

# **Toroidal Dipole All‑Dielectric Metasurfaces with High Sensitivity, High Figure of Merit, and Robustness for Refractive Index Sensing**

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#### **Abstract**

Refractive index sensing is of great signifcance in biological detection. Especially, all-dielectric metasurfaces can greatly improve the sensitivity of biological detection. However, the *Q* factor and electric feld enhancement of most metasurfaces are generally low, resulting in low sensitivity and fgure of merit (FOM). Meanwhile, fabrication tolerances may result in inability to achieve high-performance refractive index sensing. Here, we use fnite element method (FEM) simulation to design a conical hole structure on an all-dielectric metasurface. The toroidal dipole resonance based on a conical hole structure can achieve a large-area electric feld enhancement and a high *Q* factor, thereby achieving a sensitivity of 540 nm/ RIU and FOM of 154.3. Meanwhile, considering the real fabrication tolerance, the proposed structure can still achieve highsensitivity sensing when the conical hole structure changes the ellipsoidal structure. Therefore, the high sensitivity, high FOM, and robustness of the proposed structure make it highly signifcant for practical applications.

**Keywords** Metasurfaces · toroidal dipole · high sensitivity · robustness · refractive index sensing

## **Introduction**

Due to the advantages of high sensitivity, high selectivity, low cost, and so on, $1-3$  $1-3$  optical biosensors play an important role in modern biomedical, material, and environmental monitoring applications.

In recent years, metasurfaces<sup>[4](#page-7-2)[–6](#page-7-3)</sup> have emerged as a crucial area for advancing the development of optical sensing technology. Metasurfaces are optical devices composed of subwavelength structures that can be designed reasonably to achieve specific functions.<sup> $7-9$  $7-9$ </sup> For optical sensing, metasurfaces can confne light to micro/nanoscale electromagnetic hotspots to improve sensitivity. In addition, due to the important role played by the anopole mode in regulating the light field, $10,11$  $10,11$  the anopole metasurface can also be applied to optical sensing.[12](#page-7-8) Metasurface optical sensors have been applied in many works.<sup>[13](#page-7-9)-[16](#page-7-10)</sup>

Refractive index sensors are one of the most common types of optical biosensors.<sup>[17–](#page-7-11)[19](#page-7-12)</sup> When the refractive index of the analyte increases, it will cause a redshift of resonance.

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The sensitivity is defned as the ratio of the shift of the resonance peak to the change in refractive index. $^{20}$  In addition, the change in resonance intensity can also be used as a detection indicator for refractive index sensing. $2<sup>1</sup>$  However, the main problem currently limiting the performance of refractive index sensors is the weak interaction between the light feld and the analyte, resulting in low sensitivity. At present, most methods enhance the interaction between light and analytes by increasing the *Q* factor, including the coupling of localized surface plasmon resonance with surface lattice modes, high-refractive-index dielectric materials, and Fano resonance structures[.22](#page-7-15)–[24](#page-7-16) Due to the near-feld enhancement and strong nonlinear efects, toroidal dipole resonance also can signifcantly enhance the interaction between light and matter.<sup>[25,](#page-7-17)26</sup> Therefore, Wang et al.<sup>[27](#page-7-19)</sup> designed the toroidal dipole to achieve high sensitivity by using a strong electric feld generated near the microstructure interface around the toroidal dipole. Moreover, as a new method for achieving an infnite *Q* factor, bound states in the continuum (BIC) have been proposed.<sup>[27](#page-7-19)–[30](#page-7-20)</sup> High- $Q$  and high-sensitivity sensing can be achieved by quasi-BICs. $31-33$  $31-33$  Although the BIC can achieve high *Q* factor and high fgure of merit (FOM), most studies have found that electric feld enhancement is localized in a small area, resulting in weak interaction between light and analytes, and the sensitivity is still not suboptimal.

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Plasma plays a crucial role in confning and manipulating local electromagnetic felds. However, in optical frequencies, metals exhibit signifcant losses, leading to a low *Q* factor. Moreover, fabrication tolerances can reduce the *Q* factor, which results in an inability to achieve high-performance refractive index sensing. Due to the low loss of dielectric material, all-dielectric metasurfaces with high *Q* can be achieved. Therefore, we have designed a conical hole structure for all-dielectric metasurfaces. The toroidal dipole resonance mode achieved by using the conical hole structure not only can achieve a high *Q* factor, but also can achieve large-area electric feld enhancement, thus achieving high refractive index sensitivity sensing and high FOM. We also confrm the strong robustness of the structure.

#### **Structure and Model**

Figure [1](#page-1-0) shows the designed all-dielectric conical hole unit structure. The side length *L* of the unit is 1 μm, height *H* is 0.2 μm, and the upper diameter *D* of the conical hole is  $0.7 \mu$ m. The material is glass (LaSF), with a fixed refractive index of 1.8. Here, the fnite element method (FEM) is



<span id="page-1-0"></span>**Fig. 1** (a) The three-dimensional unit structure of the metasurface; (b) cross-section of the unit structure.

used for simulation, with the electric feld polarized in the *X* direction and the wave vector incident perpendicular to the metasurface in the *Z* direction. Periodic conditions are set in the *X* and *Y* directions, and the *Z* direction is defned as a perfectly matched layer. To avoid interference, the monitor is placed at a distance of 10 μm from the surface of the structure.

### **Results and Discussion**

Firstly, the efect of the conical hole bottom radius on the transmission of the structure was studied. The circular hole can obtain two obvious resonances when the bottom radius is 0.35  $\mu$ m, as indicated in Fig. [2a](#page-1-1). As the bottom radius of the conical hole decreases to  $0 \mu m$ , the resonance line width of long wavelengths is signifcantly reduced, while the change in short wavelength resonance is not very signifcant. The narrower the resonance peak, the higher the *Q* factor obtained. Therefore, the bottom radius of the conical hole chosen here is 0 μm for further research. As shown in Fig. [2b](#page-1-1), the wavelengths of the two resonances are 1.087 μm and 1.255 μm, and the corresponding *Q* factors are 1767.4 and 173.7. Compared to the *Q* factor of resonance at 1.255 μm, the *Q* factor of resonance at 1.087 μm is about 10 times higher.

A higher *Q* factor does not necessarily lead to high refractive index sensitivity. Therefore, these two resonance modes need further research. To analyze the electromagnetic resonance modes of these two resonances, multipole decomposition can be performed by integrating the current density of the structure in the Cartesian coordinate system. $34,35$  $34,35$  $34,35$ Multipole resonance can be written in the form of the following current description:



<span id="page-1-1"></span>**Fig. 2** (a) Transmission with varying bottom radius; (b) transmission of the bottom radius of 0 μm.

Electric dipole (ED):

$$
P = -\frac{1}{iw} \int j d^3 r \tag{1}
$$

Magnetic dipole (MD):

$$
M = \frac{1}{2c} \int (r \times j) d^3 r \tag{2}
$$

Toroidal dipole (TD):

$$
T = \frac{1}{10c} \int \left[ (r \cdot j)r - 2r^2 j \right] d^3r \tag{3}
$$

Electric quadrupole (EQ):

$$
Q_{\alpha\beta} = -\frac{1}{2iw} \int \left[ r_{\alpha} j_{\beta} + r_{\beta} j_{\alpha} - \frac{2}{3} (r \cdot j) \delta_{\alpha\beta} \right] d^3 r \tag{4}
$$

Magnetic quadrupole (MQ):

$$
M_{\alpha\beta} = \frac{1}{3c} \int \left[ (r \times j)_{\alpha} r_{\beta} + (r \times j)_{\beta} r_{\alpha} \right] d^3 r
$$
 (5)

where *j* is the surface current density, *c* is the speed of light in vacuum, and *r* is the displacement vector. Only ED, MD, TD, EQ, and MQ have been calculated here, as shown in Fig. [3](#page-2-0)a. It can be observed that the resonance at 1.087 μm is mainly EQ and MD, while the resonance at 1.255 μm is mainly TD resonance. Meanwhile, the impedance of the metasurface can be calculated by the impedance formula. The formula is as follows: $36$ 

$$
Z = \sqrt{\frac{(1 + S_{11})^2 - S_{21}^2}{(1 - S_{11})^2 - S_{21}^2}}
$$
(6)

where  $S_{11}$  and  $S_{21}$  represent the reflection and transmission, respectively. As shown in Fig. [3](#page-2-0)b, the effective impedance of the two resonances is  $Z = 0.02 + 1.09i$  and  $Z = 0.00 + 0.79i$ . Because the transmission of the two resonances approaches zero, the real part of the impedance is close to zero, and the imaginary part of the impedance is close to  $1<sup>37</sup>$  $1<sup>37</sup>$  $1<sup>37</sup>$ 

Since it is diferent from traditional EDs and MDs, the TD can greatly promote the interaction between light and matter, and is extremely sensitive to environmental changes. Equations ([7\)](#page-2-1) and [\(8](#page-2-2)) are the electric feld radiation of tradi-tional dipole and toroidal dipole resonance, respectively.<sup>[38](#page-8-5)</sup> From one of the equations, it can be seen that, compared to dipole resonance, the electric feld of the TD is more sensitive to changes in environmental refractive index. By utilizing the characteristics of the TD, highly sensitive biosensing can be achieved. For refractive index sensing, the TD plays an important role, and future research needs to focus on TDs.

<span id="page-2-1"></span>
$$
E_P = n^2 k_0^2 \left(\hat{r} \times \hat{r} \times \frac{\hat{P}}{r}\right) \tag{7}
$$

<span id="page-2-2"></span>
$$
E_T = n^3 k_0^3 \left(\hat{r} \times \hat{r} \times \frac{\hat{T}}{r}\right)
$$
 (8)

To further analyze the resonance modes, we analyzed the electromagnetic felds of these two resonances, as shown in Fig. [4](#page-3-0). Figure [4](#page-3-0)a, c and b, d show the cross-section position at  $Z=0$  µm and  $X=0$  µm, respectively. Figure [4](#page-3-0)a shows the electric field at  $1.255 \mu m$ . The black arrow indicates the current vector, and the blue arrow indicates the direction. The direction of the middle electric feld and the upper and lower electric felds are opposite. The middle and upper electric felds can form an upward magnetic feld, while the middle and lower magnetic felds can form a downward magnetic feld, which is also proven by Fig. [4b](#page-3-0). The



<span id="page-2-0"></span>Fig. 3 (a) Scattering power of multipole decomposition; (b) effective impedance of the metasurface.



<span id="page-3-0"></span>**Fig. 4** (a), (c) Electric feld and (b), (d) magnetic feld of the conical hole at (a), (b) 1.255 μm and (c), (d) 1.087 μm, respectively. The black arrows are the current vector, the white arrows are the magnetic feld vector, and the blue arrow indicates the direction (Color fgure online).

white arrow in Fig. [4](#page-3-0)b represents the magnetic field vector, while the blue arrow represents the direction. The left upward magnetic feld and the right downward magnetic feld form the TD, which is also the main resonance mode of 1.255 μm. Figure [4](#page-3-0)c shows the electric feld at 1.087 μm has four directions, which can form an EQ. In Fig. [4](#page-3-0)d, the magnetic feld propagates only along the *y*-axis. Therefore, an MD is formed. Analyzing the electric and magnetic felds at 1.087 μm shows that EQ and MD are formed, which correspond to the multipole decomposition results in Fig. [3](#page-2-0)a.

In addition to considering the resonance mode, attention should also be paid to the location and the size of the electric feld enhancement area. Figure [5](#page-4-0)a and b shows the crosssection of the electric feld of the resonance of 1.255 μm at  $Y=0$  μm and  $X=0$  μm, respectively. As shown in Fig. [5c](#page-4-0) and d, the cross-section is the electric feld of the resonance of the 1.087  $\mu$ m at *Y*=0  $\mu$ m and *X*=0  $\mu$ m, respectively. The electric fields of 1.255  $\mu$ m and 1.087  $\mu$ m show signifcant enhancement. However, the location of these two resonance enhancements is diferent. The resonance electric felds of 1.255 μm and 1.087 μm are mainly located inside and outside of the conical hole, respectively. Meanwhile, the diference in the size of the electric feld enhancement area is not signifcant.

Previous studies have confrmed that the thickness of the analyte layer has a signifcant impact on frequency shift. Firstly, the frequency shift will increase as the thickness of the analyte layer increases. When the thickness of the analyte layer increases to a threshold, no matter how the thickness of the analyte layer increases, the frequency shift will not increase significantly.<sup>39</sup> The main reason for this phenomenon is that the electric feld intensity decays exponentially in the vertical direction of the sample, resulting in a weak interaction between the electric feld and the analyte. Therefore, when the analyte increases to a certain thickness, the frequency shift of the resonance peak will not change significantly.

According to the results shown in Fig. [5](#page-4-0), the electric feld is still enhanced at 0.5 μm from the surface of the structure. Therefore, we frst investigated the variation in transmission with different thicknesses of analytes. As shown in Fig. [6](#page-4-1)a, the analyte has a refractive index of 1.5, and its transmission spectrum varies with its thickness. As the thickness of the analyte increases, the resonance peak of the two white



<span id="page-4-0"></span>**Fig. 5** Electric feld of the conical hole at (a), (b) 1.255 μm and (c), (d) 1.087 μm, respectively.



<span id="page-4-1"></span>**Fig. 6** (a) Transmission with varying analyte thickness; (b) transmission at 1-μm-thick analyte with analytes of diferent refractive indexes. The white dotted line in (a) shows the trend of the resonance with increasing analyte thickness.

dotted lines does not continue to increase at a thickness of about 1 μm. Therefore, the thickness of the analyte is chosen to be 1 μm, and the transmission obtained by varying the refractive index of the analyte is shown in Fig. [6](#page-4-1)b. As the refractive index of the analyte increases, the resonance peak exhibits a signifcant redshift. After calculation, the sensitivity of the resonance at 1.255 μm can reach 540 nm/ RIU with a FOM (the ratio of the sensitivity to the full width of the half-peak) of 154.3, and sensitivity of the resonance at 1.087 μm can reach 749.6 nm/RIU. However, the resonance at 1.087 μm shows a signifcant decrease in intensity as the refractive index changes, which is not conducive to the detection of the signal. Therefore, resonance of 1.255 μm was chosen here for refractive index sensing.

In addition, compared to the previous all-dielectric toroidal dipole resonance structure reported in Table [I,](#page-5-0) the sensitivity and FOM obtained here are signifcantly increased. Although some studies have higher FOM values, the sensitivity is lower. The high FOM is because they can produce a very narrow line width and obtain a high *Q* factor. And the low sensitivity is mainly because the local electric feld enhancement is small, or the electric feld enhancement is located inside of the structure, resulting in a weak interaction between the electric feld and the analyte. Our structure can achieve higher sensitivity because the electric feld enhancement has a large area, and the electric feld enhancement is mainly outside the structure, so it can fully enhance the interaction between the electric feld and the analyte.

Considering the real fabrication tolerance, the conical hole is more difficult to fabricate in practice, and an ellipsoidal hole may be obtained in the end. Therefore, the conical hole is changed to an ellipsoid hole. The long axis *L*1 is 0.7 μm, and half of the short axis *L*2 is 0.2 μm, as shown in Fig. [7a](#page-6-0). When the conical hole is changed to an elliptical hole, the transmission is obtained in Fig. [7](#page-6-0)b, and the *Q* factor of resonance at 1.222 μm is 54. Compared to the electric feld of the conical hole in Fig. [5,](#page-4-0) the electric feld of the ellipsoidal hole structure shown in Fig. [7c](#page-6-0) and d is weak, which leads to a low *Q* factor. However, there is an increase in the area of the electric feld enhancement.

Next, we investigated the effect of the ellipsoidal hole on refractive index sensing. When the ellipsoidal hole covers the analyte with a thickness of  $1 \mu m$ , the sensitivity of the TD obtained from the simulation in Fig. [8](#page-6-1)a can reach 590 nm/RIU and FOM of 62.6. Although structural changes lead to low *Q* factors, the increase in the area of the electric feld enhances the light–matter interaction. Therefore, it can be found that the fabrication tolerance has very little efect on the refractive index sensing, which indicates that the structure has a certain robustness. This is of great signifcance for the practical application of the structure. In addition, when the height  $H$  of the conical hole is fixed, the resonance is redshifted, and the line width of the resonance peak is also narrowed as the thickness of the structure increases, as shown in Fig. [8b](#page-6-1). Multiple resonance peaks also appear as the thickness of the structure increases. Multiple resonance peaks can appear in more abundant electromagnetic resonance modes, so the sensitivity detection of multiple resonance peaks can be realized based on the different thicknesses of the structure and multiple wavelengths, which can be further optimized to improve the refractive index sensitivity and FOM.

#### **Conclusion**

The all-dielectric conical hole structure obtains toroidal dipole resonance, which leads to signifcant enhancement of light–matter interaction and large-area electric feld. Moreover, the refractive index sensitivity and FOM can reach 540 nm/RIU and 154.3, respectively. Compared to the previous all-dielectric toroidal dipole resonance metasurfaces, the conical hole structure indicates a substantial improvement in sensing performance. The modifcation of the conical hole into an elliptical hole retains high sensitivity, confrming that the structure has a certain robustness, which is of great signifcance for practical application. At the same time, by changing the thickness of the structure, multiple resonances can be realized, and thus high-sensitivity

<span id="page-5-0"></span>**Table I** Performance index parameters of refractive index sensing based on a toroidal dipole all-dielectric metasurface

Structure	Material	Sensitivity	<b>FOM</b>	Year
Rectangular microporous structure	Silicon and quartz (loss)	161 nm/RIU	$\tilde{\phantom{a}}$	$2020^{40}$
Asymmetric two parallel block structure	Titanium oxide and quartz (lossless)	$80.6$ nm $/RIU$	$80.6$ RIU <sup>-1</sup>	$2020^{41}$
Two semicircles	Silicon and quartz (lossless)	$70 \text{ nm}$ /RIU	$2970$ RIU <sup>-1</sup>	$2022^{42}$
Asymmetric X-type block structure	Silicon and quartz (lossless)	321 nm/RIU	5262 RIU <sup>-1</sup>	$2023^{43}$
Conical hole structure	Glass (LaSF) (lossless)	540 $nm/RIU$	$154.3$ RIU <sup>-1</sup>	This work





<span id="page-6-0"></span>**Fig. 7** (a) The three-dimensional image and cross-section of the ellipsoidal hole; (b) transmission of the ellipsoidal hole; electric feld of the ellipsoidal hole in the (c) *XZ* and (d) *YZ* planes.



<span id="page-6-1"></span>**Fig. 8** (a) Transmission of an ellipsoidal hole structure at 1-μm-thick analyte with analytes of diferent refractive indexes; (b) transmission of conical hole structure varying with increasing thickness of the structure.

detection at multiple wavelengths can also be achieved based on multiple resonance modes.

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**Data Availability** The datasets are available from the corresponding author on reasonable request.

**Conflict of interest** The authors declare no confict of interest.

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