

Thermodynamic Modeling of the Pt-Te and Pt-Sb-Te Systems

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The Pt-Te and the Pt-Sb-Te systems are modeled using the calculation of phase diagram (CALPHAD) technique. In the Pt-Te system, the liquid phase is modeled as (Pt, PtTe₂, Te) using the associate model, and four intermediates, PtTe₂, Pt₂Te₃, Pt₃Te₄ and PtTe, are treated as stoichiometric compounds and their enthalpies of formation are obtained by means of first-principles calculations. The solution phases, fcc(Pt) and hex(Te), are described as substitutional solutions. Combined with the thermodynamic models of the liquid phase in the Pt-Sb and Sb-Te systems in the literature, the liquid phase of the Pt-Sb-Te ternary system is modeled as (Pt, Sb, Te, Sb₂Te₃, PtTe₂) also using the associate model. The compounds, PtTe₂, Pt₂Te₃, Pt₃Te₄ and PtTe in the Pt-Te system and PtSb₂, PtSb, Pt₃Sb₂ and Pt₇Sb in the Pt-Sb system are treated as line compounds $Pt_m(Sb,Te)_n$ in the Pt-Sb-Te system, and the compound Pt₅Sb is treated as (Pt,Sb)₅(Pt,Sb,Te). A set of self-consistent thermodynamic parameters is obtained. Using these thermodynamic parameters, the experimental Pt-Te phase diagram, the experimental heat capacities of PtTe and PtTe₂, the enthalpies of formation from first-principles calculations for PtTe₂, Pt₂Te₃, Pt₃Te₄, and PtTe, and the ternary isothermal sections at 873 K, 923 K, 1073 K and 1273 K are well reproduced.

Key words: Pt-Te system, Pt-Sb-Te system, thermodynamic properties, CALPHAD technique, thermoelectric materials

INTRODUCTION

Platinum can be used as the plating of electrodeposition of Sb₂Te₃ thermoelectric materials, so the interfacial phase equilibria among Pt, Sb and Te are very important to obtain thin film thermoelectric alloys.¹ Additionally, the platinum group elements commonly form compounds with S, Sb, Te, As, Se, Bi, Sn, Fe, Sb, Hg, Ni, Cu, etc., so most of the platinum group minerals exhibit complex compositions.² Because of the existence of platinum antimonides and tellurides in nature, the phase relationships in the Pt-Sb-Te system are very important for mineralogists.³

In this study, the phase diagram of the Pt-Te binary system and the isothermal sections of the Pt-Sb-Te ternary system at 873, 923, 1073 and

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1273 K are critically evaluated and the thermodynamic parameters for each phase of the systems are optimized in order to obtain complete phase equilibria information.

LITERATURE INFORMATION

Pt-Te System

The partial phase diagram between Pt and PtTe₂ was first determined by Gimpl et al.⁴ Two intermediate compounds, PtTe and PtTe₂, were reported. But the liquidus between PtTe₂ and hex(Te) was not mentioned. Bhan et al.⁵ measured the Pt-Te phase diagram, and four compounds, PtTe, PtTe₂, Pt₃Te₄ and Pt₂Te₃, were determined. However, the liquidus between PtTe₂ and hex(Te) was still shown as a dashed line.

In order to confirm the existence of the above compounds and liquidus between PtTe₂ and Te, Kim⁶

re-investigated the Pt-Te system by reflected light microscopy, x-ray diffraction (XRD), and electron probe microanalysis (EPMA). Four compounds, PtTe, Pt₃Te₄, Pt₂Te₃ and PtTe₂, were confirmed, and the solid solubilities of Te in fcc(Pt) and Pt in hex(Te) were less than 0.5 at.%. Two eutectic reactions, liquid \rightarrow PtTe + fcc(Pt) at 1143 K and liquid \rightarrow PtTe₂ + hex(Te) at 722 K, and two peritectic reactions, liquid + PtTe₂ \rightarrow Pt₃Te₄ at > 1273 K and liquid +Pt₃Te₄ \rightarrow PtTe at 1208 K, and one peritectoid reaction, Pt₃Te₄ + PtTe₂ \rightarrow Pt₂Te₃ between 923 K and 973 K, were recommended.

The enthalpies of formation of PtTe and Pt Te_2 were given by Karzhavin⁷ by means of the comparative methods. Grønvold et al.⁸ and Westrum et al.⁹ determined the heat capacities of PtTe and PtTe₂ by means of calorimeter.

Sb-Te System

The Sb-Te system was optimized by Ghosh et al.¹⁰ using the ionic model for liquid and by Guo et al.¹¹ using both the ionic model and the associate model for liquid. The thermodynamic parameters obtained by Guo et al.¹¹ were used in the present work because the latest pure element Gibbs energies of Sb and Te were used. Figure 1 presents the calculated Sb-Te phase diagram using the thermodynamic parameters of Ref. 11, in which liquid was described using the associate model (Sb, Sb₂Te₃, Te).

Pt-Sb System

The Pt-Sb system was optimized by Liu et al.¹² and Guo et al.¹³ In order to keep the thermodynamic parameters consistent, the optimized thermodynamic parameters of Ref. 13 were adopted in the



Fig. 1. Calculated Sb-Te phase diagram using the thermodynamic parameters in Ref. 11.

present work. Figure 2 shows the calculated Pt-Sb phase diagram.

Pt-Sb-Te System

The isothermal section of the Pt-Sb-Te system at 923 K was first determined by El-Boragy and Schubert,¹⁴ and no ternary compound was found.

The phase relationships at 873 K, 1073 K and 1273 K were studied by Kim and Chao in 1990.¹⁵ Later on, the isothermal sections at 873 K, 1073 K and 1273 K were reported by Kim,^{3,16,17} respectively, which were almost the same as the results of Ref. 15.

THERMODYNAMIC MODEL

The Gibbs energy functions for the unary phases of elements Pt, Sb and Te are taken from the Scientific Group Thermodata Europe (SGTE) database of pure elements.¹⁸

Pt-Te System

In the Pt-Te system, the liquidus in the left and right sides of the compound $PtTe_2$ is very asymmetric, and it is hard to obtain such asymmetric liquidus using the substitution model (Pt, Te) for liquid. Since Te and Pt are always anion and cation, respectively, in the compounds, the ionic model for liquid is appropriate in the Pt-Te system. However, Pt can form Pt^{+2} , Pt^{+4} , or Pt^{+6} , which will make the ionic model (Pt, PtTe₂, Te) is used to describe the liquid instead of the ionic model. The molar Gibbs energy is expressed as follows:



Fig. 2. Calculated Pt-Sb phase diagram using the thermodynamic parameters in Ref. 13.

$$G^{\text{liquid}} = x_{\text{Pt}} G^{\text{liquid}}_{\text{Pt}}(T) + x_{\text{Te}} G^{\text{liquid}}_{\text{Te}}(T) + x_{\text{PtTe}_2} G^{\text{liquid}}_{\text{PtTe}_2}(T) + RT(x_{\text{Pt}} \ln x_{\text{Pt}} + x_{\text{Te}} \ln x_{\text{Te}} + x_{\text{PtTe}_2} \ln x_{\text{PtTe}_2}) + {}^E G_m,$$
(1)

where x_{Pt} , x_{Te} and x_{PtTe_2} are the mole fractions of the pure elements Pt, Te and the associate PtTe₂, respectively. $G_{\text{Pt}}^{\text{liquid}}$ and $G_{\text{Te}}^{\text{liquid}}$ are the Gibbs energies of Pt and Te from the SGTE pure elements database¹⁸ and $G_{\text{PtTe}_2}^{\text{liquid}}$ is the Gibbs energy of the associate PtTe₂ in liquid.^{*E*}G_m is the excess Gibbs energy of liquid and is expressed as Eq. 2.

$${}^{E}G_{m} = x_{\text{Pt}}x_{\text{Te}} \sum_{j}{}^{j}L_{\text{Pt,Te}}(x_{\text{Pt}} - x_{\text{Te}})^{j} + x_{\text{Pt}}x_{\text{PtTe}_{2}} \sum_{j}{}^{j}L_{\text{Pt,PtTe}_{2}}(x_{\text{Pt}} - x_{\text{PtTe}_{2}})^{j} + x_{\text{PtTe}_{2}}x_{\text{Te}} \sum_{j}{}^{j}L_{\text{PtTe}_{2},\text{Te}}(x_{\text{PtTe}_{2}} - x_{\text{Te}})^{j}.$$
(2)

The solution phases, fcc(Pt) and hex(Te), are described using the substitutional solution model, and the molar Gibbs energies are modeled as:

$$G_m^{\phi}(T) = x_{\text{Pt}} G_{\text{Pt}}^{\phi}(T) + x_{\text{Te}} G_{\text{Te}}^{\phi}(T) + RT(x_{\text{Pt}} \ln x_{\text{Pt}} + x_{\text{Te}} \ln x_{\text{Te}}) + {^E}G_m^{\phi},$$
(3)

where ${}^{E}G_{m}^{\phi}$ is the excess Gibbs energy and is expressed by the Redlich–Kister polynomial,

$${}^{E}G_{m}^{\phi} = x_{\mathrm{Pt}}x_{\mathrm{Te}}\sum_{j}{}^{j}L_{\mathrm{Pt,Te}}^{\phi}(x_{\mathrm{Pt}} - x_{\mathrm{Te}})^{j}.$$
 (4)

 ^{j}L in Eqs. 2 and 4 is the interaction parameter for liquid, fcc(Pt) and hex(Te), and is expressed as the following equation:

$$^{j}L = a_{i} + b_{i}T, \tag{5}$$

where a_j and b_j are the parameters to be optimized in the present work.

The intermetallic compounds Pt_3Te_4 and Pt_2Te_3 in the Pt-Te system are treated as stoichiometric compounds in the present work. Due to a lack of experimental heat capacity data, the molar Gibbs energy of Pt_mTe_n is expressed as:

$$G^{\operatorname{Pt}_m\operatorname{Te}_n} = m\operatorname{GHSER}_{\operatorname{Pt}} + n\operatorname{GHSER}_{\operatorname{Te}} + \Delta G_f^{\operatorname{Pt}_m\operatorname{Te}_n}, \ (6)$$

where $\Delta G_f^{\operatorname{Pt}_m\operatorname{Te}_n}$ is the Gibbs energy of formation of compounds and is expressed as following:

$$\Delta G_f^{\operatorname{Pt}_m\operatorname{Te}_n} = a + bT,\tag{7}$$

where a and b are the parameters to be optimized according to the enthalpy of formation obtained from first-principles calculations in the present work and the experimental phase relationships in Refs. 4-6.

For the intermetallic compounds PtTe and PtTe₂, the heat capacity data are available from literature.^{7–9} These two compounds are also treated as stoichiometric compounds in the present work, while each of the Gibbs energy functions is described as a two-piecewise polynomial with the high and the low temperature parts according to the experimental heat capacity data.

Taking PtTe as an example, the Gibbs energy function is divided into two parts. Considering the experimental heat capacity data of Grønvold et al.,⁸ the Gibbs energy functions are expressed as follows:

$$0 < T < 80 \text{ K} G_{m1}^{\text{PtTe}} = a + bT + cT^3 + dT^4,$$
(8)

$$T \ge 80 \text{ K}$$

 $G_{m2}^{\text{PtTe}} = e + fT + gT \ln(T) + hT^2 + mT^{-1} + nT^3,$ (9)

where a, b, c, d, e, f, g, h, m and n are the parameters to be optimized according to the experimental heat capacity and phase relationships. During the process of optimization, the following conditions between the high and the low temperature parts, $G_{m1}^{\text{PtTe}} = G_{m2}^{\text{PtTe}}$, $H_{m1}^{\text{PtTe}} = H_{m2}^{\text{PtTe}}$, $S_{m1}^{\text{PtTe}} = S_{m2}^{\text{PtTe}}$, $Cp_{m1}^{\text{PtTe}} = Cp_{m2}^{\text{PtTe}}$ and $\frac{dCp_{m1}}{dT} = \frac{dCp_{m2}}{dT}$, should be met when T equals 80 K.

Table I. Space groups (SG), atoms per primitive cell, and k-point meshes used for first-principles calculations of Pt, Te, PtTe, Pt₃Te₄, Pt₂Te₃, and PtTe₂ along with the calculated equilibrium volumes $(Å^{3}/atom)$ at 0 K using PBE exchange-correlation functionals and experimental data

Material	SG	Atoms	k-mesh	E_0 (ev/cell)	PBE	Experimental volume (Å ³ /atom)
Pt	$\overline{Fm\bar{3}m}$	4	$16 \times 16 \times 16$	-24.412	15.5927	15.09 ²¹
Те	$P3_{1}21$	3	$16 \times 16 \times 16$	-9.426	34.8087	33.6897^{22}
PtTe	C2/m	8	$10 \times 16 \times 10$	-39.715	23.8074	22.3875^{3}
Pt_3Te_4	C2/m	14	10 imes 16 imes 6	-67.028	24.5621	23.2929^{16}
Pt ₂ Te ₃	C2/m	20	9 imes15 imes4	-94.173	25.0268	23.345^{16}
$PtTe_2$	$P\bar{3}m1$	3	$19\times19\times12$	-13.572	25.8098	23.6667^{23}

Phase	Thermodynamic parameters	Ref.
liquid	$egin{array}{llllllllllllllllllllllllllllllllllll$	13
	$^{1}L_{ m Pt,Sb}^{ m liquid} = -50982.5 + 9.1148T$	13
	$G_{ m Sb_2Te_3}^{ m liquid} = 0.4 { m GLIQ}_{ m Sb} + 0.6 { m GLIQ}_{ m Te} - 20557.0 + 15.6503 T$	11
	$^{0}L_{ m Sb_{2}Te_{3},Te}^{ m liquid}=+8348.8-1.8429T$	11
	$^{1}L_{ m Sb_2Te_3,Te}^{ m liquid} = +1179.4 - 3.5931T$	11
	$^{0}L_{ m Sb,Sb_{2}Te_{3}}^{ m liquid}=+8559.3-3.6932T$	11
	$^{1}L_{ m Sb,Sb_{3}Te_{3}}^{ m liquid}=-4703.8+9.8773T$	11
	$G_{ m PtTe}^{ m liquid} = 0.333 { m GLIQ}_{ m Pt} + 0.667 { m GLIQ}_{ m Te} - 31029.9 + 4.6984 T$	This work
	$^{0}L_{ m Pt,PtTe_{2}}^{ m liquid} = -26718.2 + 12.0857T$	This work
	$^1L_{ m Pt.PtTe_o}^{ m liquid}=+7740.0$	This work
	$^{0}L_{ m PtTe_2,Te}^{ m liquid}=+18086.5-2.3028T$	This work
	$^{1}L_{ m PtTe}^{ m liquid}=+4165.6$	This work
	$^0L^{ m liquid}_{ m Pt,PtTe_o,Sb}=-50000.0$	This work
	$^{0}L^{ m liquid}_{ m PtTe_2,Sb_2Te_3}=+20000.0$	This work
hex(Te)	Model (Pt, Sb, Te) ₁ $G(hex,Pt;0) = GHSER_{Pt} + 5000.0$ $G(hex,Sb;0) = GHSER_{Pt} + 5000.0$	This work This work
fcc(Pt)	$\begin{array}{l} \text{Model (Pt, Sb, Te)}_1(\text{Va})_1 \\ \text{G(fcc, Te;0)} = \text{GHSER}_{\text{Te}} + 5000.0 \\ {}^0L_{\text{fcc}}^{\text{fcc}} = -13004.2 + 60.7336T \end{array}$	13
	${}^{ m Pt,50} {}^1L_{ m Pt,st}^{ m fcc} = -222530.2$	13
	${}^{PL,SD} = +35966.7$	This work
	${}^{ m rt,1e} = +52726.7$	This work
rhom(Sb)	$\begin{array}{l} \text{Model (Pt, Sb, Te)}_1 \\ \text{G}(\text{rhom,Pt;0}) = \text{GHSER}_{\text{Pt}} + 5000.0 \\ \text{G}(\text{rhom,Te;0}) = \text{GHSER}_{\text{Te}} + 5000.0 \\ {}^0L_{\text{Sb}Te}^{\text{rhom}} = -4000.0 \end{array}$	13 11 11
Pt_7Sb	$egin{aligned} { m Model \ Pt_7(Sb,Te)} \ G_{ m Pt_7Sb}^{ m Pt_7Sb} = 7 { m GHSER_{Pt}} + { m GHSER_{Sb}} - 150253.0 + 26.8127T \end{aligned}$	13
	$G_{\mathrm{Pt:Te}}^{\mathrm{Pt_7Sb}} = G_{\mathrm{Pt:Te}}^{\mathrm{PtTe}} + 7\mathrm{GHSER_{Pt}} + 40000.0$	This work
Pt_5Sb	$\begin{array}{l} \text{Model} \ (\text{Pt}, \text{Sb})_5 \ (\text{Pt}, \text{Sb}, \text{Te}) \\ G_{\text{Pt}, \text{Sb}}^{\text{Pt}_5 \text{Sb}} = 5 \text{GHSER}_{\text{Pt}} + \text{GHSER}_{\text{Sb}} - 126606.3 + 28.7544T \end{array}$	13
	$G_{\mathrm{Pt;Pt}}^{\mathrm{Pt_5Sb}}=6\mathrm{GHSER}_{\mathrm{Pt}}{+}30000.0$	13
	$G_{ m Sb:Sb}^{ m Pt_5Sb}=6 m GHSER_{ m Sb}\!+\!30000.0$	13
	$G_{\mathrm{Sb:Pt}}^{\mathrm{Pt_5Sb}} = G_{\mathrm{Pt:Pt}}^{\mathrm{Pt_5Sb}} + G_{\mathrm{Sb:Sb}}^{\mathrm{Pt_5Sb}} - G_{\mathrm{Pt:Sb}}^{\mathrm{Pt_5Sb}}$	13
	${}^{0}L_{\mathrm{Pt,Sb:Pt}}^{\mathrm{Pt_5Sb}} = {}^{0}L_{\mathrm{Pt,Sb:Sb}}^{\mathrm{Pt_5Sb}} = -558341.2$	13
	$^{1}L_{\mathrm{Pt,Sb:Pt}}^{\mathrm{Pt_{5}Sb}} = ^{1}L_{\mathrm{Pt,Sb:Pt}}^{\mathrm{Pt_{5}Sb}} = +190567.2$	13
	$^{0}L_{\mathrm{Pt;Sb}}^{\mathrm{Pt;Sb}} = ^{0}L_{\mathrm{Sb:Pt,Sb}}^{\mathrm{Pt;Sb}} = -111626.8$	13
	$G_{\mathrm{Pt:Te}}^{\mathrm{Pt_5Sb}} = G_{\mathrm{Pt:Te}}^{\mathrm{PtTe}} + 4\mathrm{GHSER_{Pt}} + 30000.0$	This work
	$G_{ m Sb:Te}^{ m Pt_5Sb} = 1.667 G_{ m Sb:Te}^{ m Sb_2Te_3} + 4.333 { m GHSER}_{ m Sb} + 30000.0$	This work

Table II. Thermodynamic parameters in the Pt-Sb-Te system^a

Table II. continued

Phase	Thermodynamic parameters	Ref.
Pt ₃ Sb	$egin{aligned} { m Model \ Pt_3(Sb,Te)}\ G_{ m Pt_3Sb}^{ m Pt_3Sb}=3{ m GHSER_{Pt}}+G{ m HSER_{Sb}}-104971.6+8.4047T \end{aligned}$	13
	$G_{ m Pt, Te}^{ m Pt_3Sb}=G_{ m Pt, Te}^{ m PtTe}+2 m GHSER_{ m Pt}+20000.0$	This work
Pt_3Sb_2	$\begin{array}{c} \text{Model } \mathrm{Pt_3(Sb,Te)_2} \\ G_{\mathrm{Pt:Sb}}^{\mathrm{Pt_3Sb_2}} = 3\mathrm{GHSER_{Pt}} + 2\mathrm{GHSER_{Sb}} - 174658.4 + 10.8848T \end{array}$	13
	$G_{\mathrm{Pt:Te}}^{\mathrm{Pt_3Sb_2}} = 2G_{\mathrm{Pt:Te}}^{\mathrm{PtTe}} + \mathrm{GHSER_{Pt}} + 25000.0$	This work
	$^{0}L_{ m Pt_{s}Sb_{2}}^{ m Pt_{3}Sb_{2}} = -11552.7$	This work
PtSb	$\begin{array}{c} \text{Model Pt(Sb,Te)} \\ G_{\text{Pt:Sb}}^{\text{PtSb}} = \text{GHSER}_{\text{Pt}} + \text{GHSER}_{\text{Sb}} - 81220.5 + 6.8230T \end{array}$	13
	$G_{\mathrm{Pt:Te}}^{\mathrm{PtSb}}=G_{\mathrm{Pt:Te}}^{\mathrm{PtTe}}\!+\!10000.0$	This work
	$^{0}L_{ m Pt:Sb.Te}^{ m PtSb}=+33456.1-36.1949T$	This work
$PtSb_2$	Model Pt(Sb,Te) ₂	
	$G_{\mathrm{Pt:Sb}^2}^{\mathrm{PtSb}_2} = \mathrm{GHSER}_{\mathrm{Pt}}$ + 2 $\mathrm{GHSER}_{\mathrm{Sb}} - 149612.0 - 21.4560T$	This work
	$G^{ ext{PtSb}_2} = G^{ ext{PtTe}_2} \pm 15000.0 \pm 10000000000000000000000000000000$	This work
	$0_{Pt:Te} - 0_{Pt:Te} + 15000.0$	This work
	$L_{ m Pt:Sb,Te} = +575.1\pm0.04417$ $^1L_{ m Pt:Sb_2}^{ m PtSb_2} = -19263.8$	This work
$\mathrm{Sb}_{2}\mathrm{Te}_{3}$	Model $Sb_{0.4}Te_{0.6}$	
	$^0G_{ m Sb_2Te_3}^{ m Sb_2Te_3} = -17961.5602 - 3.27284441T + 0.0294155953T^2$	11
	$-0.00185310048T^3+7.92008333\times 10^{-6}T^4$	11
	60 < T < 1000	
	$^{0}G_{ m Sb:Te}^{ m Sb_2Te_3} = -19376.6 + 106.2655T - 22.5753T\ln(T) - 4.87264934$	11
gamma	$ imes 10^{-3}T^2 + 3.62456157 imes 10^{-7}T^3 + 12931.1094T^{-1} \ ext{Model Sb}_{0.4}(ext{Sb}, ext{Te})_{0.6} \ ^0G_{ ext{Sb}, ext{Sb}}^{ ext{gamma}} = ext{GHSER}_{ ext{Sb}} + 1460.0 - 0.4900T$	11
	${}^0G^{\mathrm{gamma}}_{\mathrm{Sb},\mathrm{Te}_a} = {}^0G^{\mathrm{Sb}_2\mathrm{Te}_3}_{\mathrm{Sb},\mathrm{Te}_a} + 872.2$	11
	${}^{0}L_{{ m Sh}\cdot{ m Sh}}^{ m gamma}=-2835.6+9.3216T$	11
	${}^{1}L_{ m Sburge}^{ m gamma} = +10593.5 - 10.1425T$	11
delta	Model Sb _{0.4} (Sb,Te) _{0.6} ${}^{0}G_{\text{cl.sl.}}^{\text{delta}} = \text{GHSER}_{\text{Sb}} + 1070.0 - 0.3600T$	11
	${}^{0}G^{\text{delta}}_{\text{ct.m}} = {}^{0}G^{\text{Sb}_{2}\text{Te}_{3}}_{\text{ct.m}} + 1471.4$	11
	${}^{0}L_{delta}^{delta} = -6394.9 + 12.1759T$	11
	${}^{1}L_{\text{delta}}^{\text{delta}} = \pm 1425.0 \pm 0.9063T$	11
	$^{2}L_{\text{delta}}^{\text{delta}} = -2243.2$	11
PtTe	Model Pt (Sh Te)	
1010	0 < T < 80	
	$G_{ ext{Pt:Te}}^{ ext{rtue}} = -72630.0 - 11.5638T - 0.0017000286T^5 + 5.3633 imes 10^{-6}T^4$	This work
	$T \ge 80$	
	$G_{\text{Pt:Te}}^{+} = -76497.4 + 223.2802T - 45.9684213T \ln(T) - 0.00975528427T^{2} + 48426.7206T^{-1} + 1.66916155 \times 10^{-6}T^{3}$	This work
	$+46430.72001 + 1.00210133 \times 10^{-1}$ $G_{\rm et Te}^{\rm pt Te} = G_{\rm et Sb}^{\rm pt Sb} + 30000.0$	This work
	${}^{0}L_{\text{pt:sb}}^{\text{pt:sb}} = -1271.7 + 5.5585T$	This work
	$\frac{1}{17} \frac{\text{PtTe}}{\text{Pt}} = -\pm 31473.3$	This work
	$\mu_{\text{Pt:Sb,Te}} = \pm 0.1410.0$	THIS WOLK

2643

Phase	Thermodynamic parameters	Ref.	
$Pt_{3}Te_{4}$	$egin{array}{l} { m Model \ Pt_3 \ (Sb,Te)_4} \ G_{ m Pt_3Te_4}^{ m Pt_3Te_4} = 3 { m GHSER_{Pt}} + 4 { m GHSER_{Te}} - 247457.0 + 10.7064 T \end{array}$	This work	
	$G_{\mathrm{Pt:Sb}}^{\mathrm{Pt_3Te_4}}=2G_{\mathrm{Pt:Sb}}^{\mathrm{PtSb}}\!+\!G_{\mathrm{Pt:Sb}}^{\mathrm{PtSb_2}}\!+\!35000.0$	This work	
	$^{0}L_{\mathrm{Pt:Sb,Te}}^{\mathrm{Pt_{3}Te_{4}}} = -56934.2 + 88.5995T$	This work	
Pt_2Te_3	$egin{array}{l} ext{Model Pt}_2 \ (ext{Sb}, ext{Te})_3 \ G_{ ext{Pt}: ext{Te}}^{ ext{Pt}_2 ext{Te}_3} = 2 ext{GHSER}_{ ext{Pt}} + 3 ext{GHSER}_{ ext{Te}} - 184917.0 + 10.7101T \end{array}$	This work	
	$G_{\mathrm{Pt:Sb}}^{\mathrm{Pt_2Te_3}}=G_{\mathrm{Pt:Sb}}^{\mathrm{PtSb}}\!+\!G_{\mathrm{Pt:Sb}}^{\mathrm{PtSb_2}}\!+\!25000.0$	This work	
	$^{0}L_{\mathrm{Pt:Sb,Te}}^{\mathrm{Pt_2Te_3}} = -24840.3 + 37.1112T$	This work	
$PtTe_2$	$egin{aligned} { m Model \ Pt \ (Sb,Te)_2} \ 0 < T < 80 \ G_{ m PtTe_2}^{ m PtTe_2} = -134749.3 - 13.4795T - 0.00274613806T^3 + 8.4700 imes 10^{-6}T^4 \end{aligned}$	This work	
	$T \ge 80$		
	$G_{ ext{Pt:Te}}^{ ext{PtTe}_2} = -140469.4 + 337.4973T - 68.8581519T\ln(T) - 0.0172150206T^2 \ +7.737.708T^{-1} + 3.06779819 imes 10^{-6}T^3$	This work	
	$G_{\mathrm{Pt:Sb}}^{\mathrm{PtTe_2}}=G_{\mathrm{Pt:Sb}}^{\mathrm{PtSb_2}}{+}15000.0$	This work	
	$^{0}L^{\mathrm{PtTe_{2}}}_{\mathrm{Pt:Sb,Te}} = -28401.5 + 27.6216T$	This work	
	$^{1}L_{ m Pt^{-Sh}_{Pt^{-Sh}_{-Sh}_{-Th}}}^{ m Pt^{Te_{2}}}=-6724.3$	This work	

^aIn J mol⁻¹ of the formula units.

	Present work			Kim ⁶				
Reaction	<i>T</i> (K)	2	r(Te)		<i>T</i> (K)		x (Te)	
$\overline{\text{liquid}} \rightarrow \text{fcc}(\text{Pt}) + \text{PtTe}$	1146	0.3630	_	_	1143	0.400		
liquid + $Pt_3Te_4 \rightarrow PtTe$	1208	0.4342	_	_	1208	_	_	_
liquid + PtTe ₂ \rightarrow Pt ₃ Te ₄	1290	0.5208	_	_	> 1273	0.164	_	_
liquid \rightarrow PtTe ₂	1423	0.6667	_	_	1423	0.667	_	_
$PtTe_2 + Pt_3Te_4 \rightarrow Pt_2Te_3$	954	_	_	_	923-973	_	_	_
liquid \rightarrow PtTe ₂ + hex(Te)	720	0.9957	-	-	722	1.000	-	-

Table III. Invariant reactions in the Pt-Te system

Pt-Sb-Te System

In the Pt-Sb-Te system, there are four solution phases: liquid, fcc(Pt), hex(Te), and rhom(Sb). Combining the model of liquid in the Pt-Sb,¹³ Sb-Te¹¹ and Pt-Te systems, the liquid phase in the Pt-Sb-Te system is treated as (Pt, PtTe₂, Sb, Sb₂Te₃, Te). The molar Gibbs energy is described by the following expression:

$$\begin{aligned} G_{m}^{\text{liquid}}(T) = & x_{\text{Pt}} G_{\text{Pt}}^{\text{liquid}}(T) + x_{\text{Sb}} G_{\text{Sb}}^{\text{liquid}}(T) \\ &+ x_{\text{Te}} G_{\text{Te}}^{\text{liquid}}(T) + x_{\text{PtTe}_2} G_{\text{PtTe}_2}^{\text{liquid}}(T) \\ &+ x_{\text{Sb}_2\text{Te}_3} G_{\text{Sb}_2\text{Te}_3}^{\text{liquid}}(T) + RT(x_{\text{Pt}} \ln x_{\text{Pt}} \\ &+ x_{\text{Sb}} \ln x_{\text{Sb}} + x_{\text{Te}} \ln x_{\text{Te}} + x_{\text{PtTe}_2} \ln x_{\text{PtTe}_2} \\ &+ x_{\text{Sb}_2\text{Te}_3} \ln x_{\text{Sb}_2\text{Te}_3}) + {}^E G_{m}^{\text{liquid}}, \end{aligned}$$
(10)

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where x_{Pt} , x_{Sb} , x_{PtTe_2} , $x_{\text{Sb}_2\text{Te}_3}$ and x_{Te} are the mole fractions of Pt, Sb, PtTe₂, Sb₂Te₃ and Te, respectively; ${}^EG_m^{\text{liquid}}$ is the excess Gibbs energy composed of binary and ternary excess Gibbs energies and is expressed by the Redlich–Kister polynomial,

$$\begin{aligned} G_{m}^{\text{liquid}} &= x_{\text{Pt}} x_{\text{Sb}} \sum_{j} {}^{j} L_{\text{Pt,Sb}}^{\text{liquid}} (x_{\text{Pt}} - x_{\text{Sb}})^{j} \\ &+ x_{\text{Sb}} x_{\text{Sb}_{2}\text{Te}_{3}} \sum_{j} {}^{j} L_{\text{Sb,Sb}_{2}\text{Te}_{3}}^{\text{liquid}} (x_{\text{Sb}} - x_{\text{Sb}_{2}\text{Te}_{3}})^{j} \\ &+ x_{\text{Sb}_{2}\text{Te}_{3}} x_{\text{Te}} \sum_{j} {}^{j} L_{\text{Sb}_{2}\text{Te}_{3},\text{Te}}^{\text{liquid}} (x_{\text{Sb}_{2}\text{Te}_{3}} - x_{\text{Te}})^{j} \\ &+ x_{\text{Pt}} x_{\text{Pt}\text{Te}_{2}} \sum_{j} {}^{j} L_{\text{Pt,PtTe}_{2}}^{\text{liquid}} (x_{\text{Pt}} - x_{\text{Pt}\text{Te}_{2}})^{j} \\ &+ x_{\text{Pt}} x_{\text{Pt}\text{Te}_{2}} x_{\text{Te}} \sum_{j} {}^{j} L_{\text{Pt,PtTe}_{2}}^{\text{liquid}} (x_{\text{Pt}\text{Te}_{2}} - x_{\text{Te}})^{j} \\ &+ x_{\text{Pt}\text{Te}_{2}} x_{\text{Sb}_{2}\text{Te}_{3}} {}^{0} L_{\text{Pt,Te}_{2},\text{Sb}_{2}\text{Te}_{3}} \\ &+ x_{\text{Pt}\text{Te}_{2}} x_{\text{Sb}_{2}\text{Te}_{3}} {}^{0} L_{\text{Pt,PtTe}_{2},\text{Sb}_{2}\text{Te}_{3}} \\ &+ x_{\text{Pt}} x_{\text{Pt}\text{Te}_{2}} x_{\text{Sb}} {}^{0} L_{\text{Pt,PtTe}_{2},\text{Sb}}^{\text{liquid}}, \end{aligned}$$
(11)

where ${}^{j}L_{\rm pt,Sb}^{\rm liquid}$ is the binary interaction parameter between elements Pt and Sb in liquid in the Pt-Sb system;¹³ ${}^{j}L_{\rm Sb,Sb_2Te_3}^{\rm liquid}$ and ${}^{j}L_{\rm Sb_2Te_3,Te}^{\rm liquid}$ are the interaction parameters of liquid in the Sb-Te system;¹¹ ${}^{j}L_{\rm pt,PtTe_2}^{\rm liquid}$ and ${}^{j}L_{\rm pt,PtTe_2,Te}^{\rm liquid}$ are interaction parameters of liquid in the Pt-Te system, which are to be optimized in the present work. ${}^{0}L_{\rm PtTe_2,Sb_2Te_3}^{\rm liquid}$ and ${}^{0}L_{\rm Pt,PtTe_2,Sb}^{\rm liquid}$ are the ternary interaction parameters to be optimized according to the phase equilibria of liquid at different isothermal sections.^{3,16,17}

The solution phases fcc(Pt), hex(Te), and rhom(Sb) are treated as a substitutional solid solution, and the expression of the molar Gibbs energy is similar to Eq. (2) in Ref. 13.

The compounds, PtTe₂, Pt₂Te₃, Pt₃Te₄ and PtTe in the Pt-Te system and PtSb₂, PtSb, Pt₃Sb₂ and Pt₇Sb in the Pt-Sb system, with a solid solubility of the third elements, are treated as line compounds $Pt_m(Sb,Te)_n$. The molar Gibbs energy of each of these compounds is expressed as follows,

$$G_{m}^{\phi} = y_{\text{Sb}}G_{\text{Pt:Sb}}^{\phi} + y_{\text{Te}}G_{\text{Pt:Te}}^{\phi} + nRT(y_{\text{Sb}}\ln y_{\text{Sb}} + y_{\text{Te}}\ln y_{\text{Te}}) + y_{\text{Sb}}y_{\text{Te}}\sum_{j}{}^{j}L_{\text{Pt:Sb,Te}}^{\phi}(y_{\text{Sb}} - y_{\text{Te}})^{j}$$
(12)

The compound Pt_5Sb with a homogeneity range in the Pt-Sb system was treated as $(Pt,Sb)_5(Pt,Sb)$ by a two-sublattice model^{19,20} in Ref. 13 The solubility of Te in Pt_5Sb is about ~1 at.%,³ and it is described as $(Pt\%,Sb)_5(Pt,Sb\%,Te)$ in the Pt-Sb-Te system.

ASSESSMENT PROCEDURE

In order to model the Pt-Sb-Te system, the thermodynamic parameters of the Pt-Sb, Sb-Te, and Pt-Te binary systems should be obtained. Those of the Sb-Te and Pt-Sb systems are taken from Refs. 11 and 13, respectively, and the calculated Sb-Te and Pt-Sb phase diagrams are shown in Figs. 1 and 2. Due to the lack of experimental measurements for Pt₂Te₃ and Pt₃Te₄ in the Pt-Te system, the enthalpies of the formation of Pt₂Te₃ and Pt₃Te₄, as well as PtTe₂ and PtTe, are calculated in the present work by means of first-principles calculations. The process of obtaining enthalpies of formation of compounds using first-principles calculations is described in Ref. 13.



Fig. 3. Calculated Pt-Te phase diagram in comparison with the experimental data⁶.



Fig. 4. Calculated thermochemical properties of PtTe with the experimental data.⁸ (a) Cp, (b) S-S₀, (c) H-H₀.

The space group, atoms per primitive cell, and the k-point mesh used for Pt, Te, PtTe₂, Pt₂Te₃, Pt₃Te₄ and PtTe, and the latest experimental lattice parameters^{3,16,21-23} are listed in Table I.

The optimization is carried out by means of the optimization module PARROT of the thermodynamic software Thermo-Calc,²⁴ which can handle various kinds of experimental data. Before optimizing the Pt-Sb-Te ternary system, the Pt-Te system is optimized based on the experimental data in Refs. 4–6.

During the optimization procedure, the experimental data of the Pt-Te phase diagram in Ref. 6 is given a larger weight. The experimental



Fig. 5. Calculated thermochemical properties of PtTe₂ with the experimental data.⁹ (a) Cp, (b) S-S₀, (c) H-H₀.

heat capacities measured by Grønvold et al.⁸ and Westrum et al.⁹ are used to optimize the thermodynamic parameters of PtTe and PtTe₂, respectively. As for the formation enthalpies of compounds in the Pt-Te system, the values calculated from firstprinciples calculations are used as the starting values at the beginning of the optimization. Then,

thermodynamic parameters of compounds are optimized to fit the experimental phase equilibria. $^{4-6}$

As for the Pt-Sb-Te ternary system, three isothermal sections at 873 K,³ 1073 K¹⁶ and 1273^{17} K are given larger weight during the optimization, while the part between 0 at.% and 33 at.% Pt of the isothermal section at 923 K is not considered in the present work because its phase relationships in the Sb-Te binary terminal adopted by El-Boragy and Schubert¹⁴ is inconsistent with the phase diagram assessed by Ghosh et al.¹⁰ and Guo et al.¹¹

The thermodynamic descriptions of liquid, fcc(Pt), rhom(Sb) and hex(Te) in the Pt-Sb-Te system are obtained by combining the corresponding Gibbs energy functions from the assessments of the binary systems using Muggianu interpolation for excess terms.²⁵ In the present work, the coefficients ${}^{0}L_{\rm PtTe_2,Sb_2Pt_3}^{\rm liquid}$ and ${}^{0}L_{\rm Pt,PtTe_2,Sb}^{\rm liquid}$ are optimized on the basis of the phase relationships related to liquid in isothermal sections determined by Kim.^{3,16,17}

For the compounds $PtTe_2$, Pt_2Te_3 , Pt_3Te_4 , PtTe, $PtSb_2$, PtSb, Pt_3Sb_2 , Pt_5Sb and Pt_7Sb in the Pt-Sb-Te system, the thermodynamic parameters are optimized according to the experimental data.^{3,14,16,17} The assessment procedure is similar to that for treating the C40 compound in Ref. 26.

RESULTS AND DISCUSSIONS

Figures 1 and 2 are the calculated Sb-Te and Pt-Sb phase diagrams using the thermodynamic parameters from Refs. 11 and 13, respectively.

The thermodynamic parameters of the Pt-Te and Pt-Sb-Te systems obtained in the present work are shown in Table II. The liquid phase is described using the associate model. Table III shows the calculated invariant reactions in the Pt-Te system. It can be seen by comparison that the experimental temperatures and compositions for the invariant reactions are well reproduced.

Figure 3 is the calculated Pt-Te phase diagram using the present thermodynamic parameters, which is basically consistent with the experimental data.⁶ Figures 4a–c and 5a–c show the calculated Cp, S-S₀ and H-H₀ of PtTe and PtTe₂, respectively, in comparison with the experimental data.^{8,9} As shown in Figs. 4 and 5, the calculated results are consistent with the experimental data. Figure 6 shows the calculated enthalpies of the formation of the compounds PtTe₂, Pt₂Te₃, Pt₃Te₄ and PtTe in comparison with the values from first-principles calculations and the calculated value from Ref. 7. In Fig. 6, the values from the first-principles calculations are reproduced well.

Figure 7a–d are the calculated isothermal sections at 873, 923, 1073 and 1273 K, respectively. Comparing the three-phase region $PtSb + PtSb_2 + PtTe_2$

at 873, 923, 1073 and 1273 K, the experimental equilibrium compositions of $PtSb_2$ at 923, 1073 and 1273 K are more reasonable than the one at 873 K when $PtSb_2$ is treated as a linear compound. Therefore, two experimental alloys with the compositions of 39.97 Pt + 55.03 Sb + 5.00 Te and 40.03 Pt + 49.98 Sb + 9.98 Te $(at.\%)^3$ are not included in the threephase region of $PtSb + PtSb_2 + PtTe_2$ at 873 K. The other two Te-rich experimental data with the compositions of 37.00 Pt + 57.00 Te + 6.00 Sb and 20.00 Pt + 19.99 Sb + 60.01 Te (at.%) are not included in the three-phase regions of $PtSb_2 + PtTe_2 + Pt_2Te_3$ and PtSb₂ + PtTe₂ + liquid at 873 K, respectively. If these two experimental data are reproduced in the calculated results, several four-phase invariant reactions would occur at about 673 K. Considering that the solid state phase transformation is very difficult at low temperature due to the low atomic diffusion ability, the above two experimental data are not reproduced in the present work in order to make sure that the phase relationships in the temperature range between 300 K and 873 K are unchanged.

Figure 8 is the predicted liquidus projection of the Pt-Sb-Te system. As shown in Fig. 8a, the liquidus



Fig. 6. Calculated enthalpy of formation in the Pt-Te system at 298 K in comparison with the calculated results of Karzhavin⁷ and from first-principles calculations in the present work.



Fig. 7. Calculated isothermal sections of the Pt-Sb-Te system using the present thermodynamic description. (a) 873 K with the experimental data from Ref. 3, (b) 923 K with the experimental data from Ref. 14, (c) 1073 K with the experimental data from Ref. 16, (d) 1273 K with the experimental data from Ref. 17.

surface of Pt_2Te_3 occurs in the liquidus projection because Pt_2Te_3 becomes stable at high temperature with the addition of Sb, which can be seen in the isothermal section at 1073 K. Table IV shows the predicted invariant reactions in the Pt-Sb-Te system.



Fig. 8. (a) Predicted liquidus projection of the Pt-Sb-Te system using the present thermodynamic description. (b) Enlarged section of (a) in the rich Sb-Te side, (c) Enlarged section of (a) in the rich Pt-Sb side.

CONCLUSIONS

The phase relationships of the Pt-Te and Pt-Sb-Te systems, thermodynamic parameters Cp, S-S₀, and H-H₀, of PtTe and PtTe₂ are critically optimized on the basis of the experimental information available in the literature. A set of self-consistent

thermodynamic parameters describing the Gibbs energies of individual phases in the Pt-Sb-Te system as the functions of composition and temperature is obtained. With the present optimized parameters, various thermodynamic calculations of practical interest can be made.

	Present work						
Reaction	Туре	<i>T</i> (K)	x(Pt)	x(Sb)	x(Te)		
liquid + $PtTe_2$ + $PtSb_2$	C_1	1354	0.3361	0.2689	0.4005		
liquid + $PtSb_2 + Sb_2Te_3$	$\overline{C_2}$	890	0.0043	0.4013	0.5944		
liquid + $PtSb_2$ + delta	$\overline{C_3}$	817	0.0010	0.7049	0.2942		
liquid + Pt_3Te_4 + $PtTe_2 \rightarrow Pt_2Te_3$	P_1	1230	0.6006	0.1982	0.2012		
liquid + $PtSb_2 \rightarrow PtSb + PtTe_2$	$\overline{\mathrm{U}_1}$	1246	0.5232	0.3361	0.1407		
liquid + $PtTe_2 \rightarrow Pt_2Te_3 + PtSb$	U_2	989	0.6658	0.3045	0.0297		
liquid +fcc \rightarrow PtTe + Pt ₅ Sb	$\overline{\mathrm{U}_3}$	982	0.7187	0.2525	0.0288		
liquid + PtSb \rightarrow Pt ₂ Te ₃ + Pt ₃ Sb ₂	U_4	976	0.6687	0.3042	0.0270		
liquid + $Pt_2Te_3 \rightarrow Pt_3Sb_2 + Pt_3Te_4$	U_5	947	0.6835	0.2942	0.0223		
liquid + $Pt_5Sb \rightarrow PtTe + Pt_3Sb$	U_6	931	0.7104	0.2700	0.0196		
liquid + PtTe \rightarrow Pt ₃ Te ₄ + Pt ₃ Sb	U_7	914	0.6991	0.2834	0.0175		
liquid + $Pt_3Te_4 \rightarrow Pt_3Sb + Pt_3Sb_2$	U_8	913	0.6978	0.2851	0.0172		
liquid + $PtSb_2 \rightarrow PtTe_2 + Sb_2Te_3$	U_9	872	0.0068	0.3035	0.6897		
liquid + $Sb_2Te_3 \rightarrow PtSb_2 + Gamma$	U_{10}	831	0.0011	0.5933	0.4056		
liquid +rhom(Sb) \rightarrow PtSb ₂ +delta	U_{11}	821	0.0011	0.7561	0.2428		
liquid + gamma \rightarrow PtSb ₂ + delta	U_{12}	820	0.0010	0.6556	0.3434		
liquid \rightarrow PtTe ₂ +Sb ₂ Te ₃ + hex(Te)	$\mathbf{E_1}$	687	0.0024	0.0726	0.9250		

Table IV. Invariant reactions in the Pt-Sb-Te system

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REFERENCES

- J. Yang, W. Zhu, X. Gao, S. Bao, X. Fan, X. Duan, and J. Hou, J. Phys. Chem. B 110, 4599 (2006).
- L.J. Cabri, Platinum-Group Elements: Mineralogy, Geology, Recovery (Washington, DC: Geology Division of CIM, 1981).
- 3. W.-S. Kim, J. Alloys Compd. 252, 166 (1997).
- M.L. Gimpl, C.E. Nelson, and N. Fuschillo, Trans. Am. Soc. Metals 56, 209 (1963).
- Y.C. Bhan, T. Godecke, and K. Schubert, J. Less-Common Metals 19, 121 (1969).
- 6. W.-S. Kim, Met. Mater. 2, 9 (1996).
- 7. V.K. Karzhavin, Geochem. Int. 45, 931 (2007).
- F. Grønvold, T. ThurmannMoe, E.F. Westrum Jr, and E. Chang, J. Chem. Phys. 35, 1665 (1961).
- E.F. Westrum Jr, H.J. Carlson, F. Grønvold, and A. Kjekshus, J. Chem. Phys. 35, 1670 (1961).
- G. Ghosh, H.L. Lukas, and L. Delaey, Z. Metallkd. 80, 731 (1989).

- C. Guo, C. Li, and Z. Du, J. Electron. Mater. 43, 4082 (2014).
 J. Liu, Y. Zhang, and C. Guo, Int. J. Nonferrous Metall. 2, 95
- (2013).
 13. C. Guo, C. Li, and Z. Du, Int. J. Mater. Res. 105, 525 (2014).
- C. Guo, C. Li, and Z. Du, *Int. 5. Matter. Res.* 105, 525 (2014).
 M. El-Boragy and K. Schubert, *Z. Metallkd.* 62, 667 (1971).
- 15. W.-S. Kim and G.Y. Chao, *Can. Mineral.* 28, 675 (1990).
- 16. W.-S. Kim, J. Alloys Compd. 284, 218 (1999).
- W.-S. Kim, J. Alloys Compd. 204, 210 (1999).
 W.-S. Kim, J. Alloys Compd. 407, 235 (2006).
- 18. http://www.thermocalc.com/resources, SGTE pure elements (unary) database, Version 5.1 (2010).
- 19. M. Hillert and L.I. Staffansson, Acta Chem. Scand. 24, 3618 (1970).
- B. Sundman and J. Ågren, J. Phys. Chem. Solids 42, 297 (1981).
- J.P. Perdew, K. Burke, and M. Ernzerhof, *Phys. Rev. Lett.* 77, 3865 (1996).
- Y. Ohmasa, I. Yamamoto, M. Yao, and H. Endo, J. Phys. Soc. Jpn. 64, 4766 (1995).
- C. Soulard, P.E. Petit, P. Deniard, M. Evain, S. Jobic, M.H. Whangbo, and A.C. Dhaussy, *J. Solid State Chem.* 178, 2008 (2005).
- 24. J.O. Andersson, T. Helander, L.H. Hoglund, P.F. Shi, and B. Sundman, *Calphad* 9, 273 (2002).
- Y.M. Muggianu, M. Gambino, and J.-P. Bros, J. Chim. Phys. 72, 83 (1975).
- C. Guo, C. Li, P.J. Masset, and Z. Du, *Calphad* 36, 100 (2012).