

# Improving the performance of feature selection and data clustering with novel global search and elite-guided artificial bee colony algorithm

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# Abstract

As known, the artificial bee colony (ABC) algorithm is an optimization algorithm based on the intelligent foraging behavior of honey bee swarm that has been proven its efficacy and successfully applied to a large number of practical problems. Aiming at the trade-off between convergence speed and precocity of ABC algorithm with elite-guided search equations (ABC\_elite), an enhanced version, namely EABC\_ elite, is proposed in this paper, and the improvements are twofold. As the global best (gbest) solution is introduced to the search equation and acceleration of the convergence in the bee phase of EABC\_elite, the former in the ordinary solution is embodied to the search equation yet balance the gbest's ability. The enhancement to the global search by making the information of gbest and ordinary solutions be adequately used while keeping the exploration-exploitation balance well maintained, the usual solution is introduced to the search equation to avoid the precocity problem in the onlooker bee phase of EABC\_elite as the latter one. Experimental analysis and evaluations of EABC elite against several state-of-the-art variants of the ABC algorithm demonstrate that the EABC elite is significantly better than the compared algorithms in the feature selection problem. Also, the proposed EABC elite algorithm is modified to combine the K-means initialization strategy and chaotic parameters strategy to further enhance the global search of EABC\_elite for data clustering. Experimental results show that the derived EABC elite clustering algorithm "Two-step EABC\_elite," TEABC\_elite for short, delivered better and promising results than previous works for data clustering.

Keywords Artificial bee colony · Data clustering · Feature selection · Global search

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With the advances in science and engineering moving at a faster pace than ever, optimization techniques play an essential role. During the recent past, evolutionary algorithms (EAs) have achieved with success yet solving in effectively way optimization problems characterized by non-convex, discontinuous, and nondifferentiable. Some famous EAs have been proposed, such as genetic algorithm (GA) [1], differential evolution (DE) [2], particle swarm optimization (PSO) [3], and ant colony optimization (ACO) [4]. Artificial bee colony algorithm (ABC) [5–8] is a most recently proposed EA that belongs to the group of swarm intelligence algorithms that mimics the intelligent foraging behavior of honey bees. When compared to selected state-of-the-art EAs, such as GA, DE, and PSO [5–7], comparison results indicate its efficacy and also competitive performance. It has been proven to show superior performance when dealing with optimization problems, owing to its simple structure and excellent performance [8], such as flowshop scheduling problem [9], filter design problem [10], and vehicle routing problem [11].

Despite ABC's excellent performance, it suffers from slow convergence speed yet easily being trapped by local optimum, which is mainly due to its solution search equation, that is very good in exploration though poor in exploitation, unfortunately. For the sake of the excellent performance on optimization problems, the primary challenge is how to maintain the exploration–exploitation balance during the search process [12].

A large number of ABC variants have been proposed to improve the overall performance. Firstly, Zhu and Kwong [13] introduced the global best (gbest) solution into the search equation of ABC to enhance the exploitation ability of ABC, though some follow-up researches indicate that the use of gbest easily outcome in the precocity problem since all individuals learn from the gbest solution. To settle this problem, Gao and Liu [14] proposed a novel crossover operator-based ABC (CABC), which has no bias in any search direction. Cui et al. pointed out that, despite CABC can avert precocity effectively, the useful information of the population has not been utilized effectively, especially the information of gbest [15]. After that, they proposed a novel elite-guided ABC, ABC\_elite for short, which can keep a better balance between accelerating convergence and averting precocity problem. Experiments show that the ABC elite is significantly better than several state-of-theart ABC variants, such as BABC [12], CABC [14], ABCVSS [16], best-so-far ABC [17], MABC [18], qABC [19], EABC [20], and several PSO and DE variants on most of the test functions in terms of solution quality, robustness, and convergence speed. Thus, it is noted that the novel revised search equations are the main factors for the success of ABC elite. Nevertheless, all candidates are generated around elite solutions in the search equations of ABC\_elite, where the information of ordinary solutions has not been utilized effectively, so the search area is relatively small and the global search ability should be improved. Meanwhile, the information of gbest is only utilized by the elite individuals, added to the hard exploitation ability of ABC\_ elite in the onlooker bee phase, which quickly falls in precocity problem.

To solve the abovementioned items, this paper proposes an enhanced version of ABC\_elite, namely EABC\_elite. The contributions of this paper are as follows:

- A novel enhanced version of ABC\_elite is proposed using two novel search equations. In EABC\_elite, all individuals are guided by the global best solution that can accelerate the convergence process. Ordinary individuals are also embedded in the search equation to balance exploration and exploitation that effectively enhance the global search ability of ABC\_elite. Through the experimental data, EABC\_elite has not only faster convergence speed but also good global search ability, maintaining the simplicity of ABC\_elite, and bringing the computation complexity of EABC\_elite and ABC\_elite approximately the same. Experimental results show that EABC\_elite performs well on unimodal, multimodal, shifted, and rotated functions when compared with recently ABC and non-ABC variants. Additional experiments on UCI machine learning datasets show that EABC\_elite is a compelling feature selection tool.
- By combining the *K*-means initialization strategy and chaotic parameters strategy with EABC\_elite, a novel data clustering method named TEABC\_elite is proposed. Experimental results on UCI machine learning datasets show its effectiveness as clustering tool, owing to its excellent global search ability.

The remaining of this paper is organized as follows. Related work on ABC is presented in Sect. 2, and a novel elite-guided ABC with global search equations is proposed in Sect. 3, EABC\_elite for short. Section 4 presents the comparison experiments with other ABC variants and deriving a variant of the EABC\_elite named two-step EABC\_elite (TEABC\_elite for short) by combining the *K*-means initialization strategy and chaotic parameter strategy to further enhance the global search ability aiming at solving the clustering problem in Sect. 5. Finally, concluding remarks are given in Sect. 6.

# 2 Related work

# 2.1 Original ABC

As known, the ABC algorithm has been developed to mimic the foraging behaviors of honey bee colonies, where the location of the food source represents the potentially best solution to a problem, and the amount of nectar per food source represents the quality of the solution. It consists of four sequentially realized phases, namely initialization, employed bee, onlooker bee, and scout bee phases. After initialization, it turns to be a cycle that uses the employed bee phase, onlooker bee phase, and scout bee phase. The complete execution for each phase is depicted as follows:

• Initialization phase: At the beginning of ABC, each food source is randomly generated, following

$$x_{i,j} = x_j^L + rand_j(x_j^U - x_j^L)$$
(1)

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where i = 1,...SN, j = 1,...D, SN denoting the number of food sources (SN=the number of employed bees = the number of onlooker bees) and D the dimensionality of the optimization problem. The  $x_j^L$  and  $x_j^U$  are the lower and upper bounds of the *j*-th dimension, respectively, and *rand<sub>j</sub>* is a randomly generated number in the range [0, 1]. Next, the fitness value of each food source is obtained as:

$$fit_{i} = \begin{cases} \frac{1}{1+f(x_{i})} & \text{if } (f(x_{i}) \ge 0) \\ 1+|f(x_{i})|, & \text{otherwise} \end{cases}$$
(2)

where *fit<sub>i</sub>* denotes the fitness of the *i*-th food source  $x_i$ , and  $f(x_i)$  the objective function value of the food source  $x_i$ . In the initialization phase, the parameter *limit* should be predetermined, whereas the parameter *counter* is used to record the number of unsuccessful updates and set to zero for all food sources.

• Employed bee phase: Each employed bee searches for a food source and tries to locate a candidate food source near the corresponding parent food source according to

$$v_{ij} = x_{ij} + \phi_{ij} * (x_{ij} - x_{kj})$$
(3)

where  $i, k \in \{1, 2, ..., SN\}, j \in \{1, 2, ..., D\}, v_{i,j}$  is the *j*-th dimension of the *i*-th candidate food source (new solution);  $x_{i,j}$  is the *j*-th dimension of the *i*-th food source;  $x_{k,j}$  is the *j*-th dimension of the *k*-th food source; k is picked up from  $\{1, 2, ..., SN\}$  randomly and  $k \neq i$ ; *j* is randomly selected from  $\{1, 2, ..., D\}$ ;  $\phi_{i,j}$  is a randomly generated number in the range of [-1, 1]. After establishing a new food source, the fitness of the candidate food sources is calculated by Eq. (2). If the candidate food source is superior to the old food source, the food source will replace the old food source and the *counter* value of the food source will be reset to zero. Otherwise, the *counter* value is incremented by 1.

Onlooker bee phase: According to the quality information of the food sources provided by the employed bees, each of the onlooker bees will fly to the food source x<sub>s</sub>, as chosen by the roulette wheel to generate a candidate food source using Eq. (3). Besides, the selection probability of the i-th food source is calculated as Eq. (4). Note that, the higher the fitness value is, the higher the selection probability is. If a candidate food source v<sub>s</sub> generated by the onlooker bee is better than the food source x<sub>s</sub>, x<sub>s</sub> will be replaced by the new one, and its *counter* value is reset to zero. Otherwise, its *counter* value is increased by 1.

$$P_i = \frac{fit_i}{\sum_{i=1}^{SN} fit_i} \tag{4}$$

• Scout bee phase: The food source with the highest *counter* value is selected. If the *counter* value is larger than the *limit* value, the food source is reinitialized according to Eq. (1). After the new food source is generated, the corresponding *counter* value is reset to zero. Note that, if  $v_{i,j}$  violates the boundary constraints in the employed bee phase and onlooker bee phase, the reset is required, according to Eq. (1).

# 2.2 Improved ABCs

The balance between exploration and exploitation abilities plays an essential role in EAs. The exploration ability denotes the ability of an EA to search unknown area, whereas the exploitation ability denotes the ability of an EA to search around the already found area elaborately. An EA with strong exploration ability can easily escape the local optima, though the EA will evolve slowly. Nevertheless, if an EA has strong exploitation ability, the EA will evolve fast and quickly get trapped into the local minima. Whether an EA can balance the two contradictory aspects is the key to obtain a relatively high performance yet efficiency.

# 2.2.1 GABC algorithm

Inspired by PSO in 2010, Zhu and Kwong [13] proposed an improved version of ABC algorithm called GABC, which incorporates the information of the global best (gbest) solution into their solution search equation, enhancing the exploitation ability of ABC.

$$x_{i,j} = x_{i,j} + \phi_{i,j} \cdot (x_{i,j} - x_{k,j}) + \psi_{i,j} \cdot (x_{best,j} - x_{i,j})$$
(5)

where  $\psi_{i,j}$  is a randomly generated number in the range of [0, 1.5]. The term  $x_{best,j}$  denotes the *j*-th element of the gbest, a newly proposed term. Experimental results demonstrate that GABC is better than the original ABC on most of the cases. Based on GABC, many improved versions have been proposed consecutively.

# 2.2.2 IABC algorithm

As claimed in [14], Eq. (5) may cause oscillations, so the convergence may be deteriorated, since the guidance of the last two terms may be in opposite directions. To solve this problem, Gao and Liu [21] proposed IABC, an improved search equation given by:

$$x_{ij} = x_{best,j} + \phi_{i,j} \cdot (x_{i,j} - x_{r1,j})$$
(6)

where r1 is randomly picked up from  $\{1, 2, ..., SN\}, r1 \neq i$ .

# 2.2.3 CABC algorithm

Gao et al. [14] identified that all candidates are generated around gbest according to Eq. (6), so that the exploitation ability of IABC is too strong and easy to result in precocity problem. Therefore, to address the above issues in (5) and (6), they proposed CABC, an enhanced search equation inspired by the crossover operator of GA, as shown in (7):

$$v_{ij} = x_{r1,j} + \phi_{i,j} \cdot (x_{r1,j} - x_{r2,j})$$
<sup>(7)</sup>

where *r*1 and *r*2 are two distinct integers randomly picked up from {1, 2,..., *SN*}, and both are different from the base index *i*. Equation (7) has no bias to any search direction, and there is only one guidance  $\phi_{i,j}(x_{r1,j} - x_{r2,j})$  in (7) that can effectively avoid oscillation phenomenon. After that, the search capability of ABC is significantly improved by (7).

# 2.2.4 MGABC algorithm

To avoid the oscillation phenomenon in GABC, Cui et al. [22] proposed an improved version of GABC, namely MGABC, shown as

$$v_{i,j} = \begin{cases} x_{i,j} + \phi_{i,j}.(x_{i,j} - x_{k,j}), & \text{if } rand < P\\ x_{i,j} + \psi_{i,j}.(x_{best,j} - x_{i,j}), & \text{otherwise.} \end{cases}$$
(8)

where *P* is a newly introduced parameter, 0 < P < 1, and other symbols have the same meaning as (5).

### 2.2.5 ABC\_elite and DFSABC\_elite algorithms

Cui et al. [15] have pointed out that, despite CABC has strong global search ability, the success information of the population is not utilized, either not utilized the valuable information of gbest. To best utilize the useful information and maintain the balance between exploration and exploitation, they proposed ABC\_elite, a novel version of elite-guided ABC using two novel search equations as shown in (9) and (10):

$$x_{i,j} = x_{e,j} + \phi_{i,j} \cdot (x_{e,j} - x_{k,j})$$
(9)

$$x_{e,j} = \frac{1}{2}(x_{e,j} + x_{best,j}) + \phi_{e,j} \cdot (x_{best,j} - x_{k,j})$$
(10)

where  $x_e$  is a randomly selected elite solution from the top *p.SN* solutions,  $p \in (0, 1)$ ,  $x_k$  is randomly chosen from the current population;  $e \neq k \neq i$ ,  $x_{best}$  is the global best solution;  $\phi_{i,j}$  and  $\phi_{e,j}$  are two randomly generated numbers in [-1, 1].

Equation (9) is used in the employed bee phase that exploits the beneficial information from the elite solutions, while Eq. (10) is used in the onlooker bee phase to simultaneously exploit the valuable information among current best solution and other elite solutions. Meanwhile, Cui et al. [15] proposed a novel depth-first strategy (DFS) to accelerate the convergence process. In DFS, a food source will search its vicinity continuously until a failed search is finished. By combining ABC\_elite with DFS, the DFSABC\_elite algorithm is proposed in [15].

Under the guidance from only one term, Eqs. (9) and (10) can also easily avoid the oscillation problem. In this way, the ABC\_elite and DFSABC\_elite algorithms can better balance the exploration and exploitation and have shown better performance when compared with other state-of-the-art EA variants, such as the GABC [13], CABC [14], best-so-far ABC [17], MABC [18], qABC [19], EABC [20], ABCVSS [16], BABC [12], and several PSO and DE variants.

## 2.2.6 IABC\_elite algorithm

The high performance of ABC\_elite and DFSABC\_elite has attracted some followup researches. Inspired by the theory of labor division of honey bees, Du et al. [7] proposed IABC\_elite, an improved version of the ABC\_elite algorithm to enhance the exploitation ability of ABC\_elite by using two new search equations in the employed bee phase and onlooker bee phase of ABC\_elite, respectively.

$$v_{i,j} = N\left(\frac{x_{best,j} + x_{i,j}}{2}, |x_{best,j} - x_{i,j}|\right)$$
(11)

$$v_{e,j} = \frac{1}{2}(x_{e,j} + x_{best,j}) + \phi_{e,j}(x_{best,j} - x_{e',j})$$
(12)

where  $x_{i,j}$  is the *j*-th element of elite solution  $x_i$ ;  $x_{best,j}$  is the *j*-th element of the global best solution found so far; *j* is randomly selected from  $\{1, 2, ..., D\}$ ; e' is the number of a randomly selected elite solution; and Eq. (11) is used in the employed bee phase only to refine the elite individuals and enhance the exploitation ability. For the sake of the exploration–exploitation balance, ordinary individuals still use Eq. (9). In the onlooker bee phase of IABC\_elite, the elite individuals alternatively use Eqs. (10) and (12) at probability  $P_o$  and  $1 - P_o$ , respectively, and  $P_o$  decreases as the iteration number increases to enhance the exploitation ability gradually. Given that Eqs. (11) and (12) have strong exploitation ability, the DFS strategy of DFSABC\_elite is discarded in IABC\_elite to maintain a better balance of exploration–exploitation.

# 2.2.7 ECABC algorithm

To further enhance the exploitation ability of DFSABC\_elite and inspired by the natural phenomenon that honey bees follow the elite group in the foraging process, Kong et al. [23] proposed ECABC, a novel elite group center-based artificial bee colony algorithm. In ECABC, Eqs. (9) and (10) are all replaced by equation

$$v_{i,j} = XEC_j + \phi_{i,j}(x_{best,j} - x_{k,j}) \tag{13}$$

where *XEC* is the center of the elite group. By comparing Eq. (13) to Eqs. (9) and (10), we can identify that Eq. (13) has strong exploitation ability, since the base vector *XEC<sub>j</sub>* of Eq. (13) is only composed of elite individuals and the disturbation part  $\phi_{i,j}(x_{best,j} - x_{k,j})$  always include the gbest term  $x_{best}$  both in the employed bee phase and in the onlooker bee phase. That is, ECABC only searches around elite individuals. To better maintain the balance of exploration–exploitation, ECABC abandoned the DFS strategy of DFSABC\_elite in the employed bee phase and still use the DFS strategy in the onlooker bee phase.

# 2.2.8 ABCLGII algorithm

With the introduction of communication mechanisms into ABC, Lin et al. [24] proposed ABCLGII, a novel ABC algorithm with local and global information interaction. They use Eq. (14) in the employed bee phase to mimic the local interaction of honey bees.

$$v_{i,j} = x_{i,j} + rand(0,1) \cdot (x_{nbest,j} - x_{i,j})$$
(14)

where  $x_i$  is a randomly selected ordinary individual; j = 1,...D;  $x_{nbest}$  is the best food source with the smallest objective function within the distance *md* from  $x_i$ . In the onlooker bee phase, ABCLGII alternatively uses two new search Eqs. (15) and (16) at probability  $P_{str}$  and  $1 - P_{str}$ , respectively. At the initial stage,  $P_{str}$  is initialized to 0.5, and after all high-quality food source positions are searched by the onlooker bees (i.e., elite individuals),  $P_{str}$  will be updated.

$$v_{ij} = x_{pbest,j} + \phi \cdot (x_{i,j} - x_{k,j}) \tag{15}$$

$$v_{i,j} = x_{best,j} + \phi \cdot (x_{best,j} - x_{i,j}) \tag{16}$$

where  $x_i$  and  $x_{pbest}$  are all randomly selected elite individuals,  $i \neq pbest$ . That is, only elite individuals (high-quality food sources) have a chance to attract onlooker bees to exploit within their vicinity, which is the same as DFSABC\_elite.

# 3 Proposed approach

In this section, we will first analyze the merits and demerits of ABC\_elite and then propose an enhanced global search ABC\_elite, EABC\_elite for short.

### 3.1 Evaluations of ABC\_elite

In contrast to GABC, CABC, and IABC, the main advantage of ABC\_elite is that it can better balance the exploration and exploitation ability by using elite-guided search equations. GABC and IABC are guided by gbest, yet easy to result in precocity problem. Although CABC can solve precocity problem effectively by removing gbest from its search equation and maintain higher global search ability, CABC can also suffer from a slow convergence speed due to the lack of the previous success information of the population.

Although ABC\_elite has shown to be competitive to other EAs, there are still drawbacks in its solution search equations. In such equations, a candidate solution is produced by adding a disturbation vector to a base vector. To be specific, in Eq. (9), the base vector is  $x_e$  and the disturbation vector is  $x_e - x_k$ . In Eq. (10), the base vector is  $(x_{best} + x_e)/2$ , and the disturbation vector is  $x_{best} - x_k$ .

For simplicity, the coefficient  $\phi$  is not considered since it is the same in all ABCs. As noted, the base vectors of these equations are elite solutions, and all candidates are generated around elite solutions, so the search area of ABC\_elite is relatively small since elite solutions only account for a small proportion p (p=0.1 in [15]).

In the search equation of ABC, GABC, and CABC (respectively, Eqs. (3), (5) and (7)), the base vectors are all ordinary solutions, providing sufficient opportunity for ordinary solutions to take part in the evolution process. Therefore, the algorithms have a high global search ability. However, in the search Eqs. (9) and (10) of ABC\_elite, the base vectors are all elite solutions. Thus, the ordinary solutions have no sufficient opportunities to be exploited, as they take only part in the evolution process as a disturbation vector but not a base vector. Besides, the disturbation amplitude in (9) is relatively significant, since the  $x_{best}$  is the current best solution in

the population, and  $x_k$  is an ordinary solution. Generally speaking, the fitness of  $x_{best}$  is far better than  $x_k$ , thus  $|x_{best,j} - x_{k,j}|$  is a relatively big disturbation with high probability, which will result in the candidate generated by (10) away from elite solutions and  $x_{best}$ .

# 3.2 Motivation

In the literature, the high performance of ABC\_elite and DFSABC\_elite has attracted much attention. Although recently developed ABC\_elite variants have improved the performance of ABC\_elite, they have their shortcomings. IABC\_elite is the first improved ABC\_elite variant, but in IABC\_elite only elite individuals have a chance to be guided by the gbest solution since Eq. (11) is used only by elite individuals to maintain exploration–exploitation balance and Eqs. (10) and (12) in IABC\_elite are all used for elite individuals. That is, the search of the ordinary individuals is almost blind, which make up most of the population. Therefore, the proposed Eqs. (11) and (12) are mainly used to refine elite solutions.

ECABC is the latest proposed ABC\_elite variant and has shown excellent performance when compared to several state-of-the-art ABC variants, though we have not seen its comparisons with non-ABCs especially on shifted and rotated functions or real-world problems. The most significant shortcoming of ECABC is its excessive exploitation ability since, as mentioned above, the basic vector of the right hand of Eq. (13) is only composed of elite individuals (including gbest) and the disturbation part in the right hand of Eq. (13) includes the gbest term. Results show that ECABC beats DFSABC\_elite when D=30 by a large score 3:9, but when the dimension Dincreases to 50 and 100, the scores are only 5:6 and 5:7, respectively [23]. That is, ECABC only beats DFSABC\_elite in low-dimensional functions due to the excessive exploitation ability which is beneficial for solving simple functions (i.e., unimodal functions and low-dimensional functions). ABCLGII faces the same problem as ABC\_elite and IABC\_elite, i.e., ordinary individuals are not influenced by gbest.

In this paper, a novel enhanced ABC\_elite (EABC\_elite) is proposed, where all the ordinary individuals are guided by gbest while the balance of exploration–exploitation can still be well maintained. Experimental results show that EABC\_elite has significant advantages over DFSABC\_elite on 22 basic functions and CEC 2015 [25] shifted and rotated functions. By contrast, several recent proposed ABC variants have similar performance with DFSABC\_elite. For example, the newly proposed grey ABC beats DFSABC\_elite only at a score of 15:14 on CEC functions [26]; DFSABC\_elite beats the newly proposed ABCG on CEC functions [8].

# 3.3 Proposed algorithm

Li and Zhan [27] summarized the developing rules of several EAs and gave a conclusion that "the more information is efficiently utilized to guide the flying, the better performance the algorithm will have." In the original PSO, all particles learn from gbest, which often result in the precocity problem. To settle this problem, a series of improved PSO is proposed consecutively, such as the competitive and cooperative PSO [27], social learning PSO [28], and self-learning PSO [29]. Although the theory of PSO variants is different, they all use more population information to escape the local minima differently. The development of ABC has gone through a similar process. In contrast with GABC, CABC, and IABC, ABC\_elite uses more information to help the algorithm to escape the local minima, so ABC\_elite results the best performance.

In EAs, a prevalent theory is that if an EA employs stronger heuristic information to guide the evolution, a better balance strategy between exploration and exploitation should be employed simultaneously, or the EA will trap in local minima fastly under the guidance of firm heuristic information. ABC\_elite uses the gbest to guide the evolution and uses the elite solutions to weaken the excellent guidance of gbest, so the balance between exploration and exploitation can be well maintained. Although Eqs. (9) and (10) of ABC\_elite can significantly improve the performance of ABC, the valuable information of the gbest is not fully exploited in Eq. (9). To further improve the performance of ABC by using gbest and get a better exploration–exploitation balance effectively, two novel search Eqs. (19) and (20) are proposed, as follows:

$$\mu = \frac{1}{3} \cdot (x_{best,j} + x_{e,j} + x_{k,j}) \tag{17}$$

$$\delta = \frac{1}{3} \cdot \left( \left| x_{best,j} - x_{e,j} \right| + \left| x_{e,j} - x_{k,j} \right| + \left| x_{best,j} - x_{k,j} \right| \right)$$
(18)

$$v_{i,j} = \mu + \phi_{i,j} \cdot \delta \tag{19}$$

$$v_{e,j} = \mu + \phi_{e,j} \cdot \delta \tag{20}$$

where  $\phi_{i,j}$  and  $\phi_{e,j}$  are random real numbers in the range of [-1, 1];  $|\cdot|$  is the absolute value symbol,  $\mu$  is the base vector,  $\delta$  is the disturbation vector;  $x_e$  is a randomly generated elite solution from the top *p.SN* solution,  $p \in (0, 1)$ ;  $x_k$  is randomly chosen from the current population;  $e \neq k \neq i$ ,  $x_{best}$  is the current best solution. Equation (19) is used in the employed bee phase of the proposed algorithm and replace Eq. (9) of ABC\_elite; Eq. (20) is used in the onlooker bee phase of the proposed algorithm and replace Eq. (10) of ABC\_elite.

In the left-hand side of Eq. (20), only elite solutions have a chance to produce candidates, which is the same as (10) of ABC\_elite. By doing so, the computing resources can be focused on elite solutions and the exploitation ability of the algorithm can be enhanced [15]. Herein, the proposed algorithm is called EABC\_elite (enhanced ABC\_elite). Except for (19) and (20), the rest of EABC\_elite is the same as ABC\_elite.

## 3.4 Execution process Of EABC\_elite

The pseudocode of the complete EABC\_elite is shown in Algorithm 1. In each generation, an employed bee will search the neighbor of a randomly selected solution



Fig. 1 Balance strategy comparison

 $x_i$  and produce a candidate solution  $v_i$  according to (19) (line 5) in the employed bee phase. If the candidate solution  $v_i$  is better than  $x_i$ ,  $v_i$  will be recorded by its employed bee and replace  $x_i$ . (lines 6–7). In the onlooker bee phase, an elite solution  $x_e$  is selected randomly to generate a candidate solution  $v_e$  by (20). If the candidate solution  $v_e$  outperforms  $x_e$ ,  $v_e$  will replace  $x_e$ . (lines 15–16). After the employed bee phase and onlooker bee phase, the scout bee phase will begin (lines 22–25). The above three phases will be repeated until the predetermined termination threshold is met. The global best solution which has the smallest objective function value in the final population will be treated as the final optimization results.

# 3.5 Discussions

In EABC\_elite, population information is efficiently utilized to guide the search, as EABC\_elite has no bias to any search directions. Therefore, the global search ability is enhanced, and the precocity problem is effectively averted. The global best (gbest) individual  $x_{best}$  is introduced to Eq. (19) to accelerate convergence. The ordinary individual  $x_k$  is introduced to the search equation to balance the gbest's great leadership ability as well enhance the global search ability of EABC\_elite, so the information of  $x_{best}$  and ordinary individuals  $x_k$  can all be used and the balance between exploration and exploitation can be well maintained.

In Eq. (9) of ABC\_elite, the base vector is composed of only one term, the elite solution  $x_e$ , while in Eq. (19) of EABC\_elite, the base vector is composed of the global best solution  $x_{best}$ , the elite solution  $x_e$ , and the ordinary solution  $x_k$ . Because the global best solution  $x_{best}$  has the strongest exploitation ability and the ordinary solution  $x_k$  has the strongest exploration ability,  $x_{best}$  is "neutralized" by adding  $x_k$ . Finally, the proposed algorithm EABC\_elite can still maintain a good balance between exploration and exploitation.

The balance strategy of Eqs. (9) and (19) has been shown in Fig. 1a, b. In the latter, although the use of  $x_{best}$  can enhance the exploitation ability of EABC\_elite greatly, the use of ordinary solution  $x_k$  can enhance the exploration ability and help EABC\_elite escape from the local minimum. Thus, the balance between exploration and exploitation can be well maintained. Similarly, by using the ordinary solution  $x_k$  in the base vector of (20), the global search ability of EABC\_elite is enhanced, and the precocity problem is effectively averted. Also, the oscillation phenomenon will be effectively avoided since there is only one guiding term in Eqs. (19) and (20).

# 4 Experimental results

In this section, three experiments are conducted to compare the proposed EABC\_ elite with some recently developed ABC and non-ABC variants to validate the performance of EABC\_elite. Two classic test suites are used in experiments 1 and 2, the former one is widely adopted by BCABC [12], CABC [14], ABC\_elite [15], ABCVSS [30] and ECABC [23], and the latter one is the set of famous test suite (CEC 2015 [25]) that consists of 15 shifted and rotated functions, which is harder to solve compared to the basic functions. Experiment 3 is conducted to test the performance of EABC\_elite in solving the feature selection problem, and seven wellknow UCI machine learning datasets (http://archive.ics.uci.edu/ml) are selected to this experiment.

EABC\_elite is compared to ABCLGII [24], ECABC [23], DGABC [31], ABC\_ elite [15], and DFSABC\_elite [15], since the search equation of the basic ABC algorithm is improved using these methods. For the sake of fairness, the initial population of each algorithm is created randomly according to Eq. (1). Experimental results are shown in Tables 3 and 4.

To show the difference between the EABC\_elite and other algorithms, the Wilcoxon [32] rank sum test is carried out for the nonparametric statistics of the independent sample, with the experimental results carried out at the significant level 0.05. That is, the symbols "–," "+," and "=" represent the performance of the corresponding algorithm worse than, better than and similar to that of EABC\_elite, respectively, at a 0.05 significance level of Wilcoxon's rank test in Tables 3, 4, 6 and 7. In Tables 3, 4, 6, 7 and 9, the best results are marked in boldface.

01:	Initialization: Generate SN solutions that contain D variables according to (1); FEs=0
02:	while FEs <max_fes< td=""></max_fes<>
03:	Select the top <i>T=p.SN</i> solutions as elite solutions from population
04:	for <i>i</i> =1 to SN //employed bee phase
05:	Generate a new candidate solution $v_i$ in the neighborhood of $x_i$ using (19), evaluate the candidate solution $v_i$
06:	$\inf_{x \in \mathcal{F}} f(x_i) < f(x_i)$
07:	Replace $x_i$ by $v_i$ and counter(i)=0
08:	else
09:	counter(i)= counter(i)+1
10:	end if
11:	
12:	end for //end employed bee phase
13:	for $i=1$ to $r \cdot p \cdot SN$ //onlooker bee phase
14:	Select a solution $x_e$ from elite solutions randomly to search
15:	Generate a new candidate solution $v_e$ using (20), evaluate the new candidate solution $v_e$
16:	$\text{if } f(v_e) < f(x_e)$
17:	Replace $x_e$ by $v_e$ and counter(e)=0
18:	else
19:	counter(e)= counter(e)+1
20:	end if
21:	end for //end onlooker bee phase
22:	FEs=Fes+ SN + r · p · SN
23:	Select the solution x <sub>max</sub> with max <i>counter</i> value //Scout bee phase
24:	if <i>counter</i> (max)> <i>limit</i> //only one food source with max <i>counter</i> value can be initialized
25:	Replace x <sub>max</sub> by a new solution generated according to (1), FEs=FEs+1,counter(max)=0;
26.	end if //end scout bee phase
20.	end while

### Algorithm 1: The pseudo-code of the proposed EABC\_elite

# 4.1 Experiment 1: comparison of state-of-the-art ABCs on benchmark functions

In this section, 22 scalable benchmark functions with dimensions D=50 and D=100 are used to evaluate the performance of EABC-elite, as shown in Table 1. These functions include continuous, discontinuous, unimodal, and multimodal

	Function	Search range	Min		Function	Search range	Min
$f_1$	Sphere	$[-100, 100]^{D}$	0	$f_{12}$	NCRastrigin	$[-5.12, 5.12]^{D}$	0
$f_2$	Elliptic	$[-100, 100]^{D}$	0	$f_{13}$	Griewank	$[-600, 600]^{D}$	0
$f_3$	SumSquare	$[-10, 10]^{D}$	0	$f_{14}$	Schwefel2.26	$[-500, 500]^{D}$	0
$f_4$	SumPower	$[-1, 1]^D$	0	$f_{15}$	Ackley	$[-50, 50]^{D}$	0
$f_5$	Schwefel2.22	$[-10, 10]^{D}$	0	$f_{16}$	Penalized1	$[-100, 100]^{D}$	0
$f_6$	Schwefel2.21	$[-100, 100]^{D}$	0	$f_{17}$	Penalized2	$[-100, 100]^{D}$	0
$f_7$	Step	$[-100, 100]^{D}$	0	$f_{18}$	Alpine	$[-10, 10]^{D}$	0
$f_8$	Exponential	$[-10, 10]^{D}$	0	$f_{19}$	Levy	$[-10, 10]^{D}$	0
$f_9$	Quartic	$[-1.28, 1.28]^D$	0	$f_{20}$	Weierstrass	$[-1, 1]^{D}$	0
$f_{10}$	Rosenbrock	$[-5, 10]^{D}$	0	$f_{21}$	Himmelblau	$[-5, 5]^{D}$	-78.33236
$f_{11}$	Rastrigin	$[-5.12, 5.12]^{D}$	0	$f_{22}$	Michalewicz	$[0,\pi]^D$	- 500, - 100

**Table 1** Benchmark functions used in experiment 1 (D = 50)

functions. In the search range, the optimal global value of each function is shown in Table 1, and their definitions are found in the literature [15].

The mean value and standard deviation (SD) of the best objective function value are calculated by each algorithm to evaluate the quality or accuracy of the solutions obtained by different algorithms. The smaller the value of this metric is, the higher the quality/accuracy of the solution has. According to [15], the maximum function evaluation ( $max\_FEs$ ) is used as the termination condition and set to 5000  $\cdot$  *D*; *SN* set to 50 and *D* set to 50 for all algorithms, note that *D* represents the number of decision variables. Other parameters are set following the original literature, as shown in Table 2. For each function, all algorithms have a minimum of 30 independent execution runs. Experiment results when D=50 and D=100 are depicted in Tables 3 and 4, respectively.

In this text,  $f_1$ - $f_9$  are unimodal functions. From Table 3, when solving the unimodal functions  $f_1$ ,  $f_2$ ,  $f_3$ ,  $f_5$ , and  $f_6$ , the solution accuracy and robustness of the EABC\_elite are better than other algorithms except for ECABC, and all algorithms show similar performance on the unimodal functions  $f_7$  and  $f_8$ .  $f_7$  is a discontinuous step function which can be easily solved [14], since its optimal global solution is a region rather than a point. Therefore, all algorithms can find the optimal global solution on  $f_7$ . Since  $f_9$  is a quartic function with noise, its optimal global solution is complicated to be found. All algorithms can approximate the global optimal solution though cannot find out the real global optimum, despite EABC elite, ECABC, and DGABC exhibit better solution quality than other competitors. That is, EABC\_elite is the second-best algorithm on the unimodal functions  $f_1-f_9$ , whereas ECABC performs best among all algorithms. Additionally, the solution quality of EABC\_elite on unimodal function is approximately optimal to ECABC. The main reason why EABC\_elite and ECABC get the best results on most unimodal functions lies in the search Eqs. (19) and (13) because they utilize the information of gbest to guide the whole population; thus, the convergence speed of EABC\_elite and ECABC is enhanced.

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setting
Parameters
Table 2

	S				
Algorithm	Year	Parameters setting	Algorithm	Year	Parameters setting
ABCLGII	2018	$limit = SN \cdot D0, r = 1, q = 0.2$	ABC_elite	2016	$limit = SN \cdot D0, p = 0.10, r = 1/p$
ECABC	2018	$limit = SN \cdot D0, p = 0.1, Dim = 2$	DFSABC_elite	2016	$limit = SN \cdot D0, p = 0.10, r = 1/p$
DGABC	2016	$limit = SN \cdot D0, C = 1.50, F = 0.20, CR = 0.3$	EABC_elite	I	$limit = SN \cdot D0, p = 0.10, r = 1/p$

Alg	ABCLGII [24] Mean (SD)	ECABC [23] Mean (SD)	DGABC [31] Mean (SD)	ABC_elite [ <b>15</b> ] Mean (SD)	DFSABC_elite [15] Mean (SD)	EABC_elite Mean (SD)
$f_1$	2.13e-92 (5.24e-92)-	<b>1.19e-99</b> (5.34e-99)+	5.83e-69 (6.16e-69)-	2.39e-80 (8.28e-80)-	1.71e-83 (5.12e-83)-	8.53e-98 (1.18e-97)
f.	6.51e-90 (5.82e-90)-	<b>5.39e-97</b> (3.92e-97)+	4.38e-65 (1.22e-64)-	1.07e-76 (2.91e-76)-	8.55e-79 (3.56e-79)-	4.39e-95 (3.36e-95)
$f_3$	3.84e-93 (4.89e-93)-	<b>3.24e-101</b> (3.8e-101)+	1.22e-68 (3.85e-68)-	4.61e-80 (7.15e-82)-	2.58e-83 (3.45e-83)-	2.64e-99 (2.32e-98)
$f_4$	1.34e-145 (3.9e-122)+	<b>3.67e-239</b> (4.0e-239)+	8.21e-25 (3.55e-24)-	2.64e-108 (1.1e-108)-	4.66e-110 (8.3e-110)-	3.11e-130 (7.6e-129)
f5	1.25e-47 (9.22e-47)-	<b>2.57e-53</b> (4.82e-53)+	1.23e-41 (1.42e-41)-	1.28e-40 (1.07e-40)-	1.53e-42 (4.81e-42)-	5.74e-51 (3.84e-51)
$f_6$	1.31e+00 (1.82e+00)-	<b>1.21e-02</b> (3.03e-02)+	9.23e+00 (3.56e+00)-	7.20e-01 (9.22e-02)-	7.44e-01 (3.23e-01)-	3.30e-01 (5.09e-02)
$f_7$	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)			
$f_8$	2.67e-109 (8.1e-125)=	2.67e-109 (2.2e-125)=	<b>2.67e-109</b> (4.8e-125)=	<b>2.67e-109</b> (9.6e-125)=	2.67e-109 (8.3e-122)=	2.67e-109 (2.6e-109)
$f_9$	3.06e-02 (2.82e-02)-	1.01e-02 (3.99e-02)+	8.52e-03 (2.15e-03)+	2.52e-02 (4.96e-03)-	2.35e-02 (3.22e-03)-	1.89e-02 (4.70e-03)
$f_{10}$	<b>3.32e-02</b> (9.82e-02)+	7.82e+00 (4.92e+00)-	7.56e+01 (3.87e+01)-	1.83e+00 (1.02e+00)-	1.43e + 00(5.72e + 00) -	5.21e-01 (1.12e+00)
$f_{11}$	<b>0.00e + 00</b> (0.00e + 00)=	4.31e-01 (3.28e-01)-	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)
$f_{12}$	<b>0.00e + 00</b> (0.00e + 00)=	6.23e-02 (5.80e-02)-	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)
$f_{13}$	<b>0.00e + 00</b> (0.00e + 00)=	8.82e-03 (3.37e-03)-	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)
$f_{14}$	3.81e-11 (2.21e-11)-	2.42e-02 (3.40e-2)-	1.84e-11 (5.31e-11)+	5.79e-11 (6.56e-11)-	2.42e-11 (4.72e-11)=	2.32e-11 (2.01e-11)
$f_{15}$	6.48e-14 (3.82e-15)-	6.22e-14 (7.91e-14)-	1.53e-14 (4.88e-14)+	4.73e-14 (4.46e-15)=	<b>4.68e–14</b> (5.98e–14)=	<b>4.68e-14</b> (4.03e-15)
$f_{16}$	<b>9.42e-33</b> (5.88e-33)=	<b>9.42e-33</b> (3.92e-48)=	<b>9.42e-33</b> (8.78e-48)=	<b>9.42e-33</b> (2.78e-48)=	<b>9.42e-33</b> (2.22e-48)=	<b>9.42e-33</b> (1.44e-48)
$f_{17}$	<b>1.50e-33</b> (3.82e-32)=	<b>1.50e-33</b> (4.93e-32)=	4.22e-32 (4.67e-32)-	<b>1.50e-33</b> (0.00e+00)=	<b>1.50e-33</b> (0.00e + 00)=	<b>1.50e-33</b> (0.00e+00)
$f_{18}$	1.08e-15 (2.89e-16)+	3.17e-10 (6.37e-10)-	1.69e-15 (7.82e-15)-	5.55e-17 (1.61e-16)+	<b>2.17e–17</b> (4.43e–16)+	7.23e-17 (9.24e-16)
$f_{19}$	<b>1.35e–31</b> (2.82e–31)=	<b>1.35e–31</b> (4.89e–32)=	<b>1.35e–31</b> (1.64e–32)=	<b>1.35e–31</b> (6.68e–47)=	<b>1.35e–31</b> (5.80e–47)=	<b>1.35e–31</b> (4.34e–48)
$f_{20}$	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)			
$f_{21}$	-78.332 (2.83e-14)=	-78.332 (3.80e-14)=	-78.332 (1.84e-14)=	- 78.332 (1.65e-14)=	-78.332 (4.32e-14)=	- <b>78.332</b> (2.89e-15)
$f_{22}$	-49.61 (2.83e-02)+	-49.20 (4.82e-02)-	-49.37 (8.27e-02)-	-49.87 (3.33e-02)+	-49.92 (1.34e-02)+	- <b>49.53</b> (3.05e-02)
-/=/+	4/10/8	8/L/L	3/9/10	2/11/9	2/12/8	I

**Table 3** The comparison results of ABC variants on 22 test functions at D=50

Alg	ABCLGII Mean (SD)	ECABC Mean (SD)	DGABC Mean (SD)	ABC_elite Mean (SD)	DFSABC_elite Mean (SD)	EABC_elite Mean (SD)
$f_1$	7.85e-88 (2.99e-88)-	<b>3.59e-97</b> (3.73e-97)+	8.24e-52 (3.32e-52)-	1.03e-79 (4.23e-79)-	1.50e-81 (1.72e-81)-	2.56e-96 (6.44e-96)
$f_2$	1.23e-84 (4.97e-84)-	<b>3.30e-94</b> (7.11e-94)+	7.78e-50 (8.23e-50)-	9.74e-75 (8.22e-75)-	3.33e-77 (9.54e-77)-	3.01e-92 (7.08e-92)
$f_3$	7.89e-88 (3.36e-88)-	1.66e-92 (2.82e-92)+	8.22e-49 (2.82e-48)-	1.43e-79 (9.18e-79)-	5.04e-82 (4.89e-82)-	1.15e-88 (5.17e-88)
$f_4$	3.66e-140 (1.6e-140)+	1.70e-230 (6.8e-230)+	3.88e-24 (8.8e-24)-	7.83e-106 (4.9e-106)-	1.65e-106 (5.2e-106)-	3.66e-130 (1.6e-129)
$f_5$	1.33e-46 (9.05e-47)-	1.00e-53 (5.29e-53)+	8.23e-40 (7.89e-40)-	6.83e-39 (7.82e-39)-	5.10e-42 (3.56e-42)-	3.99e-50 (3.64e-50)
$f_6$	2.02e+00 (3.46e-01)+	7.23e-01 (2.37e-01)+	2.03e+01 (3.83e+01)-	4.54e+00 (4.20e-01)-	4.50e+00 (3.63e-01)-	2.81e+00 (2.21e-01)
$f_7$	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)				
$f_8$	<b>7.12e–218</b> (0.0e + 00)=	<b>7.12e–218</b> (0.0e + 00)=	<b>7.12e–218</b> (0.0e + 00)=	<b>7.12e–218</b> (0.0e+00)=	<b>7.12e–218</b> (0.0e + 00)=	<b>7.12e–218</b> (0.0e+00)
$f_9$	6.83e-02 (5.67e-03)-	4.07e-02 (3.92e-02)=	9.82e-02 (3.77e-02)-	5.55e-02 (4.81e-02)-	5.29e-02 (4.71e-03)-	<b>4.07e-02</b> (7.10e-03)
$f_{10}$	9.23e-01 (5.65e-01)-	3.73e+01 (1.24e+01)-	3.83e+02 (8.82e+02)-	4.56e + 00(3.13 + 01) -	8.65e+00 (2.22e+01)-	1.63e-01 (3.08e-01)
$f_{11}$	<b>0.00e + 00</b> (0.00e + 00)=	9.92e-01 (7.84e-01)-	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)
$f_{12}$	<b>0.00e + 00</b> (0.00e + 00)=	8.31e-01 (3.02e-01)-	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)
$f_{13}$	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	8.72e-14 (2.78e-14)-	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)
$f_{14}$	7.32e-02 (1.35e-02)-	1.87e-01 (2.40e-01)-	6.45e-10 (3.81e-10)-	9.47e-10 (9.99e10)-	1.12e-10 (6.84e-12)-	1.09e-10 (3.87e-12)
$f_{15}$	1.39e-13 (6.45e-14)-	4.35e-13 (1.83e-13)-	2.89e-07 (3.88e-07)-	1.10e-13 (8.23e-13)-	1.09e-13 (6.52e-15)-	9.27e-14 (8.41e-15)
$f_{16}$	<b>4.71e–33</b> (3.81e–33)=	<b>4.71e–33</b> (4.27e–33)=	1.37e-02 (1.92e-02)-	<b>4.71e–33</b> (5.28e–33)=	<b>4.71e–33</b> (7.21e–49)=	<b>4.71e–33</b> (1.40e–48)
$f_{17}$	<b>1.50e-33</b> (0.00e + 00)=	<b>1.50e-33</b> (0.00e + 00)=	<b>1.50e-33</b> (0.00e + 00)=	<b>1.50e-33</b> (0.00e+00)=	<b>1.50e-33</b> (0.00e + 00)=	<b>1.50e-33</b> (0.00e+00)
$f_{18}$	4.45e-14 (4.34e-15)-	4.07e-07 (6.93e-07)-	7.33e-12 (4.29e-12)-	3.44e-15 (5.72e-15)-	5.94e-16 (6.87e-15)+	1.16e-15 (3.22e-15)
$f_{19}$	<b>1.35e–31</b> (0.00e + 00)=	1.35e-31 (0.00e+00)=	4.72e-31 (4.18e-31)-	<b>1.35e–31</b> (0.00e+00)=	<b>1.35e–31</b> (0.00e + 00)=	<b>1.35e–31</b> (0.00e+00)
$f_{20}$	<b>0.00e + 00</b> (0.00e + 00)=	<b>0.00e + 00</b> (0.00e + 00)				
$f_{21}$	-78.332 (7.21e-14)=	<b>-78.332</b> (7.71e-02)=	-78.27 (5.28e-02)-	-78.332 (4.28e-14)=	-78.332 (5.71e-14)=	-78.332 (2.01e-14)
$f_{22}$	<b>-99.60</b> (5.23e-02)+	-98.22 (2.46e-01)-	-98.32 (1.07e-01)-	-99.54 (3.92e-02)+	-99.52 (1.42e-02)+	-99.41 (2.08e-02)
-/=/+	3/10/9	L/6/9	0/6/16	1/10/11	2/10/10	

Still, in this text,  $f_{10}$ - $f_{22}$  are multimodal functions. As  $f_{10}$  is Rosenbrock function and its global optimum is inside of a long and parabolic shaped valley, the variables are strongly dependent, as the gradients do not point toward the optimum. Generally speaking, if the population evolves under the guidance of the global best solution or some other good solutions, the search is easy to get into hopeless areas. Therefore, except for ABCLGII and EABC\_elite, all other algorithms perform poorly on  $f_{10}$ , since the search equation utilizes the information of gbest to guide search direction. In ABCLGII, only elite individuals have chances to be guided by the information of gbest at a probability  $P_{str}$  (0 <  $P_{str}$  < 1); hence, ABCLGII may obtain better results than BCABC, DGABC, ABC\_elite, and DFS-ABC\_elite on  $f_{10}$ . Although all individuals in EABC\_elite are guided by gbest in the employed bee and onlooker bee phases, the ordinary solution  $x_k$  is also used to diminish the great lead ability of gbest (see Fig. 1) and help the algorithm escape the local optima. Therefore, the EABC elite can achieve a better balance between exploration and exploitation and produce the second-best result on function  $f_{10}$ . Although ECABC performs very well on unimodal functions  $f_1 - f_0$ , it performs poorly on multimodal function  $f_{10}$  since ECABC only searches around the elite individuals according to Eq. (13), so the exploitation ability of ECABC is too strong and easy to result in precocity problem.

Similarly, regarding the accuracy and reliability of the multimodal functions  $f_{11}$ - $f_{22}$ , the EABC\_elite is superior to or at least comparable to the compared EAs while ECABC performs poorly on most of the multimodal functions, owing to its excessive exploitation ability.

Overall, EABC\_elite outperforms ABCLGII, ECABC, DGBAC, ABC\_elite, and DFSABC\_elite on 8, 8, 10, 9, and 8 out of 22 functions, respectively. EABC\_ elite is beaten by ABCLGII, ECABC, DGBAC, ABC\_elite, and DFSABC\_elite on 4, 7, 3, 2, and 2 functions, respectively. Although ECABC performs better on unimodal functions  $f_1$ - $f_9$ , EABC\_elite shows robust results on both unimodal and multimodal functions. Comparison results between EABC\_elite and other ABC variants on 22 test functions at D = 100 are shown in Table 4, and a similar conclusion is sought. As overall, due to the superior design of search equations, the EABC\_elite shows the best overall performance among all six ABC variants.

To further verify the performance of EABC\_elite, we compare EABC\_elite on aforementioned 22 benchmark functions at D=40 with five most widely used DE and PSO variants, i.e., SRPSO [33], SLPSO [28], JADE [34], sinDE [35], and ABCADE [36]. As the comparison, the parameters of all DE and PSO methods are set following the corresponding original papers, and parameter setting details of all DE and PSO methods are tabulated in Table 5. Experimental results of "mean" and "SD" are given in Table 6, from which we can observe that EABC\_elite outperforms SRPSO, SLPSO, JADE, sinDE, and ABCADE on 21, 14, 12, 13, and 7 out of 22 functions and is beaten solely by SRPSO, SLPSO, JADE, sinDE, and ABCADE on 1, 2, 2, 2, and 3 functions, respectively. Therefore, EABC\_elite performs better than all other algorithms both on unimodal functions and on multimodal functions due to its excellent exploration–exploitation balance.

Table 5     The para       Algorithm     SRPSO	meters of EAB Year 2015	C_elite and non-ABC variants Parameters setting $N = 400, w_{\text{initial}} = 1.050, w_{\text{inal}} = 0.5,$ $c_1 = c_2 = 1.49445, V_{\text{max}} = 0.06708 \times \text{Range}$	Algorithm sinDE	Year 2015	Parameters setting $NP = 40$ , freq = 0.25
SLPSO	2015	All parameters depend on the function dimension $D$ .	ABCADE	2017	SN = 50, $limit = 200$ , $m = 5$ , $n = 10$ , $c_1 = 0.9$ , $c_2 = 0.999$
JADE	2009	NP = 100, c = 0.1, p = 0.05	EABC_elite	I	SN = 50, $limit = 200$ , $p = 0.10$ , $r = 1/p$

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	SRPSO	SLPSO	JADE	SinDE	ABCADE	EABC_elite mean (SD)
	mean (SD)	mean (SD)	mean (SD)	mean (SD)	mean (SD)	
f <sub>1</sub>	3.91e-73 (1.22e-73)-	1.41e-71 (2.08e-71)-	1.11e-76 (3.98e-76)-	1.33e-54 (1.37e-54)-	4.30e-70 (1.59e-69)-	1.65e-98 (4.05e-98)
$f_2$	4.49e-77 (1.47e-77)-	2.68e-68 (2.35e-68)-	1.35e-65 (6.69e-65)-	1.66e-51 (1.61e-51)-	.54e-64 (1.84e-63)-	8.35e-96 (1.61e-95)
$f_3$	2.74e-75 (9.87e-75)-	1.04e-72 (1.07e-72)-	7.20e-74 (3.45e-73)-	2.30e-55 (2.12e-55)-	1.77e-71 (5.77e-71)-	1.15e-99 (5.01e-99)
$f_4$	3.30e-206 (0.00e+00)+	5.30e-163 (2.22e-162)+	1.80e-92 (7.39e-92)-	4.67e-86 (2.33e-85)-	8.86e-172 (0.00e+00)+	3.60e-122 (1.94e-121)
$f_5$	1.10e-22 (4.79e-22)-	2.35e-37 (2.93e-37)-	1.03e-30 (4.24e-30)-	1.87e-31 (1.02e-31)-	1.03e-42 (1.90e-42)-	3.96e-51 (5.22e-51)
$f_6$	1.27e+00 (2.04e+00)-	8.32e-16 (1.23e-15)+	3.62e-14 (4.90e-14)+	2.38e-02 (9.26e-02)+	1.02e-03 (1.95e-03)+	2.28e-01 (1.72e-01)
$f_7$	1.01e+01 (1.31e+01)-	0.00e + 00 (0.00e + 00) =	0.00e + 00 (0.00e + 00)=	0.00e + 00 (0.00e + 00)=	0.00e + 00 (0.00e + 00)=	0.00e + 00 (0.00e + 00)
$f_8$	6.00e-71 (2.68e-71)-	1.38e-87 (9.77e-103)=	1.38e-87 (4.56e-103)=	1.38e-87 (1.16e-93)=	1.38e-87 (4.56e-103)=	1.38e-87 (4.56e-103)
$f_9$	5.74e-02 (4.26e-02)-	2.57e-02 (2.6e-03)-	1.30e-03 (3.82e-04)+	6.66e-03 (1.81e-03)+	1.33e-02 (2.57e-03)-	1.17e-02 (5.29e-03)
$f_{10}$	3.52e+01 (4.19e+01)-	2.61e+01 (2.63e+01)-	6.38e-01 (1.49e+00)-	3.27e+01 (5.98e-01)-	1.97e+01 (3.16e+01)-	4.56e-01 (1.45e-01)
$f_{11}$	4.63e + 01 (1.03e + 01) -	1.96e + 01 (4.19e + 00) -	3.33e-11 (2.94e-11)-	1.60e + 02 (8.49e + 00) -	0.00e+00 (0.00e+00)=	0.00e + 00 (0.00e + 00)
$f_{12}$	6.15e+01 (1.46e+01)-	3.31e + 01 (5.30e + 00) -	2.86e-08 (1.69e-08)-	1.23e + 02 (1.06e + 01) -	0.00e + 00 (0.00e + 00)=	0.00e + 00 (0.00e + 00)
$f_{13}$	1.74e-16 (2.64e-16)-	0.00e + 00 (0.00e + 00) =	0.00e + 00 (0.00e + 00) =	0.00e + 00 (0.00e + 00)=	0.00e+00 (0.00e+00)=	0.00e + 00 (0.00e + 00)
$f_{14}$	1.69e+03 (5.67e+02)-	2.00e+03 (3.74e+02)-	4.74e + 00(2.39e + 01) -	1.46e + 03 (1.60e + 03) -	7.27e-12 (0.00e+00)-	6.06e-13 (1.37e-12)
$f_{15}$	3.47e-08 (5.11e-08)-	7.99e-14 (1.37e-15)-	5.40e-15 (1.81e-15)=	6.54e-15 (1.33e-15)=	5.25e-15 (1.81e-15)=	2.22e-15 (1.15e-15)
$f_{16}$	5.19e-30 (6.22e-30)-	1.18e-32 (2.79e-48)=	1.18e-32 (2.79e-48)=	1.18e-32 (2.79e-48)=	1.18e-32 (2.79e-48)=	1.18e-32 (2.79e-48)
$f_{17}$	8.22e-30 (7.38e-30)-	1.50e-33 (0.00e+00)=	1.50e - 33 (0.00e + 00) =	1.55e-33 (2.47e-34)=	1.55e-33 (2.47e-34)=	1.50e-33 (0.00e+00)
$f_{18}$	1.85e-13 (8.30e-13)-	8.32e-17 (1.97e-16)=	1.19e-04 (6.37e-05)-	1.87e-02 (3.68e-03)-	4.04e-40 (1.40e-39)+	5.75e-17 (3.15e-06)
$f_{19}$	6.17e-30 (4.22e-30)-	9.10e-31 (2.84e-31)-	1.35e-31 (2.23e-47)=	1.35e-31 (2.23e-47)=	1.35e-31 (2.23e-47)=	1.35e-31 (2.23e-47)
$f_{20}$	1.02e+00 (2.41e+00)-	3.30е-02 (3.33е-02)-	2.25e-01 (2.26e-02)-	9.19e-05 (4.59e-04)-	0.00e + 00 (0.00e + 00)=	$0.00e + 00 \ (0.00e + 00)$
$f_{21}$	-74.728 (2.19e+00)-	-74.56 (1.23e+00)-	-78.332 (0.00e+00)=	- 78.304 (1.41e-01)-	-78.332 (6.48e-15)=	-78.332 (2.38e-14)
$f_{22}$	-22.38 (5.52e-01)-	-20.75 (4.20e-01)-	-39.882 (2.14e-02)-	-29.613 (8.76e-01)-	-40.00 (0.00e+00)=	-40.00 (0.00e+00)
-/=/+	1/0/21	2/6/14	2/8/12	2/7/13	3/12/7	

**Table 6** Comparison of EABC\_elite with non-ABC variants on 22 test functions at D=40

### 4.2 Experiment 2: comparison of state-of-the-art ABCs on CEC 2015 functions

In this subsection, the performance of the proposed algorithm EABC\_elite is tested by solving a set of problems taken from the CEC2015 competition on learning-based real-parameter single objective optimization [25]. The CEC2015 benchmark contains 15 shifted or rotated problems, which are very difficult to solve when compared to basic functions. In this subsection, functions  $F_1-F_2$  are unimodal,  $F_3-F_5$  multimodal,  $F_6-F_8$  hybrid and  $F_9-F_{15}$  are composite functions, and the search space of each problem is  $[-100, 100]^D$ . We evaluated the procedures of the CEC2015 benchmark competition, and results are obtained based on 51 independent runs with 10000.D function evaluations ( $max\_FEs$ ) as the termination criterion for each test function, the error value of the found solution is defined as ( $f(x) - f(x^*)$ ), where  $x^*$  is the optimum value of the function. As a threshold, error values lower than  $10^{-8}$  (zero-threshold) are approximated to zero.

The population size is set to 100, so the parameter  $SN = 0.5 \times \text{population}$  size = 50. For all the algorithms, *D* is set to 30, and other parameters are shown in Table 2.

The mean error and standard deviation (SD) of the best objective function value are calculated by each algorithm to evaluate the quality or accuracy of the solutions obtained by different algorithms. The smaller the value of this metric is, the higher the quality/accuracy of the solution has. From Table 7, EABC\_elite is the second-best algorithms on unimodal function  $F_1$ , and ECABC ranks first among all the algorithms. On function  $F_2$ , EABC\_elite has significant advantages over all other algorithms. The reason is that Eq. (19) is guided by the gbest, and thus, the exploitation ability of ABC is enhanced, which is beneficial to unimodal functions.

 $F_3$ - $F_{15}$  are complicated multimodal functions with numerous local minima. As known, an algorithm should own strong global search ability to produce good results; otherwise, the algorithm may fall fastly into a local minimum. From Table 7, the EABC\_elite performs significantly better than all compared algorithms regarding solution accuracy and robustness on almost all the test functions. On all 15 functions, EABC\_elite is beaten by ABCLGII, ECABC, DGABC, ABC\_elite, and DFSABC\_elite only on 2, 2, 2, 1, and 2 functions, respectively. The reason is that EABC elite has no bias to any search directions and the global search ability of EABC\_elite is relatively strong. Although ECABC performs well on 22 test functions above discussed, it performs poorly on CEC 2015 functions due to ECABC always searches around elite individuals so that the exploitation ability of ECABC is too strong and easy to result in precocity problem. Observing experiments 1 and 2, since the EABC elite uses stronger heuristic information and better balance strategy simultaneously, the overall performance of EABC\_elite is better than all other algorithms regarding solution quality and robustness. For the convenience and clearness of illustration, the convergence curves of six representative functions are plotted in Fig. 2, where EABC\_elite exhibits faster convergence speed than most of the competitors.

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Alg	ABCLGII Mean error (SD)	ECABC Mean error (SD)	DGABC Mean error (SD)	ABC_elite Mean error (SD)	DFSABC_elite Mean Error (SD)	EABC_elite MeanError (SD)
$F_1$	2.32e+06 (1.01e+06)-	<b>2.01e + 06</b> (9.07e + 05)+	3.10e + 06(1.53e + 06) -	2.97e+06 (1.51e+06)-	3.20e+06 (1.08e+06)-	2.27e+06 (9.86e+05)
$F_2$	2.61e+03 (3.32e+03)-	2.44e+03 (3.20e+03)-	2.51e+03 (2.34e+03)-	2.67e+03 (3.59e+03)-	1.64e + 03(2.03e + 03) -	<b>1.20e + 03</b> (2.26e + 03)
$F_3$	2.01e+01 (2.74e-01)-	2.03e+01 (3.52e-02)-	2.01e+01 (3.91e-02)-	2.01e+01 (3.96e-02)-	2.01e+01 (4.61e-02)-	<b>2.00e + 01</b> (3.83e-02)
$F_4$	4.96e+01 (8.52e+00)-	3.88e+01 (5.47e+00)-	4.09e + 01 (6.79e + 00)-	4.24e+01 (7.09e+00)-	4.21e+01 (6.8e+00)-	<b>3.73e + 01</b> (6.40e + 00)
$F_5$	1.81e+03 (3.38e+02)-	1.83e + 033.67e + 02) -	1.83e+03 (2.06e+02)-	1.69e+03 (2.58e+02)-	1.68e+03 (2.47e+02)-	<b>1.67e + 03</b> (2.40e + 02)
$F_6$	1.03e + 06(5.54e + 05) -	8.03e+05 (4.36e+05)-	8.01e+05 (5.80e+05)-	1.07e+06 (5.78e+05)-	1.03e + 06(5.58e + 05) -	<b>6.34e + 05</b> (4.65e + 05)
$F_7$	8.46e + 00 (1.30e + 00) -	8.68e+00 (1.65e+00)-	1.01e+01 (7.93e-01)-	8.32e+00 (1.41e+00)-	8.52e+00 (1.31e+00)-	<b>7.96e + 00</b> (1.30e + 00)
$F_8$	1.73e+05 (1.11e+05)+	<b>1.55e + 05</b> (1.01e + 05)+	1.73e+05 (8.95e+04)+	2.74e+05 (1.69e+05)-	2.36e + 05 (1.36e + 05) +	2.50e+05 (1.33e+05)
$F_9$	<b>1.03e + 02</b> (2.77e-01)=	<b>1.03e + 02</b> (2.02e-01)=	<b>1.03e + 02</b> (1.72e-01)=	1.04e+02 (2.24e-01)-	1.04e + 02 (2.63e - 01) -	1.03e+02 (2.41e-01)
$F_{10}$	4.77e+05 (2.63e+05)-	4.20e + 05(2.43e + 05) -	4.17e+05 (2.34e+05)-	6.31e+05 (4.50e+05)-	6.99e + 05 (5.80e + 05) -	<b>4.09e + 05</b> (5.26e + 05)
$F_{11}$	3.49e + 02(9.39e + 01) -	3.93e+02 (1.21e+02)-	4.50e + 02 (1.49e + 02)-	3.43e+02 (8.09e+01)-	3.65e+02 (1.30e+02)-	<b>3.28e + 02</b> (9.80e + 01)
$F_{12}$	<b>1.04e + 02</b> (4.08e-01)=	<b>1.04e + 02</b> (3.22e-01)=	1.05e+2 (4.76e-01)-	1.05e+02 (3.37e-01)-	1.05e+02 (6.69e-01)-	1.04e+02 (3.20e-1)
$F_{13}$	2.62e-02 (3.61e-04)+	2.65e-02 (4.31e-04)=	<b>2.61e-02</b> (7.67e-04)+	2.63e-02 (3.38e-04)+	2.63e-02 (3.87e-04)+	2.65e-02 (5.12e-04)
$F_{14}$	3.22e+04 (9.34e+02)-	3.28e+04 (8.50e+02)-	3.28e + 04 (8.23e + 02)-	3.21e+04 (8.92e+02)-	3.21e+04 (9.64e+02)-	<b>3.19e + 04</b> (7.51e + 02)
$F_{15}$	<b>1.00e + 02</b> (3.11e-12)=	<b>1.00e + 02</b> (4.22e-14)=	<b>1.00e + 02</b> (7.22e-14)=	<b>1.00e + 02</b> (6.83e-14)=	1.00e+02 (4.25e-13)=	1.00e+02 (3.23e-14)
-/=/+	2/3/10	2/4/9	2/2/11	1/1/13	2/1/12	I

**Table 7** The mean error and standard deviation of six ABCs on CEC 2015 test function suite at D=30

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Fig. 2 Convergence curves of different ABCs on six CEC 2015 functions

## 4.3 Experiment 3: feature selection problem

Feature selection (FS) technology is an important step when extracting a subset of useful features subset and discarding irrelevant features of a given dataset [37]. It is a preprocessing step to solve the concerns of classification problems in recent years [38]. All features of a given data set may include noise, redundant, or misleading information, so exhaustive search strategy applied to all features should be a time-consuming process, that is unrealistic in the real world. Based on this consideration, we apply ABC variant that aims at the optimization algorithm to search the optimal subset *d* of related features from the original feature set *D* (d < D), to shorten the calculation time and obtain higher classification accuracy.

# 4.3.1 Individual encoding

Binary vectors are contemporary techniques in the feature selection problem [39], where 1 represents that the corresponding feature is selected, and 0 represents that the corresponding feature is not selected. According to the literature [39], each element of an individual is limited to [0, 1] that represents the probability of the related feature to be selected. Taking the dataset with *D* features as an example, an individual can be encoded as

$$X_i = (x_{i,1}, x_{i,2}, \dots x_{i,D})$$
(21)

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The corresponding feature subset  $S_i$  can be generated by

$$s_{i,j} = \begin{cases} 1 \ rand < x_{i,j} \\ 0, \ otherwise \end{cases}$$
(22)

where j=1, 2,..., D; rand denotes a randomly generated random number in the range of [0, 1].

# 4.3.2 Fitness evaluation

The K-nearest neighbor (KNN) is a simple yet efficient classifier used to evaluate the performance of each individual. In this section, the parameter k of KNN is set to 1.

The tenfold cross-validation method is used to train and test the KNN classifier, where the dataset is divided into ten un-duplicated subsets, and any nine of the ten subsets are used for training and the remaining one for testing.

Herein, the classifier will be trained and tested ten times. Note that, the satellite dataset cannot be tested under the tenfold cross-validation method since the dataset has been divided into testing and training dataset.

In EABC\_elite for feature selection, the classification accuracy obtained by the *i*-th individual (food source)  $X_i$  is calculated as the proportion of correctly determined instances to all instances, shown as

$$Accuracy_i = \frac{\text{Number of correctly determined samples}}{\text{Total number of all the samples}}$$
(23)

$$f(X_i) = 1 - \operatorname{Accuracy}_i \tag{24}$$

For each  $X_i$ , a subset of *d* relevant features from the original feature set D (d < D) is generated according to (21) and (22), then the KNN classification is used to classify the dataset with selected *d* features. Next, the classification accuracy is computed by Eq. (23), in which the higher the accuracy, the better is the selected subset performance. At last, since the EABC\_elite algorithm is proposed to solve the minimization problem, though Eq. (23) is a maximization problem, and thus, Eq. (24) is used to transfer the maximization problem into minimization problem, and the value  $f(X_i)$  is the objective function of the i-th food source  $X_i$ .

### 4.3.3 Experiments of feature selection problem

In this section, the EABC\_elite-based feature selection method is evaluated and compared with DE [2], ABC [5], CBPSO1 [37], and NSABC [39] algorithms, and experimental results are taken from [39].

Three groups of datasets in this feature selection problem are applied, cited from the UCI repository. In this paper, we apply three well-known datasets in the UCI repository<sup>1</sup> to study the problem of feature selection. For the features between 10

<sup>&</sup>lt;sup>1</sup> http://archive.ics.uci.edu/ml.

<b>Table 8</b> The datasets used infeature selection problem	Dataset	No. of Samples	No. of classes	No. of features
•	Glass	214	7	10
	Wine	178	3	13
	Letter	20,000	26	16
	Segmentation	2310	7	19
	Ionosphere	351	2	34
	Satellite	6435	6	36
	Sonar	208	2	60

and 19, it is considered as a small group. This group contains glass, wine, letter, and segmentation. If the number of features is between 20 and 49, it is considered a medium size group. Say, the ionosphere and the satellite are in this group. Finally, if the number of features is higher than 50, it is looked on as a large group, e.g., sonar is in the large group. Table 8 gives a detailed description of these datasets.

The normalization is a favorite preprocessing step, as all features are normalized by projecting their feature value to the interval [0, 1] to diminish the significant impact of great numbers [40]. As a comparison, the population size of the EABC\_ elite algorithm is set to 20, which is the same as the literature [39], and the parameter p in EABC\_elite is set to 0.3. Given that the maximum iteration number in most feature selection studies [37-39] is set to 100, this paper also utilizes the same maximum iteration number. Note that the maximum number of functions is related to the population size and the maximum iterations (MAX\_ITER), and expressed as: population size  $\times$  MAX\_ITER = 2 $\times$ SN  $\times$  MAX\_ITER. As shown in Table 9, we can observe that EABC\_elite is the best feature selection method in all compared algorithms, and the classification accuracies of EABC\_elite on the wine, letter, segmentation, satellite and sonar datasets are 99.85%, 85.67%, 98.23%, 91.59%, and 92.06%, respectively, which is better than other methods. On the glass dataset, the EABC\_elite performs as well as other algorithms. The proposed EABC\_elite ranks fourth on the ionosphere dataset and the ECABC ranks the first. As seen from the experimental results, the proposed EABC\_elite is an efficient tool for feature selection.

# 5 Data clustering

In this section, the proposed EABC\_elite is modified by embedding the *K*-means initialization strategy and chaotic parameters strategy to solve the clustering problem, to further verify its superiority.

# 5.1 Description of the clustering problem

Clustering is an essential tool for many applications such as data mining, statistical data analysis, data compression, and vector quantization [41, 42]. The purpose of clustering

lable 9 The result:	s of feature selection (	d: the selected feature i	numbers; Acc: the clas	ssification accuracy)			
Dataset	DE d (Acc)	ABC d (Acc)	CBPSO1 d (Acc)	BBPSO d (Acc)	NSABC d (Acc)	ECABC d (Acc)	EABC_elite d (Acc)
Glass	4.6 (100%)	6 (100%)	4.2 (100%)	4 (100%)	4 ( <b>100</b> %)	4 (100%)	4.3 (100%)
Wine	8 (99.10%)	8 (99.10%)	8 (99.33%)	8(98.88%)	7.8 (99.78%)	7.6 (99.80%)	7.2 (99.85%)
Letter	11 (80.50%)	9.8 (79.84%)	9.6 (79.33%)	9.6 (79.80%)	10 (80.67%)	10.7 (81.16%)	10.4 (85.67%)
Segmentation	10.8 (98.11%)	13.8(98.00%)	12.6~(98.04%)	10.8 (98.05%)	11.4 (98.11%)	10.3(98.09%)	9.3 (98.23%)
Ionosphere	14 (94.81%)	16.6 (94.53%)	15 (94.64%)	11.6 (94.70%)	15 (94.87%)	12.7 (94.90%)	14.2 (94.71%)
Satellite	24 (90.51%)	22.2 (90.51%)	20.6 (90.26%)	18.2 (90.42%)	20.8 (90.54%)	19.6 (90.46%)	20.2 (91.59%)
Sonar	28.8 (91.83%)	28.8 (91.83%)	30.4~(91.63%)	25.6 (91.54%)	32 (91.92%)	32 (91.96%)	31.6 ( <b>92.06</b> %)

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is to gather data into clusters (or groups), so that the similarity of data in each cluster is highly similar while being very dissimilar to data from other clusters [43].

There are two main classes of clustering techniques: hierarchical clustering and partitioning clustering. The time complexity of the hierarchical clustering is quadratic, whereas it is almost linear in the partitioning approaches, the reason why the partitioning approaches are widely used rather than hierarchical ones [44]. In a partitional clustering problem [45], we need to divide a set of *n* objects into *k* clusters [46]. Let  $O(o_1, o_2, ..., o_n)$  be the set of *n* objects. Each object has *q* characters, and each character is quantified with a real value. Let  $X_{n \times q}$  be the character data matrix. It has *n* rows and *q* columns. Each row represents data and  $x_{i,j}$  represents the j-th feature of the i-th data (*i*=1, 2,..., *n*, *j*=1, 2,..., *q*).

Let  $C = (C_1, C_2, \dots, C_k)$  be the k clusters. Then:

$$C_i \neq \emptyset, \ C_i \cap C_i \neq \emptyset, \ C_1 + C_2 + \dots + C_k = 0, \quad i, j = 1, 2, \dots, k, i \neq j$$

The goal of the clustering algorithm is to find such a C, so that objects in the same cluster can be as similar as possible, while objects in different clusters are different. These can be measured by some standards, such as total cluster variance or total mean square error (MSE) [47]:

$$Perf(O,C) = \sum_{i=1}^{n} Min\{||o_i - c_j||^2, j = 1, 2, \dots, k\}$$
(25)

where  $||o_i - c_j||^2$  represents the similarity between the i-th object and the center of *j*-th cluster. The most popularly used similarity metric in clustering is Euclidean distance, which is derived from the Minkowski metric:

$$d(o_i, c_j) = \left(\sum_{m=1}^{p} (x_{im} - c_{jm})^r\right)^{1/r}$$
(26)

where  $c_j$  is the center of *j*-th cluster  $C_j$  and *m* is the dimension within *q*. In this study, we will use the Euclidean metric as a distance metric, i.e., r=2 in Eq. (26). *K*-means clustering is one of the most popular partitional clustering algorithms due to its simplicity and linear time complexity. The main steps of the *K*-means algorithm are given below.

Initialize the k number of cluster centers  $(C_1, C_2, ..., C_k)$  from the data points  $\{X_1, X_2, ..., X_N\}$  in random,

Assign the data points  $X_i$ , where i = 1, 2, 3, ..., N to cluster center j = 1, 2, 3, ..., k, such that  $X_i - C_j \le X_i - C_l$ , l = 1, 2, 3, ..., k and  $l \ne j$ , where  $X_i - C_j$  is the Euclidean distance between data points  $X_i$  and cluster center  $C_j$ .

Compute the new cluster centers  $C'_1, C'_2, \ldots, C'_k$  as follows:

$$C'_{j} = \frac{1}{M_{j}} \sum_{X_{i} \in C_{j}} X_{i}, \quad j = 1, 2, 3, \dots k$$
(27)

where  $M_i$  indicates the number of data points related to cluster  $C_i$ .

Replace each  $C_j$  with  $C'_j$ , j = 1, 2, ..., k, until  $C_j \neq C'_j$ .

As a result for the multi-step K-means algorithm, k number of cluster centers positions are obtained and represented as the possible locations of the food source in D-dimensional search space for the employed bee phase of the ABC algorithm.

### 5.2 Traditional ABC-based clustering

From the view of optimization, clustering *N* objects to *k* clusters is a typical NP-hard problem [45], given that the swarm intelligent evolution algorithms have advantages in solving the NP-hard problem, a large number of EAs have been applied to the clustering problem [40, 45, 47]. It is easy to apply ABC variants for data clustering, as two changes are needed to be done for this approach according to the literature [46], as detailed in 5.2.1 and 5.2.2.

# 5.2.1 Solution presentation

In the numerical optimization of ABC, each food source represents a solution to the problem. When clustering in ABC, each food source represents a set of clusters, shown as

$$X_i = \{x_1, x_2, \dots, x_q, x_{q+1}, \dots, x_{k \times q}\}$$
(28)

$$c_m = \left\{ x_{(m-1) \times q+1}, x_{(m-1) \times q+2}, \dots x_{m \times q} \right\}$$
(29)

where  $X_i$  represents a food source in the ABC algorithm, k is the number of clusters, and q the number of features for the data clustering problem, for k centers clustering problem with q characters, the real dimension of ABC is  $k \times q$ .

There is no relationship between the population size of the ABC algorithm and the clustering problem. First, the upper and lower bounds on each feature are obtained by scanning the clustering data. At the initialization phase and scout bee phase, when the new food source is generated, the value on the *j*-th dimension should be restricted to the boundary of the *l*-th feature, where *l* is calculated as

$$l = mod((j-1), q) + 1$$
(30)

# 5.2.2 Fitness calculation

Unlike solving numerical optimization problems, the total within-cluster variance in Eq. (25) is employed to evaluate the quality of cluster partition when solving data clustering problems. The pseudocode of fitness calculation of ABC algorithm for solving cluster problems is shown in Algorithm 2, where each food source will be decoded to *k* clusters centers and the distances between objects and each center are calculated. Next, each of the objects will be assigned to the nearest cluster, and the total within-cluster variance will be calculated and taken as the food source's fitness [46].

# 5.3 Representative ABC-based clustering

Karaboga et al. [43] have applied the ABC algorithm for clustering analysis. Performance evaluation of the ABC algorithm shows that the ABC algorithm can efficiently be applied for data clustering. Yan et al. [46] have proposed a hybrid ABC (HABC) algorithm for data clustering by introducing the crossover operator of GA between the onlooker bee phase and scout bee phase of ABC:

Algorithm 2. Pseudo-code of fitness calculation of the ABC algorithm for clustering

Input: food sources X, data D
Output: fitness F
For each food source $X_i$
Decode $X_i$ to the k cluster centers following (29)
Calculate the distance between all objects in $D$ and each cluster center following (26)
Assign objects to the nearest clusters centers
Compute the total within-cluster variance $V_i$ following (25)
$F_i = V_i$
End for
Return F

 $child = rand(0, 1) \times parent_1 + rand(0, 1) \times parent_2$ (31)

where *a child* represents the newly produced offspring, while *parent1* and *parent2* are the two selected parents according to the binary tournament. Experiments indicate that the proposed HABC algorithm outperforms the original ABC and several other population-based clustering algorithms. Dang [48] et al. proposed an enhanced ABC and *K*-means (EABCK) to solve the clustering problem, where Eq. (5) of GABC instead of (3) ABC is used in employed bee phase and onlooker bee phase to improve the exploitation ability of ABC. Meanwhile, they proposed an improved information exchange mechanism as shown in

$$v_{i,j} = rand(0,1) \cdot (x_{i,j} - x_{k1,j}) + rand(0,1) \cdot (x_{best,j} - x_{k2,j})$$
(32)

where k1 and k2 are two randomly selected individuals, and  $x_{best,j}$  is the *j*-th dimension of the global best individual. We can see that the exploitation ability of EABCK is highly strong since the global best is used both in the employed bee phase and in the onlooker bee phase.

Algorithm 3. Pseudo-code c	f Two-step ABC c	lustering
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<sup>1.</sup> Apply K-means algorithm to initialize SN food sources;

2. Employed bee phase: perform the same process as ABC, i.e., the search Equation (3) is used;

Kumar et al. proposed an improved ABC (two-step ABC) to solve the clustering problem [49], and they also used Eq. (5) of GABC instead of Eq. (3) of ABC in the onlooker bee phase of two-step ABC to enhance the exploitation ability of ABC.

<sup>3.</sup> Like ABC, calculate the probability values according to (2);

<sup>4.</sup> Onlooker bee phase: perform the same process as ABC except that the (5) instead of (3) is used;

<sup>5.</sup> Scout bee phase: unlike ABC, the (33) is used to initialization the food source with maximum trial value.

Nevertheless, to better balance the exploitation and exploration ability of two-step ABC, they still use Eq. (3) of ABC in the employed bee phase of two-step ABC. Another improvement in the two-step ABC is that the random initialization of the scout bee of ABC, i.e., (1) is modified as follows:

$$x_{new} = x_{best} + rand[0, 1] \cdot (x_{best} - x_{curr})$$
(33)

where  $x_{best}$  is the global best solution;  $x_{curr}$  is the position of the abandoned food; and *rand*[0, 1] is a randomly generated number within [0, 1].

The procedure of two-step ABC clustering is shown in Algorithm 3. The EABCK and two-step ABC employ Eq. (5) of GABC instead of Eq. (3) to improve the exploitation ability of ABC. However, as mentioned above, it is pointed out that Eq. (5) of GABC used in EABCK and two-step ABC may cause oscillations [14, 15], so it may also reduce convergence, since the guidance of the last two terms may be in opposite directions. Therefore, the balance of EABCK and two-step ABC has not been well maintained and the performance of EABCK and two-step ABC can be improved.

Based on the above experiments, the proposed EABC\_elite has shown to be very competitive with the optimization ability in complex test functions given its excellent balance ability between exploitation and exploration. It is anticipated that the EABC\_elite achieves a better performance in the task of data clustering.

## 5.4 Proposed clustering algorithm

In the field of engineering, chaos theory is very useful in practical application. Chaos is a common nonlinear phenomenon, which is very complex and similar to randomness [50, 44]. Besides, it is susceptible to the initial value and can provide ergodicity, that is, the chaotic value has the opportunity to traverse all the domains within the specified range without repetition.

Recently, chaotic maps have been integrated with several meta-heuristic algorithms, such as the genetic algorithm [51] and cuckoo optimization [44]. In the field of ABC, Alatas [52] proposed a new ABC variant by combining the chaotic mapping into ABC (ChABC for short), but the chaotic maps are only used in the initialization phase and the scout bee phase, and most search behaviors of the bees have not been affected.

The clustering problem is a highly nonlinear complex problem with numerous local minima. In order to further enhance the global search ability of EABC\_elite when solving the clustering problem, this paper incorporates chaotic mapping with ergodic, irregular, and stochastic properties in EABC\_elite to further improve the global convergence. It is observed that the use of chaotic sequences in EABC\_elite can further facilitate the escape from local minima, so sequences generated by the logistic map [53] replace the random parameter  $\phi$  used in Eqs. (19) and (20) of EABC\_elite. The parameter  $\phi$  is replaced by the logistic sequence  $\hat{c}$  shown in (35):

$$c_{t+1} = a \times c_t \times (1 - c_t), \ a = 4$$
(34)

$$\hat{c}_{t+1} = 2 \times (c_{t+1} - 0.5) \tag{35}$$

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Datasets	K	D	Number of data objects	Description
Iris	3	4	150 (50, 50, 50)	Fisher's iris data
Wine	3	13	178 (59, 71, 48)	Wine quality data
Glass	6	9	214 (70, 76, 17, 13, 9, 29)	Glass identification data
WBC	2	9	683 (444, 239)	Wisconsin breast cancer
CMC	3	9	1473 (629, 334, 510)	Contraceptive method choice

Table 10 The summary of test datasets used in clustering experiments

From Eq. (34), the chaotic value  $(c_{t+1})$  at time t+1 depends only on the chaotic value at time  $t(c_t)$ . Note that  $c \in (0, 1)$  and a=4 were adopted in these experiments, as suggested in most research works. In Eq. (34),  $c_0$  is generated randomly for each independent run, with  $c_0 \neq \{0, 0.25, 0.5, 0.75\}$ .

By using the new chaotic sequences shown in (35), Eqs. (19) and (20) can all be modified as follows:

$$v_{i,j} = \mu + \hat{c} \cdot \delta \tag{36}$$

where the meaning of  $\hat{c}$  is the same as (35),  $0 < \hat{c} < 1$ , and  $\mu$  and  $\delta$  are the same as (19) and (20), respectively. Unlike [52], the chaotic sequence is used in the entire search process, so the global ability of EABC\_elite is enhanced when solving the clustering problem. Hybridization of the algorithm is one of the active research areas used to enhance the performance of algorithms. In wto-step ABC, a multi-step *K*-means algorithm is embedded into the ABC algorithm to enhance the performance of the ABC algorithm to enhance the performance of the *ABC* algorithm in clustering. EABCK also employs *K*-means to enhance its performance. Thus, for fair comparison purposes, the proposed clustering also employs the *K*-means algorithm to initialize the food source.

By combining the chaotic parameter generated and *K*-means initialization strategy with EABC\_elite, a novel two-step clustering algorithm, namely TEABC\_elite, is proposed, as depicted in Algorithm 4.

Al	gorithm 4: The pseudo-code of the TEABC_elite for data clustering Input: the original data used for clustering
01:	For <i>i</i> =1 to SN // <i>i</i> represent the <i>i</i> th employed bee and SN represents the total number of food sources
02:	Initialize k cluster centers $\{C_1, C_2,, C_k\}$ randomly from the data points within the boundary of a given dataset
03:	Apply the K-means to iterate the k clusters until the k centers no longer changed or termination criteria satisfied
04: 05:	The <i>i</i> th food source is coded as $x = \{C_1, C_2,, C_k\}$ ;//Initialization Phase
06.	End
07:	Fes=0
08:	while Fes <max_fes< td=""></max_fes<>
09:	Select the top T=p.SN solutions as elite solutions from population
10:	for <i>i</i> =1 to <i>SN</i> //employed bee phase
11:	Generate a new candidate solution $v_i$ using equation (36), evaluate the candidate solution $v_i$
12:	Adjust boundary according to equation (30);
13:	$ \text{if } f(v_i) < f(x_i), $
14:	Replace x <sub>i</sub> by v <sub>i</sub> and counter(i)=0
15:	else
16:	counter(i)= counter(i)+1
17:	end if
18:	end for //end employed bee phase
19:	for i=1 to SN //onlooker bee phase
20:	Select a solution $x_e$ from elite solutions randomly to search
21:	Generate a new candidate solution $v_e$ using equation (36), evaluate the new candidate solution $v_e$
22:	Adjust boundary according to equation (30);
23:	$if f(v_e) < f(x_e)$
24:	Replace $x_e$ by $v_e$ and $counter(e)=0$
25:	else
26:	<pre>counter(e)= counter(e)+1</pre>
27:	end if
28:	end for //end onlooker bee phase
29:	Fes=Fes+SN×2
30;	Select the solution x <sub>max</sub> with max <i>counter</i> value // <b>Scout bee phase</b>
31:	if counter(max)>limit //only one food source with max counter value can be initialized
32:	Replace x <sub>max</sub> by a new solution generated according to (1), <i>Fes=Fes+1,counter</i> (max)=0;
33:	Adjust boundary of $x_{max}$ according to equation (30);
34:	end if //end scout bee phase
35:	end while
	decode the $x_{best}$ to k clusters center { $C_1, C_2,, C_k$ } according to (29), get partitioned data according to Algorithm 2.
Outp	but: k clusters center $\{C_1, C_2, \dots, C_k\}$ ; the partitioned data

# 5.5 Experiments of TEABC\_elite for data clustering

To investigate the performance of TEABC\_elite algorithm for data clustering, we make a comparison between TEABC\_elite and two-step ABC [49], EABCK [48], HABC [46], ARABC [54], ECABC [23], ABCLGII [24], SLPSO [28], sinDE [35], and *K*-means [49] on five well-known datasets. These datasets are the benchmark datasets in the clustering field and widely used to analyze the performance of the newly developed algorithms, and they are iris, wine, CMC, glass, and WBC, available for download from the UCI repository.<sup>2</sup> They are listed briefly as Table 10, where the number of clusters of each cluster is denoted by *k*, and *d* specifies the number of attributes of each dataset. For the sake of fairness, the maximum number of fitness function evaluations (*max\_FEs*) is set to 10,000 as recommended and presented in [46].

The values of the common control parameters in all algorithms are set as follows. For all ABC and variants, the population size is set to 100 [46], and *limit* set to 100 as well. Moreover, the number of employed bees and onlooker bees were set to be half of the total population, SN=employed bees=onlooker bees=50. For PSO and DE variants such as sinDE and SLPSO, the population size is set to 50. Other algorithmic parameters of all algorithms being compared are as follows, set according to the original literature: two-step ABC, *limit*=10, $\varphi$ =1.5; for EABK, *limit*=100; for HABC, *limit*=100; for ARABC, *limit*=SN · D,  $\Delta$ =0.01,  $\alpha_{min}$ =0,  $\alpha_{max}$ =5; for ABCLGII, r=1, q=0.2; and for sinDE, freq=0.25.

Note that the *K*-means algorithm needs the initial cluster centers only, and no additional parameters are needed. In SLPSO, all parameters are set adaptively according to population size and dimension D. In [49], the population size of two-step ABC was set to 20, but we use 100 here instead of it for all algorithms to make a fair comparison. The outcome of the proposed method is described regarding average within-cluster distances and standard deviation.

Experimental results are given in Table 11 on the iris, wine, CMC, WBC, and glass datasets, where "mean" denotes the average total within-cluster variance for 30 executions and "SD" denotes the standard deviation. The symbol "Rank" denotes the performance order of all compared algorithms according to the total within-cluster variance ter variance criterion on five data sets.

On iris dataset, the performance order of the algorithms is TEABC\_elite = Twostep ABC>ECABC = ABCLGII>EABCK = ABC\_elite > sinDE>HABC>>DG ABC>ARABC>SLPSO>K-means. Results obtained by TEABC\_elite and twostep ABC are close with each other since they employ the global best individual to guide the search process, meanwhile adopt mechanisms to avoid premature convergence. Specifically, two-step ABC only uses the global best solution in the onlooker bee phase, while the TEABC\_elite uses the ordinary solution to balance the great lead ability of the global best solution. By comparison, the EABCK employs the global best solution to guide the search process, both in the employed bee phase and in the onlooker bee phase, so the algorithm is easy to get trapped in the local minimum. Therefore, EABCK achieves the biggest deviation except for K-means.

<sup>&</sup>lt;sup>2</sup> http://archive.ics.uci.edu/ml.

Table 11	Average	total within-	cluster varia	ance of 12 algorithn	ns (Ave. Rar	nk denotes av	verage ranki	ng)					
Data sets	Mean (SD)	TEAB C_elite	ABC_ elite	Two-step ABC	DGA BC	EAB CK	HABC	ARA BC	ECA BC	ABCL GII	SLP SO	SinDE	K-m eans
Iris	Mean	96.65	<b>99.9</b> 6	96.65	96.80	69.96	96.71	96.83	96.66	99.96	97.20	96.70	104.32
	(SD)	0.0031	0.0548	0.0042	0.76	3.78	0.64	0.26	0.12	0.013	0.54	0.16	5.34
	Rank	1	3	1	9	3	5	7	2	2	8	4	6
Wine	Mean	16293.2	16308.1	16294.3	16303.1	16298.3	16301.9	16299.5	16294.4	16297.3	16306.1	16296.5	16555.0
	(SD)	3.27	5.78	4.18	4.37	6.19	3.18	5.22	4.27	9.34	21.84	10.78	473.82
	Rank	1	11	2	6	9	8	7	3	5	10	4	12
CMC	Mean	5534.2	5538.1	5633.3	5550.9	5672.4	5698.3	5567.7	5536.1	5553.3	5701.8	5569.3	5742.1
	(SD)	1.81	3.23	2.29	4.17	3.24	2.98	5.12	2.23	4.83	5.21	4.78	23.18
	Rank	1	3	8	4	6	10	9	2	5	11	7	12
WBC	Mean	2965.41	3021.39	2964.82	3025.18	2969.62	2973.72	2966.72	2988.32	2975.89	2987.72	2980.28	3217.72
	(SD)	9.76	0.07	11.87	12.53	23.25	22.29	12.82	11.76	8.98	38.46	29.82	126.87
	Rank	2	10	1	11	4	5	3	6	9	8	7	12
Glass	Mean	210.75	246.72	211.53	248.30	242.43	237.56	247.12	218.83	236.6012	244.78	264.28	241.79
	(SD)	3.14	5.64	3.20	5.37	4.78	7.23	11.85	4.49	4.81	4.42	8.82	10.03
	Rank	1	6	2	11	7	5	10	3	4	8	12	9
Ave. Rank		1.2	7.2	2.8	8.2	5.8	9.9	9.9	3.8	4.4	9.0	6.8	10.2
Total Rank		1	6	2	10	у.	9	9	ю	4	11	×	12
Bold ind	licates the	best results											

In other datasets, similar rank results are obtained. In Table 11, a rank function is used to determine the performance of all algorithms with corresponding datasets, and finally, an average rank is obtained using the individual rank of algorithms. To sum up, the proposed algorithm TEABC\_elite obtains the best average rank among the compared ones of 1.2, while SLPSO and *K*-means obtain the worst two ranks, 9.0 and 10.2, respectively.

As can be seen from Table 11, the proposed algorithm TEABC\_elite achieves the best clustering results on four datasets and ranks second on one dataset. The main reason is that the proposed TEABC\_elite effectively utilizes ordinary solutions and has a better global search ability, so it avoids falling into the local optimal solution, achieving more stable performance.

# 6 Conclusions

In order to accelerate convergence and seeking for a better exploration–exploitation balance, an improved elite-guided ABC variant EABC\_elite is proposed by using two novel search equations. The global best solution is used in the first equation on the employed bee phase to accelerate the convergence process, while the ordinary solution is used on the employed bee phase and onlooker bee phase to avert precocity. Comparing existing elite-guided ABC variants, such as ABC\_elite, IABC\_elite, and ABCLGII, each individual is guided by the global best individual to accelerate convergence in EABC\_elite and ECABC, while EABC\_elite uniquely has no bias to any search directions and show better global search ability by using novel balance strategy. Experiments on well-known test suites demonstrate that the proposed algorithm is significantly better than other ABC variants also some non-ABC variants on most of the functions tested regarding solution quality, robustness, and convergence speed. Additionally, the proposed EABC\_elite can also be applied to solve the feature selection problems, where experimental results show that the performance of EABC\_elite is superior to other feature selection methods.

Furthermore, TEABC\_elite is designed to enhance the global search ability to solve data clustering, where the chaos parameter and *K*-means initialization strategies are integrated into EABC\_elite. Experimental results executed on well-known datasets show that TEABC\_elite has superior performance than other existing clustering methods, confirming that it is a competitive clustering tool.

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