

Effects of Vanadium Intergranular Segregation at FCC/L1₂ Interfaces in Ni-Al-V Alloys

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Abstract A study of the interfacial properties of Ni-Al-V alloys is presented further, together with the interatomic potentials of the Ni-Al-V ternary phase system given in this paper, with the application of the Phase-field method and atomistic simulations, based on the second nearest-neighbor modified embedded-atom method (2NN MEAM) potential formalism. It is discovered that the alloy elements have different preferences of segregation or depletion at the (100) FCC/L1₂ interface (the γ -FCC-Ni(Al, V) and the L1₂-Ni₃(Al, V)) of diffusion phases. Nickel atoms segregate first and then deplete, Vanadium atoms segregate while aluminum atoms deplete at the (100) FCC/L12 interfaces forming new diffusion phases. Both, vanadium segregation and aluminum depletion affect the alloy's interfacial properties which in turn, will lower the interfacial energy and increase the work of separation. The results of the Phase-field method coincide with the results of the atomistic computation based on the 2NN MEAM method. Furthermore, the applicability of the atomistic approach to an elaborate alloy design of advanced Ni-based superalloys through the investigation of the effect of alloying elements at the interfacial properties is discussed.

Wei-ping Dong dwp@zjnu.cn **Keywords** atomistic simulation \cdot interfacial properties \cdot new phase transformation \cdot phase-field method \cdot vanadium segregation

1 Introduction

In Ni-based superalloys, the application of the intermetallic compound Ni₃Al (L1₂) in the series of high temperature structural materials is restricted due to severe brittleness problems. There are two reasons for this poor brittleness, one is the existing slip system, and another is the poor grain boundary cohesive force. A single crystal Ni₃Al has good plasticity, while the poly-crystalline Ni₃Al shows brittleness at both room and high temperatures, which suggests that its intrinsic brittleness of the interface, determines the brittleness of the Ni₃Al crystal. Many researchers have studied that the addition of the element B, which is partially scattered at the interfaces of the Ni₃Al crystal, can improve the alloy's tensile plasticity significantly.^[1,2] Some other alloy elements can also improve the intrinsic brittleness of the Ni₃Al crystal plane interface by adsorbing the alloying elements which are segregated at the interface, and therefore improving the alloy plasticity.^[3] As a result, the occupied behavior of alloy elements in the Ni₃Al alloy^[4,5] and the segregation of the alloy elements on the Ni₃Al crystal's plane interface^[6-8] have been widely studied. What should be further pointed out is that the segregation of atoms can change the anisotropy in the interfacial energy and the shape of the γ' precipitates. It is believed that the material's grain size distribution can also be changed by alloying and, consequently change the lattice mismatch or the misfit strain energy at the interface of the crystal due to the atoms segregation.^[9-11] Therefore, information on the interfaces in Ni-based superalloys,

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particularly regarding the structure, energy, migration and segregation dynamics behavior, is highly required to get a better understanding of their strengthening effect.

The experimental measurement of interfacial energy, migration and solute segregation is very difficult to conduct. Alternatively, the forehand parameters can be calculated rather easily using the atomistic simulations that combine molecular dynamics (MD) or Monte Carlo (MC) methods with the Phase-field method. These atomistic simulations have been successfully applied in both binary and ternary systems, whereas for exploring various interfacial properties of solids. Particularly, the interface structure and the interfacial energy as well, with simultaneous use for searching of candidate alloying elements that modify the interfacial energy, misfit the strain or the change in the volume fraction of precipitates for an improvement of the alloys' mechanical properties.^[12-15]

First, the interfacial migration and the elements segregation will be studied by the Phase-field method. Then, the alloying elements that modify the interfacial energy and the work of separation will be studied by the use of both MD and MC simulations.

2 Atomistic Modeling

2.1 Phase Field Model

The phase field equation, based on Onsager and Ginzburg-Landau theories,^[16-19] describes the atomic configuration and precipitation pattern of the ordered phases by the occupation probability $P(\vec{r},t)$ at the crystal lattice site \vec{r} and the random time *t*, with a proportional change rate to the corresponding variation of free energy. The atomic occupation probabilities of the ternary systems are $P_A(\vec{r},t) + P_B(\vec{r},t) +$ $P_C(\vec{r},t) = 1$, where the subscripts *A*, *B* and *C* designate three kinds of atoms (*A*, *B* and *C* designate Ni, Al and V respectively, in this paper). In this simulation, the phase field equation puts the simplification for crystalline defects, and just considers the integrated lattice to response atomic diffusion. Then the kinetic equation can be written as:

$$\begin{cases} \frac{\mathrm{d}P_A(\vec{r},t)}{\mathrm{d}t} = \frac{1}{k_{\mathrm{B}}T} \sum_{r'} \left[L_{AA}(\vec{r}-\vec{r}') \frac{\partial F}{\partial P_A(\vec{r}',t)} + L_{AB}(\vec{r}-\vec{r}') \frac{\partial F}{\partial P_B(\vec{r}',t)} \right] + \zeta_1(\vec{r},t) \\ \frac{\mathrm{d}P_B(\vec{r},t)}{\mathrm{d}t} = \frac{1}{k_{\mathrm{B}}T} \sum_{r'} \left[L_{BB}(\vec{r}-\vec{r}') \frac{\partial F}{\partial P_B(\vec{r}',t)} + L_{AB}(\vec{r}-\vec{r}') \frac{\partial F}{\partial P_A(\vec{r}',t)} \right] + \zeta_2(\vec{r},t) \end{cases}$$

$$(\mathrm{Eq}\ 1)$$

The free energy F for the ternary system is given by:

$$\begin{split} F &= -\frac{1}{2} \sum_{r} \sum_{r'} \left[(-V_{AB}(\vec{r} - \vec{r}') + V_{BC}(\vec{r} - \vec{r}') + V_{AC}(\vec{r} - \vec{r}') P_A(\vec{r}) P_A(\vec{r}) P_B(\vec{r}') + V_{AC}(\vec{r} - \vec{r}') P_A(\vec{r}) P_A(\vec{r}') + V_{BC}(\vec{r} - \vec{r}') P_B(\vec{r}) P_B(\vec{r}') \right] \\ &+ k_B T \sum_{r'} \left[P_A(\vec{r}) \ln(P_A(\vec{r})) + P_B(\vec{r}) \ln(P_B(\vec{r})) + (1 - P_A(\vec{r}) - P_B(\vec{r})) \ln(1 - P_A(\vec{r}) - P_B(\vec{r})) \right] \end{split}$$
(Eq 2)

where the first sum represents the chemical energy, the second sum represents the thermal dynamic energy of the system, k_B is the Boltzmann constant and $V_{ab}(\vec{r} - \vec{r}')$ is the effective interactive energy. Details regarding Microscopic phase field modeling are referred.^[16-19]

It is proven convenient and even computationally advantageous for the kinetic equations to be solved in the reciprocal space. First, the Euler method was used for solving the equation, whereas consequently the inverse Fourier transformation was executed; finally the relationship between the occupation probability and the random time were obtained.

2.2 MEAM Potential Formalism

During the MEAM, the total energy of a system is:

$$E = \left[\sum_{i} F_i(\bar{\rho}_i) + \frac{1}{2} \sum_{j(\neq i)} S_{ij} \varphi_{ij}(R_{ij})\right], \quad (\text{Eq 3})$$

where F_i is the embedding function for an atom *i* embedded in a background electron density $\overline{\rho_i}$, S_{ij} and $\varphi_{ij}(R_{ij})$ are the screening function and pair interaction between atoms *i* and *j* separated by a distance R_{ij} . In order for energy calculations to be executed, the functional forms for F_i and φ_{ij} should be utilized. The background electron density at each atomic site is computed with directionality of bonding consideration, such as by several partial electron density terms combinations for various angular contributions with the weight factors of $t^{(h)}(h = 1-3)$. Each partial electron density constitutes a function of both atomic configuration and atomic electron density. The atomic electron densities $\rho^{a(h)}$ (h = 0-4) are:

$$\rho^{a(h)}(R) = \rho_0 \exp\left[-\beta^{(h)}(R/r_e - 1)\right],$$
 (Eq 4)

where ρ_0 (the atomic electron density scaling factor) and $\beta^{(h)}$ (the decay lengths) are adjustable parameters, and r_e is the nearest-neighbor distance in the equilibrium reference structure. A specific form is given to the embedding function F_i , but not to the pair interaction φ_{ij} . Instead, a reference structure where individual atoms are on the exact lattice points was defined and the total energy per atom of the reference structure was estimated from the zero-

temperature universal equation of state of metals by Rose et al.^[20] Following, the value of the pair interaction was estimated from the known values of total energy per atom and the embedding energy as a function of the nearestneighbor distance. In the original MEAM,^[21] only firstnearest-neighbor interactions were considered. Neglect of second- and more distant nearest-neighbor interaction was accomplished by a strong, screening and many-body effects function.^[22] The second-nearest-neighbor interactions during the modified formalism were considered by an adjustment in the screening parameters C_{min} , in order for the screening and many-body effects to become less severe. In addition, a radial cutoff function^[22] was applied to reduce calculation time. Details of the (2NN) MEAM formalism have been published.^[21-26]

3 Results and Discussion

As mentioned forehand, the interfacial properties are crucial to the control of size distribution and the shape of precipitates. Therefore, it is necessary to know their migration formation and the effect of alloying elements on the interfaces in order to prepare the design of the Ni-Al-Vbased superalloys. In this section, three methods of study are used. One method is the Microscopic Phase-field method, which leads to an easy study of the interfacial migration and the alloy elements performance. Additional methods are the MD and MC simulations based on the modified embedded-atom method, which leads to an easy calculation of the interfacial energy and separation.

The simulation based on the Microscopic phase field method was performed in a supercell consisting of 128×128 unit cells, in a periodical boundary condition imposed along both dimensions. The time increment Δt was 0.0002 and the thermal fluctuations were removed after the nucleation process, leading the system to choose the dynamic path automatically. The simulated pictures included here are two-dimensional projections along the [001] direction and depicted with different colors, if the occupation probability of aluminum is 1.0, consequently the site is green, therefore the L1₂-Ni₃Al phase is green, whereas if the occupation probability of vanadium is 1.0, consequently the site is red, consequently the DO_{22} -Ni₃V phase is red, and if the occupation probability of nickel is 1.0, then the site is blue, so the matrix is almost blue. The precipitation sequences will be various; therefore the DO_{22} phase will be referred as a new phase or a second phase in this paper.

Microstructure evolution of the Ni₇₅Al₁₉V₆ alloy under the temperature of 1000K is shown in Fig. 1. At the $t = 2.0 \times 10^3$ time step as shown in Fig. 1(a), there are some small ordered structures called non-stoichiometric ordered phases that randomly appear in the matrix, since their degree of order is low, leading to an uneasy observation of the corresponding structure. Subsequently, at the $t = 2.0 \times 10^4$ time step as shown in Fig. 1(b), a large number of ordered L1₂ precipitates appear (L1₂ phase is green) and there are many interfaces between these ordered L1₂ phases. While time increases, at the $t = 1.0 \times 10^5$ time step shown in Fig. 1(c), the L1₂ phases increase in size gradually, and the interfaces reduce and migrate (certain interfaces disappear), and the new DO₂₂ phase crystals (DO₂₂ phase is red) were encircled by the $L1_2$ phases. The region within the white arrow squares A/B is enlarged and shown in the boxes located on the lower left side, whereas the new DO₂₂ phases increased in size and the $L1_2$ phases were coarser as shown in Fig. 1(d). Conclusively from Fig. 1, the interfaces between $L1_2$ phases are observed with the existence of DO_{22} phases formed on these interfaces.

For further clarification of the effect of the alloying elements performance on the new DO₂₂ phase formed on the interfaces, the distribution and evolution of the three alloying elements across the ordered domain interfaces in different steps according to Fig. 1 arrow square A are consequently analyzed as shown in Fig. 2 of the Ni₇₅₋ $Al_{19}V_6$ alloy, precipitated at the temperature of 1000K. The definition of distance (lattice plane) of the arrow square A interface in Fig. 1(d) is presented in Fig. 2(f). In Fig. 2(a), (b), (c) the variation of the Ni, Al, V concentrations at different steps on the arrow square A interface is respectively shown. In these figures, segregation is declared as the raised above concentration and depletion is declared as the pushed below concentration, of the curves. In the early stage of precipitation at the time step of $t=2.0\times10^3$, the concentration curves of Ni, Al, V have little effect, according to Fig. 1(a), in the matrix. As time increases to a 1.0×10^4 time step, the concentration curves of Ni, is rising above (segregation) and the Al curves are pushing below (depletion) but the V curves change little and according to the Fig. 1(b) the interface is formed. At the 1.0×10^5 and 2.0×10^5 time steps, the concentration curves of Ni, Al, and V have a similar trend and the distribution of the three elements at the 2.0×10^5 time step as shown in Fig. 1(d), in which the Al is pushing below the curves and the Ni elements are pushing less below the curves and the V curves are raising above (the Al pushing below the curve in a nearly equivalent manner to the V curve raising above) according to the new DO₂₂ phase formed in the arrow square A ordered at the interfaces, being in accordance with Fig. 1(c, d). Furthermore, the volume fraction of both L12 and DO22 phases as presented in Fig. 2(e) was calculated. It is concluded that the DO_{22} phase increased and the L12 phase decreased gradually from the 1.0×10^5 step, correlating with forehand results



Fig. 1 Ni₇₅Al₁₉V₆ alloy simulated atomistic microstructure temporal evolution pictures at 1000K, (a) $t = 2.0 \times 10^3$, (b) $t = 2.0 \times 10^4$, (c) $t = 1.0 \times 10^5$, (d) $t = 5.0 \times 10^5$, arrow squares A/B indicate the interface

that the new DO_{22} phase was formed among $L1_2$ phases at the corresponding interfaces as presented in Fig. 1 and Fig. 2(a-d).

Conclusively, the Ni, Al, V elements have a different distribution and evolution trend during the formation of the interface; specifically both the Al and Ni elements are depleted and V is segregated (Al depletion according to V segregation) to form the new DO_{22} phase; Ni is segregated first and then depleted, as the interfaces migrate; the Al depletion is larger and segregation of the V is simultaneously larger as the new DO_{22} phase is formed; the new DO_{22} phase was formed among L1₂ phases at the interfaces. This shows that the interfaces have local characteristics in the structure of the DO_{22} phase, upon which the V atoms easily precipitate and to be the new DO_{22} phase nucleation position.

The distribution and evolution of the alloying elements across the ordered domain plane interfaces, in the Ni₇₅₋ $Al_{22}V_3$ alloy at 1000*K* presented in Fig. 3, were studied further and the enlargement of the region within the white arrow square C is presented. In Fig. 3(a), all the phases are $L1_2$ and there is no DO₂₂ phase appearance (no red color). Although the Al and Ni elements are depleted and V is segregated in the same trend as in Fig. 2(d), the V concentration resulted being significantly low and could not increase to the concentration of 0.25 (or 25%)to form the $DO_{22}(Ni_3V)$ phase.

For the study of the effect of the distribution and evolution of the alloy elements addition on the interfacial properties, the interfacial energy and the effect of separation should be calculated as it couldn't be executed with the use of the Microscopic Phase-field method. The calculations of the interfacial energy and the work of separation based on the modified embedded-atom method were performed by the computation of the total energy of a supercell that involved an interface between the two phases and the sum of the total energies of the individual phase samples of equal size.^[13,14] When a random solid solution is used in an atomistic computation, it becomes necessary for attention to be paid in the probable effect of a solute distribution on the computation results because it could result in a statistical error due to the limited atomic size (number of atoms) of the samples. For the probable statistical error to be reduced, a relatively large sample with $4000 \sim 12000$ atoms was used and ten independent calculations were performed for the individual interfaces. The interfacial energy was calculated by the following equation:



Fig. 2 Distribution and evolution of alloying elements across ordered domain interfaces formed among L1₂ phases in the Ni₇₅Al₁₉V₆ alloy at 1000*K*, (a) Ni, (b) Al, (c) V, (d) $t = 2.0 \times 10^5$; (e) volume fraction

of $L1_2$ and DO_{22} phases in the $Ni_{75}Al_{19}V_6$ alloy at 1000K; (f) the definition of distance (lattice plane) of the arrow square A interface in Fig. 1(d)

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Fig. 3 (a) $Ni_{75}Al_{22}V_3$ alloy simulated atomistic microstructure temporal evolution pictures aging at 1000*K* for $t = 2.0 \times 10^5$, arrow C indicating the interface, (b) distribution and evolution of alloying elements across ordered domain interfaces formed among L1₂ phases of the C interface



Table 1 The interfacial energy and the work of separation of γ -Ni(Al₂₂, V₃) and Ll₂-Ni₃(Al₂₂, V₃) (100) interfaces at 1000 K. (unit: J/m²)

	Interfacial energy	Work of separation
Previous to MC simulation	0.0375	3.90
Following MC simulation	-0.1418	4.37

$$\sigma = \left\{ E_{\sup ercell} - 1/2 \left[E_{one phase} + E_{another phase} \right] \right\} / 2A.$$
(Eq 5)

where, $E_{sup\,ercell}$ is the total energy of the supercell, $E_{one\,phase}$ and $E_{another\,phase}$ are the total energies of individual phase samples, A represents the area of the interface. The work of separation is the following equation:

$$W_{se} = \left[\left(E'_{one \ phase} + E'_{another \ phase} \right) - E_{sup \ ercell} \right] / 2A.$$
(Eq 6)

where, $E_{supercell}$ is also the total energy of the supercell (the same as in the calculation of interfacial energy), $E'_{one \ phase}$ and $E'_{another \ phase}$ are the total energies of individual phase samples (the difference between the calculations of the interfacial energy was that, at the side of each sample composing the interface was left as a free surface, without the application of the periodic boundary condition and the same lattice parameters were maintained in both directions parallel to the interface).

All samples with coherent interfaces of the γ -Ni(Al₂₂, V₃) and the L1₂-Ni₃(Al₂₂, V₃) (100) interface were prepared by the combination of equal amounts of both γ and L1₂phase addition. The results are shown in Table 1 and

Fig. 4. Before the Monte Carlo (MC) simulation, the interfacial energy of 0.0375 J/m² and the work of separation of 3.90 J/m²were calculated. Following, the temperature was increased to 1000K and the MC simulation was performed in each situation to keep the interface stable. Moreover, the interfacial energy of -0.1418 J/m^2 and the work of separation of 4.37 J/m²were also calculated. The results coincided with the Cr atoms lowering the interfacial energy when replacing the Al atoms on the interface.^[27] It is known that a variety of segregations can cause three effects: a segregation that might enhance the interface; reversely, segregation might reduce the cohesion and the bonding strength of the interface; or the segregation might result in a new phase transformation.^[9]The results showed that the interface was unstable as the interfacial energy was lower than zero and might form a new phase being in agreement with forehand results. In Fig. 4(a) the distribution and evolution of V across the interface is shown. It can be seen from the concentration of V that it segregated itself near the interface. Comparing Figures 4(c) and (d), the interface after the 200 steps MC simulation has a much higher concentration of vanadium atoms than measured before the MC simulation. The V concentration in Fig. 4(a) is approximately 0.08, nearly equal to the V concentration presented in Fig. 3(b) of being approximately 0.075. The MC simulation results shown in Table 1 and displayed in Fig. 4 resulted in vanadium atoms segregating on the $\gamma/L1_2$ interface; showing that the vanadium segregation was lower from the interfacial energy simultaneously increasing the work of separation; the MC method results matched the Microscopic Phase-field method results.



(b) $E=0.0375 (d/m^2)$ (d) $E=-0.1418 (J/m^3)$

Fig. 4 γ -Ni(Al₂₂, V₃) and L1₂-Ni₃(Al₂₂, V₃) (100) interface at 1000 K. (a) V concentration, (b) the supercell before MC simulation, (c) the dark profile layer before MC simulation, (d) the same layer after MC

simulation. Yellow, gray, and red circles denote Ni, Al, and V atoms, respectively (Color figure online)

With the combination of the Microscopic Phase-field method and the modified embedded-atom method results, the conclusion that the alloying elements segregation or depletion can affect the interfacial properties and form a new phase on the interfaces if the concentration of the segregated elements was adequate, could be reached.

Elements segregation in alloys on the interface is related to a new phase formation and the grain stability in the alloys, also being closely connected with the materials' mechanical properties. Many researches showed that interface segregation is affected by the materials properties and directly related to the alloying elements, varying in the concentration of the alloying elements and the position of the segregation elements: Elements such as H, O, S, or P causing interface segregation could reduce the material plasticity to be detrimental to the material as a brittle fracture; and the elements Re, Co, Mo, B, and C, in interface segregation could enhance the performance of materials by strengthening the interfacial cohesion; the fundamental physical reason was that the interface segregation was caused by the electronic structure on the interface.^[1-8,28-32] Therefore, an important field in the interface segregation study is that it is used in microstructure and alloy design. A difficult challenge in these researches is the structure of the interface and the chemistry of the interfacial properties at an atomic scale. Historically, studies showed that each method, such as experimenting, ab initio, MD, MC and phase field simulation, has different disadvantages. Preferably, a new simplifying method or combination of several methods for better results to be reached should be developed. More research to improve the materials' mechanical properties is proven to be needed.

4 Conclusions

The main conclusions are:

- 1. The results showed that the Ni, Al, V elements have different preferences of segregation or depletion during the interface forming in the $Ni_{75}Al_{19}V_6$ alloy; both the Al and Ni elements were depleted and V segregated (Al depletion percentage nearly equal to V segregation) to form the new DO_{22} phase; Ni first segregated and then was depleted according to the interface migration.
- Also the Al and Ni elements were depleted and the V was segregated in the Ni₇₅Al₂₂V₃ alloy in the same trend as in the Ni₇₅Al₁₉V₆ alloy, but the V element concentration was not enough to form a new DO₂₂ phase.

3. The results of the 2NN MEAM method matched the results based on the Phase-field method. Vanadium segregation and aluminum depletion both affect the interfacial properties which in turn, both lower the interfacial energy and increase the work of separation.

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