

## Forced Convection Heat Transfer in Porous Structure: Effect of Morphology on Pressure Drop and Heat Transfer Coefficient

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**Abstract:** A light-weight structure with sufficient mechanical strength and heat transfer performance is increasingly required for some thermal management issues. The porous structure with the skeleton supporting the ambient stress and the pores holding the flowing fluid is considered very promising, attracting significant scientific and industrial interest over the past few decades. However, due to complicated morphology of the porous matrices and thereby various performance of the pressure drop and heat transfer coefficients (HTC), the comprehensive comparison and evaluation between different structures are largely unclear. In this work, recent researches on the efforts of forced convection heat transfer in light-weight porous structure are reviewed; special interest is placed in the open-cell foam, lattice-frame, structured packed bed, and wire-woven structures. Their experimental apparatus, morphological of the porous structures, effect of morphology on pressure drop and HTC, and further applications are discussed. The new method which measure morphology accurately should be paid more attention to develop more accuracy correlation. Also, the most research focused on low Reynolds number and existing structure, while very few researchers investigated the property of forced convection heat transfer in high velocity region and developed new porous structure.

**Keywords:** forced convection, heat transfer, heat transfer coefficient, pressure drop, morphological characteristics, porous structure

### 1. Introduction

Heat transfer enhancement has long been crucial for energy saving, equipment safety, and production improvement, and others. Many heat transfer devices have been developed. However, a number of thermal management issues have become evident in various fields, for example in aero-engine thermal management [1, 2], high power electron device cooling [3], and

nuclear reactor cooling [4], and others [5, 6]. It has become clear that more effective compact heat transfer devices with smaller volumes are needed for such applications. Porous structures with large specific surface areas, tortuous passages and porosity [7, 8], as well as attractive mechanical properties [9, 10] is suitable to face those regard. The use of such structures to design heat transfer devices is therefore a promising avenue for addressing thermal management issues.

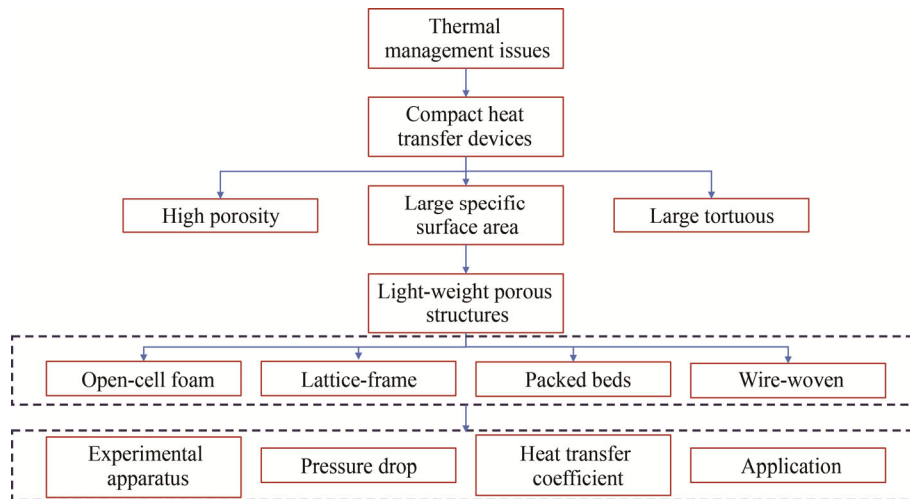
**Nomenclature**

|       |   |                      |   |
|-------|---|----------------------|---|
| $A$   | constant  | $S_{\text{cell}}$    | unit cell length/m                                      |
| $a$   | constant  | $S_{\text{v-g}}$     | geometric specific area/m <sup>2</sup> ·m <sup>-3</sup> |
| $b$   | constant  | $S_{\text{v}}$       | specific surface area/m <sup>2</sup> ·m <sup>-3</sup>   |
| $C$   | inertia coefficient/m <sup>-1</sup>   | $T$                  | temperature/K   |
| $c$   | specific heat capacity/J·kg <sup>-1</sup> ·K <sup>-1</sup>                      | $u$                  | velocity/m·s <sup>-1</sup>                              |
| $c_p$ | specific heat capacity at constant pressure/J·kg <sup>-1</sup> ·K <sup>-1</sup> | $V$                  | volume/m <sup>3</sup>                                   |
| $c_1$ | constant  | <b>Greek Symbols</b> |   |
| $c_2$ | constant  | $\alpha$             | constant  |
| $d$   | diameter/m  | $\beta$              | constant  |
| $E_1$ | viscous coefficient for Eq. (39)/m <sup>2</sup>                                 | $\varepsilon$        | porosity  |
| $E_2$ | inertia coefficient for Eq. (39)/m <sup>-1</sup>                                | $\mu$                | dynamic viscosity/Pa·s                                  |
| $F$   | Forchheimer coefficient/m <sup>2</sup>  | $\chi$               | tortuosity  |
| $f$   | friction factor   | $\rho$               | density/kg·m <sup>-3</sup>                              |
| $G$   | constant  | <b>Subscripts</b>    |   |
| $H$   | height/m  | $c$                  | cell  |
| $h$   | heat transfer coefficient/W·m <sup>-2</sup> ·K <sup>-1</sup>                    | $D$                  | Darcy   |
| $K$   | permeability coefficient/m <sup>2</sup>   | $f$                  | foam of fluid   |
| $k$   | thermal conductivity/W·m <sup>-1</sup> ·K <sup>-1</sup>                         | $h$                  | hydraulic   |
| $l$   | length/m  | $i$                  | inner   |
| $l'$  | addition length/m   | $o$                  | open or outlet  |
| $Nu$  | Nusselt number  | $p$                  | pore or particle  |
| $n$   | constant  | $s$                  | solid or strut  |
| PPC   | pores per centimeter  | $t$                  | total   |
| PPI   | pores per inch  | $v$                  | volume  |
| $Pr$  | Prandtl number  | $w$                  | window  |
| $Re$  | Reynolds number   |                      |   |

Several investigations have focused on forced convection heat transfer through porous structures, showing that such structures are able to enhance heat transfer. However, these are subject to large pressure drops in turbulence regions, with high Reynolds numbers. In order to design a compact heat transfer device, it is therefore necessary to develop a correlation for porous structures that would enable prediction of pressure drop and heat transfer. In recent decades, some authors have developed methods and correlations for morphological characterization and to determine pressure drop and heat transfer coefficients for a number of porous structures. However, there are no such general predictive correlations for certain random porous structures, such as open-cell foam structures, due to differences in morphological characterization, different experimental conditions and methods, and different theoretical backgrounds. It is easier to develop predictive correlations for regular porous structures (such as lattice-frame structures, structured packed beds, and

wire-woven structures) than for random porous structures. However, many different structures need to be investigated for different applications of heat transfer enhancement. In addition, several reviews of heat transfer in porous media were published [11–13]. However, the focus of those reviews is media with low porosity, flowing in porous media with nanofluid, or application of porous media. We hope to figure out the key factors which affect the accuracy of predicted correlations and to give the future research interest for the industrial application of porous structure. Therefore, it is thus essential to explore the similarities and differences between these various methods and correlations by reviewing previous literature.

As briefly discussed, predictive correlations are crucial for forced convection heat transfer in porous structures; however, relevant studies remain limited. The aim of this study is two-fold: providing a basic understanding of forced convection heat transfer properties in porous media and revealing gaps in present



**Fig. 1** The conceptual framework of present review

research. This study provides a brief review of the application of forced convection heat transfer in light-weight porous media, including open-cell foam structures, lattice-frame structures, structured packed bed structures, and wire-woven structures. This review considers experimental apparatus, the morphological characteristics of porous structures, the effect of morphology on pressure drop, HTC, and applications for heat transfer enhancement. Predictive correlations for forced convection in porous structures are compared and summarized. This review makes a significant contribution to the literature, given that few such reviews considering the effect of morphology on pressure drop and HTC for porous structure have yet been published. In addition, the conceptual framework is shown in Fig. 1.

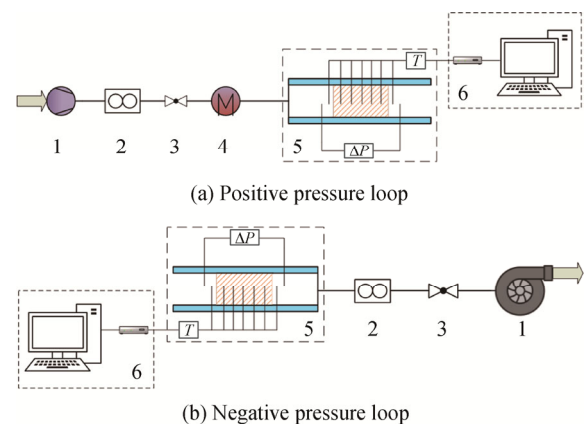
**2. Experimental Apparatus**

In the case of porous structures, the loop is the basic experimental apparatus for determining pressure drop, HTC, and the properties of heat exchangers. As shown in Fig. 2, this mainly consists of an air/fluid source, heater, testing section, and data acquisition section. The electrical heater is used by many author for heating air/fluid, besides, several heating loop are used in experimental system [14–16]. The function of each loop section differs from different applications. For pressure drop measurement, the heater can be bypassed to reduce pressure loss. However, the heater is necessary to determine the HTC. The position of the heater can also vary with different experimental methods: (1) before the test section for heating fluids (transient methods), or (2) heating the test section (steady-state methods). To determine heat exchanger properties, another loop is needed to provide cooling/heating media.

Table 1 summarizes the parameters of several loops which use air and water as work medium. The air

compressor and blower mostly were used to provide air. The velocity range of most loops is within 0 m/s to 16 m/s, with the velocity range of the Dukhan loop being 0.5 m/s to 35 m/s. As shown in Fig. 2, the loop can be classified as positive or negative based on the position of the air/fluid source. The air compressor is used as the air source of a positive pressure loop which given in Table 1, while the blower is used for the negative pressure loop. The positive pressure loop can provide a wider inlet pressure according to the different experimental requirements. However, there is little research specifically discussing the inlet pressure of loops. The most important element of the loop is the measuring equipment. Pressure transmitters and thermocouples are widely used for this purpose. Furthermore, an IR camera [17] and thermochromic liquid crystals [9] can be used to determine temperature distribution.

The basic components of loops are similar, and the commonly-used measuring equipment can only determine the macro characteristics of forced convection



**Fig. 2** Scheme of loop, (a) positive pressure loop, (b) negative pressure loop: 1. air/fluid source, 2. flowmeter, 3. heater, 4. control valve, 5. testing section, 6. data acquisition

**Table 1** Summary of experimental apparatus parameters and applications

| Authors                  | media        | Velocity/m·s <sup>-1</sup>                  | Pressure/kPa | Applications         | Air source                    |
|--------------------------|--------------|---|--------------|----------------------|-------------------------------|
| Mancin et al. [18–21]    | air          | 2.00 to 5.00                                | 700          | HTC<br>Pressure drop | Air compressor system         |
| Dirtrich et al. [22, 23] | air          | 0.50 to 9.00                                | –            | HTC<br>Pressure drop | Blower                        |
| Wallenstein et al. [24]  | air          | 0.60 to 3.00                                | –            | HTC                  | Not mentioned                 |
| Moreira et al. [25, 26]  | air or water | 0.00 to 18.50 (air)<br>0.00 to 0.33 (water) | –            | Permeability         | Air compressor system<br>pump |
| Giani et al. [27]        | air          | 1.00 to 16.00                               | –            | Pressure drop        | –                             |
| Xia et al. [28]          | air          | 2.00 to 9.00                                | –            | HTC                  | Air compressor system         |
| Lacroix et al. [29]      | air          | 0.00 to 5.00                                | –            | Pressure drop        | Not mentioned                 |
| Dixit et al. [30]        | air          | 0.8 to 5.50                                 | Negative     | Pressure drop<br>HTC | Blower                        |
| Yan et al. [31]          | air          | 2.87 to 12.52                               | –            | Pressure drop        | Blower                        |
| Kurian et al. [32]       | air-water    | 0.50 to 3.00                                | –            | Heat exchanger       | Blower                        |
| Nawaz et al. [33]        | air-water    | 0.30 to 7.00                                | –            | Heat exchanger       | Blower (cycle)                |
| T'joen et al. [34]       | air-water    | 0.70 to 7.40                                | –            | Heat exchange        | –                             |
| Chen et al. [35]         | air-water    | 0.50 to 12.00                               | 1200         | Heat exchanger       | Air compressor system         |
| Fuller et al. [7]        | air          | 0.00 to 16.00                               | –            | HTC                  | Blower                        |
| Madani et al. [36]       | water        | 0.00 to 0.20                                | –            | Pressure drop        | Pump                          |
| Garrido et al. [37]      | air          | 0.00 to 15.00                               | –            | Pressure drop        | –                             |
| Son et al. [38]          | air          | 0.05 to 1.00                                | Negative     | HTC<br>pressure drop | Blower                        |
| Dukhan et al. [39]       | air          | 0.5 to 35                                   | Negative     | Permeability         | Blower                        |

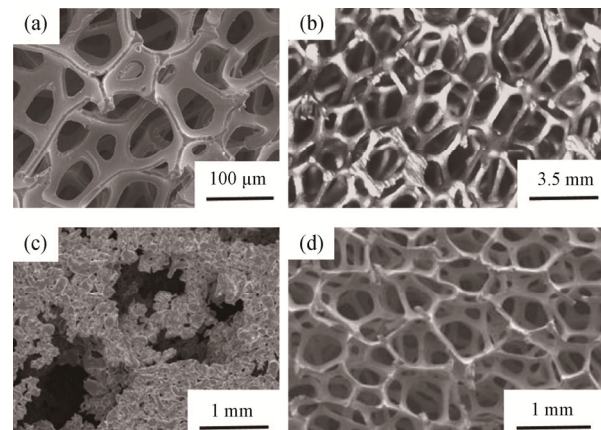
heat transfer in porous structures. Measurement at pore scale is difficult and few authors have investigated this in detail. More effective measuring equipment is needed for determination of heat transfer properties at pore scale.

### 3. Morphological Characterization of Porous Structures

The pressure drop and heat transfer performance of porous structures greatly depend on their morphological characterization; this therefore provides a basis for applications of porous structures. Accurate morphological characterization of such structures is important for measurement of pressure drop and HTC.

#### 3.1 Morphological characterization of open-cell foam structures

The open-cell foam structures manufactured by different method have different morphological characteristics. As shown in Fig. 3, there are different types of open-cell foam structures. The dimension and form of skeletons are very different among four types of open-cell foam structure. In addition, the pores of foam manufactured by using powdered metal are more closed than other three foams. Therefore, the open-cell foam structure discussed at present work did not include the foam manufactured by using powdered metal. Banhart et al. [40] classified production methods of metallic foam



**Fig. 3** (a) Using vapor technology to produce "INCOFOAM" [42]; (b) using liquid metal to produce "Duocel" aluminum foam [43]; (c) using powdered metal to produce inconel 600 foam [44]; (d) using metal ions to produce nickel foam [45]

structures into metal vapor, liquid metal, powdered metal, and metal ions, according to the state of the metal. Deng et al. [41] reviewed production methods of ceramic foams for fabricating porous ceramics, classifying these into direct foaming, three-dimensional printing, and molten salt methods.

Several geometrical characters are used to describe the open-cell foam structure:  $\varepsilon$  (porosity), PPI (pores per

inch),  $d_s$  (strut diameter),  $d_w$  (window diameter),  $d_c$  (cell diameter),  $S_v$  (specific surface area),  $\chi$  (geometric tortuosity), and others. The manufacturer generally only provides  $\varepsilon$  and sometimes PPI; other geometry characters therefore need to be measured or calculated. In the literature,  $\varepsilon$ ,  $d_s$ ,  $d_w$ ,  $d_c$ , and  $S_v$  are often used to develop the correlation between pressure drop and HTC for open-cell foam structures. In the following section, methods for determining  $\varepsilon$ ,  $d_s$ ,  $d_w$ ,  $d_c$  and  $S_v$  are reviewed.

### 3.1.1 Porosity

$\varepsilon$  is defined as the fluid storage capacity of porous media [46]. Normally,  $\varepsilon$  of open-cell foam can be determined using Eq. (1). Here,  $V$  is the volume of foam;  $V_s$  is the volume of the solid skeleton, and  $\rho_f$  is the density of foam, i.e., the specific value of the mass of the foam sample and apparent volume of the foam sample.  $\rho_s$  is the density of the solid. However, as shown in Fig. 4, the strut of most open-cell foams is hollow due to the production methods-replication technique [47]. Inayat et al. [48] summarized porosities as:  $\varepsilon_o$  open porosity,  $\varepsilon_s$  strut porosity,  $\varepsilon_t$  total porosity, and  $\varepsilon_n$  normal porosity, which is given by the manufacturer.

$$\varepsilon_t = 1 - \frac{V_s}{V} = 1 - \frac{\rho_f}{\rho_s} \quad (1)$$

In the literature, many different ways of measuring  $\varepsilon_o$ ,  $\varepsilon_s$  and  $\varepsilon_t$  are presented, such as magnetic resonance imaging (MRI), Scanning Electron Microscopy (SEM), and mercury porosimetry. Crosse et al. [49] used MRI to determine  $\varepsilon_t$  and  $\varepsilon_o$  by counting solid voxels in unfilled data and counting solid voxels in filled data respectively.  $\varepsilon_s$  can be calculated using Eq. (2):

$$\varepsilon_s = \varepsilon_t - \varepsilon_o \quad (2)$$

Fuller et al. [7] used SEM images to determine the average ligament inner  $d_i$  and outer diameter  $d_o$ .  $\varepsilon_o$  can be determined using Eq. (3):

$$\varepsilon_o = 1 - \frac{\rho_f}{\rho_s} \left( \frac{1}{1 - (d_i/d_o)^2} \right) \quad (3)$$

Some authors [37, 50] have used mercury porosimetry to measure  $\varepsilon_t$  and  $\varepsilon_o$ . This involves first using mercury intrusion in large pores and obtaining  $V_o$  (volume of open pores) at atmospheric pressure. Mercury is then used to fill every pore of open-cell foam at high pressure and obtain  $V_s$ . Finally,  $\varepsilon_t$ ,  $\varepsilon_o$ , and  $\varepsilon_s$  can be determined. However, since mercury cannot be used to fill every pore, this method is not suitable for every open-cell foam. Therefore, the approach which measures porosity more accurately should be paid much more attention.

$\varepsilon_o$  is hard to measure in all samples and is therefore neglected by many authors.  $\varepsilon_t$  is instead used to develop the correlation between pressure drop and HTC. Inayat et al. [48] investigated differences in pressure drop

prediction with  $\varepsilon_t$  and  $\varepsilon_o$ . The authors found that the small difference between  $\varepsilon_t$  and  $\varepsilon_o$  can lead to a significant influence on the prediction of pressure drop. To determine heat transfer progress, the authors use the correlation determined by Xia [28] to predict  $Nu_v$  using five  $\varepsilon$  levels, with a difference of only 0.03 between these. As shown in Fig. 5, this small difference can significantly impact  $Nu_v$ . Therefore,  $\varepsilon_s$  must be accurately determined, in particular when open-cell foam is used under high velocity conditions. For open-cell foam in which  $\varepsilon_s$  is 0,  $\varepsilon_s$  is equal and can be determined using Eq. (1) directly. In the other hand, the existence of  $\varepsilon_s$  influences the effective thermal conductivity of open-cell foam significantly, and then the overall heat transfer performance decreases. Therefore, the new method which manufactured open-cell foam without hollow skeletons should be developed such as additive manufacturing.

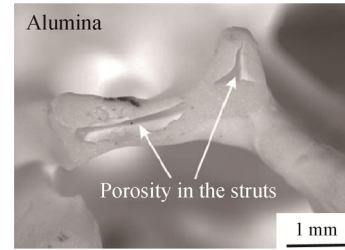


Fig. 4 Hollow strut of open-cell foam [8]

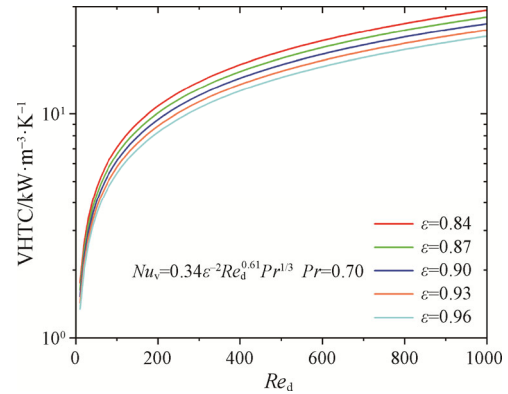


Fig. 5 Prediction of  $Nu_v$  with five  $\varepsilon$  which have the difference only 0.03 by using correlation of Xia [28]

### 3.1.2 Pore diameter

Pore diameter had been extensively defined [20, 51] and measured [23] over past decades. However, it is interpreted differently by different authors, with definitions used including average diameter with an area the same as that of the tetrakaidecahedral window [52], or average diameter with a volume the same as that of a sphere [53], or 25.4 mm/PPI [20, 21]. To address this problem of unclear definition, Inayat et al. [48] defined

four characteristic pore diameters:  $d_w$  (average window diameter),  $d_s$  (strut diameter),  $d_c$  (average cell diameter), and  $D_p$  (average value of sum,  $d_s+d_w$ ). Additionally, some authors [23, 54, 55] use hydraulic diameter  $d_h$  to develop a correlation, while others use  $d_p$  (equivalent particle diameter) as a characteristic length scale. Several authors [56, 57] also use  $\sqrt{K}$  due to the different definition and measurement of morphological characteristics, where  $K$  is the permeability coefficient. However, the values of  $K$  obtained experimentally are not accurate, and thus using  $K$  as a length scale has limitations.

It is easy to measure the values of  $d_s$  and  $d_w$  using SEM, light microscopy images, and 3D scanned images [37, 58, 59], but these techniques may be less effective for determining  $d_p$  and  $d_c$ . Furthermore,  $d_h$  cannot be measured using such equipment. Correlations have therefore been developed to determine  $d_p$ ,  $d_c$ , and  $d_h$ .

In the literature [27, 29], equivalent particle diameter  $d_p$  has been calculated using Eqs. (4) and (5), which were developed using the cubic cell model and pentagonal dodecahedron geometry, respectively. Neither correlation can be applied to every sample due to changes in pore diameter with manufacturing processes [60]; errors in these correlations can lead to significant errors in results.

$$d_p = 6(1 - \varepsilon_0) / S_v \tag{4}$$

$$d_p = 1.5d_s \tag{5}$$

Eq. (6) is referenced in some studies [29, 61] for calculation of  $d_c$ . Huu et al. [62] investigated the coefficient between  $d_c$  and  $d_w$  for a  $\varepsilon$  in the range of 0.8 to 0.92. Results showed that 2.3 is a good approximation and can be used by future authors.  $d_h$  is not a morphological character of open-cell foam struts and is merely a characteristic length scale which can only be determined through correlations. Several authors [27, 54] used Eq. (7) to determine  $d_h$ , while Dietrich et al. [23] developed a simple correlation between  $d_h$  and the value of PPI (Eq. (8)).

$$d_c = 2.3d_w \tag{6}$$

$$d_h = 4 \frac{\text{Cross section available for flow}}{\text{wetted perimeter}} = \frac{4\varepsilon_0}{S_v} \tag{7}$$

$$d_h = 0.028(m) \text{PPI}^{-0.721} \tag{8}$$

The above definitions and pore diameter correlations have been used by different authors as a characteristic length scale for development of predictive correlations. This is one of the reasons for the lack of a unified correlation. In addition, the concept of different diameter is shown in Table 2. Eqs. (4), (7) and (8) establish the relationship between pore diameter and  $d_s$ ,  $\varepsilon_0$ ,  $S_v$ , PPI, respectively. And then, the errors of  $d_s$ ,  $\varepsilon_0$ ,  $S_v$  and PPI will influence accuracy of pore diameter. Therefore,  $d_w$  and  $d_s$  are better choices to develop predictive correlations and used by many researcher.

### 3.1.3 Tortuosity

Kozeny et al. [63] defined tortuosity ( $\chi$ ) as the ratio of effective (tortuous) path  $l_e$  to the thickness of the porous medium. It is significant for describing the morphology and transport properties of open-cell foam structures. Furthermore, the permeability and turbulence of transport in open-cell foam structures can be directly influenced by tortuosity.

Some authors have used different methods to determine tortuosity, such as ultrasonic transverse transmission methods [64], finite volume techniques [65], geometrical approaches [61, 66, 67], diffusion techniques [63, 68] and electrical resistivity methods [26]. Other authors have developed correlations to calculate tortuosity. For example, Du Plessis et al. [69] developed a model for tortuosity as a function of  $\varepsilon$  by using the cubic representative unit cell, given in Eq. (9):

$$\frac{1}{\chi} = \frac{3}{4\varepsilon_0} + \frac{\sqrt{9-8\varepsilon_0}}{2\varepsilon_0} \times \cos \left\{ \frac{4\pi}{3} + \frac{1}{3} \cos^{-1} \left[ \frac{8\varepsilon_0^2 - 36\varepsilon_0 + 27}{(9-8\varepsilon_0)^{3/2}} \right] \right\} \tag{9}$$

Bhattacharya et al. [70] investigated whether the correlation developed by Du Plessis remains accurate in high PPI ranges, subsequently developing another correlation for determining tortuosity (Eq. (10)), which is accurate across a wide range of PPI values:

**Table 2** The concept of diameter

| Diameter        | Concept  |
|-----------------|--|
| $d_w$ and $d_s$ | Measured by using SEM, light microscopy images, and 3D scanned images  |
| $D_p$           | average value of sum ( $d_s+d_w$ )   |
| $d_p$           | $d_p=6(1-\varepsilon_0)/S_v$ or $d_p=1.5d_s$   |
| $d_c$           | $d_c=2.3d_w$   |
| $d_h$           | $d_h = 4 \frac{\text{Cross section available for flow}}{\text{wetted perimeter}} = \frac{4\varepsilon_0}{S_v}$ or $d_h = 0.028(m) \text{PPI}^{-0.721}$ |

$$\begin{aligned} \frac{1}{\chi} &= \frac{\pi}{4\varepsilon_0} \left\{ 1 - \left( 1.18 \sqrt{\frac{(1-\varepsilon_0)}{3\pi}} \frac{1}{G} \right)^2 \right\} \\ &= \frac{\pi}{4\varepsilon_0} \left\{ 1 - \left( 1.18 \sqrt{\frac{(1-\varepsilon_0)}{3\pi}} \frac{1}{1 - e^{-(1-\varepsilon_0)/0.04}} \right)^2 \right\} \end{aligned} \quad (10)$$

Inayat et al. [48] developed a correlation to determine tortuosity using a tube model, as in Eq. (11):

$$\chi = \frac{l'}{1} = 1 + \frac{d_w (\pi d_w l' / v)}{4\varepsilon_0} = 1 + \frac{\text{Dimensionless}(S_v)}{4\varepsilon_0} \quad (11)$$

Here,  $v$  is the volume of the tube model;  $l'$  is additional length;  $S_v$  is the dimensionless specific surface area of the open-cell foam structure.

Tortuosity can be easily determined using the above methods and correlations but the relationship between tortuosity and thermodynamic properties is not yet clear. There is a need for further model development to describe this relationship.

### 3.1.4 Specific surface area

The  $S_v$  of an open-cell foam structure is defined as the  $S_v$  per unit geometric volume [37]. From the correlations in Eqs. (4), (7), and (11), it is known that  $S_v$  is an important parameter to determine equivalent particle diameter  $d_p$ , average cell diameter  $d_c$ , hydraulic diameter  $d_h$ , and tortuosity  $\chi$ . A large  $S_v$  is an advantage for many applications of open-cell foam structures, such as heat exchangers, catalyst supports, porous burners, and gas filters [50]. In addition, the accurate determination of  $S_v$  plays an important role on the design of heat transfer equipment.

In the literature, many methods have been used to measure  $S_v$  of an open-cell foam structure, such as X-ray absorption tomography [50, 71, 72], MRI [23, 49], and some novel methods. Diao et al. [73] used cyclic voltammetry and quantitative stereology to measure the  $S_v$  of Cu open-cell foam. However, such methods are inconvenient and expensive and not suited for engineering purposes. Therefore, the correlations that enable prediction of  $S_v$  are needed and some such correlations were developed in previous literature. For example, Giani et al. [27], Lacroix et al. [29], and Liu et al. [74] used the cubic cell model to develop the correlation for predicting  $S_v$ :

$$S_v = \frac{4(1-\varepsilon_0)}{d_s} \quad (12)$$

However, the cubic model does not represent well the cell of open-cell foam structures. Gisbson et al. [75] investigated three different models (hexagonal prisms, tetrakaidecahedral, and dodecahedral), concluding that the tetrakaidecahedral model is the best suited for

open-cell foam structures. Buciuman et al. [76] and Kumar et al. [77] used the tetrakaidecahedral model to develop correlations for predicting  $S_v$ . However, Kumar's correlation, which uses three dimensionless parameters, as shown in Eqs. (13) and (14), is too complex to use:

$$S_v = 4.82 \frac{1}{D_p} \sqrt{(1-\varepsilon_0)} \quad (13)$$

$$S_v = \frac{1}{\sqrt{2}L} \left[ \frac{3}{2} \alpha \beta \left( 2\pi - 3\Omega + \frac{45}{32} \pi \alpha^2 (1-\varepsilon_s) \right) \right] \quad (14)$$

where  $\alpha$  and  $\beta$  can be calculated by combining Eqs. (15) and (16), and  $\Omega$  can be calculated using Eq. (17).

$$1.6\alpha + \beta = 1 \quad (15)$$

$$12\pi\alpha^2\beta(1-\varepsilon_s) + \frac{32}{3}\pi\alpha^3(1-\Omega\varepsilon_s) = 8\sqrt{2}(1-\varepsilon_t) \quad (16)$$

$$\Omega = \sqrt{4\pi\varepsilon_s/\sqrt{3}} \quad (17)$$

Richardson et al. [59] investigated three different geometric models to develop the correlations given in Eqs. (18), (19), and (20) respectively and compared  $S_v$  values calculated using these three correlations. The authors found the values to be close to each other and selected Eq. (18) for prediction of  $S_v$ .

$$S_v = \frac{4\varepsilon_0}{d_w} \quad (18)$$

$$S_v = \frac{4}{d_w} \quad (19)$$

$$S_v = \frac{12.979 \left[ (1-\varepsilon_0)^{0.5} - 0.971(1-\varepsilon_0) \right]}{d_w} \quad (20)$$

Grosse et al. [78] developed a correlation (Eq. (21)) using the Weaire-Phelan model but this correlation did not fit experimental results well. The coefficients were therefore redefined by fitting experimental data, as shown in Eq. (22):

$$S_v = \frac{8.21\sqrt{(1-\varepsilon)} - 1.55(1-\varepsilon)}{d_w + d_s} \quad (21)$$

$$S_v = \frac{4.84\sqrt{(1-\varepsilon_0)} - 2.64(1-\varepsilon_0)}{d_w + d_s} \quad (22)$$

Inayat et al. [50] used the tetrakaidecahedral model to develop three correlations with different strut shapes, i.e., cylindrical, triangular, and triangular concave struts, given in Eqs. (23), (24), and (25), respectively. In other literature [48], the same authors use several correlations developed by different authors to predict  $S_v$  and compare with experimental data from other literature. Results showed that correlations almost always overestimate experimental data in the range of low porosity ( $\varepsilon_0 < 90\%$ ). However, Eqs. (23) to (25) showed good agreement with experimental data. Due to limited availability of



experimental data from the literature, the authors did not compare theoretical with measured values.

$$S_{v-cylindrical} = 4.867 \frac{[1 - 0.971(1 - \varepsilon_0)^{0.5}]}{d_w (1 - \varepsilon_0)^{0.5}} (1 - \varepsilon_0) \quad (23)$$

$$S_{v-triangular} = 5.62 \frac{[1 - 0.971(1 - \varepsilon_0)^{0.5}]}{d_w (1 - \varepsilon_0)^{0.5}} (1 - \varepsilon_0) \quad (24)$$

$$S_{v-triangular-concave} = 6.49 \frac{[1 - 0.971(1 - \varepsilon_0)^{0.5}]}{d_w (1 - \varepsilon_0)^{0.5}} (1 - \varepsilon_0) \quad (25)$$

In summary, all above correlations are subject to errors in predicting  $S_v$  and have limited information for high porosity ranges ( $\varepsilon > 90\%$ ). However, the correlations based on the tetrakaidecahedral model may agree well with periodic open-cell foam structures manufactured by 3D printing.

### 3.2 Morphological characterization of lattice-frame structures

The literature discusses different lattice-frame structures produced through various manufacturing technologies, such as brazing and assembling [79], metal wire weaving [80], investment casting [81], metal sheet folding [82, 83], and 3D printing [38]. As shown in Fig. 6, there are four lattice-frame structures (tetrahedral, pyramidal, kagome, and X-type), produced through various manufacturing methods. This section will review these four types of structures, and their  $\varepsilon$  and  $S_v$ .

#### 3.2.1 Tetrahedral structure

Fig. 7 shows the details of the tetrahedral structure.

Although there is little literature that provides correlations to predict  $\varepsilon$  and  $S_v$ , Kim et al. provide a correlation for calculating  $\varepsilon$  and  $S_v$  of a tetrahedral structure, as shown in Eqs. (26) and (27), respectively:

$$\varepsilon = 1 - \frac{\sqrt{3}}{2} \left(\frac{d}{l}\right)^2 \left(\frac{l}{H}\right) \quad (26)$$

$$S_v = \frac{\frac{3}{d} + 2S_x l - 3\frac{d^2}{4}}{HS_x l} \quad (27)$$

Eq. (26) includes three variates: diameter of ligament, length of ligament, and height of cell. According to the geometrical relationship between height and length of ligament, the two variates can be integrated into one. Son et al. [38] gave a correlation of  $\varepsilon$  with two variates, as in Eq. (28):

$$\varepsilon = 1 - \frac{\sqrt{2}}{2} \left(\frac{d}{l}\right)^2 + \frac{\sqrt{66} + 2\sqrt{3}}{9} \left(\frac{d}{H}\right)^3 \quad (28)$$

Definitions of  $d$ ,  $l$ ,  $H$ , and  $S_x$  can be obtained from Fig. 7.

#### 3.2.2 Pyramidal structure

Fig. 8 shows the details of a pyramidal structure with hollow strut. However, when the pyramidal structure is used for enhancing heat transfer, the strut must be solid due to its high thermal conductivity. There are hardly any correlations for predicting  $\varepsilon$  in relevant heat transfer literature. However, mechanics literature gives some correlations for predicting  $\varepsilon$ . St-Pierre et al. [84] developed a correlation for predicting the relative density  $\bar{\rho}$  of a pyramidal structure with hollow strut. The correlation for  $\varepsilon$  can then be derived as shown in Eq. (29):

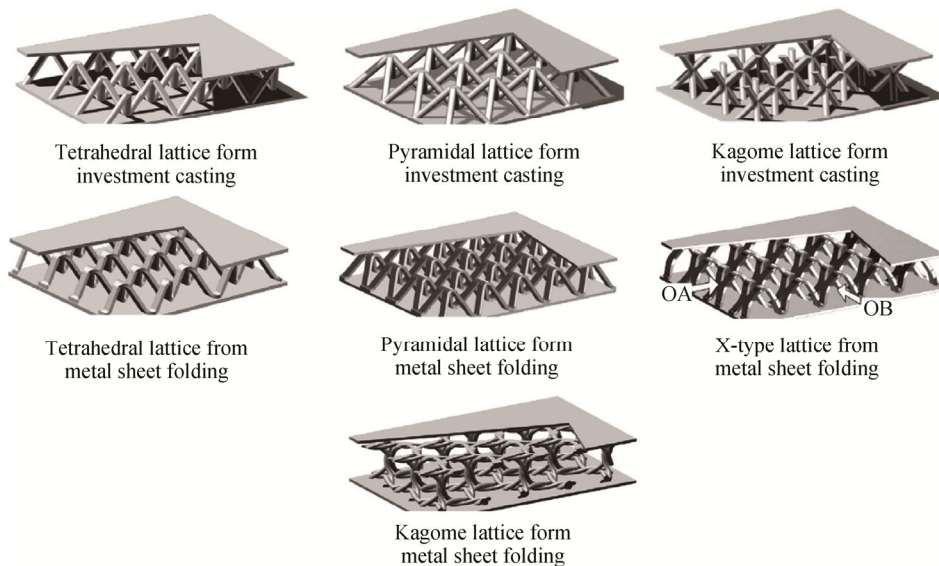


Fig. 6 Different lattice-frame structure with different manufacturing methods [31]



$$\varepsilon = 1 - \bar{\rho} = 1 - \frac{2\pi(d^2 - (d-2t)^2)}{(4k + 2l\cos\omega)^2 \sin\omega} \quad (29)$$

Details of  $d$ ,  $t$ ,  $k$ , and  $\omega$  can be obtained from Fig. 8. For a pyramidal structure with solid strut,  $t$  in Eq. (29) can equal  $d/2$  and the correlation can be thus changed to that shown in Eq. (30). When  $k$  is equal to 0, Eq. (30) can be changed to Eq. (31), as in the correlation developed by Wei et al. [85]:

$$\varepsilon = 1 - \bar{\rho} = 1 - \frac{2\pi d^2}{(4k + 2l\cos\omega)^2 \sin\omega} \quad (30)$$

$$\varepsilon = 1 - \bar{\rho} = 1 - \frac{2\pi d^2}{(2l\cos\omega)^2 \sin\omega} \quad (31)$$

The shape of the pyramidal structure differs in different literature, with different correlations for calculating  $\varepsilon$  of pyramidal structures [86–88]. However, there is little research that considers determination of  $S_v$ .

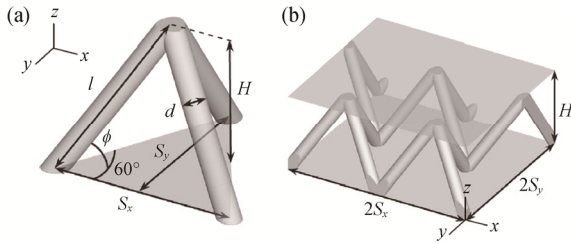


Fig. 7 Detail of tetrahedral lattice-frame structure [38]

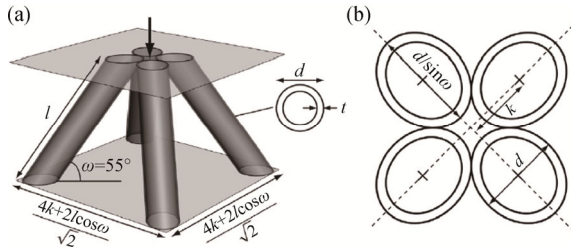


Fig. 8 Detail of pyramidal lattice-frame structure with hollow strut [84]

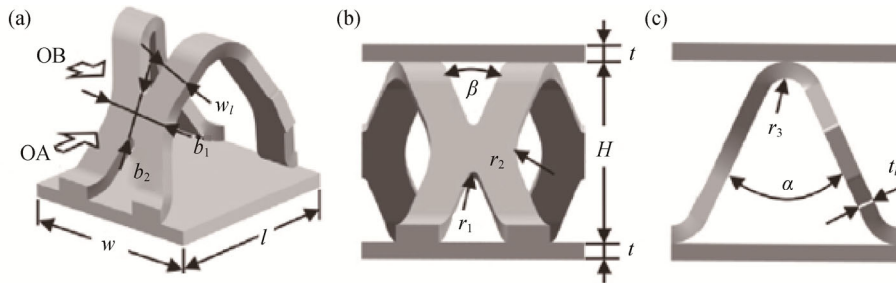


Fig. 9 Detail of x-type [83]

When using a pyramidal structure for heat transfer, the  $S_v$  is a significant characteristic and should be determined. A correlation for this purpose should therefore be developed.

### 3.2.3 X-type structure

No correlation for Kagome structure morphological parameters was found in available literature; however, Yan et al. [83] developed correlations for predicting  $\varepsilon$  and specific area of X-type structures, as shown in Eqs. (32) and (33), respectively:

$$\varepsilon = 1 - \frac{t_1}{lwH} \left[ wl_1 - 4 \left( \frac{w-b_1}{2} + r_2 / \cos \frac{\beta}{2} - r_2 \right) \times \left( \frac{l-b_2}{2} + r_1 / \sin \frac{\beta}{2} - r_1 \right) \right] \quad (32)$$

$$S_v = \frac{2(1-\varepsilon)}{t_1} + \frac{8t_1}{lwH} \left\{ \left( \frac{1}{\sin \frac{\beta}{2}} \right) \cdot \left[ \frac{w}{4} - w_1 / \left( 2\cos \frac{\beta}{2} \right) + \frac{l_1}{4} \tan \frac{\beta}{2} \right] + \left( \frac{\pi-\beta}{2} - \cot \frac{\beta}{2} \right) r_1 + \left( \frac{\beta}{2} - \tan \frac{\beta}{2} \right) r_2 \right\} \quad (33)$$

Definitions of the following dimensions:  $l$ ,  $w$ ,  $w_1$ ,  $H$ ,  $t$ ,  $t_1$ ,  $b_1$ ,  $b_2$ ,  $r_1$ ,  $r_2$ ,  $r_3$ ,  $\alpha$ , and  $\beta$ , can be obtained from Fig. 9.  $l_1$  can determined using Eq. (34):

$$l_1 = l / \sin \frac{\alpha}{2} + \left( 2\pi - 2\alpha - 4\cot \frac{\alpha}{2} \right) r_3 + \left( \pi - \alpha - 2\cot \frac{\alpha}{2} \right) t_1 \quad (34)$$

The morphology of lattice-frames is simpler than that of metal foams; however, there are no correlations for predicting  $\varepsilon$  and  $S_v$  of these structures. The relationship between characteristics of lattice-frames which are easily measured and those that are hard to measure should be therefore more widely investigated, and related correlations should be developed.

### 3.3 Morphological characterization of structured packed beds and wire-woven structures

Wire-woven metal and packed bed structures, which can serve porous media for heat transfer, can have a variety of complex structures; it is therefore difficult for a single correlation to explain their morphological characterization. However,  $\varepsilon$ , a fundamental character, can be predicted through correlations developed by some authors.

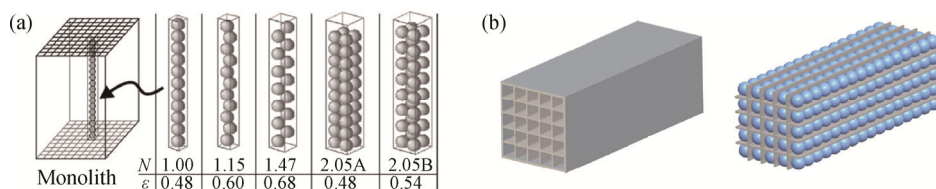
#### 3.3.1 Packed beds

Based on packing method, packed beds can be classified as random or structured. Van Antwerpen et al. [89] reviewed descriptions of random packed beds in the literature and related correlations for predicting  $\varepsilon$ ; noting that however, there are too many factors of influence to allow accurate prediction: packing mode (very loose random packing ( $\varepsilon$ : 0.46 to 0.47), loose random packing ( $\varepsilon$ : 0.40 to 0.41), poured random packing ( $\varepsilon$ : 0.375 to 0.391), close random packing ( $\varepsilon$ : 0.359 to 0.391)) [90], Wall effect [91], ratio of tube and particle diameter [92], roughness of the particle surface, particle shape and size distribution [93], the shape of the container [94], particle material density [95], and the ratio of filling height and particle diameter [96], and others. Few authors have investigated structured packed beds, but Romkes et al. [97] investigated the thermodynamic properties of composite structured packing (CSP), shown in Fig. 10. Wang et al. [98] developed a grille-sphere composite structured packed bed (GSCSPB), also shown in Fig. 10.

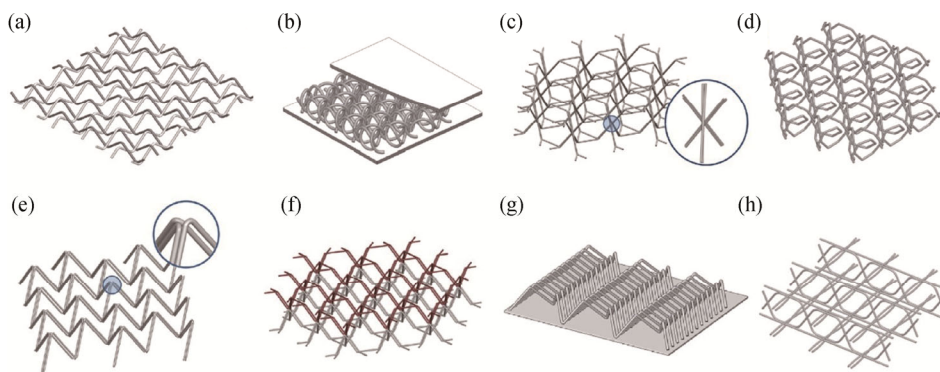
#### 3.3.2 Wire-woven structure

The morphology of wire-woven metal is classified by Kang [80] as single-layered or multi-layered, depending on the process of manufacture. As shown in Fig. 11, single-layered structures include the Pyramid [99], Circular Spring Kagome (CSK) [100, 101], Hexagonal Spring Kagome (HSP) [101], Dual Wired Octet (DWO) [101, 102], Dual Wired Kagome-1 (DWK-1) [102], Dual Wired Kagome-2 (DWK-2) [101, 102], Zigzag truss [103, 104], and Three dimensional woven wire structure (3DWT) [105, 106], and others. As shown in Fig. 12, multi-layered structures include Textilecore [107], Wire-woven Bulk Kagome (WBK) [108], Struwire [109], Wire-woven Bulk Diamond (WBD) [110], Wire-woven Bulk Cross (WBC) [111, 112], and '3WEAVE' [113]. Kang [80] summarized correlations for predicting  $\varepsilon$  for the above structures, determining the following order for the  $\varepsilon$  of single-layered structures: HSK<CSK<DWK-1 = DWK-2 <DWO<Pyramid<3DWT<Zigzag. The order of  $\varepsilon$  of multi-layered structures was as follows: Textilecore<WBC<WBD< Strucwire<WBK.

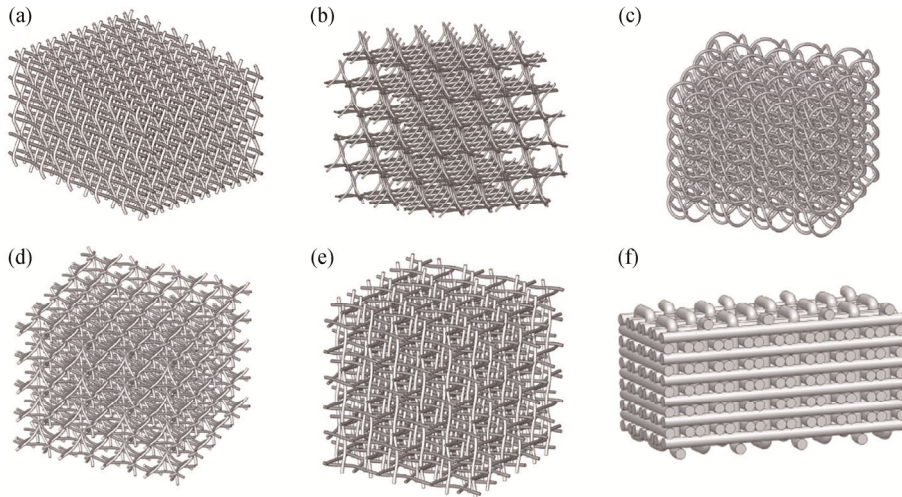
The above structures all can enhance heat transfer at special condition. However, the comparison among those structures is hard to obtain by using non-dimensional number due to the different characteristic length. Field synergy is a novel concept for realizing that the flow field plays a very important role in convective heat transfer [114]. The synergy angle is an important parameter which could evaluate the overall heat transfer performance of porous structure in this theory. In



**Fig. 10** Concept of (a) composite structured packing (CSP) [97]; (b) grille-sphere composite structured packed bed (GSCSPB) [98]



**Fig. 11** Concept of single-layering: (a) Pyramid, (b) Circular Spring Kagome (CSK), (c) Hexagonal Spring Kagome (HSK), (d) Dual Wired Octet (DWO), (e) Dual Wired Kagome-1 (DWK-1), (f) Dual Wired Kagome-2 (DWK-2), (g) Zigzag truss, (h) Three dimensional woven wire structure (3DWT) [80]



**Fig. 12** Concept of multi-layering: (a) Textilecore, (b) Wire-woven Bulk Kagome (WBK), (c) Struwire, (d) Wire-woven Bulk Diamond (WBD), (e) Wire-woven Bulk Cross (WBC), (f) 3WEAVE [80]

addition, field synergy theory has been widely used in the multidisciplinary optimization of porous media [115–117]. Therefore, field synergy theory can be used to developed new porous structure which enhances heat transfer.

**4. Effect of Morphology on Pressure Drop**

One of the thermodynamic properties of porous media is pressure drop. Accurate prediction of pressure drop is very important for designing heat exchangers and reactors using porous structures. In this section, a number of correlations given in the literature for predicting pressure drop of porous structures, including metal foam, lattice-frame structures, and other porous media, are reviewed.

**4.1 Pressure drop correlations for open-cell foam structures**

Fluid flow regimes are divided into pre-Darcy, Darcy, Forchheimer, and turbulent [118, 119]; there can also be transitional flow between two adjacent regimes. Few authors have investigated pre-Darcy regimes. Dukhan et al. [119] found that the range of pre-Darcy is  $Re < 0.4$  for aluminum with 20 PPI,  $\epsilon_0=0.87$ , velocity increases with a reduction in pressure drop. For Darcy regimes, the correlation for predicting pressure drop can be given by Eq. (35):

$$\frac{\Delta P}{\Delta l} = \frac{\mu}{K_D} u \tag{35}$$

where  $\Delta P$  is pressure drop;  $\Delta l$  is the length along the flow direction of the foam structure;  $\mu$  is dynamic viscosity;  $u$  is velocity, and  $K_D$  is the Darcy permeability of the foam structure. The correlation can be used at low Reynolds numbers. However, for post-Darcy regimes like

Forchheimer and turbulent regimes, Forchheimer equations are always used to describe pressure drop, as in Eq. (36):

$$\frac{\Delta P}{\Delta l} = \frac{\mu}{K_D} u + C \rho u^2 \tag{36}$$

where  $C$  is the inertia coefficient. However, some authors [120–122] used  $\frac{F}{\sqrt{K_D}}$  to replace  $C$ , where  $F$  is the

Forchheimer coefficient. Other authors used the cubic law to describe transition regimes [53], as in Eq. (37):

$$\frac{\Delta P}{\Delta l} = \frac{\mu}{K_D} u + \frac{\gamma \rho}{\mu} \rho u^2 \tag{37}$$

where  $\gamma$  is a dimensionless parameter. Kumar et al. [123] note that the Reynolds number range of transitional regimes is very small and it is difficult to control velocity during experiments. There is therefore almost no literature using the cubic law for predicting pressure drop.

The interpretation of the Forchheimer equation presented by Ergun and Orning [124] is widely accepted by others. Ergun and Orning developed this equation to predict pressure drop over packed beds. The basic form of the Ergun equation [48, 125] is given in Eq. (38):

$$\frac{\Delta P}{\Delta l} = \alpha \frac{S_v^2 (1-\epsilon_0)^2}{\epsilon_0^3} \mu u + \beta \frac{S_v (1-\epsilon_0)}{\epsilon_0^3} \rho u^2 \tag{38}$$

where  $\alpha$  and  $\beta$  are viscous and inertial coefficients respectively. This equation can also be given as follows:

$$\frac{\Delta P}{\Delta l} = \alpha \frac{(1-\epsilon_0)^2}{\epsilon_0^3} \frac{1}{d_p^2} \mu u + \beta \frac{(1-\epsilon_0)}{\epsilon_0^3} \frac{1}{d_p} \rho u^2 \tag{39}$$

The Ergun equations have been widely used by many authors for development of pressure drop correlations for foam structures.

Several correlations have been developed by different authors, using different methods, and reviews and comparisons have also been published. For example, Dietrich et al. [126] reviewed previously-published pressure data, drawing comparisons with the correlation developed by the authors, which can predict pressure drop within a range of  $10^{-1} < Re < 10^5$  and an error range of  $\pm 40\%$ . The velocity range of previous pressure drop data was found to be 0 m/s to 20 m/s. Edouard et al. [127] reviewed pressure drop correlations for foam structures, finding that no correlation works perfectly and that some may be subject to significant error. Kumar et al. [128] reviewed correlations with three different kinds of coefficient: (1) constant Ergun parameters, (2) no constant Ergun parameter, (3) without Ergun-like model, and using new morphological parameters to determine permeability  $K$  and  $F$ . Based on these reviews, no simple, accurate, uniform correlation for predicting pressure drop could be identified, and previously-published data is varied. Kumar et al. [123] considered the cause of these data variations to be lack of uniformity in the methods used to obtain pressure drop, the methods used to treat data, the choice and definition of morphological, and flow law characteristics, and the choice of characteristic length. Furthermore, Dukhan et al. [118, 119] found that permeability  $K$  and  $F$  vary with different flow regimes. The choice of different velocity ranges during experiments will hence lead to different predictive correlations.

As shown in Table 3, correlations based on experimental data were reviewed and determined with the range of  $K$  in 1.03 to 1420, and the range of  $C$  is within 110.24 to 5460. There are wide variations in  $K$  and  $C$ , caused by the different morphological parameters of foam structures. Comparing Eq. (36) with Eqs. (38) and (39), the following can be obtained:

$$K = \frac{\varepsilon_0^3}{\alpha S_v^2 (1 - \varepsilon_0)^2}, \quad K = \frac{\varepsilon_0^3 d_p^2}{E_1 (1 - \varepsilon_0)^2},$$

$$C = \beta \frac{S_v (1 - \varepsilon_0)}{\varepsilon_0^3}, \quad C = E_1 \frac{(1 - \varepsilon_0)}{\varepsilon_0^3} \frac{1}{d_p}$$

We find that  $K$  increases with increasing  $\varepsilon_0$  and characteristic lengths ( $d_p, d_h, d_s, D_p, d_c$  etc. have different definitions);  $K$  increases with decreasing  $S_v$ , while  $C$  increases with increasing  $S_v$ , and decreasing  $\varepsilon_0$  and characteristic length. However, the definitions of  $K$  and  $C$  only provide an approximate value, and can't be used at all open-cell foam. Therefore, it is essential to develop correlations for specific foam used at engineering application.

Furthermore, as shown in Table 3, the range of experimental velocity is within 0 m/s to 20 m/s, and most authors investigated the range of 0 m/s to 10 m/s.

Experimental data from various sources are summarized in Fig. 13. Because of the non-uniform definition of Reynolds number  $Re$  and Hagen number  $Hg$ , this work summarized the original experimental data of pressure drop vs. velocity. Fig. 13 gives the same conclusion as Table 3, with the range of experimental velocity being 0 m/s to 20 m/s. There are therefore few experimental data for turbulence regions. For the design of heat exchangers to be used under high Reynolds number conditions, there is a need for pressure drop experimental data under high velocity conditions. For a deep understand of the difference of various correlations in high Reynolds number, the predictive curves of correlations developed by different authors are shown in Figs. 14 and 15. The velocity ranges are set within 0 m/s to 10 m/s and 0 m/s to 50 m/s, respectively; the morphological parameters of the sample are assumed to be  $\varepsilon_0=0.91$ ,  $PPI=20$ ,  $d_s=2 \times 10^{-4}$ , and  $d_w=1 \times 10^{-3}$  respectively. Other morphological parameters in correlations are calculated using definitions given by different authors. From Figs. 14 and 15, the deviation among all correlations are huge even blow 10 m/s. Furthermore, the pressure drop prediction difference between Liu [74] and Topin [129] is 302 816.73 Pa/m at 10 m/s; the gap increases with an increase in velocity, to 3 572 914.22 Pa/m at 50 m/s. These correlations have different ranges of application, but the increase in difference with increase in velocity shows that it is hard to predict pressure drop under high Reynolds number conditions in the region of turbulence. Therefore, the more attention should be paid on the investigation of higher Reynolds number to face specially application such as aerospace.

From the above analysis, the following conclusions can be drawn:

- (1) The flow law for different flow regions should be chosen before developing the pressure drop prediction correlation.
- (2) Forchheimer and Ergun equations are mostly used in post-Darcy regions, to develop pressure drop prediction correlations for open-cell foam structures.
- (3) There is no generally-applicable correlation to predict pressure drop for a given sample.
- (4) There is a strong need for correlations to be developed for turbulence regions with high Reynolds numbers.

#### 4.2 Pressure drop correlations of lattice-frame structures

Although there are many pressure drop correlations for open-cell foam structures, only few authors give correlations for lattice-frame structures. In this case, due to the regular periodic structure, it is easy to obtain more accurate correlations.

**Table 3** Pressure drop correlation

| Author                    | Simple                             | $\varepsilon_0$ | PPI  | $D_p$ /mm | $d_f$ /mm | $K \times 10^{-9}/m^2$ | $C/m^{-1}$ | Correlation  | Range of investigate velocity/ $m \cdot s^{-1}$ |
|---------------------------|------------------------------------|-----------------|------|-----------|-----------|------------------------|------------|--|---|
| Du Plessis et al. [69]    | G100                               | 0.973           | 100  | 0.1265    | 0.047     | 1.77                   | 2247       | $\frac{\Delta P}{\Delta l} = \frac{36\chi(\chi-1)}{\varepsilon_0^2 D_p^2} \mu u + \frac{2.05\chi(\chi-1)}{\varepsilon_0^2 (3-\chi) D_p} \rho u^2$ $\frac{1}{\chi} = \frac{3}{4\varepsilon_0} + \frac{\sqrt{9-8\varepsilon_0}}{2\varepsilon_0} \times \cos \left\{ \frac{4\pi}{3} + \frac{1}{3} \cos^{-1} \left[ \frac{8\varepsilon_0^2 - 36\varepsilon_0 + 27}{(9-8\varepsilon_0)^{3/2}} \right] \right\}$ | 0-0.7 (glycerol)<br>0-0.16 (water)              |
|                           | G60                                | 0.975           | 60   | 0.2609    | 0.054     | 8.00                   | 1023       |  |   |
|                           | G45                                | 0.978           | 45   | 0.3568    | 0.054     | 16.02                  | 695        |  |   |
| Richardson et al. [59]    | Al <sub>2</sub> O <sub>3</sub>     | 0.878           | 10   | 1.68      | -         | 19.251                 | 110.24     | $\frac{\Delta P}{\Delta l} = E_1 \frac{S_v^2 (1-\varepsilon_0)^2}{\varepsilon_0^3} \mu u + E_2 \frac{S_v (1-\varepsilon_0)}{\varepsilon_0^3} \rho u^2$ $E_1 = 973 D_p^{0.743} (1-\varepsilon_0)^{-0.0982} \quad E_2 = 368 D_p^{-0.7523} (1-\varepsilon_0)^{-0.07158}$  | 0.7-6 (air)                                     |
|                           |                                    | 0.874           | 30   | 0.826     | -         | 4.821                  | 560.72     |  |   |
|                           |                                    | 0.802           | 45   | 0.619     | -         | 3.963                  | 921.62     |  |   |
|                           |                                    | 0.857           | 65   | 0.359     | -         | 2.395                  | 1765.72    |  |   |
|                           |                                    | 0.94            | 8    | 2.30      | -         | 363.00                 | 302.59     |  |   |
| Moreira et al. [25]       | SiC-Al <sub>2</sub> O <sub>3</sub> | 0.88            | 20   | 0.80      | -         | 60.18                  | 572.46     | $\frac{\Delta P}{\Delta l} = 1.36 \times 10^8 \frac{(1-\varepsilon_0)^2}{\varepsilon_0^3 D_p^{0.234t}} \mu u + 1.8 \times 10^4 \frac{(1-\varepsilon_0)}{\varepsilon_0^3 D_p^{0.234t}} \rho u^2$  | 0-20 (air)<br>0-0.35 (water)                    |
|                           |                                    | 0.76            | 45   | 0.36      | -         | 9.09                   | 1467.42    |  |   |
| Ghani et al. [27]         | Fe-alloy                           | 0.927           | 5.4  | 4.70      | 0.82      | 40.11                  | 202.56     | $\frac{\Delta P}{\Delta l} = \frac{26.12}{d_s^2} \left( \frac{1}{1-G} \right)^4 \frac{G}{4} \mu u + \frac{1.74}{d_s} \left( \frac{1}{1-G} \right)^4 \frac{G}{4} \rho u^2$ $G = 2 \left[ (1-\varepsilon_0) / 3\pi \right]^{1/2}$  | 1-16 (air)                                      |
|                           |                                    | 0.938           | 11.5 | 2.20      | 0.37      | 46.51                  | 387.12     |  |   |
|                           |                                    | 0.937           | 12.8 | 2.00      | 0.33      | 45.85                  | 440.26     |  |   |
|                           |                                    | 0.911           | 5.6  | 4.60      | 0.80      | 33.20                  | 250.85     |  |   |
|                           |                                    | 0.690           | 20   | 0.218     | 0.0651    | 130                    | 1136.36    |  |   |
|                           |                                    | 0.765           | 10   | 0.322     | 0.0967    | 77                     | 534.76     |  |   |
|                           |                                    | 0.748           | 20   | 0.1567    | 0.0476    | 54                     | 877.19     |  |   |
|                           |                                    | 0.752           | 30   | 0.1275    | 0.0391    | 32                     | 1020.41    |  |   |
|                           |                                    | 0.757           | 45   | 0.082     | 0.0195    | 20                     | 1315.79    |  |   |
|                           |                                    | 0.811           | 20   | 0.2008    | 0.0544    | 144                    | 555.56     |  |   |
| Dietrich et al. [23, 126] | Mullite                            | 0.741           | 20   | 0.1992    | 0.0612    | 90                     | 1050.63    | $\frac{\Delta P}{\Delta l} = \frac{110}{\varepsilon_0 d_h^2} \mu u + \frac{1.45}{\varepsilon_0^2 d_h} \rho u^2$  | 1-10 (air)                                      |
|                           |                                    | 0.748           | 30   | 0.3006    | 0.0895    | 299                    | 537.63     |  |   |
|                           |                                    | 0.744           | 45   | 0.195     | 0.0545    | 88                     | 819.67     |  |   |
|                           |                                    | 0.744           | 45   | 0.166     | 0.0533    | 45                     | 980.39     |  |   |
|                           |                                    | 0.744           | 45   | 0.0973    | 0.0293    | 29                     | 1515.15    |  |   |
|                           |                                    | 0.811           | 20   | 0.2032    | 0.051     | 120                    | 529.32     |  |   |
|                           |                                    | 0.744           | 20   | 0.2257    | 0.0896    | 65                     | 1052.63    |  |   |
|                           |                                    | 0.744           | 10   | 0.332     | 0.1063    | 276                    | 740.74     |  |   |
|                           |                                    | 0.744           | 20   | 0.2208    | 0.0719    | 56                     | 813.01     |  |   |
|                           |                                    | 0.744           | 30   | 0.1651    | 0.0544    | 46                     | 1190.48    |  |   |
| OBSiC                     |                                    | 0.744           | 45   | 0.099     | 0.0275    | 17                     | 2000.00    |  |   |
|                           |                                    | 0.744           | 20   | 0.7687    | 0.0622    | 220                    | 666.67     |  |   |

Continued Table 3

| Author                   | Simple | $\epsilon_0$ | PPI | $D_p$ /mm | $d_s$ /mm | $K \times 10^{-9}/m^2$ | $C/m^{-1}$ | Correlation   | Range of investigate velocity/ $m \cdot s^{-1}$ |      |      |
|--------------------------|--------|--------------|-----|-----------|-----------|------------------------|------------|---|---|------|------|
| Dukhan et al. [130, 131] | Al     | 0.919        | 10  |           | 0.406     | 100                    | 210        | $10 \text{ PPI } K = 10^{-8} (0.0013e^{9.55\epsilon_0}), C = 100(-61.33\epsilon_0 + 58.362)$<br>$20 \text{ PPI } K = 10^{-8} (0.0009e^{9.46\epsilon_0}), C = 100(-114.61\epsilon_0 + 108.44)$<br>$40 \text{ PPI } K = 10^{-8} (8 \times 10^{-7} e^{16.39\epsilon_0}), C = 100(-239.92\epsilon_0 + 22.51)$ | 0.5-3 (air)                                     |      |      |
|                          |        | 0.915        | 10  |           | 0.406     | 80                     | 270        |   |   |      |      |
|                          |        | 0.919        | 20  | -         | 0.203     | 63                     | 290        |   |   |      |      |
|                          |        | 0.924        | 20  |           | 0.203     | 54                     | 280        |   |   |      |      |
|                          |        | 0.923        | 40  |           | 0.102     | 47                     | 380        |   |   |      |      |
| Tadrist et al. [132]     | Al     | 0.917        | 10  |           | 1.00      | 130                    | 128        | $\frac{\Delta P}{\Delta l} = \alpha \frac{(1-\epsilon_0)^2}{\epsilon_0^3 d_s^2} \mu u + \beta \frac{(1-\epsilon_0)}{\epsilon_0^3 d_s} \rho u^2$<br>$100 < \alpha < 865; 0.65 < \beta < 2.6$   | -   |      |      |
|                          |        | 0.933        | 20  |           | 0.86      | 250                    | 240        |   |   |      |      |
|                          |        | 0.905        | 40  |           | 0.69      | 66                     | 389        |   |   |      |      |
| Mancin et al. [20]       | Al     | 0.921        | 5   | 5.08      | 0.540     | 236                    | 205        | $\frac{\Delta P}{\Delta l} = \frac{2FG^2}{\rho d_h} G = \rho u \quad F = \frac{1.765 Re^{-0.1014} \epsilon^2}{PPI^{0.6}}$<br>$Re = \frac{d_h G}{\mu \epsilon} \quad d_h = 0.0122 \times PPI^{-0.849}$   | 2-6 (air)                                       |      |      |
|                          |        | 0.903        | 10  | 2.54      | 0.529     | 190                    | 170        |   |   |      |      |
|                          |        | 0.934        | 10  | 2.54      | 0.450     | 187                    | 190        |   |   |      |      |
|                          |        | 0.956        | 10  | 2.54      | 0.445     | 182                    | 240        |   |   |      |      |
|                          |        | 0.932        | 20  | 1.27      | 0.367     | 82.4                   | 226        |   |   |      |      |
|                          |        | 0.930        | 40  | 0.635     | 0.324     | 63.4                   | 342        |   |   |      |      |
| Lacroix et al. [29]      | SiC    | 0.915        |     |           | 0.143     | 32.5                   | 905        | $\frac{\Delta P}{\Delta l} = 150 \frac{(1-\epsilon_0)^2}{\epsilon_0^3 d_p^2} \mu u + 1.75 \frac{(1-\epsilon_0)}{\epsilon_0^3 d_p} \rho u^2$<br>$d_p = 1.5 d_s$  | 0-5 (air)                                       |      |      |
|                          |        | 0.910        |     |           | 0.143     | 28.5                   | 974        |   |   |      |      |
|                          |        | 0.914        | -   |           | 0.390     | 236                    | 337        |   |   |      |      |
|                          |        | 0.890        |     |           | 0.103     | 9.27                   | 177        |   |   |      |      |
|                          |        | 0.810        | 40  |           | 0.110     | 2.67                   | 379        |   |   |      |      |
| Khayargoli et al. [133]  | NC     | 0.86         |     | 0.4       |           | 1.79                   | 2256       | $\frac{\Delta P}{\Delta l} = 100 \frac{(1-\epsilon_0)^2}{\epsilon_0^3 d_p^2} \mu u + \frac{(1-\epsilon_0)}{\epsilon_0^3 d_p} \rho u^2$<br>$d_p = 1.5 \frac{(1-\epsilon_0)}{\epsilon_0} D_p$   | 0-15 (air)                                      |      |      |
|                          |        | 0.83         | -   | 0.5       |           | 3.39                   | 1755       |   |   |      |      |
|                          |        | 0.9          |     | 0.6       |           | 4.76                   | 374        |   |   |      |      |
|                          |        | 0.89         |     | 0.9       |           | 15.41                  | 483        |   |   |      |      |
|                          |        | 0.9          |     | 1.4       |           | 27.64                  | 374        |   |   |      |      |
| Wu et al. [134]          | AS     | 0.55         |     |           |           | 3.12                   | 5460       | $\frac{\Delta P}{\Delta l} = \frac{(1039-1002\epsilon_0)}{d_c^2} \mu u + \frac{0.5138\epsilon_0^{-5.739}}{d_c} \rho u^2$  | 0-10 (air)                                      |      |      |
|                          |        | 0.7          |     |           |           | 5.52                   | 2360       |   |   |      |      |
|                          |        | 0.85         | -   |           |           | 1.03                   | 893        |   |   |      |      |
|                          |        | 0.7          |     |           |           | 2.17                   | 990        |   |   |      |      |
|                          |        | 0.7          |     |           |           | 3.03                   | 662        |   |   |      |      |
| Topin et al. [129]       | NC     | -            |     |           |           | Water                  | Water      | $\frac{\Delta P}{\Delta l} = 1.391 \times 10^{-4} \frac{(1-\epsilon_0)^2}{\epsilon_0^3 D_p^2} \mu u + 1.32 S_v \rho u^2$  | (water)<br>0-2 (air)                            |      |      |
|                          |        | 0.90         |     | 40        |           | air                    | air        |   |   |      |      |
|                          |        | 0.87         |     | 569       |           | 2.28                   | 1.85       |   |   | 2194 | 2138 |
|                          |        | 0.91         | -   | 831       |           | 2.68                   | 2.13       |   |   | 1622 | 1330 |
|                          |        | 0.88         |     | 1840      |           | 6.19                   | 4.44       |   |   | 1130 | 1075 |
|                          |        | 0.89         |     | 2452      |           | 23.2                   | 28.1       |   |   | 631  | 490  |
|                          |        |              |     | 29.8      | 60.2      | 400                    | 381        |   |   |      |      |



Continued Table 3

| Author              | Simple    | $\varepsilon_0$ | PPI | $D_p$ /mm | $d_p$ /mm | $K \times 10^{-9}/m^2$ | $C/m^{-1}$ | Correlation  | Range of investigate velocity/ $m \cdot s^{-1}$ |   |
|---------------------|-----------|-----------------|-----|-----------|-----------|------------------------|------------|--|---|---|
| Liu et al. [74]     |           | 0.914           | 5   | 1.21      |           | 370                    | 164.07     | $\frac{\Delta P}{\Delta l} = \frac{22(1-\varepsilon_0)^2}{\varepsilon_0^3 d_p^2} \mu u + \frac{0.22(1-\varepsilon_0)}{\varepsilon_0^3 d_p} \rho u^2$ | 0–10 (air)                                      |   |
|                     |           | 0.918           | 10  | 1.19      |           | 623                    | 230.58     |  |   |   |
|                     |           | 0.870           | 20  | 8.27      |           | 125                    | 280.86     |  |   |   |
|                     | Al        | 0.909           | 20  | 8.05      | –         | 102                    | 231.08     |  |   |   |
|                     |           | 0.935           | 20  | 8.14      |           | 242                    | 264.26     |  |   |   |
|                     |           | 0.958           | 20  | 8.00      |           | 1420                   | 285.32     |  |   |   |
|                     |           | 0.935           | 40  | 6.85      |           | 133                    | 282.43     |  |   |   |
|                     |           |                 |     |           |           |                        |            |  |   |   |
| Inayat et al. [135] |           | 0.871           |     | 4.189     | 1.104     |                        |            | $\frac{\Delta P}{\Delta l} = \frac{\alpha}{36} \frac{S_v}{\varepsilon_0^3} \mu u + \frac{\beta}{6} \frac{S_v}{\varepsilon_0^3} \rho u^2$             | 0–6 (air)                                       |   |
|                     | Ti-6Al-4V | 0.846           | –   | 3.413     | 1.016     | –                      | –          |  |   | $\alpha = \left[ \left( \frac{1-0.971(1-\varepsilon_0)^{0.5}}{0.6164(1-\varepsilon_0)^{0.5}} \right)^{-1} \right]^{-1}$ |
|                     |           | 0.799           | –   | 2.688     | 0.999     | –                      | –          |  |   |   |

#### 4.2.1 Tetrahedral structure

Kim et al. [9, 137, 138] investigated the hydraulic characteristics of tetrahedral structures, defining unit cell length  $S_{\text{cell}}$  (as shown in Fig. 7, this is  $S_x$  for the  $x$  direction, and  $S_y$  for the  $y$  direction) as characteristic length. They used a pressure loss coefficient per unit cell  $K_{\text{cell}}$  based on periodic flow patterns, as in Eq. (40):

$$K_{\text{cell}} = \frac{\Delta P_{\text{cell}}}{\rho u^2 / 2} \quad (40)$$

where  $\Delta P_{\text{cell}}$  is pressure drop per unit cell. Through experiments, the authors obtained the following correlations:

$$K_{\text{cell}} = 1000 \frac{1}{Re_{S_{\text{cell}}}}, \quad Re_{S_{\text{cell}}} < 2000 \quad (41)$$

Transition range:  $2000 < Re_{S_{\text{cell}}} < 3000$ ,  $K_{\text{cell}}=0.32$  for  $x$  direction,  $K_{\text{cell}}=0.62$  for  $y$  direction:  $3000 < Re_{S_{\text{cell}}}$ . The same trends were noted by Son et al. [38].

#### 4.2.2 Pyramidal and Kagome structure

Krishnan et al. [139] numerically investigated Tetrahedral, Pyramidal, and Kagome structures, concluding that the friction factor ( $f$ ) values vs. Reynolds number of these three structures, were ranked according to select flow direction as: Kagome>Pyramidal>Tetrahedral. Hoffmann [140] also defined a correlation for predicting pressure drop in Kagome structures in the region of turbulence, given in Eq. (42):

$$f = \frac{\Delta P}{L} \frac{H}{\rho u^2 / 2} = 0.56 \quad (42)$$

#### 4.2.3 X-type structure

For X-type structures, Yan et al. [83] found that the  $f$  value of 2.58 is constant within  $1400 < Re_H < 7500$ .

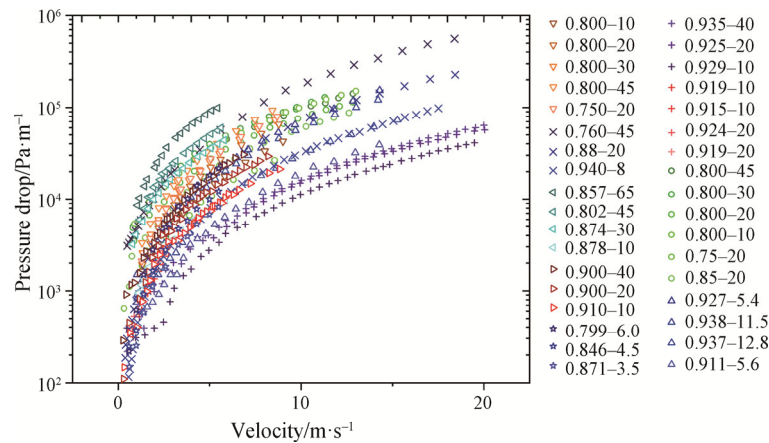
Although the periodic nature of the lattice-frame structure allows for development of accurate pressure drop correlations, more extensive dynamic experiments for these structures with different morphological parameters are needed.

### 4.3 Pressure drop in structured packed beds and wire-woven structures

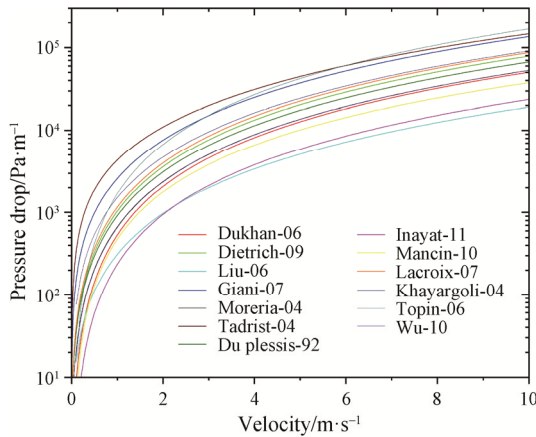
#### 4.3.1 Packed beds

For the prediction of pressure drop in packed beds, Ergun [124] developed the most widely used correlation, given by Eq. (39), where  $E_1$  and  $E_2$  are 150 and 1.75 respectively; Eq. (39) can be transformed to Eq. (43), as shown:

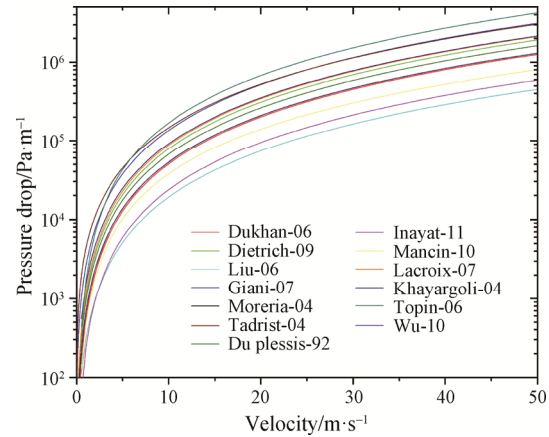
$$f = 150 \frac{(1-\varepsilon)}{Re} + 1.75 \quad (43)$$



**Fig. 13** Pressure drop vs velocity of various foam: (1) Dukhan-11 (Al) [39], (2) Dukhan-06 (Al) [130], (3) Garrido-08 (Al<sub>2</sub>O<sub>3</sub>) [37], (4) Gianni-05 (Fe-alloy) [27], (5) Dietrich-09 (Al<sub>2</sub>O<sub>3</sub>) [23], (6) Moreira-04 (SiC-Al<sub>2</sub>O<sub>3</sub>) [26], (7) Richardson-00 (Al<sub>2</sub>O<sub>3</sub>) [59], (8) Leong-06 (Al) [136], (9) Inayat-11 (Ti-6Al-4V) [135]. The experimental velocity is within 0 m/s to 20 m/s, and most authors investigate the range of 0 m/s to 10 m/s



**Fig. 14** Pressure drop vs velocity prediction with different correlation developed by different author within 0–10 m/s. The morphological parameters of the sample are assumed to be  $\epsilon_0=0.91$ , PPI=20,  $d_s=2 \times 10^{-4}$ , and  $d_w = 1 \times 10^{-3}$ , respectively



**Fig. 15** Pressure drop vs velocity prediction with different correlation developed by different author within 0–50 m/s. The morphological parameters of the sample are assumed to be  $\epsilon_0=0.91$ , PPI=20,  $d_s=2 \times 10^{-4}$ , and  $d_w = 1 \times 10^{-3}$  respectively

where  $f = \frac{\Delta P}{L} \frac{d_p}{\rho u^2} \frac{\epsilon^3}{(1-\epsilon)}$  and Reynolds number

$Re = \frac{d_p \rho u}{\mu}$ . Many correlations have almost the same

formation as Eq. (43). This can also be modified as follows:

$$f = c_1 \frac{(1-\epsilon)}{Re} + c_2 \quad (44)$$

where  $c_1$  and  $c_2$  are constant; in some correlations  $c_1$  and  $c_2$  are related to  $\epsilon$ . Erdim et al. [141] reviewed many pressure drop correlations for packed beds and related  $Re$  ranges of application. They concluded that, although many new correlations have been developed, few authors

have compared and evaluated existing correlations widely enough. There is therefore no general agreement on which correlations are the most accurate. However, the random packed beds always show a huge pressure drop due to the lower porosity and complex air pathways. Therefore, the packed methods have been investigated to decrease pressure drop.

For structured packed beds, the Ergun correlation over predicted pressure drop [142]. The flow pressure drop in structured beds is much lower than that in random packed beds. Furthermore, pressure drop is closely connected with packing form [97, 143]. Susskind et al. [144] investigated flow in various packing forms, finding that pressure drop decreases with an increase in relative horizontal spacing. Yang et al. [145] numerically

investigated five different packed channels, finding that pressure drop will greatly decrease and overall heat transfer performance will increase, given well-selected packing form. Wang et al. [98] developed a new packing form (the GSCSPB) and investigated its pressure drop and overall heat transfer performance. For heat transfer enhancement, structured packed beds have more potential than random structures. Different packing forms can be developed to flexibly satisfy different heat transfer enhancement applications. There should therefore be further investigation of packing forms.

#### 4.3.2 Wire-woven structure

Wire-woven metals have various applications for heat transfer due to their flexible structure. However, only a few structures have been investigated in relation to pressure drop. Tian et al. [146] experimentally

A-direction

$$f = -2.608 \ln(Re_H) + 3.0116 \quad 5.5 \times 10^3 \leq Re_H \leq 1.8 \times 10^4 \quad (45a)$$

$$f = 0.0645 \ln(Re_H) - 0.1847 \quad 1.8 \times 10^4 \leq Re_H \leq 3.3 \times 10^4 \quad (45b)$$

B-direction

$$f = -0.8049 \ln(Re_H) + 8.2254 \quad 5.2 \times 10^3 \leq Re_H \leq 1.7 \times 10^4 \quad (46a)$$

$$f = -0.2165 \ln(Re_H) + 2.5497 \quad 1.7 \times 10^4 \leq Re_H \leq 2.5 \times 10^4 \quad (46b)$$

$$f = 0.0585 \ln(Re_H) - 0.2570 \quad 2.5 \times 10^4 \leq Re_H \leq 3.1 \times 10^4 \quad (46c)$$

where  $Re_{D_h} = \frac{\rho u D_h}{\mu}$ .  $D_h$  is the hydraulic diameter of a rectangular test section. They also investigated three-layered WBK, obtaining other correlation forms for pressure drop prediction [8], given by Eq. (47):

A-direction

$$f = 3120 (Re_{D_h})^{-1} \quad Re_{D_h} < 6000 \quad (47a)$$

B-direction

$$f = 3430 (Re_{D_h})^{-1} \quad 6000 < Re_{D_h} < 10\,000 \quad (47b)$$

$$\text{Transition region} \quad 6000 < Re_{D_h} < 10\,000 \quad (47c)$$

The difference in pressure drop between A-direction and B-direction is due to the open area ratio. The A-direction open area ratio (0.75) is larger than that of the B-direction (0.62) [8]. The open area ratio should thus be factored into pressure drop prediction. Furthermore, the pressure drop of wire-woven structure should be compared with lattice-frame structure with the same shape, and figured out the difference between two structures. In addition, many other structures have still not been investigated for their pressure drop properties.

## 5. Effect of Morphology on HTC

The HTC is an indispensable parameter for heat exchangers, solar energy collection and storage, and

investigated the pressure drop of plane weave copper meshes, giving  $f$  for different samples in Reynolds number ranges of 700 to 10 000. The authors also found that  $f$  is not only a function of  $\varepsilon$ , but also a function of the open area ratio. Compared with other wire-woven metal structures, wire-woven bulk Kagome (WBK) has been more widely investigated for its pressure drop qualities. The pressure drop properties of single-layered WBK have been numerically investigated by Shen et al. [147], who found its  $f$  to be 0.54 in the Reynolds range of 3995 to 8710. The authors also compared the pressure drop with that of Kagome lattice-frame structures, finding that both structures have almost identical pressure drop. For the multi-layered WBK, Joo et al. [148] obtained the  $f$  vs. Reynolds number functions for two directions of multi-layered WBK (five layers), given by Eqs. (45) and (46):

cooling systems, and other applications. However, it is hard to predict HTC though theoretical derivation, especially in the case of porous structures. Some authors have therefore combined experimental and numerical analysis to develop HTC correlations. In this section, a number of HTC correlations for open-cell foam, lattice-frame, and other porous structures will be reviewed.

### 5.1 Correlations for predicting HTC of open-cell foam structures

It is important to understand transport properties at pore scale in open-cell foam structures. These can explain macroscopic heat transfer phenomena and can also offer methods of optimizing pore scale structure design for different applications. However, it is hard to determine microscopic properties through experimentation due to the complexities of pore scale structure. The volume averaging method is generally used to analyze heat transfer in open-cell foam structures. This method is applied if the pore size of porous media is much smaller than the scale of the research system [149]. Two types of models are used to apply the volume average method in investigating heat transfer: local thermal equilibrium (LTE) and local thermal non-equilibrium (LTNE) models [150]. LTE models are also referred as one-equation models; these are always used under conditions of small local temperature

differences between fluid and solid. However, in many applications, local temperature differences are larger and in these situations, the LTNE model (two-energy equation) is applied. The LTNE energy equations can be divided into fluid energy and solid energy equations, given in Eqs. (48) and (49), respectively:

Fluid energy:

$$\varepsilon(\rho c_p)_f \frac{\partial T_f}{\partial t} + (\rho c_p)_f v \cdot \nabla T_f = \nabla \cdot (\underline{K} \cdot \nabla T_f) - h_v (T_f - T_s) \quad (48)$$

Solid energy:

$$(1 - \varepsilon)(\rho c)_s \frac{\partial T_s}{\partial t} = \nabla \cdot (\underline{K} \cdot \nabla T_f) - h_v (T_s - T_f) \quad (49)$$

where  $\underline{K}$  is total effective thermal conductivity tensor, and  $h_v$  is volumetric heat transfer coefficient (VHTC). VHTC couples the fluid energy and solid energy equations.

There are three ways to obtain VHTC: experimentally, through theoretical derivation [151], or through numerical simulation [65, 152]. Experimental methods can be divided into steady state [7] and transient methods (single-blow method) [28, 120, 153]. VHTC values obtained using steady state methods are affected by the thermal conductivity of open-cell foam; while in the case of transient methods, the temperature difference can be neglected in the transverse direction [7, 28]. Xia et al. [28] also noted that transient methods are simpler in their operation than steady state methods. A few authors have obtained VHTC through theoretical derivation, due to the complexities of pore scale structure. Nakayama et al. [151] developed a correlation for predicting VHTC (given in Table 4) through rigorous mathematical derivation. Many authors have used numerical simulation to develop correlations for predicting VHTC. One group of authors used the real structure of open-cell foam obtained through computer tomography, and used CFD to simulate the heat transfer characteristics of open-cell foam. However, the scale of reconstructed structures is always small and these cannot model fluid lateral mixing in open-cell foam very well. Another group of authors used simplified geometry, such as cubic [154] dodecahedron [155] tetrakaidecahedral models [152, 156]. Although these can give a large scale through the use of a periodic boundary, such models still differ from the real structures. The transient methods are most of the methods used by authors due to the reliable theoretical basis, simple experimental process and less influence factors.

This present work reviewed several VHTC-predicting correlations developed in different ways. As shown in columns 2, 3, and 4 of Table 4, many samples with a large range of  $\varepsilon$  (0.65 to 0.97) and PPI (5 to 66.04) have been investigated. As in the case of pressure drop

predicting correlations, from column 5 of Table 4 it can be noted that there is no unique characteristic length for VHTC correlations.  $d_w$  and  $d_s$  are widely used as characteristic length, due to the ease of determination. Furthermore, Fu et al. [157] developed four VHTC predictive correlations with four different characteristic lengths:  $d_h$ ,  $d_m$ ,  $1/S_v$ , and  $d_r$ . The characteristic length  $1/S_v$  is also used by Peng et al. [158]. Dietrich [22] used hydraulic diameter  $d_h$  as characteristic length, but this is defined differently than by Fu et al. Although, the VHTC predictive correlation used  $d_h$ ,  $d_m$  also showed a good agreement with experimental data in their own work, as discussed in section 3, the errors of  $d_s$ ,  $\varepsilon_0$ ,  $S_v$  and PPI will influence accuracy of pore diameter. And then, the correlations are hard to use to predict VHTC for other open-cell foam accurately. From column 7, it can be noted that the investigative range of velocity is below 10 m/s; the VHTC of turbulence regions with velocities higher than 10 m/s therefore remains to be investigated. Some predictive correlations of interstitial Nusselt number  $Nu = \frac{hl}{k_f}$  and volumetric Nusselt number

$Nu_v = \frac{h_v l^2}{k_f}$  are given in column 6, where  $l$  is characteristic length,  $h$  is interstitial heat transfer coefficient;  $h_v$  is VHTC, and  $k_f$  is fluid thermal conductivity. Additionally, if  $Nu_v = \frac{h_v}{k_g S_v}$  when  $1/S_v$  is

the characteristic length, the correlation between VHTC  $h_v$  and interstitial heat transfer coefficient  $h$  is  $h_v = h S_v$ . The form of most correlations can be given as in Eq. (50):

$$Nu_v = a Re^b \quad (50)$$

where  $a$  and  $b$  are coefficients. Coefficient  $a$  is related to parameters like  $\varepsilon_0$  [151, 152], thickness of porous media  $H$  [153, 157], Reynolds number  $Re$  [22], and Prandtl number  $Pr$  [159, 160], while coefficient  $b$  is almost constant. Younis and Viskanta take  $d_w/H$  into consideration. Hwang et al. [120] developed three different Nusselt number correlations with three different porosities. Ando et al. [161] also developed five correlations for five samples with different PPIs. Some authors used different correlation forms; for example, Peng et al. [158] took temperature  $T$  and  $\varepsilon_0$  into consideration and used the form:  $Nu_v = A + a Re^b$ , while Dietrich et al. [22] developed Nusselt-Hagen correlations that can allow easy and accurate prediction of HTC based on pressure data of the foam structure. Therefore, different effects were taken into consideration by different authors, and this is the reason why lacking uniform predictive correlations.

**Table 4** HTC correlations

| Author                       | samples                        | $\varepsilon_0$ | PPI   | Characteristic length      | Correlation  | Range of Velocity /m s <sup>-1</sup> | Method                 |  |   |
|------------------------------|--------------------------------|-----------------|-------|----------------------------|--|--------------------------------------|------------------------|--|---|
| Younis-Viskanta et al. [153] | Al <sub>2</sub> O <sub>3</sub> | 0.870           | 10.16 | $\varepsilon_0$            | $Nu_v = 0.819 \left[ 1 - 7.33 \frac{d_w}{H} \right] Re_{d_w}^{0.36} \left[ 1 + 15 \frac{d_w}{H} \right]$ | 1.24–6.75                            | Transient              |  |   |
|                              |                                | 0.850           | 20.34 |                            |  | 1.00–7.15                            |                        |  |   |
|                              |                                | 0.830           | 30.48 |                            |  | 1.20–6.37                            |                        |  |   |
|                              |                                | 0.840           | 45.72 |                            |  | 1.16–6.48                            |                        |  |   |
|                              |                                | 0.834           | 66.04 |                            |  | 1.56–5.72                            |                        |  |   |
| Fu et al. [157]              | YZA                            | 10.16           | 10.16 | $d_h = 4\varepsilon_0/S_v$ | $Nu_v = [0.0730 + 1.302(H/d_h)] Re_{d_h}^{0.36}$   | 0.08–6.00                            | Transient              |  |   |
|                              |                                | 20.34           | 20.34 |                            |  |                                      |                        | $d_m = \frac{\sqrt{4\varepsilon_0/\pi}}{PPC}$            | $Nu_v = [0.0426 + 1.236(H/d_m)] Re_{d_m}^{0.36}$    |
|                              |                                | 30.48           | 30.48 |                            |  |                                      |                        |  |   |
|                              | Mullite                        | 20.34           | 20.34 | $d_s = 1/S_v$              | $Nu_v = [0.0252 + 1.280(H/d_s)] Re_{d_s}^{0.36}$   | 0.08–6.00                            | Transient              |  |   |
|                              |                                | 20.34           | 20.34 |                            |  |                                      |                        | $d_s = C/F$  | $Nu_v = [0.000267 + 1.447(H/d_s)] Re_{d_s}^{0.601}$ |
| Cordierite                   |                                | 45.72           | 45.72 |                            |  |                                      |                        |  |   |
| Hwang et al. [120]           | Al                             | 0.700           |       | $d_w$                      | $Nu_v = 0.1569 Re_{d_w}^{0.825}$   | 0.40–2.00                            | Transient              |  |   |
|                              |                                | 0.800           |       |                            |  |                                      |                        | $Nu_v = 0.3560 Re_{d_w}^{0.644}$                         |   |
|                              |                                | 0.950           |       |                            |  |                                      |                        |  | $Nu_v = 0.3248 Re_{d_w}^{0.601}$                    |
| Giani et al. [27]            | Fe-Cr alloy                    | 0.927           | 5.4   | $d_s$                      | $Nu_v = 1.2 Re_{d_s}^{0.43} Pr^{1/3}$  | 1.20–5.70                            | Transient              |  |   |
|                              |                                | 0.937           | 12.8  |                            |  |                                      |                        |  |   |
|                              | Cu                             | 0.911           | 5.6   | $d_s$                      | $Nu_v = 0.52 Re_{d_s}^{0.5} Pr^{0.37}$   | 0.61–3.20                            | steady                 |  |   |
|                              |                                | 0.9726          | 5     |                            |  |                                      |                        |  |   |
|                              |                                | 0.9118          | 5     |                            |  |                                      |                        |  |   |
| Calmidi et al. [160]         | Al                             | 0.9486          | 10    | $d_s$                      | $Nu_v = 0.52 Re_{d_s}^{0.5} Pr^{0.37}$   | 0.61–3.20                            | steady                 |  |   |
|                              |                                | 0.9546          | 20    |                            |  |                                      |                        |  |   |
|                              |                                | 0.9005          | 20    |                            |  |                                      |                        |  |   |
|                              |                                | 0.9272          | 40    |                            |  |                                      |                        |  |   |
|                              |                                | 0.9132          | 40    |                            |  |                                      |                        |  |   |
| Nakayama et al. [151]        | -                              | 0.70–0.95       | -     | $d_c$                      | $Nu_v = 0.07 \left( \frac{\varepsilon}{1-\varepsilon} \right)^{2/3} Re_{d_c} Pr^{0.37}$                  | -                                    | Theoretical derivation |  |   |
|                              |                                | 0.66–0.93       | -     |                            |  |                                      |                        | $Nu_v = 2.069 S_v \varepsilon_0^{0.38} Re_{d_c}^{0.438}$ |   |
| Wu et al. [152]              | -                              | 0.66–0.93       | -     | $d_c$                      | $Nu_v = 2.069 S_v \varepsilon_0^{0.38} Re_{d_c}^{0.438}$   | 0.60–8.00                            | Numerical simulations  |  |   |
| Ando et al. [161]            | Ceramic                        | -               | 6     | $d_w$                      | $Nu_v = 0.055 Re_{d_w}^{1.15}$   | 1.00–10.00                           | Transient              |  |   |
|                              |                                | -               | 9     |                            |  |                                      |                        | $Nu_v = 0.012 Re_{d_w}^{1.27}$                           |   |
|                              |                                | -               | 13    |                            |  |                                      |                        |  | $Nu_v = 0.015 Re_{d_w}^{1.21}$                      |
|                              |                                | -               | 20    |                            |  |                                      |                        |  |   |

Continued Table 4

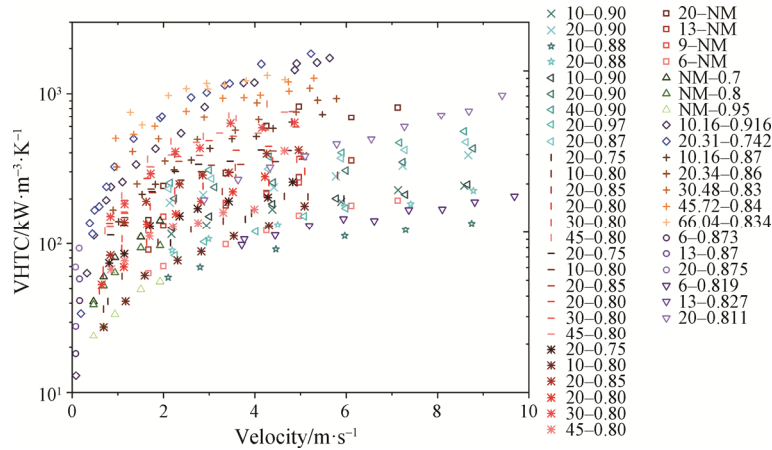
| Author                | samples                        | $\varepsilon_0$ | PPI | Characteristic length  | Correlation  | Range of Velocity (m/s) | Method               |           |
|-----------------------|--------------------------------|-----------------|-----|--|--|-------------------------|----------------------|-----------|
| Dietrich [22]         | Al <sub>2</sub> O <sub>3</sub> | 0.800           | 10  |  |  |                         |                      |           |
|                       |                                | 0.800           | 20  |  |  |                         |                      |           |
|                       |                                | 0.800           | 30  |  |  |                         |                      |           |
|                       |                                | 0.800           | 45  |  |  |                         |                      |           |
|                       |                                | 0.750           | 20  |  |  |                         |                      |           |
|                       |                                | 0.850           | 20  |  |  |                         |                      |           |
|                       | OBSiC                          | 0.800           | 10  | $d_h = 4 \frac{\varepsilon_0}{S_v}$  | $Nu = 0.45 C_{Re} C_{Re_{geo}} Hg_{d_h} Pr^{1/3}$<br>$Nu = 0.57 C_{Re} C_{Re_{geo}} Re_{d_h} Pr^{1/3}$ |                         | 0.50–5.00            | Transient |
|                       |                                | 0.800           | 20  |  |  |                         |                      |           |
|                       |                                | 0.800           | 30  |  |  |                         |                      |           |
|                       |                                | 0.800           | 45  |  |  |                         |                      |           |
|                       |                                | 0.750           | 20  |  |  |                         |                      |           |
|                       |                                | 0.850           | 20  |  |  |                         |                      |           |
| Mullite               | 0.800                          | 10              |     | $Hg_{d_h} = \frac{\Delta P}{\Delta L} \frac{d_h^3}{\rho_1 \mu^2}$<br>$C_{Re} = \left( \frac{Re+1}{Re+100} \right)^{0.25}$<br>$C_{geo} = \left( \frac{d_h/L}{(d_h/L)_{mean}} \right)^{1.5}$ |  |                         |                      |           |
|                       | 0.800                          | 20              |     |  |  |                         |                      |           |
|                       | 0.800                          | 30              |     |  |  |                         |                      |           |
|                       | 0.800                          | 45              |     |  |  |                         |                      |           |
|                       | 0.750                          | 20              |     |  |  |                         |                      |           |
|                       | 0.850                          | 20              |     |  |  |                         |                      |           |
| Peng et al. [158]     | Al <sub>2</sub> O <sub>3</sub> | 0.995           | 30  | $1/S_v$  | $Nu_v = 3.43 \times 10^{-11} \varepsilon_0 T^3 + 0.0340 Re_{S_v}$                                      | 0.60–1.00               | Steady               |           |
| Kamimoto et al. [163] | RD                             | RD              | RD  | $d_s$  | $Nu_v = 0.124 (Re_{d_s} Pr)^{0.791}$   | 0.05–15                 | Transient and steady |           |
|                       | Cu                             | 0.900           | 10  |  |  |                         |                      |           |
| Xia et al. [28]       | Ni                             | 0.900           | 20  | $d_w$  | $Nu_v = 0.34 \varepsilon_0^{-2} Re_{d_w}^{0.61} Pr^{1/3}$  | 2.00–9.00               | Transient            |           |
|                       |                                | 0.900           | 10  |  |  |                         |                      |           |
|                       |                                | 0.900           | 20  |  |  |                         |                      |           |
|                       | 0.970                          | 20              |     |  |  |                         |                      |           |
|                       | 0.870                          | 20              |     |  |  |                         |                      |           |
|                       | 0.88                           | 10              |     |  |  |                         |                      |           |
| SiC                   | 0.88                           | 10              |     |  |  |                         |                      |           |
|                       | 0.88                           | 20              |     |  |  |                         |                      |           |

RD: Review data

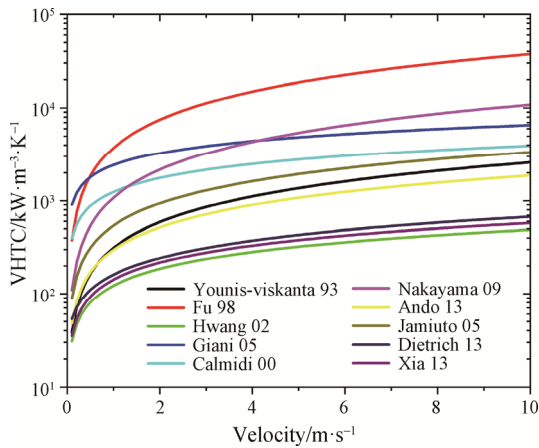


This present work reviewed experimental data of VHTC vs. velocity; as shown in Fig. 16, the obtained data were mostly within a velocity range of 0 m/s to 10 m/s. It is also noted that some data obtained differ from those given by other authors by some orders of magnitude, even at the same velocity. As in the case of experimental pressure data, discussed in the previous section, there are few experimental VHTC data for turbulence regions. Future work should thus focus on obtaining the VHTC of open-cell foam structures at high Reynolds number ranges. Fig. 17 summarizes the predictive curve of some VHTC correlations. Some assumed conditions are given: the morphological parameters of the sample are set as  $\varepsilon_0=0.95$ , PPI=20,  $d_s=2\times 10^{-4}$ ,  $d_w=1\times 10^{-3}$  respectively; other morphological parameters in correlations are calculated using different definitions given by different authors. The velocity

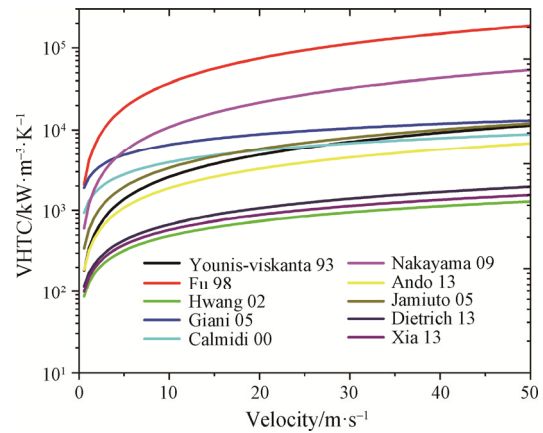
ranges are set to 0 m/s to 10 m/s and 0 m/s to 50 m/s, respectively. From Figs. 17 and 18, an increase in difference with velocity can be noted; for example, the VHTC values predicted by Xia [28] and Fu [157] are 32 728.61 kW/(m<sup>3</sup>·K) and 164 077.8 kW/(m<sup>3</sup>·K) at 10 m/s and 50 m/s, respectively. Furthermore, some curves cross in the predicting velocity range. Differences between correlations may result from using different methods to develop correlations, from different shapes and materials of samples, or from different experimental conditions. There is thus no general correlation for predicting the VHTC of open-cell foam structures in the turbulence region with high Reynolds numbers. It is noteworthy that the above correlations are not distinguished according to flow region (Darcy and non-Darcy). Dukhan et al. [162] found that the Nusselt number is constant in the Darcy region.



**Fig. 16** Data of VHTC vs. velocity: (1) Xia-17 (Cu, SiC, Ni) [28]; (2) Ditecth-13 (Al<sub>2</sub>O<sub>3</sub>, OBSiC, Mullite) [22]; (3) Ando-13 (Al<sub>2</sub>O<sub>3</sub>) [161]; (4) Hwang-02 (Al) [120]; (5) Fu-98 (YZA) [157]; (6) Younis-Viskanta-93 (Al<sub>2</sub>O<sub>3</sub>) [153]; (7) Ichimiya-99 (Al-Ceramic) [164]; (8) Kamiuto-05 (Al-Ceramic) [163]



**Fig. 17** VHTC vs. velocity prediction with different correlation developed by different author within 0 m/s to 10 m/s



**Fig. 18** VHTC vs. velocity prediction with different correlation developed by different author within 0 m/s to 50 m/s

From the above analysis, it can be concluded that:

(1) LTNE models are used for application of the volume average method in investigating heat transfer of open-cell foam structures.

(2) Transient experiments are most widely used by authors to determine VHTC.

(3) There are no generally-applicable VHTC predictive correlations.

(4) There is a need for development of correlations that can be applied in turbulence regions with high Reynolds numbers.

## 5.2 Correlations for predicting HTC of lattice-frame structures

### 5.2.1 Tetrahedral structure

As in the case of pressure drop correlations, there are few HTC correlations for lattice-frame structures. Kim et al. [137, 138] investigated forced convection heat transfer of single-side heating tetrahedral structures. Correlations for predicting the spatially-averaged HTC for different materials in the  $y$  direction (shown in Fig. 7) were developed [138], given in Eq. (51):

LM25 core and substrates

$$Nu_{S_y} = 1.02 Re_{S_y}^{0.55} \quad (51a)$$

Polycarbonate core with Al substrates

$$Nu_{S_y} = 0.14 Re_{S_y}^{0.68} \quad (51b)$$

The authors found that the tetrahedral structure contributed 57% of overall heat transfer when using a high thermal conductivity material. In the  $x$  direction, the spatially-averaged HTC predictive correlation for LM25 core and substrates [9] is as shown in Eq. (52):

$$Nu_{S_y} = 0.98 Re_{S_y}^{0.56} \quad (52)$$

The authors also analyzed the influence of flow characteristic of the tetrahedral structure on overall heat transfer [137], with arch-shaped vortices, horseshoe vortices, and the delay of flow separation was found to contribute to an increase in overall heat transfer. Other authors also investigated tetrahedral structures. Zhang et al. [165] numerically investigated such structures with different strut shapes, i.e., cylinder-shaped and rectangular-shaped struts. For a given Reynolds number, the tetrahedral structure with rectangular-shaped struts has higher overall Nusselt numbers than that with cylinder-shaped struts. Son et al. [38] experimentally investigated forced convection heat transfer of tetrahedral structures with heating on both sides. They correlated strut diameter with  $\varepsilon$ , as in Eq. (28), finding that the Nusselt number increases with a decrease in  $\varepsilon$  for a given Reynolds number.

### 5.2.2 X-type structure

Jin et al. [166] compared the average overall Nusselt

number of X-type structures with that of pyramidal structures for a given Reynolds number. X-type structures contributed 47% to 60% higher Nusselt numbers than pyramidal structures. Krishnan et al. [139] compared the Nusselt number of a tetrahedral, pyramidal, and Kagome structure for a given direction and Reynolds number, finding that the Nusselt number rank is as follows: Tetrahedral > Pyramidal > Kagome. Shen et al. [147] compared the overall Nusselt number of Kagome and single-layered wire-woven bulk Kagome (WBK) structures, concluding that the Kagome structure provided 26% to 31% higher overall Nusselt numbers than WBK in the Reynolds number range of 3995 to 8710. Hoffmann et al. [140] developed a correlation for predicting average HTC, given in Eq. (53):

$$Nu_H = 1.3513 Re_{S_y}^{0.5414} \quad (53)$$

Yan et al. [31, 167] developed a correlation for predicting HTC in X-type structures, given in Eq. (54):

$$Nu_H = 3.228 Re_{S_y}^{0.428} \quad (54)$$

The same with friction factor correlation, the Nusselt number correlations of lattice-frame structure are also obtained easily, and the height is always be defined to be characteristic length. Therefore, it is possible to compare heat transfer performance between different structures with the same porosity. With further development of manufacturing technologies, more lattice-frame structures with different shapes and sizes can be obtained. Forced convection heat transfer characteristics of these different structures can therefore be more widely investigated.

## 5.3 Forced convection heat transfer of structured packed beds and wire-woven structures

### 5.3.1 Packed beds

Forced convection heat transfer in random packed beds has been widely investigated, through both experimental and numerical methods. Many correlations for predicting HTC have been developed. However, random packed beds have poor controllability and large pressure drops. Structured packed beds have therefore been more extensively investigated in recent years. This work reviews the correlations for predicting HTC of several structured packed beds.

Romkes et al. [97] investigated CSP with five different square channel-particle diameter ratios, fitting computational fluid dynamics (CFD) results using the correlation given in Eq. (55):

$$Nu = c_1 + c_2 Re^n Pr^{1/3} \quad (55)$$

where  $c_1$ ,  $c_2$ , and  $n$  are constant and the characteristic length is the particle diameter. These constants are different for five square channel-particle diameter ratios.

Yang et al. [145] numerically investigated a number of novel structured packed beds with different particle shapes, also comparing packed beds with non-uniform and uniform particles. They further developed interstitial Nusselt number correlations for these packed beds based on Eq. (56):

$$Nu = c_1 + c_2 Re_{d_h}^n Pr^{1/3} \left( \frac{d_p}{d_h} \varepsilon \right)^n \quad (56)$$

where  $d_h = 4 \frac{\varepsilon}{1-\varepsilon} \left( \frac{V_p}{A_p} \right)$ ;  $d_h = 2 \left( \frac{3V_p}{4\pi} \right)^{1/3}$ ;  $Re = \frac{ud_h}{\varepsilon \nu}$ ,

and  $A_p$  and  $V_p$  are the particle surface and volume, respectively. The authors [142] also experimentally investigated packed beds using single blow methods, finding that numerical methods are appropriate for determining the interstitial Nusselt number. With proper selection, some structured packed beds can reduce pressure drop and improve heat transfer. The Nusselt number for such packed beds is over-predicted when using Wakao's equation [168] given in Eq. (57):

$$Nu = 2 + 1.1 Re_{d_h}^{0.6} Pr^{1/3} \quad (57)$$

Wang et al. [98] developed the GSCSPB and investigated its pressure drop and heat transfer performance. It was found to have lower pressure drop and higher overall heat transfer than random packed beds and some traditional structured beds.

### 5.3.2 Wire-woven structure

Wire-woven structures have similar thermal performance to lattice-frame structures due to similar geometry. Some differences between these two can be attributed to the tortuous shape and thicker ligaments of lattice-frame structures [80]. Few authors have investigated the thermal performance of wire-woven structures and few correlations for these have been developed. Tian et al. [146] experimentally investigated the overall heat transfer performance of two wire-woven structures with square-shaped and diamond-shaped pores, respectively, using steady-state methods. They found that  $\varepsilon$  and surface area density have a strong influence on overall heat transfer, while direction has only a weak influence. Joo et al. [148] experimentally investigated the heat transfer performance of five-layered WBK under forced convection heat transfer and single heating. They found that the Nusselt number increased with a decrease in open area ratio, developing the WBK Nusselt number predictive correlation for two directions given in Eq. (58):

A-direction

$$Nu_H = 0.183 Re_H^{0.8} Pr^{0.4} \quad 5.5 \times 10^3 \leq Re_H \leq 1.8 \times 10^4 \quad (58a)$$

$$Nu_{S_y} = 0.14 Re_{S_y}^{0.68} \quad 1.8 \times 10^3 \leq Re_H \leq 3.3 \times 10^4 \quad (58b)$$

B-direction

$$Nu_H = 0.212 Re_H^{0.8} Pr^{0.4} \quad 5.2 \times 10^3 \leq Re_H \leq 3.1 \times 10^4 \quad (58c)$$

where  $Re_H = \frac{\rho u H}{\mu}$  and  $Pr$  is assumed to be 0.7. Joo et

al. [8] also developed predictive correlations for three-layered WBK using the same method as previous work; the equations are given below:

A-direction

$$Nu_{D_h} = 0.3137 Re_{D_h}^{0.785} \quad 2.0 \times 10^3 \leq Re_H \leq 2.0 \times 10^4 \quad (59a)$$

B-direction

$$Nu_{D_h} = 0.4824 Re_{D_h}^{0.751} \quad 2.0 \times 10^3 \leq Re_H \leq 2.0 \times 10^4 \quad (59b)$$

For a given Reynolds number range, the Nusselt number of the A-direction is lower than that of the B-direction. Shen et al. [147] numerically investigated the heat transfer characteristic of single-layered WBK in the Reynolds number range of 3995 to 8710, comparing the Nusselt numbers of WBK and Kagome structures. For similar pressure drop, they found that the overall Nusselt number of Kagome is 26% to 31% higher than that of the WBK, while the Nusselt number of WBK ligaments is 42% higher than that of Kagome.

From the above review, it can be concluded that, with proper design, structured packed beds have potential for heat transfer enhancement. The heat transfer performance of structured packed bed forms should be more widely investigated. In the case of wire-woven structures, there is limited literature investigating the heat transfer performance and few predictive correlations have been developed; more research is therefore needed.

## 6. Application of Porous Structures to Enhance Heat Transfer

Due to their advantageous thermal properties, porous structures can be applied in many fields, such as chemical, aerospace, electronics, and energy engineering, and others. This section will introduce some applications of open-cell foam structures, lattice-frame structures, structured packed beds, and wire-woven structures.

### 6.1 Application of open-cell foam

Open-cell foam structures hold promise for many applications. In particular, there are many ways to use open-cell metal foams to enhance heat transfer in different situations. Many authors have explored the use of heat sinks filled with metal foam for electronic cooling [169, 170], finding that they have better heat transfer properties than the conventional heat sinks. The tube bank heat exchanger is widely used in thermal engineering. To enhance its heat transfer properties, some authors investigated wrapping the exchanger in metal

foam [171, 172]. Odabae et al. [172] found that the heat transfer properties of a tube wrapped with metal foam are an order of magnitude higher than of an empty tube; however, the pressure drop increases. Research has also focused on optimization of heat exchanger design to enhance heat transfer with less pressure drop, for example through partially wrapped tubes [171], and wrapping with gradient metal foam [173]. Another application of metal foam in heat exchangers is using it to fill passages [174, 175]. Lu et al. [175] found that the heat transfer properties of tubes filled with metal foam were forty times higher than that of empty tubes. Partially-filled passages can therefore enhance heat transfer with smaller pressure drop [176–178]. Other novel ways to enhancing heat transfer have also been developed, such as metal foam with coating [179], metal foam heat exchangers for high temperature flow [180], and double tubes filled with metal foam [181]. In addition, with the development of 3D printing, the pore structure of open-cell foam can be designed to improve overall heat transfer performance. Some structures used to model real pore structure of open-cell foam should be considered. And then, a more accurate predictive correlation is possible to develop for the application of open-cell foam.

### 6.2 Application of Lattice-frame structure

Lattice-frame structures can be used in plate-fin heat exchangers for aerospace applications and power engineering, and others, due to the good load-bearing and heat transfer properties. However, there has been little investigation of the heat transfer properties of complete heat transfer devices. Yan et al. [182] used X-type structures for brake discs, investigating related heat transfer properties. X-type structure brake discs showed better heat transfer properties than radial vane brake discs. With further development of manufacturing technologies, compact heat exchangers can be obtained and their heat transfer properties should be investigated.

### 6.3 Application of packed beds and wire-woven structures

Packed beds are widely used for enhancing heat transfer, for example in solar receivers, high temperature gas-cooled nuclear applications [183], and others. Structured packed beds have especially good heat transfer properties, with lower pressure drop. Compared to packed beds, wire-woven structures are more widely used for designing heat exchangers, such as wire-on-tube heat exchangers [32, 184], brake discs [167], and plate-fin exchangers.

The application of porous structures in engineering to enhance heat exchange is still limited, due to ambiguities about heat transfer properties. However, these structures

could contribute to the design of heat transfer devices in future, due to their excellent structural features. More work is therefore needed to determine their heat transfer properties.

## 7. Conclusion

The porosity is considered as one of the most significant morphological characteristics for the performance of force convection heat transfer in the discussed light-weight porous media. For open-cell foam, the pressure drop and heat transfer coefficient are also governed by pore diameter, tortuosity and specific surface area. Note that, the specific surface area and tortuosity are determined by porosity and pore diameter. Therefore, porosity and pore diameter were most commonly taken into consideration. For lattice-frame structure, wire-woven structure and structured packed beds, the morphologic structure is crucial for the determination of porosity and property and thereby playing an important role in the heat transfer.

Currently, there is no general predicting correlation for open-cell foam structure due to the inaccurate determination of morphological characteristic, selection of characteristic length and flow laws, and difficulty in experiments. Besides, the difference in the predictions increases with an increase in velocity; especially, the gap is huge at turbulence regions with high Reynolds numbers. The general predicting correlation is more available for lattice-frame structure, wire-woven structure and structured packed beds due to the controllable structure.

Although there is substantial work on the forced heat transfer in porous structure, more researches should be carried in the following aspect: more accurate determination of the morphological characteristics and selection of a more general characteristic length; development of more accurate prediction correlations at turbulence regions with high Reynolds numbers; further controlled organization of the structure of lattice-frame, structured packed beds, and wire-woven structures.

## Acknowledgement

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