

# Fano Resonance-Based Blood Plasma Monitoring and Sensing using Plasmonic Nanomatryoshka

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#### Abstract

The fast label-free detection of specific antibodies and their concentration in blood plasma is useful for many applications, e.g., in Covid-19 patients. The change in biophysical properties like the refractive index of blood plasma due to the production of antibodies during infection may be very helpful in estimating the level and intensity of infection and subsequent treatment based on blood plasma therapy. In this article, Fano resonance-based refractive index sensor using plasmonic nanomatry-oshka is proposed for blood plasma sensing. The interaction between hybridized modes (bright and dark modes) in optimized nanomatryoshka leads to Fano resonance, which by virtue of steeper dispersion can confine the light more efficiently compared with Lorentzian resonance. We propose the excitation of Fano resonances in sub 100-nm size nanomatryoshka based on newly emerging plasmonic materials ZrN and HfN, and one of the most widely used conventional plasmonic material, Au. Fano resonance-based plasmonic sensors leads to sensitivity = 188.5 nm/RIU, 242.5 nm/RIU, and 244.9 nm/RIU for Au, ZrN, and HfN, respectively. The corresponding figure of merit (nm/RIU) is ~  $3.5 \times 10^3$ ,  $3.1 \times 10^3$ , and  $2.8 \times 10^3$  for Au, ZrN, and HfN, respectively. Present theoretical analysis shows that refractive index sensors with high sensitivity and figure of merit are feasible using Fano modes of plasmonic nanomatryoshka.

Keywords Plasmonics · Sensor · Fano resonance · Mie-theory · Transition metal nitrides

## Introduction

In the backdrop of the fast growing world population, the need for developing efficient healthcare systems, particularly for medical testing and diagnostics, is at its high demand [1, 2]. The recent worldwide spread of COVID-19 pandemic has emphasized on the vitality of fast testing and diagnostic techniques. This is the motivation that encourages the researchers to explore the possibility and scope of developing efficient, long-lasting, economical, and practically feasible solutions to the existing as well as future medical challenges posing threat to the existence of humanity. The photonic systems provide solution for the development of label free fast detection/sensing system in which various types of resonances, e.g., Fabry-Perot resonators, Bragg

<sup>2</sup> Galogotias College of Engineering and Technology, 201312 Greater Noida, India resonators, reflection filters, antireflection filters, and transmission gratings, have played the key role [3]. Beyond classical diffraction limit, sub wavelength metallic structures show nanoscale optical confinement by virtue of excitation of surface plasmons having unique properties [4]. Such structures will provide a better platform for switching, spasing, molecular energy transfer, energy harvesting, bacteria detection, cancer therapy, etc. [5–16]. Plasmonic systems are emerging as the backbone of medical diagnostics, e.g., large efforts of physicists, chemists, biologists, and material scientists, are focused on the development of an ultrasensitive plasmonic sensor for bio-molecular sensing. The origin of asymmetric resonant (Fano resonance) interaction [17] in the complex geometry like concentric or non-concentric nanoshell [18–20], rings [21], septamer [22], trimers [23], and disks-ring [24] provides hybrid plasmonic systems characterized by rich plasmonic spectra. This not only open the possibility for new devices based on Fano modes but may also improve the performance of existing plasmonic device [25, 26]. Fano resonance usually involves the interference of two modes, the one with spectrally broad background and the other with narrow resonanceand characterized by strong

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light confinement [27]. Fano resonance shows steeper dispersion and strong dependence on size, shape, and surrounding medium, compared with Lorentzian resonance [27]. In the last decade, asymmetric Fano resonances in plasmonic nanostructures have been a subject of intensive reaserch. For example, N. Halas and S. Link [28] at Rice University reported the first "plasmonic Fano switch for color display" based on tiny gold nanoparticles and liquid crystals. It is now well established that the Fano resonances originate from near-field coupling of "bright" and "dark" plasmon modes of individual nanoparticle within the cluster [28]. The excitations of Fano resonances in optimized structure provide a platform for detection [29], surface-enhanced Raman spectroscopy [30], nanolithography, microscopy, sub-diffraction imaging [31], ultra-small size laser [31], interferometric phase detection, ultrasensitive spectroscopy, identification of molecular monolayer [32], X-Ray tomography, structural analysis, and precision metrology [33]. Irrespective of geometry, polarization insensitive sub 100 nm multilayered core-shell structure called nanomatryoshka (core/shell/shell) shows the inherent capability of spectral tuning and unique characteristics [16]. In optimized nanomatryoshka the interaction and coupling of low and high energy hybridized modes lead to the excitation of Fano modes [20, 21]. In addition to the choice of an appropriate geometry of plasmonic nanostructure, the proper selection of plasmonic material is also very crucial for designing fast and efficient optoelectronic systems. Traditionally, the coinage metals like gold, silver, copper, and aluminum have been the primary choice of plasmonic materials in the plasmonic systems and devices. The real-time fabrication issue and incompatibility with standard fabrication [34], with inherent loss due to large real part in noble metals, are the key motivations for using newly emerging plasmonic materials like refractory transition metal nitrides (ZrN, HfN, etc.) for existing plasmonic-based devices [35–40]. In our previous work, it was examined that the refractory transition metal nitrides (RTMNs) like ZrN and HfN show plasmonic properties similar to the conventional plasmonic material Au [7, 8]. Hence, refractory transition metal nitrides (i.e., ZrN, TiN, and HfN) and the ternary alloy (Ti<sub>x</sub>Zr<sub>1-x</sub>N) exhibit attractive plasmonic properties which play a crucial role in designing a better platform for refractive index sensing/detection. The unique biophysical signature (like refractive index and morphology) of bio-molecules (e.g., cells, bacteria, blood plasma, proteins) pave the way for label-free detection and sensing [41–43]. In a normal human being, the blood consists of about 55% plasma (90% water and 10% proteins) and 45% cells (99% erythrocytes, 1% leukocytes, and thrombocytes). Since, blood plasma contains proteins (antibodies) and other ingredients, due to slight variation in the blood plasma concentration cause variation in the pH value of blood, which in turn leads to serious health deterioration.

The detection of specific antibodies and the concentration of blood plasma in Covid-19 patients are key for monitoring their health and extremely useful in blood plasma therapy. It is therefore very crucial to develop a label free sensing system to monitor the concentration of blood plasma. Microfluidic techniques for estimating the concentration of hydrogen sulphide [44], glucose, and cholesterol in blood plasma have already been reported [45]. For example, silver-based luminescent probe has been designed for enzymatic sensing/detection of glucose level in blood plasma [46]. Further, the cancer bio-marker changes the thermal behavior of most abundant proteins in blood plasma and its detection in blood plasma and urine is normally done by techniques such as differential scanning calorimeter and mass spectrometry [47]. The excitation of SPR in optical fiber leads to the detection of fibrinogen traces in the blood plasma of Alzheimer's patients with a detection limit of 20 ng/ml [48]. In the backdrop of above discussion, it is therefore imperative to develop improved methods for detecting minute changes in the blood plasma concentration for early diagnosis of the diseases.

The present work analyzes the feasibility of efficient refractive index sensing of blood plasma concentration using Fano modes of transition metal nitride-based nanomatryoshka. The crucial role of Fano mode's lineshape requires effective and efficient theoretical tools. The present work intends to accomplish the following objectives: (I) to study the origin of asymmetric Fano line shape in subwavelength sized nanomatryoshka, (II) to investigate the unique features of Fano resonances and their comparative study with symmetric localized modes, (III) to assess the sensitivity and figure of merit of Fano resonances for different sensing environments, and (IV) quantitative analysis of sensing properties as suitable for blood plasma sensing.

## **Theoretical Model**

The nanomatryoshka-based plasmonic system considered for present investigations consists of three concentric layers, namely, the metallic core having permittivity  $\varepsilon_1$  and radius  $R_1$ , dielectric layer having permittivity  $\varepsilon_2$  and radius  $R_2$ , and metallic shell having permittivity  $\varepsilon_3$  and radius  $R_3$  as shown in Fig. 1. The nanoparticle is ingrained in the medium of dielectric constant,  $\varepsilon_m = n^2$ , where *n* is the refractive index of the ingrained medium. The numerous analytical (quasi-static approach, Mie scattering theory, transfer matrix approach, etc.), and numerical (FEM, FDTD, etc.) methods are available for studying and simulating optical properties of nanomatryoshaka. In the present work, the well-established Mie theory has been used to treat plasmonic nanomatryoshka [49]. Mie theory consider that the uniform field incident on nanomatryoshka produces scattered and internal fields. These fields may be expressed as an infinite series of vector



**Fig. 1** The schematic diagram of plasmonic nanomatryoshka particle. The nanomatryoshka consists of metallic core having permittivity  $\varepsilon_1$  and radius  $R_1$ , dielectric layer having permittivity  $\varepsilon_2$  and radius  $R_2$ , and metallic shell having permittivity  $\varepsilon_3$  and radius  $R_3$ . Nanomatryoshka particle is ingrained in the medium of dielectric constant  $\varepsilon_{av}$ . It is assumed that the particle is placed in the uniform electric field  $E_0$ 

spherical harmonics. This is to be emphasized that the Mie analysis is based on the full wave solutions of electromagnetic Maxwell equation formulated for the system under consideration. The solutions are commonly expressed in the form of Mie coefficients ( $a_l$  and  $b_l$ ) as defined below [50, 51], Eq. 1

$$a_{l} = \frac{\Psi_{l}(x_{3})H_{l}^{a}(f_{3}x_{3}) - f_{3}D_{l}^{(1)}(x_{3})}{\xi_{1}(x_{3})H_{l}^{a}(f_{3}x_{3}) - f_{3}D_{l}^{(3)}(x_{3})}$$

$$b_{l} = \frac{\Psi_{l}(x_{3})f_{3}H_{l}^{b}(f_{3}x_{3}) - D_{l}^{(1)}(x_{3})}{\xi_{l}(x_{3})f_{3}H_{l}^{b}(f_{3}x_{3}) - D_{l}^{(3)}(x_{3})}$$
(1)

Here, for four layer system, and size parameter  $x_3 = kR_3$  where *k* is the wavenumber,  $f_3 = \varepsilon_3/\varepsilon_m$  is the relative refractive index of outer shell medium with respect to the ingrained medium, Ricatti-Bessel functions  $\psi_l(z) = zj_l(z)$ ;  $\chi_l(z) = -zy_l(z)$ ,  $\xi_l(z) = zh_l^1(z)$  are written in the form of spherical Bessel functions  $j_l(z)$ ,  $y_l(z)$ , and  $h_l^1(z)$ . The logarithmic derivative of Ricatti-Bessel function like  $D_l^{(1)}, D_l^{(2)}$  and  $D_l^{(3)}$  are written as

$$D_l^{(1)} = \frac{\psi_l'(z)}{\psi_l(z)}; D_l^{(2)} = \frac{\chi_l'(z)}{\chi_l(z)}; D_l^{(3)} = \frac{\xi_l'(z)}{\xi_l(z)}, \text{ and } H_l^a(f_3x_3), H_l^b(f_3x_3)$$

are calculated as in Eq. 2

$$H_{l}^{a}(f_{3}x_{3}) = \frac{[\Psi_{l}(f_{3}x_{3})/\chi_{l}(f_{3}x_{3})]D_{l}^{(1)}(f_{3}x_{3})}{[\Psi_{l}(f_{3}x_{3})/\chi_{l}(f_{3}x_{3})] - A_{l}^{(3)}} - \frac{A_{l}^{(3)}D_{l}^{(2)}(f_{3}x_{3})}{[\Psi_{l}(f_{3}x_{3})/\chi_{l}(f_{3}x_{3})] - A_{l}^{(3)}} \\H_{l}^{b}(m_{3}x_{3}) = \frac{[\Psi_{l}(f_{3}x_{3})/\chi_{l}(f_{3}x_{3})]D_{l}^{(1)}(f_{3}x_{3})}{[\Psi_{l}(f_{3}x_{3})/\chi_{l}(f_{3}x_{3})] - B_{l}^{(3)}} - \frac{B_{l}^{3}D_{l}^{(2)}(f_{3}x_{3})}{[\Psi_{l}(f_{3}x_{3})/\chi_{l}(f_{3}x_{3})] - B_{l}^{(3)}}$$
(2)

the corresponding terms  $A_l^{(3)}$ ,  $B_l^{(3)}$  can be written as in Eq. 3

$$A_{l}^{(3)} = \frac{\psi_{l}(f_{3}x_{2})}{\chi_{l}(f_{3}x_{2})} \frac{f_{3}H_{l}^{a}(f_{2}x_{2}) - f_{2}D_{l}^{(1)}(f_{3}x_{2})}{f_{3}H_{l}^{a}(f_{2}x_{2}) - f_{2}D_{l}^{(2)}(f_{3}x_{2})}$$

$$B_{l}^{(3)} = \frac{\psi_{l}(f_{3}x_{2})}{\chi_{l}(f_{3}x_{2})} \frac{f_{2}H_{l}^{b}(f_{2}x_{2}) - f_{2}D_{l}^{(1)}(f_{3}x_{2})}{f_{2}H_{l}^{b}(f_{2}x_{2}) - f_{2}D_{l}^{(2)}(f_{3}x_{2})}$$
(3)

where Eq. 4

$$H_{l}^{a}(f_{2}x_{2}) = \frac{\left[\psi_{l}(f_{2}x_{2})/\chi_{l}(f_{2}x_{2})\right]D_{l}^{(1)}(f_{2}x_{2})}{\left[\psi_{l}(f_{2}x_{2})/\chi_{l}(f_{2}x_{2})\right] - A_{l}^{(2)}} - \frac{A_{l}^{(2)}D_{l}^{(2)}(f_{2}x_{2})}{\left[\psi_{l}(f_{2}x_{2})/\chi_{l}(f_{2}x_{2})\right] - A_{l}^{(2)}}$$
$$H_{l}^{b}(m_{2}x_{2}) = \frac{\left[\psi_{l}(f_{2}x_{2})/\chi_{l}(f_{2}x_{2})\right]D_{l}^{(1)}(f_{2}x_{2})}{\left[\psi_{l}(f_{2}x_{2})/\chi_{l}(f_{2}x_{2})\right] - B_{l}^{(2)}} - \frac{B_{l}^{3}D_{l}^{(2)}(f_{2}x_{2})}{\left[\psi_{l}(f_{3}x_{3})/\chi_{l}(f_{2}x_{2})\right] - B_{l}^{(2)}}$$
(4)

where the coefficients  $A_l^{(2)}$ ,  $B_l^{(2)}$  are written as in Eq. 5

$$A_{l}^{(2)} = \frac{\Psi_{l}(f_{2}x_{1})f_{2}H_{l}^{a}(f_{1}x_{1}) - f_{1}D_{l}^{(1)}(f_{2}x_{1})}{\chi_{l}(f_{3}x_{2})f_{3}H_{l}^{a}(f_{1}x_{1}) - f_{1}D_{1}^{(2)}(f_{2}x_{1})}$$

$$B_{l}^{(2)} = \frac{\Psi_{l}(f_{3}x_{2})f_{2}H_{l}^{b}(f_{1}x_{1}) - f_{1}D_{l}^{(1)}(f_{2}x_{1})}{\chi_{l}(f_{3}x_{2})f_{2}H_{l}^{b}(f_{1}x_{1}) - f_{1}D_{l}^{(2)}(f_{2}x_{1})}$$
(5)

where in Eq. 6

$$A_l^{(1)} = 0, H_l^a(f_1 x_1) = D_l^1(f_1 x_1)$$
  

$$B_l^{(1)} = 0, H_l^b(f_1 x_1) = D_l^1(f_1 x_1)$$
(6)

Here,  $x_1 = kR_1$ ,  $x_2 = kR_2$ ,  $x_3 = kR_3$  are the size parameters and k is the wave vector and,  $f_1$ ,  $f_2$  and  $f_3$  are the refractive indices of the core, sandwich layer, and shell relative to the surrounding medium, respectively. Moreover, the extinction efficiencies ( $Q_{\text{ext}}$ ), scattering ( $Q_{\text{sca}}$ ), and absorption ( $Q_{\text{abs}}$ ) efficiencies are written as [49] in Eq. 7

$$Q_{ext} = \frac{2}{(kR_3)^2} \sum_{l=1}^{\infty} [2l+1] \operatorname{Re}(a_l + b_1)$$

$$Q_{sca} = \frac{2}{(kR_3)^2} \sum_{l=1}^{\infty} [2l+1] (|a_1|^2 + |b_l|^2)$$

$$Q_{abs} = Q_{ext} - Q_{sca}$$
(7)

where k is the wavenumber of medium and  $R_3$  is the radius of nanomatryoshka.

## **Results and Discussion**

In order to validate the present approach and the code that we developed, the results reported in Wu et al. [50] are reproduced for Au-based nanomatryoshka (NMS) and nanoshell (NSH) with outer radius of 50 nm as shown in Fig. 2a. The validation for three different core sizes (15, 21, 25 nm) is shown. The optical constants of refractory transition metal nitrides ZrN and HfN are adopted from Kumar et al. [39] and that of Au are adopted from Shishodia and Juneja [13]. The spectral variation of scattering efficiency for ZrN-based nanomatryoshka ( $R_1 = 30$  nm,  $R_2 = 50$  nm, and  $R_3 = 70$  nm) is presented in Fig. 2b. For the sake of comparison, the corresponding overlay plots for spherical (R = 70 nm) and nanoshell ( $R_1 = 50 \text{ nm}, R_2 = 70 \text{ nm}$ ) geometries are also presented. The scattering spectra show the possibility of the appearance of Fano resonance in nanomatryoshka. This is possible by virtue of indirect coupling between non-radiative (dark) and radiative (bright) modes of plasmonic nanostructure [52–54]. Figure 2 b clearly shows that, Fano modes appear in nanomatryoshka but not in sphere and nanoshell. Evidently, Fano dip and peak appears at,  $\lambda = 635$  nm and  $\lambda = 743$  nm. In order to confirm that the resonance appeared in nanomatryoshka is Fano resonance, the calculated data is fitted into the following standard lineshape expression of Fano resonance [17],

$$f(\lambda) = \frac{\left(F \times w + \lambda - \lambda_R\right)^2}{\left(\lambda - \lambda_R\right)^2 + w^2}$$
(8)

In Eq. 8, F is called Fano parameter (degree of asymmetry),  $\lambda_R$  is the position of resonance, and w is the width



**Fig.2 a** Validation of Mie theory–based extinction efficiency  $(Q_{ext})$  for Au-based nanomatryoshka (NMS) and nanoshell (NSH) with specifications same as in Ref. [50]. **b** The calculated spectral variation of scattering efficiency for ZrN-based nanosphere (70 nm), nanoshell (50–70 nm), and nanomatyroshka (30-50-70 nm) particle ingrained in the medium of refractive index 1.333



**Fig. 3** The calculated spectral variation of scattering efficiency of ZrN-based nanomatyroshka (30-50-70 nm) and corresponding fitting of calculated data into Fano expression. The excellent fitting of calculated data into the standard Fano expression confirm the Fano nature of resonance

of Fano resonance. The calculated spectral variation of scattering efficiency and the corresponding fitting into Eq. 8 is presented in Fig. 3 for ZrN-based nanomatryoshka ingrained in the medium of refractive index 1.333. The fairly good fitting of calculated data into Fano expression confirms the Fano nature of resonance in nanomatryoshka. The fitting parameters are summarized in Table 1. The calculated spectral variation of scattering efficiency  $(Q_{sca})$  for nanomatryoshka consisting of Au, ZrN, and HfN shell is shown in Fig. 4a. Unless mentioned otherwise, the sandwich dielectric medium is assumed to be lossless silica with wavelengthindependent dielectric constant,  $\varepsilon_2 = 2.04$ . The size parameters considered for this analysis are  $R_1 = 30$  nm,  $R_2 = 50$  nm, and  $R_3 = 70$  nm. This is evident that the scattering efficiency (normalized scattering cross-section) spectra show resonant behavior by virtue of excitation of localized surface plasmon modes, whose interaction results in the characteristic Fano resonance. For the nanomatryoshka under consideration, Fano peak appears at  $\lambda = 737$  nm, 741 nm, 703 nm, and Fano

**Table 1** The Fano fitting parameter of nanomatryoshka with  $R_1 = 30 \text{ nm}, R_2 = 50 \text{ nm}, \text{ and } R_3 = 70 \text{ nm}$ 

Fitting Parameters	Au	ZrN	HfN
F	2.24	2.17	2.12
$\lambda_R$ (nm)	738	743	705
W(nm)	45.16	57.45	61.23



**Fig. 4 a** The calculated spectral variation of scattering efficiencies of Au, ZrN, and HfN-based nanomatryoshka with  $R_1 = 30$  nm,  $R_2 = 50$  nm, and  $R_3 = 70$  nm. **b** The spectral variation of scattering efficiency of ZrN-based nanomatryoshka (30, 50, 70) ingrained in the surrounding medium of slightly different refractive indices. The red-shift of Fano resonance peak with increasing refractive index of ingrained medium is clearly evident

dip appears at  $\lambda = 650$  nm, 635 nm, 599 nm for Au-, ZrN-, and HfN-based nanomatryoshka, respectively. It is evident that the Fano peak scattering efficiencies of Au, ZrN, and HfN are comparable having magnitude 5.9, 5.7, and 5.4, respectively. Moreover, FWHM (nm) values are 45.57 nm, 57.16 nm, and 61.23 nm, respectively. Figure 4b clearly shows the red-shift of Fano resonance peak as the refractive index of the surrounding medium around ZrN-based nanomatryoshka is varied slightly. It is evident that the resonant Fano peak wavelength is extremely sensitive even to a slight change in the refractive index of the surrounding medium. As it is well known that the healthy blood plasma comprises of water and crucial proteins with refractive index, 1.32459 [55], the small change in the concentration of blood plasma leads to a change in the refractive index. Next, let us consider a practical scenario, where the sensing medium is the defected blood containing different blood plasma concentrations. The refractive index change resulting from the change in plasma concentration, e.g., resulting from contaminations and diseases may be written as [55],

$$n = 1.32459 + 0.000194C_p \tag{9}$$

In Eq. 9,  $C_p$  denotes the concentration of defected plasma in the blood and it is normally expressed in the units of grams per liter. In the present calculations,  $C_p$  is varied from 0 to 50 g/l in the steps of 10 g/l. The refractive index values of blood for different concentrations of contaminants in blood plasma are tabulated in Table 2. The calculated spectral variations of scattering efficiency ( $Q_{sca}$ ) for nanomatryoshka consisting of Au, ZrN, and HfN are shown in Fig. 5a–c, respectively. The results are shown for six different plasma concentrations in blood. It is evident that the Fano resonance appears in the scattering spectra of Au-, ZrN-, and HfN-based nanomatryoshka. This is clearly

 Table 2 The optimized refractive index of defected concentration of blood plasma [55]

Sr. no	Concentration (g/l)	Refractive index (n)	
1	0	1.324590000	
2	10	1.339692811	
3	20	1.359112811	
4	30	1.378592811	
5	40	1.397952811	
6	50	1.417372811	

evident that the peak position of Fano resonance shifts on varying the plasma concentration. Moreover, Fano resonance wavelength varies almost linearly with the concentration of blood plasma as is evident from Fig. 5d. A significant shift in Fano resonance wavelength is observed with minuscule change of blood plasma concentration. Interestingly, the Fano dip wavelength remains almost unaltered with the change in blood plasma concentration. It is interesting to note that the scattering efficiency at resonance dip wavelength in all cases is very close to zero. This corresponds to the high optical absorption in this spectral region. This feature is desired for designing efficient light absorbing nanostructures. It is evident that the scattering peak wavelength is also a highly sensitive function of the refractive index of the surrounding/sensing medium. The fractional change in the refractive index leads to the drastic reduction in scattering efficiency, and the shift in resonant wavelength makes the basis of Fano resonance-based biosensing. The calculated Fano peak wavelength positions for six different plasma concentrations in Au-, ZrN-, and HfN-based nanomatryoshka (30, 50, 70) are summarized in Table 3. The sensitivity (S) of refractive index sensor is defined as the rate of change of resonant peak wavelength (nm) with the refractive index of sensing medium. Mathematically, the sensitivity (nm/RIU) of the sensor can be written as [14]

$$S = \frac{d\lambda_R}{dn} \tag{10}$$

The dependence of Fano peak wavelength on the concentration of defected blood plasma and hence the refractive index can be fitted into a linear equation of the following form,

$$\lambda_R(nm) = \lambda_0 + S \times n \tag{11}$$

In Eq. 11,  $\lambda_0$  and *S* are the fitting parameters. The dependence of resonant wavelength ( $\lambda_R$ ) with change in refractive index of sensing blood plasma medium and corresponding sensitivity (S) for (a). Au, (b). ZrN, and (c). HfN based nanomatryoshka are shown in Fig. 6. The analysis

**Fig. 5** The calculated spectral variation of scattering efficiency  $(Q_{sca})$  spectra of **a** Au, **b** ZrN, and **c** HfN-based nanomatryoshka with  $R_1 = 30$  nm,  $R_2 = 50$  nm, and  $R_3 = 70$  nm. The variation of resonant peak wavelength with concentration of contaminated blood plasma is shown in **d** 



of data shown in Fig. 6 shows that the sensitivity values corresponding to the Fano resonances in Au-, ZrN-, and HfN-based nanomatryoshka are 188.5 nm/RIU, 242 nm/ RIU, and 244.9 nm/RIU, respectively. This suggests that the sensitivity values of ZrN- and HfN-based nanoparticle systems are higher than that of commonly used plasmonic material gold. Another important sensor parameter is the figure of merit (FOM), which is simply the product of quality factor (QF) of resonance and the sensitivity (*S*), and it is defined as [14]

$$FOM (nm/RIU) = QF \times S$$
(12)

The calculated FOM (nm/RIU) values are  $3.5 \times 10^3$ ,  $3.1 \times 10^3$ , and  $2.8 \times 10^3$  for Au-, ZrN-, and HfN-based nanomatryoshka, respectively. This suggests that the FOM

**Table 3** The optimized plasmonic Fano resonant wavelength for different defected concentration of blood plasma and size of nanomatryoshka with  $R_1 = 30$  nm,  $R_2 = 50$  nm, and  $R_3 = 70$  nm

Sr. no	Blood plasma concen- tration (g/l)	Fano wavelength (nm)		
		Au	ZrN	HfN
1	0	737	741	703
2	10	740	745	705
3	20	743	750	711
4	30	747	754	715
5	40	750	759	720
6	50	755	764	726

of ZrN- and HfN-based nanomatryoshka is comparable with that of Au-based nanomatryoshka. The summary of calculated parameters for Au-, ZrN-, and HfN-based nanomatryoshka is provided in Table 4. The assessment of Fano resonance-based sensing characteristics shows the following: (I) Scattering efficiencies of ZrN- and HfNbased nanomatryoshka are comparable with Au, one of the most widely used conventional plasmonic material.



**Fig. 6** The calculated dependence of resonant Fano peak position on the concentration and hence the refractive index of the blood plasma medium for **a** Au, **b** ZrN, and **c** HfN-based nanomatryoshka specified by  $R_1 = 30$  nm,  $R_2 = 50$  nm, and  $R_3 = 70$  nm

**Table 4** The optimized plasmonic Fano resonance based sensing parameters for nanomatryoshka with  $R_1 = 30$  nm,  $R_2 = 50$  nm, and  $R_3 = 70$  nm

Nanomatryoshka (NMS), $R_1 = 30$ nm, $R_2 = 50$ nm, and $R_3 = 70$ nm						
S. no	Parameters	Au	ZrN	HfN		
1	$\lambda_R$ (nm)	738	743	705		
2	S (nm/RIU)	188.5	242.5	244.9		
3	FWHM (nm)	45.57	57.16	61.23		
4	FOM (nm/RIU)	$3.5 \times 10^3$	$3.1 \times 10^{3}$	$2.8 \times 10^{3}$		

(II) Refractory transition metal nitrides like ZrN and HfN are potential plasmonic materials for Vis-NIR spectral region. (III) Scattering efficiencies of nitride-based nanomatryoshka geometry are extremely sensitive to the thicknesses, aspect ratio, and the refractive index of constituent mediums.

## Summary

In this work, the sensing characteristics of Fano resonancebased plasmonic nanomatryoshka comprising of Au, ZrN, and HfN plasmonic materials are assessed. It is shown that Au, ZrN, and HfN nanomatryoshka-based Fano sensors can exhibit the sensitivity (nm/RIU) ~ 188.5, 242.5, and 244.9, respectively. Moreover, the corresponding figure of merit (nm/RIU) ~  $3.5 \times 10^3$ ,  $3.1 \times 10^3$ , and  $2.8 \times 10^3$  HfN is exhibited. Therefore, biosensors with high sensitivity and figure of merit can be developed by employing Fano modes in plasmonic nanomatryoshka. The availability of compatible nitride-based plasmonic materials can open the door for additional applications. The present research can play a vital role in developing refractory transition metal nitride-based plasmonic systems like solar cells, molecular electronic devices, optical switches, and biosensors.

Authors Contributions Both authors contributed to the study conception and design. The calculations were performed by Pankaj Pathania. Material preparation, manuscript writing, and analysis were performed by Pankaj Pathania and Manmohan Singh Shishodia. Both authors read and approved the final manuscript.

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**Data Availability** The data that support the findings of this study are available from the corresponding author upon reasonable request.

## **Compliance with Ethical Standards**

**Competing Interest** The authors declare that they have no conflict of interest.

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