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Competition Between Growth and Removal in Zirconia Nanocrystal‑Derived Triboflms: The Role of Co‑additives

Parker LaMascus[1](http://orcid.org/0000-0002-7945-849X) · Meagan B. Elinski1,2 [·](http://orcid.org/0000-0001-8664-770X) Daniel Delghandi1,[3](http://orcid.org/0009-0009-4147-8303) · Pranjal Nautiyal1,4 · Julia Grifn5 · Lei Zheng⁶ · Andrew Jackson^{[1](http://orcid.org/0000-0002-3235-3156),6} · Robert J. Wiacek⁶ · Robert W. Carpick¹

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Abstract

Antiwear additives permit energy-efficient lubrication of gearboxes, bearings, and other tribological interfaces. We study zirconia ($ZrO₂$) nanocrystal additives, which readily form protective tribofilms in tribological contacts. Our prior work demonstrated cooperative antiwear performance between $ZrO₂$ and the S- and P-based co-additives in fully formulated hydrocarbon gear oils. Here, we extend that work by examining the growth kinetics of the $ZrO₂$ tribofilms, including the influence of the co-additives. In the boundary lubrication regime for mixed rolling-sliding contacts, the initial phase of $ZrO₂$ triboflm growth is soon overtaken by removal processes, phenomena whose importance has gone unnoticed in prior work. Triboflm removal afects the steady-state thickness and morphology of the triboflm as well as its growth kinetics. The Sand P-based co-additives are incorporated into the $ZrO₂$ tribofilm, and alter the competition between the growth and removal processes, increasing initial net growth rates per contact cycle and contributing to a more polished fnal interface. This work highlights the signifcance of removal processes in determining triboflm antiwear performance, and suggests several routes for improving triboflm growth kinetics using co-additives.

Graphical abstract

Keywords Nanoparticles · Nanocrystals · Tribofilms · Extreme pressure additives · Tribosintering · Low viscosity gear oil · Coadditives · Elastohydrodynamic lubrication

 \boxtimes Robert W. Carpick carpick@seas.upenn.edu

- ¹ Department of Mechanical Engineering & Applied Mechanics, University of Pennsylvania, Philadelphia, PA 19104, USA
- ² Present Address: Department of Chemistry, Hope College, Holland, MI 49423, USA
- ³ Present Address: Department of Mechanical Engineering, Stanford University, Stanford, CA 94305, USA
- Present Address: Department of Mechanical and Aerospace Engineering, Oklahoma State University, Stillwater, OK, USA
- ⁵ Department of Chemistry, Mount Holyoke College, South Hadley, MA 01075, USA
- ⁶ Pixelligent Technologies LLC, Baltimore, MD 21224, USA

1 Introduction

Industrial and commercial machines rely on lubricants to reduce friction and wear of contacting components [[1](#page-9-0)]. Low-viscosity lubricants can decrease churning losses in such machines, signifcantly reducing energy and revenue costs [\[2\]](#page-9-1). However, contacts lubricated with lower-viscosity lubricants are more likely to enter mixed and boundary lubrication regimes [[1,](#page-9-0) [3\]](#page-9-2). To reduce wear from surface contact, low-viscosity lubricant blends typically include antiwear (AW) additives, such as zinc dialkyldithiophosphates (ZDDPs) [[4](#page-9-3)[–6](#page-9-4)] or metal oxide nanoparticles [[7](#page-9-5)[–10](#page-10-0)], or other additive classes like sulfur- or phosphorus-based extreme pressure (EP) additives [[11\]](#page-10-1).

Zirconium dioxide $(ZrO₂)$ NCs are an appealing candidate as next-generation AW additives since they are free from sulfate ash to comply with new environmental regulations [[12](#page-10-2)[–14\]](#page-10-3). The potential of several metal oxide NCs as AW additives was demonstrated by Kato and Komai [[10](#page-10-0)], who used a pin-on-disc tribometer and dry nanopowders to form triboflms from nine diferent metal oxide species. Though a dry contact in pure sliding does not emulate liquid-lubricated gearbox or bearing conditions, Kato and Komai [[10\]](#page-10-0) nonetheless showed that oxide species with higher oxygen difusivity prevented wear more efectively, which they attributed to faster tribofilm formation through a stress-assisted sintering mechanism named "tribosintering" by Adachi and Kato [[15](#page-10-4)]. Subsequently, researchers showed that the nanoparticles suspended in liquid lubricants can form triboflms via tribosintering when subjected to tribological sliding in macroscale tribotests [[16,](#page-10-5) [17](#page-10-6)]. Other studies of metal oxide nanoparticle additives claim other mechanisms, such as surface healing, polishing, or a ball-bearing action that converts sliding friction to rolling friction [\[18,](#page-10-7) [19](#page-10-8)].

To study AW triboflm formation with greater verisimilitude, later work employed the atomic force microscopy (AFM) technique of Gosvami et al*.* [\[5\]](#page-9-6), which provides lubricated single-asperity contacts in the boundary regime under pure sliding and permits concurrent measurement of triboflm thickness and morphology. However, AFM has so far been limited to low sliding speeds (at most a few hundred μ m/s). Khare et al. $[20]$ $[20]$ $[20]$ used this technique to show that $ZrO₂$ AW tribofilms derived from $ZrO₂$ NCs in polyalphaolefn (PAO) base oil form in three distinct stages: a nucleation or induction period with limited growth, followed by a linear growth regime, and ending in thickness saturation. Khare et al*.* [[20](#page-10-9)] expanded on the tribosintering mechanism of Kato and Komai for $ZrO₂$ tribofilm formation by showing that nanoscale $ZrO₂$ tribofilms grow from NC suspensions in lubricant, and that triboflm growth rates are pressure dependent but relatively independent

of temperature (unlike the Arrhenius growth kinetics of ZDDPs, e.g., [\[20,](#page-10-9) [21](#page-10-10)]).

Tribosintering, a process by which heat and stress drive the nanoparticles to form a dense, surface-bound solid phase, is not well understood [[20\]](#page-10-9). Experiments by Hernández Battez et al. created antiwear triboflms from metal oxide nanoparticle additives, achieving more realistic loads and steel substrates, but limited by pure sliding conditions [[16,](#page-10-5) [17](#page-10-6)]. Work by Thrush et al. $[22-24]$ $[22-24]$ and Elinski et al. $[8]$ $[8]$ on $ZrO₂$ NCs appealed to the tribosintering mechanism to explain their results in the Mini-Traction Machine (MTM) which achieved mixed rolling and sliding conditions. Elinski et al*.* showed that scuffing damage seen for MTM experiments in pure PAO is prevented for the same PAO with 1 wt.% $ZrO₂$ NCs added, attributed to the presence of a protective triboflm formed via tribosintering [\[8\]](#page-9-7). The set of studies by Thrush et al*.*, respectively, demonstrated that higher NC concentrations [[22\]](#page-10-11), contact pressures [\[23](#page-10-13)], and temperatures [\[24](#page-10-12)] benefit tribofilm growth rate for MTM experiments conducted with polyalphaolefn (PAO) base oils and the same $ZrO₂ NCs$. Lahouij et al. also observed $ZrO₂$ tribofilm formation via tribosintering for the same NCs in PAO in harsh micropitting rig (MPR) tests, where the steel surfaces are much rougher and the primary failure mode is pitting rather than the MTM's scuffing $[25]$ $[25]$ $[25]$.

Benefits of $ZrO₂$ tribofilms formed via tribosintering are also seen in lubricants with other AW/EP co-additives pre-sent. Elinski et al. [\[8](#page-9-7)] test ZrO₂ NC additives in an especially relevant lubricant, 75W-80, which has the same Sand P-based AW/EP additive package as the commercial 75W-90, but a reduced viscosity that yields energy efficiency at the cost of surface separation. They observe that $ZrO₂$ triboflms formed with S-/P-based co-additives evince less substrate wear, which they attribute to the fast-acting antiscuffing co-additives preventing initial damage while the thicker $ZrO₂$ AW tribofilm nucleates [\[8](#page-9-7)]. They also hypothesize that the co-additives lead to faster tribosintering of the $ZrO₂ NCs [8]$ $ZrO₂ NCs [8]$. Consistent with this, Demas et al. [[26\]](#page-10-15) observe in MPR tests that $ZrO₂ NCs$ in the same fully formulated 75W-80 gear oil used by Elinski et al*.*[[8\]](#page-9-7) prevent scuffing under conditions where NC-free gear oil scuffs. Collectively, these studies demonstrate signifcant potential for $ZrO₂$ NCs to function effectively as AW additives. Though all these studies employ more application-relevant contact conditions than AFM, the lack of connection to nanoscale phenomena and observation hampers understanding. Maximizing NC AW performance and translating that to practice necessitates greater mechanistic understanding of triboflm growth.

We employ a mini-traction machine (MTM) and polyalphaolefn (PAO)-lubricated bearing steel to study the AW performance of $ZrO₂$ NCs. We vary the slide-to-roll ratio (SRR) between steel ball and disc specimens to replicate a variety of application-relevant contact conditions, from the teeth of a gear at higher SRR to the rollers of a bearing at lower SRR. Using a novel analysis method, we obtain triboflm thickness data with high temporal resolution, and use this to demonstrate nanoscale triboflm removal which occurs alongside tribosintering-driven growth. When commercial S- and P-based AW/EP co-additives are included in the PAO, the $ZrO₂$ tribofilms form more rapidly, validating the hypothesis of Elinski et al. [[8\]](#page-9-7). Moreover, our insight into the removal process demonstrates that co-additives can beneft triboflm performance by leading to a smoother interface at steady state.

2 Experimental Methods

2.1 Mini‑Traction Machine and Spacer Layer Imaging Method

We use precisely the method described by Elinski et al. [\[8\]](#page-9-7); for full details, see Sects. [2.1–](#page-2-0)[2.3](#page-3-0) of that work, with a slight modifcation to our solvents used for post-processing, as described in the erratum to that work [[27](#page-10-16)]. The main instrument for this method is the Mini-Traction Machine (MTM, PCS Instruments, London, UK), a ball-on-disc tribometer which permits lubricated tribological testing and in situ measurements of rolling and/or sliding speeds, and traction. The Spacer Layer Imaging Method (SLIM) that accompanies the MTM measures triboflm thickness at a single location on the MTM ball specimen [[28](#page-10-17)]. Experimental parameters are given in Table [1.](#page-2-1)

Table 1 Summary of MTM Testing Conditions

MTM entrainment speed 150 mm/s	
Slide-Roll Ratio (SRR)	Independent variable: 25%, 50%, and 100%
Temperature	100 °C
Test duration	2 h $(62,000-110,000$ contact cycles on the ball, depending on SRR)
Applied load	50 N (1.11 GPa maximum Hertzian pres- sure)

The figures in this work will typically have a normalized x-axis of Ball Contact Cycles. The equation used for normalization is $n_{ball} = t \cdot v_{ball}/r_{ball}$, where *t* is the seconds recorded by the MTM, *vball* is the ball speed recorded by the MTM, and ball radius r_{ball} is assumed a constant 8.673 mm.

Table [2](#page-2-2) contains information on the materials used in the MTM. The steel tribopair and fuid blends were selected to mimic conditions in high-performance gears or bearings. Polyalphaolefn (PAO) is a common base stock, and 75W-80 is a lower-viscosity version of the commercial oil 75W-90. The latter blends contain proprietary S- and P-based co-additives for AW and EP protection.

The materials of Table [2](#page-2-2) were carefully chosen to enforce a single independent variable, the presence of coadditives. The elastohydrodynamic (EHD) characteristics of the base oils are nearly identical, and $ZrO₂$ dispersed in either oil at 1wt% did not signifcantly afect the viscosity [[22](#page-10-11)]. The only significant difference between PAO10 and 75W-80 is the presence of the commercial S- and P-based AW and EP co-additives in the latter.

2.2 White Light Interferometry

White light interferometry (WLI) measures tribofilm roughness. We used a Zygo NewView interferometer, sputter-coating our MTM specimens with ~ 25 nm Au–Pd to enhance the uniformity of light refection [\[29](#page-10-18)]. RMS roughness is calculated on a 300 μ m \times 500 μ m area. Notably, this WLI data are only taken at the end of each traction test, as the Au–Pd coating process would disrupt the tribology of the interface, meaning that the number of contact cycles on each end-of-test ball specimen is not constant. Therefore, WLI is mostly used to contextualize our SLIM results qualitatively. Namely, if the WLI's measurement of the triboflm's height above the adjacent substrate to be smaller in magnitude than the SLIM's measurement of the transparent triboflm's total thickness, it implies that the triboflm is embedded into the steel substrate through plasticity or wear prior to triboflm growth [[8\]](#page-9-7).

2.3 Time‑of‑fight Secondary Ion Mass Spectrometry

Time-of-flight secondary ion mass spectrometry (ToF-SIMS) measures spatially resolved chemical composition of tribofilms deposited on MTM disc specimens at the end of test. A TOFWERK CTOF ToF-SIMS spectrometer (TOFWERK, Thun, Switzerland) installed inside a Tescan S852X FIB-SEM system (Tescan, Brno, Czech Republic) was employed. A Xe⁺ ion beam (30 kV voltage, 30 nA current, and 10 µs dwell time) was used to sputter the triboflm and the surrounding region to determine chemical composition as a function of triboflm thickness. To establish a conversion from frames to nm, WLI is used before and after milling to measure the depth of the milled trench.

3 Results and Discussion

3.1 Non‑monotonic Triboflm Growth

For all the contact conditions and blends under consideration, we observe the formation of thick, surface-bound triboflms (Fig. [1](#page-3-1), bottom). As mentioned above, Elinski et al*.* [\[8\]](#page-9-7), using identical blends and experimental conditions to this study, show that these tribofilms prevent scuffing and alleviate wear of the substrate, ofering substantial practical beneft. We also observe that a higher SRR hastens the onset of growth, and that co-additized oil has thinner fnal tribofilms than those formed in $PAO+ZrO₂$. The latter observation matches that of Elinski et al. on the identical system [\[8](#page-9-7)]. Finally, we also observe that traction generally increases in magnitude as the triboflms develop, but defer discussion of this phenomenon to Sect. [3.3](#page-4-0).

A surprising trend in these data is that triboflm growth is non-monotonic—interruptions of triboflm growth occur for nearly every set of conditions (Fig. [1,](#page-3-1) gray circled regions). This effect was not observed in the nanoscale AFM results of Khare et al. [\[20](#page-10-9)]. Non-monotonic triboflm growth is seen in the MTM studies of the same $ZrO₂ NCs$ in Elinski et al. [\[8](#page-9-7)] and Thrush et al. [\[22](#page-10-11), [30](#page-10-19)] but these works did not examine the causes of this efect. Khare et al.'s [[20\]](#page-10-9) AFM study of nanoscale $ZrO₂$ tribofilm growth reported that tribofilm removal processes do occur, but the removal was limited to the upper few nanometers of triboflm once it reached its maximum height, and did not lead to substantial changes in triboflm height during the growth phase, unlike the transient periods of Fig. [1.](#page-3-1) Meanwhile, studies on other metal oxide nanoparticles, such as ZnO [\[9](#page-9-8), [31](#page-10-20)] or CuO [\[17](#page-10-6)], tend to focus on steady-state AW performance without interrogating triboflm growth kinetics. In contrast to these prior studies, we can observe non-monotonic triboflm growth clearly when it occurs, because we obtained SLIM images

Fig. 1 Traction and $ZrO₂$ tribofilm evolution data as a function of contact cycles in mixed rolling/sliding experiments (conditions specifed in Tables [1](#page-2-1) and [2\)](#page-2-2). Left: experiments in 75W-80; Right: experiments in PAO10; Top: traction coefficient; Bottom: tribofilm thickness. The insets provide linear plots of the same data. For every condition save $PAO10+ZrO₂$ at 100% SRR, the tribofilm growth regime is non-monotonic (highlighted with gray ovals)

at a relatively high rate of one image per minute for the frst 10 min of each MTM test (except for PAO10 at 100% SRR, whose first SLIM image occurs at 10 min). The evidence of non-monotonic triboflm growth is a clue to elucidate the mechanisms by which NC-based triboflms form and stabilize.

3.2 Removal Competes with Tribosintering

Figure [2](#page-4-1) demonstrates that the non-monotonic triboflm growth observed in Fig. [1](#page-3-1) is the cumulative efect of triboflm *removal* from the ball specimen outpacing growth. (Supporting Information includes annotated movies for a more comprehensive look at these data.) Because SLIM is an interferometric optical technique, we can assume that this change in triboflm thickness is real, rather than an artifact due to a plastically deformed substrate beneath the tribofilm (as observed in the MPR experiments of $[25]$ $[25]$). It is also unlikely that the non-monotonic events are merely artifacts of refractive index changes in the triboflm as it densifies $[32]$, particularly since successive $ZrO₂$ removal and regrowth events were observed in the SLIM images for all SRRs and blends under consideration. This removal does not occur as a single global delamination or failure of the triboflm, but as the local thinning of patches or azimuthal

Fig. 2 Annotated, cropped, representative SLIM images demonstrating the triboflm removal phase. The left-most images show the steel MTM ball (blue in appearance) with relatively few contact cycles and no visible triboflm. As the ball undergoes contact cycles in mixed rolling/sliding, a triboflm builds up and is visible in SLIM as patches and striations—the darker in shade, the thicker the triboflm. The

bands of triboflm throughout the Hertzian ball-disc contact. When these events were averaged to obtain Fig. [1,](#page-3-1) the cumulative efect of these events led to non-monotonicity. In other words, triboflm removal is not a single event, but occurs constantly in competition with tribosintering-driven growth; the non-monotonic periods of Fig. [1](#page-3-1) are simply the moments when removal outpaces tribosintering on average (PAO10+ $ZrO₂$ at 100% SRR was the one case where local removal never outweighed growth in this way). When the two processes occur at equal rates, we see a plateau of growth; at steady state, Khare et al. dubbed this saturation.

3.3 Test Conditions Change Removal Process

The competition between triboflm removal and tribosintering dictates triboflm growth kinetics and steady-state triboflm thickness. This is evident in the diferences between the PAO10 and 75W-80 experiments of Fig. [1](#page-3-1)—co-additives disrupt the balance between removal and growth, leading to diferent kinetics (see Sect. [3.5\)](#page-6-0), and thinner steady-state triboflm thicknesses by a factor of almost 2. However, to understand the importance of the removal process for triboflm properties and performance, we utilize an ex situ study of triboflm morphology.

rightmost images show that, with additional cycles, regions of the triboflm get thinner, and that this thinning can occur via the removal of local patches or striations in the running direction. Removal is observed in both PAO10 blends (top) and 75W-80 blends (bottom), leading to a transient phase involving an overall net decrease in mean triboflm thickness, as seen in Fig. [1](#page-3-1)

Examination of the end-of-test morphologies of the MTM ball and disc specimens show that the triboflms formed in $75W-80+ZrO₂$ have uniformly smoother surfaces than those formed without co-additives at the same SRR (ball specimens shown in Fig. [3;](#page-5-0) disc specimens are similar and displayed in SI1, and bearing areas of these flms are examined in SI2). There is also a modest but clear trend for both blends that as the SRR increases, so does the composite roughness of the interface $R_q = \sqrt{R_{q,ball}^2 + R_{q,disk}^2}$. We examined the bearing area of the triboflms to confrm this interpretation (Supporting Information). Taken together, these results show that co-additives cooperate with $ZrO₂$ to form a smoother triboflm that bears contact more evenly than triboflms formed in $PAO10+ZrO₂$.

These changes in triboflm morphology have signifcant benefts for the ultimate performance of the triboflms. We can predict one such beneft using the defnition of the nondimensional EHD flm thickness λ, the ratio between EHD fuid flm thickness and the composite RMS roughness of the interface R_a . Smoother interfaces imply a larger λ ratio, with more surface separation and a lower-traction coefficient, all else equal. Therefore, the change in the interfacial roughness due to co-additives or SRR, without changing the

Fig. 3 Left: End-of-test morphologies for white light interferometry (WLI) of MTM ball specimens on which triboflms were formed in 2 h of rolling-sliding contact (top: PAO10; bottom: 75W-80). The RMS roughness $R_{a,ball}$ and mean tribofilm heights \overline{z} with respect to

the substrate are indicated on each plot. Right: End-of-test composite RMS roughness R_a for the MTM ball and disc tribofilm surfaces, with connecting lines to guide the eye

EHL response of the lubricant rheology, should also lead to changes in traction in the boundary regime. For these experiments, the initial λ , estimated using the Hamrock–Dowson equation, is 2.00 ± 0.03 for both PAO10 and 75W-80, putting the contact in the mixed lubrication regime. However, λ decreases as rough triboflms form in the interface, reaching the boundary lubrication regime, where the contact is asperity-mediated, at about 10 nm of composite roughness. Note that the initial composite areal roughness of the bare steel surfaces is 5–10 nm. We next make use of this insight with a novel analysis method to obtain high time-resolution measurements of the character of the tribological interface.

3.4 Traction Estimates Triboflm Growth with High Time Resolution

SLIM is not an ideal technique to measure triboflm growth with high time resolution, as it requires pausing the test for each SLIM image to be acquired, thus slowing down the experiment and creating a practical limit to image rate. However, traction data, collected in situ in the MTM, are sampled by default at 1 Hz. Traction is a force transmitted across an interface [[3\]](#page-9-2), and because our experiments progress into the boundary regime as rough triboflms grow in the interface, we expect that a change in the interface—like wear or triboflm growth—would lead to a change in the traction coefficient. Figure [4](#page-5-1) plots SLIM thickness data and SLIM RMS roughness data against the MTM traction data for both $PAO10+ZrO₂$ and $75W-80+ZrO₂$, validating the expectation of a nearly linear thickness-traction correlation over a substantial range of thicknesses. Notably, this does not apply below SLIM thickness values of \sim 5–10 nm, partly because the SLIM measurement uncertainty is of a similar magnitude, and partly because the initial λ ratio for these tests is above 1. However, once the growth of a rough triboflm instantiates, a quasi-linear correlation holds within the range of 10–50 nm of triboflm growth, our region of

Fig. 4 Top: An approximately linear correlation between traction and SLIM signals under boundary contact conditions for all but the lowest (below~10 nm) and highest (above~50 nm) tribofilm thicknesses. This holds for all SRRs and blends under consideration (left: 75W-80, right: PAO10). The inset on 75W-80 magnifes the region outlined in gray. Bottom: The RMS of the SLIM signal is well correlated with traction in the case of PAO10, but not for 75W-80. In all graphs, the connecting lines represent the vector of time (generally left-to-right) during an MTM test

interest for growth kinetics. Below 10 nm in thickness, the uncertainty of the SLIM instrument makes quantifcation unreliable; above approximately 50 nm in thickness, most of these $ZrO₂$ tribofilms have plateaued in height. Therefore, if we remain in boundary contact conditions, and if the

triboflm is in a formation regime rather than induction or steady state, then we can draw inferences about the interface using the 1 Hz traction signal to qualitatively fll gaps in the 1/60th Hz SLIM signal.

The correlation between RMS roughness of SLIM and traction coefficient is less clear. $PAO10+ZrO₂$ displays a clear correlation regardless of SRR, but $75W-80+ZrO₂$ does not. The 100% SRR case, for example, has a nearly $5 \times$ spread in RMS values without significant change to the traction coefficient. Roughness does affect the traction coefficient, but it is not the only process to do so.

This technique enables new experimental approaches to take advantage of the MTM-SLIM system. It can be used to save time over long MTM tests by acquiring less SLIM data without loss of nuance, or even to augment ex situ tribofilm measurements with traction data if SLIM is unavailable, or if triboflm formation only occurs on the disc which SLIM does not image (this could happen, for instance, with dissimilar ball and disc materials). Indeed, for these data, we supplement the 6 MTM-SLIM experiments shown in Fig. [1](#page-3-1) with an additional 18 traction-only MTM tests for the sake of replication (viewable in SI3). The traction trends shown throughout the remainder of this paper are the averages of 4 experiments $(n=4)$ per combination of SRR and blend. However, we did not attempt (nor do we recommend) the use of curve-fts to *predict* SLIM thickness values using a recorded traction signal. Rather, we use traction as corroboration and context for the SLIM thickness data.

3.5 Co‑additives Alter Tribological Interface During Growth

For all triboflm-forming blends in this study, observable tribofilm growth begins near 10^3 contact cycles (Fig. [5\)](#page-6-1). After this initial growth period, we observe non-monotonic triboflm growth via SLIM, indicating that removal processes overtake growth processes (Fig. [2](#page-4-1)), followed by net growth again, eventually reaching a steady-state for the last portion of each test. As a frst-order, lower-bound approximation, RMS values from the SLIM data add context to the endof-test morphologies shown in Fig. [3](#page-5-0) by providing cycleresolved information during triboflm growth (namely, that RMS tends to increase with the mean SLIM value). Apart from this commonality, the behavior of traction, thickness, and roughness varies signifcantly as a function of SRR and co-additive.

For example, $75W-80+ZrO₂$ at 25% and 50% SRR have very uniform RMS SLIM values throughout the entire test, unlike the corresponding PAO10 tests. As well, all three co-additized tribofilms are, by the end of experiment, 1.6x–2.3× thinner and 1.1x –4.8× smoother than their PAO10 analogs. One reason for these diferences is already suggested by Figs. $1-3$ $1-3$: tribofilm removal processes. The

Fig. 5 Triboflm interfacial traction data (top), SLIM triboflm thickness (middle row), and the RMS of the SLIM thickness (bottom) *vs.* logarithmic ball cycles for $ZrO₂$ tribofilms grown in mixed rolling/ sliding experiments. The right set of plots describes triboflms formed from $ZrO₂$ in PAO10, while the left set is for $ZrO₂$ in the co-additized 75W-80 oil. The insets for the traction and SLIM thickness data are plotted on a linear scale for ball cycles for comparison (with the same vertical range as each full plot). The inset for the 75W-80 RMS SLIM

thickness magnifes the outlined region for clarity

co-additives present in $75W-80+ZrO₂$ apparently make triboflm removal more favorable than in PAO10 blends, hence a thinner fnal triboflm in Figs. [1](#page-3-1), [5.](#page-6-1) However, that same removal also polishes the interfaces of 75W-80-based tests to be smoother at end of test (Fig. [3](#page-5-0)) and during the latter stages of growth (Fig. [5](#page-6-1)) compared to the PAO10-based formulation at each SRR. A more polished triboflm bears contact more evenly (SI 2) and shifts the EHD lubrication regime toward mixed contact, giving a lower-traction signal during the majority of the MTM experiments (Fig. [5\)](#page-6-1).

Note, however, that $75W-80+ZrO₂$ formulations have slightly *higher* traction $(1.4x-1.6x)$ during the initial $10³$ cycles of contact than the $PAO10 + ZrO₂$ formulations, before the triboflms are fully formed. It may be that the S- and P-based co-additives are reacting with surface

steel to prevent early scuffing in the interface $[8]$ $[8]$, and/or that the $ZrO₂$ tribofilm initially grows more quickly due to chemical cooperation with the co-additives (discussed further in Sect. [3.7](#page-8-0)). Either way, after the removal rates of $75W-80+ZrO₂$ tribofilms begin to temporarily equal and/or outstrip triboflm growth rates, as demonstrated by SLIM, traction grows less quickly, suggesting that removal and polishing does indeed lead to more favorable traction conditions.

This further supports the hypothesis that, for the boundary contact regime, triboflm removal acts to polish the tribofilm and increases the λ ratio, decreasing traction. This polishing, the removal of local outliers seen in Fig. [2,](#page-4-1) appears to be more signifcant in the presence of co-additives, which explains why the traction coefficients for the 75W-80-based blends are generally lower than that of the PAO10-based blends after the non-monotonic flm thickness events (i.e., after the moments when removal outstrips growth). We hypothesize that, if the S- and P-based co-additives in 75W-80 are incorporated into $ZrO₂$ tribofilm, they promote faster-growing but less removal-resistant triboflms, leading to a smoother and lower-traction interface as the triboflm reaches steady state.

3.6 Co‑additives Are Incorporated into Triboflm

To further test the hypothesis that co-additives contribute to the smoother and lower-traction triboflms at the end of test, we used ToF-SIMS to measure the chemical constituents of the steady-state triboflm formed on the steel MTM disc in 75W-80 + 1wt%ZrO₂ at 50% SRR (a replicate of the specimen shown in Figs. [1](#page-3-1), [2,](#page-4-1) [3\)](#page-5-0). As ToF-SIMS does not give absolute concentrations (*i.e.*, a similar ion count per extraction does not imply two elements have similar concentrations in the sample), this technique is only used here to confrm elemental abundance—relative to that element—as a function of depth.

Figure [6](#page-7-0) confrms that the steady-state triboflm is comprised of Zr and O species. The 52,100 steel substrate means Fe is also present; because the ToF-SIMS measurement did not etch all the way to the substrate, we cannot be certain whether Fe is a trace signal or is intermixed with the $ZrO₂$. However, TEM lamella analyzed for similar $ZrO₂$ tribofilms formed in MPR tests show a sharp Fe-ZrO₂ interface $[25]$ $[25]$, and ToF-SIMS results from Elinski et al. (albeit a diferent ToF-SIMS instrument, with diferent primary beam and other settings) show far more Fe in the substrate than in the triboflm region [[8\]](#page-9-7).

Additionally, several P-containing species are seen in the negative polarity spectrum(S-containing species are also possible, but the S peak is convoluted with O_2). The 75W-80 oil is formulated with phosphorus- and sulfur-based (P/S) EP additives, resulting in 0.1–0.17 wt% P and 2.0–2.7 wt%

Fig. 6 Chemical depth profles measured by ToF-SIMS of the tribofilm formed on the steel MTM disc in $75W-80+1wt\%ZrO₂$ at 50% SRR. Bottom: negative polarity profles; top: positive polarity profles. P- and S-containing species (red and green profles, respectively) coincide with Zr species (blue profles) for tens of nm into the surface of the triboflm, evidence of integration of co-additives into the triboflm. Species originating as components of the steel substrate are shown in gray

S in the fnished product [\[33\]](#page-10-22), but the specifc molecular details are proprietary. Though the 52,100 steel substrate has C, Cr, and Mn inclusions [[34\]](#page-10-23), as well as a native oxide surface layer, P and S are minimal in the steel $(< 0.025$ wt.% [\[34](#page-10-23)]) and in the $ZrO₂$ nanocrystals. Therefore, P- and S-containing species present in the $ZrO₂$ tribofilm for tens of nm of depth (Fig. [6](#page-7-0)) can be attributed to the incorporation of P- and S-based EP co-additives into the triboflm at non-negligible levels, potentially infuencing the growth and removal processes and the tribological properties of the triboflm. This supports the hypotheses posed above that incorporated co-additives infuence the balance between tribosintering and triboflm removal processes, in most cases leading to a smoother and thinner flm, and a lower-traction interface at steady state than for $ZrO₂$ alone (Fig. [5](#page-6-1)). The co-additives lead to smoother $ZrO₂$ interfaces once steady state is reached (Fig. [3](#page-5-0)), but the physico-chemical mechanisms by which these processes occur remain to be understood. Eforts to understand this using the quantum chemical calculations of ab initio density functional theory (DFT) are in progress on models representative of the $75W-80/ZrO₂/ligand system$ and will be the subject of a future publication.

3.7 Growth Kinetics and Formation Mechanisms

To compare the growth kinetics explicitly, we isolated the growth stages of each SLIM and traction signal (Fig. [7\)](#page-8-1) and estimated their growth rates (SI 3 and SI 4). The earliest work on these $ZrO₂$ nanocrystals proposed a 3-phase tribosintering mechanism for flm formation, supported by later studies on the same NC system [[8,](#page-9-7) [20](#page-10-9), [23\]](#page-10-13): an induction period of no observable growth, a nearly linear growth phase, and a steady-state phase. As discussed above, in most of our MTM experiments, the growth phase exhibited transient reversals of triboflm growth, attributed to removal processes overtaking growth processes. For those cases, we calculated two linear stages of growth, before (flled data markers and colorful guidelines) and after (hollow data markers and gray guidelines) the transient.

The increased SRR negligibly changes the initial growth rate from SLIM for $PAO10 + ZrO₂$, but significantly increases that of $75W-80+ZrO₂$ (Fig. [7](#page-8-1), left). The traction data exhibit the same trend (Fig. [7](#page-8-1), right), consistent with our contention in Sect. [3.3](#page-4-0) that traction may be taken to be a higher time-resolution proxy for triboflm growth for the linear growth stages of the experiment. The latter also allows us to leverage our large experimental dataset for the $n=4$ trials for each set of conditions. Moreover, the increased initial growth rate with increased SRR for $75W-80+ZrO₂$ provides new and strong support for the claim by Elinski

Fig. 7 Average growth rates as a function of sliding speed and lubricant co-additives, derived from SLIM (left, number of trials $n=1$) and traction (right, $n=4$). The slopes are obtained from linear fits before and after any net-negative removal events (method in SI3); the latter linear stage is plotted with hollow data points and gray lines to guide the eye and ofset right to illustrate the temporal ordering. Blue lines guide the eye for the initial rates of PAO10 blends, and orange lines do the same for those of 75W-80. Increasing the SRR has a stronger positive effect on the growth rates of $ZrO₂$ tribofilms in 75W-80

et al*.* [[8\]](#page-9-7) that the S- and P-based co-additives cooperate with $ZrO₂$ to promote faster tribofilm growth that largely prevents the moderate amount of early-stage wear of the substrate that occurs with $PAO10 + ZrO₂$.

When tribosintering again outpaced triboflm removal after the transient period (*i.e*., during the second linear stage), the growth rates were consistently smaller than during the frst linear stage in all cases. Especially striking was that the strongly SRR-dependent growth rates seen for $75W-80+ZrO₂$ prior to the transient period no longer occur; their kinetics resemble those of additive-free $PAO10+ZrO₂$. Co-additives thus boost tribosintering rates of $ZrO₂$ only during the frst linear stage. While we are unable to formulate a mechanism to explain this presently, we will attempt to use the aforementioned DFT simulations to determine whether and how S and P chemistries alter the chemical affinity of $ZrO₂$ surfaces in ways that would alter growth and removal processes including sintering, abrasion, and adhesive transfer.

4 Conclusions

Metal oxide nanocrystal additives quickly form robust antiwear flms under a variety of conditions that normally lead to scuffing and micropitting $[8, 20, 22-25]$ $[8, 20, 22-25]$ $[8, 20, 22-25]$ $[8, 20, 22-25]$ $[8, 20, 22-25]$ $[8, 20, 22-25]$ $[8, 20, 22-25]$, including in fully formulated commercial gear oils with lower viscosities intended to increase energy efficiency $[26]$ $[26]$ $[26]$. This work unlocks new insights into metal oxide nanocrystal triboflm formation by pairing in situ triboflm thickness measurements via SLIM with analysis of high-resolution traction data in MTM experiments.

We attributed the interrupted, two-stage growth of $ZrO₂$ triboflms to transient triboflm removal events observed with SLIM. Traction coefficients and thickness values were correlated during most of the triboflm growth phase, including when triboflm removal events temporarily outpaced growth. This correlation assumes boundary contact, triboflms thicker than the SLIM's measurement error (5–10 nm), and triboflms not yet saturated in thickness. Thus, high time-resolution traction measurements can, with caution, be used as proxies to track triboflm growth kinetics to supplement SLIM measurements and/or provide replication of trends without the need to perform additional SLIM measurements, thus increasing experimental throughput.

The addition of industry-standard S- and P-based AW and EP co-additives to a PAO-based, ZrO_2 -containing lubricant:

increases the initial growth rate of tribofilms. We propose that this contributes to the superior anti-scuffing performance these blends exhibit compared to those with $ZrO₂$ alone;

- enhances tribofilm polishing to generate overall thinner triboflms but with smoother triboflm surfaces, and thus more favorable lubrication conditions; and
- does not afect the second-stage triboflm growth rate (*i.e.*, after triboflm removal outpaces triboflm growth).

As S and P are incorporated into the triboflms, all of the above efects may be driven by chemical mechanisms that will be the subject of future investigation.

In summary, consistent with earlier work, we demonstrate in further depth here that S- and P-based co-additives provide substantial benefits for $ZrO₂$ tribofilm performance [\[8](#page-9-7)]. This work offers a more precise look at the qualities and features of triboflm performance which are improved by the cooperative behavior of co-additives and $ZrO₂$.

Future work will explore the removal mechanisms of the triboflm. Several mechanisms are possible: adhesive transfer of $ZrO₂$ to the MTM disc specimen (as the disc's tribofilm is not measured in SLIM), abrasive wear of the triboflm, plastic flow, and/or erosive wear (which is unlikely because of the boundary contact in these conditions). MTM, AFM, and nanoindentation techniques are being used to explore these, along with DFT calculations. Whatever the mechanism, this connection between co-additives and triboflm removal is perhaps most important when it comes to growth kinetics, so that $ZrO₂$ tribofilms can form rapidly and thus prevent failure of contacting parts.

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Author Contributions All authors contributed to the study conception and design. Nanocrystals and formulations were prepared by L.Z. and R.J.W. Data collection and analysis were performed by P.L., M.B.E., D.D., P.N., and J.G. The manuscript was drafted by P.L. with significant input from J.G. and D.D., and overseen and edited by R.W.C. All authors read and approved the fnal manuscript.

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Data Availability Data unavailable.

Declarations

Competing Interests L.Z., A.J., and R.J.W. are afliated with the commercial vendor for the ZrO2 nanocrystals (Pixelligent Technologies, LLC). L.Z. and R. J.W. are employees of Pixelligent and have equity in the company. A.J. is a consultant to Pixelligent. No other coauthors declare competing fnancial interest.

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