



Corrosion fatigue crack growth mechanisms in welded joints of marine steel structures

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Abstract: This paper presents a model of fatigue crack growth in a welded joint and a two-dimensional model of anodic dissolution based on Donahue model and anodic dissolution mechanism, respectively. In addition, a model for predicting the corrosion fatigue crack growth rate in welded joints of steel marine structures is established and crack growth mechanisms are analyzed. The results show that during early stages of crack growth, corrosion fatigue crack growth rate in welded joints is mainly controlled by corrosion action, whereas cyclic loading becomes more influential during the later stage of crack propagation. Loading frequency and effective stress ratio can affect rupture period of protective film at the corrosion fatigue crack tip and the length of corrosion crack increment, respectively, which changes the influence of corrosion action on crack growth rate. However, the impact of stress amplitude on crack growth rate is only significant when crack propagation is caused by cyclic loading. Welding residual stress not only improves the effective stress ratio of cyclic loading, but also promotes crack closure and increases corrosion fatigue crack growth rate in welded joints. Compared to corrosion action, welding residual stress has a more significant influence on crack growth caused by cyclic loading.

Key words: welded joints; corrosion fatigue; growth mechanism; multi-factor

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1 Introduction

Welding is widely used to connect steel components of marine structures. However, welded joints have complex microstructures that retain high levels of welding residual stress, and therefore, often promote initiation of corrosion fatigue cracks. Moreover, the combined effects of the marine environment and wave loading can quickly lead to corrosion fatigue failure of welded marine structures [1–3]. Thus, the corrosion fatigue life of welded joints is much shorter in marine

environments compared to inert environments; moreover, the safety and integrity of welded marine structures are often reduced by corrosion. Therefore, further investigation on corrosion fatigue crack growth mechanisms in welded joints of marine steel structures is merited to improve both the safety and service life of steel marine structures.

Compared to the fatigue process in inert environments, corrosion fatigue of welded joints in marine environments is more complex; nonetheless, some important results have been achieved to date. ZHAO et al [4] used finite element simulations to study the corrosion fatigue crack initiation

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mechanism of X80 steel in a marine environment and showed that, in addition to the effects of corrosion pit-induced stress concentrations, corrosion products that adhere to the metal surface can promote the initiation of corrosion fatigue cracks. In another study, CHANG [5] used acoustic emissions to examine the corrosion fatigue crack growth mechanism of X52 steel and AZ31 aluminum alloy in a 3.5% sodium chloride (NaCl) solution, and found that for X52 steel, anodic dissolution is the main mechanism of corrosion fatigue crack propagation in simulated seawater. Meanwhile, WU et al [6] reported that corrosion fatigue crack growth is accelerated in the marine environment when the surrounding temperature increases, and the impact of temperature on the corrosion fatigue crack growth rate of FV520B steel was most significant at relatively low stress amplitudes.

At present, most research on corrosion fatigue is empirically performed in a simulated marine environment. However, materials used in welded joints, and therefore corrosion fatigue crack growth mechanisms, vary widely in real-world conditions and real-world parameters differ greatly from the corrosion and loading parameters used in experiments; therefore, previous empirical results cannot be universally adopted. Moreover, real-world data on corrosion fatigue crack growth mechanisms of welded joints in steel marine structures are difficult and expensive to obtain due to harsh marine environments. Theoretical studies can considerably shorten research time, reduce research costs, and produce results with universal applicability. To this end, theoretical research on corrosion fatigue crack growth mechanisms of welded joints in steel marine structures can effectively fill the gaps in existing experimental research.

The initiation region and growth rate of a corrosion fatigue crack are determined by many factors including the weld geometry, microstructures of different zones of the welded joint, stress concentrations, weld defects, and the crack growth path [7–9]. As a result, theoretical parameters must be treated as random variables affected by a number of influencing factors, which increases the complexity of theoretical analyses. Owing to the geometry, microstructure, and stress concentration at the weld toe, this area is typically

the most sensitive to corrosion fatigue crack initiation in defect-free joints [10–12]. Therefore, studies on corrosion fatigue crack initiation at the weld toe are greatly important and the research can be universally applied.

This paper presents a model for predicting fatigue crack growth rate based on the model proposed by DONAHUE et al [13]. By introducing additional parameters including the shape coefficient, opening ratio, and welding residual stress, the Donahue crack growth model can be extended to welded joints. Meanwhile, a two-dimensional model of corrosion-induced anodic dissolution is established according to the anodic dissolution mechanism. Then, fatigue crack growth model and the anode dissolution rate model are combined to establish a new model suitable for calculating the corrosion fatigue crack growth rate of welded joints in steel marine structures. The proposed model was validated and can be used to effectively analyze corrosion fatigue crack growth mechanisms in welded joints of steel marine structures. The influences of various factors on the corrosion fatigue crack growth rate are discussed.

2 Fatigue crack growth model of welded joint

2.1 Model selection

2.1.1 Basic fatigue crack growth model

In 1963, PARIS et al [14] proposed a formula for calculating the fatigue crack growth rate. Further to this, FORMAN [15] and DONAHUE et al [13] proposed several fatigue crack growth models with a wider range of applications. However, as the scope of application increased, more experimental parameters were required to perform calculations, which placed practical limitations on the model.

To reduce the number of unknown parameters and consider many stages of fatigue failure of welded joints as possible, the basic form of the fatigue crack growth model proposed by DONAHUE et al [13] can be expressed as

$$(da/dN)_m = C \cdot [\Delta K - \Delta K_{th}]^m \quad (1)$$

where $(da/dN)_m$ is the fatigue crack growth rate in an inert environment; ΔK is the stress intensity factor (SIF) range; ΔK_{th} is the threshold of the SIF

range; and C and m are material constants. When predicting the corrosion fatigue crack growth rate, the model proposed by DONAHUE et al [13] can eliminate the influence of the crack initiation stage on the prediction of the crack growth rate during the stable growth stage, and is therefore suitable for the aims of our study.

2.1.2 Stress intensity factor range

High temperature and uneven heating can produce irregular deformation of a joint during the welding process, resulting in a different stress distribution on the welded surface compared to the unwelded metal. Therefore, the traditional formula for calculating the SIF of a surface crack of a welded joint must be improved. Most experimental results suggest that a load parallel to the crack growth direction will have little effect on crack propagation. Therefore, in the mathematical model, the load acts perpendicular to the direction of crack growth and is modeled as unidirectional stress.

The SIF range of the surface crack of the welded joint can be expressed as [16]

$$\Delta K = \frac{M_s M_T M_k}{\Phi_0} \Delta \sigma \sqrt{\pi a} \quad (2)$$

where Φ_0 is a complete elliptic integral of the second kind; M_s is the free surface correction coefficient; M_T is the finite thickness correction factor; M_k is the correction factor of the weld toe; $\Delta \sigma$ is the actual stress amplitude; and a is the crack depth.

Furthermore, if the following two conditions are met: 1) There is no longitudinal fillet weld on the surface of the welded joint; 2) The welded joint does not bear the load directly. then, the average contour of the weld can be expressed as [16, 17]

$$2c = 6.71 + 2.58a \quad (3)$$

where c is the semi-elliptical surface crack length.

Correction factor $M_s M_T / \Phi_0$ can be used to modify the SIF of a surface crack in the welded joint [16]:

$$\frac{M_s M_T}{\Phi_0} = 1.122 - 0.231 \frac{a}{B} + 10.55 \left(\frac{a}{B} \right)^2 - 21.7 \left(\frac{a}{B} \right)^3 + 33.19 \left(\frac{a}{B} \right)^4 \quad (4)$$

where B is the thickness of the welded plate.

The value of M_k can be calculated as [17]

$$\begin{cases} M_k = \left(5 \frac{a}{B} \right)^{-q}, & 0.1 \leq a < 0.2B \\ M_k = 1, & a \geq 0.2B \end{cases} \quad (5)$$

$$q = \ln[(11.584 - 0.0588\theta) / 2.30] \quad (6)$$

where θ is a degree related to the residual height of the welded joint, as shown in Figure 1.

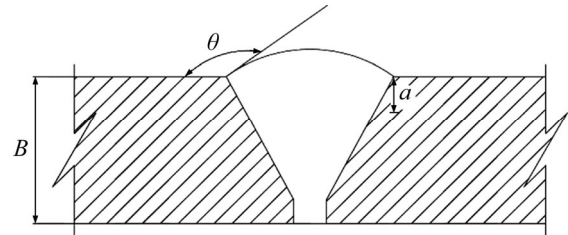


Figure 1 Physical meaning of θ

2.1.3 Threshold value of SIF range

The threshold value of the SIF range (ΔK_{th}) is closely related to the metal type, service environment, and stress ratio. Hence, ΔK_{th} used in calculations is generally obtained experimentally, which increases the number of experiments required. To solve this problem, YU [18] proposed the concept of fatigue crack growth threshold value. The empirical formula for fatigue crack growth threshold can be obtained by summing experimental values, as follows:

$$a_{th} = \left(\frac{1}{\pi^{0.5}} \right)^{0.5+b_1} = 0.564 \frac{1}{0.5+b_1} \quad (7)$$

where a_{th} is the fatigue crack growth threshold value and b_1 is the fatigue strength factor, expressed as

$$b_1 = -\frac{1}{m} \quad (8)$$

When $a \geq a_{th}$, the fatigue crack is considered to be in the stable growth stage.

2.1.4 Opening ratio

Fatigue cracks in welded joints are only considered fully open when the cyclic tensile load exceeds a certain critical value, referred to as the crack closure effect. The closure effect has a significant influence on the crack growth threshold value and results in significant changes of residual fatigue lifetime of welded joints [19]. Owing to the complexity of experimental methods for calculating the opening ratio, researchers are constantly

searching for a theoretical method. Many literatures consider the closure effect by introducing the opening ratio into computational model, and the calculation models with higher accuracy are achieved, such as the iLAPS model [20] and modified NASGRO equation [21]. The formula used for calculating the opening ratio can be expressed as [22]:

$$U = \frac{1 - f'}{1 - R} \tag{9}$$

where

$$f' = \begin{cases} \max(R, A_0 + A_1R + A_2R^2 + A_3R^3), & R \geq 0 \\ A_0 + A_1R, & -2 \leq R < 0 \end{cases} \tag{10}$$

$$A_0 = (0.825 - 0.34\alpha + 0.05\alpha^2) [\cos(\pi\sigma_{\max} / 2\sigma_f)]^{1/\alpha} \tag{11}$$

$$A_1 = (0.415 - 0.071\alpha)\sigma_{\max} / \sigma_f \tag{12}$$

$$A_2 = 1 - A_0 - A_1 - A_3 \tag{13}$$

$$A_3 = 2A_0 + A_1 - 1 \tag{14}$$

where α is the stress–strain constraint coefficient, which is equal to 1 during the plane stress state and equal to 3 under the plane strain state; σ_f is the flow stress. Flow stress σ_f can be expressed as [23]

$$\sigma_f = 1.15(\sigma_y + \sigma_u) / 2 \tag{15}$$

where σ_y is the yield strength and σ_u is the tensile strength.

The opening ratio can be solved by substituting Eqs. (10)–(15) into Eq. (9).

2.1.5 Welding residual stress

The SIF due to welding residual stress can be calculated using the weight function method. If the welding residual stress distribution perpendicular to the direction of crack growth is $\sigma_{\text{res}}(x)$, the SIF increment due to welding residual stress can be expressed as

$$K_{\text{res}} = \int_0^a h(x, a) \sigma_{\text{res}}(x) dx \tag{16}$$

where x is the distance from the crack initiation point along the crack growth direction and $h(x, a)$ is the weight function.

To facilitate this calculation, the relationship between the welding residual stress and the position of the crack can be simplified using a piecewise function, as shown in Figure 2 [24].

$$\text{If } a \leq b, \tag{17}$$

$$K_{\text{res}} = \sigma_0^{\text{res}} \sqrt{\pi a}$$

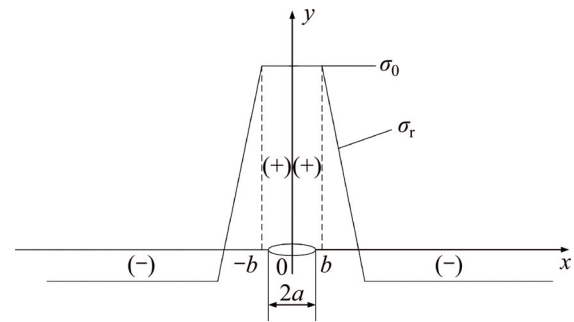


Figure 2 Simplified representation of welding residual stress distribution ((+) denotes tensile stress section and (–) denotes compressive stress section)

where σ_0^{res} is the welding residual stress at the crack tip perpendicular to the crack growth direction. The positive and negative values of σ_0^{res} represent the residual tensile stress and the residual compressive stress, respectively.

If $b < a \leq l$,

$$K_{\text{res}} = \sigma_0^{\text{res}} \sqrt{\pi a} (2/\pi) \left\{ \frac{\pi}{2} - \frac{1}{l-b} \left[\sqrt{(a^2 - b^2)} - \frac{b\pi}{2} + b \arcsin \frac{b}{a} \right] \right\} \tag{18}$$

2.2 Model deduction

Based on the equations in Section 2.1, the fatigue crack growth model of welded joint can be deduced.

Substituting the shape coefficient $\chi(a, B, \theta) = \frac{M_s M_T M_k}{\Phi_0}$ into Eq. (2), we obtain the formula for calculating the SIF range, as follows:

$$\Delta K = \chi(a, B, \theta) \Delta \sigma \sqrt{\pi a} \tag{19}$$

Since

$$\Delta \sigma = \sigma_{\text{max}} (1 - R) \tag{20}$$

Then, substituting Eq. (20) into Eq. (19), we obtain

$$\Delta K = \chi(a, B, \theta) \sigma_{\text{max}} (1 - R) \sqrt{\pi a} \tag{21}$$

where σ_{max} is the maximum cyclic stress and R is the actual stress ratio.

By substituting Eqs. (4)–(6) and $\chi(a, B, \theta)$ into Eq. (21), the SIF range of the surface crack of the welded joint can be solved. Meanwhile, by substituting Eqs. (7) and (8) into Eq. (21), the threshold value of the SIF range for a surface crack of the welded joint can be also achieved:

$$\Delta K_{\text{th}} = \chi(a_{\text{th}}, B, \theta) \sigma_{\text{max}} (1 - R) \sqrt{\pi a_{\text{th}}} \tag{22}$$

The crack closure effect can be included by introducing the opening ratio into the fatigue crack growth model. Therefore, the relationship between the effective stress amplitude and the actual stress amplitude is

$$\Delta\sigma_{\text{eff}} = U\Delta\sigma \quad (23)$$

where $\Delta\sigma_{\text{eff}}$ is the effective stress amplitude, and U is the opening ratio.

The SIF at a crack tip containing welding residual stress can be obtained by superimposing the SIF of the crack tip without the welding residual stress field and the SIF with the welding residual stress field according to ASME-FFS/API 579-1. Therefore, when welding residual stress is present, the effective SIF of the crack tip is

$$\begin{cases} K_{\text{eff}}^{\text{max}} = K_{\text{max}} + K_{\text{res}} \\ K_{\text{eff}}^{\text{min}} = K_{\text{min}} + K_{\text{res}} \end{cases} \quad (24)$$

where $K_{\text{eff}}^{\text{max}}$ and $K_{\text{eff}}^{\text{min}}$ are the maximum and minimum effective SIF of the crack tip under cyclic loading, respectively; K_{res} is the increment of SIF caused by welding residual stress. If $K_{\text{eff}}^{\text{min}} < 0$, then $K_{\text{eff}}^{\text{min}}$ is 0.

The presence of welding residual stress will not affect the SIF range of crack tip but will change the fatigue crack growth rate by influencing the effective stress ratio of cyclic loading. Considering welding residual stress, the effective stress ratio of cyclic loading is

$$R_{\text{eff}} = \frac{K_{\text{eff}}^{\text{min}}}{K_{\text{eff}}^{\text{max}}} \quad (25)$$

where R_{eff} is the effective stress ratio.

Substituting Eqs. (16)–(18) and (24) into Eq. (25), the effective stress ratio of cyclic loading considering welding residual stress can be obtained and the influence of welding residual stress can be introduced into the model.

By determining the shape coefficient, SIF range, threshold value of the SIF range, opening ratio, and welding residual stress of the welded joint, the fatigue crack growth rate of welded joint can be calculated by substituting Eqs. (21)–(23) into Eq. (1). Replacing $\Delta\sigma$ and R with $\Delta\sigma_{\text{eff}}$ and R_{eff} , respectively, the model can be expressed as

$$(da/dN)_m = CU^m \left[\chi(a, B, \theta) \sigma_{\text{max}} (1 - R_{\text{eff}}) \sqrt{\pi a} - \chi(a_{\text{th}}, B, \theta) \sigma_{\text{max}} (1 - R_{\text{eff}}) \sqrt{\pi (0.564)^{0.5+b_1}} \right]^m \quad (26)$$

3 Model of corrosion fatigue crack growth in welded joint

3.1 Basic corrosion fatigue crack growth model

The corrosion fatigue failure of welded joints caused by the corrosion and cyclic loading is complicated. Under the influence of corrosion, the corrosion damage and crack source regions will first appear between the area of weld joint and heat-affected zone [25]. During the growth of corrosion fatigue crack, the passivation film at the crack tip will be teared under the action of cyclic loading, and then the corrosion of bare metal at the crack tip is promoted and the growth of crack is further accelerated. The corrosion process of bare metal at the crack tip is shown in Figure 3. Both the corrosion and fatigue damages can be observed at the fracture of corrosion fatigue crack, and the fatigue striations and corrosion damages will appear alternately on the surface of the fracture as shown in Figure 4 [26–28].

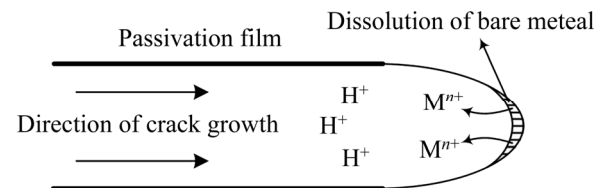


Figure 3 Corrosion process of bare metal at crack tip

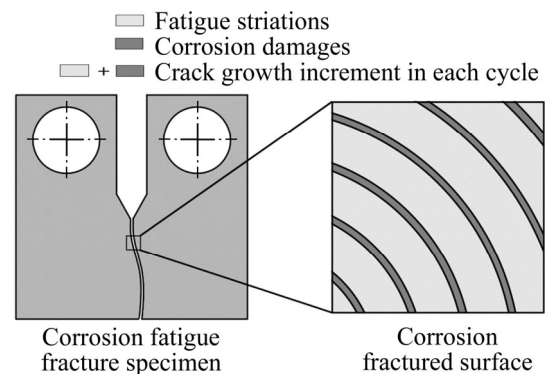


Figure 4 Corrosion and fatigue damages at fracture of corrosion fatigue crack

The corrosion and fatigue behaviors of welded joints can be analyzed separately in corrosion fatigue life prediction [29, 30]. According to the corrosion environment and material, the basic model for calculating corrosion fatigue crack growth rate can be divided into three separate models: superposition model, competition model,

and dislocation dipole model. High-strength steel is often used in marine structures; therefore, the superposition model is chosen as the base model for calculating the corrosion fatigue crack growth rate of the welded joint [31]:

$$(da/dN)_c = (da/dN)_m + (da/dN)_{cf} \quad (27)$$

where $(da/dN)_c$ is the total growth rate of the corrosion fatigue crack, and $(da/dN)_{cf}$ is the crack growth rate caused by corrosion. During the calculation, crack growth due to corrosion is usually expressed as da/dt . Hence, Eq. (28) can be converted into:

$$(da/dN)_c = (da/dN)_m + \frac{1}{f}(da/dt)_{cf} \quad (28)$$

where f is the loading frequency.

3.2 One-dimensional model of anodic dissolution

When a welded structure is subjected to fatigue loading in a corrosive environment, stress concentration phenomena occur at the crack tip and accelerate the oxidation reaction of the bare metal surface. Metal atoms lose electrons, which are converted into metal ions that diffuse into the corrosive medium, leading to anodic dissolution. FORD et al [32] decomposed this process into three stages: cation diffusion, fracture of the oxide film at the crack tip, and dissolution of new metal. Among them, corrosion fatigue crack growth due to anodic dissolution is mainly related to fracture of the oxide film and dissolution of new metal. According to Faraday’s law, a relationship can be established between the crack growth rate and oxidation charge density and rupture strain of the oxide film, as follows:

$$\bar{V}_t = \frac{MQ_f \varepsilon_{ct}}{n\rho F \varepsilon_f} \quad (29)$$

where \bar{V}_t is the crack growth rate due to anodic dissolution; Q_f is the oxidation charge density; ε_{ct} is the strain rate at the crack tip; ε_f is the rupture strain of oxide film; n is the number of electrons released by the oxidation of a single metal atom; F is Faraday’s constant; M is the molar mass of a single metal atom; and ρ is the metal density at the crack tip.

As bare material at the crack tip is transformed into a passivation film, current generated by the oxidation reaction is attenuated and the current

density of anodic dissolution at this stage can be expressed as [33]:

$$i(t) = i_0 \exp[-\lambda(t-t_d)] \quad (30)$$

where i_0 is the corrosion current density generated by the corrosion of new metal at the crack tip; λ is the passivation coefficient of current attenuation, and t_d is the generation cycle of passivated film.

Changes in the anodic dissolution current density at the crack tip over time are shown in Figure 5.

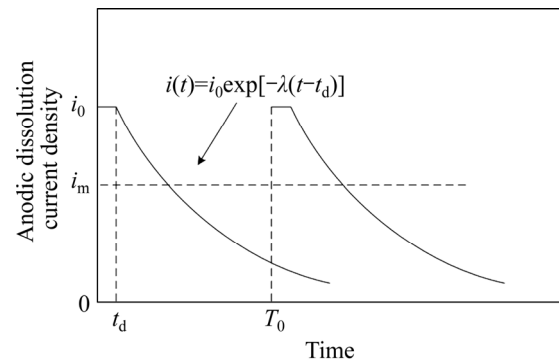


Figure 5 Variation of anodic dissolution current density at crack tip with time

Assuming the rupture period of the oxide film at the crack tip T , the crack growth rate due to anodic dissolution can be derived from Eqs. (29) and (30) as

$$(da/dN)_{cf} = \frac{1}{f} \frac{da}{dt} = \begin{cases} \frac{1}{f} \frac{Mi_0}{n\rho F}, & 0 \leq t \leq t_d \\ \frac{1}{f} \frac{Mi_0}{n\rho F} [1 - \exp(-(t-t_d))], & t_d < t < T \end{cases} \quad (31)$$

3.3 Two-dimensional model of anodic dissolution

Since Eq. (31) presents a one-dimensional model, it cannot be superimposed with Eq. (26), which is a two-dimensional model. Therefore, it is necessary to convert Eq. (31) into a two-dimensional model. The crack growth increment due to anodic dissolution can be approximated as a rectangle and the crack width can be a time-dependent function $w(t)$, as shown in Figure 6 [34].

The two-dimensional form of Eq. (31) is

$$(da/dN)_{cf} = \frac{1}{f} \frac{da}{dt} =$$

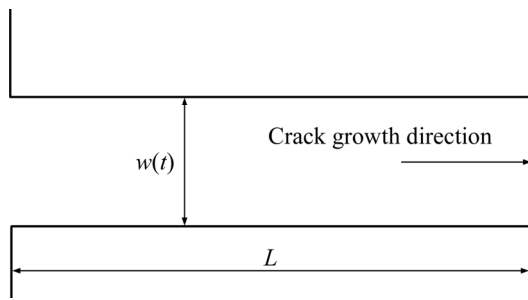


Figure 6 Crack growth increment due to anodic dissolution

$$\begin{cases} \frac{1}{f} \frac{Mi_0}{n\rho Fw(t)}, & 0 \leq t \leq t_d \\ \frac{1}{f} \frac{Mi_0}{n\rho Fw(t)} [1 - \exp(-(t-t_d))], & t_d < t \leq T \end{cases} \quad (32)$$

Under cyclic loading, the width of a parallel crack can be expressed as:

$$w(t) = w_m g(t) \quad (33)$$

where w_m is the average width of crack increment under different cyclic loading periods. Function $g(t)$ can be expressed as:

$$g(t) = 1 + \varepsilon \sin(\omega t) \quad (34)$$

where $\omega = \pi f / 2$; ε is constant and $\varepsilon = \Delta K / 2K_m$. For a constant load,

$$\varepsilon = \frac{\Delta K}{2K_m} = \frac{K_{\max} - K_{\min}}{2 \times \frac{K_{\max} + K_{\min}}{2}} = \frac{K_{\max} - K_{\min}}{K_{\max} + K_{\min}} = \frac{1 - R_{\text{eff}}}{1 + R_{\text{eff}}} \quad (35)$$

After substituting Eqs. (34) and (35) into Eq. (33), the following equation is obtained:

$$w(t) = w_m \left(1 + \frac{1 - R_{\text{eff}}}{1 + R_{\text{eff}}} \sin\left(\frac{\pi f t}{2}\right) \right) \quad (36)$$

Thus, the corrosion fatigue crack growth rate caused by anode dissolution can finally be expressed as

$$\begin{cases} \frac{1}{f} \frac{Mi_0}{n\rho Fw_m \left[1 + \frac{1 - R_{\text{eff}}}{1 + R_{\text{eff}}} \sin\left(\frac{\pi f t}{2}\right) \right]}, & 0 \leq t \leq t_d \\ \frac{1}{f} \frac{Mi_0 [1 - \exp(t_d - t)]}{n\rho Fw_m \left[1 + \frac{1 - R_{\text{eff}}}{1 + R_{\text{eff}}} \sin\left(\frac{\pi f t}{2}\right) \right]}, & t_d < t \leq T \end{cases} \quad (37)$$

According to the superposition principle, the

corrosion fatigue crack growth rate in the welded joint can be obtained from Eqs. (26), (27) and (37), as follows:

$$\begin{aligned} (da/dN)_c &= C \left(\frac{1-f'}{1-R_{\text{eff}}} \right)^m \left[\chi(a, B, \theta) \sigma_{\max} (1-R_{\text{eff}}) \cdot \right. \\ &\quad \left. \sqrt{\pi a} - \chi(a_{\text{th}}, B, \theta) \sigma_{\max} (1-R_{\text{eff}}) \cdot \right. \\ &\quad \left. \sqrt{\pi (0.564)^{0.5+b_1}} \right]^m + \frac{1}{f} \cdot \\ &\quad \frac{Mi(t)}{n\rho Fw_m \left[1 + \frac{1 - R_{\text{eff}}}{1 + R_{\text{eff}}} \sin\left(\frac{\pi f t}{2}\right) \right]} \end{aligned} \quad (38)$$

4 Model validation

A flowchart of the steps for calculating the corrosion fatigue crack growth rate of a welded joint is shown in Figure 7.

To validate the model, published experimental data on the corrosion fatigue crack growth rate of welded joints of S355 J2+N, grade 250, and X65 in simulated seawater were collected [35–37], and compared with the results of the proposed model. The shape parameters of welded joints and main test parameters, taken from Refs. [35–37], are presented in Table 1. During the test, S355J2+N and X65 steel welded joints were processed into standard compact tension specimens. For calculations, parameter θ of the welded joints was taken as 0° for both the S355J2+N and X65 steel specimens. The loading mode used in the tests presented in Refs. [35–37] is stress loading.

The model validation results are shown in Figure 8.

From Figure 8, it can be concluded that the model proposed in this paper accurately predicts the corrosion fatigue crack growth rate of S355 J2+N, grade 250, and X65 welded joints; however, calculated results are slightly lower than published values. This is because although the superposition model adopted in the modeling process takes into account the effect of corrosion on the crack growth rate to some extent, it is difficult to fully predict the coupled effect of corrosion action and fatigue loading, which reduces the predictive ability of the model. By setting appropriate parameters in the corrosion fatigue process, the proposed model can effectively predict the corrosion fatigue crack growth rate in welded joints of different steels in

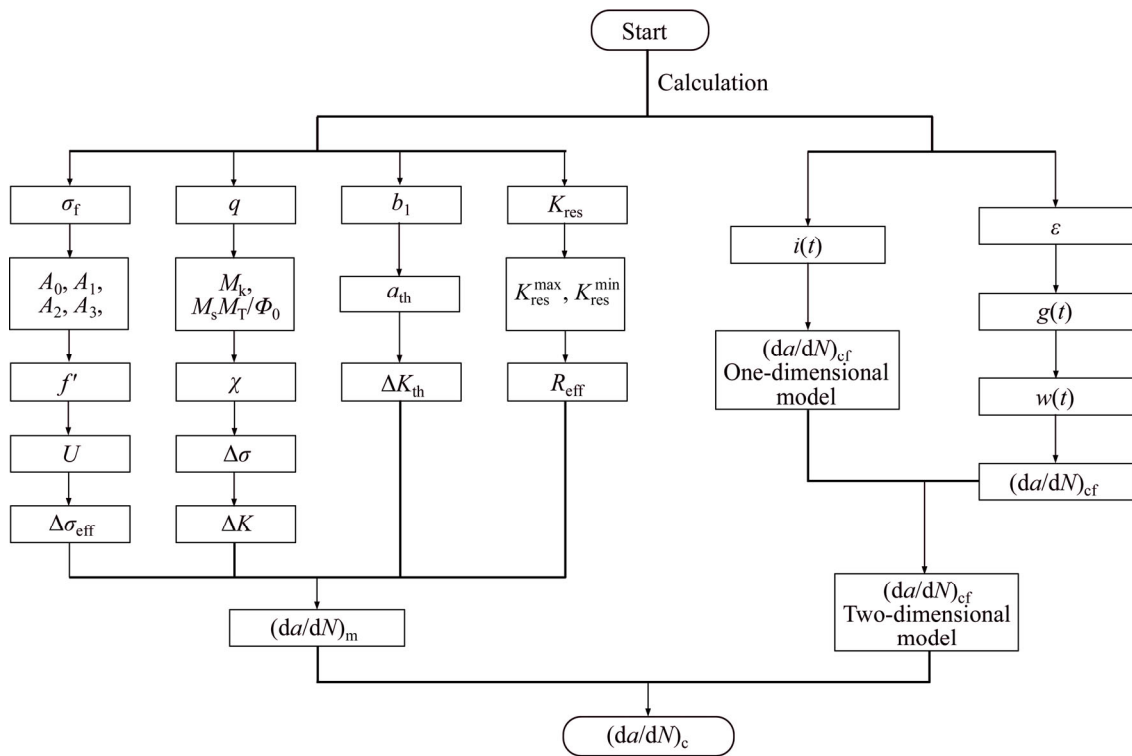


Figure 7 Analytical flow of calculation model

Table 1 Shape parameters and main experimental parameters of welded joints

Material	$\theta(^{\circ})$	B/mm	$\Delta\sigma/\text{MPa}$	R	f/Hz	Pre-cracked	Corrosion liquid	Testing machine	Standard
S355 J2+N	0	16	127	0.1	0.3	Yes	Seawater	Servo-hydraulic fatigue testing machine	ASTM E467
Grade 250	160	12	115	0.1	0.1	No	3.5 % NaCl	Instron universal tensile testing machine	ASTM E466
X65 steel	0	25	157	0.2	0.01	Yes	3.5 % NaCl	Servo-hydraulic testing machine	ASTM E467

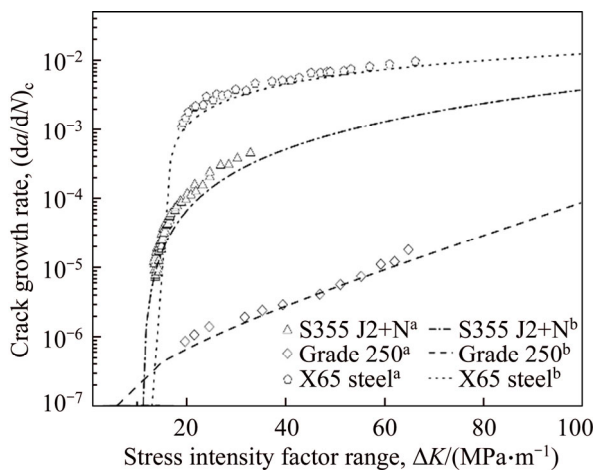


Figure 8 Model validation (a–Published experimental results and b–Calculated values)

the marine environment. Furthermore, the proposed theoretical approach can be used to study the corrosion fatigue crack growth mechanism of welded joints in steel marine structures.

5 Results and discussion

To study the corrosion fatigue crack growth mechanism of welded joints using the mathematical model established in this paper, we established a virtual experimental model. The virtual specimen and loading direction used in the experiment are illustrated in Figure 9.

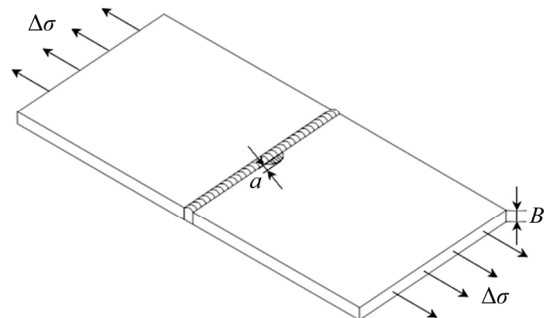


Figure 9 Virtual specimen and loading direction

No pre-crack was introduced in the virtual model. Additional shape parameters are presented along with the main test parameters in Table 2. To investigate the influence of a particular parameter on the corrosion fatigue crack propagation rate of welded joints, the parameter is replaced with a free variable, which is varied throughout the analysis.

Table 2 Shape parameters and main test parameters of virtual model

Material	$\theta/(^\circ)$	B/mm	$\Delta\sigma/\text{MPa}$	R	f/Hz
X65 steel	160	20	81	0.1	0.1

5.1 Influence of corrosion action and fatigue loading

Both corrosion action and fatigue loading can promote corrosion fatigue failure of welded joints; however, the mechanism of action is different in each case. In this paper, the influence of corrosion action and fatigue loading on the corrosion fatigue crack growth rate in a welded joint was obtained using the proposed models for calculating fatigue crack growth rate $(da/dN)_m$ and anodic dissolution rate $(da/dN)_{cf}$, as shown in Figure 10.

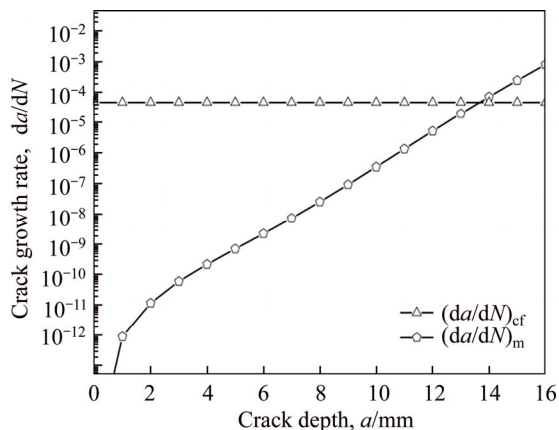


Figure 10 Influence of corrosion action and fatigue loading on corrosion fatigue crack growth rate in a welded joint

As shown in Figure 10, the effect of lifting due to corrosion on early corrosion fatigue crack growth in a welded joint is more significant than the influence of fatigue loading. This is the main reason that early growth rates of corrosion fatigue cracks are much higher than early growth rates of simple fatigue crack. During crack propagation, the influence of corrosion action on the crack growth rate remains almost unchanged, whereas the influence of fatigue loading is significantly

enhanced as the crack depth increases, finally becoming the main factor controlling crack growth during later stages of crack growth.

5.2 Loading frequency

Loading frequency can influence the anodic dissolution rate of metal at the crack tip by affecting the rupture period of the protective film and the amount of time base metal is exposed at the crack tip, both of which influence the corrosion fatigue crack growth rate in the welded joint. The influence of loading frequency on the corrosion fatigue crack growth rate is illustrated in Figure 11.

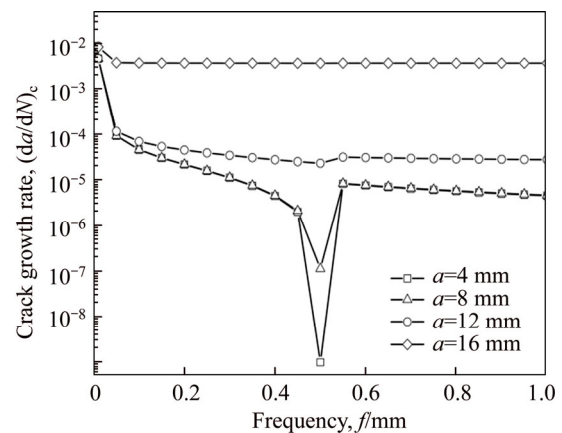


Figure 11 Influence of loading frequency on corrosion fatigue crack growth rate

During the early stages of corrosion fatigue crack propagation, the influence of loading frequency on crack growth rate is related to the generation of a passivation film. When $1/f \geq t_d$, new metal undergoes the entire passivation film generation process during a single loading cycle. Therefore, the passivation time of the metal and the average crack width at the crack tip increase simultaneously as the loading frequency increases, which leads to a slower crack growth rate. When $1/f < t_d$, the passivation film at the crack tip is continuously torn during crack propagation and the current density generated at the crack tip is always i_0 . Variation of the corrosion fatigue crack growth rate is only related to the influence of load frequency on the average crack width, and the crack growth rate slowly decreases as the loading frequency increases. Once the corrosion fatigue crack reaches a certain depth, changes in the loading frequency no longer have a significant impact on the corrosion fatigue crack growth rate and fatigue loading gradually becomes the dominant factor.

5.3 Effective stress ratio

The effective stress ratio affects both the fatigue crack growth rate and corrosion fatigue crack growth rate in welded joints, as shown in Figure 12.

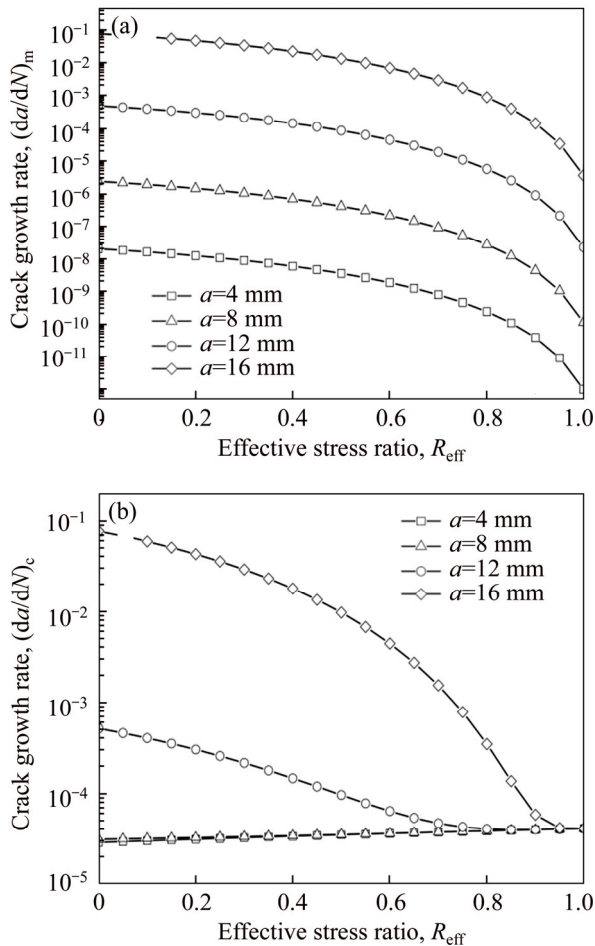


Figure 12 Influence of effective stress ratio on crack growth rate: (a) Fatigue crack; (b) Corrosion fatigue crack

The influence of the effective stress ratio on the fatigue crack growth rate remains the same throughout the various stages of fatigue crack growth. When the effective stress ratio increases, the slip band generated during fatigue crack growth is narrower, which reduces the fatigue crack growth rate in the welded joint (Figure 12(a)). Moreover, the crack depth does not significantly influence the impact of the effective stress ratio on the fatigue crack growth rate.

On the other hand, as the effective stress ratio increases, the increment in crack width caused by anodic dissolution decreases and the increment in crack length at the crack tip increases, thereby increasing the corrosion fatigue crack growth rate.

Thus, corrosion action is the main factor affecting crack growth rate during the early stages of corrosion fatigue crack propagation, and any increase in the effective stress ratio further promotes corrosion fatigue crack growth (Figure 12(b)). During the late crack growth stage, the growth rate is mainly dominated by fatigue loading and the effective stress ratio will have a similar influence on the corrosion fatigue crack growth rate and fatigue crack growth rate.

5.4 Stress amplitude

The influence of stress amplitude on the fatigue crack growth rate and corrosion fatigue growth rate in the welded joint is illustrated in Figure 13.

As the stress amplitude increases, the fatigue crack growth rate of the welded joint decreases, but only up to a critical value $\Delta\sigma_0$ (represented by solid black data points in Figure 13); thereafter, further increases in the stress amplitude will significantly increase the fatigue crack growth rate. Furthermore,

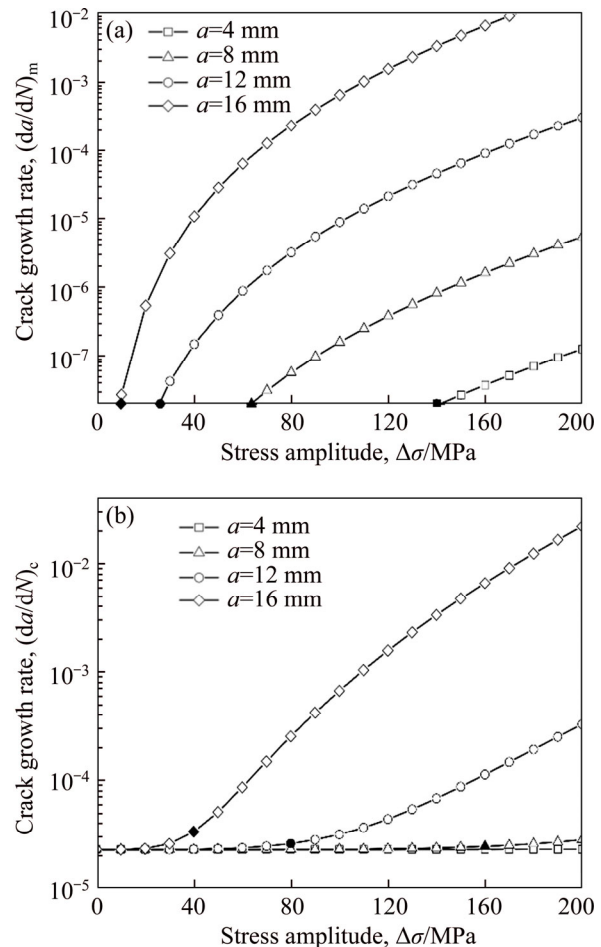


Figure 13 Influence of stress amplitude on crack growth rate: (a) Fatigue crack; (b) Corrosion fatigue crack

as the crack depth increases, $\Delta\sigma_0$ will continuously decrease and only a small amount of fatigue loading will cause significant crack growth when the crack depth is very large, and increasing the stress amplitude can also speed up the fatigue crack growth rate.

Since changes in stress amplitude have very little influence on corrosion action, the stress amplitude will not have significant influence on the corrosion fatigue crack growth rate during early stages of crack propagation (Figure 13(b)). Then, when the crack reaches a certain depth, the growth rate is gradually controlled by fatigue loading and the influence of stress amplitude on the corrosion fatigue crack growth rate is gradually strengthened and eventually, similar to the influence on fatigue crack growth.

5.5 Welding residual stress

The influences of welding residual stress on fatigue crack growth rate and corrosion fatigue crack growth rate are illustrated in Figure 14.

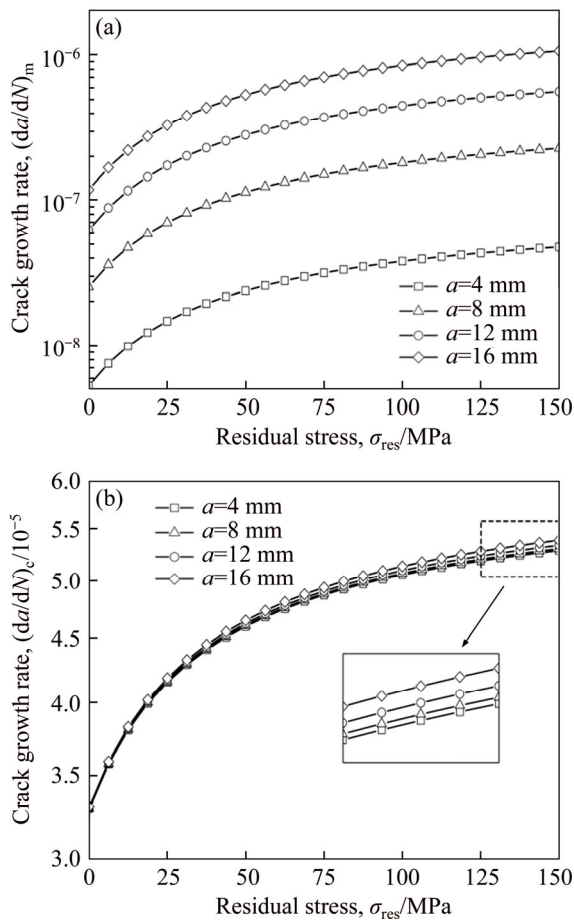


Figure 14 Influence of welding residual stress on crack growth rate: (a) Fatigue crack; (b) Corrosion fatigue crack

Welding residual stress can increase corrosion fatigue crack growth due to both corrosion action and fatigue loading. Compared to the effect of corrosion action, welding residual stress has a greater influence on fatigue loading, which enhances the dominant effect of fatigue loading on the corrosion fatigue crack growth rate.

The reason that welding residual stress has a greater influence on crack growth is that an increase in welding residual stress will increase the effective stress ratio of fatigue loading (Figure 15(a)). Although the fatigue crack growth rate is reduced, welding residual stress also accelerates anodic dissolution at the crack tip, ultimately promoting corrosion fatigue crack growth. At the same time, the increase of both welding residual stress and effective stress ratio promotes corrosion fatigue crack closure (Figure 15(b)), thus accelerating fatigue crack growth in the welded joint. Although changes in welding residual stress can significantly impact the effective stress ratio under fatigue loading, the influence of welding residual stress on

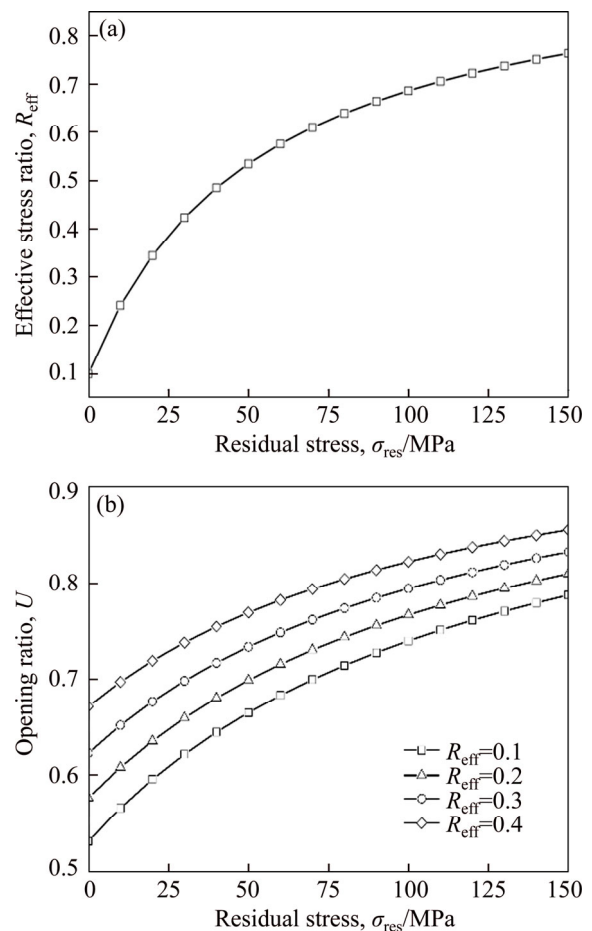


Figure 15 Influence of welding residual stress on effective stress ratio (a) and crack opening ratio (b)

the opening ratio does not change significantly under different effective stress ratios. Therefore, welding residual stress can directly promote the closure effect during the fatigue crack growth process, rather than indirectly affecting the closure effect by changing the effective stress ratio.

6 Conclusions

In this paper, a model for calculating the fatigue crack growth rate in welded joints and a two-dimensional model of anodic dissolution were presented, based on the Donahue model and anodic dissolution mechanism, respectively. In addition, the superposition principle was used to establish a model that is suitable for calculating the corrosion fatigue crack growth rate in welded joints of steel marine structures. The corrosion fatigue crack propagation mechanism in a welded joint of a steel marine structure was analyzed using the proposed model and the conclusions can be summarized as follows:

1) The corrosion fatigue crack growth model established in this paper can effectively predict the corrosion fatigue crack growth rate in welded joints made of different steels in the marine environment and offer some degree of universal applicability. The proposed theoretical model provides an effective way of studying corrosion fatigue crack growth mechanism of welded joints in steel marine structures.

2) The growth rate of corrosion cracks in welded joints during the early stages of crack propagation is mainly controlled by corrosion action. As crack depth increases, the influence of fatigue loading corrosion fatigue crack growth rate also gradually increases and becomes the dominant factor during later stages of crack growth.

3) The loading frequency can affect the rupture period of the protective film and exposure time of base material at the corrosion fatigue crack tip, which alters the contribution of corrosion action to the corrosion fatigue crack growth rate. Furthermore, the influence of fatigue loading to the corrosion fatigue crack growth rate also changes and the effective stress ratio affects the growth rate by changing the length of the corrosion crack increment. Variation of the stress amplitude only has a significant effect on the influence of fatigue loading in the corrosion fatigue crack growth

process, but very little impact on the influence of corrosion action.

4) Welding residual stress can improve the effective stress ratio of cyclic loading and promote crack closure, thereby increasing the corrosion fatigue crack growth rate in welded joints. Compared to corrosion action, welding residual stress has a more significant effect on fatigue loading.

Nomenclature

SIF	Stress intensity factor
ΔK	SIF range
ΔK_{th}	Threshold of SIF range
K_{eff}^{max}	Maximum effective SIF
K_{eff}^{min}	Minimum effective SIF
K_{res}	SIF increment due to welding residual stress
C, m	Material constants
Φ_0	Complete elliptic integral of the second kind
M_s	Free surface correction coefficient
M_T	Finite thickness correction factor
M_k	Weld toe correction factor
$\Delta\sigma$	Actual stress amplitude
$\Delta\sigma_{eff}$	Effective stress amplitude
σ_{max}	Maximum cyclic stress
σ_f	Flow stress
σ_y	Yield strength
σ_u	Tensile strength
σ_0^{res}	Welding residual stress at the crack tip
c	Semi-elliptical surface crack length
a	Crack depth
B	Welded plate thickness
θ	Parameter related to the residual height of the welded joint
χ	Shape coefficient
R	Stress ratio
R_{eff}	Effective stress ratio
a_{th}	Fatigue crack growth threshold
b_1	Fatigue strength factor
U	Opening ratio
α	Stress-strain constraint coefficient
f	Loading frequency
\bar{V}_t	Anodic dissolution crack growth
Q_f	Oxidation charge density
ε_{ct}	Strain rate at the crack tip

ε_f	Rupture strain of oxide film
n	Number of electrons released
F	Faraday's constant
M	Molar mass
ρ	Metal density
i_0	Corrosion current density
λ	Passivation coefficient of current attenuation
t_d	Passivating time required for generating passivated film
T	Time of oxide film rupture at the crack tip
w_m	Average width of crack increment

Contributors

SHAO Fei provided the concept and edited the draft of manuscript. XU Qian and BAI Lin-yue conducted theoretical analysis. XU Qian conducted manuscript writing, data analysis, and edited the draft of manuscript. MA Qing-na conducted a literature review survey. SHEN Mei conducted data verification and icon verification nuclear.

Conflict of interest

XU Qian, SHAO Fei, BAI Lin-yue, MA Qing-na and SHEN Mei declare that they have no conflict of interest.

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中文导读

海洋钢结构焊接接头的腐蚀疲劳裂纹扩展机理

摘要: 本文分别基于 Donahue 模型和阳极溶解机理, 提出了焊接接头疲劳裂纹扩展模型和阳极溶解二维模型。此外, 建立了预测海洋钢结构焊接接头腐蚀疲劳裂纹扩展速率的模型, 并分析了裂纹扩展机理。结果表明, 在裂纹扩展的早期阶段, 焊接接头的腐蚀疲劳裂纹扩展速率主要受腐蚀作用控制, 而在裂纹扩展的后期, 受到循环载荷的影响更大。加载频率和有效应力比会分别影响保护膜在腐蚀疲劳裂纹尖端的破裂时间和腐蚀裂纹扩展长度, 从而改变腐蚀作用对裂纹扩展速率的影响。但是, 应力振幅对裂纹扩展速率的影响仅在周期性载荷引起裂纹扩展时才显著。焊接残余应力不仅提高了循环载荷的有效应力比, 而且还促进了裂纹的闭合并提高了焊接接头的腐蚀疲劳裂纹扩展率。与腐蚀作用相比, 焊接残余应力对循环载荷引起的裂纹扩展的影响更大。

关键词: 焊接接头; 腐蚀疲劳; 生长机理; 多因素