#### **ORIGINAL PAPER**



# **Numerical study on charge transport and electrochemical performance of Gd and Pr co‑doped ceria‑based solid oxide fuel cells free from internal shorting**

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#### **Abstract**

To guide the composition modifcation and operation optimization of ceria-based electrolytes of solid oxide fuel cells (SOFCs) for blocking internal electronic current, a one-dimensional model considering the mixed conductivity of oxygen ions and free electrons in Gd and Pr co-doped ceria-based electrolytes  $Gd_{0.1}Pr_xCe_{0.9-x}O_{1.90}$  (GPDC) was established. The discharge curve, energy efficiency and oxygen partial pressure distribution in ceria-based electrolytes were calculated under diferent Pr doping contents, operating temperatures and electrolyte thicknesses. The results show that the doping of Pr can relieves internal short circuit current and improve the performance of the cells. The internal short circuit current of the cell increases with raising temperature. With increasing electrolyte thickness, peak power density and leakage current density decrease and the maximum overall efficiency increases. Interestingly, the factor of exponential relationship between electronic conductivity and oxygen partial pressure changes with the doping amount of Pr, and the optimal doping amount of Pr is identifed as 0.15 under 700 ℃ due to the relatively small leakage current density and the high power density. Therefore, this work can guide the design and operation of Gd and Pr co-doped ceria-based electrolyte to develop the highly-efficient low temperature SOFC.

Keywords Solid oxide fuel cells (SOFCs) · Ceria-based electrolyte · Electron-blocking effect · Internal short circuit · Oxygen partial pressure distribution · Gd and Pr co-doped

# **Introduction**

The traditional electrolyte used in solid oxide fuel cells (SOFCs) is  $ZrO<sub>2</sub>$  stabilized by  $Y<sub>2</sub>O<sub>3</sub>$  (YSZ). YSZ needs to be operated at a high temperature of  $800^{\circ}C \sim 1000^{\circ}C$  [\[1](#page-7-0)[–4](#page-7-1)].  $CeO<sub>2</sub>$  doped with three valence rare earth metal such as  $Gd^{3+}$  and  $Sm^{3+}$  has high oxygen ion conductivity under

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the relatively low temperatures due to the abundant oxygen vacancies, which has been widely used to decrease the operating temperature of SOFCs [\[5](#page-7-2), [6\]](#page-7-3). The ionic conductivity of ceria is about an order of magnitude greater than that of stabilized zirconia under the same doping conditions. Compared with the ion radius of  $Zr^{4+}$ , the ion radius of  $Ce^{4+}$ is larger, resulting in a more open structure conducive to oxygen ion migration, and therefore ceria-based electrolytes exhibit higher ionic conductivity than zirconia-based elec-trolyte [[7\]](#page-7-4). However, the reduction of  $Ce^{4+}$  to  $Ce^{3+}$  of doped  $CeO<sub>2</sub>$  can occur under the reducing atmosphere at the anode side of SOFCs, leading to the high electronic conductivity and thus the severe internal short-circuit  $[8-12]$  $[8-12]$ .

The design structure of the double-layer electrolyte with an electron-blocking layer has been proposed to reduce the internal electronic current of the cerium-based electrolyte [\[13](#page-7-7), [14](#page-7-8)]. However, the double-layer electrolyte will increase the ohmic resistance of the cell and the preparation technology is relatively complicated. Therefore, element doping in the ceria-based electrolyte material for reducing its electronic conductivity might be the promising method to prevent the internal short-circuit. The literature points out [[15\]](#page-7-9) doping Pr does not induce bulk lattice changes, but leads to more oxygen vacancies. By doping with Pr, the modifed surface property greatly reduced the grain-boundary resistance, leading to an exceptional electrical conductivity. More oxygen vacancies can be introduced into the co-doped structure. The presence of more grain boundaries leads to faster difusion of oxygen ions [[16\]](#page-7-10). Maricle et al. estimated the electronic conductivity by measuring the total conductivity of  $Ce<sub>0.8</sub>Gd<sub>0.2-x</sub>Pr<sub>x</sub>O<sub>1.9</sub>$  at 659–859 °C under low oxygen activity, indicating that the optimal doping of Pr can reduce the conductivity of n-type electrons. However, the literature [[17\]](#page-7-11) pointed out that the excessive Pr relative content will cause the increase of electronic conductivity. There is a close relationship between oxygen vacancies and the ratio of  $Pr^{3+}/Pr^{4+}$  cations. At the low Pr content,  $Pr^{3+}$  oxidation state is maintained after calcination. On the contrary, when the doping content x is larger than 0.04, the oxidation of Pr increases. As the content of Pr in the calcined sample increases, the content of  $Pr<sup>4+</sup>$  increases rapidly. Under high oxygen partial pressure, due to the electroosmotic flow effect of  $Pr^{3+}/Pr^{4+}$  ions in the vicinity of the lattice, the ion mobility number decreases and the electron mobility number increases [\[18](#page-7-12)]. Another literature [\[19](#page-7-13)] pointed out that Gd-rich,  $Ce<sub>0.8</sub>Gd<sub>0.15</sub>Pr<sub>0.15</sub>O<sub>1.9</sub>$  has the best conductivity, indicating Pr-doped GDC can obviously enhance the conductivity of the electrolyte. In addition, Pr-doped GDCs not only possess high electrical conductivity, but also can overcome the disadvantage of high electronic conductivity of GDC and SDC under reducing atmosphere. The n-type electronic conductivity of Pr-doped GDC is smaller than GDC under the reducing atmosphere [\[20](#page-7-14)].

In this work, building a 1D model to study the electrochemical performance of SOFCs using  $Gd_{0,1}Pr_{x}Ce_{0,9-x}O_{1,90}$ (GPDC) as electrolyte. Particularly, the factor change of exponential relationship between electronic conductivity and oxygen partial pressure changes with the doping amount of Pr was frstly considered in this numerical study. The infuences of temperature, the thickness of electrolyte and different doping concentrations on the performance of single cells were analyzed in terms of open circuit voltage (OCV), internal short circuit current, discharge curve, oxygen partial pressure  $(pO<sub>2</sub>)$  and efficiencies.

# **Theoretical model**

Since ceria-based electrolyte is a mixed conductivity of electrons and oxygen ions, as shown in Fig. [1](#page-1-0), both electrons and oxygen ions can be transferred in the electrolyte. Therefore, part of the electrons reach to the cathode



<span id="page-1-0"></span>**Fig. 1** Schematic diagram of charge transport in SOFC with GPDC electrolyte

through the electrolyte instead of external circuit, causing internal short-circuit and resulting in a decrease of cell performance.

Pr exists in the ceria lattice in two valence states  $(Pr<sup>3+</sup>, Pr<sup>4+</sup>)$ . The concentration of  $Pr<sup>4+</sup>$  increases with increasing  $P(O_2)$  and decreasing temperature, while the concentration of oxygen vacancies decreases. Under the low oxygen partial pressure, the co-dopants  $Pr<sup>3+</sup>$  and  $Gd<sup>3+</sup>$ generate oxygen vacancies and minimize the interaction between the oxygen vacancies and metal ions, thereby increasing the ionic conductivity and decreasing the electronic conductivity [[18,](#page-7-12) [21](#page-7-15)].

$$
2\text{Gd}_2\text{O}_3 = 2\text{Gd}'_{Ce} + O_O + V_O^{\bullet}
$$
 (1)

$$
2\text{Pr}'_{Ce} + \frac{1}{2}O_2 + V_O^{\bullet} = 2\text{Pr}^{\times}_{Ce} + O_O^{\times}
$$
 (2)

The chemical expansion increase with the increasing doping content of Pr and the increasing temperature. When Gd and Pr are co-doped, the oxygen vacancies increase with the decreasing oxygen partial pressure, causing the increase of chemical expansion  $[21]$  $[21]$ . The thermal expansion coefficient of GPDC is  $13.2 \times 21.5 \times 10^{-6}$  when the doping amount is less than  $15\%$  [[21\]](#page-7-15). The thermal expansion coefficients of Ni-YSZ anode and LSCF cathode are, respectively,  $13.2 \times 10^{-6}$ and  $13.8 \times 10^{-6}$  [[22\]](#page-7-16). Therefore, the differences of GPDC electrolyte (the doping amount<15%) and the electrodes are relatively small  $(< 7 \times 10^{-6}$  [[23\]](#page-7-17), which would not cause the severe mismatch of thermal expansion coefficients.

The literature  $[24]$  $[24]$  $[24]$  shows that when doped with 6% Pr, the peak power density can reach 305mW cm−2 at 750℃. It shows that a small amount of Pr doping has little efect on the single cell structure and performance. Thus, a lower content of Pr doping in the electrolyte is applicable. Besides, the tight connect of electrolyte doped 2% Pr and electrode have been verifed by experiments in the related literature [\[20](#page-7-14)].

#### **Charge transfer equation in electrolyte**

According to the Nernst-Planck, the oxygen ion fux and electron carrier fux in the electrolyte layer can be calculated by the following formulas  $[25, 26]$  $[25, 26]$  $[25, 26]$ :

$$
\begin{cases}\nJ_{O^{2-}} = -\frac{\sigma_{O^{2-}}}{4F^2} \frac{d\mu_{O^{2-}}}{dx} + \frac{\sigma_{O^{2-}}}{2F} \frac{d\phi}{dx} \\
J_e = -\frac{\sigma_e}{F^2} \frac{d\mu_e}{dx} + \frac{\sigma_{O^{2-}}}{F} \frac{d\phi}{dx}\n\end{cases}
$$
\n(3)

where J is the fux of oxygen ions or charge carriers in the electrolyte layer;  $\mu$ ,  $\sigma$  and  $\phi$  represent the chemical potential, electrical conductivity and electrical potential corresponding to the subscripts.

The operating current density i of SOFC is the sum of the current densities of electrons and oxygen ions, expressed as:

$$
i = F(-2J_{0^{2-}} - J_e)
$$
 (4)

For the specifc derivation process, please refer to Supplementary Information.

## **Cell efficiencies**

In order to better represent the cell's leakage and the utilization of cell energy, the voltage, current and the total efficiency of the cell are proposed here. Using the method of Gödickemeier and Gauckler  $[27, 28]$  $[27, 28]$  $[27, 28]$  to calculate cell efficiencies. The voltage efficiency  $\epsilon_{\rm v}$  can be expressed by the following formula:

$$
\varepsilon_{\rm v} = V_{\rm cell}/E \tag{5}
$$

The current efficiency  $\varepsilon_f$  can be expressed by:

$$
\varepsilon_{\rm f} = i_{\rm ex}/J_{\rm O^{2-}}\tag{6}
$$

where  $i_{ex}$  is the external electronic.

The total efficiency  $\varepsilon$  is calculated by:

$$
\varepsilon = \varepsilon_{\nu} \varepsilon_f \tag{7}
$$

#### **Modeling and Validation**

The mathematical model was built according to the anode support single cell. The model was solved by the simulation software COMSOL MULTIPHYSICS. The conductivity parameters are shown in Table [1](#page-2-0). Some parameters can be determined by simultaneously ftting the model results and experimental data. The numerical results are not afected by mesh parameters, which shows the scientifc nature of grid division.

Figure [2](#page-2-1) shows calculation results and experimental data in the literature [\[29\]](#page-7-23) I-V and I-P curves of cells. It can be seen that the calculated I-V/I-P curve is in good consistent with the experimental results of the single cell, showing the efectiveness of the model.

In this paper, the leakage current characteristics of several electrolytes are mainly studied, as shown in Table [2](#page-2-2).

# **Discussion**

## **Performance comparison of the single cells using pure GDC and Pr‑doped GDC electrolytes**

S. Lubke et al. [[17\]](#page-7-11) found that the electronic conductivity of pure GDC and doped with low concentration Pr obeyed the



<span id="page-2-1"></span>**Fig. 2** Calculation results and experimental data I-V/P curves of cells

<span id="page-2-0"></span>

Temperature/°C	$\sigma$ <sub>i</sub> S/m <sup>-1</sup>	$\sigma_e$ S/m <sup>-1</sup>	Exchange current density $(A \cdot m^{-2})$	
			Anode	Cathode
600	0.8	$5.55 \times 10^{-7}$	300	100
650	1.3	$3.31 \times 10^{-6}$	564	200
700	1.7	$9.1 \times 10^{-6}$	1000	250
750	2.4	$2.735 \times 10^{-5}$	1500	350

<span id="page-2-2"></span>**Table 2** The full name of the abbreviation in the article



 $-1/5$  power of the oxygen partial pressure  $P(O_2)$ , which is diferent from the electronic conductivity of GDC following the typical  $-1/4$  [[30](#page-7-24)] power:

$$
\sigma_e = \sigma_e^0 P_{O_2}^{-\frac{1}{5}} \tag{8}
$$

Figure [3](#page-3-0) shows the performance of the cells at diferent temperatures. With the temperature increases, the internal short circuit current increases, which leads to a decrease in OCV. Compared with pure GDC, the leakage current is much smaller and the open circuit voltage (OCV) is much larger for the GPDC doped with 2 mol% Pr. By comparing Figs. [2](#page-2-1) and [3](#page-3-0), the peak power density (PPD) using the GPDC electrolyte is much larger than that using pure GDC electrolyte. The higher performance of GPDC can be attributed to that Pr doping will reduce the  $Gd_2O_3$  segregation at the grain boundary to increase the ionic conductivity, and it can also effectively inhibit the reduction of  $CeO<sub>2</sub>$  from  $Ce^{4+}$  to  $Ce^{3+}$ . The electronic conductivity increases with temperature, so the leakage current increases and the OCV of the cell decreases.



<span id="page-3-0"></span>**Fig. 3**  $Gd_{0.18}Pr_{0.02}Ce_{0.8}O_{1.90}$  as the electrolyte at different temperatures of (**a**) single cell performance (**b**) open circuit voltage and leakage current

Figure [4](#page-3-1) shows the voltage and total efficiencies of a gadolinium-doped ceria cell under different temperatures. We can also see that the voltage efficiencies decrease linearly as the increase of current density. The change in voltage efficiency is affected by leakage current and polarization loss. It shows that the overall efficiency curve first rises and then drops with current increases. With temperature raises, the short-circuit current increases and the OCV decreases, leading to a decrease in the maximum efficiency. Comparing with the cell using pure GDC, the peak full efficiency of the cell doping with Pr greatly increases from 51.33%, 44.79%, 40.76%, 35.47% to 57.25%, 54.77%, 51.47%, 47.61% under  $600^{\circ}C \sim 750^{\circ}C$ . This is because the presence of Pr increases the ionic conductivity and reduces the electronic conductivity.

## **The performance**  of Gd<sub>0.1</sub>Pr<sub>x</sub>Ce<sub>0.9-x</sub>0<sub>1.90</sub>(x = 0.05,0.08,0.15,0.25,0.30) **cells with diferent Pr doping contents**

The electronic conductivity of GPDC has a more diverse  $P(O_2)$  dependence than that of GDC which follows the typical relationship  $\sigma_e = \sigma_e^0 P_{O_2}^{-\frac{1}{4}}$ . Lightly doped samples (GPDC5, GPDC8, and GPDC15) have n-type electron conductivity slopes close to -1/4 at low  $P(O_2)$ , while heavily doped samples (GPDC25, GPDC30) have a reduced slope, especially at low temperatures. Figure [5](#page-4-0) shows that a more accurate slope according to the literature  $[21]$  $[21]$  $[21]$  is as follows:  $-1/5(GPDC5)$ ,  $-1/5(GPDC8)$ , -3/20(GPDC15), -3/25(GPDC25), -1/20(GPDC30).

The substitution of R for Ce in  $CeO<sub>2</sub>$  fluorite structure produces oxygen vacancy by Eq. [\(9](#page-4-1)) [[31](#page-4-1)]



<span id="page-3-1"></span>Fig. 4 Voltage efficiency and Overall efficiency of GDC and  $Gd_{0.18}Pr_{0.02}Ce_{0.8}O_{1.90}$  as the electrolyte at different temperatures



<span id="page-4-0"></span>**Fig. 5** Logarithm of electronic conductivity of  $Gd_{0.1}Pr_xCe_{0.9x}O_{1.90}(x=0.05,0.08,0.15,0.25,0.30)$  versus  $log_{10}O_2$  $Gd_{0.1}Pr_xCe_{0.9-x}O_{1.90}(x=0.05,0.08,0.15,0.25,0.30)$  versus log pO<sub>2</sub> 700◦C [\[21\]](#page-7-15)

$$
R_2O_3 \stackrel{CeO_2}{\rightarrow} 2R'_{Ce} + 3O_O^{\times} + V_O^{\bullet \bullet}
$$
 (9)

The slope between free electrons and oxygen partial pressure is afected by the following three conditions:(1) The possible interaction between electron and Ce site or O site in RDC; (2)the charge neutrality condition; (3) hopping or no hopping. The doping contents of Pr can infuence the choice of above conditions, therefore the slope of relationship curves between electronic conductivity and oxygen partial pressure is diferent under diferent Pr doping contents.

It has been demonstrated that the GDC electrolyte doped with Pr has better electrochemical performance. The impact of Pr doping content on the leakage current density is studied according to the electronic and ionic conductivity parameters under diferent doping contents, which are listed in Table [3](#page-4-2) [[21](#page-7-15)]. Theoretically, on the premise that the electrolyte phase structure does not change, the more  $Pr<sup>3+</sup>$  ions with lower valence than  $Ce<sup>4+</sup>$  are doped, the more oxygen vacancies will be generated and the conductivity of oxygen ions will be improved. On the other hand, ion  $Pr<sup>3+</sup>$  with a larger doping radius will make the lattice larger.

<span id="page-4-2"></span>**Table 3** conductivities ( $\sigma_i$ ,  $\sigma_e$ ) of GPDC with different Pr doping con-centration at 700 °C (log pO<sub>2</sub>=0) [[19](#page-7-13)]

	$\sigma_i$ S/m <sup>-1</sup>	$\sigma_e$ S/m <sup>-1</sup>	
GPDC5	2.6	$1.5 \times 10^{-5}$	
GPDC8	2.8	$2 \times 10^{-5}$	
GPDC15	3.2	$1.6 \times 10^{-4}$	
GPDC25	3	$3.865 \times 10^{-4}$	
GPDC30	$\mathcal{D}_{\mathcal{A}}$	$2.20 \times 10^{-3}$	



<span id="page-4-3"></span><span id="page-4-1"></span>**Fig. 6**  $Gd_{0.1}Pr_xCe_{0.9-x}O_{1.90}(x=0.05,0.08,0.15,0.25,0.30)$  as electrolyte (**a**) Single cell performance curves (**b**) OCV and internal short circuit current at 700℃

A larger lattice constant makes it easier for oxygen ions to pass through, increasing the conductivity of oxygen ions. However, with the further increase of  $Pr<sup>3+</sup>$  doping amount, the increase of lattice oxygen vacancies results in the lattice distortion, causing a decrease of electrical conductivity [[20,](#page-7-14) [24](#page-7-18)]. So when  $x < 0.15$ , the ion conductivity increases with the increase of doping amount, but when  $x > 0.15$ , the ion conductivity decreases with the increasing doping amount. The literature generally indicates maximal ionic conductivity at doping levels between 10 and 20%. The maximum ionic conductivity is a trade-off between the development of deep vacancy associations due to the increased concentration of oxygen vacancies and electrostatic interactions.

The electronic conductivity in ceria-based electrolyte is related to the electron hopping on the ceria sites. Therefore, substitution of Pr for Ce can decrease the ceria site, thus decreasing the electronic conductivity. Besides, the reduction of  $Pr^{4+}$  to  $Pr^{3+}$  can increase the oxygen vacancy concentration, and the high oxygen vacancy concentration can hinder the electron migration. Pr doping in GDC decreases the electronic conductivity [[21\]](#page-7-15).

From Fig.  $6(a)$  $6(a)$  we can see that when  $0 < x < 0.15$ , the electrochemical performance increases with the increase of the Pr doping concentration. When  $0.15 < x < 0.30$ , as the Pr doping concentration increases, the electrochemical performance decreases. At 700℃, when the doping ratio of Pr is 0.15, the peak power density is 1.02 W cm<sup>-2</sup>. Figure  $6(b)$  $6(b)$  shows that with the increase of Pr doping ratio, the OCV increases, and the internal short circuit current density decreases. Although leakage current is only 40 mA cm−2 when doped with 0.3 Pr, the cell power density decreases rapidly, sacrifcing the electrochemical performance of the cell. The optimal doping amount should be determined by the tradeoff between reducing leakage current and improving peak power density. From Fig. [6](#page-4-3), the optimal doping contents of Pr is 0.15%, and the corresponding leakage current, peak power density and open circuit voltage are, respectively, 195 mA  $cm^{-2}$ , 1.02 W cm−2 and 0.97 V.

Figure [7](#page-5-0) shows that the oxygen partial pressure distribution of diferent Pr-doped electrolyte cells, when the Pr doping amount is large,  $P(O_2)$  in the electrolyte increases, which resulting in a decrease in the electronic conductivity of the electrolyte and a decrease in Internal short circuit current.

Figure  $8$  shows the current efficiency increases with the increasing doping. The maximum voltage efficiency under opening also increases with the increasing Pr doping ratio, which can reach 92.98%. Under the high current density, with the increase of Pr doping ratio, the voltage efficiency curve frst rises and then drops. The maximum overall efficiency increases with the increasing Pr doping ratio, which can reach 60.22% with the doping concentration of 15%. It can be concluded that the optimal Pr doping concentration is 0.15, which leads to the best electrochemical performance.



<span id="page-5-0"></span>**Fig. 7** Oxygen partial pressure distribution of  $Gd_{0.1}Pr_xCe_{0.9-x}O_{1.90}(x=0.05,0.08,0.15,0.25,0.30)$  cells at 700°C



<span id="page-5-1"></span>Fig. 8 Current efficiency Voltage efficiency and Overall efficiency of  $Gd_{0.1}Pr_xCe_{0.9-x}O_{1.90}(x=0.05,0.08,0.15,0.25,0.30)$  cells with different doping at 700℃

# **The infuence of electrolyte thickness on the performance of single cell using GPDC electrolyte**

It has been demonstrated the single cell using GPDC electrolyte has much better electrochemical performance. For the sake of further analyzing the effect of the electrolyte thicknesses on the cell performances and leakage, the electrochemical performances of the single cell were calculated by changing the GPDC electrolyte thicknesses for comparison.

At 700 °C, the I-V/I-P curves of  $Gd_{0.18}Pr_{0.02}Ce_{0.8}O_{1.90}$ cells with diferent thicknesses of electrolyte are shown in Fig.  $9a$ . The electrolyte thicknesses are set to  $25 \mu m$ ,  $30 \mu m$ , 40 μm, 50 μm, and the corresponding maximum peak power is 0.92 W cm<sup>−2</sup>, 0.87 W cm<sup>−2</sup>, 0.79 W cm<sup>−2</sup>, 0.73 W cm<sup>−2</sup>. Figure [9b](#page-6-0) shows as the thickness increases, so does the OCV, and internal short circuit current density drops from 368.2 mA cm−2 to213.9 mA cm−2. When the electrolyte thickness is 50 μm, the OCV is 0.94 V and the leakage current is 213.9 mA cm−2. This is because the thickness of the electrolyte increases, the ohmic impedance of the cell increases, and the polarization resistance of the cell also increases [\[32](#page-7-25)]. Therefore, the appropriate electrolyte thickness should be reasonably selected according to the actual situation.

Figure [10](#page-6-1) shows that under the same current density, the current efficiencies rise as the electrolyte thicknesses increases. Under the low discharge current, the voltage efficiencies and the overall efficiencies both increase with the increase of the electrolyte thickness. However, the change rule with electrolyte thickness is opposite under the high discharge current since the increase of electrolyte thickness improves the ohm resistance.



<span id="page-6-0"></span>**Fig. 9 a** I-V/I-P curves (**b**) OCV and Internal short circuit current density of  $Gd_{0.18}Pr_{0.02}Ce_{0.8}O_{1.90}$  cells with different electrolyte thicknesses at 700℃



<span id="page-6-1"></span>Fig. 10 Current efficiency v Voltage efficiency and overall efficiency of  $Gd_{0.18}Pr_{0.02}Ce_{0.8}O_{1.90}$  cells with different electrolyte thicknesses at 700℃

# **Conclusion**

In this work, by reasonably considering the charge transport of electrons and ions, a model was established to analyze the electrochemical performance of cells using GPDC with diferent doping concentrations as the electrolyte. We can draw the conclusions that:

- (1) It has been demonstrated that the single cell using GPDC has much low leakage current and much higher OCV, PPD and cell efficiency, since the Pr doping in GDC can increase the ionic conductivity and decrease the electronic conductivity.
- (2) The increase of operation temperature can lead to the increase of leakage current and the decrease of OCV and cell overall efficiency. However, oxygen ion conductivity increase with the increasing temperature, thus the peak power density increases.
- (3) The maximum power density and internal short circuit current density of the cells decrease with the increase of electrolyte thickness; the OCV increases with the increasing thicknesses, leading to the rise of maximum overall efficiency. However, due to the increase of ohm resistance, too thick electrolyte will result in a decrease of power density.
- (4) The exponential factor of the exponential relationship between electronic conductivity of GPDC and the oxygen partial pressure increases from -1/4 to -1/20, which cause that the electronic conductivity decreases with the increasing Pr doping concentration. When the temperature is 700℃ and the electrolyte thickness is 50um, the optimal doping amount of Pr is 0.15. In this case, the OCV and PPD can reach 0.97 V and 1.02 W cm<sup>-2</sup>, and the leakage current density is only 195 mA  $cm^{-2}$ .

**Supplementary Information** The online version contains supplementary material available at<https://doi.org/10.1007/s11581-022-04563-x>.

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**Data availability** All data are available in the manuscript.

#### **Declarations**

**Conflict of interest** The authors declare no competing interests.

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