

# **A Novel Coupled Model for Monthly Rainfall Prediction Base[d](http://crossmark.crossref.org/dialog/?doi=10.1007/s11269-024-03815-x&domain=pdf)  on ESMD‑EWT‑SVD‑LSTM**

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## **Abstract**

Precise predicting of rainfall is paramount for effective water resource management, ecological conservation, and the prevention of droughts and foods. Infuenced by numerous variables, the process of rainfall is complex and the rainfall series exhibit high degrees of nonlinearity, making it challenging for traditional statistical prediction models to accurately capture the characteristics of rainfall series. Therefore, this paper proposes a new coupled model for predicting monthly rainfall based on Extreme-Point Symmetric Mode Decomposition (ESMD), Empirical Wavelet Transform (EWT), Singular Value Decomposition (SVD) and Long Short-Term Memory Neural Network (LSTM). By training and evaluating the ESMD-EWT-SVD-LSTM model on Kaifeng City's monthly rainfall data from 2009 to 2020 and comparing its predictions with those of the ESMD-SVD-LSTM, SVD-LSTM, LSTM models, the analysis reveals that: the quadratic decomposition of ESMD-EWT and SVD denoising can further reduce the complexity of rainfall data, obtain more predictable feature IMFs, and enhance the precision in LSTM predicting; in comparison with alternative models, the ESMD-EWT-SVD-LSTM coupled model shows the highest accuracy in predicting results, with MAE of 4.96, RMSE of 6.13, and SI of 0.12, indicating that the ESMD-EWT-SVD-LSTM model has strong nonlinear process learning ability and accuracy in regional monthly rainfall prediction. This study can ofer dependable scientifc grounding and technical assistance for regional rainfall predicting, water resources planning, and disaster mitigation.

**Keywords** Extreme-point symmetric mode decomposition · Empirical wavelet transform · Singular value decomposition · Long short-term memory neural network · Rainfall prediction

**Highlights**

<sup>(1)</sup> ESMD can decompose rainfall series into multiple real feature IMFs.

<sup>(2)</sup> Combining ESMD and EWT methods for data preprocessing can further simplify and extract information from rainfall series.

<sup>(3)</sup> The IMFs after ESMD-EWT decomposition and SVD processing can efectively improve the prediction accuracy of LSTM.

<sup>(4)</sup> The coupled model of ESMD-EWT-SVD-LSTM has a better prediction performance and strong applicability for nonlinear rainfall series.

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### **1 Introduction**

Rainfall plays a crucial role in the terrestrial water cycle, as global warming leads to increased climate instability, extreme rainfall and drought events are occurring frequently, introducing numerous uncertainties into the sustainable growth of the local economy and the well-being of its inhabitants. (Aydin and Sevgi [2022;](#page-13-0) Fatimi et al. [2023](#page-13-1); Zhuang et al. [2023\)](#page-14-0). Therefore, scientifc and accurate rainfall prediction based on hydrological characteristics is important for efective hydrological planning and development of strategies to manage rainfall risks.

The hydrological processes, such as rainfall, are characterized by complexity and fuctuation, making their precise forecasting a key issue in contemporary research (Moraga et al. [2022;](#page-14-1) Li et al. [2012;](#page-13-2) Zhou et al. [2017](#page-14-2)). During the past few years, scholars have extensively researched rainfall predicting and attained remarkable outcomes (Wu et al. [2021;](#page-14-3) Yang et al. [2022\)](#page-14-4). Currently, the common practice for rainfall prediction is analyzing available rainfall data and constructing corresponding prediction models (Chen et al. [2022](#page-13-3)). The GP, SVR, ANN and other classical time series modeling methods are now efectively used in hydrological forecasting (Chadalawada et al. [2017;](#page-13-4) Kajewska Szkudlarek [2020;](#page-13-5) Devi et al. [2016](#page-13-6)). However, owing to the randomness of rainfall and the infuence of climate, the actual rainfall may exhibit signifcant fuctuations within a single year, rendering the traditional statistical methods inadequate for accurate quantitative prediction of rainfall (Olmo and Bettolli [2022](#page-14-5)). As computing power increases, deep learning neural networks have found widespread applications in various felds (Han et al. [2022](#page-13-7); Afshari Nia et al. [2023;](#page-13-8) Chen and Wang [2022](#page-13-9); Hewamalage et al. [2021](#page-13-10)). Byun et al. ([2023\)](#page-13-11) analysed cloud image data using the CNN algorithm for regional rainfall prediction. Zhang et al. [\(2021](#page-14-6)) predicted the daily runoff of a river using the RNN model. However, due to its algorithmic reasons, the RNN model was prone to gradient explosion. In response to this issue, the Long Short-Term Memory (LSTM) model was proposed (Gao et al. [2020](#page-13-12)). Ni et al. [\(2020](#page-14-7)) confrmed the efectiveness of LSTM in predicting time series by examining precipitation data. Chen et al.  $(2021)$  $(2021)$  conducted an analysis of the rainfall and runoff processes in the Shishengchuan basin and discovered that the LSTM model had the capability to produce highly accurate rainfall predictions. Zhu et al. [\(2023](#page-14-8)) combined high-resolution radar rainfall data to propose an LSTM-based approach to radar rainfall nearing prediction.

Rainfall time series are always volatile and nonlinear, which seriously afects the performance of prediction models (Chen et al. [2022;](#page-13-3) Nourali [2023](#page-14-9); Ehteram et al. [2023](#page-13-14)). Therefore, the choosing of techniques capable of handling non-stationary time series is the essential foundation for the subsequent enhancement of rainfall prediction accuracy. EMD algorithm is a traditional signal feature extraction method, but it is prone to mode mixing (Johny et al. [2022;](#page-13-15) Zheng et al. [2021](#page-14-10)). As technology evolves and modernizes, methods such as ESMD, EWT, and SVD have been proposed and efectively used in the feature recognition process of prediction data. Gao et al. [\(2023](#page-13-16)) applied ESMD to decompose denoised wind speed time series adaptively and proposed FO-BSO-LSSVM for multistep wind speed prediction. Karijadi et al. ([2023\)](#page-13-17) utilized the EWT method for secondary processing of high-frequency IMFs and combined it with the LSTM method to achieve wind power prediction. Zhang and Chen [\(2022](#page-14-11)) extracted the features of wind energy data by CEEMDAN-SVD and performed wind speed prediction.

The efficiency of ESMD, EWT, SVD, and LSTM methods in data processing and prediction has been verifed in practical engineering, however, these methods are less applied in the feld of hydrology and the practical efects of the coupled algorithms have not been fully explored. Therefore, for the practical needs of rainfall prediction, a coupled model based on EMD-EWT-SVD-LSTM is proposed. Firstly, for the rainfall observation sequence of Kaifeng City, Henan Province, ESMD-EWT is applied to perform quadratic decomposition to simplify the rainfall sequence features and obtain the characteristic IMFs; Secondly, the high-frequency IMFs obtained after quadratic decomposition are subjected to SVD noise reduction to obtain the main features; Thirdly, the fnal predicted rainfall sequence is obtained by predicting and integrating by the LSTM model for all the IMFs; Finally, the results of ESMD-EWT-SVD-LSTM prediction are juxtaposed with alternative models to validate applicability and accuracy of the model. This study explores a new regional rainfall prediction method, which can improve the accuracy efectively and ofer a reliable scientifc basis for regional water resources planning and disaster mitigation.

### **2 Method and Methodology**

### **2.1 Extreme‑Point Symmetric Mode Decomposition**

Wang and Li [\(2013](#page-14-12)) proposed ESMD based on the EMD algorithm, which is applicable across various engineering felds involving data processing, such as information science, atmospheric science, and economics.

The ESMD algorithm works as follows:

Step 1: Find all maxima and minima in the data *X* and denote them as  $E_i$  ( $i = 1, 2, 3...,n$ ) in order.

Step 2: Connect neighboring extreme points with the help of a straight line and mark the midpoint of each section of the line as  $F_i$  ( $i = 1, 2, 3 \cdots n$ ).

Step 3: Complement the midpoints  $F_0$ ,  $F_n$  of the left and right boundaries by linear interpolation.

Step 4: Construct the interpolation lines  $L_1, ... L_p$  ( $p \ge 1$ ) for the obtained midpoints  $n+1$ and calculate the average value of the interpolation lines according to  $L^* = (L_1 + ... + L_p)/p$ .

Step 5: Repeat the above steps for  $X - L^*$  until  $|L^*| \leq \varepsilon$ , where  $\varepsilon$  is a predetermined tolerance error, usually taken as  $\varepsilon = 0.001\delta_0$ .  $\delta_0$  is as follows:

$$
\delta_0^2 = \frac{1}{N} \sum_{i=1}^N \left( x_i - \frac{1}{N} \sum_{i=1}^N x_i \right) \tag{1}
$$

where: *N* is length of data.

In addition to the allowable error  $\varepsilon$ , the maximum number of decompositions  $K$  is also an adjustable parameter. When the decomposition process makes  $|L^*| \leq \varepsilon$  or reaches the predetermined maximum number of decompositions  $K$ , the first empirical mode  $M_1$  is decomposed.

Step 6: Repeat the above steps for  $X - M_1$ , obtain  $M_2, M_3...$  in order, and finally the remaining extreme points are composed as residual component *R*.

Step 7: Calculate the variance ratio  $\delta/\delta_0$  to obtain the optimal number of decompositions *K*, where  $\delta$  is the relative standard deviation of *X*−*R* and  $\delta_0$  is the standard deviation of the original series *X*.

Step 8: In the integer interval [*Kmin*,*Kmax*], fnd out the maximum number of fltering times *K* corresponding to the minimum variance ratio  $\delta/\delta_0$  as an optimal number of decompositions, and accordingly repeat the frst to sixth steps to output the signal decomposition results.

#### **2.2 Empirical Wavelet Transform**

Gilles integrated wavelet transform theory with the EMD method and introduced the empirical wavelet transform (EWT) method, which can efectively avoid the phenomenon of mode mixing (Gilles [2013](#page-13-18); Peng et al. [2022](#page-14-13); Liu et al. [2022](#page-14-14)).

The Eq.[\(2](#page-3-0)) is established to distinguish the optimal decomposition order *N*.

<span id="page-3-0"></span>
$$
E_N^l = \sqrt{\sum_{i=1}^n \frac{x_i^2(i)}{n}}, l = 1, 2, \cdots N
$$
  
\n
$$
E_N = \sum_{l=1}^N E_N^l
$$
  
\n
$$
\theta_{N,N-1} = \frac{|E_N - E_{N-1}|}{E_{N-1}}
$$
\n(2)

where:  $E_N^l$  is the energy of each IMF,  $E_N$  is the sum of the energy of the *N* IMFs obtained by decomposition, and  $\theta_{N,N-1}$  represents the energy difference of the IMF under different *N* values.

When  $\theta_{N,N-1}$  suddenly becomes larger, it shows that the EWT decomposition process appears as the phenomenon of over-decomposition, resulting in false components. At this time, the corresponding decomposition time *N*−1 is the optimal decomposition order of EWT.

#### **2.3 Singular Value Decomposition**

SVD, as a traditional and efective method for reducing noise, has been extensively utilized in the domain of extracting feature information from complex signals (Zhang et al. [2022;](#page-14-15) Zhang et al. [2018](#page-14-16)).

Defne the optimal singular value decomposition order as *r*, this paper selects the order at which the singular entropy increment stabilizes as the optimal singular value decomposition order (Zhang et al. [2018\)](#page-14-16).

#### **2.4 Long Short‑Term Memory Networks**

In view of the fact that RNN is difficult to deal with long sequence data (Elsaraiti and Merabet [2021\)](#page-13-19), Hochreiter and Schmidhuber [\(1997](#page-13-20)) proposed the LSTM model. Assuming  $\sigma$  stands for the sigmoid activation function; tanh represents the hyperbolic tangent function. The formulae for  $\sigma$  and tanh are as follows (Bakhshi Ostadkalayeh et al. [2023;](#page-13-21) Johny et al. [2022\)](#page-13-15):

$$
\sigma(x) = \frac{1}{1 + e^{-x}}\tag{3}
$$

$$
\tanh(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}
$$
 (4)

The signal undergoes a series of transformations from its input to its output as follows:

$$
f_t = \sigma \big( W_f \cdot \big[ h_{t-1}, x_t \big] + b_f \big) \tag{5}
$$

$$
i_t = \sigma \big( W_i \cdot \big[ h_{t-1}, x_t \big] + b_i \big) \tag{6}
$$

$$
o_t = \sigma\big(W_o \cdot \big[h_{t-1}, x_t\big] + b_o\big) \tag{7}
$$

$$
\tilde{c}_t = \tanh\left(W_c \cdot \left[h_{t-1}, x_t\right] + b_c\right) \tag{8}
$$

$$
c_t = f_t \cdot c_{t-1} + i_t \cdot \tilde{c}_t \tag{9}
$$

$$
h_t = o_t \cdot \tanh\left(c_t\right) \tag{10}
$$

where:  $W_f$ ,  $W_i$ ,  $W_o$ ,  $W_c$  indicates the respective weight vectors of the forgotten gate, the input gate, the export gate, and the memory cell; '.' denotes the dot product operation between two vectors;  $x_t$  denotes the input to the network at time *t*;  $b_f$ ,  $b_i$ ,  $b_o$ ,  $b_c$  represent the bias vectors of the forgotten gate, the input gate, the export gate, and the memory cell, respectively;  $h_{t-1}$  denotes the hidden state at the moment  $t-1$ ;  $c_{t-1}$  indicates the cellular state of  $t-1$ ;  $x_t$  denotes the input at the moment of  $t$ ;  $f_t$  denotes the forgetting gate;  $i_t$ denotes the input gate;  $o_t$  denotes output gate.

#### **3 ESMD‑EWT‑SVD‑LSTM Coupled Prediction Model**

#### **3.1 Model Steps**

Taking into account the non-stationary of rainfall series and the benefts of diferent methods, this research suggests a coupled ESMD-EWT-SVD-LSTM model for predicting rainfall. The fowchart is illustrated in Fig. [1,](#page-5-0) and the crucial procedures are detailed underneath.

1) ESMD decomposition. The ESMD method is employed to break down the initial series of rainfall, leading to a fnite number of IMFs consisting of components M and a residual component R.

2) EWT quadratic decomposition. For the M1 with complex frequency among the IMFs of ESMD decomposition, quadratic decomposition by EWT algorithm is applied, and the main information of the IMFs is further extracted. The quadratically decomposed EM of the M1 is obtained.

3) Noise reduction. For the high-frequency IMFs that remain after the ESMD decomposition, the SVD method is employed to minimize noise, while the low-frequency IMFs are directly incorporated into both training and prediction samples.

4) Prediction. All the IMFs after quadratic decomposition and SVD noise reduction are segregated into training sample and prediction sample, and the LSTM method is used in this paper to predict and reconstruct the rainfall series.



<span id="page-5-0"></span>**Fig. 1** The fowchart of ESMD-EWT-SVD-LSTM coupled prediction model

By combining quadratic decomposition with noise reduction in signal processing, it is possible to signifcantly simplify and extract key features from monthly rainfall data, thus enhancing the precision of rainfall predictions.

#### **3.2 Model Verifcation**

To further assess the predictive accuracy of the ESMD-EWT-SVD-LSTM model, we employ MAE, RMSE, and SI as evaluation metrics (Johny et al. [2022](#page-13-15); Zhang et al. [2023](#page-14-17)). The specifc equations are as follows:

$$
MAE = \frac{1}{N} \sum_{i=1}^{N} |y_i - \hat{y}_i|
$$
 (11)

$$
\text{RMSE} = \sqrt{\frac{\sum_{i=1}^{N} (y_i - y_i)^2}{N}}
$$
(12)

$$
SI = \frac{1}{\mu} \sqrt{\frac{\sum_{i=1}^{N} (\hat{y}_i - y_i)^2}{N}}
$$
 (13)

where:  $\hat{y}_i$  is the predicted value at time *i*;  $y_i$  is the actual observed value at time *i*;  $\mu$  is the average of the observations; *N* is data length.

### **4 Example Analysis**

#### **4.1 Area Profle**

Kaifeng, located in the central region of China and the eastern part of Henan Province, is renowned as the ancient capital of eight dynasties, making it an essential city for protection and development in China. Rainfall serves as the primary water resource for Kaifeng, exerting a direct infuence on both the local ecological environment and the daily lives of its residents. Therefore, predicting monthly rainfall is crucial for water resources planning and sustainable development in Kaifeng.

This research utilizes the recorded monthly rainfall data from fve counties and four districts in Kaifeng spanning 2009 to 2020 as foundational data (Data source: the Water Resources Bulletin of Henan Province, [https://slt.henan.gov.cn/bmzl/szygl/szygb/\)](https://slt.henan.gov.cn/bmzl/szygl/szygb/).

#### **4.2 Data Preprocessing**

Before the prediction, it is essential to carry out the division of training samples and prediction samples. Here, 120 monthly rainfall series from 2009 to 2018 in Kaifeng City are used as training samples, and 24 monthly rainfall series from 2019 to 2020 are used as prediction samples to compare and validate the prediction results (Data source: the Water Resources Bulletin of Henan Province, <https://slt.henan.gov.cn/bmzl/szygl/szygb/>). According to the ESMD decomposition steps, the rainfall series is shown in Fig. [2](#page-6-0).

From Fig. [2](#page-6-0)(a), it can be observed that due to the infuence of the temperate monsoon climate, the peak and trough values of Kaifeng's rainfall exhibit obvious periodicity and uncertainty, the annual variation in rainfall is signifcant with complex characteristics. From Fig. [2](#page-6-0)(b), we can clearly observe that the ESMD efectively decomposes the original

**100**



<span id="page-6-0"></span>(a) Monthly rainfall data for Kaifeng City from 2009 to 2020 (b) The ESMD results of Kaifeng from 2009 to 2018



monthly rainfall series into M components representing information at diferent scales and a R component representing the trend. From the M1 to R, the frequency decrease gradually and the wavelength become longer. The highest frequency M1 still contains rich frequency information, which is not favorable for the next prediction. Consequently, the EWT method is utilized for the quadratic decomposition of the M1 to further simplify the component features. The EWT decomposition process is illustrated in Fig. [3](#page-7-0).

From Fig. [3\(](#page-7-0)a), it can be seen that when *N*>4, the IMF energy difference  $\theta_{N,N-1}$  starts to increase, therefore,  $N=4$  is chosen as the optimal decomposition order for the EWT algorithm. From Fig. [3](#page-7-0)(b), it's evident that the EWT decomposition efectively decomposes the M1 into feature EMs which include distinct frequency information from the frequency domain perspective and ensures that each feature EM aligns with the frequency information present in M1. Therefore, through the EWT decomposition, several EM components with simpler frequency characteristics are obtained, which can provide basic data for the subsequent prediction analyses.

The monthly rainfall time series is characterized by its high volatility, non-linearity, and non-stationary, the obtained IMFs also exhibit signifcant volatility, which is not conducive to prediction and analysis. To address this, we utilize SVD denoising on the IMFs to refne the precision of the prediction model. The process is demonstrated using M2 as an example and the SVD noise reduction results is shown in Fig. [4.](#page-8-0)

From Fig.  $4(a)$  $4(a)$ , the optimal decomposition order of the M2 is determined to be  $r=10$ which corresponds to retaining 90% of the singular value. In Fig. [4\(](#page-8-0)b), the blue curve illustrates the data before SVD processing, while the red curve illustrates the data after SVD processing. Comparing the red and blue curves, it can be found that the fuctuation peaks of the M2 are reduced in some months after SVD processing and the overall fuctuation curves are more homogeneous. By applying SVD noise reduction, the original signal characteristics are represented more comprehensively, and some detailed fuctuations are more accurately represented.

### **4.3 Rainfall Prediction**

This study utilizes the monthly rainfall data of Kaifeng City from 2009 to 2018 as a training sample for the LSTM model and predicts the monthly rainfall for the period 2019 to



<span id="page-7-0"></span>**Fig. 3** The EWT decomposition process





<span id="page-8-0"></span>**Fig. 4** The SVD noise reduction results

2020 (Data source: the Water Resources Bulletin of Henan Province, [https://slt.henan.gov.](https://slt.henan.gov.cn/bmzl/szygl/szygb/) [cn/bmzl/szygl/szygb/](https://slt.henan.gov.cn/bmzl/szygl/szygb/)). The predictions of IMFs are generated using LSTM model, the corresponding results are presented in Fig. [5](#page-9-0).

From Fig. [5](#page-9-0), although there are still a small number of points in each IMF that do not match completely, the proportion of these points is very low and does not afect the fnal prediction results, which indicates that the model exhibits a high degree of predictive accuracy.

The relative error is calculated between the predicted and actual values, as detailed in Table [1](#page-10-0).

According to Table [1](#page-10-0), the M1 and M2 have the largest prediction errors with the average relative positive error ranging from 40 to 50% and the average relative negative error ranging from −50% to −30%. This suggests that the non-smoothing of the M1 and M2 is high, the sequence's fuctuations in complex components can notably reduce prediction accuracy and cause a significant relative error. Figure [6](#page-10-1) shows the prediction of rainfall data.

From Fig. [6](#page-10-1), the predicted rainfall series can correspond to the actual observation series with small relative errors, and the prediction results are accurate without lag. This indicates that the coupled rainfall prediction model based on ESMD-EWT-SVD-LSTM has a good ability to process data and prediction, the prediction results are accurate and can be efectively used in practical engineering.

#### **5 Discussion**

In this study, the ESMD-EWT-SVD-LSTM coupled model has achieved good application in the prediction of rainfall. To further validate the feasibility and superiority of the ESMD-EWT-SVD-LSTM coupled model, ESMD-SVD-LSTM, SVD-LSTM, and LSTM are applied to compare the prediction ability respectively. The indicators such as MAE, RMSE, SI, average relative error are introduced to quantitatively evaluate the prediction results and the comparison are shown in Table [2](#page-10-2).

Table [2](#page-10-2) demonstrates that the ESMD-EWT-SVD-LSTM model yields superior predictive outcomes and boasts a higher accuracy, with the MAE of 4.96, the RMSE of 6.13, the



<span id="page-9-0"></span>**Fig. 5** The prediction results of LSTM

SI of 0.12, and the average relative error less than 1%. Taking the MAE as an example for analysis, comparing the prediction results of ESMD-EWT-SVD-LSTM and ESMD-SVD-LSTM, it can be found that after the quadratic decomposition of ESMD-EWT, the MAE is reduced by 56.53%, which indicates that reducing the complexity of the original rainfall sequence through multiple decompositions enhances the accuracy of LSTM. Besides,



<span id="page-10-0"></span>



<span id="page-10-1"></span>**Fig. 6** The prediction of rainfall data

<span id="page-10-2"></span>

comparing the SVD-LSTM and LSTM prediction results, it can be found that although the SVD can further extract the signal features, the application of the SVD in the case of complex original rainfall sequence will lead to the interference or loss of the data features, which results in an increase of the MAE by 31.83% of the prediction results. The comparison of the model prediction results is provided in Fig. [7](#page-11-0).

As can be seen from Fig. [7,](#page-11-0) the trend and period of the ESMD-EWT-SVD-LSTM prediction results can efectively coincide with the actual observation data, and the prediction



<span id="page-11-0"></span>**Fig. 7** Comparison of model prediction results

accuracy exceeds that of the other three models, which has a great potential in rainfall prediction.

Comparing the current research in the feld of rainfall prediction (Byun et al. [2023](#page-13-11); Chen et al. [2022](#page-13-3); Johny et al. [2022\)](#page-13-15), all the technique proposed by these researchers can be efectively applied to actual projects. However, in the context of the randomness, volatility, and non-linearity inherent in rainfall data, the central challenge for further investigation in the feld of rainfall prediction becomes how to efectively diminish the complexity of rainfall data and enhance the precision of predictive outcomes. On the basis of previous studies and fully considering the particularity of rainfall data, we put forward ESMD-EWT-SVD-LSTM coupled model. Diferent from the traditional direct prediction or prediction after a single decomposition, the coupled model addresses the characteristics of rainfall data by performing a quadratic decomposition with ESMD-EWT and denoising with SVD, continuously reducing data complexity and enhancing predictability, ultimately achieving accurate predicting results. In this study, we apply the ESMD-EWT-SVD-LSTM coupled model to predict the monthly rainfall data in Kaifeng City and assess the validity of the model by comparing it with alternative models. The results show that the ESMD-EWT-SVD-LSTM coupled prediction model has better theoretical advantages and accuracy in monthly rainfall prediction, and can be efectively applied to practical projects. The results show that the ESMD-EWT-SVD-LSTM coupled prediction model has better theoretical advantages and accuracy in monthly rainfall prediction, and can be efectively applied to practical projects.

Kaifeng, a city in China, exemplifes a warm temperate continental monsoon climate with complex and seasonal variations in monthly rainfall. The ESMD-EWT-SVD-LSTM coupled model has been efectively applied to the prediction of monthly rainfall in Kaifeng, indicating that this model has a strong ability to analyze and predict complex rainfall series and can be applied to rainfall predicting in regions with similar climates in China and

around the world. It is particularly worth mentioning that, based on the theoretical advantages of the ESMD-EWT-SVD-LSTM coupled model, it is feasible to perform rainfall prediction tasks well in complex rainfall areas diferent from Kaifeng, but the specifc practical application efects require further research and exploration.

## **6 Conclusion**

In this study, we present the ESMD-EWT-SVD-LSTM coupled prediction model to address the challenge of monthly rainfall prediction. By applying this approach to the analysis of monthly rainfall in Kaifeng City from 2009 to 2020, the results demonstrate that the predicted rainfall series closely aligns with the actual observation series, exhibiting small relative errors and without any lag. Comparing the predictive outcomes of the ESMD-EWT-SVD-LSTM model against those from the ESMD-SVD-LSTM, SVD-LSTM, and LSTM models, it is found that the ESMD-EWT-SVD-LSTM has the best prediction results, with MAE of 4.96, RMSE of 6.13, SI of 0.12, and average relative error less than 1%. This suggests that the coupled ESMD-EWT-SVD-LSTM monthly rainfall prediction model possesses strong predictive capabilities and can be efectively applied to regional water resources scheduling.

Although the proposed ESMD-EWT-SVD-LSTM model has demonstrated efficacy in monthly rainfall prediction, the current model solely focuses on the rainfall time series during the prediction process and overlooks the physical mechanisms that contribute to changes in rainfall. How to explore the connection between predicting rainfall and other pertinent factors will be a crucial focus for future studies.

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**Author Contributions** Conceptualization: Z. X. Methodology and analysis: L. Z; Z. X. Writing—original draft preparation: L. Z; Z. X. Writing—review and editing: L. Z; Z. X. Supervision: Z. X.

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**Data Availability** The data that support the fndings of this study are available on request.

## **Declarations**

**Ethical Approval** All research activities conducted for this article have obtained ethical approval from the relevant institutional review board or ethics committee. This ensures that the research complies with ethical standards and safeguards the rights and well-being of the participants.

**Consent to Participate** Participants involved in this study have provided informed consent to voluntarily participate. Clear and comprehensive information regarding the study's purpose, procedures, and potential risks has been communicated, allowing participants to make informed decisions about their involvement.

**Consent to Publish** Authors have obtained explicit consent from study participants, when applicable, for the publication of any identifable information. This ensures respect for individuals' privacy and confdentiality, aligning with ethical publishing practices.

**Competing Interests** Authors disclose any competing interests that could infuence the interpretation or presentation of the research. This includes fnancial interests, relationships, or afliations that may be perceived as infuencing the work.

### **References**

- <span id="page-13-8"></span>Afshari Nia M, Panahi F, Ehteram M (2023) Convolutional neural network-ANN-E (Tanh): a new deep learning model for predicting rainfall. Water Resour Manag 37(4):1785–1810. [https://doi.org/10.](https://doi.org/10.1007/s11269-023-03454-8) [1007/s11269-023-03454-8](https://doi.org/10.1007/s11269-023-03454-8)
- <span id="page-13-0"></span>Aydin MC, Sevgi B (2022) Flood risk analysis using GIS-based analytical hierarchy process: a case study of Bitlis Province. Appl Water Sci 12(6):122. <https://doi.org/10.1007/s13201-022-01655-x>
- <span id="page-13-21"></span>Bakhshi Ostadkalayeh F, Moradi S, Asadi A, Moghaddam Nia A, Taheri S (2023) Performance improvement of LSTM-based deep learning model for streamfow forecasting using Kalman fltering. Water Resour Manag 37(8):3111–3127.<https://doi.org/10.1007/s11269-023-03492-2>
- <span id="page-13-11"></span>Byun J, Jun C, Kim J, Cha J, Narimani R (2023) Deep learning-based rainfall prediction using cloud image analysis. IEEE Trans Geosci Remote Sens 61:1–11. [https://doi.org/10.1109/TGRS.2023.](https://doi.org/10.1109/TGRS.2023.3263872) [3263872](https://doi.org/10.1109/TGRS.2023.3263872)
- <span id="page-13-4"></span>Chadalawada J, Havlicek V, Babovic V (2017) A genetic programming approach to system identifcation of rainfall-runoff models. Water Resour Manag 31:3975–3992. [https://doi.org/10.1007/](https://doi.org/10.1007/s11269-017-1719-1) [s11269-017-1719-1](https://doi.org/10.1007/s11269-017-1719-1)
- <span id="page-13-3"></span>Chen C, Zhang Q, Kashani MH, Jun C, Bateni SM et al (2022) Forecast of rainfall distribution based on fxed sliding window long short-term memory. Engineering Applications of Computational Fluid Mechanics 16(1):248–261. <https://doi.org/10.1080/19942060.2021.2009374>
- <span id="page-13-9"></span>Chen G, Wang WC (2022) Short-term precipitation prediction for contiguous United States using deep learning. Geophys Res Lett 49(8):e2022GL097904. <https://doi.org/10.1029/2022GL097904>
- <span id="page-13-13"></span>Chen YC, Gao JJ, Bin ZH, Qian JZ, Pei RL, Zhu H (2021) Application study of IFAS and LSTM models on runoff simulation and flood prediction in the Tokachi River basin. J Hydroinf  $23(5)$ :1098–1111. <https://doi.org/10.2166/hydro.2021.035>
- <span id="page-13-6"></span>Devi SR, Arulmozhivarman P, Venkatesh C, Agarwal P (2016) Performance comparison of artifcial neural network models for daily rainfall prediction. Int J Autom Comput 13:417–427. [https://doi.org/10.1007/](https://doi.org/10.1007/s11633-016-0986-2) [s11633-016-0986-2](https://doi.org/10.1007/s11633-016-0986-2)
- <span id="page-13-14"></span>Ehteram M, Ahmed AN, Sheikh Khozani Z, El-Shafe A (2023) Convolutional neural network-support vector machine model-Gaussian process regression: a new machine model for predicting monthly and daily rainfall. Water Resour Manag 37(9):3631–3655. <https://doi.org/10.1007/s11269-023-03519-8>
- <span id="page-13-19"></span>Elsaraiti M, Merabet A (2021) Application of long-short-term-memory recurrent neural networks to forecast wind speed. Appl Sci 11(5):2387.<https://doi.org/10.3390/app11052387>
- <span id="page-13-1"></span>Fatimi AS, Anwar E, Shaikh T (2023) The precedent set by unprecedented rainfall: lessons to be learnt from disastrous fooding in Pakistan. Disaster Med Public Health Prep 17:e411. [https://doi.org/10.1017/](https://doi.org/10.1017/dmp.2023.79) [dmp.2023.79](https://doi.org/10.1017/dmp.2023.79)
- <span id="page-13-12"></span>Gao B, Huang X, Shi J, Tai Y, Zhang J (2020) Hourly forecasting of solar irradiance based on CEEMDAN and multi-strategy CNN-LSTM neural networks. Renew Energy 162:1665–1683. [https://doi.org/10.](https://doi.org/10.1016/j.renene.2020.09.141) [1016/j.renene.2020.09.141](https://doi.org/10.1016/j.renene.2020.09.141)
- <span id="page-13-16"></span>Gao Y, Wang B, Chen F, Zhang W, Zhou D, Wu F, Chen D (2023) Multi-step wind speed prediction based on LSSVM combined with ESMD and fractional-order beetle swarm optimization. Energy Rep 9:6114–6134.<https://doi.org/10.1016/j.egyr.2023.05.034>
- <span id="page-13-18"></span>Gilles J (2013) Empirical wavelet transform. IEEE Trans Signal Process 61(16):3999-4010. [https://doi.org/](https://doi.org/10.1109/TSP.2013.2265222) [10.1109/TSP.2013.2265222](https://doi.org/10.1109/TSP.2013.2265222)
- <span id="page-13-7"></span>Han L, Liang H, Chen H, Zhang W, Ge Y (2022) Convective precipitation nowcasting using U-net model. IEEE Trans Geosci Remote Sens 60:1–8.<https://doi.org/10.1109/TGRS.2021.3100847>
- <span id="page-13-10"></span>Hewamalage H, Bergmeir C, Bandara K (2021) Recurrent neural networks for time series forecasting current status and future directions. Int J Forecast 37(1):388–427. [https://doi.org/10.1016/j.ijforecast.](https://doi.org/10.1016/j.ijforecast.2020.06.008) [2020.06.008](https://doi.org/10.1016/j.ijforecast.2020.06.008)
- <span id="page-13-20"></span>Hochreiter S, Schmidhuber J (1997) Long short-term memory. Neural Comput 9(8):1735–1780. [https://doi.](https://doi.org/10.1162/neco.1997.9.8.1735) [org/10.1162/neco.1997.9.8.1735](https://doi.org/10.1162/neco.1997.9.8.1735)
- <span id="page-13-15"></span>Johny K, Pai ML, Adarsh S (2022) A multivariate EMD-LSTM model aided with time dependent intrinsic cross-correlation for monthly rainfall prediction. Appl Soft Comput 123:108941. [https://doi.org/10.](https://doi.org/10.1016/j.asoc.2022.108941) [1016/j.asoc.2022.108941](https://doi.org/10.1016/j.asoc.2022.108941)
- <span id="page-13-5"></span>Kajewska Szkudlarek J (2020) Clustering approach to urban rainfall time series prediction with support vector regression model. Urban Water J 17(3):235–246.<https://doi.org/10.1080/1573062x.2020.1760319>
- <span id="page-13-17"></span>Karijadi I, Chou SY, Dewabharata A (2023) Wind power forecasting based on hybrid CEEMDAN-EWT deep learning method. Renew Energy 218:119357.<https://doi.org/10.1016/j.renene.2023.119357>
- <span id="page-13-2"></span>Li CZ, Zhang L, Wang H, Zhang YQ, Yu FL, Yan DH (2012) The transferability of hydrological models under nonstationary climatic conditions. Hydrol Earth Syst Sci 16(4):1239–1254. [https://doi.org/10.](https://doi.org/10.5194/hess-16-1239-2012) [5194/hess-16-1239-2012](https://doi.org/10.5194/hess-16-1239-2012)
- <span id="page-14-14"></span>Liu Q, Yang J, Zhang K (2022) An improved empirical wavelet transform and sensitive components selecting method for bearing fault. Measurement 187:110348. [https://doi.org/10.1016/j.measurement.2021.](https://doi.org/10.1016/j.measurement.2021.110348) [110348](https://doi.org/10.1016/j.measurement.2021.110348)
- <span id="page-14-1"></span>Moraga JS, Peleg N, Molnar P, Fatichi S, Burlando P (2022) Uncertainty in high-resolution hydrological projections: partitioning the infuence of climate models and natural climate variability. Hydrol Process 36(10):e14695.<https://doi.org/10.1002/hyp.14695>
- <span id="page-14-7"></span>Ni L, Wang D, Singh VP, Wu J, Wang Y, Tao Y, Zhang J (2020) Streamfow and rainfall forecasting by two long short-term memory-based models. J Hydrol 583:124296. [https://doi.org/10.1016/j.jhydrol.2019.](https://doi.org/10.1016/j.jhydrol.2019.124296) [124296](https://doi.org/10.1016/j.jhydrol.2019.124296)
- <span id="page-14-9"></span>Nourali M (2023) Improved treatment of model prediction uncertainty: estimating rainfall using discrete wavelet transform and principal component analysis. Water Resour Manag 37(11):4211–4231. [https://](https://doi.org/10.1007/s11269-023-03549-2) [doi.org/10.1007/s11269-023-03549-2](https://doi.org/10.1007/s11269-023-03549-2)
- <span id="page-14-5"></span>Olmo ME, Bettolli ML (2022) Statistical downscaling of daily precipitation over southeastern South America: assessing the performance in extreme events. Int J Climatol 42(2):1283–1302. [https://doi.org/10.](https://doi.org/10.1002/joc.7303) [1002/joc.7303](https://doi.org/10.1002/joc.7303)
- <span id="page-14-13"></span>Peng L, Wang L, Xia D, Gao Q (2022) Efective energy consumption forecasting using empirical wavelet transform and long short-term memory. Energy 238:121756. [https://doi.org/10.1016/j.energy.2021.](https://doi.org/10.1016/j.energy.2021.121756) [121756](https://doi.org/10.1016/j.energy.2021.121756)
- <span id="page-14-12"></span>Wang JL, Li ZJ (2013) Extreme-point symmetric mode decomposition method for data analysis. Adv Adapt Data Anal 5(03):1350015.<https://doi.org/10.1142/s1793536913500155>
- <span id="page-14-3"></span>Wu S, Hu X, Zheng W, He C, Zhang G, Zhang H, Wang X (2021) Effects of reservoir water level fluctuations and rainfall on a landslide by two-way ANOVA and K-means clustering. Bull Eng Geol Environ 80(7):5405–5421.<https://doi.org/10.1007/s10064-021-02273-8>
- <span id="page-14-4"></span>Yang J, Xiang Y, Sun J, Xu X (2022) Multi-model ensemble prediction of summer precipitation in China based on machine learning algorithms. Atmosphere 13(9):1424. [https://doi.org/10.3390/atmos13091](https://doi.org/10.3390/atmos13091424) [424](https://doi.org/10.3390/atmos13091424)
- <span id="page-14-6"></span>Zhang J, Chen X, Khan A, Zhang YK, Kuang X, Liang X, Taccari ML, Nuttall J (2021) Daily runof forecasting by deep recursive neural network. J Hydrol 596:126067. [https://doi.org/10.1016/j.jhydrol.2021.](https://doi.org/10.1016/j.jhydrol.2021.126067) [126067](https://doi.org/10.1016/j.jhydrol.2021.126067)
- <span id="page-14-16"></span>Zhang J, Hou G, Ma B, Hua W (2018) Operating characteristic information extraction of food discharge structure based on complete ensemble empirical mode decomposition with adaptive noise and permutation entropy. J Vib Control 24(22):5291–5301. <https://doi.org/10.1177/1077546317750979>
- <span id="page-14-15"></span>Zhang J, Li Z, Huang J, Cheng M, Li H (2022) Study on vibration-transmission-path identifcation method for hydropower houses based on CEEMDAN-SVD-TE. Appl Sci 12(15):7455. [https://doi.org/10.3390/](https://doi.org/10.3390/app12157455) [app12157455](https://doi.org/10.3390/app12157455)
- <span id="page-14-17"></span>Zhang X, Chen H, Wen Y, Shi J, Xiao Y (2023) A new water level prediction model based on ESMD−VMD−WSD−ESN. Stoch Env Res Risk A 37:3221–3241. [https://doi.org/10.1007/](https://doi.org/10.1007/s00477-023-02446-9) [s00477-023-02446-9](https://doi.org/10.1007/s00477-023-02446-9)
- <span id="page-14-11"></span>Zhang Y, Chen Y (2022) Application of hybrid model based on CEEMDAN, SVD, PSO to wind energy prediction. Environ Sci Pollut Res 29:22661–22674. <https://doi.org/10.1007/s11356-021-16997-3>
- <span id="page-14-10"></span>Zheng J, Su M, Ying W, Tong J, Pan Z (2021) Improved uniform phase empirical mode decomposition and its application in machinery fault diagnosis. Measurement 179:109425. [https://doi.org/10.1016/j.](https://doi.org/10.1016/j.measurement.2021.109425) [measurement.2021.109425](https://doi.org/10.1016/j.measurement.2021.109425)
- <span id="page-14-2"></span>Zhou Z, Ouyang Y, Li Y, Qiu Z, Moran M (2017) Estimating impact of rainfall change on hydrological processes in Jianfengling rainforest watershed China using BASINS-HSPF-CAT modeling system. Ecol Eng 105:87–94. <https://doi.org/10.1016/j.ecoleng.2017.04.051>
- <span id="page-14-8"></span>Zhu K, Yang Q, Zhang S, Jiang S, Wang T, Liu J, Ye Y (2023) Long lead-time radar rainfall nowcasting method incorporating atmospheric conditions using long short-term memory networks. Frontiers in Environmental Science 10:1054235.<https://doi.org/10.3389/fenvs.2022.1054235>
- <span id="page-14-0"></span>Zhuang X, Fan Y, Li Y, Wu C (2023) Evaluation climate change impacts on water resources over the upper reach of the Yellow River Basin. Water Resour Manag 37(6-7):2875–2889. [https://doi.org/10.1007/](https://doi.org/10.1007/s11269-023-03501-4) [s11269-023-03501-4](https://doi.org/10.1007/s11269-023-03501-4)

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