



Influence of VO²⁺ Ion-Doped Li₂Ba₃(P₂O₇)₂ Pyrophosphate Nanopowder: Structural, Morphological, Optical, and Photoluminescence Properties

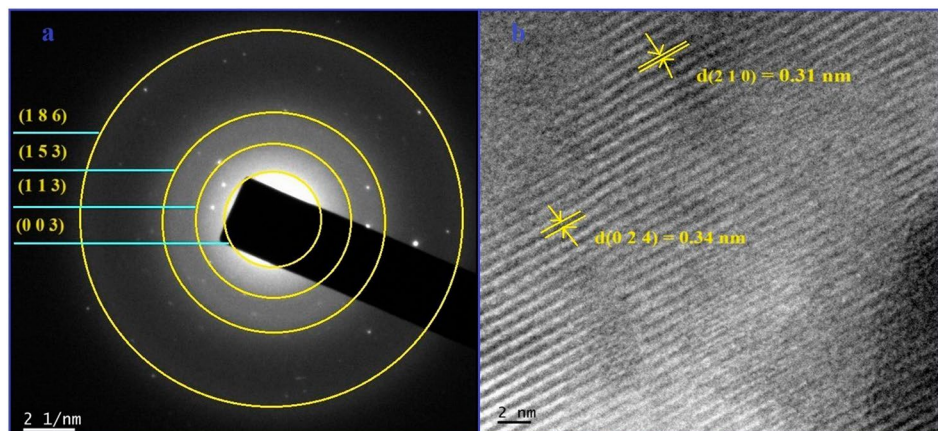
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Abstract

Solid-state reaction synthesis produced VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder at ambient temperature. The produced sample was characterized by powder x-ray diffraction (XRD), scanning electron microscopy (SEM) with energy dispersive spectroscopy (EDS), high-resolution transmission electron microscopy (HR-TEM), Fourier-transform infrared spectroscopy (FT-IR), Raman spectroscopy, UV-visible spectroscopy, electron paramagnetic resonance (EPR), and photoluminescence (PL) techniques. Powder XRD confirmed the preservation of an orthorhombic crystal structure of the sample with an average crystallite size of 34.2 nm. In addition, lattice cell parameters and internal lattice strain were evaluated. SEM and HR-TEM images revealed that a tiny agglomeration of stone-like particles appeared in the sample and also evaluated particle size distributions. FT-IR and Raman spectra exhibited characteristic vibrational modes of phosphate (PO₄³⁻) ions along with other bands. Optical absorption spectrum of the VO²⁺-doped sample exhibited three characteristic peaks at 831, 635, and 416 nm. Furthermore, crystal and tetragonal field parameters were determined as D_q = 1574, D_s = -2903, and D_t = 664 cm⁻¹. From the EPR spectrum, calculated spin Hamiltonian parameters were g_{||} = 1.954, g_⊥ = 1.977, A_{||} = 284 × 10⁻⁴ cm⁻¹ and A_⊥ = 53 × 10⁻⁴ cm⁻¹. Optical and EPR spectra revealed that VO²⁺ ions have tetragonal distortion octahedral site symmetry and have a moderate covalent nature with ligands. Using the PL spectrum, the CIE chromaticity coordinates were determined to be in the yellowish-green region appropriate for LEDs and lighting systems.

Graphical Abstract



Keywords XRD · HR-TEM · optical · EPR · photoluminescence

Extended author information available on the last page of the article

Introduction

Recent advances in science and technology necessitate developing and applying different materials based on phosphate compounds.¹ These compounds have catalytic, magnetic, and optical properties, and are frequently employed as monocrystals or polycrystals, ceramics, and so on.² Special scientific interests include a study of the characteristics of materials as well as their synthesis and development.³ Inorganic phosphate has recently received much attention because of phosphate-based luminescence materials.⁴ The great optical absorbance and superior chemical and thermal stability of pyrophosphates make them an ideal host lattice for activators.⁵ The crystal field characteristics and energy level structure of transition metal ions can be obtained through optical absorption experiments. Information on the electronic structure, oxidation state, site symmetry, and bonding type of impurity ions can be obtained by electron paramagnetic resonance (EPR) and optical absorption techniques. In addition, LEDs have low power consumption, solid structure, compact size, fast response, and friendliness.⁶ $M_2O-P_2O_5-Me_xO_y$ -type systems (where $M = Li, Na, K$) are recognized as versatile solvents for 3d-metal oxides and serve as reaction media for synthesizing diverse diphosphates.¹ One of the transition metal ions that can exist in several oxidation states based on the host structure is vanadium.⁷ Variable states of vanadium include V^{2+} , V^{3+} , V^{4+} , and V^{5+} , with V^{4+} being the majority state of them which appears as VO^{2+} . Vanadium dioxide (VO^{2+}) has garnered significant interest from scientists and technologists due to its distinct metal–insulator transition (MIT) near room temperature making it a notable thermochromic material. Vanadyl ions are well known in research because of their variety of applications in the field of lasers, electrical switches, memory devices, smart radiators, sensors, and luminescence.⁸ Recently, VO^{2+} -doped phosphor materials have been reported with VO^{2+} exhibiting different luminescence properties.^{9–12} Authors have reported pure and iron-doped $Li_2Ba_3(P_2O_7)_2$ pyrophosphate nanopowders,¹³ with pure and doped nanopowders exhibiting different luminescent properties.

As far as we are aware, no research on the characteristics of $Li_2Ba_3(P_2O_7)_2$ -doped with transition metal ions has been published. In this work, VO^{2+} -doped $Li_2Ba_3(P_2O_7)_2$ pyrophosphate nanopowder has been synthesized using a solid-state reaction technique. Additionally, we discuss various structural and optical properties, including site symmetry, bonding nature, and luminescent behavior.

Experimental

Materials

The following chemicals were employed to produce VO^{2+} -doped $Li_2Ba_3(P_2O_7)_2$ pyrophosphate nanopowder: lithium carbonate (Li_2CO_3 , 99.9%), barium carbonate ($BaCO_3$, 99.9%), ammonium dihydrogen orthophosphate ($NH_4H_2PO_4$, 99.9%), and 0.01 mol% of vanadium pentoxide (V_2O_5 , 99.9%) were procured from HiMedia laboratories, Mumbai, India. All the chemicals were analytically pure and used without further purification.

Sample Preparation

The starting chemicals, 0.739 g of Li_2CO_3 , 5.738 g of $BaCO_3$, and 4.601 g of $NH_4H_2PO_4$ were weighed and ground into a fine powder for about 30 min using an agate mortar. Next, 0.182 g of V_2O_5 was added to the mixture and ground for a further 30 min. The chemical mixture obtained was placed into a silica crucible and sintered at 350°C for 1 h, at 550°C for 1 h, and finally at 750°C for 2 h in a programmable muffle furnace. Throughout this process, the sample was ground for 1 h at each temperature to eliminate volatile components such as H_2O , NH_3 , and CO_2 . After cooling to room temperature, the mixture was further ground for 2 h to obtain the required sample. The synthesized VO^{2+} -doped $Li_2Ba_3(P_2O_7)_2$ pyrophosphate nanopowder has been characterized using various spectroscopic techniques.

Characterization Techniques

The x-ray diffraction (XRD) patterns of the prepared sample were obtained using a Rigaku-Smartlab D/MAX-2500 with graphite-monochromatic $CuK\alpha$ ($\lambda = 0.15406$ nm) radiation in the angular range of $2\theta = 10^\circ$ – 70° , employing a step size of 0.01° , and with a speed of 10° per min. A JEOL JSM-IT 500 scanning electron microscope (SEM) with energy-dispersive x-ray spectroscopy (EDS) was used to observe the surface morphology and chemical composition. Images from selected area electron diffraction (SAED) and high-resolution transmission electron microscopy (HR-TEM) were obtained at 200 KV using a JEOL JEM-2100. The attenuated total reflectance approach was used to measure the Fourier-transform infrared (FT-IR) spectrum in the 4000 – 400 cm^{-1} spectral band at room temperature using a JASCO FT/IR-4700 instrument. Furthermore, a RENISHAW micro-RAMAN spectrometer was used to produce Raman spectra between 0 cm^{-1} and 3500 cm^{-1} . Optical absorption spectra were captured at room temperature within 200 – 1400 nm wavelength range using a JASCO

V-670 UV-Vis-NIR spectrophotometer. A JEOL JES-FA 100 spectrometer operating at X-band frequencies with a 100-KHz field modulation was used to obtain the EPR spectrum at room temperature. Two 450-W Xenon lamps were used as excitation sources and a HORIBA Jobin-Yvon Fluorolog-3 spectrofluorometer was used to record the photoluminescence (PL) spectra at room temperature.

Results and Discussion

XRD Analysis

The diffraction peaks are ascribed to a mixed phase including the monoclinic structure of Li₂BaP₂O₇ (Pearson's Crystal Database No.1003786) and the hexagonal structure of Ba₂P₂O₇ (JCPDS: 01-083-0990). In the XRD pattern of the sample, peaks observed at $2\theta = 14.49, 19.28, 22.71, 25.17, 25.85, 28.42, 36.61, 39.79, 41.89, 42.91, 46.41, 53.06, 59.95,$ and 66.02 are assigned to the diffraction planes (0 2 1), (1 2 0), (1 2 1), (2 0 0), (0 0 4), (0 1 5), (1 3 4), (1 0 3), (1 5 3), (2 3 4), (1 4 5), (3 4 3), (2 1 8), and (0 3 9) of monoclinic wurtzite Li₂BaP₂O₇ (*), respectively. The peaks observed at $2\theta = 16.55, 22.71, 25.17, 29.61, 31.67, 33.12, 38.73, 41.89, 48.56, 50.31, 56.23, 58.17,$ and 62.81 correspond to the planes (1 0 1), (1 1 1), (0 0 2), (1 1 2), (3 0 0), (2 0 2), (2 1 2), (3 0 2), (3 2 0), (3 2 1), (3 1 3), (3 3 0), and (3 0 4) of a hexagonal phase of Ba₂P₂O₇ (#), respectively. For the undoped sample, XRD peaks observed at $2\theta = 14.45, 19.20, 22.69, 25.12, 25.69, 28.39, 36.51, 39.68, 41.85, 42.88, 46.36, 53.02, 59.90,$ and 65.95 correspond to the monoclinic wurtzite phase of Li₂BaP₂O₇, while peaks observed at $2\theta = 16.53, 22.69, 25.12, 29.54, 31.62, 32.89, 38.68, 41.79, 48.50, 50.27, 56.19, 58.13,$ and 62.74 correspond to the hexagonal phase of Ba₂P₂O₇. The right shift in the XRD peaks with VO²⁺ ion-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate is due to the effect of the difference in the ionic radius between the cations which causes the crystallite lattice to expand and consistent with the Bragg's equation.¹⁴ The shift in the XRD peak position of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder is depicted in Fig. 1. The resulting diffraction pattern contains information about the spacing of atomic planes within the crystal lattice as well as any deviations or distortions caused by doping-induced stresses. The unit cell parameters have been evaluated as $a = 0.517$ nm, $b = 1.318$ nm, $c = 1.611$ nm, and $V = 1.098$ nm³. These values agreed with undoped and iron-doped pyrophosphate nanopowders,¹³ and reveal an orthorhombic crystalline structure with space group 2P₁. This information was found using the Powd software, with the effective ionic radii of cations showing the following different coordination numbers (CN) of Li⁺ ion (0.076 nm, CN = 6), Ba²⁺ ion (0.135 nm, CN = 6), and VO²⁺ ion

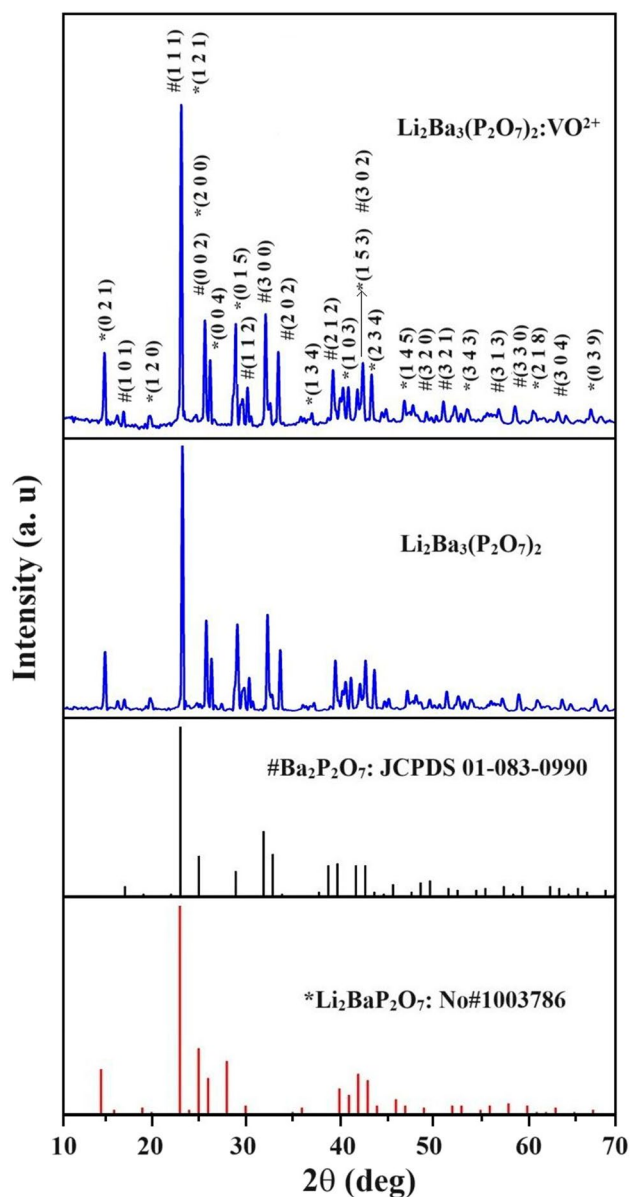


Fig. 1 X-ray diffraction pattern of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

(0.079 nm, CN = 6). VO²⁺ ions are predicted to fill any Li⁺ or Ba²⁺ ion sites that exist in the crystal lattice. The radius percentage difference (Dr) between the dopant and substituted ions was estimated by¹⁵:

$$Dr = 100\% \times \frac{\{R_m(CN) - R_d(CN)\}}{R_m(N)} \quad (1)$$

where R_m and R_d are the radii of the host cations and doped ions, respectively. The calculated Dr values between VO²⁺ and Li⁺/Ba²⁺ are -3.9% and 41.5% respectively. The tolerable percentage difference in ionic radii between the

activated and substituted ions should not reach above 30%.¹⁶ Obviously, the substitution of VO^{2+} at the Li^+ sites is preferable. By using Scherrer's equation,¹⁷ the average crystallite size has been calculated:

$$D = \frac{K\lambda}{\beta \cos \theta} \quad (2)$$

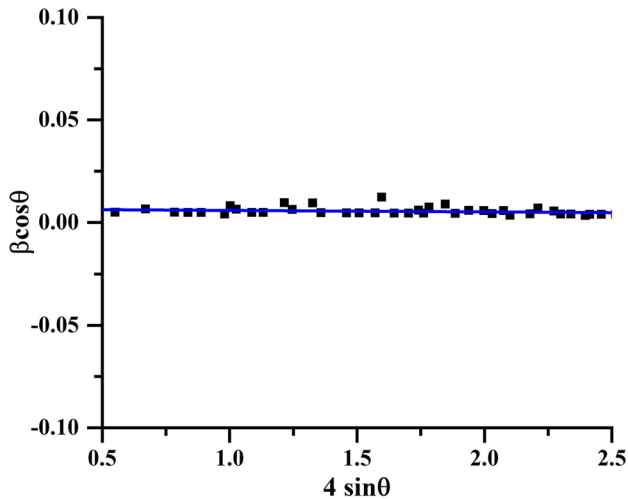


Fig. 2 Williamson-Hall plot of VO^{2+} -doped $\text{Li}_2\text{Ba}_3(\text{P}_2\text{O}_7)_2$ pyrophosphate nanopowder.

Table I Average crystalline size, lattice strain and dislocation density of VO^{2+} -doped $\text{Li}_2\text{Ba}_3(\text{P}_2\text{O}_7)_2$ pyrophosphate nanopowder

Crystalline size (nm)		Dislocation density ($\delta \times 10^{15}$)		Microstrain ($\epsilon \times 10^{-3}$)	
Scherrer	W-H	Scherrer	W-H	Scherrer	W-H
34.2	33.1	8.4	7.8	5.0	7.2

where λ is the x-ray wavelength (0.15406 nm), θ is the maximum intensity diffraction angle, β is the full width at half-maximum of the corresponding lattice planes, and K is the shape factor with a value of 0.9. The average crystallite size was found to be 34.2 nm which is in the nano-size range.

Dislocation density and micro-strain are important characteristics that provide insight into how a material deforms from its original structure.^{13,18} A critical parameter for determining the difference in atom displacement from reference positions is micro-strain, and this, and dislocation density, are also calculated to understand the structural behavior of the prepared sample. The micro-strain (ϵ) and dislocation density (δ) for the sample were obtained using¹⁹:

$$\epsilon = \frac{\beta \cos \theta}{4} \quad (3)$$

$$\delta = \frac{1}{D^2} \quad (4)$$

A method for determining the sample's crystallite size and micro-strain was proposed by Williamson and Hall (W-H). The W-H formula is written as:

$$\beta \cos \theta = \frac{K\lambda}{D} + 4\epsilon \sin \theta \quad (5)$$

Figure 2 shows a linear relationship between $4\sin\theta$ (x-axis) and $\beta\cos\theta$ (y-axis). The slope of this line corresponds to the micro-strain (ϵ) while its intercept ($k\lambda/D$) represents the crystallite size (D).²⁰ Comparison of the dislocation density and crystallite size are obtained from Debye-Scherrer's equation with those calculated using the W-H plot listed in Table I. The results obtained through the W-H method are consistent with those from Debye-Scherrer's equation with slight variations to the strain component considered in the W-H equation.

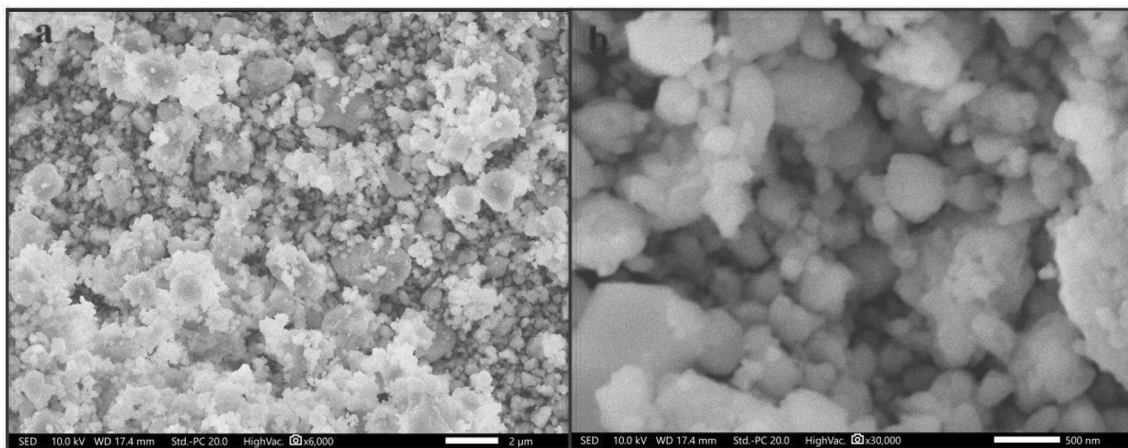


Fig. 3 SEM images (a) 2 μm and (b) 500 nm of VO^{2+} -doped $\text{Li}_2\text{Ba}_3(\text{P}_2\text{O}_7)_2$ pyrophosphate nanopowder.

SEM and EDS Analyses

SEM images of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder are illustrated in Fig. 3 captured at 2 μm and 500 nm. The images depict a stone-like configurational structure. Determining the true grain size using SEM images is challenging due to the irregular shape of the grains, a high degree of agglomeration, and wide size dispersion. The aggregation could be caused by mutual interaction between the particles, van der Waals forces, and electrostatic forces.⁶ The average grain size of the prepared sample was determined by analyzing the SEM images at a magnification of 500 nm using image-J software, and the data were utilized to create a histogram, as shown in Fig. 4 using Origin software. The calculated average grain size is 60.8 nm. The

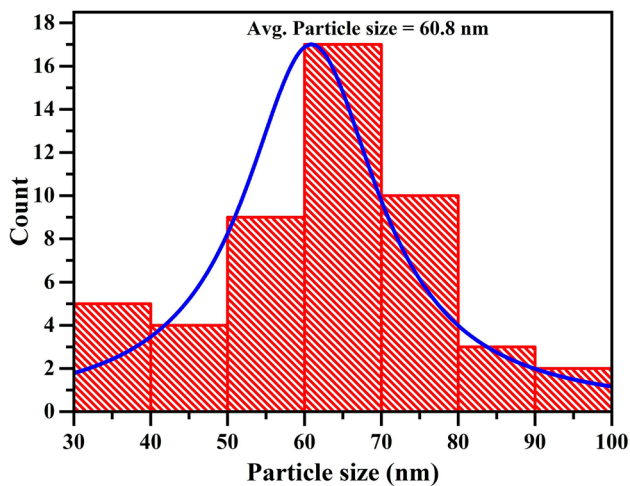


Fig. 4 Histogram of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder using SEM images of magnification 500 nm.

SEM grain size is somewhat larger than the XRD crystallite size values. This observed difference is likely due to the surface structure of converging grains which leads to enhanced grain growth as well as increased porosity and surface roughness.²¹ The elemental chemical composition of the sample was determined using EDS analysis and corresponding recorded spectra, as shown in Fig. 5. The table of determined compositions of elements Li, O, P, Ba, and V (inset in Fig. 5) closely matches the results of experimental stoichiometric calculations. Commercial EDS detectors cannot identify elements with atomic numbers less than 5 due to instrument constraints.²² This is the reason why lithium was not found in the EDS spectrum of the current investigation.

HR-TEM and SAED Analysis

Further analysis of the prepared sample was conducted using HR-TEM to examine the microstructures. Figure 6 shows HR-TEM images captured at different magnifications of 50 nm and 100 nm, which confirmed the presence of stone-like particles. The average particle size value of 36.3 nm was determined by utilizing Image-J software on the HR-TEM image of 100 nm and fitting the size distribution with a Gaussian model of the histogram, as shown in Fig. 7. The crystallite size was determined by Scherrer's equation, and the W-H plot method is a good match with HR-TEM studies. Moreover, the SAED image displayed in Fig. 8a reveals the heterogeneous nature of the sample, aligning with the cross-sectional planes corresponding to planes (1 8 6), (1 5 3), (1 1 3), and (0 0 3) which are consistent with the XRD pattern. In Fig. 8b, the measured lattice d-spacings of 0.31 and 0.34 nm correspond to the (2 1 0) and (0 2 4) planes, respectively.

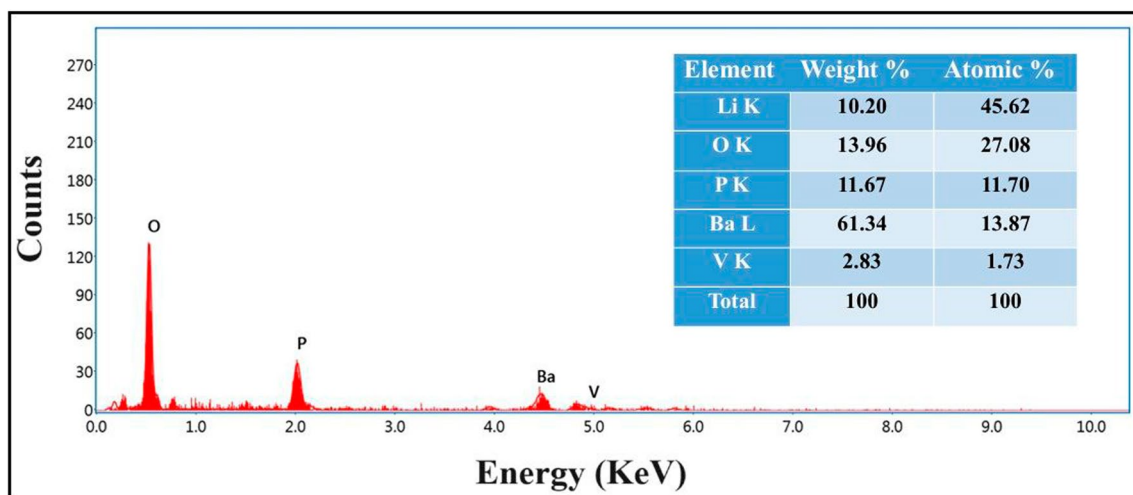


Fig. 5 EDS spectrum of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

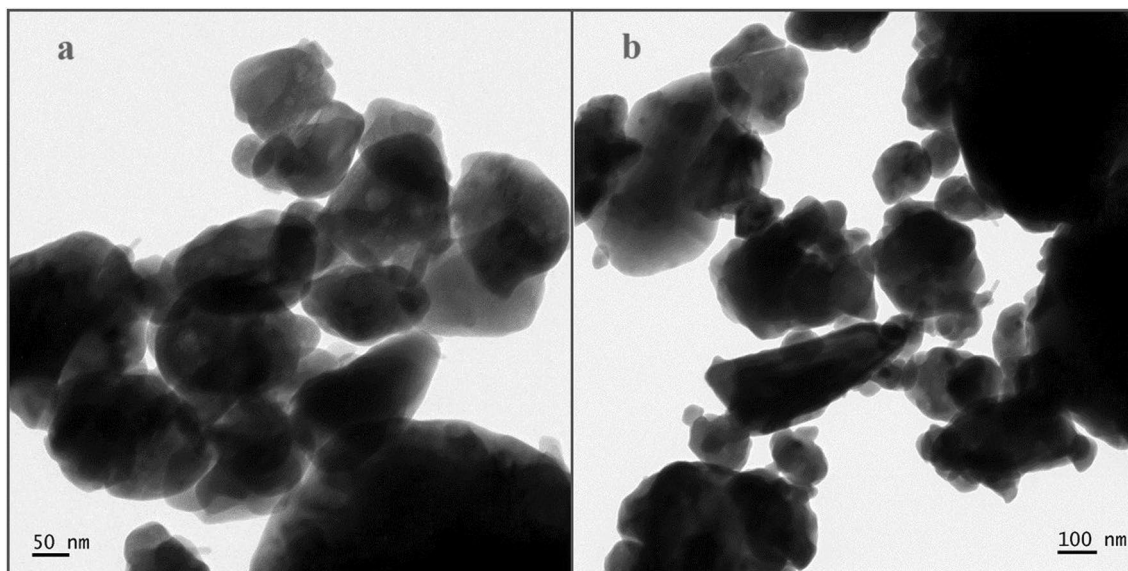


Fig. 6 HR-TEM images (a) 50 nm and (b) 100 nm of VO^{2+} -doped $\text{Li}_2\text{Ba}_3(\text{P}_2\text{O}_7)_2$ pyrophosphate nanopowder.

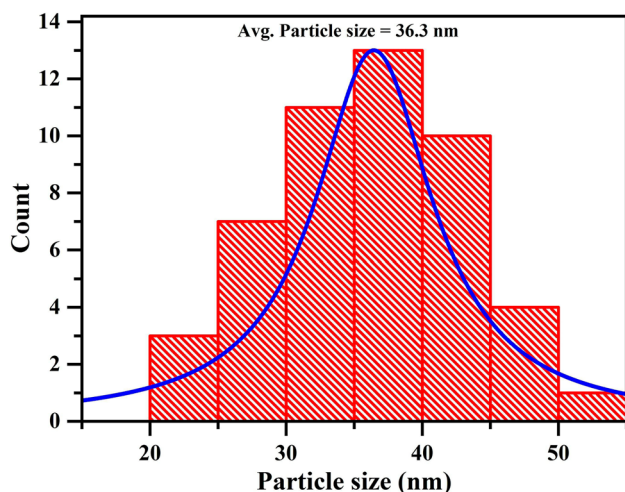


Fig. 7 Histogram of VO^{2+} -doped $\text{Li}_2\text{Ba}_3(\text{P}_2\text{O}_7)_2$ pyrophosphate nanopowder using HR-TEM images of magnification 100 nm.

FT-IR and Raman Analysis

Figure 9a shows the room-temperature FT-IR spectrum of VO^{2+} -doped $\text{Li}_2\text{Ba}_3(\text{P}_2\text{O}_7)_2$ pyrophosphate nanopowder with multiple broad peaks within the range of $1500\text{--}500\text{ cm}^{-1}$. The observed bands originate from the deformation and rocking modes of PO_3 as well as symmetric and asymmetric stretching vibrations of the PO_3 mode and P–O–P groups.²³ In the FT-IR spectrum, only a single O–H bending vibration band at 1404 cm^{-1} can be seen. We can distinguish the following bands within the range $1260\text{--}1000\text{ cm}^{-1}$ which are attributed to the stretching vibrations ν_{as} and ν_{s} of the PO_3 group.²⁴ The spectral range between 945 cm^{-1} and 720 cm^{-1}

contains bands arising from both asymmetric and symmetric stretching vibrations of $\nu(\text{P–O–P})$.²⁵ The bands observed within the range of $690\text{--}630\text{ cm}^{-1}$ are associated with asymmetric deformation mode $\delta_{\text{as}}(\text{PO}_3)$, while symmetric deformation $\delta_{\text{s}}(\text{PO}_3)$ is documented at 547 cm^{-1} . When compared to the pure sample, the bands at 691 and 640 cm^{-1} as ν_{as} of PO_3 and 987 cm^{-1} ν_{s} of PO_3 bands are not observed due to more distortion in the VO^{2+} -doped sample.¹³

The Raman spectrum assignment in the $200\text{--}1300\text{ cm}^{-1}$ region agrees quite well with the FT-IR spectrum assignment that was previously made, as shown in Fig. 9b. According to which, the strong Raman bands in the range of $1000\text{--}1280\text{ cm}^{-1}$ can be attributed to vibrations of PO_3 in both asymmetric and symmetric modes. Simultaneously, the bands in the range of $950\text{--}850\text{ cm}^{-1}$ and $800\text{--}700\text{ cm}^{-1}$ are specifically assigned to $\nu_{\text{as}}(\text{P–O–P})$ and $\nu_{\text{s}}(\text{P–O–P})$ vibrations, respectively.²⁶ The bands detected within the $500\text{--}600\text{ cm}^{-1}$ range are attributed to deformations of the PO_3 groups. The low-frequency band below 300 cm^{-1} is identified as lattice vibrations, which are mostly caused by external modes.²⁷ A slight shift was observed when compared to the pure sample.¹³ The band assignments provided in Table II for the FT-IR and Raman fundamental modes of VO^{2+} -doped sample validate the presence of diphosphate groups in the title compounds.

Optical Analysis

The UV absorption spectrum is used to investigate the production of optically mediated transitions in crystalline materials. The absorption edge in the spectrum is analyzed to determine the optical absorption coefficient,

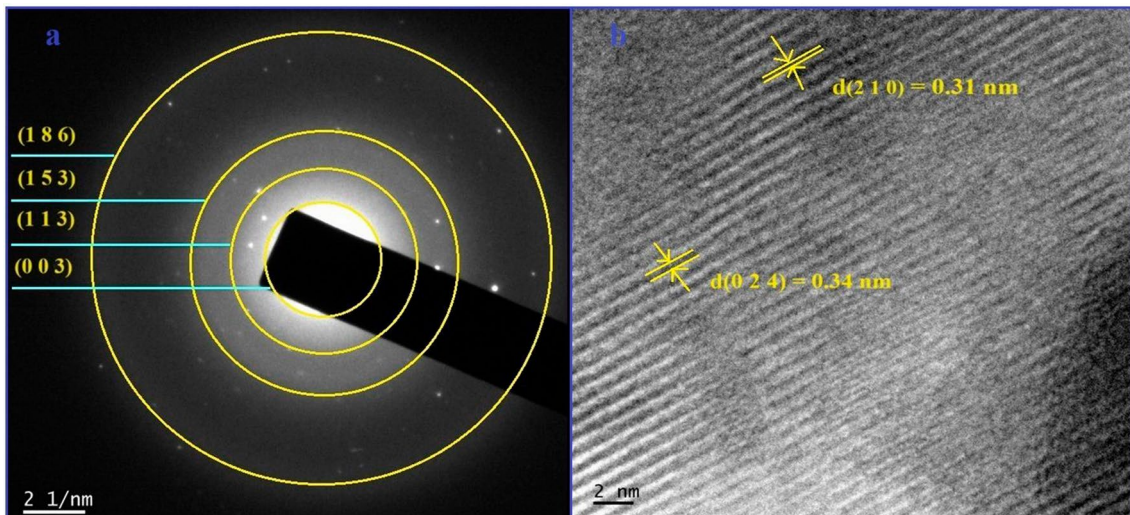


Fig. 8 (a) SAED pattern and (b) d-spacing of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

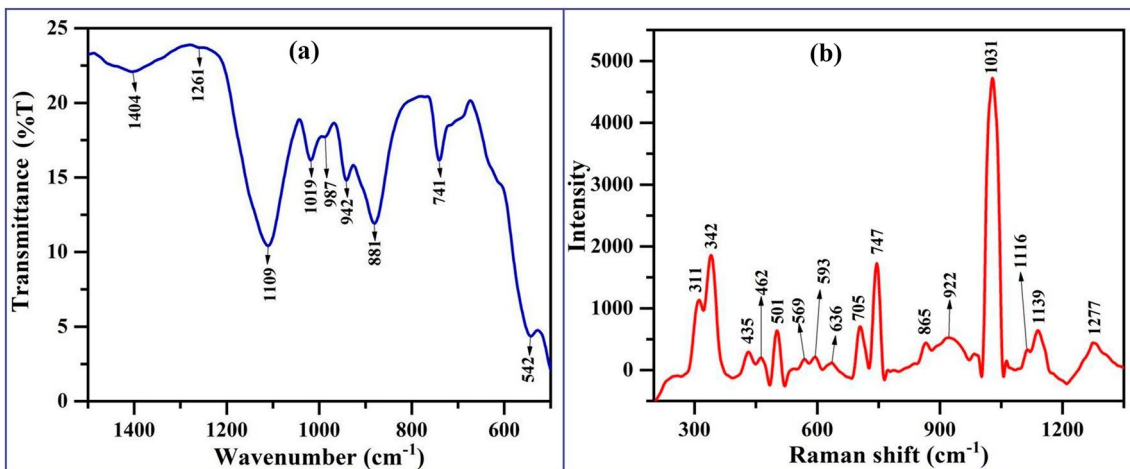


Fig. 9 (a) FTIR and (b) Raman vibrational spectra of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

Table II Assignment of FT-IR and Raman vibrational bands of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder

FT-IR	Raman	Assignment
1404	–	O–H bending vibration
1261, 1109	1277, 1139, 1116	ν_s (PO ₃)
1019	1031	ν_{as} (PO ₃)
987, 942, 881	922, 865	ν_s (P–O–P)
741	747, 705	ν_{as} (P–O–P)
–	636–569	δ_s (PO ₃)
542	501–311	δ_{as} (PO ₃)

band structure type, and energy band gap. Vanadium is paired with five or six oxygen atoms in a solid or aqueous medium. One of the oxygen atoms forms a double covalent bond with vanadium to generate the vanadyl ion.²⁸ Referring to the energy level scheme proposed by Ballhausen and Gray, the V⁴⁺ ion exhibits a d¹ configuration and possesses a ground state of ²D.⁶ The ²D state splits into ²T_{2g} and ²E_g in the presence of a pure octahedral crystal field. However, in the case of VO²⁺, it never exhibits pure octahedral symmetry (C_{4v}). Tetragonal symmetry results in a singlet ground state term ²T_{2g} and splits into ²B_{2g} and ²E_g. Two states ²B_{1g} and ²A_{1g} separate ²E_g and the ground state will be ²B_{2g} among these. The UV-Vis spectrum of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder was recorded at room temperature, as shown

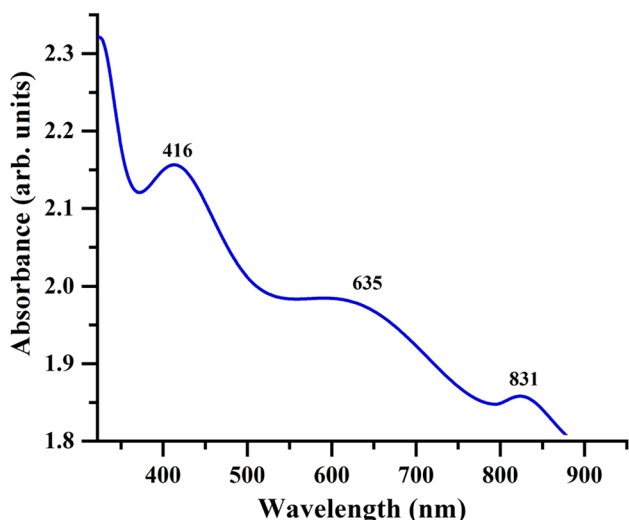


Fig. 10 Optical absorbance spectrum of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

in Fig. 10. Three bands are present in the absorption spectrum of the VO²⁺-doped sample at 831 (12,030 cm⁻¹), 635 (15,744 cm⁻¹), and 416 (24,032 cm⁻¹), respectively. The observed bands are associated with characteristic d-d transitions²⁹ and have been assigned to specific states as:

$$\Delta_{\perp} = {}^2 B_{2g} \rightarrow {}^2 E_g (d_{xy} \rightarrow d_{xz,yz}) \tag{6}$$

$$\Delta_{\parallel} = {}^2 B_{2g} \rightarrow {}^2 B_{1g} (d_{xy} \rightarrow d_{x^2-y^2}) \tag{7}$$

$$\Delta = {}^2 B_{2g} \rightarrow {}^2 A_{1g} (d_{xy} \rightarrow d_z^2) \tag{8}$$

The following relationships are used to evaluate the crystal field parameter, Dq, and the tetragonal field parameters, Ds and Dt:

$${}^2 B_{2g} \rightarrow {}^2 E_g = -3Ds + 5Dt = 12030 \text{ cm}^{-1} \tag{9}$$

$${}^2 B_{2g} \rightarrow {}^2 B_{1g} = 10Dq = 15744 \text{ cm}^{-1} \tag{10}$$

$${}^2 B_{2g} \rightarrow {}^2 A_{1g} = 10Dq - 4Ds - 5Dt = 24032 \text{ cm}^{-1} \tag{11}$$

By using the above equations, the parameters have been evaluated as: Dq = 1574 cm⁻¹, Ds = - 2903 cm⁻¹, and Dt = 664 cm⁻¹. The opposing signs found in the tetragonal field constants Ds and Dt suggest octahedral symmetry with tetragonal compression along the axis. The band head data and the corresponding transitions and calculated values are shown in Table III. The direct energy band gap (E_g) of the sample has been determined using:

Table III Observed absorption data of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder

Transitions from ² B _{2g}	Wave-length (nm)	Wave-number (cm ⁻¹)	Dq (cm ⁻¹)	Ds (cm ⁻¹)	Dt(cm ⁻¹)
² E _{2g}	831	12030	1574	- 2903	664
² B _{1g}	635	15744			
² A _{1g}	416	245032			

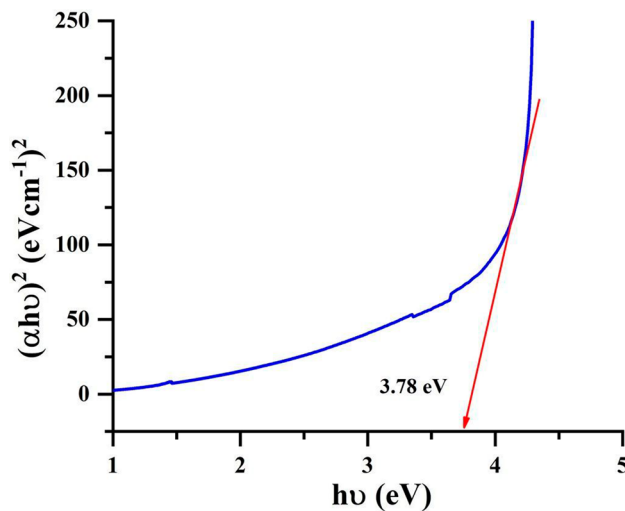


Fig. 11 Energy band gap of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

$$E_g = \frac{1240}{\lambda_c} \tag{12}$$

where λ_c is the cut-off wavelength and the evaluated band gap energy is 3.75 eV at the wavelength of 331 nm. Furthermore, the band gap energy can be determined by using Tauc’s formula which demonstrates the relationship between absorption coefficients¹²:

$$(\alpha hv)^{\frac{1}{n}} = A(hv - E_g) \tag{13}$$

where α, h, and ν represent as absorption coefficient, Plank’s constant, and the frequency of vibration, respectively. Exponent n varies depending on the types of transitions with the values 1/2, 2, 3/2, and 3 equivalent to authorize direct, allowed indirect, forbidden direct, and forbidden indirect respectively. A is a constant that depends on the transition probability and is known as the band tailing parameter. The band gap energy of the VO²⁺-doped sample has been determined graphically by plotting (αhv)² versus hv, as shown in Fig. 11. The amount of band gap energy was found to be 3.78 eV. Both the experimental and calculated band gap

energies are nearly equal. This type of pyrophosphate nanopowders may be used in optoelectronic devices.

Additional important optical characteristics that are connected to the VO²⁺-doped sample are the refractive index (R.I) and metallization criteria (*M*). The following expression was used to determine the refractive index (*n*) value for prepared nanopowder based on the optical energy band gap:

$$\frac{n^2 - 1}{n^2 + 1} = 1 - \frac{\sqrt{E_g}}{20} \quad (14)$$

The calculated refractive index (*n*) is 4.36 by using this equation. The metallization criteria (*M*) quality is measured using:

$$M = 1 - \frac{n^2 - 1}{n^2 + 1} \frac{\sqrt{E_g}}{20} \quad (15)$$

It has been stated that a substance was non-metallic if the *M* value was less than 1 and metallic if the *M* value was larger than 1.³⁰ The calculated *M* value is 0.909, according to which, the prepared pyrophosphate nanopowder was non-metallic in nature; these values are in agreement with reported values.¹³

EPR Analysis

Figure 12 shows the EPR spectrum of the VO²⁺-doped sample at room temperature which consists of parallel and perpendicular components. The VO²⁺ ions belong to the paramagnetic family and have electron spin (*S* = 1/2), nuclear spin (*I* = 7/2), C_{4v} symmetry, and just one stable natural isotope ⁵¹V which gives them a 3d¹ unpaired

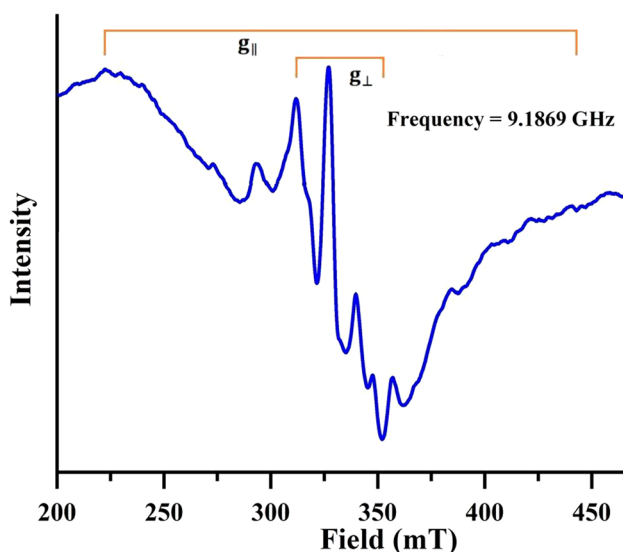


Fig. 12 EPR spectrum of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

electronic configuration.²⁹ Usually, VO²⁺-doped compounds have tetragonal distortion along the axis and octahedral symmetry. $g_{\parallel} < g_{\perp} < g_e$ is a necessary condition for tetragonally distorted octahedral site symmetry. The computed spin Hamiltonian parameters have been determined to be $g_{\parallel} = 1.954$, $g_{\perp} = 1.977$, and they satisfy the specified criteria. Furthermore, the hyperfine coupling constant values A_{\parallel} and A_{\perp} were found to be $172 \times 10^{-4} \text{ cm}^{-1}$ and $53 \times 10^{-4} \text{ cm}^{-1}$, respectively, which satisfies the requirement that $A_{\parallel} > A_{\perp}$. Through observation, $\frac{\Delta_{\parallel}}{\Delta_{\perp}} = 1.3$, and this value indicates tetragonal distortion of the VO²⁺ ions with the host lattice.

The following equations are proposed to compute the Fermi contact term, κ , the hyperfine coupling constant, *P*, and the molecular orbital coefficients such as β_1^2 , β_2^2 , and γ^2 based on optical absorption and EPR data.⁸:

$$g_{\parallel} = g_e \left(1 - \frac{4\lambda\beta_1^2\beta_2^2}{\Delta_{\parallel}} \right) \quad (16)$$

$$g_{\perp} = g_e \left(1 - \frac{4\lambda\gamma^2\beta_2^2}{\Delta_{\perp}} \right) \quad (17)$$

$$A_{\parallel} = P \left[-\frac{4}{7}\beta_2^2 - \kappa + (g_{\parallel} - g_e) + \frac{3}{7}(g_{\perp} - g_e) \right] \quad (18)$$

$$A_{\perp} = P \left[\frac{2}{7}\beta_2^2 - \kappa + \frac{11}{14}(g_{\perp} - g_e) \right] \quad (19)$$

where λ is the spin-orbit coupling constant (170 cm^{-1}) and g_e is the free electron (2.0023). The energy values for ${}^2B_{2g} \rightarrow {}^2E_g$ and ${}^2B_{2g} \rightarrow {}^2B_{1g}$ transitions are associated with Δ_{\perp} and Δ_{\parallel} . β_1^2 denotes the degree of in-plane σ bonding, β_2^2 denotes the degree of in-plane π bonding, and γ^2 measures out-of-plane π bonding. The hyperfine coupling constant, *P*, is found in the radial distribution of singular electrons linked to the wave function, which is expressed as $P = g_e g_N \beta_e \beta_N \langle r^{-3} \rangle$ where words in the expression have their usual meaning. The degree of electron orbital deformation at the vanadium nucleus is measured by the Fermi constant term, κ . Calculating the *P* value from the equation requires ignoring the second-order terms and taking into account negative values for A_{\parallel} and A_{\perp} ⁷:

$$P = \frac{7(A_{\parallel} - A_{\perp})}{6 + \frac{3\lambda}{2\Delta_{\perp}}} \quad (20)$$

The free ion *P* value for VO²⁺ is $160 \times 10^{-4} \text{ cm}^{-1}$. In this case, the computed *P* value is lower than the vanadyl free-ion value of $138 \times 10^{-4} \text{ cm}^{-1}$. This indicates the existence of a covalent nature in the vanadyl complexes such

that the smaller the P value, the greater the covalency. Additional isotropic values for g and A can be derived from:

$$g_{iso} = \frac{2g_{\perp} + g_{\parallel}}{3} \quad (21)$$

$$A_{iso} = \frac{2A_{\perp} + A_{\parallel}}{3} \quad (22)$$

The evaluated values of g_{iso} and A_{iso} are 1.969 and $92.67 \times 10^{-4} \text{ cm}^{-1}$, respectively.

$$\kappa = -\frac{A_{iso}}{P} - (g_e - g_{iso}) \quad (23)$$

The Fermi constant term, κ , is determined to be 0.64. The obtained g_{\parallel} , g_{\perp} , A_{\parallel} , A_{\perp} , β_1^2 , β_2^2 , and γ^2 values are represented in Table IV. The bonding nature is measured by β_1^2 , which has a value of 1 for complete ionic and 0.5 for complete covalence. The presence of covalent bonding in in-plane σ and π bonds is suggested by the β_1^2 and β_2^2 values which range from 0.5 to 1.0. Vanadyl oxygen bonds and their ligands are covalent due to the out-of-plane π -bond, which is shown by the γ^2 value. The near unity β_2^2 value indicates both weak π and strong ionic bonding between the vanadyl ions and pyrophosphate ligands. The weak contribution of vanadium's 4s orbital to vanadyl bond in the produced pyrophosphate is shown by the deviating κ value.

The covalency rates are described by $1 - \beta_1^2$ and $1 - \gamma^2$, which provide information about in-plane σ bonding and out-of-plane π bonding of vanadyl–oxygen and vanadium ions (V^{4+}), respectively. For this instance, $(1 - \beta_1^2) = 0.44$ and $(1 - \gamma^2) = 0.75$ demonstrate that in-plane σ -bonding is of a strong covalent nature, while out-plane π bonding is of a moderate covalent nature.

PL Analysis

The presence of PL emission bands could be caused by a variety of defects such as vacancies, dislocations, strain, atomic bond distortions in the reaction medium, the environment, and crystallites.⁷ The emission and excitation spectra of a prepared sample is shown in Fig. 13. Three emission peaks are seen in the UV and visible regions of the emission spectrum under the excitation wavelength of 321 nm. The minor peak, characterized by its lower intensity, is situated at 354 nm (3.50 eV) within the UV region, whereas the blue and green visible regions exhibit two broad peaks centered at 440 nm (2.82 eV) and 530 nm (2.34 eV), respectively. The main cause of visible

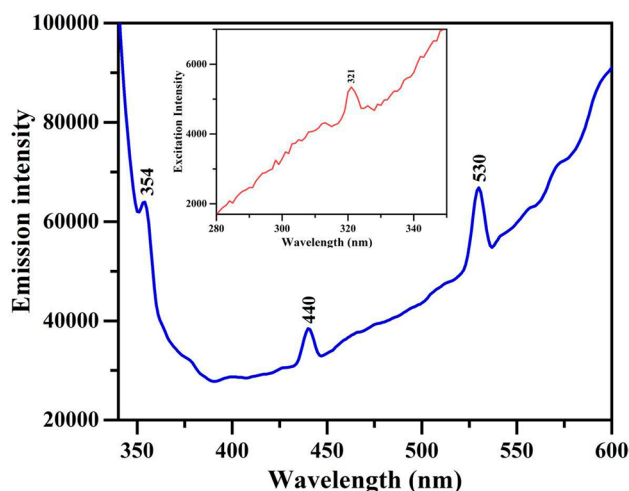


Fig. 13 Excitation and emission spectra of VO^{2+} -doped $Li_2Ba_3(P_2O_7)_2$ pyrophosphate nanopowder.

luminescence at 440 and 530 nm is intrinsic defects like oxygen vacancies, surface traps, and interstitials. A prominent UV emission in this investigation at 354 nm suggests that the sample has improved optical qualities and better crystal quality. The luminescence emission peaks at 440 and 530 nm were assigned to the following allowed transitions ${}^2A_{1g} \rightarrow {}^2B_{2g}$ and ${}^2B_{1g} \rightarrow {}^2B_{2g}$, respectively.^{13,29}

To understand the luminescent properties of the prepared sample, CIE 1931 chromaticity coordinates have been calculated based on the emission spectrum. The color coordinates of the sample are situated within the yellowish-green region with respective CIE coordinates of $x = 0.302$ and $y = 0.409$. This position is displayed on the CIE chromaticity diagram by using OSRAM-IP software, as shown in Fig. 14. The correlated color temperature (CCT) is calculated using the McCamy equation³¹ and the CIE 1931 chromaticity coordinates (x, y):

$$CCT = -437n^3 + 3601n^2 - 6861n + 5514.31 \quad (24)$$

here $n = \frac{(x-x_1)}{(y-y_1)}$ represents inverse slope of the line with $x_1 = 0.3320$ and $y_1 = 0.1858$. The corresponding color purity can be determined using³²:

$$\text{color purity} = \frac{\sqrt{(x-x_I)^2 + (y-y_I)^2}}{\sqrt{(x_d-x_I)^2 + (y_d-y_I)^2}} \quad (25)$$

Table IV EPR parameters for VO^{2+} -doped $Li_2Ba_3(P_2O_7)_2$ pyrophosphate nanopowder

g_{\parallel}	g_{\perp}	A_{\parallel}	A_{\perp}	g_{iso}	A_{iso}	$\frac{\Delta_{\perp}}{\Delta_{\parallel}}$	β_1^2	β_2^2	γ^2	$1 - \beta_1^2$	$1 - \gamma^2$
1.954	1.977	172	53	1.969	92.67	1.3	0.56	0.89	0.249	0.44	0.75

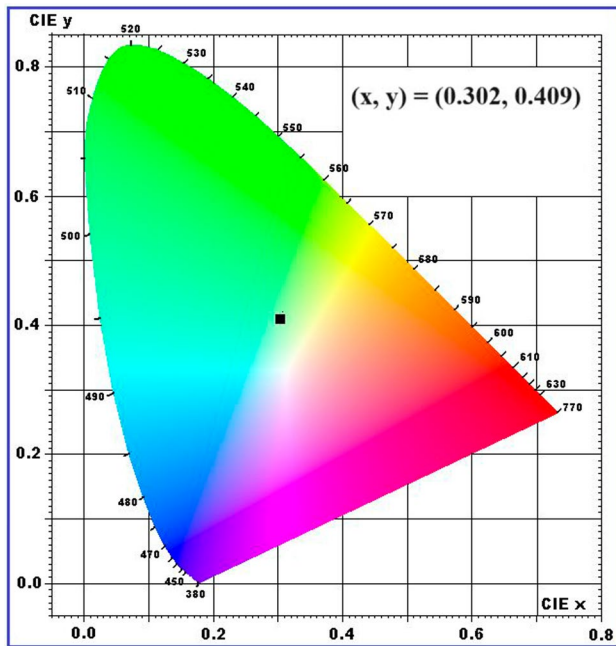


Fig. 14 CIE 1931 color chromatic image of VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder.

Among these, (x, y) represents the CIE chromaticity coordinates of the sample, (x_l, y_l) represents the CIE chromaticity coordinates of illuminant wavelength, while (x_d, y_d) corresponds to the color coordinates of the dominant wavelength and calculated color purity of 16%. The color rendering index (CRI) is an essential photometric for interpreting emission spectrum data. According to the CRI value, VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder exhibits acceptable emission properties. In the present study, the CCT, color purity, and CRI values are determined to be 6490 K, 16%, and 41%, respectively. These results indicate that the prepared sample emits a yellowish-green color making it potentially useful in display panels and other LED display devices.

Conclusions

VO²⁺-doped Li₂Ba₃(P₂O₇)₂ pyrophosphate nanopowder was synthesized using a solid-state reaction technique. The XRD pattern of the produced sample revealed an orthorhombic structure with space group 2P₁. The average crystallite size in the nano-range was determined and lattice cell parameters were evaluated for the prepared sample. SEM micrographs revealed irregularly agglomerated stone-like structures, and the elements Li, O, P, Ba, and V were verified to be present in the sample by the EDS spectrum. The HR-TEM images of the sample displayed stone-like agglomerated formations and the average particle size corresponded well with results obtained by the Scherrer and W–H techniques. The

fundamental modes of the phosphate ions were confirmed by FT-IR and Raman analyses. The crystal and tetragonal field parameters were determined as $Dq = 1574 \text{ cm}^{-1}$, $Ds = -2903 \text{ cm}^{-1}$, and $Dt = 664 \text{ cm}^{-1}$. Optical absorption and EPR studies revealed that the VO²⁺ ions were partially covalent and exhibited tetragonal compression in octahedral site symmetry concerning nearby ligands in the host lattice. The refractive index (n), determined as 4.36 with the help of an optical energy band gap of 3.78 eV, suggests that the material is useful for optical detectors and photo-electrical cells. The CIE chromaticity diagram confirms a yellowish-green emission at 321 nm excitation wavelength for the synthesized sample. CCT, CRI, and color purity values were 6490 K, 41%, and 16%, and, based on these results the sample would be useful for light-emitting diodes.

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Author Contributions NCA: Conceptualization, methodology, software, investigation, writing-original draft. GV: Analysis, analyzing data and editing. AVC: Visualization and formal analysis. RVSSNR: Supervised the research and critical revision of the article. All authors read and approved the final manuscript.

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Data Availability Data will be provided upon request.

Conflict of interest The authors declare that they have no conflict of interest.

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