#### RESEARCH PAPER



# Predicting tunnel squeezing using support vector machine optimized by whale optimization algorithm

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#### Abstract

The squeezing behavior of surrounding rock can be described as the time-dependent large deformation during tunnel excavation, which appears in special geological conditions, such as weak rock masses and high in situ stress. Several problems such as budget increase and construction period extension can be caused by squeezing in rock mass. It is significant to propose a model for accurate prediction of rock squeezing. In this research, the support vector machine (SVM) as a machine learning model was optimized by the whale optimization algorithm (WOA), WOA-SVM, to classify the tunnel squeezing based on 114 real cases. The role of WOA in this system is to optimize the hyper-parameters of SVM model for receiving a higher level of accuracy. In the established database, five input parameters, i.e., buried depth, support stiffness, rock tunneling quality index, diameter and the percentage strain, were used. In the process of model classification, different effective parameters of SVM and WOA were considered, and the optimum parameters were designed. To examine the accuracy of the WOA-SVM, the base SVM, ANN (refers to the multilayer perceptron) and GP (refers to the Gaussian process classification) were also constructed. Evaluation of these models showed that the optimized WOA-SVM is the best model among all proposed models in classifying the tunnel squeezing. It has the highest accuracy (approximately 0.9565) than other un-optimized individual classifiers (SVM, ANN, and GP). This was obtained based on results of different performance indexes. In addition, according to sensitivity analysis, the percentage strain is highly sensitive to the model, followed by buried depth and support stiffness. That means, e, H and K are the best combination of parameters for the WOA–SVM model.

Keywords Classification modeling · Squeezing · SVM · Tunnel · WOA algorithm

# 1 Introduction

Tunnel squeezing refers to the occurrence of large amount of deformation in surrounding rock mass rock, which is normally more than the designed deformation. This phenomenon, which takes a long time to form, causes many difficulties during and after construction of tunnels  $[6, 11, 69]$  $[6, 11, 69]$  $[6, 11, 69]$  $[6, 11, 69]$  $[6, 11, 69]$ . The squeezing behavior of surrounding rock can be described as the time-dependent large deformation during tunnel excavation, which is essentially related to creep created by exceeding the ultimate shear stress [\[8](#page-20-0), [19,](#page-21-0) [25,](#page-21-0) [59](#page-22-0), [69](#page-22-0)]. Different studies showed that the compressive surrounding rock has the deformation features of large deformation amount, long deformation duration, high deformation speed, large destruction range of surrounding rock and various forms of supporting structure failures [\[19](#page-21-0)]. There are objective and subjective factors for the occurrence of tunnel squeezing, where the objective conditions involve rock properties, tectonic stress, tunnel dimensions, rock type, high in situ stress and large radius or span [[8\]](#page-20-0). On the other hand, the typical subjective factors are associated with support installation, in which the deformation can be restrained if the support is installed on time [\[27](#page-21-0), [42,](#page-21-0) [62](#page-22-0)]. Tunnel squeezing may cause several unwanted issues, e.g., budget increase, construction period extension and construction safety [[8,](#page-20-0) [22](#page-21-0)]. In order to overcome these issues, many attempts have been done by various scholars, and they suggested several approaches for predicting tunnel squeezing, including empirical, semiempirical and theoretical methods [[4,](#page-20-0) [24,](#page-21-0) [32,](#page-21-0) [33,](#page-21-0) [61,](#page-22-0) [68\]](#page-22-0). With the development of the computer science and various available technologies, numerical simulation and classical

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statistics methods have been widely used in tunnel squeezing prediction [[13,](#page-21-0) [23](#page-21-0), [37–39](#page-21-0), [65](#page-22-0)].

In recent years, the successful applications of machine learning (ML) methods in solving regression, classification and time-series problems in science and engineering have been reported by many researchers all around the world [\[2](#page-20-0), [3,](#page-20-0) [30,](#page-21-0) [31](#page-21-0), [40](#page-21-0), [41,](#page-21-0) [52,](#page-22-0) [76–78,](#page-22-0) [80](#page-22-0), [81](#page-22-0), [84–88,](#page-23-0) [91,](#page-23-0) [92](#page-23-0), [94](#page-23-0), [96–101](#page-23-0)]. These methods have been used by researchers in the areas of geotechnical [[15,](#page-21-0) [55,](#page-22-0) [66,](#page-22-0) [98\]](#page-23-0) and tunnel engineering [[75](#page-22-0), [81](#page-22-0), [83](#page-23-0)] and also to solve problem related to tunnel squeezing [[50,](#page-22-0) [65\]](#page-22-0). To estimate tunnel squeezing, ML techniques like artificial neural network (ANN), decision tree (DT), naive Bayes (NB) and support vector machine (SVM) have been used in the literature. As an example, Shafiei et al. [[65\]](#page-22-0) used and introduced a SVM classifier model, which was trained and tested based on 198 samples, in particular having two predictor variables (buried depth, H, and rock tunneling quality index, Q). The accuracy of their proposed model is 84.1%. In another interesting investigation, Sun et al. [\[71](#page-22-0)] constructed a multi-class SVM prediction model based on 117 samples. There were four predictor variables (H, Q, diameter, D, and support stiffness, K,) in the multi-class SVM model, and it was able to receive an accuracy of 88.1%. Zhang et al. [\[86](#page-23-0), [87\]](#page-23-0) established a classifier ensemble based on 166 cases, which includes five different ML classifiers: ANN, SVM, DT, k-nearest neighbor (KNN), and NB. The five variables, i.e., H, D, Q, K and strength stress ratio (SSR), were selected as input parameters for the classifier ensemble, and the final accuracy was obtained as 96%. Huang et al. [\[35](#page-21-0)] proposed a hybrid model of SVM mixed by back-propagation (BP) for identifying squeezing and non-squeezing problem based on a total of 180 data samples. In the SVM-BP model, the four indicators including H, K, D and Q were considered as model inputs. The accuracy of the SVM-BP model was obtained as 92.11%. In addition, other methods and accuracy comparison results are shown in Tabl[e1](#page-2-0). In light of above discussion, the performance of the combined classifiers/models is higher than the single classifier. However, in most of the cases, the combined classifier models are complex with the lowest level of practicality, when the number of classifiers increases. To solve this problem, this article only uses a single classifier SVM. SVM has high generalization performance and can solve problems like small samples and high dimensionality [[63\]](#page-22-0). According to the existing research, we can also found that support vector machines have become popular in engineering. Many researchers have applied support vector machines to tunnel extrusion prediction. It can be roughly divided into two applications. On the one hand, it uses SVM regression to predict the deformation of the tunnel [[39,](#page-21-0) [72,](#page-22-0) [90\]](#page-23-0). On the other hand, it uses SVM classification to determine whether the tunnel

will be squeezed. So far, most of the existing forecasting methods can be used to distinguish between squeezing and non-squeezing. However this article refers to the multiclass SVM proposed by Sun et al. [\[71](#page-22-0)] and introduces a SVM-based prediction model to predict the severity of tunnel squeezing. However, the difference is that we consider the effects of the percentage strain  $(\varepsilon)$ . There are several commonly considered predictor variables in this field, which are H, K, D, K and SSR. It seems that there is a need to consider effects of other important parameters on tunnel squeezing like the percentage strain  $(\varepsilon)$ . The mentioned parameters were rarely used as input parameter in the proposed ML classifier models. Table [2](#page-2-0) is the list of commonly used predictors.

Additionally, with the deepening of research, optimization algorithms are gradually introduced into machine learning methods to optimize hyper-parameters, such as whale optimization algorithm (WOA), gray wolf optimization (GWO), Harris Hawks optimizer (HHO) and moth-flame optimization (MFO). Therefore, various hybrid models have gradually formed such as GWO-SVM [\[79](#page-22-0), [82](#page-22-0)], WOA-SVM [\[94](#page-23-0)], MFO-SVM, GS-SVM [\[46](#page-21-0)], HHO-SVM [\[91](#page-23-0)], WOA-XGBoost, GWO-XGBoost, BO-XGBoost  $[64, 101, 100]$  $[64, 101, 100]$  $[64, 101, 100]$  $[64, 101, 100]$  $[64, 101, 100]$  $[64, 101, 100]$  and SCA-RF  $[91]$  $[91]$ . The above research shows that the hybrid model has better performance than a single machine learning method. Therefore, the whale optimization algorithm is introduced to improve the prediction performance of multi-class SVM. Whale optimization algorithm (WOA) has simple structure, few parameters, strong search ability and easy to implement [\[7](#page-20-0)].

Finally, an optimized classifier model (WOA-SVM) is proposed to predict the severity of tunnel squeezing based on five parameters, that is, buried depth (H), support stiffness (K), rock tunneling quality index (Q), diameter (D), and the percentage strain (e). Firstly, we establish a database containing above five surrounding rock indicators based on the existing literature and then preprocessing these data. Then, the WOA-SVM model was trained and tested of tunnel squeezing. This study copes with not only the development of the WOA-SVM model used for the anticipating of squeezing problems, but also the sensitivity analysis of predictor variables. Finally, in order to verify the advantage of the model proposed, an evaluation and comparison on the performance of different classifier models (WOA-SVM, ANN, SVM, and genetic programming, GP) based on the same database were implemented. The performance and accuracy of the mentioned models will be assessed and discussed to select the best model in predicting tunnel squeezing.

<span id="page-2-0"></span>

Author	Classifiers	Predictors	Number of samples	Accuracy	Number of classes
Shafiei et al. $[65]$	<b>SVM</b>	H, Q	198	84.1%	2
Sun et al. [71]	M-SVM	H, Q, D, K	117	88.13%	3
Feng $\&$ Jimenez $[21]$	<b>BNs</b>	H, Q, D, K, <b>SSR</b>	166	86.65%	$\overline{2}$
Azizi et al. [6]	<b>BNs</b>	H, Q, D, K, <b>SSR</b>	4(Kerman Water Conveyance Tunnel)		$\overline{2}$
Ghasemi & Gholizadeh [23]	K-NN	H, Q, D	115	95%	2
Ghasemi & Gholizadeh [23]	C5.0	H, Q, D	115	94%	2
Chen et al. $[13]$	DT	H, D, K, SSR, GC	154	93.5%	3
Zhang et al. $[86, 87]$	the classifier ensemble (BPNN, SVM, DT, KNN, LR, MLR, NB)	H, Q, D, K, <b>SSR</b>	166	96%	2
Huang et al. $[35]$	<b>SVM-BP</b>	H, Q, D, K	178	92.11%	2

Table 2 List of commonly used predictors [[9,](#page-20-0) [13](#page-21-0), [21\]](#page-21-0)



RQD = Rock quality designation,  $J_n$  = joint set number,  $J_r$  = joint roughness number,  $J_a$  = joint alteration number,  $J_w$  = joint water reduction factor,  $SRF$  = stress reduction factor. A = the cross-sectional area of tunnel.  $K_c$  = the stiffness of shotcrete linings,  $K_{sb}$  = the stiffness of steel sets,  $K_b$  = the stiffness of rock bolts.  $\sigma_{cm}$  = Rock mass uniaxial compressive strength. u = tunnel closure.

# 2 Predictor selection and database description

According to the published literatures, the research group collected 114 historical cases of tunnel squeezing from various locations like Greece, Bhutan, India, Austria, China, Nepal and Venezuela [\[1](#page-20-0), [6,](#page-20-0) [18](#page-21-0), [20,](#page-21-0) [32](#page-21-0), [51,](#page-22-0) [62,](#page-22-0) [67](#page-22-0), [71\]](#page-22-0). There are six parameters in each case where five of them  $(K, H, Q, D \text{ and } \varepsilon)$  were set as input variables to predict tunnel squeezing. Among these six parameters, H, Q and D are often appeared in empirical formulas, such as  $H = 350Q^{0.33}$  and  $H = 275N^{0.33}B^{-0.1}$ , which are proposed by Goel and Singh [\[27](#page-21-0), [68\]](#page-22-0). The three parameters reflect the influence of in situ stress, surrounding rock properties and tunnel size on squeezing. The support stiffness is selected as the input parameter. The reason is that the support stiffness plays an important role in controlling the excessive deformation caused by the interaction

between the support pressure and the rock mass deforma-tion response [[13\]](#page-21-0). SSR and  $\varepsilon$  are usually used as grading indicators such as in the research conducted by Jethwa et al. (1984), Barla [[8\]](#page-20-0) and Aydan et al. [[4](#page-20-0), [5\]](#page-20-0).

In this study, we adopt the classification standard proposed by Hoek and Marinos [\[33](#page-21-0)]. Therefore, non-squeezing (NS) (with  $\epsilon < 1\%$ ), minor squeezing (MS) (with  $1\% \le \varepsilon < 2.5\%$ ) and severe-to-extreme squeezing (SES) (with  $\epsilon \ge 2.5\%$ ) were represented by class 0, class 1 and class 2, respectively. A correlation scatter matrix was performed to know more about the used parameters, as shown in Fig. [1](#page-3-0). The diagonal of the matrix presents probability distributions for each squeezing class, the lower panels show pairwise scatter plots of three classes of squeezing data along the axis and the upper triangle presents the Pearson's correlation coefficients. It can be clearly seen that all indicators have no relatively meaningful correlation with each other, and there is no clear

<span id="page-3-0"></span>

Fig. 1 Correlation scatter matrix of cumulative distributions and statistical evaluations for the squeezing database

separation among NS, MS and SES. The mentioned input and output parameters will be used in the next stage for classification modeling of tunnel squeezing.

# 3 Concepts of predictive models

### 3.1 Support vector machine (SVM)

The SVM has high generalization performance and does not require prior knowledge of specific models; therefore, it is widely used to solve problems in different fields, for example, finance [[47](#page-21-0)], energy [[34\]](#page-21-0), hydrological research [\[58](#page-22-0)], mechanical engineering [\[16](#page-21-0), [48](#page-21-0)], civil engineering [\[63](#page-22-0), [84\]](#page-23-0) and other fields. Of course, SVM is also widely used for tunnel extrusion prediction [[38,](#page-21-0) [65\]](#page-22-0). The initial concept of SVM is to input the training data set and output the separating classification decision function with the largest geometric interval [\[12](#page-20-0), [16,](#page-21-0) [34](#page-21-0), [47–](#page-21-0)[49,](#page-22-0) [74\]](#page-22-0). The SVM has been widely used to solve multivariate classification and regression problems [[45,](#page-21-0) [54,](#page-22-0) [58\]](#page-22-0), although it is a binary classification model on nature. The advantage of the SVM model lies in the ability to transform nonlinear problems into linear problems in high-dimensional feature spaces with the help of kernel functions [[54\]](#page-22-0).

In practical problems, it is difficult to find a hyperplane that can separate different categories of samples when the training sets are nonlinearly separable in the sample space. To solve this problem, there is a need to allow SVM for making mistakes on some datasets. Therefore, the sense of

''soft margin'' was introduced into the SVM model. In this way, the optimization objective functions of SVM can be expressed in the following [\[45](#page-21-0), [46,](#page-21-0) [73,](#page-22-0) [91](#page-23-0), [94](#page-23-0)]:

$$
\min_{w,b} \frac{1}{2} ||w||^2 + C \sum_{i=1}^m l_{0/1}(y_i(w^T x_i + b) - 1)
$$
\n(1)

where  $l_{0/1}$  is 0/1 loss function, which can measure the deviation degree and can be defined as follows:

$$
l_{0/1}(Z) = \begin{cases} 1, if Z < 0 \\ 0, otherwise \end{cases}
$$
 (2)

With the introduction of slack variables  $\xi_i$  and penalty factors C (the regularization constant), the original optimization problem can be rewritten as follows:

$$
\min_{w,b} \frac{1}{2} ||w||^2 + C \sum_{i=1}^m \xi_i
$$
  
s.t.y<sub>i</sub>(w<sup>T</sup>x<sub>i</sub>)  $\ge 1 - \xi_i$   
 $\xi_i \ge 0, i = 1, 2, ..., m$  (3)

By introducing the Lagrangian multipliers  $(\alpha_i \geq 0, u_i \geq 0)$ , the Lagrangian function is constructed to solve problems with constraints:

$$
L(w, b, \alpha, \xi, u) = \frac{1}{2} ||w||^2 + C \sum_{i=1}^m \xi_i + \sum_{i=1}^m \alpha_i (1 - \xi_i - y_i(w^T x + b)) - \sum_{i=1}^m u_i \xi_i
$$
 (4)

When the partial derivative of the above formula to W,  $b, \xi_i$  is zero, the Lagrange dual problem can be described as follows:

$$
\max_{\alpha} \sum_{i=1}^{m} \alpha_i - \frac{1}{2} \sum_{i=1}^{m} \sum_{j=1}^{m} \alpha_i \alpha_j y_i y_j x_i^T x_j
$$
  
s.t. 
$$
\sum_{i=1}^{m} \alpha_i y_i = 0
$$
  

$$
0 \le \alpha_i \le C, i = 1, 2, ..., m
$$
 (5)

Optimization problems with inequality constraints need to meet the following conditions.

$$
\alpha_i \ge 0, u_i \ge 0\ny_i(w^T x + b) - 1 + \xi_0 \ge 0\n\alpha_i(y_i(w^T x + b) - 1 + \xi_i) = 0\n\xi_i \ge 0, u_i \xi_i = 0
$$
\n(6)

To overcome nonlinear classification and clustering issues, it is essential to choose the appropriate kernel function  $\Phi_K(x, z)$  as a substitute for inner product to construct and solve the convex quadratic programming issue [\[16](#page-21-0), [34](#page-21-0), [47\]](#page-21-0). That means Eq. (5) becomes Eq. (7). In this way, the input data can be mapped into a high-dimensional feature spaces [[47\]](#page-21-0), as shown in Fig. 2.

$$
\min_{\alpha} \frac{1}{2} \sum_{i=1}^{m} \sum_{j=1}^{m} \alpha_{i} \alpha_{j} y_{i} y_{j} \Phi_{K}(x_{i}, x_{j}) - \sum_{i=1}^{m} \alpha_{i}
$$
\n
$$
s.t. \sum_{i=1}^{m} \alpha_{i} y_{i} = 0
$$
\n
$$
0 \le \alpha_{i} \le C, i = 1, 2, ..., m
$$
\n(7)

Then, we will obtain  $w$  and  $b$  after calculation of the optimal solution  $\alpha^*$   $(\alpha^*=(\alpha_1^*, \alpha_2^*, ..., \alpha_m^*)^T)$  by the SMO

(sequential minimal optimization) algorithm [\[73](#page-22-0)]. Finally, the classification decision function can be described as:

$$
f(x) = \sum_{i=1}^{m} \alpha_i^* y_i \Phi_K(x, x_i) + b^*
$$
 (8)

$$
b^* = y_i - \sum_{i=1}^m \alpha_i^* y_i \Phi_K(x_i, x_i)
$$
 (9)

#### 3.2 Whale optimization algorithm (WOA)

Inspired by the bubble-net attacking technique which is humpback whale's unique predation method, Mirjalili [[53\]](#page-22-0) suggested the WOA algorithm for solving and optimizing problems. Therefore, the WOA is widely used in energy, image processing and machine vision, structural optimization, management and other fields [[53\]](#page-22-0). Humpback whales like to hunt a group of krill or small fish near the water surface. They are gradually evolved a special hunting method called foam feeding, that's because they move slowly. Whale can construct a spiral path with a decreasing radius by creating bubbles for enforcing fish schools to approach the surface and then catching them [[43,](#page-21-0) [57](#page-22-0)]. WOA concept can be described as (1) encircling prey, (2) bubble-net attacking method and (3) search for prey, which are discussed in detail as follows (in order to distinguish, the bold letters in the following formula represent vectors):

#### Encircling prey

The exact position of prey cannot be easily identified; therefore, the system considers the solution of the current candidate for the target prey [\[57](#page-22-0)]. In the next step, after recognizing the best search agent  $(X^*, Y^*)$ , there is a need for the other search agents  $(X, Y)$  to upgrade their locations

Simple in high-dimensional feature spaces



Complex in two dimensions

Fig. 2 Mapping data from two dimensional to three dimensional

using Eqs.  $10$  and  $11$ . The nearby solutions around the best or optimized solution can be according to Eqs. 12 and 13 (Fig. 3).

$$
\mathbf{R} = \left| \mathbf{C} \cdot \mathbf{X}_{(t)}^* - \mathbf{X}_{(t)} \right| \tag{10}
$$

$$
\mathbf{X}_{(t+1)} = \mathbf{X}_{(t)}^* - \mathbf{A} \cdot \mathbf{R} \tag{11}
$$

$$
\mathbf{A} = 2\mathbf{a} \cdot \mathbf{r}_1 - \mathbf{a} \tag{12}
$$

$$
\mathbf{C} = 2\mathbf{r}_2 \tag{13}
$$

where A and C represent the coefficient vectors, and the value of  $A$  is restricted to [[1\]](#page-20-0). Parameter of  $a$  can be decreased from 2 to 0 in the search process, and it can be calculated by  $a=2-2t/T_{\text{max}}$  (t and  $T_{\text{max}}$  represent the current number and the maximum number of iterations, respectively). Factors  $\mathbf{r}_1$  and  $\mathbf{r}_2$  are random vectors in the range of [[1\]](#page-20-0);  $X_{(t)}$  and  $X^*_{(t)}$  denote the current whale position vector and the best whale solution vector (the possible location of the prey) in the tth iteration, respectively.

#### Bubble-net attacking method

The humpback whales and their bubble-net attacking behavior can be mathematically simulated by designing two procedures, which are shrinking encircling and spiral updating. The spiral equation is described in the following equation:

$$
\mathbf{X}_{(t+1)} = \mathbf{R}' \cdot e^{bl} \cdot \cos(2\pi l) \mathbf{X}_{(t)}^* \tag{14}
$$

where the shape of the logarithmic spiral depends on b which is a constant,  $l$  is a random vector which distributed uniformly within  $[-1,1]$ . The distances between the *i*th search agent and the target prey are presented by  ${\bf R}' = |{\bf X}^*_{(t)} - {\bf X}_{(t)}|.$ 

The shrinking encompassing mechanism and the spiral updating location have an equivalent probability to be selected by the humpback whale in the process of position updating. The process of simulation can be demonstrated as follows:

$$
\mathbf{X}_{(t+1)} = \begin{cases} \mathbf{X}_{(t+1)} = \mathbf{X}_{(t)}^* - \mathbf{A} \cdot \mathbf{R}, \text{ if } p < 0.5\\ \mathbf{R}' \cdot e^{bl} \cdot \cos(2\pi l) \mathbf{X}_{(t)}^*, \text{ if } p \ge 0.5 \end{cases}
$$
(15)

where  $p$  is an arbitrary number in the range of [[1\]](#page-20-0).

#### (3) Search for prey

In order to update the whale places during the exploration phase, the equation of the model is presented as follows:

$$
\mathbf{R} = |\mathbf{C} \cdot \mathbf{X}_{rand} - \mathbf{X}_{(t)}|
$$
  

$$
\mathbf{X}_{(t+1)} = \mathbf{X}_{rand} - \mathbf{A} \cdot \mathbf{R}
$$
 (16)

where  $\mathbf{X}_{rand}$  denotes the whale location vector which is selected randomly.

#### 3.3 Multilayer perceptron (MLP)

In this paper, ANN refers to multilayer perceptron (MLP). Multilayer perceptron (MLP) is promoted from a singlelayer perceptron. The main feature is that it has multiple neuron layers. Generally, the first layer of MLP is called the input layer, the middle layer is the hidden layer and the last layer is the output layer. MLP does not specify the number of hidden layers, so the appropriate number of hidden layers can be selected according to actual processing requirements. These hidden layers have different numbers of hidden neurons. The neurons in each hidden



Fig. 3 Different vector positions highlighting the best solutions

<span id="page-6-0"></span>

Fig. 4 Confusion matrix and performance indicators



Fig. 5 Model decision boundary before and after optimization: (a) SVM; (b) WOA-SVM

layer have the same activation function, and there is no limit to the number of neurons in each layer in the hidden layer and the output layer.

#### 3.4 The Gaussian process (GP)

GP means Gaussian process classification. The Gaussian process is a general supervised learning method for solving regression and probability classification problems. The

 $Accuracy=(TP+TN)/N$  $Precision=TP/(TP+FP)$ Recall=TP/(TP+FN)=Sensitivity  $F1-score=2(Recall \cdot Precision)/(Recall + Precision)$ Kappa= $(Accuracy - Pe)/(1-Pe)$  $Pe=[(TN+FN)\cdot (TN+FP)+(TP+FP)\cdot (TP+FN)]/N^2$ TP: true positive FN: false negative FP: false positive TN: true negative N: the number of the samples

advantages are: (1) predictions can explain observations. (2) The prediction is probabilistic, so that the empirical confidence interval can be calculated. (3) Versatility.

### 4 Modeling results and discussion

# 4.1 Evaluation criteria

The ROC (receiver operating characteristic) curve is very popular in the performance evaluation phase of ML classifiers [[86,](#page-23-0) [93,](#page-23-0) [95\]](#page-23-0). The ROC curve can be presented in a form of Cartesian coordinate system, in which FPR (falsepositive rate) and TPR (true-positive rate) represent as the horizontal axis and the vertical axis, respectively. The key indicator of performance evaluation in the ROC curve is the AUC value that is defined as the area under the ROC curve. The larger AUC values, the higher the classification accuracy of the model or the better performance. On the other hand, accuracy and Cohen's kappa can be also considered as performance indicators. The Kappa coefficient measures the effect of classification by evaluating the consistency between the prediction results of the model and the actual classification results. A normal range for results of kappa is in the range of 0–1. If this range is divided into five different classes, there are: 1) slight consistency  $(0 \sim 0.20)$ , 2) fair consistency  $(0.21 \sim 0.40)$ , 3) moderate consistency  $(0.41 \sim 0.60)$ , 4) substantial consistency  $(0.61 \sim 0.80)$  and 5) almost perfect consistency  $(0.81 \sim 1.00)$ . In addition to accuracy and Kappa, precision, recall and F1 can also be considered as performance indicators [\[86](#page-23-0), [92\]](#page-23-0). The mentioned performance indicators (accuracy, Kappa, precision, recall and F1-score) can be computed based on the confusion matrix, as shown in Fig. 4. Based on the confusion matrix, MCC also was introduced as performance indicators. Matthews correlation coefficient is an index used in machine learning to measure the classification performance. This indicator considers true positives, true negatives, false positives and false negatives. It is generally considered to be a relatively

<span id="page-7-0"></span>

Fig. 6 The whole analysis process of WOA-SVM classifier model



Fig. 7 Optimization of WOA-SVM with different population values

balanced indicator, and it can be applied even when the sample content of the two categories differs greatly. MCC is essentially a correlation coefficient that describes the actual classification and the predicted classification. Its value range is [-1,1], 1 indicates a perfect prediction of the subject, and a value of 0 indicates that the predicted result is not as good as a random prediction, -1 means that the predicted classification is completely inconsistent with the actual classification. The calculation formula is as follows:

$$
MCC = \frac{TP \times TN - FP \times FN}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}}
$$
\n(17)

# 4.2 WOA-SVM model development and validation

Main steps for constructing WOA-SVM model in predicting tunnel squeezing are as follows:

Step 1: Data preparation: The database collected from the existing literature has a total number of 114 cases. The source of the cited cases and the necessary information are listed in appendix. A. According to the most commonly used division ratio of 80%/20%, based on the Pareto principle [[64,](#page-22-0) [99](#page-23-0), [102](#page-23-0)], we randomly divide dataset into 80% training set and 20% testing set for model development and model validation, respectively [[71\]](#page-22-0).

Step 2: Initializing parameters of the SVM model. There are several main parameters in the SVM model, including the penalty parameter of the objective function  $(^{\circ}C^{\prime\prime})$ , the kernel function and the coefficient of the kernel function ("g"). The hyper-parameters " $C$ " and " $g$ " need to be optimized by WOA algorithm. In this research, the kernel function is determined with the help of the model decision boundary diagram. The SVM

<span id="page-8-0"></span>Table 3 The performance of the SVM model optimized with WOA

Type	Swarm	Accuracy	Rank	Kappa	Rank	<b>MCC</b>	Rank	Total
Training	50	0.9890		0.9820	5	0.9823	5	15
Training	80	0.9890	5	0.8606	4	0.9823	5	14
Training	100	0.9890	5	0.9820	5	0.9823	5	15
Training	150	0.9890	5	0.9820	5	0.9823	5	15
Training	200	0.9890	5	0.9820	5	0.9823	5	15
Testing	50	0.9565	5	0.9288	5	0.9316	4	14
Testing	80	0.9130	4	0.8606	$\overline{4}$	0.8633	3	11
Testing	100	0.9565		0.9288	5	0.9317	5	15
Testing	150	0.9565	5	0.9288	5	0.9317	5	15
Testing	200	0.9130	4	0.8606	4	0.8633	3	11



Fig. 8 Confusion matrix different prediction methods: a WOA-SVM; b ANN; c SVM; and d GP

Predicted

Measured

15

20

Predicted

Measured

 $\overline{20}$ 

**ANN** 

10

Samples

**SVM** 

Classes

 $\mathcal{C}$ 

Classes

<span id="page-9-0"></span>

Fig. 9 Actual and predicted classification results on test datasets

Table 4 Performance of different classifiers for the non-squeezing problems, minor squeezing problems and high squeezing problem

	Precision	Recall	F <sub>1</sub> -score	Precision	Recall	F <sub>1</sub> -score
	WOA-SVM			<b>ANN</b>		
<b>NS</b>	0.86	1.00	0.92	0.86	1.00	0.92
MS	1.00	0.80	0.89	0.80	0.80	0.80
<b>SES</b>	1.00	1.00	1.00	1.00	0.92	0.96
<b>SVM</b>				GP		
<b>NS</b>	1.00	0.67	0.80	1.00	0.33	0.50
MS	0.00	0.00	0.00	0.00	0.00	0.00
<b>SES</b>	0.63	1.00	0.77	0.55	0.92	0.69

model transforms the linearly inseparable problem into linearly separable with the help of the kernel functions

like linear, polynomial, radial basis function (RBF), and sigmoid. According to the model decision boundary diagram in Fig. [5,](#page-6-0) it is easy and feasible to detect that the database in this article is close to linearly separable. Therefore, the linear kernel was applied to input parameter mapping for the SVM model.

 $\overline{10}$ 

Samples

 $\overline{1}$ 

Step 3: The relevant parameters of the WOA and their ranges are the constant b, two random number  $l \in [-1, 1]$ and  $r \in [0, 1][0, 1]$ . It is necessary to determine and design the optimal hyper-parameters (C and g) of SVM using the WOA. Therefore, a WOA-SVM hybrid model can optimize the ability of the SVM classifier in predicting tunnel squeezing through WOA algorithm. The specific optimization process of the proposed WOA-SVM is shown in Fig. [6.](#page-7-0)

<span id="page-10-0"></span>

Fig. 10 ROC curves and AUC values for different individual classifiers: a non-squeezing problems; b minor squeezing problems; c severe-to-extreme squeezing problems



Fig. 11 Taylor graph a test sets, **b** train sets

Step 4: Fitness evaluation of WOA-SVM model and determination of the optimal population size. It is necessary for developing a reliable WOA-SVM model with the best performance to fix the optimal population number. This is because swarm size has a significant impact on the performance of the WOA model. To search the optimal population number, five different swarm sizes (i.e., 50, 80, 100, 150 and 200) were selected and used in the process of model development. The fitness curve presented in Fig. [7](#page-7-0) shows that the adaptation value changes with the number of iterations. When the number of iterations is greater than or equal to 80, the fitness values of the five fitness curves generated by the WOA-SVM model will tend to be stable. Table [3](#page-8-0) presents the results of performance evaluation (accuracy and Kappa) for the optimization WOA-SVM model based on the training and testing sets. Based on this table and considering all performance indexes, the optimal population or swarm size was selected as 150 with accuracy  $= 0.9565$  and Kappa  $= 0.9288$ .

<span id="page-11-0"></span>

Fig. 12 The violin chart presented for different classifier models

# 4.3 Analysis and comparison of classification performance

The optimized classifier model based on the training set needs to be validated based on testing datasets. The test datasets were randomly selected from the database prepared, i.e., 20% of the total cases (23 test samples). It is important to mention that they have not participated in the training process of the model. We will analyze and compare classification performance from different perspectives such as confusion matrix, performance evaluation indicators, violin graphs and so on. From the confusion matrix, we can get the accuracy, Kappa, MCC and other performance evaluation indicators and use then analyzing and comparing the classification performance of different models on the basis of these evaluation indicators. To examine the accuracy of the WOA-SVM model, the methods of GP, ANN and SVM were built for classification purpose of the same samples. The results of the verification are shown in Fig. [8,](#page-8-0) which represents the confusion matrix of four classification models (WOA-SVM, SVM, ANN and GP) for testing datasets. It is not difficult to observe that the WOA-SVM classifier demonstrates better performance than the other built models. Compared with the other unoptimized classifier models, the WOA-SVM classification model has the highest accuracy (approximately 0.9565). In addition, the Kappa values obtained for different classifiers from high to low are: 0.929 (WOA-SVM), 0.913 (ANN), 0.696 (SVM) and 0.565 (GP). In addition to accuracy and Kappa mentioned above, the number of cases classified correctly can be obtained from the main diagonal of the confusion matrix.

The above analysis has shown that the WOA-SVM model has certain advantages. In order to present the difference between measured tunnel squeezing results and the



Fig. 13 Variable contribution analysis: a overall analysis; b analysis of variables for non-squeezing problems, minor squeezing problems, and high squeezing problem

predicted ones obtained from different classifiers, the resultant classification results are demonstrated in Fig. [9.](#page-9-0) We can see the 23 samples of the test dataset on the horizontal axis and the class of the sample on the vertical axis (class0: non-squeezing; class1: minor squeezing; class2: severe-to-extreme squeezing). There is a sample with the actual class: class 1 in Fig. [9a](#page-9-0), which was misclassified as class 0, and this sample was defined as case No. 20. However, there are more than one sample in Fig. [9](#page-9-0) (b, c and d), which was misclassified. The WOA-SVM model is more accurate and safer in predicting the level of tunnel squeezing.

The above analysis aims to evaluate the classification performance of the model as a whole. However, imbalanced dataset may have a great impact on the prediction results of the model, but it is not enough to detect this influence based on the accuracy rate alone. Therefore, precision, recall, F1 and ROC curves were also applied and calculated to assess the prediction performance of WOA-SVM, SVM, ANN and GP models. Table [4](#page-9-0) tabulates precision, recall and F1-score of different classification models based on non-squeezing (NS), minor squeezing (MS) and severe-to-extreme squeezing(SES). According to this table, the WOA-SVM model was able to receive a better

<span id="page-12-0"></span>

Feature	Value
$\mathbf{g}$	0.77
$\overline{\mathrm{H}}$	276.00
I)	5.00
	$0.\overline{25}$
K	940.00

Fig. 14 Probabilistic interpretation of the non-squeezing category



Fig. 15 Probabilistic interpretation of the minor squeezing category

performance and higher level of accuracy. Based on the above analysis, for the optimized ML classifier, the classification performance of the optimized SVM model was significantly improved compared to the base model which is SVM.

ROC curves and AUC values of different individual classifiers for different classes are shown in Fig. [10.](#page-10-0) According to Fig. [10a](#page-10-0), the AUC values based on the class 0 were calculated as 1, 0.99, 0.78, 0.93 and 0.94 for WOA-SVM, ANN, GP and SVM approaches, respectively. Figure [10](#page-10-0)b and c demonstrates AUC values of different classifiers based on class 1 and class 2, respectively. The specific values can be obtained from the figure. In Fig. [10,](#page-10-0) the AUC values obtained from the WOA-SVM model based on class 0, class 1 and class 2 are 1, 0.93 and 1, respectively. Obviously, the WOA-SVM model is the preferred ML classifier for squeezing degree prediction.

In order to understand the capability of our proposed model better, we have drawn Taylor graph for train and test sets separately, as shown in Fig. [11](#page-10-0). Taylor chart is often

 $|0.74$ 

<span id="page-13-0"></span>

Fig. 16 Probabilistic interpretation of the high squeezing category

used to evaluate the accuracy of a model. Commonly used accuracy indicators are MCC, standard deviation and rootmean-square error (RMSE). Generally speaking, the scattered points in the Taylor diagram represent the model, the radial line represents the MCC, the horizontal and vertical axis represents the standard deviation and the dashed line represents the root-mean-square error. The Taylor chart is a change from the previous scatter chart, which can only show two indicators to express the accuracy of the model. Similarly, we still can see that the WOA-SVM model is the preferred ML classifier for squeezing degree prediction.

The above analysis is based on the test set. Below we will analyze and compare the performance of the model based on all the sample data in this article. The violin chart includes a combined specifications of the box plot and the kernel density plot. The main application of this chart is to present the probability density and distribution of datasets. Figure [12](#page-11-0) shows the distribution and probability density of prediction accuracy for different classifier models considering all 114 samples. The prediction accuracy of WOA-SVM model is higher than the other classification models, and the distribution of accuracy is more concentrated, which sufficiently illustrates that the hybrid model (WOA-SVM) has visible advantages in squeezing prediction.

#### 4.4 Sensitivity analysis of predictor variables

The key to predicting tunnel squeezing is the selection of appropriate input parameters. The research of Huang et al. [\[35](#page-21-0)] showed that the coupling effect of different parameters has different effects on tunnel squeezing prediction.

Therefore, it is particularly important to evaluate the contribution of input parameters to the developed model. The Shapley Additive Explanations was used to obtain the importance of predictive variables to WOA-SVM classification model. The calculation formula is shown as [\[99](#page-23-0)]:

$$
\Phi_i = \sum_{S \subseteq N/(i)} \frac{|S|!(|N|-|S|-1)!}{|N|!} [q_{s \cup i}(x_{s \cup i}) - q_s(x_s)] \tag{18}
$$

where  $N$  represents the set of all features in the data set,  $S$  is the set after index  $i$  is removed, the importance of feature  $i$ to the model output is represented by  $\Phi_i$ ,  $x_s$  represents the vector of input features in set S, and the contribution of features is calculated with the corresponding function q.

In practical applications, the prediction results based on the predictor variables with high contribution rates to model are more reliable and accurate. There are five features in this work, and the importance of predictor variables to the WOA-SVM classification model was calculated (Fig. [13\)](#page-11-0). It can be intuitively seen that the percentage strain  $(\varepsilon)$  is the most important parameter in predicting tunnel squeezing, followed by K and H parameters. Due to the imbalance dataset of this article, the contribution of the parameters to model based on different types of data (class0, class1 and class2) was assessed (Fig. [13b](#page-11-0)) According to Fig. [13](#page-11-0),  $\varepsilon$  is still the most influential parameter on the model for all classes. However, for class 1 and class 2, the parameter K ranks second only to  $\varepsilon$ in the contribution rate rankings, followed by H. For class 0, the parameter H ranks second only to  $\varepsilon$ , followed by K. In summary, the parameters that have important contribution to the WOA-SVM model are: e, K, H and D.

In order to verify the above conclusions, we randomly selected a sample from three different classes, and the probabilistic interpretation of the sample is given in Figs. [14–](#page-12-0)[16.](#page-13-0) That means that Figs. 14, 15 and 16 demonstrate that the five parameters  $(\varepsilon, K, D, O, A)$  have different contributions to the prediction of class0, class1 and class2. Figure [14](#page-12-0) presents the process of the sample selected was considered class0 by WOA-SVM model according to input parameters. According to the information in Fig. [14,](#page-12-0) it can be easily observed that the probabilities of the sample to class0, class1 and class2 are 0.69, 0.24 and 0.07, respectively. Therefore, the final prediction result is class0 (light squeezing problem), and parameters e, H and K are decisive predictor variables, where e plays a decisive role in the prediction results.

Similarly, Fig. [15](#page-12-0) displays the process of the sample selected was judged to be class1. The sample will be judged to be class0, class1 and class2 with corresponding probability of 0.09, 0.52 and 0.39, respectively. Finally, this sample is considered as class1 (moderate squeezing problem). The decisive predictor variables are different from that presented in Fig.  $14$ , and they are  $\varepsilon$ , H and D. Nevertheless, parameters  $\varepsilon$  still has the deepest effect on the proposed model. Figure [16](#page-13-0) demonstrates that the sample will be regarded as class0, class1 and class2 with corresponding probability of 0.05, 0.28 and 0.67, respectively. Obviously, this sample is ultimately considered as class2 (high squeezing problem), and the percentage strain  $(\varepsilon)$  is the most important parameter for predicting tunnel squeezing, followed by the parameters K and H. In other words, Figs. 14, 15 and 16 illustrate that the parameters  $\varepsilon$ , K, H and D have a considerable impact on the WOA-SVM model, while  $\varepsilon$  is the most important input parameter among them.

# 5 Conclusion

We proposed an optimized classifier model (WOA-SVM) to estimate the potential of tunnel squeezing according to 114 cases. There were five input parameters (H, K, D, Q and  $\varepsilon$ ) considered in the modeling of all ML models in this study (WOA-SVM, ANN, SVM and GP). In order to assess the performance of different classifier models based on the same database, accuracy, kappa, precision, recall, F1-score

and the AUC were calculated. The aim of the sensitivity analysis of predictor variables is to evaluate the contribution of input parameters to the model. The main results of this study are summarized as follows.

- (1) The WOA algorithm can effectively optimize the hyper-parameters of the SVM classifier and improve its classification performance. The WOA-SVM classification model has the highest accuracy (approximately 0.9565) than other un-optimized individual classifiers (SVM, ANN and GP). However, the model has a good classification effect, even if the data are unbalanced.
- (2) The results of the sensitivity analysis indicate that e, H and K are the best combination of parameters for WOA-SVM model, where the percentage strain  $(\varepsilon)$  is the most influential factor on the WOA-SVM model, the parameter K ranks second only to  $\varepsilon$  in the contribution rate rankings, followed by H.

So far, most of the existing forecasting methods can distinguish between squeezing and non-squeezing. This article refers to the multi-class SVM proposed by Sun et al. [\[71](#page-22-0)] and introduces the whale optimization algorithm to optimize the prediction performance of the multi-class SVM. Therefore, the WOA-SVM model has higher prediction accuracy than empirical methods, ordinary binary SVM and multi-class SVM and can predict the severity of tunnel squeezing. However, compared with numerical simulation, the influencing factors considered by this paper are obviously limited. In addition, in the actual construction process, it is difficult to obtain more accurate input parameter values. According to the research of Zhang et al. [73,74], the prediction performance of the classifier ensemble model is higher than that of the individual classifier. In future, other advanced single classifiers can be introduced to construct a classifier ensemble. On this basis, the introduction of suitable optimization algorithms can greatly improve the prediction accuracy of the model. In addition, expanding the existing database can improve the generalization ability of the integrated model.

#### Appendix

See Table [5](#page-15-0).

<span id="page-15-0"></span>Table 5 Performance of different classifiers at many problems in minor change

No	Tunnel		Location Rock type	H(m)	Q	D(m)	K(MPa)	$\varepsilon$ (%)	Reference	Class
1	<b>Bhutan</b>	Bhutan	AGO (adverse geological)	337.000	0.007	6.800	44.760	2.100	Sripad et al. [70]	MS
$\overline{c}$	Chameliya hydroelectric project	Nepal	Dolomite	199.700	0.020	5.400	1217.160	4.580	Basnet [10]	<b>SES</b>
	headrace tunnel $3 + 172$									
3	Chameliya hydroelectric project	Nepal	Dolomite	217.500	0.013	5.400	1217.160	25.540	Basnet $[10]$	<b>SES</b>
	Headrace tunnel $3 + 190$									
4	Chameliya hydroelectric project	Nepal	Brownish	252.200	0.010	5.400	1523.070	12.500	Basnet $[10]$	<b>SES</b>
	Headrace tunnel $3 + 296$									
5	Chameliya hydroelectric project	Nepal	Foliated phyllite	246.300	0.010	5.400	1523.070	3.800	Kumar [10]	<b>SES</b>
	Headrace tunnel $3 + 314$									
6	Chameliya hydroelectric project	Nepal	Talcose phyllite	283.900	0.008	5.400	1645.380	36.730	Basnet $[10]$	<b>SES</b>
	headrace tunnel $3 + 404$									
7	Chameliya hydroelectric project	Nepal	Talcose phyllite	284.500	0.008	5.400	1828.980	30.190	Basnet $[10]$	<b>SES</b>
	Headrace tunnel $3 + 420$									
8	Chameliya hydroelectric project	Nepal	Talcose phyllite	210.800	0.010	5.400	1575.720	18.300	Kumar $[44]$	<b>SES</b>
	Headrace tunnel $3 + 681$									
9	Chameliya hydroelectric project	Nepal	Talcose phyllite	237.700	0.010	5.400	1575.720		10.960 Basnet [10]	<b>SES</b>
	Headrace tunnel $3 + 733$									
10	Chameliya hydroelectric project	Nepal	Foliated phyllite	230.000	0.015	5.400	1217.160		9.800 Basnet [10]	<b>SES</b>
	Headrace tunnel $3 + 764$									
11	Chameliya hydroelectric project	Nepal	Foliated phyllite	222.600	0.015	5.400	1217.160	1.200	Basnet [10]	MS
	Headrace tunnel $3 + 795$									
12	Chenani-Nashri escape tunnel	India	Siltstone, silty claystone	727.000	2.287	6.000	5.880	1.700	Kumar [44]	MS
13	Chenani-Nashri escape tunnel	India	Siltstone, silty claystone	733.000	2.903	6.000	6.250	1.600	Kumar [44]	MS



Table 5 (continued)

Table 5 (continued)





Table 5 (continued)

Table 5 (continued)



<span id="page-20-0"></span>Table 5 (continued)

No	Tunnel		Location Rock type	H(m)	Q	D(m)	K(MPa)	$\varepsilon$ (%)	Reference	Class
102	Tala HRT, Bhutan	Bhutan	amphibolites and quartzites in thin bands	337.000	0.080	6.800	14.090	2.200	Sripad et al. [70]	<b>MS</b>
103	Tala HRT, Bhutan	Bhutan	occurrences):	337.000	0.011	6.800	16.050	3.800	Sripad et al. [70]	<b>SES</b>
104	Tala HRT, Bhutan	Bhutan	completely sheared,	337.000	0.006	6.800	22.580	3.100	Sripad et al. [70]	<b>SES</b>
105	Tala HRT, Bhutan	Bhutan	highly weathered biotite schist	337.000	0.006	6.800	36.360	2.200	Sripad et al. [70]	<b>MS</b>
			associated with banded gneiss,							
106	Tehri dam project	India	Argillaceous phyllite	220.000	0.800	12.000	32.890	0.380	Goel et al. $[28]$ ; Singh et al. $[69]$	<b>NS</b>
107	Udhampur rail tunnel (T1)	India	Claystone, silty claystone	300.000	0.033	6.500	10.000	3.000	Kumar [44]	<b>SES</b>
108	Udhampur rail tunnel (T1)	India	Claystone, silty claystone	280.000	0.031	6.500	11.540	2.600	Kumar $[44]$	<b>SES</b>
109	Udhampur rail tunnel (T1)	India	Claystone, silty claystone	280.000	0.042	6.500	12.500	2.400	Kumar $[44]$	<b>MS</b>
110	Udhampur rail tunnel India (T1)		Claystone, silty claystone	285.000	0.063	6.500	12.800	2.500	Kumar $[44]$	<b>SES</b>
111	Udhampur rail tunnel India (T1)		Claystone, silty claystone	270.000	0.125	6.500	15.910	2.200	Kumar [44]	<b>MS</b>
112	Udhampur rail tunnel (T1)	India	Claystone, silty claystone	280.000	0.083	6.500	29.330	1.500	Kumar $[44]$	<b>MS</b>
113	Udhampur rail tunnel (T1)	India	Claystone, silty claystone	312.000	0.094	6.500	34.670	1.500	Kumar [44]	<b>MS</b>
114	Upper Krishna project	India	<b>Banded</b> schists	52.000	15.000	13.000	16.670	0.180	Goel et al. [28]; Singh et al. $[69]$	<b>NS</b>

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