



# Superconductivity and Weak Anti-localization at $\text{KTaO}_3$ (111) Interfaces

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## Abstract

The intersection of two-dimensional superconductivity and topologically nontrivial states hosts a wide range of quantum phenomena, including Majorana fermions. We report on the observation of two-dimensional superconductivity and weak anti-localization at the  $\text{TiO}_x/\text{KTaO}_3$  (111) interfaces. A remnant, saturating resistance persists below the transition temperature as superconducting puddles fail to reach phase coherence. Signatures of weak anti-localization are observed near the superconducting transition, suggesting the coexistence of superconducting fluctuations and quantum coherent quasiparticle effects. The superconducting interfaces show roughly one order of magnitude larger weak anti-localization correction, compared to non-superconducting interfaces, alluding to a relatively large coherence length in these interfaces.

**Keywords** 2D superconductivity · weak anti-localization ·  $\text{KTaO}_3$

## Introduction

A combination of broken inversion symmetry and strong spin–orbit coupling in two-dimensional (2D) superconductors gives rise to mixed-parity superconductivity,<sup>1</sup> topological Weyl superconductivity,<sup>2</sup> a superconducting diode effect,<sup>3</sup> and an upper critical field exceeding the Pauli–Chandrasekhar–Clogston limit.<sup>4,5</sup> 2D weak anti-localization has been used to probe surface states in topologically nontrivial systems.<sup>6,7</sup> The recent discovery of 2D superconductivity<sup>8</sup> and predictions of topologically nontrivial states<sup>9</sup> at the  $\text{KTaO}_3$  (111) surface makes this material system a candidate platform for the coexistence of topologically nontrivial electronic states and unconventional superconductivity.

$\text{KTaO}_3$  is an incipient ferroelectric,<sup>10</sup> in which superconductivity emerges at low temperatures in heavily doped samples.<sup>11</sup> A robust 2D electron system is reported at the interfaces of  $\text{KTaO}_3$  with  $\text{LaTiO}_3$ ,<sup>12</sup>  $\text{LaVO}_3$ ,<sup>13</sup>  $\text{EuO}$ ,<sup>14</sup>  $\text{LaAlO}_3$ ,<sup>15</sup>

$\text{TiO}_x$ <sup>16</sup> and  $\text{LaCrO}_3$ .<sup>16</sup> The  $\text{KTaO}_3$  conduction states are derived from Ta  $5d$  and have a smaller effective mass and higher mobility and spin–orbit coupling compared to Ti  $3d$  states in  $\text{SrTiO}_3$ .<sup>17,18</sup> Spin–orbit coupling lifts the degeneracy of the Ta  $5d$  states and splits them into  $J = 3/2$  and  $J = 1/2$  with a 0.4-eV energy gap, where  $J$  is the total angular momentum.<sup>19</sup> Recently, an exotic 2D superconductivity was discovered at the (111)<sup>8</sup> and (110)<sup>20</sup>  $\text{KTaO}_3$  interfaces with  $\text{EuO}$  and  $\text{LaAlO}_3$ , which shows nearly two orders of magnitude enhancement in the critical temperature of superconductivity ( $T_C$ ) compared to its 3D counterpart.<sup>11</sup> Interestingly,  $\text{KTaO}_3$  (100) interfaces do not show a superconducting transition. The superconducting state in the  $\text{KTaO}_3$  (111) surface is highly susceptible to the interfacial structure, and a remnant resistance is observed below the superconducting transition temperature.<sup>21</sup> This failed superconductor state<sup>22</sup> is an ideal platform for the experimental realization of simultaneous superconductivity and nontrivial topology.

Here, we report on the observation of a superconducting transition at the  $\text{TiO}_x/\text{KTaO}_3$ (111) interfaces. A true superconducting ground state ( $R_s = 0$ ), however, does not emerge as the superconducting puddles fail to reach phase coherence. Signatures of weak anti-localization are observed below the superconducting transition temperature, suggesting the coexistence of superconductivity and topologically nontrivial states at the  $\text{KTaO}_3$  (111) surfaces.

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## Materials and Methods

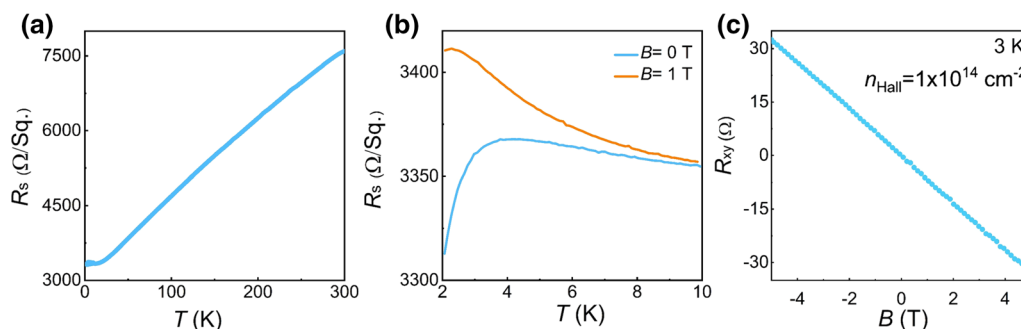
Mobile carriers were introduced to the (111) surface of the  $\text{KTaO}_3$  single crystals using a 3-nm  $\text{TiO}_x$  layer which induces oxygen vacancies. Here, the  $\text{TiO}_x$  layer acts as an oxygen getter and is grown using an oxide molecular beam epitaxy system with  $2 \times 10^{-10}$  Torr base pressure. An ultra-high purity Ti source from a high-temperature effusion cell (Veeco) was used to grow a  $\text{TiO}_x$  layer. The substrate temperature was kept at  $400^\circ\text{C}$  during growth to create an abrupt interface. Recently, atomically abrupt interfaces were demonstrated on  $\text{KTaO}_3$  interfaces grown at  $600^\circ\text{C}$  using an EELS map.<sup>23</sup> The Ti adatoms leach oxygen from  $\text{KTaO}_3$ , forming a  $\text{TiO}_x$  layer, and donating itinerant charge carriers to a Ta  $5d$ -derived conduction band in  $\text{KTaO}_3$ . The reflection high-energy electron diffraction, measured during deposition, confirms the growth of an amorphous  $\text{TiO}_x$  on the (111)  $\text{KTaO}_3$  surface (Supplementary materials, S1). Magneto-transport measurements were performed using the Van der Pauw configuration, and gold contacts were deposited using a sputter system at the corners of the samples through a shadow mask. The temperature-dependent magneto-transport measurements were carried out in a Quantum Design physical property measurement system with a lock-in amplifier (SR830; Stanford Research Systems) in AC mode with an excitation current of  $10 \mu\text{A}$  and a frequency of  $13.33 \text{ Hz}$ . Sub-Kelvin magneto-transport measurements were carried out in a Triton dilution refrigerator (Oxford Instruments).

Oxygen vacancies introduce itinerant electrons to the Ta  $5d$ -derived surface states. The conduction electrons at the low-temperature limit are derived from  $J = 3/2$ , Ta  $5d$  states due to the large spin–orbit coupling gap in  $\text{KTaO}_3$  ( $0.4 \text{ eV}$ )<sup>17,19</sup>. Figure 1(a) shows a metallic behavior,  $dR/dT > 0$ , in sheet resistance with the temperature extending from room temperature to  $\sim 15 \text{ K}$ . Here, oxygen stoichiometry plays an important role in transport phenomena.

The oxygen vacancies donate itinerant charge carriers to the  $\text{KTaO}_3$  conduction band and, similar to other point defects,<sup>24</sup> scatter itinerant carriers.<sup>25</sup> The transport in  $\text{TiO}_x$ , however, is negligible, since this layer is only  $3 \text{ nm}$  and expected to have low mobility. The sheet resistance changes somewhat linearly with temperature in this range. A resistance upturn emerges below  $15 \text{ K}$ , followed by a sharp drop below  $3 \text{ K}$  (Fig. 1(b)). The abrupt drop in sheet resistance is consistent with recently discovered 2D superconductivity at the (111)  $\text{KTaO}_3$  interface.<sup>8</sup> Hall measurements were performed to determine the sheet carrier density. The Hall carrier density,  $n = -1/(eR_H)$ , where  $R_H$  is the Hall coefficient and  $e$  is the elementary charge. The Hall coefficient,  $R_H = dR_{xy}/dB$ , is extracted from a linear fit to the transverse resistance shown in Fig. 1c. The sheet carrier density is  $\sim 1 \times 10^{14} \text{ cm}^{-2}$  at  $3 \text{ K}$ . This carrier density is consistent with optimal doping for the critical temperature of superconductivity in (111)  $\text{KTaO}_3$  interfaces.<sup>8</sup>

## Results and Discussion

The residual resistivity ratio ( $(\rho_{300\text{K}}/\rho_{2\text{K}})$ ) is 2.3 and the carrier mobility increases from  $\sim 8 \text{ cm}^2/\text{Vs}$  at room temperature to  $\sim 19 \text{ cm}^2/\text{Vs}$  at  $3 \text{ K}$ . The moderate enhancement of the carrier mobility, despite the screening of the longitudinal optical phonons at low temperatures, can be explained by the interfacial scattering of itinerant electrons.<sup>26–28</sup> The spatial distribution of “two-dimensional” charge carriers controls their exposure to the interfacial structure and, as a result, the mean free path of charge carriers. Here, despite the modest low-temperature carrier mobility, the sheet resistance remains below the 2D Mott–Ioffe–Regel limit ( $\sim 20 \text{ k}\Omega/\square$ ). Figure 1b shows a growing positive magnetoresistance with decreasing temperature ( $10\text{--}2 \text{ K}$ ). The positive magnetoresistance, particularly above  $4 \text{ K}$ , cannot be explained by the emergence of superconductivity alone, and could be partially due to the weak anti-localization correction to the



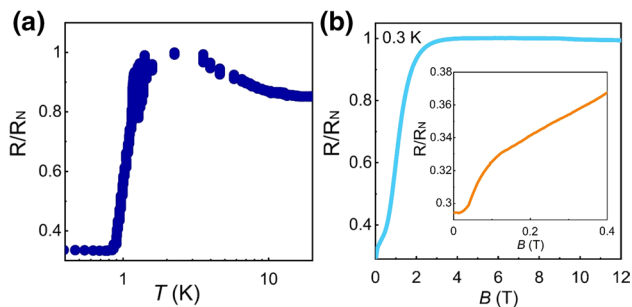
**Fig. 1** Normal state electronic transport at the  $\text{TiO}_x/\text{KTaO}_3(111)$  interfaces. (a) Sheet resistance with temperature ( $300\text{--}2 \text{ K}$ ) showing a linear scaling. (b) Magnetic field dependence of the sheet resistance–

temperature behavior ( $10\text{--}2 \text{ K}$ ). (c) Transverse magnetoresistance at  $3 \text{ K}$ , resolving the 2D carrier density ( $\sim 1 \times 10^{14} \text{ cm}^{-2}$ )

longitudinal resistance. 2D electron systems at the surface of the  $\text{KTaO}_3$  show large coherence length and signatures of weak anti-localization.<sup>16,25,29,30</sup>

Figure 2a shows the normalized resistance with temperature from 20 to 0.1 K. The resistance at 2 K and the zero field was used as normal state resistance ( $R_N$ ) in Fig. 2. The sharp drop in resistance is consistent with the observed superconducting transition at the interfaces of (111)  $\text{KTaO}_3$  with  $\text{EuO}$  and  $\text{LaAlO}_3$ .<sup>8</sup> A remnant resistance, however, is observed below the superconducting transition temperature (mid-point  $T_C \sim 1.1$  K). The sheet resistance saturates to a nonzero value below the transition temperature, which is insensitive to the presence of cryo-filters, excluding the possibility of radiation thermalization. Furthermore, the  $\text{KTaO}_3(111)/\text{LaCrO}_3$  interfaces, in which the normal state resistance is above the 2D Mott–Ioffe–Regel limit ( $\sim 33$   $\text{k}\Omega/\square$  at 3 K), do not show an abrupt drop in sheet resistance (Supplementary information, S2). Recently, a gate tunable remnant resistance was reported at the  $\text{KTaO}_3(111)/\text{LaAlO}_3$  interfaces below the superconducting transition temperature,<sup>21</sup> highlighting the role of interfacial structure on the emergence of a true superconducting ground state ( $R_s = 0$ ). A residual resistance has been observed in a wide range of 2D superconductors.<sup>31–34</sup> Here, the remnant resistance below the superconducting transition provides a unique platform for the experimental realization of 2D superconducting fluctuations coexisting with weak anti-localization.

The normalized longitudinal magnetoresistance shows that the relative change of resistance with the magnetic field ( $R_{5T} - R_{0T}/R_{0T} = 0.24$ , at 0.3 K) is large compared to the resistance change with temperature ( $R_{3K} - R_{0.3K}/R_{0.3K} = 0.198$ , at 0 T), alluding to the presence of both pair formation/breaking and weak anti-localization corrections in sheet resistance below the transition temperature.<sup>35</sup> Furthermore, a sharp change in the resistance with

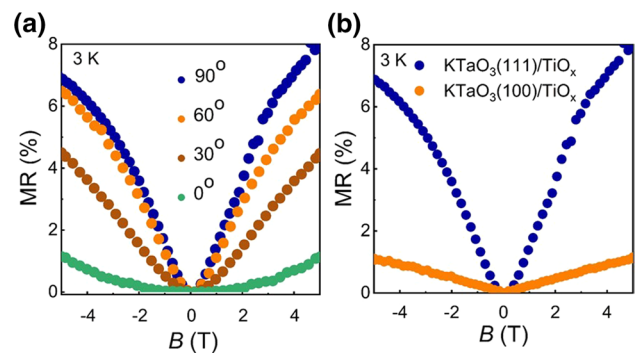


**Fig. 2** Superconducting transition at the  $\text{TiO}_x/\text{KTaO}_3(111)$  interfaces. (a) Superconducting transition with temperature (mid-point  $T_C \sim 1.1$  K); a remnant, saturating resistance is observed below the superconducting transition temperature. (b) Longitudinal magnetoresistance shows the superconducting transition and low field signatures of weak anti-localization (inset) at 0.3 K; the resistance at 2 K and the zero field was used as normal state resistance ( $R_N$ )

the magnetic field is observed at low field (inset in Fig. 2), consistent with the weak anti-localization.<sup>36</sup> The low field magneto-conduction, however, could not be explained by the Hikami–Larkin–Nagaoka model<sup>37</sup> due to the mixed weak anti-localization and superconducting corrections (Supplementary materials, S3).

The angle-dependent longitudinal magnetoresistance was measured to confirm the presence of the weak anti-localization effect. Figure 3a shows a transition from linear positive magnetoresistance to a parabolic behavior, with rotating the magnetic field from out-of-plane ( $90^\circ$ ) to in-plane ( $0^\circ$ ), respectively, suggesting a 2D weak anti-localization correction. To parse out the superconducting and weak anti-localization components, the longitudinal magnetoresistance was measured and compared between superconducting,  $\text{KTaO}_3(111)$ , and non-superconducting,  $\text{KTaO}_3(100)$ , interfaces (Fig. 3b). Both interfaces show a positive and linear magnetoresistance with the out-of-plane magnetic field. The superconducting interface, however, shows stronger weak anti-localization correction to resistance. The large magnetoresistance at (111) interfaces could also be explained by the pre-formed Cooper pairs.<sup>35</sup> The in-plane magnetoresistance of the superconducting interface shows only 1% positive magnetoresistance at 3 K and 5 T, suggesting that the pair-breaking correction could not explain the large positive magnetoresistance at the superconducting interfaces.

To briefly summarize the results, our main findings are as follows: (1)  $\text{TiO}_x/\text{KTaO}_3(111)$  interfaces show an abrupt superconducting transition; (2) The superconducting transition is sensitive to the normal state resistance and a nonzero, saturating resistance persists below the transition temperature; and (3) superconducting transition emerges near weak anti-localization, suggesting that superconducting fluctuations coexist with quantum coherent quasiparticle effects.



**Fig. 3** Weak anti-localization at the  $\text{TiO}_x/\text{KTaO}_3$  interfaces. (a) Angle-dependent magnetoresistance at the  $\text{TiO}_x/\text{KTaO}_3(111)$  interface; the transition from positive linear (out-of-plane field) to parabolic (in-plane field) suggests a 2D weak anti-localization. (b) Out-of-plane ( $90^\circ$ ) magnetoresistance shows weak anti-localization in superconducting, (111), and non-superconducting, (100),  $\text{TiO}_x/\text{KTaO}_3$  interfaces

The first important conclusion from these results is that the emergence of superconductivity at the  $\text{KTaO}_3$  interfaces depends strongly on the interfacial structure. Here, interfacial defects, microstructure, and inhomogeneity could suppress superconducting order parameters, and give rise to a remnant resistance below the transition temperature.  $\text{KTaO}_3$ , unlike  $\text{SrTiO}_3$ , does not experience structural instability and remains cubic at low temperature.<sup>17,38</sup> This excludes structural domains<sup>39–41</sup> as the source of the observed superconducting behavior. Here, the transition could be sensitive to the relaxation time of charge carriers, as the interfaces with sheet resistance above the Mott–Ioffe–Regel limit ( $h/\tau \sim E_F$ , where  $h$ ,  $\tau$ , and  $E_F$  are Planck’s constant, relaxation rate, and Fermi energy, respectively) do not show a superconducting transition. This is consistent with a recent report demonstrating electric field control of a superconductor–insulator transition at the  $\text{LaAlO}_3/\text{KTaO}_3$  (111) interface.<sup>21</sup> Alternatively, the inhomogeneity of  $\text{TiO}_x$  layer could create an inhomogeneous 2D electron system and superconductivity. The observation of a remnant resistance below the transition temperature means that the superconducting puddles form, but fail to coalesce or reach a global phase coherence mediated by Josephson coupling.<sup>32,42–44</sup> Here, the fluctuations of superconducting order parameter in different puddles could limit the long-range phase coupling.<sup>32</sup>

Next, we discuss the observation of weak anti-localization near superconducting transition. 2D electron systems at the  $\text{KTaO}_3$  interfaces show signatures of weak anti-localization.<sup>16,29,30</sup> Furthermore, topologically nontrivial states are predicted at the  $\text{KTaO}_3$  (111) surface.<sup>9</sup> The observed weak anti-localization correction, however, is present in both (111) and (100) interfaces. The large weak anti-localization, i.e., the coherence length, at the (111) interface could be due to the topologically nontrivial states.<sup>7</sup> Resolving the topological nature of surface electronic states, however, requires further study. The 2D Hikami–Larkin–Nagaoka model<sup>37</sup> does not describe the low-field magneto-conduction behavior at 30 mK, due to the mixed superconducting and weak anti-localization corrections (Supplementary materials, S3). The  $\text{KTaO}_3$  samples are air-sensitive, and exposure to ambient oxygen fills the surface vacancies, and the 2DEG carrier density declines with exposure to ambient or oxygen annealing.<sup>16</sup> We observe a similar carrier density drop and suppression of the superconductivity in samples without a capping layer, due to the strong dependence of superconductivity to carrier density (Supplementary materials, S4). Interestingly, these samples show a linear positive magnetoresistance, after the demise of superconductivity, which could be explained by a 2D Hikami–Larkin–Nagaoka fit, with a resolved coherence length of 103 nm (Supplementary materials, S5), consistent with a previous report.<sup>30</sup>

In summary, our results, especially the coexistence of superconducting fluctuations and quantum coherent

quasiparticle effects, should be of interest for the experimental realization of non-abelian excitations in a single material. We stress that our findings warrant further study of the topological nature of surface states in  $\text{KTaO}_3$  (111) and the coexistence of topologically nontrivial states with superconductivity.

**Supplementary Information** The online version contains supplementary material available at <https://doi.org/10.1007/s11664-022-09844-9>.

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**Data Availability** The data that support the findings of this study are available within the article.

## Declarations

**Conflict of interests** The authors declare that they have no conflict of interest.

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