

Sensitivity Enhancement of Surface Plasmon Resonance Biosensor with 2‑D Franckeite Nanosheets

Bhishma Karki¹ · Sandeep Sharma^{2,3,4} · Yadvendra Singh⁵ · Amrindra Pal^{[6](http://orcid.org/0000-0001-7806-2453)}

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Abstract

The sensitivity of a standard surface plasmon resonance (SPR) biosensor in angular interrogation is low. A unique 2-dimensional substantial heterostructure, franckeite/graphene layer, has been deposited over the metal surface to improve the sensitivity; moreover, the sensitivity is limited to a certain extent. A SPR biosensor based on modifed Kretschmann confguration has been investigated, contain bimetallic layers of silver (Ag) and nickel (Ni). A layer of franckeite is sandwich in the metal layer. The proposed configuration has a maximum sensitivity of $352^{\circ}/R$ IU, which is 80.80% higher than the conventional sensor. The franckeite is an air-stable 2-D material and has application in the chemical, biological, and medical felds.

Keywords Surface plasmon resonance · Chemical sensor · Finite element method (FEM) · Sensitivity enhancement

Introduction

Biosensing applications are becoming popular as the sensing capabilities of the biosensors are enhanced due to the rapid advancements in related technology. Among many available biosensors, surface plasmon resonance (SPR)-based sensing stood out to be an outstanding contender offering high sensitivity, label-free detection along with reliable outcomes for biosensing applications (chemical and biological parameters). An SPR biosensor is suitable for the study of the biological macromolecules, and it also has a wide range of applications in biochemical analysis and detection, food safety [[1–](#page-6-0)[3\]](#page-6-1), environmental detection, a biological investigation $[4, 5]$ $[4, 5]$ $[4, 5]$ $[4, 5]$, and gas detection $[6, 7]$ $[6, 7]$ $[6, 7]$ $[6, 7]$.

SPR is an optical excitation of surface plasmon wave (SPW), also referred to as surface plasmon polaritons (SPP)

 \boxtimes Amrindra Pal amrindra.ieee@gmail.com

- ¹ Department of Physics, Tri-Chandra Multiple Campus, Tribhuvan University, Kathmandu 44600, Nepal
- ² OMKARR Tech, New Delhi, India
- ³ iNurture Education Solutions, Karnataka, Bengaluru, India
- ⁴ Department of IT, Ajeenkya DY Patil University, Pune, Maharashtra, India
- 5 Applied Plasmonics & Photonics Lab, Indian Institute of Technology Roorkee, Roorkee, Uttarakhand, India
- ⁶ Department of EECE Deptt, DIT University, Dehradun, Uttarakhand, India

or surface plasmons (SP), at the metal–dielectric interface. The underlying principle of SPR is based on an evanescent wave (EW) and SPs. SP can be seen as an electron cloud wave (or an electromagnetic wave) that moves along the surface of the metal by the contact of the freely oscillating photons and electrons on the surface of metal [[8,](#page-6-6) [9\]](#page-7-0), with an exponentially decaying electric feld in both the metal and dielectric mediums. This movement heavily relies on the dielectric refractive index, thus providing high sensitivity to record changes in the analyte refractive index (RI) of the binding events.

The SPW is the transverse magnetic (TM) polarized wave propagating along the interfacing plane that may be induced by p-polarized light. When a p-polarized electromagnetic (EM) wave enters a dielectric media through a prism and, in turn, a metallic layer, an EW is observed at the interface of the two media, ensuring the absorption of energy from the incident light to excite the SPs at this interface. Essential conditions for SPR to be observed are frstly the exact matching of the surface plasmon wave vector (SPWV) and the evanescent wave vector (EWV) $[10]$ $[10]$. Secondly, the wave is incident at SPR angle or resonance angle. This specifc angle of incidence/wavelength is the angle where minima of the refected light intensity (prism base) are observed due to attenuated total internal refection (ATR), inciting SPs to couple with incident p-polarized EM Wave at the metal surface [[11](#page-7-2)].

There are two types of SPR sensors, namely, prism based [[12](#page-7-3)] and optical fber based [[12\]](#page-7-3). In SPR sensors, the prism-based technique is commonly deployed. Based on the attenuated total refection (ATR) [[13\]](#page-7-4), two geometric confgurations, namely, Kretschmann's–Raether [\[13\]](#page-7-4) and Otto [\[14\]](#page-7-5), are employed for prism coupling.

Because of the ease of practical implementation, Kretschmann's geometry/confguration is preferred for SPR applications $[15–17]$ $[15–17]$ $[15–17]$. This configuration conventionally has a single metal flm-coated at one end of the glass prism or coated with an air gap between a prism and this metal flm, leading to low sensitivity. The objective of the biosensor designer is to increase the momentum of the incoming photon and excite the coupling of the SP to analyte. The analyte attachment to the sensor's surface holds the key for accurate and enhanced performance for the sensors. The SPR is generally controlled by either wavelength [[18,](#page-7-8) [19](#page-7-9)], or angular interrogation [\[12](#page-7-3), [20](#page-7-10)] of the incidence light.

The refectance curve provides sensing performance of the SPR sensor, and it displays refectivity versus angle of incidence. Generally, Au or Ag is the preferred choice of metal $[21]$ $[21]$ $[21]$. Au has a low oxidation coefficient but offers a lower absorption rate for biological molecules [[22\]](#page-7-12), renders reduced biosensor sensitivity. In contrast, Ag provides higher sensitivity, but it is highly susceptible to oxidation [\[14\]](#page-7-5), leading to poor sensitivity in the end. One way to prevent Ag oxidation is to substitute a single layer Ag flm with a bimetallic flm [[23–](#page-7-13)[26](#page-7-14)], and this indeed improves sensors performance by rendering the Ag surface chemically inert [[27\]](#page-7-15). Au produces a larger SPR resonant angle shift on a refection curve, while Ag has a narrower peak, attributed to a higher value of Ag's dielectric constant (real part).

Sensitivity is a key performance indicator for any sensor. Diferent biosensors have been proposed in recent decades [\[28](#page-7-16), [29\]](#page-7-17). With the recent advancement in the technology of 2-D materials, transition metal dichalcogenides (TMDCs) $(MoS₂, WS₂, MoSe₂, WSe₂)$ and graphene are used as biorecognition element (BRE), and they have shown to enhance the performances of SPR sensors. Lin et al. [\[30](#page-7-18)] reported a biosensor using a few layers of gold, molybdenum disulfde $(MoS₂)$, and graphene with a sensitivity maximum of 182^o/ RIU**.** Here gold is used as a metal layer, and it has a lower absorption ability with the biological molecules. Srivastava and Prajapati [[21\]](#page-7-11) designed a biosensor based on blue phosphorene/MoS₂ and achieved the highest sensitivity of 230.66 \degree / RIU. Wu et al. [\[31\]](#page-7-19) proposed a biosensor structure along with a few-layer of black phosphorus and graphene/TMDCs with enhanced sensitivity of 279°/RIU.

In particular, graphene has attractive properties such as tunable electrical and optical characteristics [\[32\]](#page-7-20), ring-type carbon structure, and high surface-to-volume ratio. Thus, the adsorbates can easily interact with this structure, increasing the adsorption suitable for biosensors [[33](#page-7-21), [34\]](#page-7-22). Graphene can be made to be a monolayer or multiple layers via Van der Waal (VDW) force between the layers. VDW heterostructure

[[35\]](#page-7-23)-based sensors exist in both natural and artificial forms. The synthetic materials are made using diferent 2-D materials selectively stacked $[31–36]$ $[31–36]$, and the natural materials are layered minerals from the sulfosalt family [\[37](#page-7-25)[–39](#page-7-26)].

While the sensitivity of the biosensor based on these artificially designed heterostructure (s) can be high, as in those mentioned above, it is not easy to control the lattice orientations. Consequently, undesired atmospheric adsorbates between the layers occur [[40\]](#page-7-27). On the other hand, naturally occurring layered minerals such as Franckeite (member of the sulfosalt family), which is alternating stacks of PbS-like pseudotetragonal (Q) layer and SnSe-like pseudohexagonal (H) layer, are found to possess naturally VDW superlattices [[37–](#page-7-25)[39\]](#page-7-26), and it is free from surface contaminations in contrast to the artifcially designed heterostructure(s).

Franckeite is a 2-dimensional p-type material, and it can be exfoliated into layers mechanically [[41](#page-7-28)]. It has a crystalline structure and is reported to be stable in the air. Franckeite has a narrow energy band gap of less than 0.7 eV; it can be an alternate material for graphene and black phosphorus, which also have a narrow bandgap. The franckeite nanosheet has been found to have great potential in optoelectronic devices [[41,](#page-7-28) [42](#page-7-29)]. Gan et al. [[43](#page-7-30)] have designed a franckeite-based SPR sensor using a layer of Ag and a few layers of graphene. The sensitivity for this is obtained as high as 188°/RIU.

In this work, a bi-metallic structure having a sandwiched franckeite layer between the Ag/Ni layers with a graphenecoated adsorbate interface based on Kretschmann's confguration is proposed. It has been shown to enhance the sensitivity of the biosensor. The work also demonstrates the sensitivity of the sensing layers RI depending upon the number of layers of 2-D materials (franckeite and graphene).

The rest of the article is structured as follows. Biosensor theoretical modeling and its design are demonstrated in "[Theoretical Modeling and Design Analysis](#page-1-0)." "[Results and](#page-2-0) [Discussions](#page-2-0)" presents our modeling results and discussion. "[Conclusion"](#page-6-7) provides the conclusion of this work.

Theoretical Modeling and Design Analysis

Figure [1](#page-2-1) depicts our design of the SPR biosensor in a typical Kretschmann confguration. The TM polarized optical signal of 633 nm is incident at one surface of the BK7 prism, and the refracted optical signal is received at the other end.

The prism is coated with a thin layer of Ag (a single layer of thickness $w_1 = 50$ nm), which in turn is covered by a 2-D franckeite nanosheet (thickness $w_2 = M * 1.8$ nm where *M* is an integer with values 0, 1, 2, etc. *M* represents the number of franckeite layers), followed by a Ni thin flm (single layer of thickness $w_3 = 10$ nm). Ni layer is coated with layer(s) of graphene (thickness $w_4 = N \times 0.34$ nm, where *N* is an integer

Fig. 1 Layered structure of biosensor based on franckeite

with values 0, 1, 2, etc. *N* represents the number of graphene layers). The graphene layer is sandwiched between Ni flm and the sensing layer. The graphene layer improves the macromolecular captivation of the sensor. The BK7 prism is used as a coupling prism; the RI of the prism is given as

$$
n_{pBK7} = \sqrt{1 + \frac{\alpha_1 \lambda^2}{\lambda^2 - \beta_1} + \frac{\alpha_2 \lambda^2}{\lambda^2 - \beta_2} + \frac{\alpha_3 \lambda^2}{\lambda^2 - \beta_3}}
$$
(1)

where λ is the wavelength of the applied optical signal. The values of the constants $\alpha_1, \alpha_2, \alpha_3, \beta_1, \beta_2$ and β_3 are 1.03961212, 0.231792344, 1.01046945, 0.00600069867, 0.0200179144, and 103.560653, respectively [\[44\]](#page-7-31). The RI of the metal layer (Ag) is expressed using the Drude model, $n_{Ag, Ni} = \sqrt{1 - (\lambda^2 \lambda_c)/[\lambda_p^2(\lambda_c + i\lambda)]}$, where $\lambda_c = 17.614 \,\mu\text{m}$ and $\lambda_p = 0.14541 \mu m$ [\[11](#page-7-2), [12,](#page-7-3) [19](#page-7-9), [23\]](#page-7-13). Similarly, the RI for Ni is obtained using the above formula with $\lambda_c = 0.28409 \,\mu\text{m}$ and $\lambda_p = 0.25381 \mu \text{m}$. λ_c and λ_p are the plasma and the collision wavelength for silver and nickel, respectively. The RI (n_f) of franckeite at 1.8-nm thickness is $3.53 + i * 0.39$ in the visible range $[12, 13, 20, 26]$ $[12, 13, 20, 26]$ $[12, 13, 20, 26]$ $[12, 13, 20, 26]$ $[12, 13, 20, 26]$ $[12, 13, 20, 26]$ $[12, 13, 20, 26]$ $[12, 13, 20, 26]$. The RI of graphene is given as $n_G = 3.0 + iC_1 * \lambda/3$ with $C_1 \approx 5.446 \mu \text{m}^{-1}$; λ is the wavelength of the applied optical signal [[20,](#page-7-10) [26\]](#page-7-14). The RI of the sensing layer is taken $n_s = 1.33$ [[12,](#page-7-3) [13\]](#page-7-4).

Detailed numerical analysis by varying thickness of metal layers was carried out and simulated to get minimum

Table 1 Designing parameters for the implemented biosensor

refectance for the geometry so that optimal thicknesses (for maximum sensitivity) of metals including silver and nickel, layers can be found. The sensing performance of the systems is estimated using the Fresnel equations [\[7,](#page-6-5) [20\]](#page-7-10). The refectance is estimated with the formula: [[12,](#page-7-3) [13,](#page-7-4) [20](#page-7-10), [26\]](#page-7-14).

$$
r_{pm_1d_1m_2d_2} = \frac{r_{pm_1} + r_{m_1d_1m_2d_2}e^{2iK_{m_{1x}dm_1}}}{1 + r_{pm_1d_1m_2d_2}e^{2iK_{m_{1x}dm_1}}}
$$
(2)

where

$$
K_{ix} = \left(\left(\frac{2\pi}{\lambda}\right)^2 \varepsilon_i - K_z^2\right)^{1/2}; i = p, m_1 d_1 m_2 d_2
$$

$$
r_{pm} = \frac{(\varepsilon_m K_{px} - \varepsilon_p K_{mx})}{(\varepsilon_m K_{px} - \varepsilon_p K_{mx})}; r_{md} = \frac{(\varepsilon_d K_{mx} - \varepsilon_d K_{dx})}{(\varepsilon_d K_{mx} - \varepsilon_m K_{dx})}
$$

In the subscribes, prism is denoted by *p*, metal by *m*, and dielectric by *d,* respectively.

The dip in the resonance curve can be written as [[7,](#page-6-5) [20\]](#page-7-10)

$$
K_{sp} = \frac{2\pi}{\lambda} n_0 \text{Sin}\theta_{\text{SPR}} = \text{real}\left(\frac{2\pi}{\lambda} \sqrt{\frac{\epsilon_m \epsilon_s}{\epsilon_m + \epsilon_s}}\right)
$$
(3)

 n_0 is the RI of the coupling prism; ϵ_s and ϵ_m are dielectric constants of the sample and metal, respectively; angle of resonance is θ_{SPR} ; and K_{sp} is the propagation constant. The reflectance is defined as $R_P = \left| r_{pm_1d_1m_2d_2} \right|$ $r_{pm_1d_1m_2d_2}$ denotes the reflection coefficient of the incident 2 , where optical signal. Sensitivity is represented as $S_n = \delta \theta_{SPR}/\delta n_s$, where $\delta\theta_{SPR}$ and δn_s represent the change in the resonance angle and the change in RI of the sensing layer respectively. The consolidated design parameters for the implemented biosensors are listed in Table [1](#page-2-2).

Results and Discussions

To achieve high sensitivity, the coupling prism should offer a low refractive index $[44]$ $[44]$ $[44]$. The prism made of BK7 material suits this description [\[45\]](#page-7-32). The prism made from higher refractive index materials provides very sharp

resonance curves compared to those with lower refractive indices. However, the prism made from lower refractive index materials provides values of full width half maximum (FWHM), SPR angle, angular shift, and sensitivity that are larger than higher ones [[44](#page-7-31)]. For higher fgure of merit and a deep SPR curve, the fat end of the prism was coated with 50-nm-thick silver flm. The diferent number of franckeite layers on top of the Ag flm was studied to examine its efect on the structure's sensitivity. The franckeite layer(s) were coated with a 10-nm nickel flm. Ni was chosen for several reasons. It acts as a protective layer to prevent Ag from oxidizing rapidly at room temperature. It also acts as a high RI layer, and it can facilitate enlargement of multi-layer graphene grains by suppressing the nucleation of these multi layers as reported by Murata et al. [[46](#page-7-33)]. Finally, the structure was coated with graphene layer(s) to improve the adsorption rates of the analyte with the biosensor.

Figure [2](#page-3-0) shows the enhanced performance of sensitivity where refectance is plotted against the incident angle for various refractive indices of the sensing layers. Figure [2a](#page-3-0) shows a conventional sensor with no layers of franckeite or graphene in the biosensor, i.e., corresponding to $M = N$ $= 0$. The sharp downfall in the reflectance curve found in the range of specifc angles is attributed to the SPR excitation, describing the absorption of incident light by the sensor due to the generated SPs. The resonance dip has small excursion $\delta\theta_{SPR} = 0.99^\circ$, showing that the change in the RI of the sensing layer (contact layer) due to molecular interaction is very low. The sensitivity obtained was 198° /RIU for this conventional sensor. The traditional sensor in Fig. [2a](#page-3-0) is modifed by adding a single graphene layer (no franckeite layer added that is for $M = 0$ and $N = 1$), retaining all other parameters. An increase in both the resonance offset dip as well as sensitivity was observed with values $\delta\theta_{SPR} = 1.03°$ and 206°/RIU, respectively. These values are higher when compared with the values of the conventional biosensor ($M = N = 0$). The enhanced sensitivity and the increase in resonance curve offset dip in this structure are attributed to the higher adsorption rates due to the large surface area and rich π conjugation structure ofered by graphene, making it the appropriate choice for dielectric top layer SPR sensing applications [\[32,](#page-7-20) [46](#page-7-33)].

Further investigating the impact of single-layer franckeite with no graphene layers added ($M = 1$ and $N = 0$), again an increase in both the resonance offset dip as well as sensitivity was observed with values $\delta \theta_{SPR} = 1.17$ ° and 234° /RIU (Fig. [2](#page-3-0)c), respectively. These values are better than both the cases that are the conventional biosensor as well as the modifed conventional biosensor with single-layer graphene (no layer of franckeite); this enhanced performance is attributed to the narrow bandgap of the franckeite material and better absorption efficiency as compared to graphene (single layer) [[37](#page-7-25)[–42](#page-7-29)].

Another scenario was evaluated for the impact by introducing a single layer of franckeite and a monolayer of graphene in the biosensor ($M = N = 1$). This resulted in significant shifts and a dip in the resonance curve. The resonance

Fig. 2 Plot of refectance vs. incident angle at same RI with *M*=0 and *N*=0 (**a**), *M*=0 and *N*=1 (**b**), *M*=1 and *N*=0 (**c**), and $M=1$ and $N=1$ (**d**)

Fig. 3 Variation in sensitivity of sensor w.r.t. RI

angle was obtained as $\delta\theta_{SPR} = 1.21^{\circ}$, whereas the sensitivity was 242◦ /RIU as depicted in Fig. [2](#page-3-0)d. This comparative study reveals that the resonance angle offset increases with the addition of a single layer of graphene, a single layer of franckeite, compared to the conventional sensor. The best results were obtained by adding a single layer of graphene and a single layer of franckeite.

Upon further addition of layers of frankiete and/or graphene (for values of $M \ge 2$ and or $N \ge 2$), increase in the refectance was observed as depicted in Fig. [4.](#page-4-0) Thereby makes it difficult to measure accurate resonance angle in the dip; this lowers the sensitivity. The above discussions indicate that the sensitivity of the sensor depends on the RI of the sensing layer. A plot of sensitivity versus RI of the sensing layer (as depicted in Fig. [3\)](#page-4-1) helps understand the impact of various combinations of addition of franckeite and graphene layers. The range of the RI was taken from 1.33 to 1.345. From Fig. [3,](#page-4-1) it is also evident that there is a signifcant variation in sensitivity due to the corresponding variation in the RI. The sensitivity varies from 198 to 242°/RIU for $M = N = 0$ to 1, whereas for the case $M = 0$ and $N = 1$,

the sensitivity varies from 206 to 258°/RIU; likewise for $M = 1$ and $N = 0$, the variation from 234 to 335°/RIU was observed. Hence, it can be concluded that the sensitivity increase in the case of the addition of the franckeite sheet is better than that due to the graphene sheet, attributed to the higher optical absorption efficiency of franckeite with respect to graphene. The sensitivity of the biosensor ranges from 242 to 352°/RIU due to the addition of both the single layer of franckeite and single layer of graphene $(M = N = 1)$. This justifes the addition of both franckeite and graphene layers to further enhance sensitivity compared with the conventional biosensor.

The analysis provided above shows that the use of franckeite and graphene sheets supports enhancement in the sensor's sensitivity. The number of layer(s) in the structure of the biosensor 2-D materials is varied to analyze the efect of this change in the sensitivity. Figure [4](#page-4-0)a shows the impact of franckeite nanosheets on the sensitivity of the biosensor. As is evident that with the introduction of several franckeite sheets, refectance increases. Thus, the refectance dip transfers to a larger incident angle and broadening of the SPR curve.

Similarly, the efect of the change of the graphene layer on the sensitivity is given in Fig. [4b](#page-4-0). A similarity in results with franckeite is observed. The refectance dip transfers to a larger incident angle, and the broadening of the SPR curve takes place as the number of graphene layers is increased from 1 through 4. Thus, for analysis purposes, the values of M and N are confined to 0 and 1. For the value *M* and $N=2$ (and higher), it was observed that the shift in refectance curve for various values of refractive indices of sensing layer was either overlapping or one of the refectances was over 0.5 makes. It is challenging to measure accurate resonance angle in the dip for these values and lower sensitivity. Upon further analysis of the results as reported in Fig. [4a](#page-4-0), b, it can be observed that the resonant angle offset is more affected by the increase in the number of franckeite nanosheets than the corresponding increase in the number of graphene layers. Also, it can be further inferred that the collective addition

Fig. 4 a, **b** Change in the refectance w.r.t incident angle: **a** variation in the number of franckeite layers at one graphene layer and **b** variation in the number of graphene layers at one franckeite

Fig. 5 Change in sensitivity w.r.t. to **a** variation in the number of franckeite layers at one graphene layer and **b** variation in the number of graphene layers at one franckeite

from single franckeite nanosheet and single graphene layer to multiple franckeite nanosheets and multiple graphene layers leads to worsening of the outcome as explained earlier.

Optical energy loss is more due to the increase in the number of franckeite layers than due to the corresponding increase in the graphene layer. From Fig. [5](#page-5-0)a, b, it can be clearly seen that the sensitivity of the biosensor frst improves (the case of adding a single layer of graphene and single layer of franckeite nanosheet) and then signifcantly decreases with an increase in the number of layers of graphene and franckeite layers increased either individually or collectively. The imaginary RI part for graphene (non-zero) and amortization in the absorption of SP at the Ni/graphene interface [\[22,](#page-7-12) [47,](#page-7-34) [48](#page-7-35)] causes damped extension of SP field inside the graphene layer resulting in more insufficient sensitivity or detection accuracy or increase in refectance. This can be visibly seen in the breadth of the SPR curve.

The analysis was carried out for 633-nm wavelength light source. The analysis aptly supports for optical signals at other wavelengths. Table [2](#page-5-1) depicts the comparative analysis with the existing work reported in the literature, clearly indicating that the proposed structure offers by far the best sensitivity to the compared structures. The proposed biosensor is highly sensitive for chemical, medical diagnosis, and biological mass detection.

The entire analysis was carried out with the help of the fnite element method (FEM) using COMSOL Multiphysics and MATLAB software. In this paper, the electric feld enhancement between diferent layers has been analyzed, and the thickness of the bimetallic (Ag/Ni) layer was also optimized. The electric feld analysis provides the confnement of the feld at the metal–dielectric interface. It can be noted that the feld is well confned at this interface. The coupling of the wave vector at the metal–dielectric interface shows the intensity of the electric feld [\[9](#page-7-0)]. Figure [6](#page-6-8) depicts the density distribution of the electric feld X-component with respect to the distance normal to the prism interface for a diferent number of graphene layers. This electric feld distribution verifes the efect of increasing graphene layers on SP feld distribution at the graphene-sensing layer interface. As the increasing the number of graphene layers, the sensitivity will decrease. Mathematically, the feld intensity enhancement factor (FIEF) is equal to the ratio of the square of the feld at graphene–sensing layer interface to the incoming intensity at the prism–metal interface for p-polarized light [\[7](#page-6-5)]. Therefore, the FIEF at graphene–sensing layer interface can be obtained by relating the electric feld to magnetic feld as per Eq. ([4\)](#page-6-9) [[27\]](#page-7-15).

Table 2 Comparative of the earlier reporte

Fig. 6 Electric feld distribution inside the biosensor (normalized feld)

$$
\left| \frac{E_{\parallel} \left(\frac{N}{N-1} \right)}{E_{\parallel} \left(\frac{1}{2} \right)} \right|^2 = \frac{\varepsilon_1}{\varepsilon_N} \left| \frac{H_{y||} \left(\frac{N}{N-1} \right)}{H_{y||} \left(\frac{1}{2} \right)} \right|^2 \tag{4}
$$

Conclusion

An SPR biosensor based on the heterostructure of franckeite nanosheet is proposed for the improvement of sensitivity. In the designed structure, franckeite nanosheet is sandwiched between two metal layers of Ag and Ni with the thickness of 50 and 10 nm, respectively. The investigation carried out in this work reveals that the introduction of franckeite layer(s) and graphene layer(s) in the SPR biosensor in the Kretschmann confguration enhances the sensitivity of the biosensor. Upon further increasing the number of layers from 1 to 2 of graphene and/or franckeite, the 2-D materials tend to exhibit more of metallic nature than semiconducting; this was concluded based upon the enhanced refection $(Fig. 4)$ $(Fig. 4)$ $(Fig. 4)$, thereby broadening the curve and making it difficult to measure accurate resonance angle in the dip for these values. It is also observed that the thickness of the franckeite and graphene layer afects the sensitivity of the biosensor. The sensitivity of the biosensor enhances with the introduction of a single layer of franckeite and a single layer of graphene for individually exclusive as well as collective cases as compared to a conventional sensor. The absorption efficiency of the franckeite nanosheet is more than the graphene layer for separately exclusive single-layer cases. However, using both a single layer of franckeite and graphene layer further improves the sensitivity of the individually exclusive case. The maximum sensitivity of 352◦ /RIU was observed for the biosensor at a single layer of franckeite and a single graphene layer.

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Author Contribution SS formulated the problem statement wherein giving the theoretical background for SPR biosensor. He also helped in drafting the manuscript. YS provided the theoretical background to biosensing and importance of Optical Biosensing. He also helped in reviewing the manuscript. AP provided statistical analysis for the results. He provided the theoretical background to SPR biosensors. He also helped in reviewing and formatting the manuscript. BK worked towards the revision of the complete manuscript, formatting and fnalizing the comments of the reviewers.

Declarations

Ethics Approval Not applicable. The work presented in this manuscript is mathematical modeling only for the proposed biosensor. No experiment was performed on the human body and/or living organism/animal. So, an ethical approval from an ethical committee is not required.

Consent to Participate All the authors are willing to participate in the work presented in this manuscript. On the behalf of all authors, communicating author is authorized to give their consent.

Consent for Publication All the authors have given their consent to publish this work.

Conflict of Interest The authors declare no competing interests.

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