputting parameters according to drilling field situation in a horizontal well, taking the size of the hydro-oscillator as the analysis object, the calculation results mainly include the hydro-oscillator vibration force, displacement, velocity and acceleration.

For the parameters of drilling in a horizontal well, the elastic modulus of the drill string  $E = 210$  GPa, its inside diame-**Fig. 1.4** mm,  $\frac{10,589}{222}$ <br> **Example 12.4 mm,**  $\frac{1}{2}$  **mm,**  $\frac{1}{2}$  **mm, \** Volumetric flow rate of drilling thial (*Ls*)<br>
Inquiring present of drilling thial (Mh)<br>
Outer dismeter of statio (mm)<br>
Outer dismeter of statio (mm)<br>
Pitch of hydro-assillator motor (mm)<br>
Pitch of hydro-assillator motor acceleration <sup>2</sup> *<sup>g</sup>* <sup>=</sup> 9.8 m/s , friction coefficient <sup>m</sup> <sup>=</sup>0.1, *<sup>c</sup>*<sup>1</sup> acceleration  $g = 9.8 \text{ m/s}^2$ , friction coefficient  $\mu = 0.1$ ,  $c_1 = 1400 \text{ N}$ ,  $c_2 = 400$ , PDM frequency  $\omega = 38.13 \text{ rad/s}$ ,  $F_{\text{sta}} =$ Outer diameter of state (mm)<br>
Outer diameter of state (mm)<br>
the of hydro-oscillator motor (mm)<br>
and calculation and analysis<br>
and calculation and analysis<br>
and calculation and analysis<br>  $\frac{F(g. 9, A \sin \theta)F(g. 9, A \sin \theta)F(g. 9, A$ 5500 N,  $F_0 = 550$  N. The hydro-oscillator parameters are shown in Table 1.

Using the established calculation method, inputting the parameters above, the change curve of the drilling fluid flow area between the static and dynamic valve plates is obtained, as shown in Fig. 8. Simultaneously, the change of the axial force is shown in Fig. 9, caused by the hydro-oscillator in a cycle. Compared with Figs. 8 and 9, the change of the flow area is inversely proportionate to the axial force; with the decrease of the flow area, the axial force will increase. When the flow area decreases to the minimum, the axial force can increase to 34 KN, which could improve the efficiency of rock breaking for bits.

Moreover, from the figure shown, the axial force is a continuous and gentle sine-cosine fitting pulse, which can solve the problems of drill-string sticking and dragging, and improve the extension capacity of bits efficiently. On the other hand, the axial force is influenced not only by the continuing movement between the static and dynamic valve plates, but also by the pressure of the drilling fluid, which is the coupling results of the hydro-oscillator and drilling fluid.

Fig. 10 is the excitation spectrum generated by the hydro-



Fig. 8. Flow area between the static and dynamic valve plates.



Fig. 9. Axial force caused by the hydro-oscillator.



Fig. 10. Characteristics of excitation generated by the hydro-oscillator.

oscillator; for the axial harmonic force function could be expanded by the Fourier series. The numbers in the vertical coordinate refer to the amplitudes of different frequency, the fundamental wave amplitude (refers to 1/T) is greater than the other high order waves, all the high order wave amplitudes fluctuate in a small scope, which means that the axial harmonic force generated by the hydro-oscillator changes smoothly and the vibration waveform closes to the fundamental wave. In addition, according to the example parameters and formulas in Sec. 2.2, the hydro-oscillator vibration frequency is 12.14 Hz and its amplitude is small, so the hydro-oscillator vibration is a vibration with high frequency and micro amplitude, which has a remarkable effect on improving wall smoothness and reducing wellbore friction.

Taking the axial force results into vibration analysis model, the vibration characteristics of the hydro-oscillator can be obtained, including the displacement, velocity and acceleration shown in Fig. 11. Moreover, the displacement amplitude is about 3.7 mm, the velocity amplitude is about 0.25 m/s, and the acceleration amplitude is about 20 m/s<sup>2</sup> in three circles, which also proves the micro-amplitude vibration. Besides, the



(c) Acceleration calculation results

Fig. 11. Calculation results of vibration characteristics.



Fig. 12. Analytical response result of acceleration spectrum.

analytical result of acceleration response spectrum is calculated by Fast Fourier transform (FFT), the strong point of acceleration spectrum manly concentrates on 12.52 Hz, which meets the excitation spectrum change rule.

# **3. Experiment test and analysis**

To verify the correctness of the analysis model, corresponding to the numerical example parameters, an experiment test was conducted. The parameters of the hydro-oscillator were consistent with the numerical examples, as shown in Fig. 11. The experimental equipment included the downhole tool, plunger pumps, hydro-oscillator, absorber, test-sensor, throttle valves, inlet and outlet pipes. Each test lasted two minutes.



Fig. 13. Hydro-oscillator bench test.



Fig. 14. Displacement, velocity and acceleration results of experiment test.

According to the experiment test results shown in Fig. 14, the displacement, velocity and acceleration were obtained during 0~3 seconds. When the mud pump flow rate kept 22 L/s, the axial vibration displacement of the hydro-oscillator was about 3~4 mm, the velocity was about 0.2~0.25 m/s, and the acceleration was about  $18{\sim}20$  m/s<sup>2</sup>, which was consistent with the numerical calculation results, as shown in Fig. 11.

Furthermore, the vibration parameters, especially for the velocity and acceleration, fluctuated up and down to a certain extent, which was due to the effects of some uncertainty force, such as the frictional force between the drill string and test bench, or the unstable hydraulic shock force of drilling fluids.

Fig. 15 is the experimental test of the hydro-oscillator axial force, the American BDI (strain measuring device) was used to test the axial force spectrum. Four strain gages were installed to the connecting rods on the test bench. Before the force testing, pre-pressure was applied and the four specimen EA was tested. When the hydro-oscillator was working, the axial force could be transferred to the four rods, so the axial force generated by the hydro-oscillator could be tested through the rod force. From Fig. 15(c) shown, the frequency points are mainly distributed from 10.8 Hz to 12 Hz, which meets the analytical results in Sec. 3.

# **4. Conclusions**

By analyzing the movement of the hydro-oscillator and the results of axial harmonic force, a vibration analysis model of a new drill string system is established, and its vibration characteristics in a horizontal well are analyzed. The following conclusions can be obtained:

(1) Based on the theoretical analysis and test results, the



(a) Bench test of axil force



(b) Specimen strain change with time





(c) Drawing of axial force spectrum

Fig. 15. Experimental test of axial force spectrum.

change of the flow area is inversely proportionate to the axial force; the hydro-oscillator could produce a vibration with high frequency and micro amplitude.

(2) The continuous and gentle vibration effects will turn the static friction between the drill string and wellbore to dynamic friction. Owing to the friction-reduced in the drilling process, it can result in a significant increase in ROP and run length.

(3) By adjusting the corresponding parameters according to the operation conditions, the analysis method and model can also be applied to similar drilling tool or technology research, and provide references to the study of downhole tools dynamics or mechanical properties under new complex drilling conditions.

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#### **Nomenclature-**

- *q* : Flow quantity of per revolution
- *A<sup>s</sup>* : Sectional area of stator
- *A<sup>r</sup>* : Sectional area of rotor
- *N* : Rotor lobes
- *e* : Rotor eccentricity value
- *D*r : External diameter of stator
- *h* : Motor screw pitch
- *R* : Rotor radius
- *ω* : Rotation angular velocity of rotor around its center
- *Q* : Total flow rate
- $\eta$  : Flow efficiency
- *e*m : Eccentricity of the eccentric hole relative to dynamic valve plate central axis
- *A* : Flow area of drilling fluid
- *T* : Time cycle of the flow area
- $r_0$  $r_0$  : Radius of dynamic valve plate<br> $r_1$  : Radius of eccentric hole
- : Radius of eccentric hole

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