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# **Preliminary analysis of earthquake probability based on the synthetic seismic catalog**

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**Abstract** The analysis of seismic hazards relies on the statistical analysis of historical seismic data and the instrumental seismic catalog to obtain the regional earthquake recurrence interval and earthquake probability. The accuracy of analysis thus depends strongly on the completeness of the seismic data used. However, available seismic catalogs are too short or incomplete for the reliable analysis of the statistical characteristics of earthquakes. If a long-term synthetic seismic catalog can be generated using a physics-based numerical simulation, and the simulation results match the crustal deformation, seismicity, and other observations, then such a synthetic catalog helps us to further understand the characteristics of seismic activity and analyze the regional seismic hazard. In this paper, taking the northeastern Tibetan Plateau as a case study, we establish a three-dimensional visco-elastoplastic finite-element model to simulate earthquake cycles and the spatiotemporal evolution of earthquakes on the model fault system and obtain a seismic catalog on a time scale of tens of thousands of years. On the basis that the model satisfies the regional geodynamics of the northeastern Tibetan Plateau, we analyze seismicity on the northeastern Tibetan Plateau using the simulated synthetic earthquake catalog. The characteristics of earthquake recurrence at different locations and different magnitudes, and the long-term average probability of earthquake occurrence within the fault system on the northeastern Tibetan plateau are studied. The results are a reference for regional seismic hazard assessment and provide a basis for the physics-based numerical prediction of earthquakes.

**Keywords** Synthetic seismic catalog, Seismic hazard, Recurrence interval of earthquakes, Earthquake probability, Northeastern Tibetan Plateau

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## **1. Introduction**

Mainland China faces a serious hazard in the form of earthquakes. Earthquakes frequently occur, with great intensity and wide distribution, resulting in severe damage in mainland China [\(Chen, 2009](#page-12-0); [Zhang et al., 2013\)](#page-13-0). In the 20th century, nearly half (~590000) of the world's deaths resulting from earthquakes  $(\sim 1200000)$  were in China [\(Zhang et al.,](#page-13-1)

[2005;](#page-13-1) [Ma et al., 2007](#page-12-1); [Chen, 2009](#page-12-0)). It is, therefore, of great practical and social importance for China to explore and analyze earthquake predictions.

Since the Xingtai earthquake struck in 1966, China has been carrying out large-scale earthquake prediction research in a planned manner [\(Zhang et al., 2005;](#page-13-1) [Huang et al., 2017](#page-12-2); [Shi et al., 2018\)](#page-13-2). Most earthquake prediction methods are presently empirical, and this situation is expected to continue for the foreseeable future ([Shi et al., 2018\)](#page-13-2). However, for more than half a century, there has been no remarkable

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breakthrough in the empirical prediction of earthquakes [\(Shi](#page-13-2) [et al., 2018](#page-13-2)). Although the 1975 Haicheng earthquake was successfully predicted, there were no advance forecasts of the subsequent Tangshan earthquake in 1976 and the Wenchuan earthquake in 2008. Internationally, the United States, Japan, and other countries have planned programs of earthquake prediction research ([Press and Brace, 1966;](#page-13-3) [Ha](#page-12-3)[giwara and Rikitake, 1967](#page-12-3)) and have explored the use of several observation methods, such as those based on re-sponses of the gravity field [\(Kisslinger, 1975\)](#page-12-4), geomagnetic field [\(Rabeh et al., 2009](#page-13-4)), geoelectricity ([Zhao and Qian,](#page-13-5) [1994](#page-13-5)), streamflow and water wells ([Montgomery and Man](#page-12-5)[ga, 2003\)](#page-12-5) and geochemical methods ([Grant et al., 2011\)](#page-12-6). However, the difficulties of earthquake prediction were far beyond expectations. In particular, the Parkfield Earthquake Prediction experiment in the United States failed; i.e., scientists predicted that an earthquake would strike around 1988 and by 1993 at the latest, yet the earthquake did not strike until September 28, 2004, at a magnitude of  $M_w$ 6.0. This failure resulted in the practice of earthquake prediction being questioned for a long time. Some researchers, therefore, hold the view that earthquakes are unpredictable ([Geller, 1997;](#page-12-7) [Geller et al., 1997\)](#page-12-8). However, most researchers, including those who believe that earthquakes cannot be predicted deterministically, still insist that earthquakes can be predicted probabilistically. [Shi et al. \(2018\)](#page-13-2) pointed out that, strictly speaking, natural-science forecasting is always probabilistic forecasting, with deterministic forecasting being the special case that the probability approximates 100%.

Internationally, the earliest and most famous systematic regional earthquake probabilistic model was proposed by the Working Group on California Earthquake Probabilities in the United States [\(Working Group on California Earthquake](#page-13-6) [Probabilities, 1988\)](#page-13-6) and applied to the San Andreas fault system for probabilistic seismic hazard analysis; the group then developed the Uniform California Earthquake Rupture Forecast (UCERF) system [\(Field et al., 2014\)](#page-12-9). The UCERF system calculates regional earthquake probabilities for different earthquake magnitudes in a certain time window. This system, to some extent, covers long-term, mid-term and, short-term earthquake probability prediction. Although the UCERF system is the best model for earthquake probability prediction in California, it still has problems. As an example, the number of unknowns in the inversion is much larger than the number of equations (i.e., there are 22000 unknowns versus 2630 equations). There is thus no unique solution for this model; i.e., there are still many subjective factors affecting the quality of the results ([Shi et al., 2018](#page-13-2)). Italy developed the Operational Earthquake Forecast system following the 2009  $M_w$ 6.3 Laquila earthquake ([Jordan et al.,](#page-12-10) [2011](#page-12-10)). This system provides a spatial map of the earthquake probability for different earthquake magnitudes in a certain future time window in monitoring areas and provides an earthquake probability forecast continuously updated according to real-time seismic data. Chinese scholars have used a variety of probability models to analyze the earthquake probability in China. As an example, the fifth Generation Seismic Zonation Map of China is currently combined with maps of active faults and potential seismic zones in probabilistic seismic hazard analysis, providing a new means of probabilistic seismic hazard analysis that considers the nonuniform spatial distribution of intraplate earthquakes [\(Hu, 2001](#page-12-11); [Gao, 2015](#page-12-12)). [Jiang and Wu \(2008\)](#page-12-13) used a predictive model of earthquake physics based on the statistical mechanics of complex systems, namely the Pattern Informatics (PI) model, to estimate the probability of future earthquakes in the Sichuan-Yunnan region and conducted a retrospective forecast test of the PI model using data of earthquakes that had struck since 1988 in the region. They then explored the possibility of applying this model to the estimation of the time-dependent seismic hazard in continental China. [Wen \(1998\)](#page-13-7) analyzed the time-dependent probability of earthquakes in the Sichuan-Yunnan region. [Rong and Jackson \(2002\)](#page-13-8) applied a smoothed seismicity method to intraplate regions and estimated the long-term earthquake potential in mainland China. Most of these studies were based on the recorded seismic catalog for prediction of the probability of future earthquakes in a region, and the results thus strongly depended on the timespan and the completeness of seismic magnitude information of the recorded seismic catalog. A more extended and more complete seismic catalog would provide more reliable results of modeling. Therefore, a seismic catalog containing a longer timespan can help us fully understand the characteristics of seismicity, and analyze the earthquake probability and regional seismic hazards. However, available seismic catalogs are mainly based on historical and instrumental records. The accuracies of the locations and magnitudes of historical earthquakes are relatively low, and there are often omissions, especially in sparsely populated areas. Modern instrumental seismic observations have only been developed over the last 100 years. Relative to the recurrence interval of hundreds or even thousands of years for large earthquakes in mainland China, this recording time is too short. Using an instrumental seismic catalog spanning only 100 years or even decades as primary data to calculate earthquake probabilities and analyze regional seismic hazards is obviously not enough. A synthetic long-term seismic catalog can largely make up for the shortcomings (i.e., being too short or incomplete) of an available seismic catalog. It is, therefore, important that we can synthesize a long-term seismic catalog for seismic tectonic research and seismic hazard analysis.

Many studies have investigated the simulation of synthetic seismic catalogs and proposed and developed various models, such as the Burridge-Knopoff model [\(Burrideg and](#page-12-14)

[Knopoff, 1967\)](#page-12-14), cellular automata model [\(Wolfram, 1984](#page-13-9)) and synthetic seismicity simulation models ([Ward, 1992;](#page-13-10) [Robinson and Benites, 1996;](#page-13-11) [Ben-Zion et al., 2003](#page-12-15); [Zhou,](#page-13-12) [2008](#page-13-12)). These studies are essential to the theoretical analysis of seismicity and the preliminary analysis of the regional seismic hazard. However, the studies were mainly based on two-dimensional, single-fault models, which are inadequate to use for a real complex multi-fault system. The finite-element method can be adopted to establish a geological model that is closer to reality.

In this study, taking the northeastern Tibetan Plateau as an example, we establish a three-dimensional visco-elastoplastic finite-element model and simulate earthquake cycles and the spatiotemporal evolution of the earthquake sequence (i.e., the synthetic seismic catalog) on the fault system in this region. We analyze the characteristics of earthquake recurrence and earthquake probability for different magnitudes and different locations along faults, using the synthetic seismic catalog and available earthquake data. The results obtained in this paper provide a reference for seismicity, the characteristics of earthquake recurrence, and an assessment of the long-term seismic hazard in the northeastern Tibetan Plateau and provide a basis for the numerical forecasting of earthquakes based on physical principles.

#### **2. Tectonic background**

The northeastern Tibetan Plateau is located at the junction of the Tibet, Ordos, and Alxa blocks [\(Zhang et al., 1988;](#page-13-13) [Burchfiel et al., 1991\)](#page-12-16); it is one of the most seismically active regions in mainland China ([Tapponnier and Molnar, 1977;](#page-13-14) [Zhang et al., 1988\)](#page-13-13) with several active faults, such as Haiyuan fault, Xiangshan-Tianjingshan fault, Helanshan fault, and Luoshan fault [\(Figure 1](#page-2-0)). Over the past several hundred years, there have been six major earthquakes with magnitude  $M \ge 7$  in this region: the  $M7\frac{1}{4}$  Luoshan earthquake occurred on the Luoshan fault in 1561; the *M*7 Guyuan North earthquake occurred on the Yunwushan-Xiaoguanshan fault in 1622; the *M*7.5 Zhongwei earthquake occurred on the Xiangshan-Tianjingshan fault in 1709; the *M*8 Pingluo earthquake occurred on the Helanshan fault in 1739; the *M*8.5 Haiyuan earthquake occurred on the Haiyuan fault in 1920; and the *M*8 Gulang earthquake occurred on the Xiangshan-Tianjingshan fault in 1927 [\(Figure 1](#page-2-0)). These major earthquakes occurred on major faults in this region ([Figure 1](#page-2-0)). Researchers have carried out a large number of seismic, geological, geophysical studies, etc. in this region ([Zhang et al., 1988](#page-13-13); [Min et al., 2000](#page-12-17); Zhang et al., 2005; [Liu-](#page-12-18)[Zeng et al., 2007](#page-12-18); Wang et al., 2012; [Zheng et al., 2013\)](#page-13-15). These fundamental researches provide important constraints for the study of geodynamic numerical simulation.



<span id="page-2-0"></span>**[Figure 1](#page-2-0)** Tectonic background in the northeastern Tibetan Plateau. Red circles show regional historical earthquakes. Earthquake data are taken from the literature (Institute of Geology, China Earthquake Administration and Ningxia Bureau of China Earthquake Administration, 1990).

#### **3. Finite-element model**

We set up a three-dimensional finite-element model and simulate earthquake cycles in the northeastern Tibetan Plateau. The basic codes used in this study have been successfully applied in many regions [\(Luo and Liu, 2010](#page-12-19), 2012; [Sun and](#page-13-16) [Luo, 2018](#page-13-16); [Yin et al., 2018;](#page-13-17) [Sun et al., 2019\)](#page-13-18); the reliability of this codes has been verified. We then describe the model setting in the following sections.

#### **3.1 Model setup**

[Figure 2](#page-3-0) shows the finite-element model in the northeastern Tibetan Plateau. The length and width are both 500 km in the model, and the depth is 100 km. The model consists of two rheological layers: a 20 km thick, elasto-plastic upper crust (the faults embedded in the upper crust are simulated by 2 km thick, strain-softening material), and an 80 km thick, visco-elastic lower crust and upper mantle layer.

The setting of the model parameters is based on the results of previous researches. The Young's modulus and Poisson's ratio for the elasto-plastic layer are  $8.75 \times 10^{10}$  Pa and 0.25, respectively. The cohesion and internal frictional angle for the crust of the Tibetan Plateau are 20 MPa and 15°, respectively; while the cohesion and internal frictional angle are 30 MPa and 25° for the crust of the Alxa block and the Ordos block. Since the strength of the fault system is relatively weak, the cohesion and internal frictional angle are set as 10 MPa and 5°, respectively ([Turcotte and Schubert, 1982](#page-13-19); [Li et al., 2009;](#page-12-20) [Luo and Liu, 2010](#page-12-19); [Sun and Luo, 2018\)](#page-13-16). The Young's modulus and Poisson's ratio for the lower crust and



<span id="page-3-0"></span>**[Figure 2](#page-3-0)** Finite-element model and fault system in the model. (a) Mesh and boundary conditions of the model for the northeastern Tibetan Plateau. Lateral boundary conditions are determined by the interpolation of Global Positioning System data [\(Gan et al., 2007](#page-12-21)). (b) Fault system in the model. HLSF, Helanshan fault; HHF, Huanghe fault; LSF, Luoshan fault; NSSF, Niushoushan fault; YTSF, Yantongshan fault; XTF, Xiangshan-tianjingshan fault; YXF, Yunwushan-xiaoguanshan fault; HYF, Haiyuan fault.

upper mantle layer are  $8.75 \times 10^{10}$  Pa and 0.25, respectively (Turcotte and Schubert, 1982; [Luo and Liu, 2010;](#page-12-19) [Sun and](#page-13-16) [Luo, 2018\)](#page-13-16). The viscosity for the lower crust and upper mantle of the Tibetan Plateau is  $1 \times 10^{20}$  Pa·s, while the value is  $1\times10^{23}$  Pa s for the lower crust and upper mantle of the Ordos block and the Alxa block [\(Zang et al., 2005;](#page-13-20) [Xiao and](#page-13-21) [He, 2015\)](#page-13-21).

In this study, we use the GPS data [\(Gan et al., 2007](#page-12-21)) which revealed the velocity field relative to the stable Eurasian plate during 1998–2004, and interpolate the velocity field to the lateral boundaries in our model. We use the velocities multiply the loading time steps as the displacement boundary conditions in the model. We assume the lateral boundary conditions of the model do not change with depth, and this is also used in many other studies [\(Luo and Liu, 2010](#page-12-19); [Zhu and](#page-13-22) [Zhang, 2013](#page-13-22); [Xiao and He, 2015](#page-13-21); [Pang et al., 2019](#page-13-23)). The upper surface is set for free, and the bottom surface can move freely horizontally but fixed vertically.

#### **3.2 Governing equations**

The model simulates lithospheric deformation by solving the static equation of force equilibrium:

$$
\frac{\partial \mathbf{\sigma}_{ij}}{\partial x_j} + f_i = 0,\tag{1}
$$

where  $\sigma_{ij}$  is stress tensor (*i*, *j*=1, 2, 3),  $f_i$  is body force.

Our model calculates strain increments in each time step; and the strain increment consists of viscous, elastic, and plastic components:

$$
\{d\varepsilon\} = \{d\varepsilon^{\nu}\} + \{d\varepsilon^{\rho}\} + \{d\varepsilon^{\rho}\},\tag{2}
$$

where  ${de^v}$ ,  ${de^e}$  and  ${de^p}$  represent viscous strain com-

ponent, elastic strain component, and plastic strain component, respectively. {} represents a tensor.

The model follows the Maxwell linear visco-elastic deformation when the stresses do not reach the yield strength. The visco-elastic constitutive relation can be written as:

$$
\begin{aligned} \{\mathrm{d}\varepsilon^{\nu}\} &= [\mathbf{Q}]^{-1} \{\boldsymbol{\sigma}^{\iota}\} \mathrm{d}t = [\mathbf{Q}]^{-1} \{\{\boldsymbol{\sigma}^{\iota-\mathrm{d}t}\} + \{\mathrm{d}\sigma\}\} \mathrm{d}t, \\ \{\mathrm{d}\varepsilon^{\varepsilon}\} &= [\mathbf{D}]^{-1} \{\mathrm{d}\sigma\}, \end{aligned} \tag{3}
$$

where  $\{\sigma^t\}$  is the stress tensor at model time *t*, d*t* is the time increment,  $\{d\sigma\}$  is the increment stress tensor, [D] and [Q] represent the elastic and viscous material matrices, respectively.

When the model stresses reach the yield strength, the plastic deformation occurs.

The Drucker-Prager yield criterion is used:

$$
F(\sigma, C) = \sqrt{J_2} - \alpha I_1 - \beta,
$$
  
\n
$$
\alpha = \frac{2\sin\varphi}{\sqrt{3}(3 + \sin\varphi)},
$$
  
\n
$$
\beta = \frac{6C\cos\varphi}{\sqrt{3}(3 + \sin\varphi)},
$$
\n(4)

where  $I_1$  is the first invariant of stress tensor,  $J_2$  is the second invariant of deviatoric stress tensor, *α* and *β* are parameters of the Drucker-Prager criterion that related to cohesion (*C*) and internal frictional angle (*φ*).

Since the plastic shear strain increment of the model material is much larger than the plastic volume strain increment, the non-associated flow law is adopted ([Chen, 2007;](#page-12-22) [Sun and](#page-13-16) [Luo, 2018](#page-13-16)). The plastic strain increment can be written as:

$$
\{d\varepsilon^p\} = d\lambda \left\{\frac{\partial G}{\partial \sigma}\right\},\tag{5}
$$

 $\sigma$ 

where  $d\lambda$  is the plastic multiplier.

Three-dimensional visco-elasto-plastic constitutive relation is given as:

$$
\{\mathrm{d}\sigma\} = \left(\left[\widetilde{\mathbf{D}}\right] - \left[\mathbf{D}_p\right]\right)\{\mathrm{d}\varepsilon\} + \{\mathrm{d}\widetilde{\sigma}\} - \left\{\mathrm{d}\widetilde{\sigma}_p\right\}.\tag{6}
$$

More details can be found in [\(Li et al., 2009](#page-12-20); [Luo and Liu,](#page-12-19) [2010](#page-12-19); [Sun and Luo, 2018\)](#page-13-16).

#### **3.3 Simulating earthquake cycles**

We used the Drucker-Prager yield criterion to determine whether there is an earthquake that occurred in the model. When stresses on the fault elements do not reach the yield strength  $(F(\sigma, C) \le 0)$ , the model stays within the interseismic tectonic loading states [\(Figure 3\)](#page-4-0). With continuous tectonic loading, stresses increase; when the stresses reach the yield strength  $(F(\sigma, C)=0)$ , we decrease the cohesion on fault elements (the cohesion drops ΔC on faults are estimated from the coseismic stress drop ([Kanamori and Anderson,](#page-12-23) [1975](#page-12-23)) on each fault, where, Haiyuan fault:  $6.2 \times 10^6$  Pa, Yunwushan-Xiaoguanshan fault:  $4\times10^6$  Pa, Xiangshan-Tianjingshan fault:  $5\times10^6$  Pa, Helanshan fault:  $7\times10^6$  Pa, Luoshan fault:  $5.8 \times 10^6$  Pa, Huanghe fault:  $3.2 \times 10^6$  Pa, Yantongshan fault:  $5.8 \times 10^6$  Pa, and Niushoushan fault:  $5\times10^{6}$  Pa). A sudden decrease of cohesion will cause instability in the model, and thus, causing the coseismic slip. Namely, an earthquake occurs; at the same time, we set the time step to be 1 s. The stresses state at this moment shows *F* (*σ*, *C*−Δ*C*)>0. Due to the release of coseismic stress, the instability stresses state will change; stresses on fault elements will decrease. Until the residual stresses on fault elements satisfy the weakened yield strength  $(F(\sigma, C-\Delta C)=0)$ , the earthquake ends ([Figure 3](#page-4-0)). We can calculate the moment magnitude for each earthquake in the model according to the areas of failure elements and coseismic slips. Generally, a fault element yield represents a small earthquake; multiple elements yield represents a big earthquake. A big earthquake usually takes several hundred seconds to complete. After an earthquake ends, the cohesion of the yield elements immediately returns from *C*−Δ*C* to *C*. The model enters the postseismic viscoelastic stress relaxation period and the interseismic loading period toward the next earthquake. This process can be repeated, so we simulate the earthquake cycles ([Figure 3](#page-4-0)) [\(Luo and Liu, 2010,](#page-12-19) [2018;](#page-12-24) [Sun and Luo,](#page-13-16) [2018](#page-13-16); [Sun et al., 2019](#page-13-18)).

### **4. Model results**

#### **4.1 Background stress**

Initial stress conditions are important in geodynamic numerical simulation [\(Zhu and Zhang, 2013;](#page-13-22) Zhu et al., 2015), yet the initial conditions are difficult to determine and con-

coseismic stress drop post-seismic phase  $F(\sigma_{\rm on}, C) = 0$ **Yield stress**  $\sigma_{\rm w}$ **Stress**  $\sigma_{\rm re}$ **Residual stress**  $F(\sigma_{\text{y0}}, C-\Delta C)=0$ Time

interseismic tectonic loading

<span id="page-4-0"></span>**[Figure 3](#page-4-0)** Sketch showing stress accumulation and stress release during earthquake cycles.

strain owing to the complexity and inaccessibility of the earth [\(Chen, 2009\)](#page-12-0).

The stress states of the earth's crust mainly include the tectonic loading state, co-seismic stress release state, and postseismic stress acceleration state. These states occur on the basis of the background stress field during earthquake cycles. Stress changes relating to these three stages are small compared with the background stress. As an example, the average background stress or tectonic shear stress of the upper crust is generally several dozen megapascals, while the average shear stress change due to an earthquake is several megapascals or even smaller [\(Kanamori and Anderson, 1975](#page-12-23)).

The initial stress state in our modeling is a lithostatic stress state [\(Luo and Liu, 2010;](#page-12-19) [Sun and Luo, 2018\)](#page-13-16). With continued tectonic loading, the stress accumulates and reaches a steady-state in a model time of about 50000 years. This steady-state is the background stress state in our modeling; we calculate and analyze the model results using this background stress field. The results show that the modeled interseismic velocity field after the model reaches the steady-state is comparable to the velocity field acquired by the Global Positioning System [\(Sun and Luo, 2018](#page-13-16)); and the modeled stress state is consistent with that revealed by regional earthquake mechanisms ([Sun et al., 2019\)](#page-13-18). The model results and observation data compare well, indicating that the model reveals the geodynamic background [\(Shi et al., 2018\)](#page-13-2) in the northeastern Tibetan Plateau. We thus keep the model running and get the synthetic seismic catalog for this region [\(Figure 4](#page-5-0)).

#### **4.2 Synthetic seismic catalog**

We simulate earthquake cycles and the spatiotemporal evolution of the earthquake sequence and synthesize the longterm (on the scale of tens of thousands of years) seismic catalog [\(Figure 4\)](#page-5-0) using the modeled background stress field for the northeastern Tibetan Plateau.



**[Figure 4](#page-5-0)** Synthetic seismic catalog on the fault system of the northeastern Tibetan Plateau.

<span id="page-5-0"></span>We calculate the relation between the earthquake magnitude and earthquake frequency using this synthetic seismic catalog to test whether this synthetic catalog satisfies the *G*-*R* relation. The *G*-*R* relation is one of the most important statistical relations of seismicity [\(Gutenberg and Richter, 1944\)](#page-12-25), indicating a negative linear correlation between the seismic magnitude and the cumulative number of earthquakes ([Gu](#page-12-25)[tenberg and Richter, 1944;](#page-12-25) [Wiemer and Wyss, 2000;](#page-13-24) [Schorlemmer and Wiemer, 2005;](#page-13-25) [Parsons, 2007](#page-13-26)). The *G*-*R* relation can, therefore, be used as an important criterion in testing whether a synthetic seismic catalog is correct, complete, and reasonable. [Figure 5](#page-6-0) shows the magnitude-frequency distribution of the synthetic seismic catalog. The results show that the synthetic seismic catalog satisfies the *G*-*R* relation when the earthquake magnitude  $M_w \geq 5.5$  (i.e., the complete magnitude  $M_c$  is 5.5), and the *b*-value is 1.01 ([Figure 5](#page-6-0)a). We also calculate the regional *b*-value using the instrumental seismic catalog for 2008–2017 provided by the China Seismic Network Center; results show that  $M_c=1.2$  and *b*=0.96 [\(Figure 5](#page-6-0)b). We find that the *b*-value calculated using our synthetic seismic catalog is consistent with the value obtained using the instrumental seismic catalog; the values are also near the global-average *b*-value (1.0) [\(Nuannin et al.,](#page-12-26) [2005](#page-12-26); [El-Isa and Eaton, 2014\)](#page-12-27). We thus assume that our synthetic seismic catalog reflects seismicity in the northeastern Tibetan Plateau.

#### **4.3 Characteristics of earthquake recurrence on the model fault system**

We synthesized the long-term (on the order of tens of thou-

sands of years) seismic catalog for the northeastern Tibetan Plateau ([Figure 4\)](#page-5-0). We can also calculate the synthetic seismic catalog for each fault in the model [\(Figure 6\)](#page-6-1). According to the synthetic seismic catalog for each fault, we initially estimate the average recurrence interval of earthquakes with different magnitudes for each fault in the model. [Table 1](#page-7-0) gives the average recurrence interval of earthquakes with  $M_{\rm w}$ ≥6.0 and  $M_{\rm w}$ ≥7.0 for regional faults. Model results show that the average recurrence interval of earthquakes (both  $M_{\text{w}}\geq 6.0$  and  $M_{\text{w}}\geq 7.0$ ) is shortest for the Haiyuan fault; i.e., the recurrence interval of earthquakes is 32 years for  $M_{\rm w} \ge 6.0$ and 309 years for  $M_w \ge 7.0$ . The recurrence interval of earthquakes is the longest (2858 years) for the Niushoushan fault when with  $M_w \ge 6.0$ . There are no earthquakes with  $M_{\rm w}$ ≥7.0 for some individual faults in the model, e.g., the Luoshan fault. The maximum magnitude of earthquakes is  $M_{\rm w}$ 6.9 for the Luoshan fault in our modeling. However, paleoearthquake studies and historical earthquake records show that there have been earthquakes with magnitude greater than 7 along this fault (The Research Group on Active Fault System around Ordos Massif, 1988; [Min et al.,](#page-12-17) [2000\)](#page-12-17). According to the empirical magnitude conversion relation  $(M_w=(1.06\pm0.08)M-(0.58\pm0.60))$  ([Chen, 2017\)](#page-12-28), the moment magnitude of  $M_w$ 6.7 is close to  $M$ 7. We thus also calculate the recurrence interval of earthquakes with  $M_w \geq 6.7$ on the Luoshan fault in the model (2500 years); this result is comparable to that of *M*7 earthquakes (2300–2700 years) obtained in paleoearthquake studies ([Min et al., 2000](#page-12-17)). We find that the initially estimated recurrence intervals of earthquakes with  $M_w \ge 7.0$  on the Haiyuan fault and Xiangshan-Tianjingshan fault [\(Table 1,](#page-7-0) Haiyuan fault: 309 years;



<span id="page-6-0"></span>**[Figure 5](#page-6-0)** Earthquake magnitude-frequency distribution. (a) Earthquake magnitude-frequency distribution from the synthetic seismic catalog; (b) earthquake magnitude-frequency distribution from the instrumental record seismic catalog. The triangles and squares show the noncumulative and cumulative magnitude-frequency distributions, respectively.



**[Figure 6](#page-6-1)** Synthetic seismic catalog on different faults in the model.

<span id="page-6-1"></span>Xiangshan-Tianjingshan fault: 612 years) are shorter than the intervals obtained in previous paleoearthquake studies (Haiyuan fault: ~500–2500 years; Xiangshan-Tianjingshan fault: ~2000 years (Institute of Geology, China Earthquake Administration and Ningxia Bureau of China Earthquake Administration, 1990; [Min et al., 2000](#page-12-17); Zhang et al., 2005)). This is because we treat each fault zone as a whole when we estimate the recurrence interval of earthquakes. Here, the recurrence interval of earthquakes on each fault is defined as the ratio of the statistical model time to the number of earthquakes with  $M_w \ge 6.0$  or  $M_w \ge 7.0$  on each fault. However, the seismicity of the Haiyuan fault and Xiangshan-Tianjingshan fault is segmented along the fault strike (Zhang et al., 2005; [Zheng et al., 2013;](#page-13-15) [Sun et al., 2019](#page-13-18)). In our

	Recurrence interval of earthquakes (year)			
Fault	Model results	Paleoearthquake results		References
	$M_{\rm w}$ $\geq$ 6.0	$M_{\rm w}$ $\geq$ 7.0	$M \geq 7.0$	
Haiyuan fault	32	309	500-2500	Institute of Geology, China Earthquake Administration and Ningxia Bureau of China Earthquake Administra- tion (1990); Zhang et al. (2005); Min et al. (2000); Liu- Zeng et al. (2007). Liu et al. (1992)
Xiangshan-Tianjingshan fault	89	612	2000	Zhang et al. $(2005)$ ; Min et al. $(2000)$
Yantongshan fault	1250	-		
Luoshan fault	1819		2300-2700	Zhang et al. (2005). The Research Group on Active Fault System around Ordos Massif (1988)
Yunwushan-Xiaoguanshan fault	159	1112		
Niushoushan fault	2858	-		
Huanghe fault	572	2500	1500-2000	Lin et al. $(2015)$
Helanshan fault	870	6667	2300-3000	Lin et al. $(2015)$ , Deng and Liao $(1996)$

<span id="page-7-0"></span>**[Table 1](#page-7-0)** Average recurrence interval of earthquakes on faults in the model

model, the fault elements do not always fail together but have a certain segmentation when an earthquake occurs ([Sun and](#page-13-16) [Luo, 2018](#page-13-16)); even the seismicity on different fault segments of the same fault is not evenly distributed. Therefore, for a fault zone with obvious segmentation of seismicity, large errors may occur when using the seismicity of the whole fault zone and its related period to estimate the recurrence interval of earthquakes, as shown in [Table 1.](#page-7-0)

Therefore, we also calculate seismicity at different locations along each fault in the model and obtain the average recurrence interval of earthquakes of different magnitudes at different locations on each fault. [Figure 7](#page-8-0) shows the recur-rence interval ([Figure 7](#page-8-0)a) of earthquakes with  $M_w \ge 6.0$  and its standard deviation ([Figure 7](#page-8-0)b) and the recurrence interval ([Figure 7](#page-8-0)c) of earthquakes with  $M_w \ge 7.0$  and its standard deviation [\(Figure 7d](#page-8-0)). Results show that the earthquake recurrence is uneven in the modeling; i.e., values for different faults or at different locations along the same faults are re-markably different [\(Figure 7](#page-8-0)). The recurrence interval of earthquakes with  $M_w \ge 6.0$  in the middle segment of the Haiyuan fault is 300–1000 years with a standard deviation of about 100–300 years; the recurrence interval of earthquakes with  $M_{\text{w}}\geq$ 7.0 on this fault segment is 900–1200 years with a standard deviation of about 500 years. The recurrence interval of earthquakes at both ends of the Haiyuan fault (both *M*<sub>w</sub>≥6.0 and *M*<sub>w</sub>≥6.0) is around 2000–3500 years, or even larger ([Figure 7](#page-8-0)). The Haiyuan fault is the most crucial fault of the northeastern Tibetan Plateau, and seismicity on this fault is the most frequent in the regional fault system. Researchers have carried out many seismic and geological studies on this fault [\(Liu et al., 1992;](#page-12-29) [Min et al., 2000;](#page-12-17) Zhang et al., 2005; [Liu-Zeng et al., 2007](#page-12-18)). They found that the recurrence interval of earthquakes with *M*≥7.0 is 500–2500 years on the Haiyuan fault [\(Liu et al., 1992;](#page-12-29) [Min et](#page-12-17) [al., 2000;](#page-12-17) Zhang et al., 2005; [Liu-Zeng et al., 2007\)](#page-12-18); this result is consistent with our modeling results ([Figure 7\)](#page-8-0). Currently, the Maomaoshan-Laohushan fault in the western segment of the Haiyuan fault does not have a record of big earthquakes; i.e., there is a seismic gap ([Gaudemer et al.,](#page-12-30) [1995\)](#page-12-30). Therefore, this fault segment is more likely to have a major earthquake in the future. Seismicity along the Xiangshan-Tianjingshan fault shows that the recurrence interval of earthquakes with  $M_w \ge 6.0$  is about 1000 years ([Figure 7](#page-8-0)a) with a standard deviation of 300–500 years [\(Figure 7](#page-8-0)b) while the recurrence interval of earthquakes with  $M_w \ge 7.0$  is about 1500 years at most locations along this fault ([Figure 7](#page-8-0)c) with a standard deviation of about 400 years ([Figure 7d](#page-8-0)); the exceptions are isolated locations at which the interval is greater than 3000 years. Paleoearthquake studies on the Xiangshan-Tianjingshan fault found that the recurrence interval of earthquakes is about 2000 years [\(Wang et al., 1990](#page-13-27); [Min et al., 2000](#page-12-17)). The recurrence interval of earthquakes with  $M_w \ge 7.0$  is nearly 1500 years, with a standard deviation of 200 years, on the Yunwushan-Xiaoguanshan fault. There has been less research on the Yunwushan-Xiaoguanshan fault, resulting in fewer seismic records (Institute of Geology, China Earthquake Administration and Ningxia Bureau of China Earthquake Administration, 1990). However, this fault is likely to have a major earthquake because an *M*7 earthquake has occurred on this fault (i.e., the *M*7 Guyuan North earthquake that struck in 1622). The number and magnitudes of earthquakes on the Yunwushan-Xiaoguanshan fault in our modeling are more and larger than those obtained in previous research (Institute of Geology, China Earthquake Administration and Ningxia Bureau of China Earthquake Administration, 1990) because we connect the different fault segments seen at the surface into one fault zone [\(Figure 2\)](#page-3-0). In addition, we set the dip angle of the Yunwushan-Xiaoguanshan fault to be constant (70°) in our modeling. The dip angle of a fault may change with depth in reality, affecting the seismicity. The recurrence interval of earthquakes on the faults where seismicity does not show obvious segmentation



<span id="page-8-0"></span>**[Figure 7](#page-8-0)** Recurrence interval of earthquakes and the standard deviation. (a) Recurrence interval of earthquakes with magnitude  $M_w \ge 6.0$ ; (b) the standard deviation; (c) recurrence interval of earthquakes with magnitude *M*w≥7.0; (d) the standard deviation. The gray color indicates that there is no related earthquake in the region.

in the modeling is basically approximate to the results given in [Table 1.](#page-7-0) The recurrence interval of earthquakes with  $M_{\rm w}$  > 6.0 on the Helanshan fault is about 3000 years, the maximum interval is 6667 years ([Table 1](#page-7-0)), and the standard deviation is 1000–3000 years [\(Figure 7](#page-8-0)b, 7d). The recurrence interval of earthquakes with  $M_w \geq 6.0$  on the Huanghe fault is 1000–2500 years [\(Figure 7](#page-8-0)a), with a standard deviation of about 700–1500 years ([Figure 7b](#page-8-0)). The recurrence interval of earthquakes with  $M_w \ge 7.0$  on the Huanghe fault is about 2300 years [\(Figure 7c](#page-8-0)) with a standard deviation of about 1200 years [\(Figure 7d](#page-8-0)). The recurrence interval of earthquakes with  $M_w \ge 6.0$  on the Luoshan fault, Yantongshan fault, and Niushoushan fault is 2500–3000 years ([Figure 7a](#page-8-0)) with a standard deviation of about 1500–2000 years [\(Figure](#page-8-0) [7](#page-8-0)d). Our modeling results show that seismicity on the Luoshan fault, Yantongshan fault, and Niushoushan fault is relatively weak, which is consistent with results obtained by previous studies (Institute of Geology, China Earthquake Administration and Ningxia Bureau of China Earthquake Administration, 1990).

We also calculate the variation coefficient of earthquake recurrence for different magnitudes at different locations along each fault in the model. The variation coefficient  $\sigma$  is defined as:

$$
\sigma = \frac{T_{\text{std}}}{T_{\text{av}}},\tag{7}
$$

where  $T_{\text{av}}$  and  $T_{\text{std}}$  respectively represent the average and standard deviation of the recurrence interval of earthquakes [\(Kagan and Jackson, 1991](#page-12-32); [Yi et al., 2002](#page-13-28)). Earthquake clusters while the variation coefficient greater than 1.0; earthquake recurrence is an entirely random Poisson process while the variation coefficient equals to 1.0; and the earthquake recurrence is quasi-periodic while the variation coefficient less than 1.0 [\(Yi et al., 2002\)](#page-13-28). It is usually believed that a variation coefficient less than 0.5 well represents the quasi-periodic behavior of earthquake recurrence [\(Yi et al.,](#page-13-28) [2002\)](#page-13-28).

[Figure 8](#page-9-0) shows the variation coefficient of earthquake recurrence for  $M_w \ge 6.0$  ([Figure 8](#page-9-0)a) and  $M_w \ge 7.0$  (Figure 8b) on the fault system in the modeling. The variation coefficient of earthquake recurrence is uneven in the modeling; the values for different faults or for different locations along the same faults are remarkably different [\(Figure 8\)](#page-9-0). The variation coefficients of earthquake recurrence for  $M_{\rm w} \ge 6.0$  mostly range 0.5–1.0 in the modeling; i.e., the recurrence of earthquakes with  $M_w \ge 6.0$  shows weak quasi-periodic behavior ([Figure 8a](#page-9-0)). The variation coefficient of earthquake recurrence for  $M_w \ge 7.0$  is around 1.0 along the Helanshan fault ([Figure 8](#page-9-0)b), which means earthquakes with  $M_w \ge 7.0$  do not have quasi-periodicity on the Helanshan fault but rather a particular random behavior. Except in a small region where the variation coefficients are greater than 1.0, the variation coefficients along the Yunwushan-Xiaoguanshan fault, Xiangshan-Tianjingshan fault, and Haiyuan fault are mostly around 0.5 ([Figure 8b](#page-9-0)). This means that earthquake recurrence with  $M_w \ge 7.0$  at most locations along these faults has quasi-periodicity, and this quasi-periodicity is stronger than that of earthquake recurrence for  $M_w \ge 6.0$  [\(Figure 8](#page-9-0)).

#### **4.4 Earthquake probability on model fault system**

The genesis of an earthquake is complex, while the time required for earthquake genesis in mainland China is relatively long. In addition, it is difficult to predict earthquakes with certainty at present owing to the numerous shortcomings of observation technologies. Probabilistic seismic hazard analysis is, therefore, the main method of earthquake prediction adopted in seismic science research.

The available seismic catalog is relatively short, and many

hypothetical probabilistic distribution models have, therefore, been proposed for mathematical convenience (e.g., [Hagiwara, 1974](#page-12-33); [Utsu, 1984\)](#page-13-29). However, earthquakes do not always satisfy the assumptions of the models; i.e., the observed seismicity tends to be complex. Our model results also show that earthquake recurrence does not strictly obey a Poisson distribution but instead shows complexity; i.e., earthquakes at different locations along a fault system exhibit both quasi-periodicity (for which the variation coefficient of earthquake recurrence is less than 1.0) and clustering (for which the variation coefficient of earthquake recurrence is greater than 1.0) [\(Figure 8](#page-9-0)). We therefore directly analyze the synthetic long-term seismic catalog and then calculate the probability of earthquakes in the region. This probability is calculated without making any assumptions about the distribution of earthquake recurrence.

We calculate the long-term average probability of earthquakes striking at different locations of the fault system (i.e., along the fault direction and with depth) using the synthetic seismic catalog for a model time of 20000 years. In this paper, the earthquake probability is defined as the ratio of the number of earthquakes above an absolute magnitude to the number of earthquakes in the model at a fault position during a specific period. [Figure 9](#page-10-0) shows the probability of earthquakes with  $M_w \ge 6.0$  [\(Figure 9](#page-10-0)a) and  $M_w \ge 7.0$  [\(Figure 9b](#page-10-0)) along with the fault system in the modeling. The earthquake probability is heterogeneous on different faults [\(Figure 9](#page-10-0)). For earthquakes with  $M_w \ge 6.0$ , the probability of recurrence is a maximum on the middle segment of the Haiyuan fault, while the probability on the deep fault is greater than that on the shallow fault (i.e., the highest probability of earthquakes is on the location of the fault depth of about 20 km); the



<span id="page-9-0"></span>**[Figure 8](#page-9-0)** Variation coefficients of earthquake recurrence in the modeling. (a) Variation coefficients of earthquake recurrence for magnitude *M*w≥6.0; (b) variation coefficients of earthquake recurrence for magnitude *M*w≥7.0. The gray color means there is no related earthquake in the region.



<span id="page-10-0"></span>**[Figure 9](#page-10-0)** Long-term average probability of earthquake recurrence in the modeling. (a) Probability of earthquake recurrence for magnitude *M*w≥6.0; (b) probability of earthquake recurrence for magnitude  $M_{\text{w}} \ge 7.0$ .

maximum probability of earthquakes with  $M_w \geq 6.0$  can be as high as  $0.6\%$  ([Figure 9](#page-10-0)a). The probabilities of earthquakes on the Yunwushan-Xiaoguanshan fault and Xiangshan-Tianjingshan fault respectively reach 0.4% and 0.2%. The probabilities of earthquakes on the Helanshan fault, Huanghe fault, Luoshan fault, Yantongshan fault, and Niushoushan fault are low compared with those on the Haiyuan fault, Yunwushan-Xiaoguanshan fault, and Xiangshan-Tianjingshan fault; the value is basically around 0.01%, or even less ([Figure 9a](#page-10-0)). Among the faults, the probability of earthquake occurrence is lowest on the Niushoushan fault (about 0.005%) in the model fault system, and some locations along the fault do not even have earthquakes with  $M_w \geq 6.0$ .

The spatial distribution of earthquakes with  $M_w \ge 7.0$  is similar to that of earthquakes with  $M_w \ge 6.0$  in the modeling; i.e., the probability of earthquake recurrence in the middle segment of the Haiyuan fault is relatively high as a whole ([Figure 9b](#page-10-0)). In general, the number of earthquakes with a certain magnitude is 8–10 times the number of earthquakes with a magnitude one level greater, within a certain period in a region ([Chen, 2009](#page-12-0)). We see that the probability of earthquakes with  $M_{\text{w}} \ge 7.0$  (0.06%) is lower than that of earthquakes with  $M_w \ge 6.0$  (0.6%). Results show that the probability of earthquake recurrence is a maximum in the middle segment of the Haiyuan fault [\(Figure 9](#page-10-0)). We note that the probability of earthquake recurrence calculated here is a long-term average probability, which is independent of historical earthquakes. According to elastic rebound theory, after a major earthquake occurs in a fault zone, the region enters a stage of stress accumulation, which is relatively safe. As an example, the 1920 *M*8.5 Haiyuan earthquake struck in the middle segment of the Haiyuan fault, and the probability of the next major earthquake occurring in the middle segment of the Haiyuan fault is then lower than that for any other fault segment. The results thus provide a reference for the assessment of a long-term seismic hazard in a region.

#### **5. Discussion**

The earthquake recurrence interval and earthquake probability are basic references used in seismic hazard analysis, while the seismic catalog is basic data of the recurrence interval and earthquake probability. However, the available seismic catalogs are too short or incomplete for reliable analysis of the statistical characteristics of earthquakes. In this study, we developed and constructed a three-dimensional visco-elasto-plastic finite-element model for the northeastern Tibetan Plateau. We simulated earthquake cycles and the spatiotemporal evolution of earthquakes and obtained a synthetic seismic catalog on a time scale of tens of thousands of years for the northeastern Tibetan Plateau. We also calculated seismicity at different locations within the model fault system. By analyzing seismicity at different locations within the model fault system, we obtained the recurrence interval of earthquakes and the probability of earthquakes at each location within the fault system (i.e., the tendency along the fault direction). The results obtained in the present study can help us further understand the characteristics of earthquake recurrence and earthquake probability and analyze the regional seismic hazard.

We found that earthquake recurrence within the fault system of the northeastern Tibetan Plateau is complex; i.e., earthquake recurrence on faults exhibits both quasi-periodicity and clustering. It is difficult to accurately predict seismicity in the region according to the characteristics of

earthquake recurrence. Probabilistic seismic hazard analysis is a main means of earthquake prediction. We also calculated the long-term average probability of earthquakes striking in the northeastern Tibetan Plateau. The results show that the probability is a maximum for the middle segment of the Haiyuan fault, followed by the Yunwushan-Xiaoguanshan fault and Xiangshan-Tianjingshan fault. We emphasize that our calculated earthquake probability is the long-term average earthquake probability, which is independent of historical earthquakes. [Shi et al. \(2018\)](#page-13-2) suggested that the numerical prediction system of earthquakes in China should comprise long-term time-independent earthquake probabilistic forecasting, mid-term time-dependent earthquake probabilistic forecasting, and short-term earthquake probabilistic forecasting. The earthquake probability calculated in this paper is part of the long-term earthquake probabilistic forecasting of this numerical prediction system for earthquakes.

In the compilation of the seismic hazard map of China, the earthquake activity modeling makes three basic assumptions: the earthquake magnitude distribution in a seismic area satisfies the truncated *G*-*R* relation, earthquakes obey a Poisson distribution, and earthquakes in potential seismic zones are evenly distributed [\(Pan et al., 2013](#page-12-34)). We can get the annual average probability of earthquake occurrence by interpolating from the statistical results of the *G*-*R* relation for smalland medium-sized earthquakes. However, for earthquakes of larger magnitude, the magnitude-frequency distribution often deviates from the linear *G*-*R* relation of small- and medium-sized earthquakes ([Figure 5](#page-6-0)a) ([Cornell, 1968;](#page-12-35) [Wesnousky, 1994](#page-13-30); [Kagan, 2002\)](#page-12-36). That is to say, the statistical relations of large earthquakes and small- and medium-sized earthquakes may differ and exhibit different patterns, and the annual probability of earthquakes estimated only using the truncated *G*-*R* relation may have errors ([Wyss, 2015](#page-13-31)). Additionally, our model results show that earthquake recurrence is uneven and does not simply follow a Poisson distribution. In this study, we directly analyzed the synthetic seismic catalog and calculated the long-term average probability of earthquakes, and the calculation did not make any assumptions about the distribution of earthquake recurrence.

Previous studies simulated the seismic cycle according to the rate and state friction law (e.g., [van Dinther et al., 2013;](#page-13-32) [Zilio et al., 2018\)](#page-13-33). However, owing to difficulties in implementing numerical methods, most studies adopted twodimensional single-fault models and thus could not explore the characteristics of seismicity for complex three-dimensional fault systems. In reality, earthquakes occur within complex three-dimensional fault systems. In this study, we used a stress drop model to simulate earthquakes, allowing the simulation of seismic cycles for complex three-dimensional fault systems. This modeling helps us further analyze seismicity within regional multi-fault systems.

Previous research suggests that the Jingtai segment of the Haiyuan fault zone is currently in a creeping state ([Cavalié et](#page-12-37) [al., 2008\)](#page-12-37); its impact on regional seismicity remains unclear. The Haiyuan fault was treated as a stick-slip fault in this paper. Additionally, the modeling in this study made many approximations and simplifications. At the same time, owing to parameter uncertainty, it is not enough to calculate and analyze the model results for only one case. [Shi et al. \(2018\)](#page-13-2) pointed out that we can make calculations for many cases having a reasonable range of parameters, thus obtaining a series of results. The results can be moderately weighted to obtain a comprehensive probability of earthquakes, which is more reliable. The present paper presents preliminary results. These results are a reference for the seismicity of a regional fault system, the characteristics of earthquake recurrence, and the assessment of the long-term seismic hazard and provide a basis for the numerical prediction of earthquakes based on physical principles. The results thus promote the further development of physical-based seismic numerical prediction in China.

#### **6. Conclusions**

We analyzed the regional characteristics of earthquake recurrence and the probability of earthquakes using a synthetic seismic catalog for the northeastern Tibetan Plateau and available seismic data for this region. The main conclusions of this study are as follows.

(1) The numerical model developed in this study is a new tool for simulation of regional seismic catalog of a complex fault system. Available seismic catalogs are too short or incomplete, and the synthetic seismic catalog thus helps us better understand the characteristics of seismicity and analyze the regional seismic hazard.

(2) Earthquake recurrence on the fault system of the northeastern Tibetan Plateau shows quasi-periodic behavior as a whole, but this quasi-periodicity is not strong in that there is often a large deviation. It is, therefore, difficult to accurately predict the regional seismicity according to the characteristics of earthquake recurrence.

(3) Seismicity within the fault system of the northeastern Tibetan Plateau is uneven in that earthquake recurrence is different for different faults and different segments of the same fault.

(4) The modeled long-term average probability of earthquakes is a maximum on the middle segment of the Haiyuan fault (where the probability of earthquakes with  $M_w \ge 6.0$ reaches 0.6% and the probability of earthquakes with  $M_{\rm w}$ ≥7.0 reaches 0.06%), followed by the Yunwushan-Xiaoguanshan fault and Xiangshan-Tianjingshan fault.

(5) The results of this paper provide a reference for the seismicity of a regional fault system, the characteristics of

earthquake recurrence, and the assessment of the long-term seismic hazard, and provide a basis for the numerical forecasting of earthquakes based on physical principles.

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