

Experimental Liquidus Studies of the CaO-ZnO-Fe₂O₃ System in Air

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Abstract Phase equilibria in the CaO-ZnO-Fe₂O₃ system have been investigated at 1483-1673 K (1210-1400 °C) for oxide liquid in equilibrium with air and solid oxide phases: (a) zincite $(Zn,Fe,Ca)O_{1+x}$; (b) spinel $(Zn,Fe,Ca)Fe₂O₄$; (c) lime (Ca,Zn)O; (d) calcium ferrites dissolving zinc oxide: brownmillerite $Ca_2(Fe,Zn)_2O_{5-x}$, and calcium diferrite $(Ca,Zn)Fe₄O₇$. High-temperature equilibration on inert metal (platinum) substrates, followed by quenching and direct measurement of the Ca, Zn and Fe concentrations in the phases with the electron probe x-ray microanalysis (EPMA) has been used to accurately characterize the system in equilibrium with air. All results are projected onto the CaO-ZnO-"FeO_{1.5}" plane for presentation purposes. The present paper presents systematic characterization of liquidus over a wide range of compositions in this system in equilibrium with air.

Keywords calcium · iron · phase diagrams · slags · zinc

1 Introduction

The present experimental studies of the gas–slag–solid oxide phase equilibria in the CaO-ZnO-Fe₂O₃ "low-order" system is an important part of an integrated thermodynamic modeling and experimental research program for the Pb-Zn-Fe-Cu-Ca-Si-Al-Mg-O multicomponent system, important for the lead smelting and recycling.

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Only one study of the subsolidus phase relations in this system has been found in the literature.^{[\[1](#page-6-0)]} There are no previous studies of the liquidus in this system found in literature; this fact is likely to be related to the difficulties of preventing crystallisation of the liquid phase on quenching these highly fluid, silica-free slags.

In the present study experiments were focussed on a composition range having low liquidus temperature that is found to be located in the central part of the CaO-ZnO-FeO_{1.5} triangle: zincite (ZnO dissolving Fe₂O₃, FeO and CaO), spinel $(Zn,Fe,Ca)Fe₂O_{4+v}$, lime (CaO dissolving ZnO), brownmillerite $(Ca_2Fe_2O_5$ dissolving ZnO), and calcium diferrite ($CaFe₄O₇$ dissolving ZnO) primary phase fields at 1483-1673 K (1210-1400 °C).

2 Experimental Technique and Procedure

The experimental procedure and apparatus have been described in detail in previous publications by $PYROSEARCH.^[2-4] Initial mixtures were made by mixing$ high-purity powders of Fe₂O₃ (99.945 wt.% purity), ZnO (99.8 wt.% purity), CaCO₃ (99.9-99.99 wt.% purity), supplied by Alfa Aesar, MA, USA. Envelopes made of platinum foil $(> 99.9\%$ purity, 0.05 mm thickness, provided by Johnson Matthew, Australia) were used for equilibration of slags.

The technique of equilibration experiments and parameters of electron probe x-ray microanalysis (JEOL 8200L EPMA; Japan Electron Optics Ltd., Tokyo, Japan) were similar to.^{[[2\]](#page-6-0)} The sample was suspended in the hot zone of the furnace by Kanthal support wire (0.7 or 1-mm diameter). Samples were pre-melted for 10-45 min (see Table [1\)](#page-1-0) at 20-130 K above the equilibration temperature, to form a homogeneous slag. This was followed by equilibration at

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Table 1 continued

Substrate for all samples was Pt foil

*High-Fe zincite; otherwise—low-Fe zincite

the final target temperature for the required time (1-20 h, see Table [1](#page-1-0)), to allow solid phases to crystallize from the melts.

At the end of the equilibration process, the sample was rapidly quenched in iced calcium chloride brine $(< 253 \text{ K})$ $(-20 \degree C)$). The specimen was then washed thoroughly in water and ethanol before being dried on a hot plate, mounted in epoxy resin, and then cross-sections were prepared using conventional metallographic polishing techniques.

Hematite (Fe₂O₃), wollastonite (CaSiO₃) (supplied by Charles M. Taylor Co., Stanford, CA, USA), and zincite (ZnO, sintered from powder) standards were used for calibration of EPMA. The ratios of the different oxidation states of iron cations were not measured with EPMA, and the iron oxide concentrations were recalculated as $FeO_{1.5}$ for presentation purposes only. Stoichiometric calcium ferrites $Ca₂Fe₂O₅$, $CaFe₂O₄$ and $CaFe₄O₇$ were prepared to test the JEOL ZAF correction in the Ca-Fe-O system. Systematic overestimation of CaO concentration was found after application of the standard JEOL ZAF correction for all compounds: apparent CaO concentrations were

50.6 \pm 0.2 mol.% in Ca₂Fe₂O₅, 33.9 \pm 0.3 mol.% in CaFe₂O₄, and 20.5 \pm 0.3 mol.% for CaFe₄O₇. Later study by Cheng et al.^{[\[5](#page-6-0)]} confirms these values for $Ca_2Fe_2O_5$. Similar to procedures described previously by the authors, $[6, 7]$ $[6, 7]$ $[6, 7]$ $[6, 7]$ $[6, 7]$ an additional correction polynomial has been developed to adjust the CaO concentrations to stoichiometric (50, 33.33, and 20 mol.%, respectively) and applied to all measurements:

$$
x(CaO)^{corr} = x(CaO) - x(CaO) \cdot x(FeO_{1.5}) \cdot (0.0208 + 0.0119(x(FeO_{1.5}) - x(CaO)))
$$
(Eq 1)

where x is molar fraction of cation.

No reference stoichiometric compounds are available in the Ca-Zn-O and Zn-Fe-O systems, so the correction is extended into ternary in a simplified way:

$$
x(FeO_{1.5})^{corr} = x(FeO_{1.5}) \cdot (1 - x(CaO)^{corr})/(1 - x(CaO))
$$
\n
$$
- x(CaO))
$$
\n(Eq 2)

$$
x(\text{ZnO})^{\text{corr}} = x(\text{ZnO}) \cdot (1 - x(\text{CaO})^{\text{corr}}) / (1 - x(\text{CaO})) \tag{Eq 3}
$$

In studies of several ZnO- and $Fe₂O₃$ -containing systems, $\left[2,8-10\right]$ it was found that a significant fraction of apparent solubility of ZnO and $Fe₂O₃$ in other solid phases (e.g. tridymite $SiO₂$) was not a real solubility but an effect of secondary fluorescence. According to the current hypothesis of the authors, derived from the review by Llovet et al.^{[[11](#page-6-0)]} bremsstrahlung (continuum) x-rays from electrons decelerating in particles can excite Zn or Fe atoms in the surrounding ZnO- or $Fe₂O₃$ -containing matrix (at least several hundreds of microns around), and then those could emit characteristic radiation. To resolve this issue, several experiments for unreacted small particles pelletized in a matrix of Zn- or Fe-containing powder have been conducted, with the following results:

- Apparent 1.45 mol.% " $FeO_{1.5}$ " is measured by EPMA in pure ZnO particles (average size 50 micron) surrounded by $Fe₂O₃$;
- Apparent 1.64 mol.% "ZnO" is measured by EPMA in $Ca_2(Fe, Zn)_2O_{5-x}$ particles (average size 30 micron) surrounded by ZnO.

Similar to, $[8,9,12]$ the following correction for the secondary x-ray fluorescence therefore has been developed and applied in the present study to the compositions in the phases of CaO-ZnO-" $FeO_{1.5}$ " system measured by EPMA:

$$
x(FeO1.5 in ZnO)corr = x(FeO1.5 in ZnO)initial
$$

- 0.0145 wt. fraction (FeO_{1.5} in slag), (Eq 4)

x(ZnO in Ca₂(Fe,Zn)₂O_{5-x})^{corr}

$$
= x(ZnO in Ca2(Fe,Zn)2O5-x)initial
$$
 (Eq 5)
- 0.0164 wt. fraction (ZnO in slag),

Other calcium ferrites were only found in equilibrium with low-ZnO slag, so correction was not applied for them.

To ensure the achievement of equilibrium in the sam-ples, the four-point test approach^{[\[4,](#page-6-0) [13](#page-6-0)]} was used, including: (1) varying equilibration time; (2) confirming homogeneity of each phase; (3) approaching equilibrium from different directions (if available); (4) analyzing possible reactions that may not complete during equilibration or interfere with achievement of equilibrium. The approach used to obtain accurate, repeatable, and objective measurements by EPMA-line analysis was similar to the one described by Nikolic et al. $[14]$ $[14]$ $[14]$ in which the average composition of the liquid phase is calculated from 20 points measured in a well-quenched area within 15 microns from the surface, with the allowed limit of standard deviation $\lt 1$ wt.%. The accuracy of the EPMA measurements was estimated to be within 1 wt. %, and the typical detection limit of minor components was estimated to be about 0.01 wt.%.^{[[11\]](#page-6-0)}

3 Results and Discussion

Examples of micrographs of quenched CaO-ZnO-" $FeO_{1.5}$ " samples are given in Fig. $1(a)$ $1(a)$, (b) , (c) , (d) , (e) and (f) .

The results of experiments after correction according to Eq [1,](#page-2-0) [2](#page-2-0), and [3](#page-2-0) are reported in Table [1.](#page-1-0) The phase liquidus surface constructed based on the present results and stud-ies^{[[5,8](#page-6-0),[16,17\]](#page-6-0)} for the binary joins is given in Fig. [2\(](#page-4-0)a) and (b). Isotherms and boundaries at high temperatures are estimated with FactSage model. $\left[15\right]$ $\left[15\right]$ $\left[15\right]$ Isotherms are plotted as thin solid lines, boundaries as thick solid lines, and tielines as dashed lines. All phases observed in the system in the present study are listed in Table [2](#page-4-0).

The liquidus surface is characterized by three ternary eutectics:

- Lime + zincite + brownmillerite at ~ 1264 °C
- Zincite (high-Fe, see details below) $+$ brownmillerite + spinel at \sim 1249 °C
- Spinel + brownmillerite + calcium diferrite $(Ca,Zn)Fe₄$ O₇ at \sim 1208 °C

Calcium diferrite $(Ca,Zn)Fe₄O₇$ is expected to form through peritectic reactions:

- $Spinel + hematite = calcium$ diferrite $+ liquid$ at \sim 1284 °C (estimation subject to large uncertainty)
- Brownmillerite + CaFe₂O₄ = calcium diferrite + liquid at ~ 1214 °C.

Liquidus of calcium diferrite goes up on addition of ZnO due to dissolution of high ZnO in this solid solution phase exceeding its concentrations in slag. Unlike the data, $[1]$ $[1]$ the phase combination spinel $+$ CaFe₂O₄ was not observed in the present study, probably due to the difference in temperature.

Saddle points are predicted between zincite $+$ brownmillerite and spinel $+$ brownmillerite.

3.1 Composition of Zincite

Previous studies of solubility of iron oxides in zincite in air by Hansson et al. $\left[18\right]$ $\left[18\right]$ $\left[18\right]$ reported the predominating form to be " $FeO_{1.5}$ " rather than "FeO" from the wet chemistry analysis, and a significant increase in iron oxide solubility in zincite was observed above 1250 °C. Jak et al. $[19-22]$ measured the concentration of iron oxide in zincite in equilibrium with Pb-Zn-Fe-Si-O slag and spinel; again, there is a sharp change of solubility of " $FeO_{1.5}$ " in zincite at ~ 1260 °C from $\lt 2$ mol.% Fe/(Fe + Zn) to 10-30%. Recently, the same trend for iron oxide solubility in zincite was observed in the ZnO -" $FeO_{1.5}$ "-Si $O₂$ ^{[\[8\]](#page-6-0)} PbO-ZnO-"FeO_{1.5}",^{[[23](#page-6-0)]} PbO-ZnO-"FeO_{1.5}"-SiO₂ and CaO-ZnO-"FeO_{1.5}"-SiO₂ (at low CaO/SiO₂ ratios) systems^{[\[24\]](#page-6-0)} in air.

Fig. 1 Backscattered scanning electron micrographs of quenched slag in the CaO-ZnO-" $FeO_{1.5}$ " system in equilibrium with one or two crystalline phases and air, $p(O_2) = 0.21$ atm. (a) Liquid + low-Fe zincite.
(b) Liquid + high-Fe zincite. $Liquid + high-Fe$

(c) Liquid + spinel + brownmillerite $Ca₂Fe₂O₅$. (d) Liq $uid + spinel + "2CaO·3FeO_{1.5}" phase. (e) Liquid + lime + low-$ Fe zincite. (f) Liquid + lime + brownmillerite $Ca₂Fe₂O₅$

Fig. 2 Liquidus surface of the $CaO-ZnO$ -" $FeO_{1.5}$ " system in air, $p(O_2) = 0.21$ atm. All temperatures are in °C and compositions in mol.%. Isotherms and boundaries at high temperatures are estimated with FactSage
model,^{[[15\]](#page-6-0)}, experimental points (brown labels) on the binary joins are from Ref [5,](#page-6-0) [8](#page-6-0), [16](#page-6-0), and [17](#page-6-0). (a) Complete diagram; (b) zoomed low-ZnO part

Table 2 Composition ranges of solid primary phases at the CaO-ZnO-" $FeO_{1.5}$ " liquidus in air

Phase name	Formula	No. of points	Composition range, mol.%
Zincite low-Fe	$(Zn, Fe, Ca)O_{1+x}$	6	$<$ 3.3% CaO, $<$ 1.8% FeO ₁₅
Zincite high-Fe	$(Zn, Fe, Ca)O_{1+x}$	6	2-8.5% CaO, 5.7-27.6% FeO ₁₅
Spinel	$(Zn, Fe, Ca)Fe2O4$	9	$<$ 7.2% CaO, 11.0-29.4% ZnO
Lime	(Ca,Zn)O	5	$< 0.5\%$ FeO _{1.5} , $< 10.5\%$ ZnO
Brownmillerite	$Ca2(Fe,Zn)2O5-x$	5	$< 2.4\%$ ZnO
Calcium diferrite	(Ca,Zn)Fe ₄ O ₇	2	4.4-5.1% ZnO
? Calcium ferrite	$Ca4Fe6O13$		1.0% ZnO
Hematite	Fe ₂ O ₃	Ω	n.a.

All concentrations are in mol.% cations

Fig. 3 Solubility of "FeO_{1.5}" in zincite at subsolidus conditions in Zn-Fe-O system in air and in presence of multicomponent slag
(Ref.^[18-22], new results^{[\[8\]](#page-6-0)}), showing sharp increase at $T > 1260$ °C, enhanced by high CaO activities (present study)

This is represented as ''experimental trend'' dashed line in Fig. 3. Note that the data reported by Hansson et al. $^{[18]}$ $^{[18]}$ $^{[18]}$ from experiments in fully solid samples, are considered to overestimate the solubility of "FeO_{1.5}" in zincite due to small size of the neighbouring crystals and secondary x-ray fluorescence effect; the data with slag phase pre-sent^{[[8](#page-6-0), [19](#page-6-0)–[24](#page-6-0)]} are considered more reliable.

The public FactSage thermodynamic database^{[[25](#page-6-0)[–28\]](#page-7-0)} describes a smooth increase of "Fe $O_{1.5}$ " dissolved in zincite with increasing concentration of iron in slag, and the CaO solubility in zincite would decrease with increasing concentration of iron in slag in the CaO-ZnO-" $FeO_{1.5}$ " system. However, the present experimental results demonstrate significantly different trends. Both "FeO_{1.5}" and CaO solubility has been found to be low $\left(\langle 1.3 \text{ mol.}\% \rangle\right)$ "FeO_{1.5}" and \lt 3.3 mol.% CaO) for low-Fe slag (\lt 39 mol.% FeO_{1.5}). At higher Fe in slag, solubility of both FeO_{1.5} and CaO rapidly increases to \sim 27% and \sim 8%, respectively. Remarkably, \sim 3 times more CaO is dissolved in zincite despite less CaO in slag. The morphology of zincite changes from ''spherical'' to ''elongated''—the latter called ''High-Fe zincite''.

The transition of low-Fe zincite to high-Fe zincite is not affected by PbO or $SiO₂$, but is promoted by CaO. This corresponds to change of morphology of zincite crystals from round-shaped (Fig. [1](#page-4-0)a) to plate-like (Fig. [1](#page-4-0)b), which strongly affects the mechanical properties of zinc sinters. This feature was studied previously^{[[18](#page-6-0)]}-both types of zincite have the same crystal group (hexagonal), but different c/a ratios. It may be considered as a second order phase transition (cooperative effect of dissolved FeO_x making the structure more flexible to include more dissolved species, such as FeO_x itself and CaO). This likely second order transition has not yet been included in any

thermodynamic model—significant efforts are required to introduce a second ''High-Fe zincite'' phase with current FactSage database.

3.2 Compositions of Other Solid Phases

- 1. The mutual effect of Zn and Ca in spinel has been observed for the first time. CaO concentration reaches maximum 7 mol.% when there is 20 mol.% ZnO in spinel (in equilibrium with 30% CaO slag and brownmillerite). At higher ZnO in spinel, it competes with CaO for divalent sites. At lower ZnO in spinel, the equilibrium of spinel with such high-CaO slags is not possible anymore, since calcium diferrite and hematite phases form; therefore, CaO in spinel decreases.
- 2. The substitution of ZnO for $FeO_{1.5}$ in brownmillerite $Ca_2(Fe, Zn)_2O_{5-x}$ has been observed, up to 2.0 mol.% ZnO is dissolved. CaO concentration remains constant at 50 mol.%.
- 3. The substitution of ZnO for CaO in dicalcium ferrite $(Ca,Zn)Fe₄O₇$ has been observed, up to 5 mol.% ZnO is dissolved. $FeO_{1.5}$ concentration remains constant at 80 mol.%.
- 4. An unusual compound $2CaO·3(FeO_{1.5}, ZnO)$ or $Ca₄$. $Fe₆O₁₃$ has been observed in one sample; the zinc-free end-member $2CaO·3FeO_{1.5}$ is unknown. Further study is needed to investigate the nature of this phase.
- 5. Up to 10.5% ZnO is observed to dissolve in lime within the studied conditions; at higher temperatures, higher solubility has been reported by Xia et al.^{[\[17\]](#page-6-0)} 23 mol.% ZnO. The solubility of iron oxide in lime does not exceed 0.5 mol.%.

In summary, present experimental study has produced the first comprehensive dataset for the Ca-Zn-Fe-O system in air that is essential for the lead and zinc smelting and recycling industry, and provides valuable new data that can be used to optimize thermodynamic databases of these systems.

4 Conclusions

New phase equilibria information in the CaO-ZnO- " $FeO_{1.5}$ " system in air has been obtained. The studied range of temperatures covered 1483-1673 K (1210- 1400 \degree C), and included the equilibria of slag with one or two crystalline phases: zincite, spinel, lime, calcium ferrites [brownmillerite $Ca_2(Fe, Zn)_2O_{5-x}$, calcium diferrite $(Ca,Zn)Fe₄O₇$, etc.]. This is the first systematic study of the Ca-Zn-Fe-O system in air, as a part of the multicomponent system Pb-Zn-Fe-Cu-Si-Ca-Al-Mg-O, essential for the lead and zinc smelting and recycling industries.

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