Transient Liquid-Phase Bonding in Two-Phase Ternary **Systems**

C.W. SINCLAIR, G.R. PURDY, and J.E. MORRAL

The process of isothermal solidification during transient liquid-phase (TLP) bonding in a ternary system is analyzed. In the most usual situation, and in contrast to the binary case, the composition of the liquid is required to change continuously as solidification proceeds. If the solubilities and/or diffusion coefficients of the two solutes are very different, the solidification stage is clearly divided into two parabolic regimes, the first dominated by the "faster" solute and the second by the slower of the two. In extreme cases, full solidification may not be realized in experimentally accessible times.

a liquid phase at a rate determined primarily by solid-state diffusion. The liquid results from the placement at the joint
of a thin layer (interlayer) with a melting point lower than
that of the material to be joined. In the simplest case, the
base material is a pure component, an base material and the interlayer will be made up of mote
than two components. For the most part, the literature makes
only passing reference to the possible effect of a third compo-
nent (a second solute) on the process o

stages. heading of the joinning emperature, solution and homogenization. The usual treation of the isothermal solidification and properation. The usual transformed by the solid-state diffusion coefficients D_{ik}^a . It is solid-state diffusion; consequently, the interlayer shrinks, (1) The most usual case will involve the continual shifting
and eventually disappears. Under the reasonable assumption of the instantaneous interfacial tie-line, and eventually disappears. Under the reasonable assump-
tions of local equilibrium at the solid-liquid interface, planar dictated by the two mass balances. This process will tions of local equilibrium at the solid-liquid interface, planar dictated by the two mass balances. This process will
solid-liquid interfaces complete mixing in the thin liquid
continue until the final liquid solidifies, l

I. INTRODUCTION layer, and constant diffusion coefficient in the solid, the THE problem of transient liquid-phase (TLP) bonding
(along with the allied one of liquid-phase sintering) has
received considerable attention in recent years. The joining
process holds high promise for the controlled bond

$$
w \propto \sqrt{D_1^{\alpha} t} \tag{1}
$$

The experimental situation is reviewed, along with the
analysis of the binary problem in a recent article by Zhou
et al.^[3] The process is considered as a sequence of distinct
stages: heating to the joining temperatur

solid-liquid interfaces, complete mixing in the thin liquid solution continue until the final liquid solidifies, leaving a set of solute profiles in the solid, which will relax by diffusion on further isothermal treatment. The last liquid to solid-C.W. SINCLAIR, Graduate Student, and G.R. PURDY, Professor, are ify will have a composition that depends on the full

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Fig. 1—Schematic illustration of the equilibrium condition between liquid interlayer and solid phase during isothermal solidification stage for a binary system. The interfacial concentrations are assumed constant and given by the local equilibrium conditions. The tie-line length is defined as $\Delta C_i^{\prime\prime}$ = $C_i^{l\prime\,\gamma}$ – $C_i^{\prime\,\gamma\overline{l}}$.

- (a) where the solubilities and solid-state diffusivities of the two solutes are similar; and
- (b) where the solubility and/or the diffusivity of one of the solutes is much smaller than that of the other.
- (2) There is a special case of some interest, for which the liquid will solidify with constant composition equal to the initial composition formed on melting back. We will call this the *stationary case*. It can be understood as follows.

Referring to Figure 2, we write for each solute *i*:

$$
\frac{dw}{dt} \left(\Delta C_i^{\alpha l} \right) = 2D_{ii}^{\alpha} \nabla C_i^{\alpha} \tag{2}
$$

where *w* is the interlayer thickness. We have ignored diffusional interaction between solutes. If, as a further approximation, we assume the D_{ii}^{α} are constant, and that $\delta C_i^{\alpha} \ll \Delta C_i^{\alpha l}$, then the error function solutions for the con-
in the initial metrics of the interlayer (a) An early stage in the solidification

$$
\nabla C_i^{\alpha} = \frac{\delta C_i^{\alpha}}{\sqrt{\pi D_{ii}^{\alpha} t}} \tag{3}
$$

where δC_i^{α} is the concentration range of solute *i* in the base solid ($=C_i^{\alpha}$ in Figure 2, which is drawn for a pure solvent base material). D_{ii}^{α} is its diffusion coefficient in the solid. base material). D_{ii}^{α} is its diffusion coefficient in the solid. of interfacial concentrations for the balance of the solidi-
On equating velocities for the two solutes, 1 and 2, we obtain fication step. We will call

$$
\frac{\sqrt{D_{11}^{\alpha}} \ \delta C_1^{\alpha}}{\Delta C_1^{\alpha'}} = \frac{\sqrt{D_{22}^{\alpha}} \ \delta C_2^{\alpha}}{\Delta C_2^{\alpha'}}
$$
 [4]

stationary case for which interfacial concentrations will be
constant throughout the isothermal solidification process. If
in addition the phase diagram is characterized by constant
solute distribution coefficients, then course of solidification.

(3) A third case may be envisaged which involves the shift- *w* ing of the interfacial tie-line until a particular liquid

by the initial melting of the interlayer. (*a*) An early stage in the solidification profiles apply, and by the initial melting of the interlayer. (*a*) An early stage in the solidification process; the two mass balances f by solute profiles. (*b*) A sequence of tie-lines, as determined by the require ment that the two mass balances be simultaneously satisfied.

composition is reached that will support a constant set fication step. We will call this liquid composition the *terminal liquid*, and the corresponding tie-line the *terminal tie-line*. Note, however, that this state is history dependent and that the condition given in Eq. [4] for which, in conjunction with the phase diagram, defines the the stationary tie-line is not relevant to this case.

$$
\frac{\partial w}{\partial t} \left[\Delta C^{\alpha l} \right] = -2[D^{\alpha}] \left[\nabla C^{\alpha} \right] \tag{5}
$$

Here, we have used the notation developed by Hopfe and Morral, $[4]$ in which column [) and row (] vectors are distinguished by differing parentheses. The concentration gradients in the α phase when $\delta C_i^{\alpha} \ll \Delta C_i^{\alpha l}$ are then given in terms of the square-root diffusivity $[5]$ as

$$
[\nabla C^{\alpha}] = \frac{1}{\sqrt{\pi t}} [r^{\alpha}]^{-1} [\delta C^{\alpha}]
$$
 [6]

Equation [6] is based on the error-function solution to the diffusion equations and is exact in the limit where the ratio of w_0 to the diffusion distance approaches zero. Then

$$
\frac{\partial w}{\partial t} [\Delta C^{\alpha l}] = -\frac{2}{\sqrt{\pi t}} [D^{\alpha}][r^{\alpha}]^{-1} [\delta C^{\alpha}]
$$

$$
= -\frac{2}{\sqrt{\pi t}} [r^{\alpha}][\delta C^{\alpha}]
$$
 [7]

Further, if we express the time dependence of the interlayer thickness *w* as $w = w_0 - \kappa \sqrt{t}$, we have

$$
\kappa[\Delta C^{\alpha l}) = \frac{4}{\sqrt{\pi}} [r^{\alpha}][\delta C^{\alpha}] \tag{8}
$$

which relates the composition vector in the solid $\left[\delta C^{\alpha}\right]$ and Fig. 3—For the special case $D_{11} \gg D_{22}$, solute 1 will be removed from the terminal tie-line $[\Delta C^{\alpha l}]$.

II. THE ISOTHERMAL SOLIDIFICATION PATH

We next inquire into the process of the evolution of the liquid composition from an arbitrarily set initial liquid com-
position. Clearly, if the two solutes have very different solid examined. As a first approximation, the diffusion profile that the two solute mass balances be simultaneously satisfied. be satisfied: If, for example, the solubility and solid-state diffusivity of component 1 yield the greater flux of this solute from the liquid layer, the solidification will proceed at a rate determined by component 1, and the slower diffusing solute, component 2, will be partitioned to the liquid. This is sug-
gested by the schematic illustration of Figure 3, in which
respectively. The subscript $j + 1$ refers to the current interfa-

of interfacial concentrations in the solid and liquid phases; ods. In Section III, we will describe two approaches: one may be found. involving simplified mass balances based on linear composi- The advantage of the preceding scheme is its simplicity of

III. COMPUTATIONAL METHODS

With the Gibbs isotherm defined by constant partition coefficients, the isothermal solidification of the liquid inter-
layer may be predicted *via* a simple mass balance. For this
purpose, diffusion in the liquid layer was assumed to be However, some means of modeling the diffusion profile in must be balanced at the interface to conserve mass:

the liquid and solute 2 will be partitioned to the liquid, as indicated schematically here.

position. Clearly, if the two solutes have very different solid examined. As a first approximation, the diffusion profile solubilities and diffusion coefficients in the solid state, then was assumed linear *(i.e.*, Zener's solubilities and diffusion coefficients in the solid state, then was assumed linear (*i.e.*, Zener's approximation). The con-
the interfacial tie-line will migrate along the two-phase centration of the liquid (which may be centration of the liquid (which may be completely defined by region of the ternary isotherm toward the terminal composi- specifying the concentration of one component and invoking tions defined above in Eq. [8]. This shift of the local equilib- local equilibrium) could then be iterated along the two-phase rium tie-line with time is a consequence of the requirement boundary. The two mass balances (one for each solute) must

$$
C_{j+1}^{\alpha} \sqrt{D^{\alpha}(t + \Delta t)} - C_j^{\alpha} \sqrt{D^{\alpha}t}
$$

= $C_j^L w - C_{j+1}^L (w + \Delta w)$ [9]

gested by the schematic illustration of Figure 3, in which respectively. The subscript $j + 1$ refers to the current interfa-
the solute flux of component 2 is taken as negligible. cal concentration, while the subscript *i* the solute flux of component 2 is taken as negligible. cial concentration, while the subscript *j* refers to the previous The solution of this problem requires continual monitoring interfacial concentration. By iterating t interfacial concentration. By iterating the concentration $g_j^{\alpha} \to C_{j+1}^{\alpha}$, the change in the width of the interlayer (2 Δw) it is clearly suited to modelling using finite-difference meth- and the increment in time needed to reach that width (Δt)

tion gradients in the solid phase in a manner first put forward implementation. However, the assumption of linear diffusion
by Zeners,^[6] and a second, in which the composition gradi-
profiles is often an inaccurate one. by Zeners,^[6] and a second, in which the composition gradi-
ents in the solid are determined more completely. In both finite-difference approach was used to model more precisely finite-difference approach was used to model more precisely. treatments, off-diagonal D_{ik} 's will be assumed negligible and the diffusion profiles in the solid. With this method, the flux
the on-diagonal D 's constant.
the solid phase at the interface at some time t may be in the solid phase at the interface at some time t may be written as

$$
J_i = D_{ii}^{\alpha} \frac{\delta C_i^{\alpha}}{\Delta x} = D_{ii}^{\alpha} \frac{C_i^{\alpha} (x = 0) - C_i^{\alpha} (x = \Delta x)}{\Delta x} \quad i = 1, 2
$$
\n[10]

where the interface is defined at $x = 0$ and Δx represents rapid, such that there develops no gradient in the liquid. the distance step in the finite-difference algorithm. This flux

and the explicit finite difference model (Eqs. [10] and [11]). Error in the finite difference algorithm is manifested as a slight underestimation of the solidification kinetics at short times.

$$
J_i = \frac{\Delta w}{\Delta t} \left[C_i^L - C_i^{\alpha} \right]_{t=t} + \frac{w + \Delta w}{\Delta t} \left[C_i^L \right]_{t=t}
$$

$$
- \frac{w + \Delta w}{\Delta t} \left[C_i^L \right]_{t=t+\Delta t} \quad i = 1, 2
$$
 [11]

The two resulting mass balances may be solved for the interfacial concentrations and change in liquid width $(2 \Delta w)$ given time and distance increments Δt and Δx . Utilization of an explicit finite-difference routine to solve for the concentration profile in the solid results in a conditionally stable solution. For this problem, the solution is stable only for combinations of Δx and Δt such that

$$
0 < \frac{D_{ij}^{\alpha} \Delta t}{\Delta x^2} \le 0.5 \quad i = 1, 2 \tag{12}
$$

The results of these two computation methods are com-
pared in Figure 4 for the Al-Zn-Sn system (aluminum sol-
vent) at 500 °C. In this system, the diffusivity of tin in
tial widths. aluminum is two orders of magnitude lower than that for zinc.[7] The Zener approximation underestimates the rate of solidification at all times (a numerical error in the finite- the diffusivity of tin a multiple of that of zinc) on the rate difference solution makes it appear that the kinetics are faster of solidification. Figure 9 is a series of computed zinc profor the Zener approach at very short times). Figure 5 shows files in the base aluminum material for different times; the the results predicted by the finite-difference model for differ- quantitative similarity to the error-function penetration curve ent concentrations of tin in the liquid at the beginning of at early times, and to the plane-source profile at later times the isothermal solidification stage. Figure 6 is a normalized is noted. representation of the width of the liquid layer *vs* time, using Figure 10 is a parabolic plot for a model system for which the normalization procedure suggested by Morral and Barka- $D_{22} = 0.01 D_{11}$. This representation, perhaps more than any low.^[8] Here the slight divergence of the curves at short times other, demonstrates the clear separation into two regimes, may be attributed to numerical error in the finite-difference each dominated by the diffusion of a particular solute. method. Figure 7 shows the variation of the interfacial- We have also used the finite-difference technique to verify

Fig. 4—Comparison of the results obtained for the isothermal solidification
of the Al-Zn-Sn system modeled using the Zener approximation (Eq. [9]) initial liquid compositions.

equilibrium liquidus concentration of tin with the width of that "stationary" kinetic states do exist; using Eq. [4] to the layer. Figure 8 shows the effect of varying the diffusivity estimate the ratio of solid-state diffusivities for the solutes, of the slow diffuser (in this case, simply by arbitrarily setting and under the assumption of constant solute-distribution

Fig. 7—Liquidus concentration as a function of width of the liquid layer.

Fig. 8—Computed liquid width *vs* time for four different ratios of the solute diffusivities.

coefficients, we find that the liquid composition remains constant through the entire course of solidification.

of a second solute on the process. Provided that the diffusiv- copy analysis on a fractured surface, and are, therefore, ity and/or solubility of the two solutes differ markedly, one subject to considerable error; the trend is unmistakable howcan expect to find two kinetic regimes, each regime con- ever, and it is consistent with the results of the modeling. trolled by a different solute. The model system Al-Zn-Sn has There is further evidence for the effect of a second solute been chosen to demonstrate this behavior. A small amount of in the literature. Ramirez and Liu^[9] reported on extensive tin added to the interlayer would be expected effectively to experiments in the nickel-boron system and noted that their arrest the isothermal solidification process and to prevent the results fell into two regimes, precisely as suggested by the complete bonding of the base material within conveniently current model. Boron was the fast-diffusing species in their accessible times. experiments, and they assumed that they were dealing with

Fig. 9—Computed solid-state concentration profiles for Zn (the fast diffusing solute) in Al after various times.

Fig. 10—Liquid width *vs* square root of time, showing the two kinetic regimes associated with the two solutes.

increases from 1:2 to approximately 7:1 on annealing a solid-**IV.** DISCUSSION iguid-solid couple for 3 days at 500 °C. During that time, the interlayer thickness decreased from 40 to 1 μ m. The Sn The results of the modeling demonstrate clearly the effect to Zn ratios were determined by electron dispersive spectros-

We have tested this prediction with a few preliminary a binary system. (Their base material was nickel of commerexperiments in this system. In particular, it has been found cial purity.) They speculated that the lack of complete solidithat the tin to zinc concentration ratio in the liquid phase fication was due to a departure from local equilibrium at the final stages of the process. We suggest instead that a predicted using the modeling techniques described in this second solute, present as an impurity in the base material work. In the case, where the two solutes are removed
or the interlayer, may have been responsible for their from the liquid at very different rates (e.g., Al-Zn-Sn or the interlayer, may have been responsible for their

Indeed, the complete isothermal solidification of interlayers may be the exception rather than the rule. Further experi- 4. If the tie-line–shifting process is not interrupted by the mental investigations are required to determine the maxi- complete solidification of the interlayer, we expect that solid and their diffusivities), that can be tolerated if complete terminal tie-line, for which the liquid composition re-
transient-liquid-phase bonding is to be accomplished. mains constant to a good approximation for the

- 1. The modeling of the isothermal solidification stage of TLP bonding in ternary systems demonstrates a rich vari- **ACKNOWLEDGMENTS** ety of responses. While the binary process is straightfor-
ward, and admits of a simple analytical treatment, the
equivalent three-component problem profits from a
equivalent three-component problem profits from a numerical approach for its full exploration.
- 2. We have identified several cases of interest. One, termed **REFERENCES** stationary, corresponds to a constant liquid-interlayer

composition throughout the full solidification process.

This situation is characterized by a set of solute fluxes

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coefficients are constant any starting liquid concentration 4. W.D. Hopfe and J.E. Morral: Acta Metall. Mater, 1994, vol. 42, pp. coefficients are constant, any starting liquid concentration
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The more usual case involves the continual shift of the ^{7. J.} Askill: *Tracer Diffusion for Metals, Alloys and Simple*
- 7. J. Askill: *Tracer Diffusion for M*
1. Askill: *Tracer Diffusion for M*
2. The mum, New York, NY, 1970. local equilibrium tie-line from the beginning to the end of
solidification. This is the direct result of the simultaneous
solidification. This is the direct result of the simultaneous
solidification. This is the direct res satisfaction of two coupled mass balances, and it can be 9. J.E. Ramirez and S. Liu: *Weld. J.*, 1992, vol. 71, pp. 365s-375s.

observations.
Indeed, the complete isothermal solidification of interlay-
the result of the removal of one solute.

mum level of impurities (related to their solubilities in the the system may, under certain circumstances, reach a mains constant to a good approximation for the balance of the solidification. Again, the modeling methods described here can be used to identify these cases. **V. CONCLUSIONS**

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