# Simultaneous absorption of carbon dioxide, sulfur dioxide and nitrogen dioxide into aqueous 2-amino-2-methy-1-propanol

Kwang-Joong Oh\*, Seong-Soo Kim\*\*, and Sang-Wook Park\*\*\*

\*School of Civil and Environmental Engineering, Pusan National University, Busan 609-735, Korea \*\*Department of Environmental Administration, Catholic University of Pusan, Busan 609-757, Korea \*\*\*School of Chemical and Biomolecular Engineering, Pusan National University, Busan 609-735, Korea (*Received 28 October 2010 • accepted 8 December 2010*)

Abstract–The absorption mechanism of three acidic gases in alkali solution, such as the system of carbon dioxide, sulfur dioxide, and nitrogen dioxide in 2-amino-2-methyl-1-propanol (AMP), was used to predict the simultaneous absorption rates using the film theory. Diffusivity, Henry constant and mass transfer coefficient of each gas were used to obtain the theoretical enhancement factor of each component. The theoretical molar fluxe of each gas was obtained by an approximate solution of mass balances with reaction regions of the first order reaction of  $CO_2$  and instantaneous reactions of  $SO_2$  and  $NO_2$  in  $CO_2$ -SO<sub>2</sub>-NO<sub>2</sub>-AMP system. From the comparison between the theoretical total fluxes of these gases and the measured ones, the solubility and the reaction rate between each gas and AMP influenced its molar flux.

Key words: Simultaneous Absorption, Carbon Dioxide, Sulfur Dioxide, Nitrogen Dioxide, 2-Amino-2-methyl-1-propanol

# INTRODUCTION

Carbon dioxide (CO<sub>2</sub>) and sulfur dioxide (SO<sub>2</sub>), nitrogen dioxide (NO<sub>2</sub>) in the flue gas generated from combustion of fossil fuel are the main cause of global, environmental problems such as air pollution and acid rain. The contents of CO<sub>2</sub>, SO<sub>2</sub>, and NO<sub>2</sub> in the flue gas are typically 15-20%, 0.1-0.4%, and 0.0001% [1], respectively.

Many studies have been done on the mechanisms and kinetics of the reaction of CO<sub>2</sub> with various alkanolamines, employing simple mass balance analysis and resulting in the zwitterion mechanism proposed by Caplow [2] and Danckwerts [3]. Some discrepancies remain according to the reaction mechanism through [4], particularly the types of amines, gas/liquid contactor, and analysis method used for the rate data, the order of the overall reactions and the rate constants. Recently, a group of sterically hindered amines were developed [5], providing a high capacity of 1.0 mol of CO<sub>2</sub>/mol of amine and a relatively high absorption rate, even at high CO<sub>2</sub> loading. One such example was 2-amino-2-methyl-1-propanol (AMP), a sterically hindered form of monoethanolamine.

The absorption of  $SO_2$  [6-8] into aqueous slurries of sodium, calcium and magnesium compounds, serving as the absorbent, and alkaline solutions, has been studied for decades. The medium used in the alkaline solutions was typically alkaline salts [9], inorganic acids [10], organic acids [11], and amines for reversible reaction [12,13]. Danckwerts [14] showed that  $SO_2$  absorption in an alkaline solution was an instantaneous reaction and Hikita et al. [15] proposed a penetration theory model based on the two-reaction model using approximate analytical solutions to investigate the kinetics of  $SO_2$  with reactants in the liquid phase.

Gas mixtures containing NO and SO<sub>2</sub> [16] or NO<sub>2</sub> and SO<sub>2</sub> [17]

emitted from stationary combustion facilities, and H<sub>2</sub>S and SO<sub>2</sub> [18] from natural, coal, and refinery gases, have been separated by simultaneous absorption into aqueous slurries or alkaline solutions. Most of this work has been done towards determining the absorption mechanism and reaction kinetics in the simultaneous absorption of two gases, proposed by Goetter and Pigford [19] and Hikita et al. [20].

Simultaneous absorption of a gaseous mixture into one solvent may become the preferred treatment over that of conventional individual separation using a module with a series in the viewpoint of energy-efficient separation. In this work, a mixture of CO<sub>2</sub>, SO<sub>2</sub>, and NO<sub>2</sub> is simultaneously absorbed into aqueous AMP solution, which is one of a series of studies containing the previous works [21,22]. Absorption kinetics in CO<sub>2</sub>-SO<sub>2</sub>-AMP system [21] and CO<sub>2</sub>-NO<sub>2</sub>-AMP system [22], one gas of which reacts instantaneously, is applied to three gaseous mixtures to predict the simultaneous absorption rates. This study will make a new attempt for removal of the gases emitted from power plant flues for the effective capture and utilization of carbon dioxide.

### THEORY

The zwitterion mechanism originally proposed by Caplow (2) and later reintroduced by Danckwerts (3) and da Silva and Svendsen (4) is generally accepted as the reaction mechanism in the absorption of  $CO_2$  into aqueous AMP (RNH<sub>2</sub>) as follows:

 $CO_2 + RNH_2 = RN^+H_2COO^-$  (i)

$$RN^{+}H_{2}COO^{-}+H_{2}O \rightarrow RNH_{3}^{+}+HCO_{3}^{-}$$
 (ii)

With overall reaction being:

$$CO_2 + RNH_2 + H_2O \rightarrow RNH_3^+ + HCO_3^-$$
 (iii)

Reactions of SO<sub>2</sub> in aqueous AMP, combined with the SO<sub>2</sub> reac-

<sup>&</sup>lt;sup>†</sup>To whom correspondence should be addressed.

E-mail: swpark@pusan.ac.kr

tion in an aqueous, alkaline solution [23], are as follows:

$$SO_2 + H_2O = 2H^+ + SO_3^{2-}$$
 (iv)

$$RNH_2+H^+ \rightarrow RNH_3^+$$
 (v)

Overall reaction being:

$$SO_2+2RNH_2+H_2O \rightarrow 2RNH_3^++SO_3^{2-}$$
 (vi)

Reactions of  $NO_2$  in aqueous alkaline solutions of AMP are as follows [24-28]:

$$2NO_2+H_2O \rightarrow HNO_2+HNO_3$$
 (vii)

$$HNO_2 + HNO_3 + 2RNH_2 \rightarrow 2RNH_3^+ + NO_2^- + NO_3^-$$
(viii)

Overall reaction being:

$$2NO_2 + 2RNH_2 + H_2O \rightarrow 2RNH_3^+ + NO_2^- + NO_3^-$$
(ix)

The irreversible reactions between the dissolved species j and the reactant (C), as shown in reactions (iii), (vi), and (ix) may be formulated as follows:

$$j + \nu C \rightarrow \text{products}$$
 (x)

where j presents CO<sub>2</sub>, SO<sub>2</sub>, and NO<sub>2</sub>, and are simplified as A<sub>1</sub>, A<sub>2</sub>, and A<sub>3</sub>, respectively. C is AMP and  $v_j$  a stoichiometric coefficient of species j.

The following assumptions are made to set up the mass balance of species j:

1) Henry's law holds, 2) the isothermal condition prevails, 3) species C is a nonvolatile solute, and 4) reaction (xii) is  $m^{th}$  order with respect to j and  $n^{th}$  order with respect to C, of which the reaction rate ( $r_i$ ) of species j is expressed by:

$$\mathbf{r}_{j} = \mathbf{k}_{j} \mathbf{C}_{j}^{m} \mathbf{C}_{c}^{n} \tag{xi}$$

For simultaneous absorption of the gases,  $A_1$ ,  $A_2$ , and  $A_3$  into reactive C solution, the following assumptions are made to set up the mass balance of species j and C: 1) The presence of one gas does not affect the rate of absorption of the other gas because the gases do not compete for the common liquid-phase reactant C, and 2) the reaction orders with respect to species, j, and C are 1 and 1, respectively. The mass balances of species j and C using the film theory accompanied by the chemical reaction and the boundary conditions are given as follows:

$$D_j \frac{d^2 C_j}{dz^2} = k_j C_j C_c \tag{1}$$

$$D_{C} \frac{d^{2}C_{C}}{dz^{2}} = \sum_{j=A_{1}}^{A_{3}} \nu_{j} k_{j} C_{j} C_{C}$$
(2)

$$z=0; C_j=C_{jj}; \frac{dC_c}{dz}=0$$
 (3)

$$z = \delta; C_i = 0, C_c = C_{c_0}$$

$$\tag{4}$$

The flux of species j at the interface of the gas-liquid phase is defined by

$$N_{j} = -D_{j} \left(\frac{dC_{j}}{dz}\right)_{z=0}$$
(5)

The enhancement factor ( $\beta$ ) here is defined as the ratio of molar

flux of Eq. (5) with the chemical reaction to that obtained without the chemical reaction:

$$\beta_j = -\frac{N_j}{k_{Lj}C_{ji}}\Big|_{Z=0} \tag{6}$$

The simultaneous solution of the differential equations of Eq. (1) and (2) is used to obtain the value of  $b_i$  through Eq. (6).

The individual and total absorption rate of  $CO_2$ ,  $SO_2$ , and  $NO_2$  are obtained as follows, respectively:

$$N_{j} = \beta_{j} k_{Lj} C_{ji}$$
(7-1)

$$N_{S} = \sum_{j=A1}^{A3} \beta_{j} k_{Lj} C_{ji}$$
(7-2)

In the simultaneous absorption of  $CO_2$  and  $SO_2$  into AMP solution, the reaction between  $CO_2$  and AMP of Eq. (iii) is a first order reaction with respect to both  $CO_2$  and AMP, respectively [21], and the reaction [14,21] between  $SO_2$  and AMP of Eq. (vi) and that [22, 26] between  $NO_2$  and AMP of Eq. (ix) are an instantaneous hydration reaction, respectively. In the simultaneous absorption of  $CO_2$ ,  $SO_2$ , and  $NO_2$  into AMP solution,  $CO_2$  assumed to be a second-order reaction, and  $SO_2$  and  $NO_2$ , an instantaneous reaction for AMP, respectively. The enhancement factor of  $SO_2$  and  $NO_2$  in AMP solution is derived as follows [29]:

$$\beta_{A2} = 1 + \frac{C_{Co}}{C_{A2i}} \frac{D_C}{V_{A2}} \cong \frac{C_{Co}}{C_{A2i}} \frac{D_C}{V_{A2}}$$
(8)

$$\beta_{A3} = 1 + \frac{C_{Co}}{C_{A3i}} \frac{D_C}{V_{A3}} \cong \frac{C_{Co}}{C_{A3i}} \frac{D_C}{V_{A3}}$$
(9)

Comparing the size of the instantaneous reaction rates of Eq. (8) and (9), the enhancement factor of NO<sub>2</sub> is given as follows:

$$\beta_{A3} = \beta_{A2} \frac{C_{A2i} v_{A2} D_{A2}}{C_{A3i} v_{A3} D_{A3}}$$
(10)

Hikita et al. [20] have presented an approximate analytical solution with the enhancement factors ( $\beta_{41}$  and  $\beta_{42}$ ) of species A<sub>1</sub> and A<sub>2</sub> absorbing two gases, one (A<sub>2</sub>) of which reacts instantaneously in the liquid phase, such as the system of CO<sub>2</sub>-SO<sub>2</sub>-AMP, as follows:

$$\beta_{A1} = \frac{\left[ (1 + r_B q_B + r_C q_C) - (1 + r_B q_B) \beta_{A1} \right] \gamma \eta}{(1 + r_C q_C - \beta_A) \tanh(\gamma \eta)}$$
(11)

where, 
$$\eta = \frac{1 + r_c q_c - \beta_{A_1}}{1 + r_B q_B + r_c q_c - \beta_{A_1}} \sqrt{\frac{1 + r_B q_B + r_c q_c - (1 + r_B q_B) \beta_{A_1}}{3 r_c q_c \beta_{A_1}}}$$
  
 $\beta_{A_2} = \frac{1 + r_B q_B + r_c q_c - \beta_{A_1}}{r_B q_B}$ 
(12)

where, 
$$\mathbf{r}_{B} = \frac{\mathbf{D}_{A2}}{\mathbf{D}_{A1}}, \mathbf{r}_{C} = \frac{\mathbf{D}_{C}}{\mathbf{D}_{A1}}, \mathbf{q}_{B} = \frac{\mathbf{v}_{A2}\mathbf{C}_{A2i}}{\mathbf{v}_{A1}\mathbf{C}_{A1i}}, \mathbf{q}_{C} = \frac{\mathbf{C}_{Co}}{\mathbf{v}_{A1}\mathbf{C}_{A1i}},$$
  
$$\gamma = \frac{\sqrt{\mathbf{k}_{A1}\mathbf{C}_{Co}\mathbf{D}_{A1}}}{\mathbf{k}_{LA1}}.$$

 $\beta_{A1}$  and  $\beta_{A2}$  are calculated from Eqs. (11) and (12) by a trial and error procedure with given dimensionless parameters, such as  $r_B$ ,  $r_C$ ,  $q_B$ ,  $q_C$ , and  $\gamma$ ,  $\beta_{A3}$  in the system of CO<sub>2</sub>-SO<sub>2</sub>-NO<sub>2</sub>-AMP is obtained from Eq. (10).

## **EXPERIMENTAL**

# 1. Chemicals

All chemicals were of regent grade and used without further purification. Purity of N<sub>2</sub>, CO<sub>2</sub>, and SO<sub>2</sub> was more than 99.9%. A stock gaseous mixture (Rigas Standard Gas Co.) containing N2 was used as a source of NO<sub>2</sub> with a 0.1%.

#### 2. Simultaneous Absorption of CO<sub>2</sub>, SO<sub>2</sub>, and NO<sub>2</sub>

Absorption experiments were carried out in an agitated vessel [30,31]. The absorption vessel was constructed of glass with an inside diameter of 0.073 m and a height of 0.151 m. Four equally-spaced vertical baffles, each one-tenth of the vessel diameter in width, were attached to the internal wall of the vessel. The gas and liquid phase were agitated with an agitator driven by a 1/4 Hp variable speed motor. A straight impeller 0.034 m in length and 0.05 m in width was used as the liquid phase agitator and located at the middle position of the liquid phase. The surface area was calculated as a ratio of the volume of added water to the measured height of water in the absorber, and its value was 40.947 cm<sup>2</sup>. The gas and liquid in the vessel were agitated at 50 rpm. The value of the cumulative volume of the soup bubble was measured by a soup bubbler for the change of absorption time to obtain the absorption rate of CO<sub>2</sub>, SO<sub>2</sub>, and NO2. Each experiment was duplicated at least once under identical conditions. It was assumed that the volumetric rising rate of the soup bubble in the soup bubbler attached to the absorption vessel was equal to the value of the absorption rate of gases. The gaseous compositions of CO<sub>2</sub>, SO<sub>2</sub> and NO<sub>2</sub> at the inlet of the absorber were measured using a gas chromatography (column A for CO<sub>2</sub> and SO<sub>2</sub>: PTFE, 6 feet x 1/8 inch OD, Chromosorb 107, 80/100; column B for NO2: SS, 30 ft x 1/8 in OD, Gas Chrom MP-1, 100/120; Detector: TCD at 100 °C; He: 18 cm<sup>3</sup>/min; retention time of CO<sub>2</sub>: 6.13 min, NO<sub>2</sub>: 7.73 min, SO<sub>2</sub>, 9.56 min). The absorption experiments were carried out in a range of 0-2.0 kmol/m3 of AMP, 5-30% mole fraction of CO<sub>2</sub>, 0.5-4% of SO<sub>2</sub>, and a fixed NO<sub>2</sub> of 0.1% at 298-323 K and 101.3 kPa to measure the simultaneous total molar flux of 3 gaseous mixture of CO<sub>2</sub>, SO<sub>2</sub> and NO<sub>2</sub> in AMP solution.

A sketch of the experimental set up is presented in Fig. 1. A typical experimental run was performed as follows:





A, B, C. Valve

G. Funnel

H. Soap film meter

June, 2011

The vent valve A is initially closed and the purge value B is open. Gas flows continuously through absorber D to make sure that the latter is filled with gas at the start of the experiment. During this initial period, the water bath temperature is brought up to the desired value, and the liquid batch is kept in bottle F inside the water bath. At the start of the experiment, the liquid batch is poured into funnel G and the agitator E in D is started. Liquid feed valve C is closed, purge value B is closed, and vent valve A is opened, as simultaneously as possible. Measurements are started at soap film meter H taking care that there are always two soap films in the meter so that a continuous reading of the cumulative volume of gas that has flowed through the soap film meter (V) can be recorded as a function of time. The gas absorption rate was obtained as a slope of the plots of V vs. time at an initial time. The mass transfer coefficient  $(k_{iw})$  was calculated by the following equation with the initial volumetric absorption rates of CO<sub>2</sub>, and V/t<sub>1</sub>, obtained from the cumulative volume of gas which flowed through the soap film meter.

$$\mathbf{k}_{Ljw} = \frac{\mathbf{P}_T - \mathbf{P}_W^o \mathbf{V}}{\mathbf{S}\mathbf{C}_{il} \mathbf{R} \mathbf{T} \mathbf{t}_1}$$
(13)

where  $P_T$  is the atmospheric pressure,  $P_W^o$  the vapor pressure of water, S the surface area of liquid phase, C<sub>ii</sub> the solubility of j gas in water, and  $V(t_1)$  the cumulative volume of gas during the absorption time,  $t_1$ . **3. Physicochemical Properties** 

Both the solubility and diffusivity of the solute gases in the liquid medium, which affect the derived reaction rate parameters, as seen in Eq. (1), (2), (11), and (12), are obtained using an approximate method of the nitrous oxide analogy as follows:

The Henry constants of N<sub>2</sub>O and CO<sub>2</sub> in water are obtained from the following empirical equations [32]:

$$H_{N20}^{o} = 8.547 \times 10^{6} \exp\left(-\frac{2284}{T}\right)$$
(14)

$$H_{A1}^{o} = 2.8249 \times 10^{6} \exp\left(-\frac{2044}{T}\right)$$
 (15)

The Henry constant of N<sub>2</sub>O in aqueous AMP solution was estimated accordingly [33]:

$$H_{N2O} = (5.52 + 0.7C_{Co}) \times 10^{6} \exp\left(-\frac{2166}{T}\right)$$
(16)

The Henry constant of  $SO_2$  in water was estimated by the empirical formula [34]:

$$H_{A2}^{o} = 101.3/\exp\left(\frac{510}{T_{o}} - 26970T_{1} + 155T_{2} - 0.0175T_{o}T_{3}/R\right)$$
(17)

where,  $T_a=298.15$ ,  $T_1=1/T_a-1/T$ .  $T_3=T_a/T-1+\ln(T/T_a)$ ,  $T_3=T/T_a-1/T_a$  $T_{T}/T - 2\ln(T/T_{o})$ 

The Henry constants of CO<sub>2</sub> and SO<sub>2</sub> in aqueous AMP solution were estimated by the N<sub>2</sub>O analogy as follows:

$$H_{j} = H_{j}^{o} \frac{H_{N2O}}{H_{N2O}^{o}}$$
(18)

The Henry constant  $(H_{43})$  of NO<sub>2</sub> in water was estimated by interand extrapolation using 1.044 atm·m3/kmol at 25 °C and 2.844 atm· m<sup>3</sup>/kmol at 40 °C [26].

The solubility  $(C_{ii})$  of species, j, at a partial pressure was esti-

mated as follows:

$$\mathbf{P}_{j} = \mathbf{H}_{j} \mathbf{C}_{ji} \tag{20}$$

The diffusivities of  $N_2O$  and  $CO_2$  in water were obtained from the following empirical equations [32]:

$$D_{N20}^{o} = 5.07 \times 10^{-6} \exp\left(-\frac{2371}{T}\right)$$
(21)

$$D_{A1}^{o} = 2.35 \times 10^{-6} \exp\left(-\frac{2119}{T}\right)$$
 (22)

Saha et al. [33] have reported that experimental diffusivity data of  $N_2O$  in aqueous AMP solution did not follow the Stokes-Einstein relation (D $\mu/T$ =constant) along with an empirical formula as follows:

$$\frac{D_{N20}\mu^{0.82}}{T} = 2.12 \times 10^{-14}$$
(23)

The diffusivity of  $SO_2$  in water was estimated by the empirical formula [34]:

$$D_{A2}^{o} = 5.08982 \times 10^{-12} \operatorname{Texp} \left( 5.15581 - \frac{1243.06}{T - 53.19} \right)$$
(24)

The diffusivities of  $CO_2$  and  $SO_2$  in aqueous AMP solution were estimated using the  $N_2O$  analogy:

$$D_{j} = D_{j}^{o} \frac{D_{N2O}}{N_{N2O}^{o}}$$
(25)

The diffusivity  $(D_{A3}^{\circ})$  of NO<sub>2</sub> in water at 25 °C was taken as  $1.40 \times 10^{-9}$  m<sup>2</sup>/s [35]. Diffusivity  $(D_{A3})$  of NO<sub>2</sub> in aqueous AMP solution was estimated from the following equation corrected [36] with viscosity of the aqueous AMP solution:

$$D_{A3} = D_{A3}^{o} \left(\frac{\mu_{W}}{\mu}\right)^{2/3}$$
(26)

The diffusivity  $(D_c)$  of AMP in AMP solution was estimated by the method of Wilke [14].

Viscosity of the aqueous AMP solution was measured with a Brookfield viscometer (Brookfield Eng. Lab. Inc, USA).

The mass transfer coefficients  $(k_{ij})$  of species, j, CO<sub>2</sub>, SO<sub>2</sub>, and NO<sub>2</sub> in AMP solution were calculated from relationship between the mass transfer coefficient in water and diffusivity ratio in reference as following [37]:

$$k_{Lj} = k_{Ljw} (D/D_{jw})^{23}$$
 (27)

The liquid-side mass transfer coefficient  $(k_{Ljw})$  of species, j, in water was measured by using the absorption rates of pure CO<sub>2</sub>, SO<sub>2</sub> and NO<sub>2</sub> at various temperatures and 50 rpm, respectively.

The reaction rate constant  $(k_{A1})$  between CO<sub>2</sub> and AMP was obtained from the following equation [21].

$$k_{A1} = 1.2 \times 10^{10} \operatorname{Exp} (-5096.4/T)$$
 (28)

# **RESULTS AND DISCUSSION**

To observe the effect of the variables such as physicochemical properties ( $k_{A1}$ ,  $C_{ji}$ ,  $D_j$ , and  $k_{Lj}$ ) based on the experimental conditions ( $y_j$ ,  $C_{Co}$  and T) on the enhancement factor ( $\beta$ ), the ratio of the amount of



Fig. 2. Effect of g on  $\beta_{A1}$  and  $\beta_{A2}$  with parameters of  $r_B q_B$  and  $r_C q_C$ .

a gas reacting in the film to that reaction in the bulk (Hatta number,  $\gamma$ ) is generally used as a variable for  $\beta$ [29].

Because SO<sub>2</sub> and NO<sub>2</sub> are instantaneous reactions with AMP, respectively, the dimensional analysis about  $\beta_{A2}$  is considered in the system of CO<sub>2</sub>-SO<sub>2</sub>-AMP, and then,  $\beta_{A3}$  in the system of CO<sub>2</sub>-SO<sub>2</sub>-NO<sub>2</sub>-AMP, using Eq. (10).

 $\beta_{A1}$  and  $\beta_{A2}$  are estimated by using Eqs. (11) and (12) at a given value of  $\gamma$  with the parameters of  $r_Bq_B$  and  $r_Cq_C$  and plotted in Fig. 2.

As shown in Fig. 2,  $\beta_{A1}$  increases and  $\beta_{A2}$  decreases with increasing  $\gamma$  at a given  $r_Bq_B$  and  $r_Cq_C$ .  $\beta_{A1}$  increases with increasing  $k_{A1}$ ,  $C_{Co}$ , or decreasing  $k_L$ . Because  $\beta_{A1}$  and  $\beta_{A2}$  inversely change each other at given  $r_Bq_B$  and  $r_Cq_C$  in Eq. (12),  $\beta_{A2}$  decreased with increasing  $\beta_{A1}$ . At a given  $r_Cq_C$  of 20 and  $\gamma$ ,  $\beta_{A1}$  and  $\beta_{A2}$  decrease with increasing  $r_Bq_B$  from 1 to 2. Decrease of  $\beta_{A1}$  means that  $\beta_{A1}$  is smaller when more SO<sub>2</sub> is present, because more AMP is then available for reaction with SO<sub>2</sub> due to the instantaneous reaction of SO<sub>2</sub> with AMP.  $\beta_{A2}$  should increase with decreasing  $\beta_{A1}$ . This result may be because the value of  $r_Bq_B$  increases on a large scale than increase of  $\beta_{A1}$  in Eq. (12).

At a given  $r_{\beta}q_{\beta}$  of 2 and  $\gamma$ ,  $\beta_{A1}$  and  $\beta_{A2}$  increase with increasing  $r_{c}q_{C}$  from 20 to 40.  $\beta_{A2}$  should decrease with increasing  $\beta_{A1}$ . This result may be due to the fact that the value of  $r_{c}q_{C}$  increases on a larger scale than increase of  $\beta_{A1}$  in Eq. (12).  $\beta_{A3}$  has a similar behavior to  $\beta_{A2}$  from the relationship between  $\beta_{A2}$  and  $\beta_{A3}$  in Eq. (10).

Simultaneous molar fluxes ( $N_{S,exp}$ ) of three gaseous mixtures were measured within a range of 0-2.0 kmol/m<sup>3</sup> of AMP, 5-30% of CO<sub>2</sub>, 0.5-4% of SO<sub>2</sub>, and 298-323 K at a fixed NO<sub>2</sub> of 0.1% and 101.3 kPa.

To observe the effect of  $y_{A1}$  on  $N_5$ ,  $\beta_{A1}$  and  $\beta_{A2}$  were estimated using Eq. (11) and (12), and  $\beta_{A3}$  by Eq. (10) at a given value of the physiochemical properties based on the typical experimental conditions of  $C_{co}=2 \text{ kmol/m}^3$ ,  $y_{A2}=1\%$ ,  $y_{A3}=0.1\%$ , and T=313.15 K. The obtained  $\beta_i$  was plotted vs.  $y_{A1}$  in Fig. 3.

As shown in Fig. 3,  $\beta_j$  decreases with increasing  $y_{A1}$ . Because  $r_B q_B$ 



Fig. 3.  $\beta_j$  vs.  $y_{A1}$  at  $C_{C_0}$ =2.0 kmol/m<sup>3</sup>,  $y_{A2}$ =1%,  $y_{A3}$ =0.1%, and T=313.15 K.



Fig. 4. N<sub>j</sub> vs.  $y_{A1}$  at C<sub>co</sub>=2.0 kmol/m<sup>3</sup>,  $y_{A2}$ =1%,  $y_{A3}$ =0.1%, and T= 313.15 K.

and  $r_c q_c$  decrease simultaneously with increasing  $C_{Ali}$  by increase of  $y_{Al}$ , as shown in Fig. 2,  $\beta_{Al}$  decreases with increasing  $y_{Al}$ . Decrease of  $\beta_{A2}$  may be due to the fact that  $r_B q_B$  and  $r_c q_c$  increase on a larger scale than decrease of  $\beta_{A1}$  in Eq. (12).

 $N_{S,eep}$  were plotted vs.  $y_{A1}$  as a symbol of circles in Fig. 4.  $N_{j,cal}$  were calculated by Eq. (7) using  $C_{ji}$ ,  $k_{Lj}$ , and  $\beta_j$  in Fig. 3 to present in Fig. 4 as solid lines.

As shown in Fig. 4,  $N_{A1}$  increases and  $N_{A2}$  and  $N_{A3}$  decrease with increasing  $y_{A1}$ . Increase of  $N_{A1}$  is due to increasing the solubility of CO<sub>2</sub>. Decrease of  $N_{A2}$  is due to decrease of AMP, which can react



Fig. 5. N<sub>j</sub> vs.  $y_{A2}$  at C<sub>Co</sub>=2.0 kmol/m<sup>3</sup>,  $y_{A1}$ =15%,  $y_{A2}$ =1%,  $y_{A3}$ =0.1%, and T=313.15 K.



Fig. 6. N<sub>j</sub> vs. C<sub>co</sub> at y<sub>A2</sub>=30%, y<sub>A2</sub>=1%, y<sub>A3</sub>=0.1%, and T=313.15 K.

with SO<sub>2</sub>.

 $N_{S,exp}$  were plotted vs.  $y_{A2}$  as a symbol of circles in Fig. 5 under the typical conditions of  $C_{co}=2.0 \text{ kmol/m}^3$ ,  $y_{A1}=15\%$ ,  $y_{A3}=0.1\%$ , and T=313.15 K.  $N_{i,cal}$  were presented in Fig. 5 as solid lines.

As shown in Fig. 5,  $N_{A1}$  decreases, and  $N_{A2}$  and  $N_{A3}$  increase with increasing  $y_{A2}$ . Increase of  $N_{A2}$  is due to increase of solubility of SO<sub>2</sub> and that the reaction rate of SO<sub>2</sub> is faster than that of CO<sub>2</sub>.

From the results of Figs. 3, 4, and 5, the molar flux of each species is mainly dependent on its solubility, as shown in Eq. (10)-(12).

To observe the effect of  $C_{co}$  on  $N_s$ ,  $N_{s,exp}$  were plotted vs.  $C_{co}$  as a symbol of circles in Fig. 6 under the typical conditions of  $y_{A1}$ =



Fig. 7. N<sub>j</sub> vs. temperature at  $C_{co}$ =2.0 kmol/m<sup>3</sup>,  $y_{A2}$ =15%,  $y_{A2}$ =1%,  $y_{A3}$ =0.1%.

30%,  $y_{A2}=1\%$ ,  $y_{A3}=0.1\%$ , and T=313.15 K.

As shown in Fig. 6,  $N_j$  increase with increasing  $C_{Co}$ . Increase of  $N_j$  is due to increasing the reactant of AMP.

To observe the effect of temperature on N<sub>s</sub>, N<sub>s, exp</sub> were plotted vs. temperature as a symbol of circles in Fig. 7 under the typical conditions of  $y_{41}$ =15%,  $y_{42}$ =4%,  $y_{43}$ =0.1%, and C<sub>co</sub>=2.0 kmol/m<sup>3</sup>.

As shown in Fig. 7,  $N_{A1}$  increases, while  $N_{A2}$  and  $N_{A3}$  decrease with increasing T. As shown in Eq. (7-1),  $N_j$  is affected by  $\beta_j$ ,  $k_{Lj}$  and  $C_{ji}$ . The values of  $k_{Lj}$  are almost constant in Table 1, but  $\beta_j$  and



Fig. 8. Comparison of the calculated and measured molar flux of mixed gases.

 $C_{ji}$  increase and decrease with increasing temperature, respectively. From these results, the molar flux of each component for the change of temperature may be given according to the relative size of its solubility and the enhancement factor.

 $N_{S,cal}$  were plotted vs.  $N_{S,exp}$  in Fig. 8 under all experimental conditions of 60 mentioned above.

As shown in Fig. 8, the observed values of the molar flux agree with the calculated values (correlation coefficient=0.9978, mean deviation=2.40% and standard deviation=0.11%).

### CONCLUSIONS

Simultaneous absorption rate of CO<sub>2</sub>, SO<sub>2</sub>, and NO<sub>2</sub> was measured into aqueous AMP in a stirred, semi-batch tank with a planar, gas-liquid interface under the experimental conditions such as  $C_{Co}$ = 0-2.0 kmol/m<sup>3</sup>, y<sub>A1</sub>=5-30%, y<sub>A2</sub>=0.5-4%, and T=298-323 K at a fixed y<sub>A3</sub>=0.1% and 101.3 kPa. Physicochemical properties were obtained from the reference data measured by N<sub>2</sub>O analogy.

The reaction mechanism in the  $CO_2$ - $SO_2$ - $NO_2$ -AMP system was assumed to be a first order reaction with respect to both  $CO_2$  and AMP, respectively, and an instantaneous reaction with respect to both  $SO_2$  and  $NO_2$ . An approximate solution of the mass balances accompanied by this reaction mechanism could predict the simultaneous absorption rate of these mixed gases. The molar flux of each component was affected according to the relative size of its solubility and the enhancement factor.

#### ACKNOWLEDGEMENTS

This work was financially supported by Korea Ministry of Environment (MOE) as Human resource development Project for Waste to Energy and the Energy Efficiency & Resources of the Korea Institute of Energy Technology Evaluation and Planning (KETEP) grant by the Korea government Ministry of Knowledge Economy (No. 20092010200011-12-1-000).

#### NOMENCLATURE

- $C_i$  : concentration of species, j [kmol/m<sup>3</sup>]
- $C_{ji}$  : solubility of species, j [kmol/m<sup>3</sup>]
- $D_i$  : diffusivity of species, j [m<sup>2</sup>/s]
- H<sub>i</sub> : Henry constant of species, j [atm $\cdot$ m<sup>3</sup>/kmol]
  - : reaction rate constant of species,  $j [m^3/kmol \cdot s]$
- $k_{Li}$  : liquid-side mass transfer coefficient of species, j [m/s]
- MD : mean deviation

k,

- $N_i$  : molar flux of species, j [kg mol/m<sup>2</sup>·s]
- $N_s$  : total molar flux [kmol/m<sup>2</sup>·s]
- r<sup>2</sup> : correlation coefficient
- SD : standard deviation
- T : temperature [°K]
- z : diffusion coordinate of gas [m]
- $z_L$  : film thickness [m]

### **Greek Letters**

- $\beta_i$  : enhancement factor of species, j
- *m* : viscosity of liquid  $[N \cdot s/m^2]$
- $v_i$ : a stoichiometric coefficients of species, j

# Subscripts

$A_1$	:	$CO_2$
1		4

- $A_2$  : SO<sub>2</sub>
- $A_3$  : NO<sub>2</sub>
- C : AMP
- j : species
- o : feed
- w : water

# REFERENCES

- G Astarita, D. W. Savage and A. Bisio, *Gas treating with chemical solvents*, John Wiley & Sons, New York (1983).
- 2. M. Caplow, J. Am. Chem. Soc., 90, 6795 (1968).
- 3. P. V. Danckwerts, Chem. Eng. Sci., 34, 443 (1979).
- 4. E. F. da Silva and H. F. Sendsen, *Ind. Eng. Chem. Res.*, **43**, 3413 (2004).
- T. Mimura, T. Suda, A. Honda and H. Kumazawa, *Chem. Eng. Commun.*, **170**, 245 (1998).
- 6. C. Brogren and H. T. Karlsson, Chem. Eng. Sci., 52, 3085 (1997).
- 7. J. Stein, M. Kind and E. Schlunder, Chem. Eng. J., 86, 17 (2002).
- S. H. Jung, G. T. Jeong, G. Y. Lee, J. M. Cha and D. H. Park, *Korean J. Chem. Eng.*, 24, 1064 (2007).
- S. Ebrahimi, C. Picioreanu, R. Kleerebezem, J. J. Heijnen and M. C. M. van Loosdrecht, *Chem. Eng. Sci.*, 58, 3589 (2003).
- S. Colle, J. Vanerschuren and D. Thomas, *Chem. Eng. Process*, **43**, 1397 (2004).
- 11. J. Xia, B. Rumpf and G. Maurer, *Ind. Eng. Chem. Res.*, **38**, 1149 (1999).
- 12. M. H. H. an Dam, A. S. Lamine, D. Roizard, P. Lochon and P. Roizard, *Ind. Eng. Chem. Res.*, **36**, 4628 (1997).
- D. Nagel, R. de Kermadec, H. G. Lintz, C. Roizard and F. Lapicque, *Chem. Eng. Sci.*, **57**, 4883 (2002).
- P. V. Danckwerts, *Gas-Liquid Reactions*, McGraw-Hill, New York (1970).
- 15. H. Hikita, S. Asai and T. Takatsuka, Chem. Eng. J., 4, 31 (1972).

- 16. M. P. Ho and G. E. Klinzing, Can. J. Chem. Eng., 64, 243 (1986).
- E. Sada, H. Kumazawa and Y. Yoshikawa, J. Am. Chem. Soc., 34, 1215 (1988).
- E. Y. Kenig, R. Schneider and A. Gorak, *Chem. Eng. Sci.*, 54, 5195 (1999).
- 19. L. A. Goetter and R. L. Pigford , J. Am. Chem. Soc., 17, 793 (1971).
- 20. H. Hikita, S. Asai and H. Ishikawa, Chem. Eng., J., 18, 169 (1979).
- S. W. Park, D. W. Park, K. J. Oh and S. S. Kim, *Sep. Sci. Technol.*, 44, 543 (2009).
- 22. K. S. Hwang, L. Han, D. W. Park, K. J. Oh and S. W. Park, *Sep. Sci. Technol.*, in review (2010).
- 23. H. Hikita, A. Asai and T. Tsufi, J. Am. Chem. Soc., 23, 538 (1977).
- 24. K. G. Denbigh and A. J. Prince, J. Am. Chem. Soc., 69, 790 (1947).
- 25. P. Gray and A. D. Yoffe, Chem. Rev., 55, 1069 (1955).
- 26. J. J. Carberry, Chem. Eng. Sci., 9, 189 (1959).
- 27. P. G. Caudle and K. G Denbigh, Trans. Faraday, Soc., 49, 39 (1959).
- 28. M. M. Wendel and R. L. Pigford, J. Am. Chem. Soc., 4, 249 (1958).
- L. K. Daraiswany and M. M. Sharma, *Heterogeneous reaction:* Analysis, example and reactor design, John Wiley Sons, New York (1984).
- 30. W. Yu, G. Astarita and D. W. Savage, *Chem. Eng. Sci.*, **40**, 1585 (1985).
- S. W. Park, D. W. Park, K. J. Oh and S. S. Kim, *Sep. Sci. Technol.*, 44, 543 (2009).
- 32. G. F. Versteeg and W. P. M. van Swaaij, *J. Chem. Eng. Data*, **33**, 29 (1988).
- A. K. Saha, S. S. Bandyopadhyay and A. K. Biswas, J. Chem. Eng. Data, 38,78 (1993).
- W. Pasiuk-Bronikowska and K. J. Rudzinski, *Chem. Eng. Sci.*, 46, 2281 (1991).
- 35. F. T. Shadid and D. Handley, Chem. Eng. Res. Dev., 67, 185 (1989).
- E. L. Cussler, *Diffusion*, Cambridge University Press, New York (1984).
- G. Carta and R. L. Pigford, *Ind. Eng. Chem. Fundam.*, 22, 329 (1983).

1450