



# Quasi-Ternary System $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$

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**Abstract** Phase equilibria in the quasi-ternary system  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  were studied by physico-chemical analysis methods on 152 alloys that were synthesized by direct single-temperature method. Phase diagrams of the quasi-binary system  $\text{Cu}_2\text{S}$ - $\text{HgS}$ , six vertical sections ( $\text{Cu}_2\text{S}$ - $\text{Cu}_2\text{HgSnS}_4$ ,  $\text{Cu}_2\text{SnS}_3$ - $\text{HgS}$ ,  $\text{Cu}_2\text{HgSnS}_4$ - $\text{SnS}_2$ ,  $\text{Cu}_2\text{Sn}_4\text{S}_9$ - $\text{Cu}_2\text{HgSnS}_4$ ,  $\text{Cu}_4\text{SnS}_4$ - $\text{Cu}_2\text{HgSnS}_4$ , A-B (A—40 mol.%  $\text{HgS}$ , 60 mol.%  $\text{Cu}_2\text{S}$ ; B—40 mol.%  $\text{HgS}$ , 60 mol.%  $\text{SnS}_2$ ), liquidus surface projection, and isothermal section at 670 K were investigated. The coordinates of eutectic points were determined: 59 mol.%  $\text{HgS}$ , 983 K (in the  $\text{Cu}_2\text{S}$ - $\text{HgS}$  system); 73 mol.%  $\text{Cu}_2\text{S}$ , 1060 K (at the  $\text{Cu}_2\text{S}$ - $\text{Cu}_2\text{HgSnS}_4$  section); 18 mol.%  $\text{HgS}$ , 1113 K and 88 mol.%  $\text{HgS}$ , 1035 K (at the  $\text{Cu}_2\text{SnS}_3$ - $\text{HgS}$  section); 83 mol.%  $\text{SnS}_2$ , 1021 K (at the  $\text{Cu}_2\text{HgSnS}_4$ - $\text{SnS}_2$  section).

**Keywords** isothermal section · liquidus surface projection · phase diagram · quasi-ternary system · quasi-binary section · vertical section

## 1 Introduction

Investigation of phase equilibria in the  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  system is part of the systematic study of quasi-ternary systems  $\text{Cu}_2\text{X}$ - $\text{B}^{\text{II}}\text{X}$ - $\text{D}^{\text{IV}}\text{X}_2$  ( $\text{B}^{\text{II}}$ -Zn, Cd, Hg;  $\text{D}^{\text{IV}}$ -Si, Ge, Sn; X-S, Se) and the crystal structure of compounds which

formed in the systems. Binary system components  $\text{Cu}_2\text{S}$ ,  $\text{HgS}$  and  $\text{SnS}_2$  melt congruently at 1401 K,<sup>[1]</sup> 1098 K,<sup>[2]</sup> and 1143 K,<sup>[3]</sup> respectively, and have narrow homogeneity regions near the stoichiometric composition.

The  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  system features the  $\text{Cu}_2\text{HgSnS}_4$  compound which is a direct-band semiconductor.  $\text{Cu}_2\text{HgSnS}_4$  has properties suitable for optoelectronic devices and absorbing layer of thin-film solar cells<sup>[4]</sup> but any possible use would be severely limited due to the toxicity of mercury.

## 2 Quasi-binary Systems

### 2.1 $\text{Cu}_2\text{S}$ - $\text{SnS}_2$ Systems

The results of the studies of the  $\text{Cu}_2\text{S}$ - $\text{SnS}_2$  system were published in Ref 5–10. According to Ref 10, three ternary compounds form in the system,  $\text{Cu}_4\text{SnS}_4$ ,  $\text{Cu}_2\text{SnS}_3$  and  $\text{Cu}_2\text{Sn}_4\text{S}_9$ . The  $\text{Cu}_2\text{SnS}_3$  compound has a natural analog, the mochite mineral<sup>[9]</sup>.

According to Ref 6, in addition to the above compounds, the ternary phase  $\text{Cu}_4\text{Sn}_3\text{S}_8$  was found in the  $\text{Cu}_2\text{S}$ - $\text{SnS}_2$  system.  $\text{Cu}_2\text{SnS}_3$  melts congruently at 1123 K. Compounds  $\text{Cu}_4\text{SnS}_4$  and  $\text{Cu}_2\text{Sn}_4\text{S}_9$  formed in solid-state reactions  $\text{Cu}_2\text{SnS}_3 + \text{Cu}_2\text{S} \rightleftharpoons \text{Cu}_4\text{SnS}_4$  and  $\text{Cu}_4\text{Sn}_3\text{S}_8 + 5\text{SnS}_2 - 2\text{Cu}_2\text{Sn}_4\text{S}_9$  at 1083 and 938 K, respectively.  $\text{Cu}_4\text{Sn}_3\text{S}_8$  is formed by the peritectic reaction  $\text{L} + \text{Cu}_2\text{SnS}_3 \rightleftharpoons \text{Cu}_4\text{Sn}_3\text{S}_8$  and exists in the temperature range 658–1063 K. There are three invariant points in the system, two eutectics and one peritectic, with the coordinates 31 mol.%  $\text{SnS}_2$  and 1093 K, 77 mol.%  $\text{SnS}_2$  and 1043 K, 70 mol.%  $\text{SnS}_2$  and 1063 K, respectively.

According to Ref 5, three phases were found in the  $\text{Cu}_2\text{S}$ - $\text{SnS}_2$  system,  $\text{Cu}_2\text{SnS}_3$ ,  $\text{Cu}_2\text{Sn}_4\text{S}_9$  and  $\text{Cu}_8\text{SnS}_6$ . The

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formation of the first two compounds occurs as described in Ref 6. The difference is in the value of the melting point of  $\text{Cu}_2\text{SnS}_3$  which according to Ref 5 is 1173 K.  $\text{Cu}_8\text{SnS}_6$  is formed by the solid-state reaction  $3\text{Cu}_2\text{S} + \text{Cu}_2\text{SnS}_3 - \text{Cu}_8\text{SnS}_6$  at 1083 K. The solid solutions range of  $\text{Cu}_2\text{S}$ ,  $\text{SnS}_2$  and ternary compounds are 2 mol.% or less.

Given existing contradictions in the literature, the authors of Ref 11 re-investigated the  $\text{Cu}_2\text{S}$ - $\text{SnS}_2$  system in detail. The authors report the existence of three compounds,  $\text{Cu}_2\text{SnS}_3$  which melts congruently at 1133 K,  $\text{Cu}_4\text{SnS}_4$ , formed by the solid-state reaction of  $\text{Cu}_2\text{SnS}_3 + \text{Cu}_2\text{S} \Leftrightarrow \text{Cu}_4\text{SnS}_4$  at 1083 K, and  $\text{Cu}_2\text{Sn}_4\text{S}_9$  formed by the reaction  $\text{Cu}_2\text{SnS}_3 + 3\text{SnS}_2 \Leftrightarrow \text{Cu}_2\text{Sn}_4\text{S}_9$  at 943 K (closely agreeing in this regard to Ref 6). The existence of  $\text{Cu}_4\text{Sn}_3\text{S}_8$  and  $\text{CuSn}_{3.75}\text{S}_8$  compounds was not confirmed. The solid solubility based on the starting components does not exceed 2 mol.%. Polymorphous transformations of  $\text{Cu}_2\text{S}$  result in solid-state processes at 656 and 381 K.

## 2.2 HgS-SnS<sub>2</sub> System

The  $\text{HgS}$ - $\text{SnS}_2$  system is a quasi-binary section of the ternary system  $\text{Hg-Sn-S}^{[12]}$  and belongs to the eutectic type. The eutectic coordinates are 920 K and 48 mol.%  $\text{HgS}$ . The solid solution ranges of the binary compounds at 700 K are 0–2 and 99–100 mol.%  $\text{SnS}_2$ .

## 2.3 Cu<sub>2</sub>S-HgS Systems

The  $\text{Cu}_2\text{S}$ - $\text{HgS}$  system was studied in Ref 13, 14. According to Ref 13, the  $\text{Cu}_2\text{S}$ - $\text{HgS}$  system is a quasi-binary section of the ternary system  $\text{Cu-Hg-S}$  and exhibits eutectic type of interaction. The eutectic coordinates are 963 K and 58 mol.%  $\text{HgS}^{[13]}$  or 976 K and 74 mol.%  $\text{HgS}^{[14]}$

Crystallographic characteristics of binary, ternary and quaternary chalcogenides of the quasi-ternary system  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  are gathered in Table 1.

## 3 Experimental

The compounds and alloys of the studied system were synthesized from semiconductor-purity elements (Cu, Ge and S) and pre-synthesized  $\text{HgS}$ . Sulfur and mercury were further purified by vacuum distillation before use. Due to the high vapor pressure of the components, the synthesis of  $\text{HgS}$  was performed in an evacuated quartz container with thickened walls. Stoichiometric amounts of starting elements were used for the synthesis. At the first stage the ampoule was heated to 473 K at the rate of 30–40 K/h. The heating to the maximum temperature of 873 K was held at

the rate of 5–10 K/h. After annealing for 48 hours, the container with synthesized  $\text{HgS}$  was cooled to room temperature at the rate of 10–15 K/h.

The calculated amounts of starting components were loaded into quartz ampoules that were evacuated to residual pressure of  $10^{-2}$  Pa and soldered.

Based on the p-T diagrams of the starting materials, single-temperature method was selected for the synthesis of alloys. The synthesis was performed in commercial programmable furnaces. The temperature was raised at the rate of 20–30 K/h to the maximum of 1400 K, with 4 h stays at the melting points of the batch components. The alloys were then cooled at the rate of 10–20 K/h to 670 K where homogenizing annealing at was held for 500 h. Annealed alloys were quenched into 25% aqueous  $\text{NaCl}$  solution.

Differential thermal analysis utilized a Paulik–Paulik–Erdei derivatograph, with Pt/Pt-Rh thermocouple and  $\text{Al}_2\text{O}_3$  as a standard. All static parameters were stable during the experiment. X-ray phase analysis using WinCSD software package<sup>[24]</sup> was performed on diffraction patterns recorded at a DRON 4-13 diffractometer ( $\text{CuK}\alpha$ -radiation). Microstructural analysis was performed using an MMU-3 metal microscope.

### 3.1 Quasi-ternary System $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$

Phase equilibria in the quasi-ternary system  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  were studied on 152 alloys the chemical and phase composition of which is shown in Fig. 1.

### 3.2 Characteristics of Quasi-binary Boundary Systems of the Quasi-ternary System

Ambiguous data regarding the melting point and coordinates of the eutectic point led to reinvestigation of the phase equilibria in the  $\text{Cu}_2\text{S}$ - $\text{HgS}$  system.

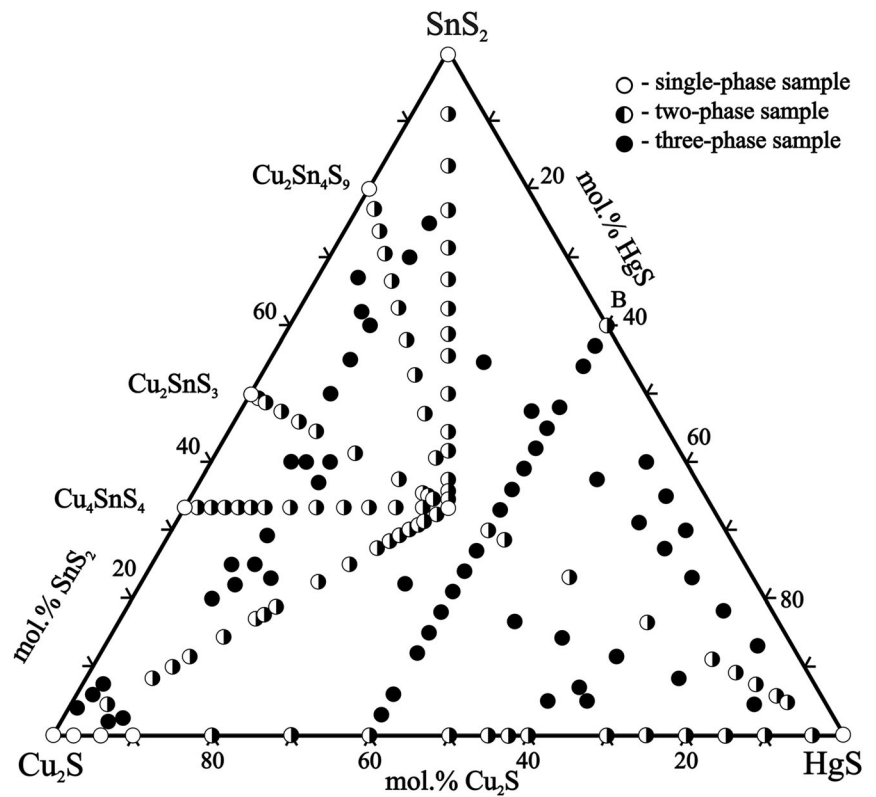
The phase diagram of this system in the entire concentration range is shown in Fig. 2. The  $\text{Cu}_2\text{S}$ - $\text{HgS}$  system is a quasi-binary section of the ternary system  $\text{Cu-Hg-S}$ . The eutectic of the section components has the coordinates of 59 mol.%  $\text{HgS}$  ( $\delta'$ ) and 983 K. The solid solution range of HT-modification of  $\text{Cu}_2\text{S}$  ( $\gamma''$ ) extends to 52 mol.%  $\text{HgS}$  at the eutectic temperature and decreases with decreasing temperature.

The presence of three polymorphous modifications of  $\text{Cu}_2\text{S}$  and one polymorphous transition of  $\text{HgS}$  determines the complex nature of phase formation in the sub-solidus part of the diagram where there are two eutectoid ( $\delta' \Leftrightarrow \gamma'' + \delta$  at 587 K and  $\gamma'' \Leftrightarrow \gamma' + \delta$  at 524 K) and one peritectoid ( $\gamma' + \delta \Leftrightarrow \gamma$  at 386 K) processes. Literature data on the investigation of the  $\text{Cu}_2\text{S}$ - $\text{SnS}_2$  and  $\text{HgS}$ - $\text{SnS}_2$  systems were used in the construction of the liquidus

**Table 1.** Crystallographic parameters of the compounds

Compound	SG	Lattice parameters, nm	References
$\gamma$ -Cu <sub>2</sub> S	<i>P2<sub>1</sub>/c</i>	$a = 1.5246, b = 1.1884, c = 1.3494, \beta = 116.35^\circ$	15
$\gamma'$ -Cu <sub>2</sub> S*	<i>P6<sub>3</sub>/mmc</i>	$a = 0.395, c = 0.675$	15
$\gamma''$ -Cu <sub>2</sub> S	<i>Fm<math>\bar{3}m</math></i>	$a = 0.545$	16
$\delta$ -HgS	<i>P3221</i>	$a = 0.4074, c = 0.9395$	17
$\delta'$ -HgS*	<i>F<math>\bar{4}3m</math></i>	$a = 0.58514$	18
SnS <sub>2</sub>	<i>P<math>\bar{3}m1</math></i>	$a = 0.3646, c = 0.5869$	19
Cu <sub>4</sub> SnS <sub>4</sub>	<i>Pnma</i>	$a = 1.3558, b = 0.7681, c = 0.6412$	20
Cu <sub>2</sub> SnS <sub>3</sub>	<i>I<math>\bar{4}2m</math></i>	$a = 0.5413, c = 1.0824$	21
Cu <sub>2</sub> SnS <sub>3</sub>	<i>Cc</i>	$a = 0.6653, b = 1.1537, c = 0.6665, \beta = 109.39^\circ$	22
Cu <sub>2</sub> Sn <sub>4</sub> S <sub>9</sub>	<i>F4<sub>1</sub>32</i>	$a = 0.1040$	6
Cu <sub>2</sub> HgSnS <sub>4</sub>	<i>I<math>\bar{4}2m</math></i>	$a = 0.5555, c = 1.0911$	23

**Fig. 1.** Chemical and phase compositions of the Cu<sub>2</sub>S-HgS-SnS<sub>2</sub> system alloys at 670 K



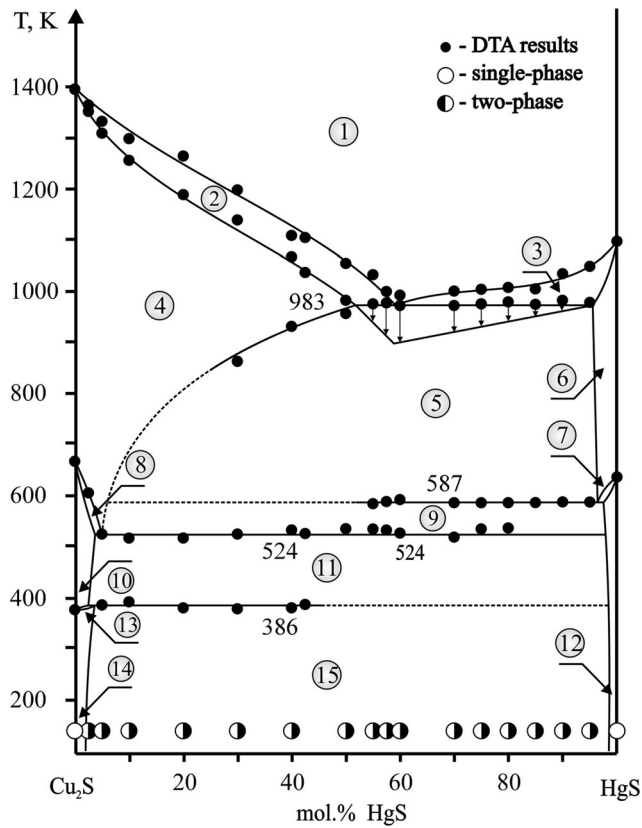
surface projection and isothermal section of the quasi-ternary system Cu<sub>2</sub>S-HgS-SnS<sub>2</sub> at 670 K.

### 3.3 Quasi-binary System Cu<sub>2</sub>S-Cu<sub>2</sub>HgSnS<sub>4</sub>

The Cu<sub>2</sub>S-Cu<sub>2</sub>HgSnS<sub>4</sub> section shown in Fig. 3 is a quasi-binary section of the quasi-ternary subsystem Cu<sub>2</sub>SnS<sub>3</sub>-HgS-Cu<sub>2</sub>S and belongs to the eutectic type. The eutectic

process  $L \rightleftharpoons \text{Cu}_2\text{HgSnS}_4 + \gamma''$  takes place at 1060 K, and the eutectic point has composition of 73 mol.% Cu<sub>2</sub>S.

The solid solubility in HT-Cu<sub>2</sub>S modification ( $\gamma''$ -solid solutions) at 1060 K does not exceed 18 mol.% Cu<sub>2</sub>HgSnS<sub>4</sub> and decreases with decreasing temperature. At the annealing temperature, the solid solubility of Cu<sub>2</sub>HgSnS<sub>4</sub> in  $\gamma''$  does not exceed 3 mol.% Cu<sub>2</sub>HgSnS<sub>4</sub>. The solid solubility based on Cu<sub>2</sub>HgSnS<sub>4</sub> is less than 2 mol.% Cu<sub>2</sub>S.



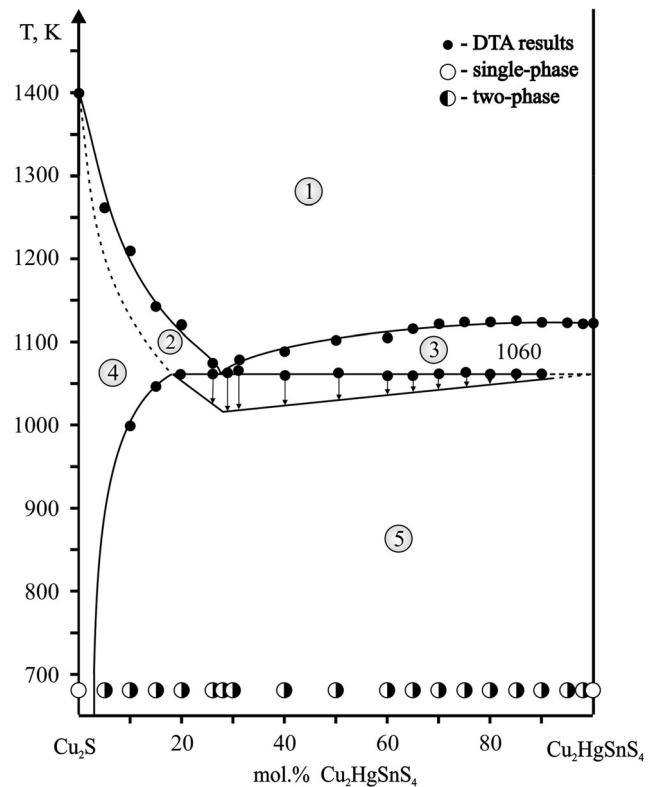
**Fig. 2.** Phase diagram of the  $\text{Cu}_2\text{S}$ - $\text{HgS}$  system: 1 - L, 2 -  $L + \gamma''$ , 3 -  $L + \delta'$ , 4 -  $\gamma''$ , 5 -  $\gamma'' + \delta'$ , 6 -  $\delta'$ , 7 -  $\delta + \delta'$ , 8 -  $\gamma'' + \gamma'$ , 9 -  $\gamma'' + \delta$ , 10 -  $\gamma'$ , 11 -  $\gamma' + \delta$ , 12 -  $\delta$ , 13 -  $\gamma' + \gamma$ , 14 -  $\gamma$ , 15 -  $\gamma + \delta$

### 3.4 Quasi-binary System $\text{Cu}_2\text{SnS}_3$ - $\text{HgS}$

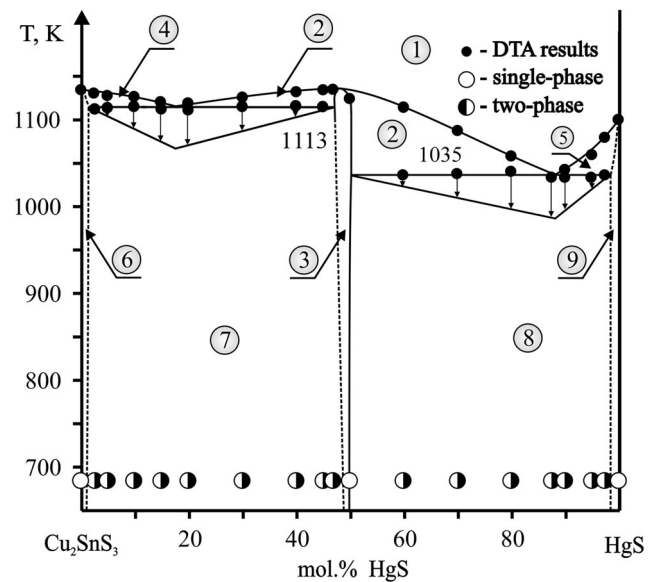
Phase diagram of the  $\text{Cu}_2\text{SnS}_3$ - $\text{HgS}$  section plotted from the results of physico-chemical analysis is shown in Fig. 4. The system is a quasi-binary section of the quasi-ternary system  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$ . The  $\text{Cu}_2\text{HgSnS}_4$  ( $\epsilon$ ) compound which melts congruently at 1122 K is formed in the system at the 1:1 ratio of the section components. The maximum melting point of the quaternary compound is shifted towards the ternary phase  $\text{Cu}_2\text{SnS}_3$  ( $\chi$ ).

The diffraction pattern of  $\text{Cu}_2\text{HgSnS}_4$  was indexed well in the tetragonal symmetry (stannite structural type, SG  $I\bar{4}2m$ ) with unit cell parameters  $a = 0.5580(2)$  nm:  $c = 1.0895(3)$  nm. The ternary compound  $\text{Cu}_2\text{SnS}_3$  crystallizes in the sphalerite structure (SG,  $a = 0.54276(2)$  nm).

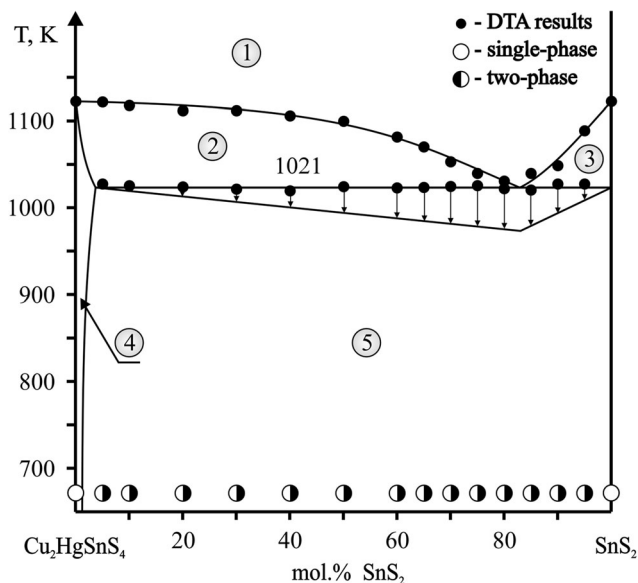
The interaction of  $\text{Cu}_2\text{HgSnS}_4$  with the section components is eutectic. The eutectics melt at 1113 K and 1035 K and have the composition of 18 and 88 mol.%  $\text{HgS}$ , respectively. The solid solubility in the section components at the annealing temperature is less than 2 mol.%.



**Fig. 3.** Phase diagram of the  $\text{Cu}_2\text{S}$ - $\text{Cu}_2\text{HgSnS}_4$  system: 1 - L, 2 -  $L + \gamma''$ , 3 -  $L + \text{Cu}_2\text{HgSnS}_4$ , 4 -  $\gamma''$ , 5 -  $\gamma'' + \text{Cu}_2\text{HgSnS}_4$



**Fig. 4.** Phase diagram of the  $\text{Cu}_2\text{SnS}_3$ - $\text{HgS}$  system: 1 - L, 2 -  $L + \epsilon$ , 3 -  $\epsilon$ , 4 -  $L + \chi$ , 5 -  $L + \delta'$ , 6 -  $\chi$ , 7 -  $\chi + \epsilon$ , 8 -  $\epsilon + \delta'$ , 9 -  $\delta'$



**Fig. 5.** Phase diagram of the  $\text{Cu}_2\text{HgSnS}_4$ - $\text{SnS}_2$  system: 1 - L 2 - L +  $\epsilon$ , 3 - L +  $\text{SnS}_2$ , 4 -  $\epsilon$ , 5 -  $\epsilon$  +  $\text{SnS}_2$

### 3.5 Quasi-binary System $\text{Cu}_2\text{HgSnS}_4$ - $\text{SnS}_2$

Phase diagram of the  $\text{Cu}_2\text{HgSnS}_4$ - $\text{SnS}_2$  section based on the results of DTA, XRD and microstructure analysis is shown in Fig. 5. The section is quasi-binary, with the eutectic nature of interaction. The eutectic reaction  $L \rightleftharpoons \epsilon + \text{SnS}_2$  takes place at 1021 K, the composition of the eutectic point is 83 mol.%  $\text{SnS}_2$ . The solid solubility based on the section components is negligible.

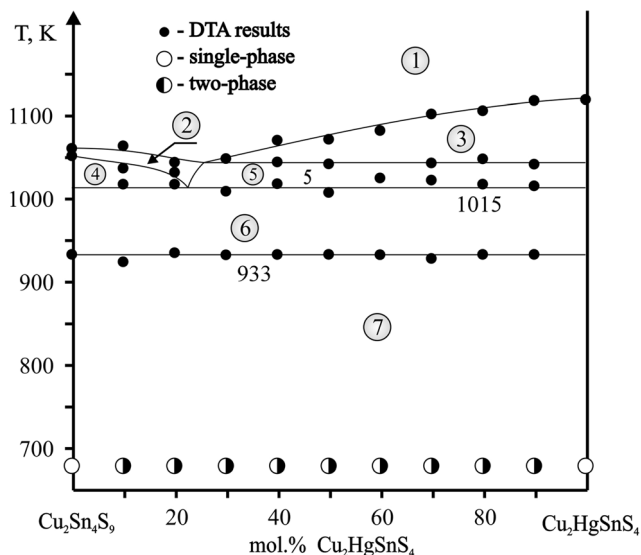
### 3.6 Vertical Section $\text{Cu}_2\text{Sn}_4\text{S}_9$ - $\text{Cu}_2\text{HgSnS}_4$

The section liquidus consists of two curves of the primary crystallization of the ternary  $\text{Cu}_2\text{SnS}_3$  and quaternary  $\text{Cu}_2\text{HgSnS}_4$  compounds (Fig. 6). The secondary crystallization is represented by the binary eutectics  $\text{Cu}_2\text{SnS}_3 + \text{SnS}_2$  (field 4) and  $\text{Cu}_2\text{HgSnS}_4 + \text{Cu}_2\text{SnS}_3$  (field 5).

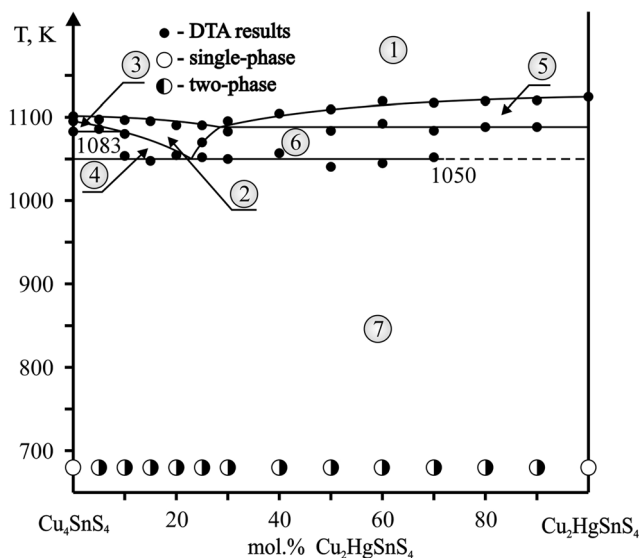
The horizontal line at 1015 K corresponds to the ternary invariant eutectic process  $L \rightleftharpoons \text{SnS}_2 + \text{Cu}_2\text{SnS}_3 + \epsilon$  which has at this section an excess of  $\text{SnS}_2$  and  $\text{Cu}_2\text{SnS}_3$ . The solid-state process  $\text{SnS}_2 + \text{Cu}_2\text{SnS}_3 \rightleftharpoons \text{Cu}_2\text{Sn}_4\text{S}_9$  at 933 K results in all alloys of the section becoming two-phase at the annealing temperature 670 K except end components of the section  $\text{Cu}_2\text{Sn}_4\text{S}_9$  and  $\text{Cu}_2\text{HgSnS}_4$ .

### 3.7 Vertical Section $\text{Cu}_4\text{SnS}_4$ - $\text{Cu}_2\text{HgSnS}_4$

The liquidus of the  $\text{Cu}_4\text{SnS}_4$ - $\text{Cu}_2\text{HgSnS}_4$  section consists of two lines of the primary crystallization of the ternary  $\text{Cu}_2\text{SnS}_3$  and quaternary  $\text{Cu}_2\text{HgSnS}_4$  phases (Fig. 7). The horizontal line at 1083 K corresponds to the four-phase peritectic process  $L + \text{Cu}_2\text{SnS}_3 + \gamma'' \rightleftharpoons \text{Cu}_4\text{SnS}_4$ .



**Fig. 6.** Vertical section  $\text{Cu}_2\text{Sn}_4\text{S}_9$ - $\text{Cu}_2\text{HgSnS}_4$ : 1 - L, 2 - L +  $\text{Cu}_2\text{SnS}_3$ , 3 - L +  $\text{Cu}_2\text{HgSnS}_4$ , 4 - L +  $\text{SnS}_2 + \text{Cu}_2\text{SnS}_3$ , 5 - L +  $\text{Cu}_2\text{HgSnS}_4 + \text{SnS}_2$ , 6 -  $\text{Cu}_2\text{SnS}_3 + \text{SnS}_2 + \text{Cu}_2\text{HgSnS}_4$ , 7 -  $\text{Cu}_2\text{Sn}_4\text{S}_9 + \text{Cu}_2\text{HgSnS}_4$

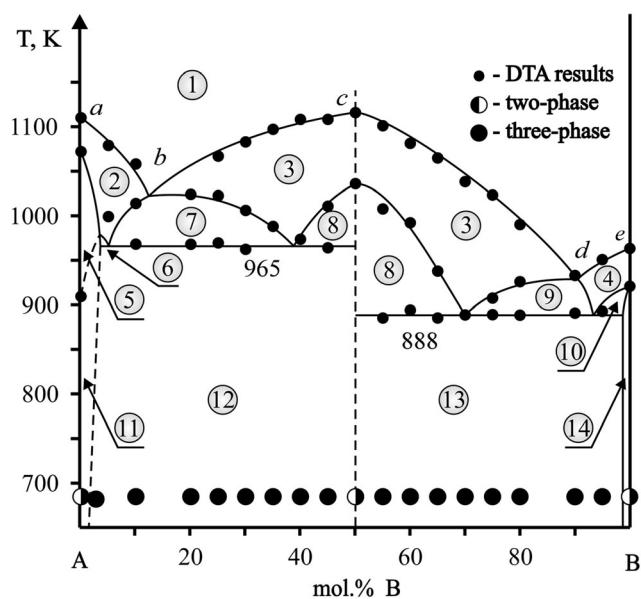


**Fig. 7.** Vertical section  $\text{Cu}_4\text{SnS}_4$ - $\text{Cu}_2\text{HgSnS}_4$ : 1 - L, 2 - L +  $\text{Cu}_2\text{SnS}_3$ , 3 - L +  $\gamma'' + \text{Cu}_2\text{SnS}_3$ , 4 - L +  $\text{Cu}_4\text{SnS}_4 + \alpha$ , 5 - L +  $\epsilon$ , 6 -  $\epsilon + \alpha$ , 7 -  $\text{Cu}_4\text{SnS}_4 + \epsilon$

### 3.8 Vertical Section A-B (A—60 mol.% $\text{Cu}_2\text{S}$ ; 40 mol.% HgS; B—60 mol.% $\text{SnS}_2$ ; 40 mol.% HgS)

The A-B section (Fig. 8) crosses two subsystems,  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{Cu}_2\text{HgSnS}_4$  and  $\text{HgS}$ - $\text{SnS}_2$ - $\text{Cu}_2\text{HgSnS}_4$ . The section liquidus consists of three lines of the primary





**Fig. 8.** Vertical section A–B: (A—60 mol.% Cu<sub>2</sub>S; 40 mol.% HgS; B—60 mol.% SnS<sub>2</sub>; 40 mol.% HgS): 1 – L, 2 – L +  $\gamma''$ , 3 – L + Cu<sub>2</sub>HgSnS<sub>4</sub>, 4 – L + SnS<sub>2</sub>, 5 –  $\gamma''$ , 6 – L +  $\gamma''$  +  $\delta'$ , 7 – L +  $\gamma''$  + Cu<sub>2</sub>HgSnS<sub>4</sub>, 8 – L + Cu<sub>2</sub>HgSnS<sub>4</sub> +  $\delta'$ , 9 – L + SnS<sub>2</sub> + Cu<sub>2</sub>HgSnS<sub>4</sub>, 10 – L + SnS<sub>2</sub> +  $\delta'$ , 11 –  $\gamma''$  +  $\delta'$ , 12 –  $\gamma''$  + Cu<sub>2</sub>HgSnS<sub>4</sub> +  $\delta'$ , 13 – Cu<sub>2</sub>HgSnS<sub>4</sub> + SnS<sub>2</sub> +  $\delta'$ , 14 – SnS<sub>2</sub>

crystallization of  $\gamma''$ -solid solution range of HT-Cu<sub>2</sub>S modification (part a–b), Cu<sub>2</sub>HgSnS<sub>4</sub> (part b–d), and SnS<sub>2</sub> (part d–e).

The section solidus is formed by the boundary compositions of  $\gamma''$ - and  $\delta'$ -solid solutions above the temperature of invariant processes and by the horizontal lines at 965 K and 888 K which belong to the eutectic processes  $L \Leftrightarrow \text{Cu}_2\text{HgSnS}_4 + \gamma'' + \delta'$  and  $L \Leftrightarrow \text{Cu}_2\text{HgSnS}_4 + \text{SnS}_2 + \delta'$ .

The space between the liquidus and solidus lines, along with the fields of the primary crystallization volumes, contains the fields of the secondary crystallization  $L \Leftrightarrow \gamma'' + \text{Cu}_2\text{HgSnS}_4$ ,  $L \Leftrightarrow \text{Cu}_2\text{HgSnS}_4 + \text{SnS}_2$ , and  $L \Leftrightarrow \text{Cu}_2\text{HgSnS}_4 + \delta'$ . Of all investigated alloys, three alloys with the content of 0, 50 and 100 mol.% B are two-phase in the subsolidus region; the remaining alloys contain three phases.

### 3.9 Liquidus Surface Projection of the Quasi-ternary System Cu<sub>2</sub>S-HgS-SnS<sub>2</sub>

Liquidus surface projection of the Cu<sub>2</sub>S-HgS-SnS<sub>2</sub> system on the concentration triangle was plotted from the results presented above (Fig. 9). The liquidus consists of six fields of the primary crystallization of Cu<sub>2</sub>S ( $\gamma''$ -solid solutions), HgS ( $\delta'$ -solid solutions), SnS<sub>2</sub>, Cu<sub>2</sub>SnS<sub>3</sub>, Cu<sub>4</sub>SnS<sub>4</sub>, and

Cu<sub>2</sub>HgSnS<sub>4</sub>. They are separated by fourteen monovariant lines and fourteen invariant points, of which eight correspond to binary and six to ternary invariant processes. The nature and temperature of invariant processes are gathered in Table 2.

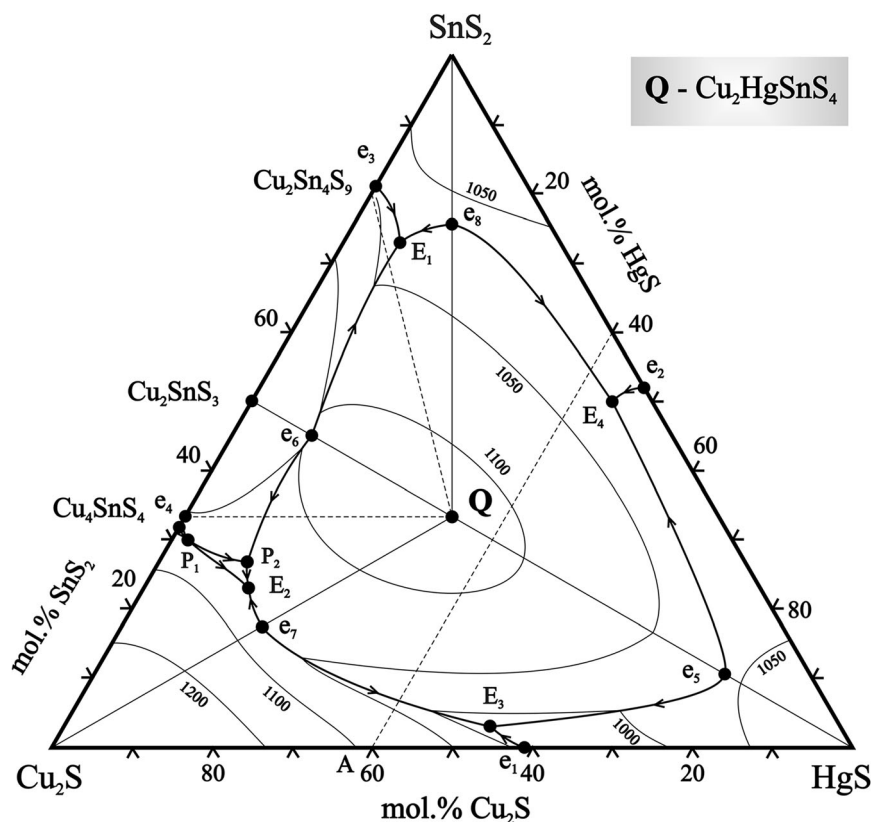
The Cu<sub>2</sub>S-HgS-SnS<sub>2</sub> system is divided by the quasi-binary sections Cu<sub>2</sub>SnS<sub>3</sub>-HgS, Cu<sub>2</sub>HgSnS<sub>4</sub>-Cu<sub>2</sub>S and Cu<sub>2</sub>-HgSnS<sub>4</sub>-SnS<sub>2</sub> into four subsystems. The sub-systems Cu<sub>2</sub>S-HgS-Cu<sub>2</sub>HgSnS<sub>4</sub>, HgS-SnS<sub>2</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub> and SnS<sub>2</sub>-Cu<sub>2</sub>-SnS<sub>3</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub> are of the eutectic type.

The crystallization of alloys in the Cu<sub>2</sub>S-Cu<sub>2</sub>HgSnS<sub>4</sub>-Cu<sub>2</sub>SnS<sub>3</sub> system is more complex, due to the solid-state process of the formation of the ternary compound Cu<sub>4</sub>SnS<sub>4</sub> ( $\gamma'' + \text{Cu}_2\text{SnS}_3 \Leftrightarrow \text{Cu}_4\text{SnS}_4$ ) in the boundary system Cu<sub>2</sub>S-SnS<sub>2</sub> at 1083 K. This is higher than the temperature of the eutectic process in the Cu<sub>2</sub>S-Cu<sub>2</sub>HgSnS<sub>4</sub> system (1060 K). Therefore, the ternary compound Cu<sub>4</sub>SnS<sub>4</sub> has its own field of the primary crystallization on the liquidus surface, caused by the peritectic process  $L + \text{Cu}_2\text{-SnS}_3 + \gamma'' \Leftrightarrow \text{Cu}_4\text{SnS}_4$  which takes place at 1083 K.

### 3.10 Isothermal Section of the Quasi-ternary System Cu<sub>2</sub>S-HgS-SnS<sub>2</sub> at 670 K

Isothermal section of the quasi-ternary system Cu<sub>2</sub>S-HgS-SnS<sub>2</sub> at 670 K was plotted based on obtained results (Fig. 10). The quasi-binary systems Cu<sub>2</sub>SnS<sub>3</sub>-HgS, Cu<sub>2</sub>-HgSnS<sub>4</sub>-SnS<sub>2</sub>, Cu<sub>2</sub>S-Cu<sub>2</sub>HgSnS<sub>4</sub>, and the Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub>-Cu<sub>2</sub>-HgSnS<sub>4</sub> and Cu<sub>4</sub>SnS<sub>4</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub> sections which are quasi-binary in the sub-solidus part, separate the quasi-ternary system Cu<sub>2</sub>S-SnS<sub>2</sub>-HgS at 670 K into six subsystems. The quaternary compound Cu<sub>2</sub>HgSnS<sub>4</sub> at the annealing temperature is in equilibrium with the components of the quasi-ternary system Cu<sub>2</sub>S, HgS and SnS<sub>2</sub>, as well as the ternary phases Cu<sub>4</sub>SnS<sub>4</sub> and Cu<sub>2</sub>SnS<sub>3</sub>. The  $\gamma''$ -solid solution range of HT-Cu<sub>2</sub>S modification is stretched at 670 K along the Cu<sub>2</sub>S-HgS side. The solid solubility in Cu<sub>2</sub>HgSnS<sub>4</sub>, Cu<sub>4</sub>SnS<sub>4</sub>, Cu<sub>2</sub>SnS<sub>3</sub>, Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub>, SnS<sub>2</sub>, and HgS is negligible and does not exceed 2-3 mol.% at 670 K. Solid-state processes involving the Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub> compound should be noted in the Cu<sub>2</sub>SnS<sub>3</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub>-SnS<sub>2</sub> subsystem. All alloys of this subsystem complete their crystallization in the ternary eutectic process  $L \Leftrightarrow \text{SnS}_2 + \text{Cu}_2\text{SnS}_3 + \text{Cu}_2\text{HgSnS}_4$  at 1015 K. The quasi-binary section Cu<sub>2</sub>S-SnS<sub>2</sub> features at 933 K the peritectoid process of the formation of the ternary phase Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub> ( $\text{Cu}_2\text{SnS}_3 + \text{SnS}_2 \Leftrightarrow \text{Cu}_2\text{Sn}_4\text{S}_9$ ) which is stable at 670 K. This process takes also place in all alloys of the Cu<sub>2</sub>SnS<sub>3</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub>-SnS<sub>2</sub> subsystem. The process ends with an excess of the ternary compound Cu<sub>2</sub>SnS<sub>3</sub> in

**Fig. 9.** Liquidus surface projection of the quasi-ternary system Cu<sub>2</sub>S-HgS-SnS<sub>2</sub>



**Table 2.** Character and temperature of invariant processes and coordinates of invariant points of the quasi-ternary system Cu<sub>2</sub>S-HgS-SnS<sub>2</sub>

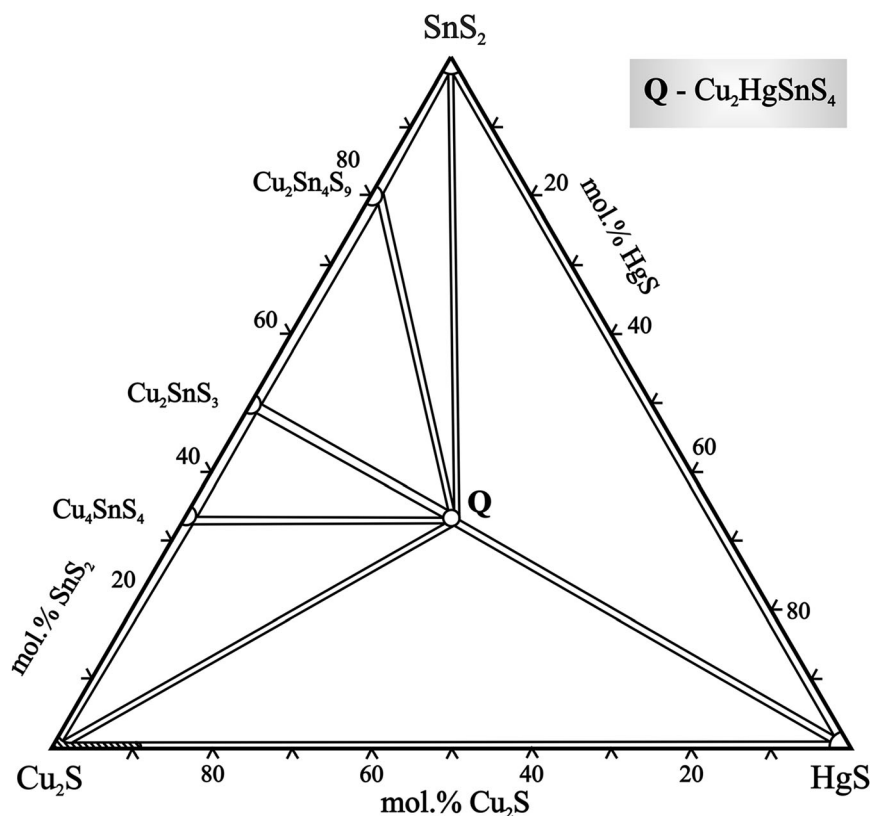
Invariant point	Process	T, K	Composition, mol.%		
			Cu <sub>2</sub> S	HgS	SnS <sub>2</sub>
e <sub>1</sub>	L ⇌ γ'' + δ'	983	41	59	...
e <sub>2</sub>	L ⇌ SnS <sub>2</sub> + δ'	920	...	48	52
e <sub>3</sub>	L ⇌ SnS <sub>2</sub> + Cu <sub>2</sub> SnS <sub>3</sub>	1061	19	...	81
e <sub>4</sub>	L ⇌ γ'' + Cu <sub>2</sub> SnS <sub>3</sub>	1093	68	...	32
e <sub>5</sub>	L ⇌ Cu <sub>2</sub> HgSnS <sub>4</sub> + δ'	1035	11	78	11
e <sub>6</sub>	L ⇌ Cu <sub>2</sub> SnS <sub>3</sub> + Cu <sub>2</sub> HgSnS <sub>4</sub>	1113	45	10	45
e <sub>7</sub>	L ⇌ Cu <sub>2</sub> HgSnS <sub>4</sub> + γ''	1060	64	18	18
e <sub>8</sub>	L ⇌ SnS <sub>2</sub> + Cu <sub>2</sub> HgSnS <sub>4</sub>	1021	13	13	74
E <sub>1</sub>	L ⇌ Cu <sub>2</sub> SnS <sub>3</sub> + SnS <sub>2</sub> + Cu <sub>2</sub> HgSnS <sub>4</sub>	1015	20	7	73
E <sub>2</sub>	L ⇌ γ'' + Cu <sub>2</sub> HgSnS <sub>4</sub> + Cu <sub>4</sub> SnS <sub>4</sub>	1045	64	13	23
E <sub>3</sub>	L ⇌ γ'' + Cu <sub>2</sub> HgSnS <sub>4</sub> + δ'	965	44	53	3
E <sub>4</sub>	L ⇌ SnS <sub>2</sub> + Cu <sub>2</sub> HgSnS <sub>4</sub> + δ'	888	5	45	50
P <sub>1</sub>	L + Cu <sub>2</sub> SnS <sub>3</sub> + γ'' ⇌ Cu <sub>4</sub> SnS <sub>4</sub>	1083	68	2	30
P <sub>2</sub>	L + Cu <sub>2</sub> SnS <sub>3</sub> ⇌ Cu <sub>4</sub> SnS <sub>4</sub> + Cu <sub>2</sub> HgSnS <sub>4</sub>	1050	62	11	27

the Cu<sub>2</sub>SnS<sub>3</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub>-Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub> part, with an excess of the binary compound SnS<sub>2</sub> in the Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub>-SnS<sub>2</sub> part, and only at the Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub> section the process is completed stoichiometrically. The above solid-state processes lead to the emergence of the binary equilibrium Cu<sub>2</sub>HgSnS<sub>4</sub>-Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub> at the isothermal section.

### 4 Conclusions and Future Work

A total of 152 alloys were investigated by DTA, x-ray diffraction and MCA methods in the quasi-ternary system Cu<sub>2</sub>S-HgS-SnS<sub>2</sub>. Phase diagrams of the quasi-binary system Cu<sub>2</sub>S-HgS, six vertical sections HgS-Cu<sub>2</sub>SnS<sub>3</sub>, Cu<sub>2</sub>HgSnS<sub>4</sub>-SnS<sub>2</sub>, Cu<sub>2</sub>S-Cu<sub>2</sub>HgSnS<sub>4</sub>, Cu<sub>2</sub>Sn<sub>4</sub>S<sub>9</sub>-Cu<sub>2</sub>HgSnS<sub>4</sub>,

**Fig. 10.** Isothermal section of the quasi-ternary system  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  at 670 K



$\text{Cu}_4\text{SnS}_4$ - $\text{Cu}_2\text{HgSnS}_4$ , A-B (A—40 mol.%  $\text{HgS}$ , 60 mol.%  $\text{Cu}_2\text{S}$ ; B—40 mol.%  $\text{HgS}$ , 60 mol.%  $\text{SnS}_2$ ), liquidus surface projection onto the concentration triangle and isothermal section of the quasi-ternary system  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  at 670 K were investigated. The sections  $\text{Cu}_2\text{HgSnS}_4$ - $\text{SnS}_2$  and  $\text{Cu}_2\text{S}$ - $\text{Cu}_2\text{HgSnS}_4$  are quasi-binary systems of eutectic type with eutectic points coordinates 1021 K, 17 mol.%  $\text{Cu}_2\text{HgSnS}_4$  and 1060 K, 27 mol.%  $\text{Cu}_2\text{HgSnS}_4$ , respectively. The existence of the quaternary compound  $\text{Cu}_2\text{HgSnS}_4$  which melts congruently at 1122 K was found in the  $\text{HgS}$ - $\text{Cu}_2\text{SnS}_3$  system at the component ratio 1:1. The interaction of  $\text{Cu}_2\text{HgSnS}_4$  with the section components is eutectic. The eutectics melt at 1113 K and 1035 K, eutectic points have composition of 18 and 88 mol.%  $\text{HgS}$ , respectively. The sections  $\text{Cu}_2\text{Sn}_4\text{S}_9$ - $\text{Cu}_2\text{HgSnS}_4$  and  $\text{Cu}_4\text{SnS}_4$ - $\text{Cu}_2\text{HgSnS}_4$  are quasi-binary only in the sub-solidus part due to the solid-state formation of ternary compounds. The  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  system is triangulated by quasi-binary sections into four subsystems. The coordinates of invariant points and positions of monovariant lines were established.

Presented results of the study of phase equilibria in the  $\text{Cu}_2\text{S}$ - $\text{HgS}$ - $\text{SnS}_2$  system expand the database in the field of semiconductor materials science. Obtained results can be used to predict phase equilibria in analogous systems and in the development of technology for obtaining ternary and

quaternary chalcogenides in the single-crystalline or polycrystalline state.

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