# **A Tunable Slow Light Device with Multiple Channels Based on Plasmon‑Induced Transparency**

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#### **Abstract**

Slow light devices with bufering capability play a critical role in all-optical signal processing. In this paper, multiple slow light phenomena are implemented based on plasmon-induced transparency (PIT) in our device. The device mainly consists of dual tooth cavities coupled with stub resonators, respectively. Temporal coupled-mode theory model illustrates that the triple PIT phenomena can be achieved based on diferent formation mechanisms. The simulation results calculated by the fnite-diference time-domain method reveal that signifcant slow light response occurs at two wavelength regions. In addition, the parameters of structure have an important infuence on PIT response and slow light characteristics. Moreover, the separate manipulation of wavelength, transmission and group index at transparency peak can be achieved in diferent slow light channels by adjusting the structural parameters. This plasmonic device is of great signifcance for the design of optical networks on chips.

**Keywords** Slow light · Surface plasmon polaritons · Resonators · Plasmon-induced transparency · Transmission characteristics

## **Introduction**

Electromagnetically induced transparency (EIT) is a quantum interference phenomenon between two diferent excitation pathways in a three-level atomic system, which can generate a narrow transparency window  $[1, 2]$  $[1, 2]$  $[1, 2]$ . It is generally accompanied with sharp dispersion near the transparency window [[3](#page-6-2)]. This attractive phenomenon has various potential applications in the areas of optical data storage, ultrafast switching and slow light devices [[4–](#page-6-3)[6\]](#page-6-4). In particular, slow light devices can slow down the propagation speed of optical signals, temporarily store blocked optical signals and resolve

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resource conficts in signals transmission [[7,](#page-6-5) [8](#page-6-6)]. Moreover, the bufering is also required for synchronization, optical time-division multiplexing and optical beamforming [[9](#page-6-7)]. Therefore, slow light propagation has been extensively studied [\[10](#page-6-8), [11\]](#page-6-9). However, practical implementation of EIT is limited by strict conditions, such as low-temperature environments and stable gas lasers [\[12](#page-6-10)[–14](#page-6-11)]. Fortunately, plasmon-induced transparency (PIT), an analogous EIT efect, has attracted the attention of researchers [\[15](#page-6-12)[–17\]](#page-6-13). Compared with EIT, the PIT can remove rigorous implementation conditions. Furthermore, since surface plasmon polaritons (SPPs), a special kind of electromagnetic wave, have the capability of breaking classical difraction limit, the PIT can be implemented in nanoscale structures [[18–](#page-7-0)[21](#page-7-1)].

Therefore, many slow light devices based on the PIT have been proposed to achieve slow light phenomena [[22–](#page-7-2)[25](#page-7-3)]. Among these devices of implementing PIT and slow light efects, for the metal-insulator-metal (MIM) waveguides having the advantages of ease fabrication, strong confnement to SPPs and acceptable propagation length, the MIM waveguides are widely employed [\[26](#page-7-4)[–28](#page-7-5)]. For example, tunable slow light was analyzed in dual stubs coupled with MIM waveguide [[2](#page-6-1)]. Slow light response was achieved in dualring resonator-coupled MIM waveguide system [\[22](#page-7-2)]. A stub MIM waveguide coupled with a nanodisk resonator for PIT and slow-light effect was proposed [[23](#page-7-6)]. Although these plasmonic devices have great performance, they can only be used to implement the PIT and slow light efect at a single wavelength. In order to solve the above problem, many plasmonic structures that can implement PIT response and slow light effect with multiple channels are investigated, such as dual coupled stub-nanodisks system [[5\]](#page-6-14), MIM stub coupled with two Fabry–Perots structure [[24\]](#page-7-7) and aperturecoupled cascade resonators [[25\]](#page-7-3). These structures proposed further improve the integration of the device. However, how to individually manipulate the slow light characteristics at one of the channels without afecting the other channels, which is urgently needed in practical applications, is not discussed in detail.

To meet these demands, a slow light device mainly consisting of two tooth cavities coupled with stub resonators is proposed in this paper. The triple PIT responses are achieved at diferent wavelengths in the proposed device. The physical mechanisms of their formation are analyzed in detail using temporal coupled-mode theory (CMT) model. The simulation results calculated by fnite-diference timedomain (FDTD) method reveal that signifcant slow light characteristics occurs at two of the wavelengths. Depending on the cause of the formation, we illustrate the methods of manipulating wavelength, transmission and group index at transparency peak for diferent slow light areas separately. The device proposed will pave the way for buffer technique in highly integrated optical systems.

#### **Structure Model and Theoretical Analysis**

A two-dimensional schematic diagram of the proposed plasmonic structure which mainly consists of dual tooth cavities coupled with stub resonators separately is shown in Fig. [1.](#page-1-0) The geometric parameters of the structure  $l_{11}$ ,  $l_{12}$ ,  $l_{s1}$  and  $l_{s2}$  are the lengths of the tooth<sub>1</sub>, tooth<sub>2</sub>, stub<sub>1</sub> and  $sub<sub>2</sub>$  resonators, respectively. The widths of waveguide, tooth cavities and stub resonators are denoted as *w*. Parameter *D* means the core-core separation between two tooth resonators,  $d_1$  ( $d_2$ ) represents the coupling distance between tooth<sub>1</sub> (tooth<sub>2</sub>) cavity and stub<sub>1</sub> (stub<sub>2</sub>) resonator. The refractive index of dielectric in waveguide and resonators is *n*. The background metal is supposed to be silver whose frequency-dependent relative permittivity can be characterized by the well-known Drude model [\[29](#page-7-8)]:

$$
\varepsilon_m(\omega) = \varepsilon_\infty - \omega_p^2 / [\omega(\omega + j\gamma)] \tag{1}
$$

where  $\epsilon_{\infty} = 3.7$ ,  $\omega_p = 9.1$  eV and  $\gamma = 0.018$  eV are the dielectric constant of the infnite frequency, the bulk plasma



<span id="page-1-0"></span>**Fig. 1** Schematic diagram of the proposed plasmonic slow light device

frequency and the electron collision frequency, respectively. (Drude model with these parameter values can well describe the permittivity at infrared frequencies [\[30\]](#page-7-9).) The angular frequency of the incident wave is denoted by  $\omega$ . In this model, since the width of the plasmonic waveguide is much smaller than the wavelength of the incident light, only the  $TM_0$  waveguide mode can propagate and dispersion relation for  $TM_0$  mode in the MIM waveguide can be obtained by the following equations $[31]$  $[31]$ :

$$
(\varepsilon_m k_d)tanh(\frac{wk_d}{2}) + \varepsilon_d k_m = 0
$$
\n(2)

$$
k_{d,m} = \sqrt{\beta^2 - \epsilon_{d,m} k_0^2}
$$
 (3)

where  $\varepsilon_d$ ,  $\varepsilon_m$ ,  $k_d$ ,  $k_m$ , respectively, represent the permittivities and propagation constants of the dielectric and metal. The wave vector  $\beta$  in the waveguide can be expressed as  $\beta =$  $k_0$   $n_{\text{eff}}$ , in which  $k_0 = 2\pi/\lambda$  stands for the wave vector in vacuum and  $n_{\text{eff}}$  is the effective refractive index in plasmonic waveguide.

When the incident light is injected, the SPPs are formed on the metallic surfaces and propagate along bus waveguide. When resonance condition is satisfied, SPPs can be coupled directly to the tooth cavities from bus waveguide and coupled indirectly into the stub resonators through the tooth cavities. The resonance condition of tooth<sub>i</sub> cavity and stub<sub>i</sub> resonator  $(i = 1, 2)$  can be, respectively, described as  $[32, 33]$  $[32, 33]$  $[32, 33]$  $[32, 33]$ :

$$
2Re(N_{\text{eff}})l_{\text{ti}}\frac{2\pi}{\lambda_{\text{tim}}} + \Delta\phi_{\text{ti}} = (2m+1)\pi
$$
\n(4)

$$
2Re(N_{\text{eff}})l_{\text{si}}\frac{2\pi}{\lambda_{\text{sin}}} + \Delta\phi_{\text{si}} = 2n\pi
$$
\n(5)

where  $Re(N<sub>eff</sub>)$  means the real part of the effective refractive index in the tooth and stub cavities,  $\lambda_{\text{tim}}$  and  $\lambda_{\text{sin}}$  are resonance wavelengths of tooth<sub>i</sub> cavity and stub<sub>i</sub> resonator, *m* is a non-negative integer and *n* is a positive integer. The additional phase shifts  $\Delta \phi_{ti}$  and  $\Delta \phi_{si}$  are caused by reflection on the interface of dielectric and metal in the tooth, cavity and stub<sub>i</sub> resonator, respectively.

Transmission characteristics of the structure can be investigated according to the CMT model. As shown in Fig. [1,](#page-1-0)  $t_1$ ,  $r_1$ ,  $t_2$  and  $r_2$  represent the transmission and reflection coefficients of the tooth<sub>1</sub> and tooth<sub>2</sub>. For obtaining the transmission coefficients  $t_i$  and reflection coefficients  $r_i$  of the device, we frst analyze the transmission characteristics of a single tooth cavity coupled with stub resonator. Figure [2](#page-2-0) illustrates the cross section schematic diagram of single tooth cavity coupled with stub resonator.

The temporal evolution of the normalized amplitude  $a_i$  of the tooth<sub>i</sub> resonator can be written as [\[34](#page-7-13)]:

$$
\frac{da_i}{dt} = (j\omega_i - k_{oi} - k_{wi} - k_{si})a_i + e^{j\varphi_{wi}}\sqrt{k_{wi}}(S^i_{+in} + S^i_{-in}) + e^{j\varphi_{si}}\sqrt{2k_{si}}S^i_{+si}
$$
\n(6)

where  $\omega_i$  means the resonance frequency of tooth<sub>i</sub> resonator,  $k_{oi}$ ,  $k_{wi}$  and  $k_{si}$  stand for decay rate due to internal loss in the tooth $<sub>i</sub>$ , the decay rate induced by the energy escape into</sub>



<span id="page-2-0"></span>**Fig. 2** Schematic diagram of single tooth cavity coupled with stub resonator

<span id="page-2-4"></span><span id="page-2-3"></span>the bus waveguide and  $\text{stab}_i$  resonator, respectively. The phases of the coupling coefficients are denoted by  $\varphi_{wi}$  and  $\varphi_{si}$ . As shown in Fig. [2,](#page-2-0)  $S^i_{\pm in}$  represent the amplitudes of the inputting waves in the MIM waveguide, subscript  $\pm$  mean two propagating directions of waveguide modes. In addition, the amplitudes  $S^i_{\pm si}$  of inputting and outgoing waves in the  $sub<sub>i</sub>$  resonator should satisfy a steady-state relation:

$$
S_{-si}^{i} = -S_{+si}^{i} + e^{-j\varphi_{si}} \sqrt{2k_{si}} a_{i}
$$
 (7)

$$
S_{+si}^i = \delta_i e^{j\phi_i} S_{-si}^i \tag{8}
$$

where  $\delta_i$  and  $\phi_i = 2l_{si}\omega Re(N_{eff})/c + \theta_i$  represent the amplitude attenuation and the phase diference between the incoming and outgoing waves of the stub<sub>i</sub> resonator,  $\theta_i$  means the additional phase shift in the stub<sub>i</sub> resonator. In the linear system, the field everywhere oscillates as  $e^{j\omega_i t}$  and  $d\alpha_i/dt = j\omega_i a_i$ . Since the light is only inputted into bus waveguide from the left port  $(S<sup>i</sup>_{-in} = 0)$ , according to the above equations, amplitude  $a<sub>i</sub>$  of the stub<sub>i</sub> resonator is derived as:

$$
a_i = \frac{e^{j\varphi_{wi}}\sqrt{k_{wi}}S^i_{+in}}{j(\omega_i - \omega) + k_{oi} + k_{wi} + k_{si} - \frac{2k_{si}\delta_i e^{i\phi_i}}{1 + \delta_i e^{i\phi_i}}}
$$
(9)

Based on energy conservation, the amplitudes  $S^i_{\text{1}}$  of the outgoing waves can be expressed as:

$$
S_{-out}^i = S_{-in}^i - e^{-j\varphi_{wi}} \sqrt{k_{wi}} a_i
$$
 (10)

$$
S_{+out}^i = S_{+in}^i - e^{-j\varphi_{wi}} \sqrt{k_{wi}} a_i
$$
 (11)

According to the above equations, the transmission  $T_i$  of the single tooth cavity coupled with stub resonator structure can be deduced as:

<span id="page-2-1"></span>
$$
T_{i} = \left| \frac{S_{+out}^{i}}{S_{+in}^{i}} \right|^{2} = \left| \frac{j(\omega_{i} - \omega) + k_{oi} + k_{si} \frac{1 - \delta_{i} e^{j\phi_{i}}}{1 + \delta_{i} e^{j\phi_{i}}}}{j(\omega_{i} - \omega) + k_{oi} + k_{wi} + k_{si} \frac{1 - \delta_{i} e^{j\phi_{i}}}{1 + \delta_{i} e^{j\phi_{i}}}} \right|^{2}
$$
(12)

Obviously, as coupling distance  $d_i$  increases,  $k_{si}$  will gradually decrease. When tooth<sub>i</sub> cavity and stub<sub>i</sub> resonator are no longer interaction  $(k_{si} = 0)$ , equation ([12\)](#page-2-1) is modified as:

<span id="page-2-2"></span>
$$
T_s = \left| \frac{j(\omega_i - \omega) + k_{oi}}{j(\omega_i - \omega) + k_{oi} + k_{wi}} \right|^2
$$
\n(13)

When  $\omega = \omega_i$ , transmission  $T_s$  approximately equals 0 under the condition of  $k_{oi} \ll k_{wi}$ , which is consistent with the transmission of the band-stop flter based on SPPs. By comparing equation  $(12)$  $(12)$  and  $(13)$ , it can be seen that due to the interaction between tooth, cavity and stub<sub>i</sub> resonator, the EIT-like response occurs, which means that a recess is generated at the original absorption peak and a transparency window is formed. Moreover, based on the above analyses, we can obtain the transmission and reflection coefficients of the single tooth<sub>i</sub> cavity coupled with stub<sub>i</sub> resonator as follows:

$$
t_{i} = \frac{j(\omega_{i} - \omega) + k_{oi} + k_{si} \frac{1 - \delta_{i}e^{i\phi_{i}}}{1 + \delta_{i}e^{i\phi_{i}}}}{j(\omega_{i} - \omega) + k_{oi} + k_{wi} + k_{si} \frac{1 - \delta_{i}e^{i\phi_{i}}}{1 + \delta_{i}e^{i\phi_{i}}}}
$$
(14)

$$
r_{i} = \frac{k_{wi}}{j(\omega_{i} - \omega) + k_{oi} + k_{wi} + k_{si}\frac{1 - \delta_{i}e^{j\phi_{i}}}{1 + \delta_{i}e^{j\phi_{i}}}}
$$
(15)

Consequently, feedback and transmitted waves of the ith tooth cavity can be expressed as following matrix:

$$
\begin{bmatrix} S^{i}_{-in} \\ S^{i}_{+out} \end{bmatrix} = \begin{bmatrix} -\frac{r_{i}}{t_{i}} & \frac{1}{t_{i}} \\ 1 + \frac{r_{i}}{t_{i}} & \frac{r_{i}}{t_{i}} \end{bmatrix} \begin{bmatrix} S^{i}_{+in} \\ S^{i}_{-out} \end{bmatrix}
$$
 (16)

According to the above equation, the feedback and transmitted waves of the proposed device can be obtained as:

$$
\begin{bmatrix} S_{-in} \\ S_{+out} \end{bmatrix} = \begin{bmatrix} -\frac{r_2}{t_2} & \frac{1}{t_2} \\ 1 + \frac{r_2}{t_2} & \frac{r_2}{t_2} \end{bmatrix} \begin{bmatrix} 0 & e^{j\theta'} \\ e^{-j\theta'} & 0 \end{bmatrix} \begin{bmatrix} -\frac{r_1}{t_1} & \frac{1}{t_1} \\ 1 + \frac{r_1}{t_1} & \frac{r_1}{t_1} \end{bmatrix} \begin{bmatrix} S_{+in} \\ S_{-out} \end{bmatrix}
$$
(17)

where  $\theta' = \omega Re(n_{\text{eff}})D/c$  is the phase difference between the 1st and 2nd tooth cavities. When the incident light is launched only from the left port in device  $(S_{-in} = 0)$ , the transmission efficiency  $T$  at the output port can be derived as:

$$
T = \left| \frac{S_{+out}}{S_{+in}} \right|^2 = \left| \frac{t_1 t_2}{1 - r_1 r_2 e^{j2\theta'}} \right|^2 \tag{18}
$$

When the separation *D* is set to 0, the smallest device size and the maximum transmission can be obtained. The maximum transmission can be written as:

$$
T_{max} = \left| \frac{S_{+out}}{S_{+in}} \right|^2 = \left| \frac{t_1 t_2}{1 - r_1 r_2} \right|^2 \tag{19}
$$

According to the above analyses, we know that transmission characteristics of proposed device are not only related to interference between radiative (directly coupled to waveguide) resonators and subradiant (indirectly coupled to waveguide) resonators but also include phase coupling mechanism. In addition, from the previous derivation, working wavelengths can be selected by changing the lengths of tooth and stub cavities as shown in equation  $(4)$  $(4)$  and  $(5)$  $(5)$  $(5)$ . Transmission of device can be manipulated by adjusting

the coupling distance  $d_i$  since the coupling distances  $d_i$ are related to the transmission coefficients  $t_i$  and reflection coefficients  $r_i$  as illustrated in equation ([12](#page-2-1)) and [\(13](#page-2-2)).

#### **Results and Discussions**

#### **Transmission Characteristics**

We take 2-D FDTD method to further investigate the transmission characteristics of the device. The mode source is introduced to excite fundamental TM mode of the waveguide and perfectly matched layer (PML) is utilized as boundary conditions. The spatial steps and temporal step are set as  $\Delta x = \Delta y = 4$  nm and  $\Delta t = \Delta x/1.43c$ . First of all, the parameters of structure are set as  $l_{11} = 120$  nm,  $l_{s1} = 260$  nm,  $l_{12} = 200$  nm,  $l_{12} = 420$  nm,  $d_1 = 25$  nm and  $d_2 = 20$  nm. In order to fx the characteristics of guided modes, the widths of waveguide and resonators are set as a constant (50 nm) in this paper. The dielectric embedded in the waveguide and resonators is regarded as air. Figure [3a](#page-4-0) shows the transmission spectra of the device calculated by the theory and simulation. As drawn in Fig. [3](#page-4-0)a, triple PIT windows can be observed and central wavelengths, respectively, are located at  $\lambda_B = 855.9$ nm,  $\lambda_D$  = 1114.5 nm and  $\lambda_F$  = 1314.3 nm. The transmission efficiencies of transparency peak reach 50%, 90% and 42%, respectively, between the four resonance dips at  $\lambda_A = 819.1$ nm,  $\lambda_C = 897.6$  nm,  $\lambda_E = 1260.6$  nm and  $\lambda_G = 1364.9$  nm, which are typical representation of PIT.

The field distributions of  $H<sub>Z</sub>$  at the transmission peaks and resonance dips represented by A, B, C, D, E, F and G are sketched in Figs. [3b](#page-4-0)-h. According to the previous theoretical analysis and feld distributions, two transparency windows are formed by interaction between tooth<sub>i</sub> cavity and stub<sub>i</sub> resonator: transparency window with a central wavelength at 855.9 nm ( $\text{PIT}_1$  window) and transparency window with a central wavelength at 1314.3 nm ( $PIT_2$  window). The formation of transparency window with a central wavelength at 1114.5 nm  $(PIT<sub>3</sub> window)$  originates from the phase interference between the two tooth cavities. Moreover,  $\text{PIT}_1(\text{PIT}_2)$  is mainly formed by the interaction of tooth<sub>1</sub> (tooth<sub>2</sub>) cavity and stub<sub>1</sub> (stub<sub>2</sub>) resonator. Therefore, the transmission characteristics of  $\text{PIT}_1$ window or  $\text{PIT}_2$  window can be individually manipulated by adjusting the structural parameters.

#### **Slow Light Effect**

The results calculated by FDTD method reveal that phase shift exhibits a sharp dithering at  $\text{PIT}_1$  and  $\text{PIT}_2$  windows, which means that obvious slow light phenomenon appeared at the two transparency windows. The group index  $n<sub>g</sub>$  of the device afects bufering time of signal, and physical signifcance of group index not only includes the meaning



<span id="page-4-0"></span>**Fig. 3 (a)** Transmission spectra at output port of proposed device calculated by the CMT and FDTD methods. Filed distributions of  $H<sub>z</sub>$  in the proposed device with the incident light wavelength of **(b)** 819.1

of refractive index but also refects the dispersion properties. Therefore, the slow light characteristic can be expressed by the group index, which is denoted by following equation:

$$
n_g = \frac{c}{v_g} = \frac{c}{L}\tau_g = \frac{c}{L}\frac{d\psi(\omega)}{d\omega}
$$
(20)

where  $v_g$ ,  $\tau_g$  and *L* are group velocity, optical delay time and the length of the plasmonic structure, respectively. The transmission phase shift  $\psi(\omega)$  is a function of angular frequency  $\omega$ , which can be obtained by  $\psi(\omega) = \text{angular}$  $(S_{+out}/S_{+in})$ .

We numerically investigated the slow light behavior of the device with the length *L* is set to 500 nm. Figure [4](#page-4-1)a shows

nm, **(c)** 855.9 nm, **(d)** 897.6 nm, **(e)** 1114.5 nm, **(f)** 1260.6 nm, **(g)** 1314.3 nm and **(h)** 1364.9 nm

<span id="page-4-2"></span>the transmission phase shift at  $\text{PIT}_1$  window. The phase jitter at  $PIT_1$  window results in delay time at  $PIT_1$  window and the delay time of peak B reaches maximum value 0.06 ps, as depicted in Fig. [4](#page-4-1)b. Based on equation [\(20\)](#page-4-2), the group index at  $PIT_1$  window is plotted, as shown in Fig. [4](#page-4-1)c. The strong dispersion around the transparency window leads to high group indices and maximum group index at peak of  $PIT_1$  window is over 34. Similarly, Figs. [4d](#page-4-1)-f illustrate the phase shift, delay time and group index at  $PIT_2$  window. The results show that the maximal group delay time and group index reach 0.074 ps and 44 at peak of  $\text{PIT}_2$  window, respectively. Therefore, diferent slow light areas are achieved at commonly used wavebands.



<span id="page-4-1"></span>**Fig. 4 (a)** Transmission phase shift, **(b)** delay time and **(c)** group index at the  $\text{PIT}_1$  window. **(d)** Transmission phase shift, **(e)** delay time and **(f)** group index at the  $PIT_2$  window

#### **Influence of Structural Parameters**

As we have analyzed in the previous theory, the controllability of the transmission characteristics can be achieved by adjusting the lengths of resonators and coupling distances, for example, selected operating wavelengths and variable transmissions. For verifying the previous analyses, sweeps of the numerical parameters are performed. Above all, the impacts of the length  $l_{t1}$  and length  $l_{s1}$  on the transmission characteristics are analyzed. The length  $l_{t1}$  is taken from 110 nm to 130 nm with an interval of 5 nm. In order to ensure the detuning state of the resonant wavelength between tooth<sub>1</sub> and stub<sub>1</sub> resonator remains invariable, the length  $l_{s1}$  satisfies the formula  $l_{s1} = 2l_{t1} + a$ . The parameter *a* is set to 20 nm, and other parameters are fixed to  $l_{12} = 200$ nm,  $l_{s2} = 420$  nm,  $d_1 = 25$  nm and  $d_2 = 20$  nm. As the length  $l_{t1}$  and length  $l_{s1}$  increase, the variation of transparency peak wavelengths at  $PIT_1$  and  $PIT_2$  windows is plotted in Fig. [5](#page-5-0)a. It is noteworthy that the central wavelength of  $\text{PIT}_1$  window exhibits a red-shift with the increase of length  $l_{11}$  and length  $l<sub>s1</sub>$ , which is basically a linear relationship. Meanwhile, the resonance wavelength of  $PIT_2$  is barely changed. So, we can manipulate the central wavelength of  $\text{PIT}_1$  window without affecting PIT<sub>2</sub> by changing the length  $l_{11}$  and length  $l_{s1}$ .

Then, we investigate the influence of the length  $l_{12}$  and length  $l_{s2}$  on the transmission characteristics. Length  $l_{12}$ increases from 190 nm to 210 nm with the step size of 5 nm. The length  $l_{s2}$  is expressed as  $l_{s2} = 2l_{t2} + a$  and the other parameters remain unchanged. Figure [5](#page-5-0)b illustrates the variation of central wavelengths at  $PIT_1$  and  $PIT_2$  windows. As the Length  $l_{12}$  and Length  $l_{s2}$  increase, central wavelength of  $PIT_2$  window exhibits red-shift while resonance wavelength of  $PIT_1$  has almost no movement. Therefore, by adjusting the length  $l_{12}$  and length  $l_{s2}$ , the transparency peak wavelength of  $PIT_2$  can be individually manipulated.



As we all know, transmission and group index are important indicators for a slow light device. Next, we explore the effects of coupling distance  $d_1$  on the transmission and group index. The coupling distance  $d_1$  is varied from 10 nm to 35 nm in steps of 5 nm whereas other parameters are kept fxed. Figure [6](#page-5-1)a depicts the relationship between transmission of transparency peak at  $PIT_1$  and coupling distance  $d_1$ . As the coupling distance  $d_1$  increases, the transmission at transparency peak of  $PIT_1$  gradually decreases. However, the group index at transparency peak of  $PIT<sub>1</sub>$  gradually increases, as drawn in Fig. [6b](#page-5-1). There is a trade-off problem between the group index and the transmission through calculation. In order to achieve appropriate transmission and higher group index at the same time, the coupling distance  $d_1$  is set to 25 nm in this paper. In addition, it can be observed from Figs. [6a](#page-5-1), b that the transmission and the group index at central wavelength of  $PIT_2$  window are hardly affected when coupling distance  $d_1$  increases. This provides a method of manipulating the transmission and group index of central wavelength at  $PIT_1$  window without affecting the slow light characteristics of  $PIT_2$  window.

Finally, the relationship between the coupling distance  $d_2$ and slow light characteristics are researched. The coupling distance  $d_2$  is taken from 10 nm to 35 nm with an interval of 5 nm, while the other parameters remain invariable. As the coupling distance  $d_2$  increases, the variation in the transmission and group index at transparency peak of  $\text{PIT}_1$ and  $PIT<sub>2</sub>$  is shown in Figs. [7a](#page-6-15), b. Contrary to the consequence of adjusting coupling distance  $d_1$ , when the coupling distance  $d_2$  increases, the transmission and group index at transparency peak of  $PIT_1$  are barely influenced. Meanwhile, the transmission and group index at central wavelength of  $PIT<sub>2</sub>$  window present a tendency to decrease and increase, respectively. Therefore, we can manipulate the transmission and group index at transparency peak of  $\text{PIT}_2$  separately.



<span id="page-5-0"></span>**Fig. 5 (a)** Variation tendency of the transparency peak wavelengths at  $PIT_1$  and  $PIT_2$  windows as length  $l_{t1}$  and length  $l_{s1}$  increase. **(b)** Variation tendency of the transparency peak wavelengths at  $PIT_1$  and  $PIT_2$ windows as length  $l_{12}$  and length  $l_{s2}$  increase

<span id="page-5-1"></span>**Fig. 6 (a)** The transmission at peak of PIT windows as functions of coupling distance  $d_1$ . (b) The relationship between group index at peak of PIT windows and the coupling distance  $d_1$ 



<span id="page-6-15"></span>**Fig. 7 (a)** The transmission at peak of PIT windows as functions of coupling distance  $d_2$ . (b) The relationship between group index at peak of PIT windows and the coupling distance  $d_2$ 

The coupling distance  $d_2$  is set to 20 nm for obtaining higher transmission and group index simultaneously in this paper.

### **Conclusion**

In summary, we proposed a novel plasmonic structure mainly consisting of two tooth cavities coupled with stub resonators, respectively. Triple PIT windows are implemented based on diferent formation mechanisms and the reasons of formation are analyzed in detail using CMT model. Simulation results calculated by the FDTD method demonstrate that the obvious slow light responses at  $PIT_1$  and  $PIT_2$  windows are achieved. In addition, we can separately manipulate the transmission characteristics of  $\text{PIT}_1$  and  $\text{PIT}_2$  windows, including the wavelength, transmission and group index of transparency peak. The proposed plasmonic slow light device has many potential applications in highly integrated photonic loop.

**Author Contributions** Yiyuan Xie contributed to conceptualization, supervision and writing—review. Junxiong Chai provided methodology and software and performed writing—original draft, and writing—editing. Yichen Ye, Tingting Song, Bocheng Liu, Liangyi Zhang, Yunchao Zhu and Yong Liu performed writing—review.

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**Data Availability** All data generated or analyzed during this study are included in this article.

#### **Compliance with Ethical Standards**

**Conflicts of Interest** The authors declare that they have no confict of interest.

**Consent to Publish** Informed consent for publication was obtained from all authors.

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