dislocations due to the presence of fine Nb(C,N) carbonitrides, as suggested by Seeger *et al.*^[11] In the A steel, Ti(C,N) **REFERENCES** carbonitrides due to the Ti addition here additionally promote carbonniques due to the 11 addition here additionary promote
the dislocation pinning, thereby leading to the larger and the Matheuse M. Matheuse M. Metall., 1956, vol. 8, pp. 21-26.
2. H. Watanabe, Y.E. Smith, and R.D. Pej Bauschinger effect. On the other hand, the strain hardening *Austenite*, AIME, New York, NY, 1997, pp. 140-68.
 Austenite, AIME, New York, NY, 1997, pp. 140-68.
 Austening *Austenite*, AIME, New York, NY, 1997, pp. 140 effect is much larger in the B steel than in the A steel, as 3. *Specification for High-Test Linepipe*, 18th ed., American Petroleum in the *standard SXL*, New York, 1971. shown in the stress-strain curves of Figure 4. This is because
considerable strain hardening occurs in the B steel under
cation No. 2950-6-6. 1973. the 1.4 pct strain applied during piping, whereas almost no 5. G.E. Dieter: *Mechanical Metallurgy*, 3rd ed., McGraw-Hill, New York, strain hardening results from the 1.6 pct strain in the A NY, 1986, pp. 236-37. strain hardening results from the 1.6 pct strain in the A
steel. This difference in strain hardening of the two steels
is attributed to the presence or absence of a yield-point
7. T. Taira, T. Osuka, and Y. Ishida: *Proc.* phenomenon. The B steel undergoes considerable strain *Steel Processing Conf.*, Pittsburgh, PA, 1977, p. 33.
 bardening under strains as small as 1.4 pct because of its 8. G. Tither and M. Lavite: *J. Met.*, 1975, vol. 2 hardening under strains as small as 1.4 pct because of its
continuous yielding behavior, whereas the A steel hardly has
any strain hardening because of the yield-point phenomenon.
11. A. Seeger, S. Mader, and H. Krammuller This yield-point phenomenon is also associated with alloy 12. A.P. Coldren, Y.E. Smith, and R.L. Cryderman: *Processing and Proper-*

compositions and microstructures According to Coldren *et* ties of Low-Carbon Steel, AIM compositions and microstructures. According to Coldren et

al.^[12,13] and Irani and Tither^[14] by adding molybdenum into

al.^[12,13] and Irani and Tither^[14] by adding molybdenum into

Gas and Oil Industry Applica HSLA steels, the $\gamma \to \alpha$ transformation temperature can be wich, CN, 1977, pp. 14-28.
lowered, pearlite formation can be discouraged, and low-
14. J.J. Irani and G. Tither: ISI Publication, 1967, vol. 104, p. 135. 16. Iowered, pearlite formation can be discouraged, and lowtemperature transformation products such as acicular ferrite having high dislocation density can be promoted. Because of this high density of mobile dislocations, the yield-point phenomenon does not occur as the movement of dislocations Measurement of the Activity of Boron
under an applied stress gradually increases and the elastic in Liquid Connect using a Fourunder an applied stress gradually increases and the elastic in Liquid Copper using a Four-
limit decreases. In this study, the Mo-containing B steel has formed acicular ferrite having high density of dislocations Phase Equilibrium Technique (Figure 3(c)) and is, accordingly, confirmed to have the lower yield strength and the continuous yielding behavior K.T. JACOB, SHASHANK PRIYA, (Figure 4 and Table III). Consequently, in the A steel, the and YOSHIO WASEDA Bauschinger effect after piping is larger due to the precip-Bauschinger effect after piping is larger due to the preciptation of fine carbonitrides, but little strain hardening occurs

bauschinger effect overriding the phenomenon. With the

Bauschinger effect overriding the strain

and the Bauschinger effect decreasing it, are operating and
explain the yield strength variations occurring in API-X70 is some uncertainty in the reported values for the eutectic
steel plates after piping. Particularly, ca that the absence of the yield-point phenomenon is associated with the larger strain hardening effect, Mo was added to eliminate or to reduce the yield-point phenomenon. This K.T. JACOB, Professor, Department of Metallurgy and Materials
proves useful in preventing the reduction of yield strength Research Center, and SHASHANK PRIYA, Graduat and increases it. In evaluating pipe formability, investiga-

India. YOSHIO WASEDA, Professor and Director, is with the Institute for

India. YOSHIO WASEDA, Professor and Director, is with the Institute for tions of the tensile properties including the yield-point phe-

nomenon provide valuable data in addition to the evaluation

of the Bauschinger effect.

Manuscript submitted October 29, 1999.

Manuscript submitted October

can be explained by two competing mechanisms: the strain
hardening effect increasing the yield strength and the
Bauschinger effect causing a yield strength drop.
Discussing the Bauschinger effect first, it is much larger
i

-
-
-
-
-
-
-
-
-
-
-
-
-
-

Research Center, and SHASHANK PRIYA, Graduate Student, Department

Manuscript submitted October 29, 1999.

Yukinobu *et al.*^[2] have determined the activity of boron in liquid Cu-B alloys at low concentrations by electromotive force measurement. A cell incorporating calcium aluminoborate melt as the electrolyte was used. The activities exhibit large positive deviation from Raoult's law. Batalin *et al.*[3] have determined partial and integral enthalpy of mixing of the liquid Cu-B alloys in the Cu-rich region at 1790 K by high-temperature calorimetry using high purity copper and amorphous boron as starting materials. Their values for partial enthalpy of boron at low concentrations show large scatter. From their results, the partial heat of mixing of boron at infinite dilution in liquid Cu-B alloys can be estimated as 57.57(\pm 20) kJ·mol⁻¹ using the subregular solution model. Witusiewicz,^[4] using an isoperibol high-temperature calorimeter, has investigated the thermodynamic properties of liquid Cu-B alloys. A value of $45(\pm10)$ kJ·mol⁻¹ for the partial enthalpy of mixing of boron at infinite dilution in liquid Cu-B alloys relative to solid boron as the standard state was obtained.

The purpose of this article is to report measurements on dilute Cu-B alloys at 1723 K using a new four-phase equilibrium technique. The method can be considered as an extension of the conventional procedure involving metal-
slag-gas equilibration, where the gas phase containing car-
 $\frac{F}{g}$. 1—Schematic diagram of the apparatus. bon monoxide is pre-equilibrated with graphite to define the carbon and oxygen chemical potentials. Under the reducing
atmosphere, liquid diboron trioxide (B_2O_3) is partially
reduced by graphite generating a liquid Cu-B alloy and
carbon monoxide at controlled pressure. After que *room temperature, the concentration of B in the liquid copper <i>p* is measured. The equilibrium boron concentration in copper is measured as a function of the partial pressure of carbon monoxide in the gas phase.

High purity materials (Cu $>$ 99.999 mass pct, B₂O₃ $>$ 99.99 mass pct, $CO > 99.99$ pct purity, and graphite of spectral grade) are used. B₂O₃ was dried first in flowing Ar for 8 hours at 423 K and then under vacuum at 473 K for 4 hours before use. Mixtures of Ar + CO of th composition are prepared by mixing metered streams of Ar and CO in a chamber filled with glass beads. Mass flow controllers are used to measure the flow rates accurately.

A schematic diagram of the apparatus used for measure-
ment is shown in Figure 1. Liquid copper is held in a graphite
crucible covered by a layer of liquid B_2O_3 melt. Carbon
monoxide or a controlled mixture of Ar + CO carbon was observed in the cooler parts of the vertical alu-
mina tube in which the crucible was placed. Since the carbon
deposition generates CO_2 in the gas phase and affects the
oxygen potential, the gas phase is re-e oxygen potential, the gas phase is re-equilibrated with graph-
ite by passing the gas through a chamber containing graphite
chips maintained at the temperature of measurement. A rotat-
each experiment, the crucible is lowe chips maintained at the temperature of measurement. A rotat-
ing stirrer allows mixing of the metal and slag and accelerates cooled region. The concentration of boron in copper is detering stirrer allows mixing of the metal and slag and accelerates cooled region. The concentration of boron in copper is deter-
the attainment of equilibrium between the gas and condensed mined using inductively-counled plas the attainment of equilibrium between the gas and condensed mined using inductively-coupled plasma–emission spec-
phases. Although the equilibrium is attained in 1.5 hours at trometer. The approach to equilibrium at consta phases. Although the equilibrium is attained in 1.5 hours at trometer. The approach to equilibrium at constant partial 1723 K, the system is maintained at the temperature with pressure of CO is verified from both higher an 1723 K, the system is maintained at the temperature with pressure of CO is verified from both higher and lower constirring for 2.5 hours. After passing over the melt, the gas centrations of boron in liquid copper. Analysis exits the constant temperature zone through a small orifice phase indicated that the concentration of copper in the melt in the graphite plug placed below the crucible. The deposi-
tion of carbon at furnace exit therefore does not alter the The equilibrium concentration partial pressure of carbon monoxide in the high-temperature K at different partial pressures of carbon monoxide in the zone. The temperature of the metal and slag is measured by gas phase is shown in Table I. The same value for the

$p_{\rm CO}/p^{\circ}$	$X_{\rm B}$	$a_{B(s)}$
1.001	0.0222	0.0757
0.886	0.0262	0.0883
0.775	0.0333	0.1097
0.679	0.0416	0.1336
0.575	0.0568	0.1746
0.471	0.0779	0.226
0.429	0.0975	0.2696
0.387	0.118	0.3108
	$p^{\circ} = 1.013 \times 10^{5}$ Pa (standard pressure).	

centrations of boron in liquid copper. Analysis of the slag

The equilibrium concentration of boron in copper at 1723

Fig. 2—Plot of the partial pressure of carbon monoxide as a function of composition of boron in liquid Cu in equilibrium with liquid B_2O_3 and

concentration of boron in liquid copper is obtained by
approaching equilibrium from higher and lower partial pres-
sures of CO. The partial pressure of CO is plotted as a
function of alloy composition in Figure 2 at 1723

$$
B_2O_3(l) + 3C \text{ (graphite)} \rightarrow 3CO \text{ (g)} + 2B_{Cu} \quad [1]
$$

boron can be calculated from the Gibbs energy change for reaction [1]: **reaction** [1]:

$$
\Delta G_{[1]}^{o} (1723 \text{ K}) = - \text{ RT} \ln K_{[1]} = - \text{RT} \ln (a_{B(s)}^{2} \cdot p_{\text{CO}}^{3})
$$
\n[2]

where $a_{B(s)}$ is the activity of boron in the liquid alloy relative assessed by Chart.^[6] It is likely that the alumina-saturated to solid boron as the standard state, p_{CO} is the partial pressure calcium alumino-silicate melt used as the electrolyte is not of CO, and $K_{[1]} = 5.60 \times 10^{-3}$ is the equilibrium constant a pure ionic conductor. Presence of some electronic conducfor the reaction at 1723 K. The computed values of $a_{B(s)}$ tivity can explain the higher activities of boron obtained by from Eq. [2] are given in Table I. The activity of boron in Yukinobu *et al.* Cu-B alloy relative to liquid boron as the standard state can The function α_B defined as be calculated from the relation

RT ln
$$
a_{B(l)} = RT \ln a_{B(s)} - (\mu_{B(l)}^0 - \mu_{B(s)}^0)
$$
 [3]

to liquid boron as the standard state, and $\mu_{B(1)}^0 - \mu_{B(s)}^0$ is the
difference in chemical potential for pure boron in solid and
liquid states. The value of $\mu_{B(1)}^0 - \mu_{B(s)}^0$ at 1723 K is com- $B_{\text{B}(l)}^{\text{o}} - \mu_{\text{B}(s)}^{\text{o}}$ at 1723 K is computed using data for the pure element boron from Knacke

composition of boron in liquid Cu in equilibrium with liquid B_2O_3 and Fig. 3—Variation of the activity of boron and copper as a function of graphite at 1723 K.

formation of tetraboron carbide $(B_{4+x}C)$ was encountered at respectively.^[5] The activity of B is plotted as a function of lower partial pressures of CO. The reduction reaction can be written as boron as the standard s to solid boron reported by Yukinobu *et al.*^[2] in the tempera-
ture from 1423 to 1523 K, using a cell with molten calcium The activity of the boron in Cu-B alloy with respect to solid alumino-silicate as the electrolyte, is also shown for compari-
horon can be calculated from the Gibbs energy change for son. After correcting for the differenc higher than those obtained in this study. Yukinobu *et al.* have also measured activities in Fe-B and Co-B alloys using the same technique. Their values for the activity of boron in the Fe-B system are significantly higher than those critically

$$
\alpha_{\rm B} = RT \ln \gamma_{\rm B}(t)/(1 - X_{\rm B})^2 = \Delta G_{\rm B}(t)/(1 - X_{\rm B})^2 \quad [4]
$$

where $a_{B(l)}$ is the activity of boron in liquid alloy relative in Figure 4. The activity coefficient of boron $\gamma_{B(l)}$ is calcu-

$$
\alpha_{\rm B} = 5418 - 38,849 \, X_{\rm B} \, (\pm 500) \tag{5}
$$

mate. The excess chemical potential or excess partial molar B) in the solid and liquid Cu-B alloys. Values for the differ-
Gibbs energy of B at 1723 K with reference to pure liquid ence in chemical potential for pure coppe Gibbs energy of B at 1723 K with reference to pure liquid ence in chemical potential for pure copper and boron in
boron as the standard state is obtained from the expression solid and liquid states are computed from the da boron as the standard state is obtained from the expression solid and liquid states are computed from the data given in the compilation of Knacke *et al.*^[5] The constant value given the compilation of Knacke *et al.*[[]

$$
\Delta \mu_{\rm B}^E = \Delta G_{\rm B}^E = RT \ln \gamma_{\rm B(0)} = (1 - X_{\rm B})^2
$$

[5418 - 38,849 X_B] J mol⁻¹ [6]

Although the equation is obtained from measurements on alloys with $X_B < 0.12$, it may be extrapolated up to phase boundary in the absence of other information. From the Gibbs-Duhem equation, the excess chemical potential of Cu and the integral excess Gibbs energy of mixing of liquid Cu-B alloys are obtained: The lattice stabilities of B in the fcc structure are taken from

$$
\Delta \mu_{\text{Cu}}^E = \Delta G_{\text{Cu}}^E = RT \ln \gamma_{\text{Cu}} = (X_{\text{B}})^2
$$
\n[24,843 - 38,849 X_B] J mol⁻¹ [7] [7] [7]

$$
\Delta G^E = X_B (1 - X_B) [5418 - 19,424 X_B] \text{ J mol}^{-1}
$$
 [8]

The system exhibits positive values for excess Gibbs energy of mixing for copper-rich alloys and negative values at higher concentrations of boron. where the subscript rho represents the phase with rhombo-

To obtain the temperature dependence of the excess Gibbs hedral structure. energy, the ratio (τ) of enthalpy to excess entropy of mixing The two terminal solid solutions were assumed to be was estimated as 4000 K. According to the correlation of regular, and excess Gibbs energy is defined by Kubaschewski,[7]

$$
\frac{\Delta H^M}{\Delta S^E} = 0.7813 \left(T_A^b + T_B^b \right) \tag{9}
$$

where T_A^b and T_B^b are the boiling points of pure metals A $\Delta G^E = X_B (1 - X_B)(24,000)$ J mol⁻¹ [15] and B, ΔH^M and ΔS^E are the extremum values for enthalpy for the B-rich rhombohedral solid solution. The solidus and

and excess entropy of mixing, the value of τ for the Cu-B system is 5450 K. Subsequently, Kubashewski $^{[8]}$ proposed that the ratio between partial enthalpy and partial excess entropy of solute elements in dilute solutions is 3400 K. Lupis and Elliot^[9] have also proposed a similar relationship and a value of τ equal to 3000(\pm 1000) K. Using τ = 4000 K, the excess Gibbs energy can be partitioned into enthalpy and entropy terms. The partial enthalpy of boron at infinite dilution at 1790 K obtained by this procedure is 58.6 $kJ \cdot mol^{-1}$, which is in fair agreement with the calorimetric values reported by Batalin *et al.*^[3] and Witusiewicz,^[4] considering their experimental uncertainties.

The chemical potential of each component at solidus composition is equal to its chemical potential at the liquidus at constant temperature and pressure: $\mu_{\rm B}^s = \mu_{\rm B}^l$ and $\mu_{\rm Cu}^s =$ μ_{Cu}^l . Expressing the chemical potentials in the solid and liquid phases as a sum of ideal and excess components, one obtains the following equations containing two unknown compositions:

$$
\ln\left(\frac{X'_{\rm B}}{X_{\rm B}^s}\right) = \left(\frac{\mu_{\rm B(s)}^0 - \mu_{\rm B(l)}^0}{RT}\right) + \left(\frac{\Delta G_{\rm B(s)}^E - \Delta G_{\rm B(l)}^E}{RT}\right) \quad [10]
$$

$$
\ln\left(\frac{(1 - X'_{\rm B})}{(1 - X'_{\rm B})}\right) = \left(\frac{\mu_{\rm Cu(s)}^0 - \mu_{\rm Cu(l)}^0}{RT}\right) + \left(\frac{\Delta G_{\rm Cu(s)}^E - \Delta G_{\rm Cu(l)}^E}{RT}\right) \quad [11]
$$

where X^s_B and X^l_B are the mole fractions of B at the solidus and liquidus at temperature T and ΔG_i^E is the relative excess The uncertainty corresponds to twice the standard error esti-
mate The excess chemical potential or excess partial molar (B) in the solid and liquid Cu-B alloys. Values for the differfor the heat capacity of the liquid above the melting point is also used for the supercooled state. The enthalpy of fusion and melting points of pure metals used in the computation are as follows.

Teppo and Taskinen:[10]

$$
G_{\rm B(fcc)}^0 - G_{\rm B(rho)}^0 = 43{,}516 - 11.607T \qquad J \, \rm mol^{-1} \qquad [12]
$$

The lattice stability of Cu in the rhombohedral structure is estimated as

$$
G_{\text{Cu(rho)}}^0 - G_{\text{Cu(fcc)}}^0 = 22,000 - 5T \qquad \text{J mol}^{-1} \quad [13]
$$

$$
\Delta G^E = X_B (1 - X_B)(34,765) \qquad \text{J mol}^{-1} \qquad [14]
$$

for the Cu-rich solid solution with fcc structure, and

$$
\Delta G^E = X_{\text{B}} \left(1 - X_{\text{B}} (24,000) \right) \quad \text{J mol}^{-1} \quad [15]
$$

Fig. 5—Computed phase diagram for the system Cu-B. The dotted line
shows the diagram reported in the current ASM compilation. The experi-
 Computed Computed System

liquidus compositions at selected temperatures are obtained

$$
\Omega_{\rm rho} > \Delta H_{\rm Cu}^{\rm o,f} + \Delta H_{\rm B}^{\rm o,f} \left(\frac{X_{\rm B}^{\rm liq}}{X_{\rm Cu}^{\rm liq}} \right)_{\rm eut} \tag{16}
$$

available in the literature.

1. D.J. Chakrabarti and D.E. Laughlin: *Bull. Alloy Phase Diagrams*, of Cordoba, 5000 Cordoba, Argentina. 1982, vol. 3, pp. 45-48. Manuscript submitted December 29, 1999.

- 2. M. Yukinobu, O. Ogawa, and S. Goto: *Metall. Trans. B*, 1989, vol. 20B, pp. 705-10.
- 3. G.I. Batalin, V.S. Sudavtsova, and M.V. Mikhailovskaya: *Sov. Nonferrous Met. Res.*, 1985, vol. 13, pp. 177-79.
- 4. V.T. Witusiewicz: *J. Alloys Compounds*, 1994, vol. 203, pp. 103-16.
- 5. O. Knacke, O. Kubashewski, and K. Hesselman: *Thermochemical Properties of Inorganic Substances*, 2nd ed., Springer-Verlag, Berlin, 1991, vols. I and II.
- 6. T.G. Chart: *Critical Assessment of Thermodynamic Data for the Iron-Boron System*, National Physical Laboratory of United Kingdom, Middlesex, United Kingdom, 1982.
- 7. O. Kubaschewski: *Phase Stability in Metals and Alloys*, P. Rudman, J. Stringer, and R. I. Jafee, eds., McGraw-Hill, New York, NY, 1967.
- 8. O. Kubashewski: *High Temp. High Pressure*, 1981, vol. 13, pp. 435-40.
- 9. C.H.P. Lupis and J.F. Elliot: *Acta Metall.*, 1967, vol. 15, pp. 265-76.
- 10. O. Teppo and P. Taskinen: *Mater. Sci. Technol.*, 1993, vol. 9, pp. 205-12. 11. S.V. Varamban and K.T. Jacob: *Metall. Mater. Trans. A*, 1998, vol.
- 29A, pp. 1525-27. 12. *Binary Alloy Phase Diagrams*, 2nd ed., T.B. Massalski, P.R. Subraminian, H. Okamoto, and L. Kaoprazak, eds., ASM INTERNATIONAL, Materials Park, OH, 1990.
- 13. J.P. Piton, G. Vuillard, and T. Lundstrom: *C.R. Acad. Sci., Ser. C*, 1974, vol. 278, pp. 1495-96.
- 14. J. Rexer and G. Petzow: *Metall.*, 1970, vol. 24, pp. 1083-86.
- 15. F. Wald and R. Stormont: *J. Less-Common Met.*, 1965, vol. 9, pp. 423-33.
- 16. I. Higashi, Y. Takahashi, and T. Atoda: *J. Less-Common Met.*, 1974, vol. 37, pp. 199-204.

Camphor System.

L.M. FABIETTI

by solving Eqs. [10] and [11] using an iterative procedure. During directional solidification of alloys, the time-depen-The solidus shows retrograde behavior at the boron-rich dent phenomenon plays a crucial role in governing the microend. Varamban and Jacob^[11] have recently discussed the structure evolution process and in the redistribution of retrograde solubility in semiconductors. The condition for solute.^[1] During the growth of a planar interface at a fixed inducing retrograde solubility is external velocity, the rejected solute (for solute distribution coefficient \leq 1) builds up a boundary layer of solute near the interface, and the interface velocity is initially zero and [16] approaches the external velocity when steady-state growth

where Ω_{rho} is the enthalpy parameter of a pseudoregular
solution for the B-rich solid solution. The expression was
solution for the B-rich solid solution. The expression was
derived assuming liquid solution as ideal is 0.24 at. pct B. Thus, the phase diagram computed from the to present these experimental results on the dynamics of results obtained in this study is consistent with information faceted interface motion.

REFERENCES L.M. FABIETTI, Assistant Professor and Researcher of Conicet, is with the Facultad of Mathematics Astronomy and Physics, Universidad Nacional