# Microstructural Effects on High-Cycle Fatigue-Crack Initiation in A356.2 Casting Alloy

B. ZHANG, D.R. POIRIER, and W. CHEN

The effects of various microconstituents on crack initiation and propagation in high-cycle fatigue (HCF) were investigated in an aluminum casting alloy (A356.2). Fatigue cracking was induced in both axial and bending loading conditions at strain/stress ratios of  $-1$ , 0.1, and 0.2. The secondary dendrite arm spacing (SDAS) and porosity (maximum size and density distribution) were quantified in the directionally solidified casting alloy. Using scanning electron microscopy, we observed that cracks initiate at near-surface porosity, at oxides, and within the eutectic microconstituents, depending on the SDAS. When the SDAS is greater than  $\sim$  25 to 28  $\mu$ m, the fatigue cracks initiate from surface and subsurface porosity. When the SDAS is less than  $\sim$  25 to 28  $\mu$ m, the fatigue cracks initiate from the interdendritic eutectic constituents, where the silicon particles are segregated. Fatigue cracks initiated at oxide inclusions whenever they were near the surface, regardless of the SDAS. The fatigue life of a specimen whose crack initiated at a large eutectic constituent was about equal to that when the crack initiated at a pore or oxide of comparable size.

THE mechanical properties of widely used A356.2 alu-<br>minum castings is needed to better reveal the interaction of<br>microstructures with the fatigue process.<br>such as secondary dendrite arm spacing (SDAS),<sup>[1,2,3]</sup> micro-<br>po ponding improvements in fuel economy and emissions. As sound commercial aluminum castings find more applica- **II. EXPERIMENTAL PROCEDURES** tions, more information on the effects of microstructures on fatigue properties would enhance both the practical improve- A. *Materials and Fatigue Testing*

fatigue cracks usually initiate from shrinkage pores at or close to the specimen surface,  $[16-23]$  often associated with a small crack-initiation period.[23] However, research has been B. *Microstructural Characterization and Fatigue* focused on fatigue-crack propagation of long cracks using *Fracture Observations*

**I. INTRODUCTION** research on small-crack propagation<sup>[24]</sup> in commercial alu-<br>minum castings is needed to better reveal the interaction of

ment of the current casting processing and the fundamental<br>
alloys.<br>
It is generally accepted that the fatigue processes in aluminum casting<br>
alloys. The melt was<br>
alloys. The melt was<br>
alloys. The melt was<br>
alloys. The ma

Using light microscopy, the line-intercept method<sup>[2,3]</sup> was applied to measure the SDAS on samples removed from the as-cast ingots. Failed fatigue samples, which contained main B. ZHANG, Graduate Research Assistant, and D.R. POIRIER, Professor,<br>
Department of Materials Science and Engineering, and W. CHEN, Assistant<br>
Professor, Department of Aerospace and Mechanical Engineering, are with<br>
The Uni the interaction between the fatigue cracks and the contiguous Manuscript submitted December 29, 1998. microstructures. Examination at finer scales was conducted



Fig. 1—Variation of SDAS along ingot height.

using SEM, which revealed the fatigue-crack initiation sites, propagation paths, fracture modes, *etc.*

### C. *Number Density of Pores and Maximum Pore Size*

Radiographs were made before mechanical testing to reveal the porosity (maximum size and number density) in the fatigue specimens removed from the bottom to the top of the ingots. A radiography unit with a tungsten target of an effective focal spot of 2.0 mm was used. Pores visible on the radiographs at a magnification of 20 times were counted within a grid of an area of 34.10 mm<sup>2</sup> (5.84  $\times$  5.84 mm). The number of pores in a total of 12 grid areas within the gage section of each specimen was counted, and then the number density was averaged. The size of the largest pore, determined at a magnification of 20 times in each  $\begin{array}{c} (b) \\ (b) \end{array}$ <br>specimen, was further measured at a magnification of Fig. 2—Pores detected by radiography in the casting ingots (a) variation of maximum length

# D. *Area and Maximum Size of Crack-Initiation Sites on Fractures* the variation in SDAS shows a change in slope at about 40

measured. A grid with an area of  $2.117 \text{ mm}^2 (1.455 \times 1.455 \text{ m}^2)$  the bottom measurem from the attention or the attention or the bottom. mm) was used for area measurement on photomicrographs. Only the crack-initiation site that caused the fatal fatigue crack was measured when multiple crack-initiation sites B. *Porosity Distribution as a Function of SDAS* were found.

height, measured upward from the bottom chill. Below a the SDAS increases from 28 to 48  $\mu$ m, the images of the distance of 50 mm from the bottom chill, the SDAS increases pores become clearer, and the maximum length increases slightly from 15 to 20  $\mu$ m as the height increases. Twenty from about 0.08 mm (80  $\mu$ m) to 0.7 mm (Figure 2(a)). seconds after pouring, a bottom plate was pulled so that the Using this radiographic technique, no pores were detected



The fatigue-crack initiation sites on the fatigue fractures mm from the chilled surface, in Figure 1. Beyond that point, were identified with the aid of either a light microscope or the SDAS increases almost linearly from 20 to 60  $\mu$ m at<br>SEM depending on the size of the sites. Both the maximum 250 mm. According to a relationship cited by S SEM, depending on the size of the sites. Both the maximum<br>size and the area of the projection of the initiation sites<br>(porosity, oxide inclusions, and eutectic constituents) were<br>magnitude and the calculated cooling rate

The variations of maximum length and density of porosity, visible on radiographs of the fatigue specimens (3-mm thick) **III.** RESULTS AND DISCUSSIONS with different SDASs, are summarized in Figures 2(a) and A. *The Variation of SDAS along the Height of the Ingot* (b). The pores are obvious when the SDAS > 28 μm; no visible pores, for specimens with a SDAS < 28 μm, could Figure 1 shows the variation of SDAS along the ingot be detected even under a magnification of 38.75 times. As casting butt was exposed to direct water impingement. Thus, in specimens that have an SDAS less than 28  $\mu$ m. Figure 2(b) shows that the number density of visible pores is between approximately 0.4 to 1.1  $\text{mm}^{-3}$  for most of the specimens, with four of the number densities less than  $0.2 \text{ mm}^{-3}$ , grouped at a SDAS of approximately 30  $\mu$ m.

Although radiography did not detect the pores at the smaller SDAS, using metallographic techniques, Fang and Granger<sup>[27]</sup> found pores which were 50 to 25  $\mu$ m in equivalent diameter for SDASs from 30 to 16  $\mu$ m, in a grainrefined and modified A356.2, which was cast in the same manner as the ingots studied herein. However, pores of such small sizes are not active in terms of crack initiation, which takes place at eutectic microconstituents of larger sizes, as is discussed later. Results in Figure 2(a) show that, as the SDAS increases (cooling rate decreases), the maximum length of the pores increases, but, when the SDAS is greater than about  $34 \mu m$ , the visible pore density decreases. These results are in agreement with the results from Tynelius *et*  $al.$ <sup>[29]</sup> and Shivkumar *et al.*,<sup>[30]</sup> where it was found that the  $\tag{a}$ maximum porosity area increases as the SDAS increases, and that, when the hydrogen content is above 0.22 mL/ 100 g in the alloy, the areal pore density decreases as the SDAS increases.

# C. *Fatigue-Crack Initiation at Near-Surface Porosity*

Porosity has been widely reported to be the major initiation site for fatigue cracks in casting alloys. In this study, detailed observations of the fracture surfaces of the bendingand axial-fatigue specimens revealed other types of initiation sites in addition to pores, depending on the SDAS and microconstituents.

Although most of the initiation sites are at the surface, cracks initiated from subsurface porosity in a few of the bending-fatigue specimens. Subsurface crack initiation, related to preexisting defects and microcracks, has been related to preexisting defects and microcracks, has been (*b*) related to preexisting defects and microcracks, has been (*b*) reported in HCF at lower stresses for high-strength alloys.<sup>[31,32]</sup> The possibility that a sub defect can initiate a crack depends not only on its size, but<br>also on its distance from the surface. The pore in Figure<br>and distances from surfaces.  $3(a)$  is approximately  $360 \mu m$  in length, and its closest distance to the surface is about 33  $\mu$ m. Figure 3(b) shows the maximum lengths of subsurface defects that initiated<br>
racks and their distances from the surface. For the fractures<br>
resulting from axial fatigue testing, we did not find any<br>
resulting from axial fatigue testing, we They found that most of the initiation sites were subsurface<br>
They found that most of the initiation sites were subsurface<br>
pores. So, whether the fatigue crack initiates from a subsurface<br>
face defect depends on the exte





the pores. The fatigue life of a bending specimen with a D. *Crack Initiation at Oxides at or near the Surface* SDAS of 25 μm, whose crack initiated at an old oxide, is 100 times less than that for a similar specimen with a crack Different types of oxides were found to initiate fatigue initiated from a eutectic constituent and is almost the same cracks in both axial- and bending-fatigue specimens. Oxides as that for a specimen with a crack initiated from a pore of poured into molds with the melts are more deleterious to  $267 \mu m$  in maximum length. Campbell *et al.*<sup>[34]</sup> and Wang



Fig. 4—Oxides revealed by SEM: (*a*) initiation site at subsurface oxide (SDAS =  $25 \mu m$ , bending fatigue with maximum strain of 0.0016,  $R =$ 

alloy castings could probably be improved by a factor of that the debonding was from a sliding mechanism. 100 to 10,000 times by a combination of attention to metal Since the silicon particles in the interdendritic area are

of the molten alloy during pouring. This oxide initiated a rest of the matrix to satisfy the deformation compatibility. fatigue crack in a specimen with a SDAS of  $17 \mu m$ . Indica-<br>Apparently, the stress concentration created in this area is tion of debonding was seen on the other half of the fatigue enough to cause microslips in the matrix close to the silicon fracture that is not shown here. The oxide consists of particles, which led to the particle debonding and then crack  $AI_xSi_yO_z$  with only a very slight indication of Mg, in contrast initiation. According to Lee *et al.*,<sup>[36]</sup> a Sr-modified eutectic to the old oxides, which showed clear indications of Mg. alloy  $(Al-12$  wt pct Si-0.35 wt pct Mg) showed better fatigue-Smaller particles sitting on the film were detected, with crack growth resistance than the unmodified version of the qualitative compositions of  $A l_x S i_y O_z$  and  $A l_x C_y S i_z$ . The alloy with coarse Si particles. Shiozawa *et al.*<sup>[24]</sup> investigated fatigue life of this specimen was about the same as in speci-<br>fatigue behavior in squeeze-cas fatigue life of this specimen was about the same as in specimens in which the eutectic constituent initiated cracks. It smooth specimens subjected to rotary bending. Crack-initiaseems that the new oxide is not particularly deleterious, if tion sites were at the silicon particles within the eutectic it is not folded and aggregated. constituents at the surfaces of specimens. They suggested

though the mold was tilted during the pouring to minimize static strength.



Fig. 5—Crack-initiation site at an oxide revealed by SEM (SDAS  $= 17$  $\mu$ m, axial fatigue with maximum stress of 175 MPa,  $R = 0.1$ , failed at  $7.8 \times 10^5$  cycles).

their formation. Figure 6(a) shows such an oxide film, which initiated the fatigue crack in a specimen with a SDAS of 16  $\mu$ m. The film is  $Al_xO_y$ , with a small amount of Si and barely a trace of Mg. At a higher magnification, we found submicron particles of  $AI_xO_y$  (probably  $AI_2O_3$ ) that decorated the surface of the films. These are the new oxides described by Campbell *et al.*<sup>[34]</sup> At a much lower magnification (Figure  $6(b)$ ), the oxide appears as folded films, which follow eutectic constituents for several SDASs.

# E. *The HCF Crack Initiation at Eutectic Areas*

When the SDAS is less than  $25 \mu m$  and no large oxide inclusions are present, HCF cracks initiate exclusively from (SDAS = 25  $\mu$ m, bending fatigue with maximum strain of 0.0016,  $R =$  the eutectic constituent. Figure 7 shows a portion of a rather  $-1$ , failed at  $1.4 \times 10^6$  eveles); and (b) initiation site at an oxide film are eutec -1, failed at  $1.4 \times 10^6$  cycles); and (b) initiation site at an oxide film<br>(SDAS = 17 µm, axial fatigue with maximum stress of 130 MPa,  $R = 0.2$ , failed at  $5.0 \times 10^6$  cycles).<br>(SDAS = 17 µm, axial fatigue with maximum from the aluminum-rich phase; EDX analysis shows that, on the surface of a debonded silicon particle, there is a layer *et al.*<sup>[35]</sup> have stated that the fatigue cracks initiate from old of aluminum. Well-organized marks left by the debonded or "new" oxides, and that the fatigue lives of most aluminum silicon particles can also be seen in Figure 7, which indicated

quality and casting technique. The stress has to be distributed stiffer than the matrix,<sup>[30]</sup> then the stress has to be distributed Figure 5 shows a new oxide that developed on the surface in such a way that the clusters bear more load than the New oxides formed during turbulent pouring were found that an improvement in fatigue strength can be expected in specimens near the bottom of the casting ingot, even by refining the eutectic silicon rather than increasing the



Fig. 6—New oxides: (*a*) initiation site at a folded oxide film (SDAS =  $16 \mu m$ , axial fatigue with maximum stress of 175 MPa,  $R = 0.1$ , failed (*b*) at  $4.9 \times 10^5$  cycles); and (b) oxide films revealed by light microscopy<br>(SDAS = 22  $\mu$ m, as cast).<br>(SDAS = 22  $\mu$ m, as cast).





of 130 MPa,  $R = 0.2$ , failed at 1.5  $\times$  10<sup>5</sup> cycles). pore lengths measured at the initiation sites on the fracture

The size of a eutectic area was found to significantly affect the fatigue life. In a specimen with a SDAS of 22 mm, a fatigue crack initiated at a relatively small eutectic constituent of  $100 \mu m$  in maximum length. The specimen exhibited the greatest life (2.49  $\times$  10<sup>7</sup> cycles) among the bending-fatigue specimens with a stress/strain ratio (*R*) of  $-1$ , which is 30 times greater than that for a specimen with approximately the same SDAS but with an initiation site of a eutectic constituent of  $417 \mu m$  in maximum length.

# F. *Variation of Size of Crack-Initiation Site with SDAS*

The maximum size and area of the fatal fatigue-crackinitiation region was measured on each fatigue-tested specimen. Figures 8 and 9 show the size and area distribution as a function of SDAS for both the axial- and bending-fatigue testing, under  $R = -1$ , 0.1 and 0.2. Both the maximum length and the area distribution of the initiation site show Fig. 7—Debonded Si particles in a crack-initiation site at an interdendritic the same trends in Figures 8 and 9. For discussion, we entectic constituent (SDAS = 29  $\mu$ m, axial fatigue with maximum stress consider the maxi consider the maximum length. It should be noted that the



specimens: (*a*) maximum length and (*b*) area.

and bending specimens. The lengths of the pores at the increased, the fatigue strength decreased. initiation sites increase as the SDAS increases, because the For axial HCF testing with  $R = 0.1$  and  $-1$  (Figures pores tend to increase in size as the SDAS increases (Figure 11(a) and 11(b)), the fatigue life decreases as the pore or  $2(a)$ ), when the SDAS is greater than 28  $\mu$ m. All specimens oxide size increases. Larger eutectic constituents also result that showed porosity on radiographs had relatively short in shorter fatigue life, although there are a few exceptions, as shown in Figures 10(b) and 11(b).

the porosity in the alloy, it appears that its effect on initiating of these particles, would increase fatigue life.



Fig. 9—Distribution of sizes of crack initiation sites in bending fatigue site: (*a*) maximum strain = 0.0016,  $R = 0.1$ ; and (*b*) maximum strain = pecimens: (*a*) maximum length and (*b*) area. 0.0016,  $R = -1$ .

fatigue cracks overshadows the effect of the eutectic constitsurfaces were larger than the lengths detected on the radio- uent, as shown in Figure 10(a) for high-cycle bending fatigue graphs (Figure 2(a)), due to much better resolution obtained with  $R = 0.1$ . But for bending fatigue with  $R = -1$  (Figure by the SEM images of the fracture surfaces. When the SDAS 10(b)), there is a tendency that the fatigue life decreases as is greater than  $\sim$ 25 to 28  $\mu$ m, the cracks usually initiated the pore size increases. Sonsino and Ziese<sup>[19]</sup> also showed at pores with lengths no smaller than  $100 \mu m$ , for both axial that, as the "degree of porosity" and maximum pore size

as shown in Figures 10(b) and 11(b).

When the SDAS is less than  $\sim$  25 to 28  $\mu$ m, either oxide When the pore size is less than a critical size of about 100 inclusions or eutectic constituents were found to be the sites  $\mu$ m, the eutectic constituent becomes the preferred initiation of fatigue-crack initiation. If there is no oxide near the sur- site, provided large oxides are absent. The larger the eutectic face, then the eutectic constituent is the site of crack initia- area, the lower the fatigue life, as a result of shorter initiation tion. Five bending-fatigue specimens with SDASs below 28 life. So, in addition to decreasing the pore size to below a  $\mu$ m had not broken after 2  $\times$  10<sup>7</sup> cycles (maximum stress critical size and eliminating oxides and oxide films in the  $=$  115 MPa,  $R = 0.1$ ) when the tests were terminated. melt, measures that would reduce the stress concentration This may indicate an absence of oxide inclusions, eutectic within the eutectic constituent, such as a refinement of the constituents, and large pores as possible initiation sites. With size of the silicon particles and reduction of the aspect ratio



site: (*a*) maximum stress = 175 MPa,  $R = 0.1$ ; and (*b*) maximum stress International, Warrendale, PA, 1995, pp. 75-90.<br>= 85 MPa,  $R = -1$ .<br>14. D. St John, C. Caceres, D. Zhang, and G. Edward

A356.2-T6 alloy, with a variety of SDASs and porosities,<br>were investigated. The results show the following.<br>16, pp. 391-403.<br>19. C.M. Sonsino and J. Ziese: *Int. J. Fat.*, 1993, vol. 15, pp. 75-83.

- 19. C.M. Sonsino and J. Ziese: *Int. J. Fat.*, 1993, vol. 15, pp. 75-83. 1. The HCF cracks initiate at porosity, oxides, or eutectic 20. J.H. Elsner, E.P. Kvam, and A.F. Grandt, Jr.: *Metall. Mater. Trans. A*,
- 2. When the SDAS is greater than  $\sim$  25 to 28  $\mu$ m, the pores 21. P.C. Inguanti: *Proc. 17th Nat. SAMPE* with a length greater than about 100  $\mu$ m are the main Lake, NY, Oct. 22–24, 1985, pp. 61-73. with a length greater than about 100  $\mu$ m are the main Lake, NY, Oct. 22–24, 1985, pp. 61-73.<br>crock initiation sites. For HCE the effect of SDAS is 22. J.M. Boileau, J.W. Zindel, and J.E. Allison: SAE Technical Papers
- 3. When the SDAS is below  $\sim$  25 to 28  $\mu$ m, the pore size 23. W. Chen, B. Zhang. T. Wu, D.R. Poirier, P. Sung, and Q.T. Fang: in is below the critical value and large eutectic constituents *Automotive Alloys II*, S.K. is below the critical value, and large eutectic constituents<br>
initiate the HCF cracks. Large eutectic constituents result<br>
in a lower fatigue life than when that type of initiation<br>
site is smaller. Most of the silicon par in the eutectic initiators of fatigue cracks.<br>The oxide defects initiate the fatigue crack when they <br>26. Q.T. Fang and D.A. Granger: in Light Metals 1989, P.G. Campbell,
- 4. The oxide defects initiate the fatigue crack when they<br>are near or at the surface, regardless of SDAS. Old oxide<br>films are more deleterious to fatigue life than the new<br>oxide films.<br>These starting and D.A. Granger: in

5. Since fatigue cracks sometimes initiate at eutectic constituents in alloy A356.2, a refinement in the size and aspect ratio of the silicon particles would improve the resistance to the fatigue-crack initiation.

# **ACKNOWLEDGMENTS**

The authors thank the United States Department of Energy for financial support. We also express our gratitude to Mr. G. Chandler, University of Arizona, for sharing his expertise in SEM with us, and to Professor L. Demer, for supervising the radiography and for being available to discuss SEM images. Dr. Q.T. Fang, Alcoa Technical Center, kindly supplied the casting ingots of A356 used in this study.

- 1. R.E. Spear and G.R. Gardner: *AFS Trans.*, 1960, vol. 68, pp. 36-44.
- 2. K. Radhakrishna, S. Seshan, and M.R. Seshadri: *AFS Trans.*, 1980, vol. 88, pp. 695-702.
- 3. K.J. Oswalt and M.S. Misra: *AFS Int. Cast Met. J.*, 1981, vol. 6, pp. 23-40.
- 4. J. Eady and D.M. Smith: *Mater. Forum*, 1986, vol. 9, pp. 217-23.
- 5. M.K. Surappa, E. Blank, and J.C. Jaquet: *Scripta Metall.*, 1986, vol. 20, pp. 1281-86.
- 6. B. Closset and J.E. Gruzleski: *Metall. Trans. A*, 1982, vol. 13A, pp. 945-51.
- 7. G. Gustafsson, T. Thorvaldsson, and G.L. Dunlop: *Metall. Trans. A*, 1986, vol. 17A, pp. 45-52.
- 8. C.H. Caceres and J.R. Griffiths: *Acta Mater.*, 1996, vol. 44, pp. 25-33.
- 9. Q.G. Wang and C.H. Caceres: *Mater. Sci. Eng. A*, 1998, vol. 241A, pp. 72-82.
- 10. D.L. Zhang and L. Zheng: *Metall. Mater. Trans. A*, 1996, vol. 27A, pp. 3983-91.
- 11. C.H. Caceres and Q.G. Wang: *AFS Trans.*, 1996, vol. 104, pp.
- 
- 13. J. Nath: SAE Technical Papers Series (SP-1097), No. 950723, SAE
- 14. D. St John, C. Caceres, D. Zhang, and G. Edwards: *Mater. Aust.*, 1996 (April), vol. 28, pp. 14-16.
- 15. C.Y. Kung and M.E. Fine: *Metall. Trans. A*, 1979, vol. 10A, pp. 603-10.
- 16. M.J. Couper, A.E. Neeson, and J.R. Griffiths: *Fat. Fract. Eng. Mater.* **IV. CONCLUSIONS** *Struct.*, 1990, vol. 13, pp. 213-27.
- High-cycle fatigue-crack initiation and propagation in 17. J.C. Ting and F.V. Lawrence, Jr.: *Fat. Fract. Eng. Mater. Struct.*, 1993,<br>356.2. T6 alloy with a variety of SDASs and porosities vol. 16, pp. 631-49.
	-
	-
- constituents, depending on the SDAS.<br>
When the SDAS is greater than  $\sim$ 25 to 28  $\mu$ m, the pores 21. P.C. Inguanti: *Proc. 17th Nat. SAMPE Technical Conf.*, Kiamesha
	-
- crack-initiation sites. For HCF, the effect of SDAS is<br>overshadowed by the effect of porosity on the fatigue life.<br>When the SDAS is below  $\sim$  25 to 28  $\mu$ m, the pore size<br>23. W. Chen, B. Zhang. T. Wu, D.R. Poirier, P. S
	-
	-
	- 25. W. Chen, B. Zhang, and D.R. Poirier: The University of Arizona,
	-
	-
	- Tests of Metallic Materials," ASTM E466-82, *Annual Book of ASTM*

- 29. K. Tynelius, J.F. Major, and D. Apelian: *AFS Trans.*, 1993, vol. 101, pp. 401-13. 34. J. Campbell, C. Nyahumwa, and N.R. Green: in *Advances in Aluminum*
- 30. S. Shivkumar, L. Wang, and R. Lavigne: *Light Metals 1993*, S.K. Das, ed., TMS, Warrendale, PA, 1993, pp. 829-38.
- 
- 32. O. Umezawa and K. Nagai: *Iron Steel Inst. Jpn. Int.*, 1997, vol. 37, pp. 1170-79.
- 33. M.E. Seniw, M.E. Fine, E.Y. Chen, M. Meshii, and J. Gray: in *High*

*Standards*, ASTM, Philadelphia, PA, 1982, vol. 03.01, pp. 465-69. *Cycle Fatigue of Structural Materials*, W.O. Soboyejo and T.S. Srivat-

- ed., TMS, Warrendale, PA, 1993, pp. 829-38.<br>
Fechnology, M. Tiryakioglu and J. Campbell, eds., ASM<br>
ed., TMS, Warrendale, PA, 1993, pp. 829-38.<br>
INTERNATIONAL, Materials Park, OH, 1998, pp. 225-34.<br>
INTERNATIONAL, Material
	- 31. H. Yokoyama, O. Umezawa, K. Nagai, and T. Suzuki: *Iron Steel Inst.* 35. Q.G. Wang, D. Apelian, and J.R. Griffiths: in *Advances in Aluminum Casting Technology*, M. Tiryakioglu and J. Campbell, eds., ASM INTERNATIONAL, Materials Park, OH, 1998, pp. 217-24.
		- 36. F.T. Lee, J.F. Major, and F.H. Samuel: *Metall. Mater. Trans. A*, 1995, vol. 26A, pp. 1553-70.