# A thermo-physical study of In additive Se–Te chalcogenide glasses

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Abstract. The study discusses the impact of indium on the thermo-physical properties of  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  ( $0 \le x \le 15$ ) glassy alloys. Theoretical predictions of some physical parameters are taken and an effort is made to describe the various trends of the examined physical properties with the addition of indium content. It is observed that the structural parameters, namely coordination number, constraints, heat of atomization and mean bond energy, increase with increasing indium concentration. Experimentally observed and theoretically calculated glass transition temperature  $(T_g)$ , using Gibbs–Di Marzio relation and an empirical equation formulated by Tichy and Ticha, is increased with the addition of indium. The results indicate that the incorporation of In to the Se–Te system increases the rigidity of this system. However, the theoretically predicted  $T_{\rm g}$  (Tichy and Ticha approach) is not consistent with experimental values.

Keywords. Chalcogenide glasses; DSC; thermo-physical study; glass transition temperature.

## 1. Introduction

Chalcogen-based alloys have made manifestations in the last two decades owing to their exciting characteristics that can be meticulously controlled by changing their chemical compositions. Selenium-based semiconducting glasses are of specific interest because of their current utilization as photoconductors in high-definition TV pickup tubes, and mainly in digital X-ray imaging. Recently, Se–Te-based glassy semiconducting alloys have been the focus of scientific and technological applications. Although they are considered capable compositions for phase-change memory materials, they present significant issues when employed as a recording layer in optical phase-change devices [[1,2\]](#page-6-0). Mainly two issues are of concern: lesser reversibility [[3\]](#page-6-0) and lower glass transition as well as crystallization temperatures. The mentioned disadvantages may be overwhelmed by doping another suitable element to the Se–Te system as a chemical modifier. The insertion of a third element, such as indium, creates compositional and configurational disorder in the Se–Te system and gives stability in thus formed glassy alloys [[4,5\]](#page-6-0). The addition of indium to the Se-rich Se–Te system forms a cross-linked structure that increases the glass transition and crystallization temperatures, resulting in a harder Se–Te alloy matrix [[4](#page-6-0),[5\]](#page-6-0).

In this research work, indium is chosen as a doping element to the Se–Te system to realise the impact of the addition of this element on physical properties. The use of indium as a doping element for the Se–Te system is due to its more attractive and important advantages in chalcogenbased glassy alloys [\[6–9](#page-6-0)]. It is found in other research contributions that the addition of indium alters the transport properties  $[10,11]$  $[10,11]$ . The ternary system under study may be a probable entrant for reversible PC optical recording material as adding indium in chalcogen-based binary Se–Te glassy samples will impact minimum eraser time [\[12](#page-6-0)]. The negligible study of physical properties of indium additive Se–Te ternary glasses is reported in the literature and motivates us to study these materials in detail.

The purpose of the research contribution is concerned with examining the compositional dependence of physical properties: average coordination number  $\langle r \rangle$ , average number of constraints f, lone-pair electrons, bond energy, cohesive energy, the heat of atomization, deviation of stoichiometry, mean bond energy, electronegativity and glass transition temperature  $(T_g)$  for  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  ( $0 \le x \le 15$ ) glassy alloys.  $T_{\rm g}$  is important to describe that glass could exist in this phase with operating temperature, and here it is estimated theoretically using the relation given by Tichy et al. [[13\]](#page-6-0) and the modified Gibbs–Di Marzio equation [[14\]](#page-6-0). The estimated theoretical values were compared to experimental results to verify the accuracy of the deduction of  $T_g$ .

## 2. Experimental

Bulk samples of  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  ( $0 \le x \le 15$ ) are synthesized via melt-quench procedure. Each material of high purity (99.999%) is weighed based on atomic percentage and



sealed in quartz ampoules under vacuum ( $\sim$ 2  $\times$  10<sup>-5</sup> mbar). Thereafter, these ampoules are placed in the furnace and the temperature is raised as per the usual procedure. The final maximum temperature of  $900^{\circ}$ C is maintained for 10 h, and the ampoule is also rocked often to maintain the homogeneity of the melt. The melted substance is rapidly cooled by submerging it in ice-cold water.

The synthesized bulk samples are thus ground into a fine powder for further study. X-ray diffraction of the prepared bulk powder samples was carried out at room temperature in the range  $10^{\circ} < 2\theta < 90^{\circ}$ . The X-ray diffraction pattern of the parent sample  $Se_{85}Te_{15}$  is given in another publication [\[15](#page-7-0)]. Figure 1 shows the patterns of the bulk samples  $(x = 2, 6, 10, 15)$  with indium additives that are currently under investigation. The absence of prominent or sharp peaks ensures the amorphous or glassy nature of the synthesized samples. The thermal behaviour of synthesized bulk samples is obtained using a differential scanning calorimetry (DSC) experiment. About 5.0 mg of powdered sample is encapsulated in a typical pan and reheated at heating rates: 5, 10, 15 and  $20^{\circ}$ C min<sup>-1</sup> between 30 and 500°C. Table [1](#page-2-0) lists characteristic temperatures: glass transition temperature  $T_{\rm g}$ , onset temperature of crystallization  $T<sub>o</sub>$ , peak temperature of crystallization  $T<sub>p</sub>$  and melting temperature  $T<sub>m</sub>$  data derived from the DSC curves. The characteristic temperatures shift to higher temperatures with increasing heating rate  $(\alpha)$ . Figure [2a](#page-3-0)–c displays DSC curves of  $Se_{83}Te_{15}In_2$ ,  $Se_{79}Te_{15}In_6$  and  $Se_{75}Te_{15}In_{10}$  at four different heating rates of 5, 10, 15 and  $20^{\circ}$ C min<sup>-1</sup> and the similar DSC curves are also observed for parent sample  $Se_{85}Te_{15}$  $Se_{85}Te_{15}$  $Se_{85}Te_{15}$  and  $Se_{70}Te_{15}In_{15}$  [5[,15](#page-7-0)]. It is found that both endothermic and exothermic temperatures, i.e.  $T_g$  and crystallization temperature  $(T_p)$ , respectively increase with increasing indium content (table [1](#page-2-0)). The peak values of  $T_{g}$ and  $T_p$  are considered in all calculations and conclusions.



Figure 1. X-ray diffraction patterns of In additive chalcogenide  $Se_{85-x}Te_{15}In_x (x = 2, 6, 10 \text{ and } 15 \text{ at. } \%)$  glasses.

#### 3. Results and discussion

## 3.1 Determination of coordination number, constraints and fraction of floppy modes

The average coordination number is vital as it tells about the cross-linking in the glassy structure and may be formulated as the atom-averaged covalent coordination of the constituent elements. The average coordination number  $\langle r \rangle$  in a ternary compound  $\text{Se}_a \text{Te}_b \text{In}_c$  (*a*, *b* and *c* are the atomic percentages) is calculated using the standard procedure  $[16]$  $[16]$ :

$$
\langle r \rangle = \frac{aZ_{\text{Se}} + bZ_{\text{Te}} + cZ_{\text{In}}}{a + b + c},\tag{1}
$$

where  $Z_{\text{Se}}$ ,  $Z_{\text{Te}}$  and  $Z_{\text{In}}$  are coordination number of elements in subscript (table [2\)](#page-3-0). The value of  $\langle r \rangle$  for Se<sub>85–x</sub>Te<sub>15</sub>In<sub>x</sub> system has been evaluated (table [3](#page-4-0)), indicating that it enhances with increasing indium content (figure [3](#page-4-0)). The average coordination number pertaining to covalent bonds is the measure representing the character of atomic units. It is found in the range between 2.00 and 2.15 for the considered system.

In any chalcogenide glass system, covalent coordinating units may be forced to mechanical constraints by interatomic valence forces, viz., bond-stretching and bondbending. The optimum composition of the glass is formed when the constituting network attains the mechanical critical point. The critical point is attained when constraints per atom  $(N_{\text{con}})$  become equivalent to the degrees of freedom per atom.  $N_{\text{con}}$  arises from bond-bending  $(N_{\text{B}} = 2\lt r > -3)$ and bond-stretching  $(N_{\alpha} = \langle r \rangle/2)$  [\[17](#page-7-0)]. Therefore, the average number of constraints  $N_{\text{con}}$  is given as  $(N_{\alpha} + N_{\beta})$ and calculated values for each investigated sample are listed in table [3.](#page-4-0) Thus, it can be seen that  $N_{\rm con}$  increases in this composition; therefore, the coordination number becomes a prominent factor as the degree of cross-linking is enhanced with the increase in  $N_{\text{con}}$ . The variation of  $N_{\text{con}}$  with indium content is described in figure [3.](#page-4-0)

According to Thorpe [\[18\]](#page-7-0), the uncoordinated networks having a finite fraction of zero frequency normal vibration modes are termed as floppy modes in the absence of weak longrange forces. The fraction  $f$  of zero frequency modes is given by:

$$
f = 2 - \frac{5}{6} < r > . \tag{2}
$$

f is calculated for varying composition of In at the cost of Se and is listed in table [3](#page-4-0). It has been observed that with increasing In content in the system, the value of the fraction of floppy modes  $(f)$  decreases (figure [4\)](#page-4-0), indicating that the rigidity of the system increases.

#### 3.2 Lone-pair electrons and ease of glass formation

Chalcogen-based glassy alloys are often called lone-pair semiconductors. The presence of lone-pair electrons in

Composition		Heating rate					
	Characteristic temperature	$5^{\circ}$ C min <sup>-1</sup>	$10^{\circ}$ C min <sup>-1</sup>	$15^{\circ}$ C min <sup>-1</sup>	$20^{\circ}$ C min <sup>-1</sup>		
$Se_{85}Te_{15}$	$T_{\rm g}$	335.23	337.77	339.11	340.08		
	$T_{\rm o}$	357.98	361.71	365.51	365.10		
	$T_{\rm p}$	372.02	375.87	380.99	380.57		
	$T_{\rm m}$	517.30	518.23	519.51	518.89		
$Se_{83}Te_{15}In_2$	$T_{\rm g}$	338.04	341.27	343.57	345.34		
	$T_{\rm o}$	367.32	373.59	376.10	378.70		
	$T_{\rm p}$	388.60	397.90	398.29	405.31		
	$T_{\rm m}$	520.05	521.68	523.38	524.02		
$Se_{79}Te_{15}In_6$	$T_{\rm g}$	339.21	343.39	345.57	347.41		
	$T_{\rm o}$	373.88	383.24	381.18	390.10		
	$T_{\rm p}$	392.63	401.44	403.51	410.35		
	$T_{\rm m}$	522.77	525.38	525.25	526.90		
$Se_{75}Te_{15}In_{10}$	$T_{\rm g}$	341.00	344.52	346.85	348.69		
	$T_{\rm o}$	374.62	379.01	382.18	385.31		
	$T_{\rm p}$	392.66	399.81	403.80	407.27		
	$T_{\rm m}$	526.65	528.20	529.34	530.53		
$Se_{70}Te_{15}In_{15}$	$T_{\rm g}$	344.79	348.95	351.65	353.78		
	$T_{\rm o}$	382.82	386.92	390.51	395.91		
	$T_{\rm p}$	392.38	399.09	405.10	408.37		
	$T_{\rm m}$	537.55	539.98	541.29	543.18		

<span id="page-2-0"></span>**Table 1.** Characteristic temperatures:  $T_g$ ,  $T_o$ ,  $T_p$  and  $T_m$  data derived from the DSC curves.

chemical bonds leads to flexibility, and these types of bonds can be easily distorted compared to the bond without unshared electrons. Thus, larger the lone-pair electrons lesser will be the strain energy in the system, which in turn favours glass formation [\[19](#page-7-0)]. Therefore, lone-pair electrons have vital importance in the formation of chalcogen-based glassy materials. The significance of lone-pair electrons can be understood in the context of valence shell electron pair repulsion theory and adequate number of these electrons leads to the existence of stable state in the system.

Zhenhua [\[20](#page-7-0)] proposed a criterion to determine the tendency of chalcogen-based systems to form a glassy state. This criterion states that a certain number of lone-pair electrons  $(L)$  are required to form a glassy state in the system. According to said criterion, (i)  $L > 4$  for individual elemental system, (ii)  $L > 2.62$  for any binary system and (iii)  $L > 1$  for any ternary system. Many materials that can be solidified in the glassy-like state are found to possess structural 'bridges'. In glassy materials, bridge formation is observed with periodic table elements from groups VI and VII. The presence of bridges of atoms along with lone-pair electrons leads to flexibility [[21\]](#page-7-0). Selenium exists with two lone-pair electrons. The flexibility of chemical bonds pertaining to chalcogens leads the atoms to form amorphous networks instantly. The number of lone-pair electrons for the present chalcogen-based system is estimated using the following equation [[22\]](#page-7-0):

$$
L = V - \langle r \rangle, \tag{3}
$$

where  $V$  is the valence electrons. The value of  $L$  calculated from equation (3) is given in table [3](#page-4-0) and it can be observed that L decreases as indium is incorporated into the parent binary system. The minimum value of lone-pair electrons is 3.25, which directs that the composition considered for study may lead to a good glass-forming system. The plot of L vs. indium at.% is shown in figure [4.](#page-4-0)

#### 3.3 Chemical-bonds and electronegativity

The probable formation of bonds in the present system under analysis are Se–Se, Se–Te, Se–In, etc. CONM [\[23](#page-7-0)] recommends that hetero-polar bonds are favoured compared to homo-polar bonds. Also, these bonds are created in such a way that bonds with lower bond energy are formed later. Hetero-polar bond energy  $(D_{A-B})$  can be estimated via homo-polar bond energy and electronegativity of the constituent elements [[24\]](#page-7-0) using the expression given below:

$$
D_{A-B} = [D_{A-A}.D_{B-B}]^{1/2} + 30(X_A - X_B)^2, \tag{4}
$$

where  $D_{A-A}$  and  $D_{B-B}$  are homo-polar bond energies and  $X_A$ and  $X_{\rm B}$  are the electronegativity values of constituent elements. Both electronegativity values and homo-polar bond energies for Se, Te and In are given in table [2.](#page-3-0) Further, the formation of bonds happens in such a way that bonds with the highest possible energy are expected to occur first, followed by bonds with decreasing energy until all the

<span id="page-3-0"></span>

Figure 2. DSC curves of (a)  $\text{Se}_{83}\text{Te}_{15}\text{In}_2$ , (b)  $\text{Se}_{79}\text{Te}_{15}\text{In}_6$  and (c)  $\text{Se}_{75}\text{Te}_{15}\text{In}_{10}$  at four different heating rates of 5, 10, 15 and  $20^{\circ}$ C min<sup>-1</sup>.

available valence of atoms is satisfied. In the examined composition, In–Se bonds ( $D_{\text{In-Se}} = 227.28 \text{ kJ mol}^{-1}$ ) are expected to occur first for having the highest possible bond energy, lagged by Se–Te bonds ( $D_{\text{Se}-\text{Te}} = 184.92 \text{ kJ mol}^{-1}$ ) to fill all available valence of selenium. Some of the unfilled vacancies may be filled with homo-polar Se–Se defect bonds.

Table 2. Physical parameters of the constituent elements.

Physical parameter	Se.	Te	In
Coordination number			
Electronegativity	2.55	2.1	17
Bond energy (kcal mol <sup>-1</sup> ) Heat of atomization (kcal per g-atom)	44.04 58	33.0 46	24.2 49.4

Cohesive energy (CE) can be deduced knowing these bond energies. The chemical bond approach [[25\]](#page-7-0) can be used to calculate the cohesive energy of the investigated samples by considering the additive nature of bond energies. It is defined as the stabilization energy of an infinitely large cluster of material per atom. Therefore, CE of primed glasses is estimated by taking the sum of bond energy of all the bonds assumed in the system as below:

$$
CE = \sum \frac{C_i D_i}{100},\tag{5}
$$

where  $C_i$  is the expected chemical bond and  $D_i$  is the corresponding bond energy. The evaluated CE and distribution of chemical bonds in each investigated glass are reported in table [4.](#page-5-0) It is observed that CE increases with increasing indium concentration. Values of electronegativity (X) for  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  ( $0 \le x \le 15$ ) glasses are also deduced by Sanderson's method  $[26]$  $[26]$ , according to which it is the geometric mean of electronegativity values of the atoms that constitute the glass. It can be found from table [4](#page-5-0) and figure [4](#page-4-0) that the electronegativity declines with the enhancement in indium concentration.

## 3.4 Average heat of atomization, deviation of stoichiometry and mean bond energy

3.4a Average heat of atomization: The heat of atomization is the amount of heat required to change one mole of an atom in its standard state  $(25^{\circ}C)$  to gaseous atoms. The heat of atomization  $H_s^{AB}$  at normal temperature and pressure of binary semiconductor made of elements A and B is the sum of the heat of atomization  $\Delta H$  and the average of the heats of atomization,  $H_s^A$  and  $H_s^B$ , corresponding to the average non-polar bond energy of the two elements [[27\]](#page-7-0):

$$
H_s^{AB} = \Delta H + \frac{1}{2} \left[ H_s^A + H_s^B \right] \tag{6}
$$

with

$$
\Delta H \propto (X_{\rm A} - X_{\rm B})^2. \tag{7}
$$

Sadagopan and Gatos [\[28](#page-7-0)] extended this to higher-order semiconductor alloys and using this, the average heat of

<span id="page-4-0"></span>**Table 3.** Values of  $\langle r \rangle$ , N<sub>o</sub>, N<sub>6</sub>, N<sub>con</sub>, f, number of lone pair electrons L, H<sub>s</sub>, average single bond energy (H<sub>s</sub>/ $\langle r \rangle$ ), R and mean bond energy ( $\lt E$ ) for Se<sub>85–x</sub>Te<sub>15</sub>In<sub>x</sub> alloys.

Composition	$\langle r \rangle$	$N_{\alpha}$	$N_{\rm R}$	$N_{\rm con}$			$H_{\scriptscriptstyle\rm e}$	$H_s$ / $\lt r$	R	E >
Se <sub>85</sub> Te <sub>15</sub>	2.00	1.00	1.00	2.00	0.333	4.00	48.99	24.45	$\infty$	1.91
$Se_{83}Te_{15}In_2$	2.02	1.01	1.04	2.05	0.300	3.90	49.06	24.05	32.7	1.95
$Se_{79}Te_{15}In_6$	2.06	1.03	1.12	2.15	0.233	3.70	49.41	23.30	10.4	2.04
$Se_{75}Te_{15}In_{10}$	2.10	1.05	.20	2.25	0.167	3.50	49.75	22.61	6.0	2.15
$Se_{70}Te_{15}In_{15}$	2.15	1.08	.30	2.38	0.083	3.25	50.18	21.82	3.8	2.30



**Figure 3.** Variation of  $\lt r > \lt E >$ , CE, N<sub>con</sub> and H<sub>s</sub> with In at.%.



Figure 4. Plot of  $X$ ,  $L$  and  $f$  vs. In at.%.

atomization  $(H_s)$  for a compound  $\text{Se}_a \text{Te}_b \text{In}_c$  may be defined as:

$$
H_s = \frac{aH_s^{Se} + bH_s^{Te} + cH_s^{In}}{a+b+c}
$$
\n<sup>(8)</sup>

 $H_s^{\text{Se}}, H_s^{\text{Te}}$  and  $H_s^{\text{In}}$  of the superscript elements are given in table [2.](#page-3-0) The calculated values for the investigated  $Se_{85-x}$ Te<sub>15</sub>In<sub>x</sub> ( $0 \le x \le 15$ ) glassy alloys are given in table 3 and it can be seen that  $H_s$  increases with the increase in indium concentration. The graphical presentation of  $H<sub>s</sub>$  for different studied compositions is shown in figure 3. Table 3 includes the average single bond energy  $H_s$ /<  $r$  >.

3.4b Deviation of stoichiometry  $R$ :  $R$  is defined as the ratio of the covalent bonding possibilities of chalcogen elements to that of non-chalcogen elements in a system. For any ternary  $\text{Se}_a \text{Te}_b \text{In}_c$  system, R may be deduced using the expression [\[29](#page-7-0),[30\]](#page-7-0):

$$
R = \frac{aZ_{\text{Se}} + bZ_{\text{Te}}}{cZ_{\text{In}}}.\tag{9}
$$

The value of R for  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  is determined and given in table 3. It is said that if R is greater than unity  $(R>1)$ , it indicates chalcogen-rich materials, while  $R \, < 1$  indicates chalcogen-poor materials. Therefore,  $R = 1$  is the critical point where hetero-polar bonds exist. From table 3, it is obvious that  $R > 1$  for all investigated glasses indicates that these examined glasses are rich in chalcogens.

3.4c Mean bond energy: The characteristics of chalcogen additive glassy alloys may be linked with the overall mean bond energy  $\lt E$   $>$  because it relates to average coordination number, bond energy and types of bonds. Using the Tichy *et al.* [\[13](#page-6-0)] expression,  $\lt E$   $>$  for a chalcogen Se-rich  $\text{Se}_a \text{Te}_b \text{In}_c$  system is given by:

$$
\langle E \rangle = E_{\rm cl} + E_{\rm rm}, \tag{10}
$$

where  $E_{cl}$  is due to strong hetero-polar bonds and may be written as:

$$
E_{\rm cl} = P_{\rm r} D_{\rm hb},\tag{11}
$$

where  $P_r$  represents the tendency for cross-linking and can be deduced by:

$$
P_{\rm r} = \frac{bZ_{\rm Te} + cZ_{\rm In}}{a + b + c},\tag{12}
$$

whereas  $D_{\rm hb}$  represents average hetero-polar bond energy and is proposed as:

$$
D_{\rm hb} = \frac{bZ_{\rm Te}D_{\rm Se-Te} + cZ_{\rm In}D_{\rm In-Se}}{bZ_{\rm Te} + cZ_{\rm In}}.\tag{13}
$$

			Distribution of chemical bonds	<b>CE</b>	Excess Se–Se bonds		
Composition	X	Se–Se	Se–Te	In–Se			
$Se_85Te_{15}$	2.48	0.823529	0.176471		1.91	140	
$Se_{83}Te_{15}In_2$	2.47	0.783133	0.180723	0.036145	1.93	130	
$Se79Te15In6$	2.45	0.696203	0.189873	0.113924	1.96	110	
$Se_{75}Te_{15}In_{10}$	2.42	0.600000	0.200000	0.200000	2.00	90	
$Se_{70}Te_{15}In_{15}$	2.39	0.464286	0.214286	0.321429	2.05	65	

<span id="page-5-0"></span>Table 4. Values of electronegativity X, CE (eV per atom), distribution of their respective bonds and excess Se–Se bonds for  $Se_{85-x}Te_{15}In_x$  alloys.

Table 5. Glass transition temperature using the formulations of Tichy and Ticha [[29,30](#page-7-0)]. Modified GDM law [\[14](#page-6-0)] and experimental values at three different heating rates for  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  alloys.

		Heating rate						
	$10^{\circ}$ C min <sup>-1</sup>		$15^{\circ}$ C min <sup>-1</sup>		$20^{\circ}$ C min <sup>-1</sup>			
Composition	Modified GDM law	Exp.	Modified GDM law	Exp.	Modified GDM law	Exp.	Tichy and Ticha	
$Se_{85}Te_{15}$		337.77		339.11		340.08	314.42	
$Se_{83}Te_{15}In_2$	340.08	341.27	341.95	343.57	342.93	345.34	319.44	
$Se_{79}Te_{15}In_6$	341.78	343.39	343.14	345.57	344.12	347.41	330.24	
$Se_{75}Te_{15}In_{10}$	343.58	344.52	344.95	346.85	345.93	348.69	342.19	
$Se_{70}Te_{15}In_{15}$	347.40	348.95	348.78	351.65	349.78	353.78	359.06	

Further, the augmentation arising from the weaker bonds that persist even after all strong bonds are maximized is deduced by the relation:

$$
E_{\rm rm} = \frac{2D_{\rm Se-Se}[0.5()-P_{\rm r}]}{}. \tag{14}
$$

The calculated value of  $\lt E$   $>$  for all compositions of investigated  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  ( $0 \le x \le 15$ ) glassy alloy are listed in table [3.](#page-4-0) It can also be observed that  $\lt E$  > enhances with the enhancement in indium concentration. Figure [3](#page-4-0) shows the enhancement of  $\lt E$  is as the at.% of indium increases.

## 3.5 Glass transition temperature

The temperature associated with the glass transition region (here denoted as  $T_g$ ) is vital for describing the vitreous state. It may be predicted by making use of different theoretical methods.  $T_{\rm g}$  can be calculated using an expression suggested by Tichy and Ticha [[29,30](#page-7-0)]:

$$
T_g = 311[ \langle E \rangle - 0.9]. \tag{15}
$$

The deduced values of  $T_g$  are mentioned in table 5 and enhancement with indium concentration is observed. It can

also be determined by another theoretical approach known as Gibbs–Di Marzio's law. An empirical relation is developed between  $T_g$  and cross-linking density in the system of molecular chains. Sreeram et al [\[14](#page-6-0)] modified Gibbs–Di Marzio equation and suggested the following form:

$$
T_{\rm g} = \frac{T_{\rm o}}{1 - \beta(-2)}.\tag{16}
$$

Here  $T_0$  is taken as  $T_g$  of base glass (binary  $Se_{85}Te_{15}$  alloy) and the denominator of the above expression defines the significance of cross-linking.  $\beta$  is a system-dependent parameter and is evaluated for each ternary alloy by substituting the values of  $T_g$  and  $T_o$  at a known heating rate (5<sup>o</sup>C min<sup>-1</sup>) and the value of  $\lt r >$  in equation (16). The values of  $T_0$  for the non-crosslinked  $Se_{85}Te_{15}$  alloy at the other three heating rates used in the present work are given in table 5.  $T_g$  values for investigated In additive alloys obtained experimentally and estimated theoretically are tabulated in table 5 at the other three heating rates. The good harmony is seen between experimentally observed and theoretically estimated  $T<sub>g</sub>$  for indium additive ternary alloys at the three heating rates. However, applying the Tichy– Ticha approach [\[29](#page-7-0),[30\]](#page-7-0) to  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  system, the estimated  $T_g$  is not consistent with experimentally observed  $T_g$ . However, there is an increasing trend in  $T<sub>g</sub>$  with increasing

<span id="page-6-0"></span>

**Figure 5.** Variation of experimental and theoretical values of  $T_g$  with indium.

indium concentration (table  $5$  and figure  $5$ ). The increasing trends of the theoretical as well as the experimental values (table [5\)](#page-5-0) indicate that the addition of In to binary  $Se_{85}Te_{15}$ alloy by compromising Se increases the rigidity of the system. The inclination of  $T_g$  with the enhancement of indium concentration can be described by considering the composition and configuration modifications due to indium doping. The more general known approach of amorphous selenium considers its two molecular species [\[31](#page-7-0)]: (i) meandering chains comprising helical chains of trigonal selenium and (ii)  $Se_8$  ring molecules of monoclinic selenium. The network of any Se–Te unit synthesized by the melt-quench procedure is taken [[31–34\]](#page-7-0) as the combination of  $Se_8$  rings,  $Se_6Te_2$  rings and  $Se-Te$  copolymer chains. As indium doping occurs by compromising selenium in any binary Se–Te unit, the number of Se–Se long chains likely increases relative to the number of  $Se_8$  rings, resulting in a reduction [\[35](#page-7-0)]. It is recognized that [[36\]](#page-7-0)  $T<sub>g</sub>$  enhances with the increase in chain length and declines with the increase in ring concentration.

## 4. Conclusions

The present study of thermo-physical properties of  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  ( $0 \le x \le 15$ ) glasses shows that the insertion of indium at the cost of Se leads to changes in physical parameters. Results indicate that adding indium in the system  $\text{Se}_{85-x}\text{Te}_{15}\text{In}_x$  leads to an increase in coordination number, the heat of atomization, average bond strength and the number of constraints. But  $L$ ,  $f$  and electronegativity values decrease in the same trend. CE of examined glasses is deduced using CBA and is found to increase with the increase in In at.%.  $T<sub>g</sub>$  is theoretically estimated using Tichy and Ticha methods and a modified Gibbs–Di Marzio's law.

The theoretically predicted and experimental values of  $T<sub>g</sub>$  at different heating rates show an increasing trend with an increase in indium content. However, theoretically deduced  $T_g$  by considering Tichy and Ticha relation is not in harmony with experimentally observed values.

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