



Revealing the cyclization selectivity in intramolecular [3 + 2] cycloaddition reactions of allenic nitrones from the molecular electron density theory perspective

Barsali Banerjee¹ · Nivedita Acharjee¹ · Debnath Palit²

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Abstract

The intramolecular [3 + 2] cycloaddition (32CA) reactions of allenic nitrones have been studied within the molecular electron density theory (MEDT) at the MPWB1K/6-311G(d,p) computational level. These zwitter-ionic type 32CA reactions show high activation free energies between 22.2 and 34.9 kcal mol⁻¹ in ethanol consistent with their predicted non-polar character and follow one-step mechanism with highly asynchronous transition states. Interestingly, when the nitrone and the allene moieties are separated by two methylene units, the [3 + 2] addition is energetically feasible along the C5-C6 terminal double bond of the allene, while the presence of four methylene units change the cyclization selectivity towards the internal C4-C5 double bond of the allene. This is in complete agreement with the experimental outcomes. The molecular mechanism study in terms of bonding evolution theory (BET) shows varied electron density changes along these two reaction paths. Finally, the topological analysis of AIM (atoms-in-molecules) reveals the presence of non-covalent interactions at the interatomic bonding regions of the transition states, which agrees well with the electron localization function analysis and the forming C–C and C–O bond distances.

Keywords Molecular electron density theory · Electron localization function · Activation energy · Allenic nitrones · [3 + 2] cycloaddition reactions

Introduction

Allenes present an intriguing group of reacting counterparts in [3 + 2] cycloaddition (32CA) reactions owing to the presence of two cumulative unsaturations [1]. Although the simplest allene shows limited reactivity in the 32CA reactions with *C*-phenyl-*N*-methyl nitrone **1**, incorporation of electron-deficient substituents (such as cyano (**2**), carbomethoxy (**3**), phenylsulfonyl (**4**), methoxy (**5**), fluoro (**6**)) overcomes the unreactive nature, affording high yield of isoxazolidines under milder reaction conditions with site selectivity towards the generation of CA_{4,5} and CA_{5,6} addition (Scheme 1) [2–7]. Nitrone-allene 32CA reactions show

well-established applications in the total synthesis of alkaloids and natural products [8], and also exhibit interesting selectivity and mechanistic implications. Recently, Lee et al. have reported the mechanism and selectivity of the intermolecular 32CA reactions of nitrones with activated allenes [9].

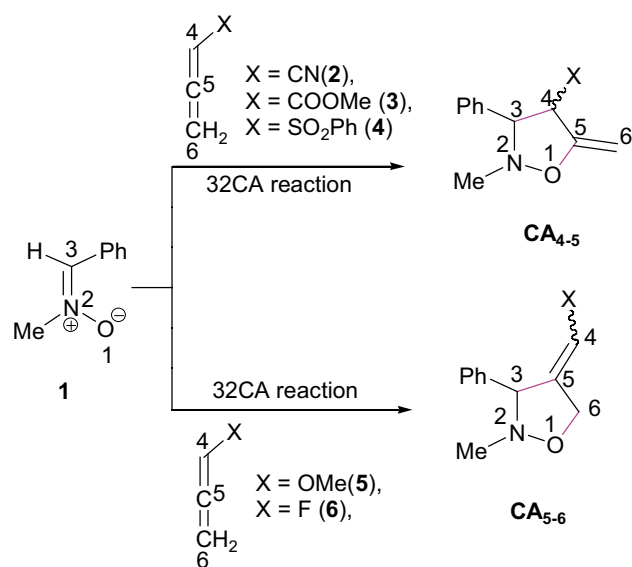
An interesting alternative to explore the reactivity of unactivated allenes was designed by Lebel and Banucci in 1970 [10] from the intramolecular [3 + 2] cycloaddition (IM32CA) reactions of allenic nitrones, and was also reported by Padwa et al. [11] in 1993 to proceed smoothly affording reasonably good yields. The IM32CA reactions consist of both nitrone and the allenic function suitably placed in the same molecule and exhibit interesting site selectivity for the two allenic double bonds depending on the substrate. For instance, the IM32CA reaction of exocyclic nitrone **7** affords isoxazolidine **8** by addition along the terminal C5-C6 double bond, while the allenic nitrone **9** involves addition along the internal C4-C5 double bond and affords the bridged bicyclic isoxazolidine **10** (Scheme 2).

The IM32CA reaction of the allenic nitrone **11** generated from 5,6-heptadien-2-one and *N*-methylhydroxylamine

✉ Nivedita Acharjee
nivchem@gmail.com

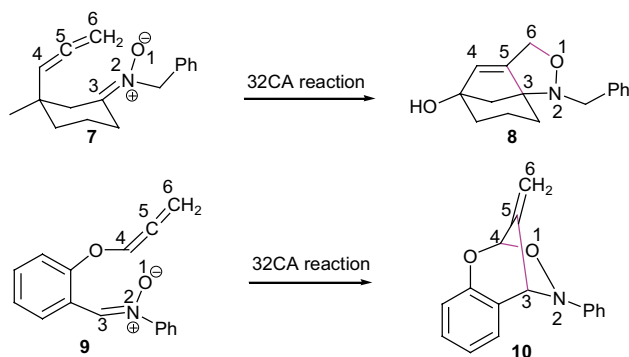
¹ Department of Chemistry, Durgapur Government College, Durgapur, West Bengal 713214, India

² Department of Botany, Durgapur Government College, Durgapur, West Bengal 713214, India



Scheme 1 Intermolecular 32CA reactions of nitrones and allenes

hydrochloride in ethanol afforded unsaturated bicyclic isoxazolidine **14** with complete site selectivity for addition along the C5–C6 terminal double bond [10] (Scheme 3). The cyclization of the homologue nitrone **12** under similar reaction conditions afforded the bicyclic adducts **15** by addition along the terminal C5–C6 double bond, and **16** by addition along the terminal C4–C5 double bond, while the latter undergoes acid-catalyzed ethanol addition to the exocyclic double bond to afford the ethers **17** and **18** (Scheme 3). The homologue nitrone **13** ($n=4$) proceeded with exclusive site selectivity for addition along the internal C4–C5 double bond of the allenic function, leading to the bicyclic adduct **19** (Scheme 3). These experimental findings imply that the separation of the nitrone and the allenic functions plays the decisive role in the mode of cyclization. Although the generation of preferred adducts have been advocated qualitatively by considering the strain factor in some cases to eliminate the possibility of the competing site selectivity, yet the correlation of molecular



Scheme 2 IM32CA reactions of allenic nitrones **7** and **8**

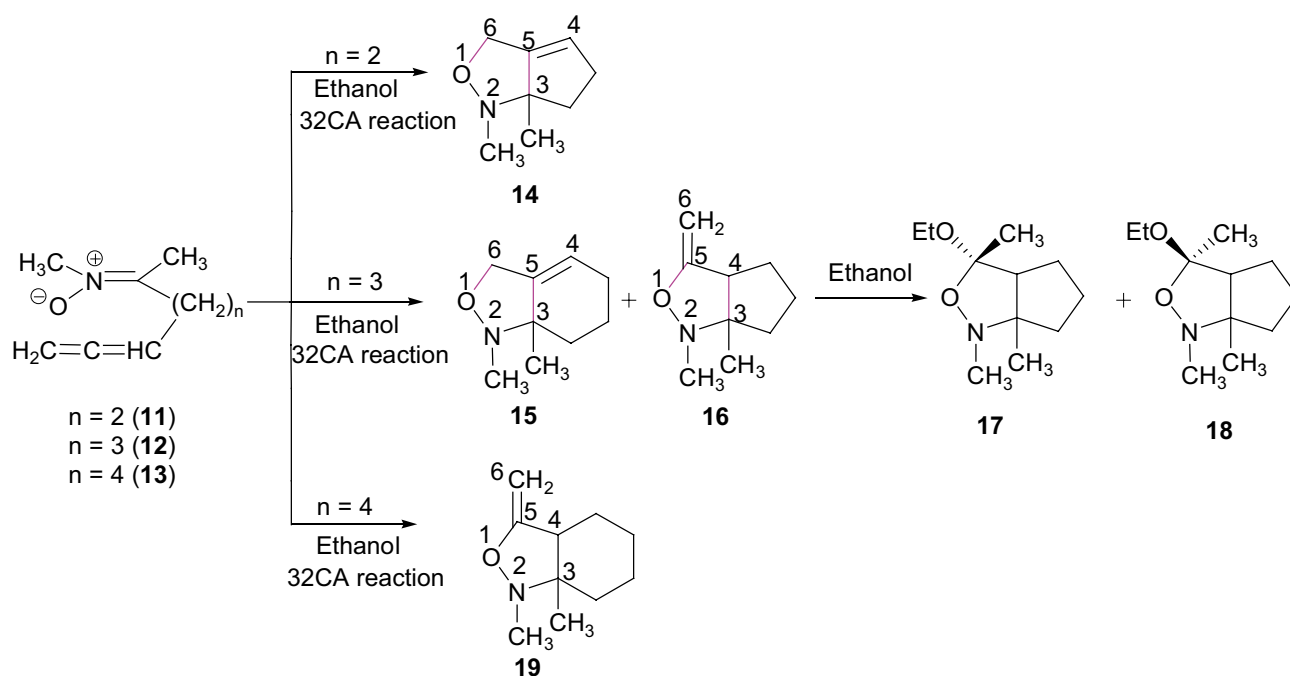
reactivity with the electron density changes along the two feasible cumulative unsaturations are worth investigating to outline the plausible mechanism and accordingly analyze the observed selectivity of these IM32CA reactions.

The molecular electron density theory [12] (MEDT) proposed by Domingo in 2016 studies the role of electron density changes in the molecular reactivity and has emerged as an appealing alternative to the FMO theory for analysis of organic reactions. Several aspects of [3 + 2] cycloaddition (32CA) reactions [13, 14] have been successfully studied within the MEDT framework, namely the strain promotion [15, 16], reactivity [17, 18], catalysis [19, 20], substituent effects [21, 22], regio- [23, 24], stereo [25, 26] and chemoselectivity [27, 28]. Very recently, we have reported the MEDT studies for the IM32CA reactions of nitrones [29] at the MPWB1K/6-311G(d,p) level of theory, recommended as a precise computational model for the analysis of 32CA reactions.

This MEDT report is presented in five sections: (1) first, the topological analysis of the electron localization function [30, 31] (ELF) at the ground state (GS) of the reagents is performed to correlate the electronic structure and the molecular reactivity; (2) second, the electronic behaviour at the GS of the reagents is analyzed on the basis of the global reactivity indices defined with the conceptual density functional theory [32, 33] (CDFT); (3) then, the potential energy surface (PES) along the feasible reactions paths is studied to locate the stationary points and analyze the energy profile with the evaluation of global electron density transfer [34] (GEDT) at the TSs to assess the polar character; (4) the mechanistic implications are studied in terms of the bonding evolution theory [35] (BET) to analyze the changes in electron density along the preferred reaction paths; (5) finally, the electronic structure at the TSs is analyzed from the ELF study, while the interatomic interactions are characterized from the AIM [36, 37] (atoms-in-molecules) parameters and subsequent NCI-Plot [38] visualization.

Computational methods

Optimization of the reagents, TSs and the products was done using Berny analytical gradient optimization method [39] at the MPWB1K/6-311G(d,p) level of theory. The stationary points were characterized as minima by the absence of imaginary frequency, while the TSs by one imaginary frequency along each reaction path. Solvent effects in ethanol were considered by full optimization at the same computational level using polarized continuum model within the self-consistent reaction field (SCRf) framework [40–42]. The relative enthalpies, entropies and free energies were calculated at 298 K and 1 atm in ethanol. The intrinsic reaction coordinate [43] (IRC)



Scheme 3 IM32CA reactions of allenic nitrones **11**, **12** and **13**

calculations using the second-order Gonzales-Schlegel integration method [44, 45] were performed to verify the reaction path connecting the reactants and the products. The GEDT at the TSs was determined by $\text{GEDT}(f) = \sum_{q \in f} q$, where q is the NBO-derived charge [46, 47] at the considered reacting framework. The reactivity indices defined within the CDFT, namely the electronic chemical potential μ [48], global hardness η [49], global electrophilicity ω [50, 51] and nucleophilicity N [52], were calculated according to reference [32].

All calculations were performed using Gaussian 03 suite of programs [53]. The electron localization function [30, 31] (ELF) ((high-quality grid with a spacing of 0.06 Bohr) and AIM [36, 37] parameters were calculated using the Multiwfn software [54]. The ELF localization domains were visualized using the UCSF Chimera software [55] at an isovalue 0.86 and Visual Molecular Dynamics (VMD 1.9.3.) was used to visualize the NCI isosurfaces [56].

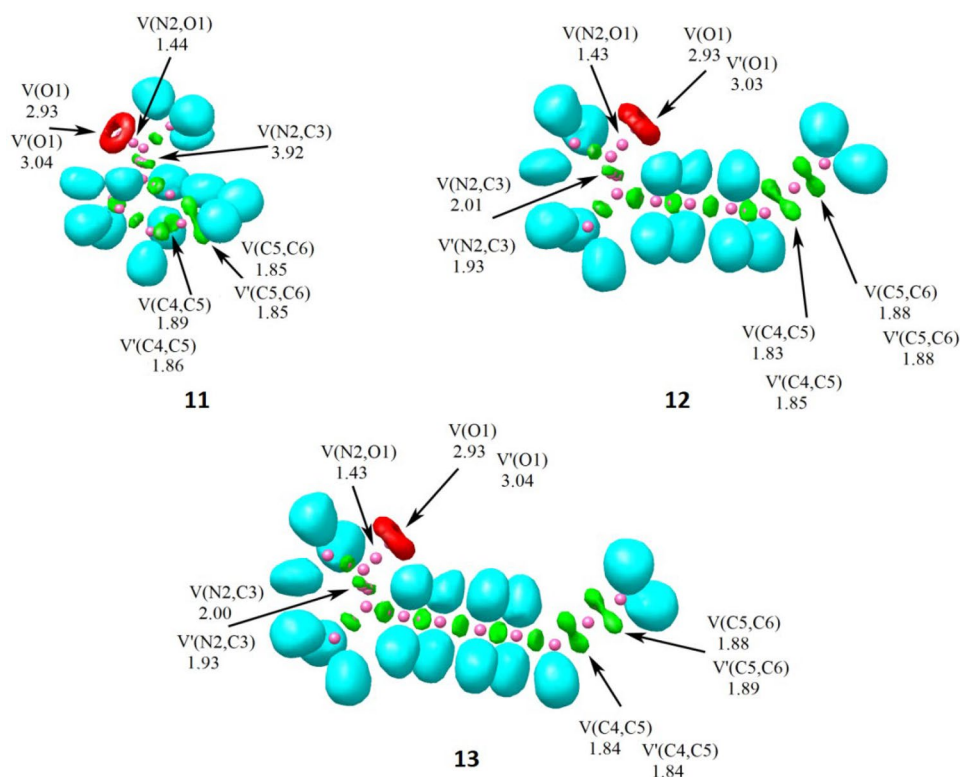
Results and discussion

ELF topological analysis at the ground state (GS) of the reactants

The ELF [30, 31] allows characterizing the electronic structures at the GS of the reagents and accordingly establishing the correlation with molecular reactivity. The three atom

components (TACs) participating in 32CA reactions can be classified as *pseudodiradical*, *pseudo(mono)radical*, carbenoid and zwitter-ionic, respectively, within the MEDT framework [12–14]. The *pseudodiradical* TACs [57] are associated with the presence of two *pseudoradical* centres (monosynaptic basin integrating less than 1 e), and show highest reactivity, while the *pseudo(mono)radical* [58] and carbenoid TACs [59] show relatively lower reactivity and are associated respectively with the presence of a *pseudoradical* and a carbenoid (monosynaptic basin integrating approximately 2 e) centre. The zwitter-ionic TACs [23] show the least reactivity in 32CA reactions and do not show the presence of *pseudoradical* and carbenoid centres. The most significant ELF valence basin populations, attraction positions and the ELF localization domains at the GS of the allenic nitrones **11**, **12** and **13** are represented in Fig. 1. The ELF of **11**, **12** and **13** show the presence of monosynaptic $V(\text{O}1)$ and $V'(\text{O}1)$ basins integrating 5.96–5.97 e associated with the non-bonding electron density at O1 oxygen. The N2-C3 and N2-O1 bonding regions integrate at 3.92–3.94 e and 1.43–1.44 e respectively associated with the N2-C3 double bond and N2-O1 single bond. The allenic moiety shows the presence of disynaptic $V(\text{C}4,\text{C}5)$ and $V'(\text{C}4,\text{C}5)$ basins integrating 3.68–3.75 e associated with the underpopulated C4-C5 double bond and the disynaptic $V(\text{C}5,\text{C}6)$ and $V'(\text{C}5,\text{C}6)$ basins integrating 3.70–3.77 e associated with the underpopulated C5-C6 double bond. Thus, the absence of *pseudoradical* and carbenoid centre in the allenic nitrones **11**, **12** and **13** allows their classification as the zwitter-ionic TACs associated with high energy barrier.

Fig. 1 MPWB1K/6-311G(d,p) calculated total electron density (isovalue = 0.1) and ELF localization domains (isovalue = 0.81) of gas phase allenic nitrones **11**, **12** and **13** along with the most significant ELF basin populations. Protonated basins are shown in blue, monosynaptic basins in red, disynaptic basins in green and the core basins in black colour. ELF attractor positions are shown in pink colour



After establishing the electronic structure of the TACs, the proposed Lewis-like structures on the basis of ELF study is represented in Fig. 2 along with the NBO-derived charges. O1 of the nitron moiety is negatively charged by -0.60 e, while C3 is positively charged by $+0.25$ e, with the negligible charge 0.08 e at N2. In the allenic part, the terminal C6 carbon is negatively charged by -0.47 e, while C4 shows the negative charge of -0.28 e and -0.29 e owing to the alkyl chain substitution.

Analysis of the CDFT indices

The reactivity indices defined with the CDFT [32, 33] have been employed in numerous studies [12–22] to analyze the electronic behaviour at the GS of the reagents.

The electronic chemical potential μ [48], chemical hardness η [49], global electrophilicity ω [50, 51] and global nucleophilicity N [52] at the GS of the allenic nitrones **11**, **12** and **13** are calculated at the B3LYP/6-31G(d) level of theory (Table 1) to characterize the reagents within the standard electrophilicity and nucleophilicity scales defined at the same computational level [51]. The electronic chemical potentials μ of the allenic nitrones are between -2.75 eV and -2.83 eV, showing minimal increase from **11** to **13** with the increase in the alkyl chain length separation between the nitron and the allene moieties. The nitrones are classified as marginal electrophiles ($\omega < 0.80$ eV) within the electrophilicity scale and strong nucleophiles ($N > 3.00$ eV) within the standard nucleophilicity scale.

Fig. 2 Proposed Lewis-like structures together with the natural atomic charges in average number of electrons, e, of the allenic nitrones **11**, **12** and **13**. Negative, negligible and positive charges are shown in red, green and blue colours, respectively

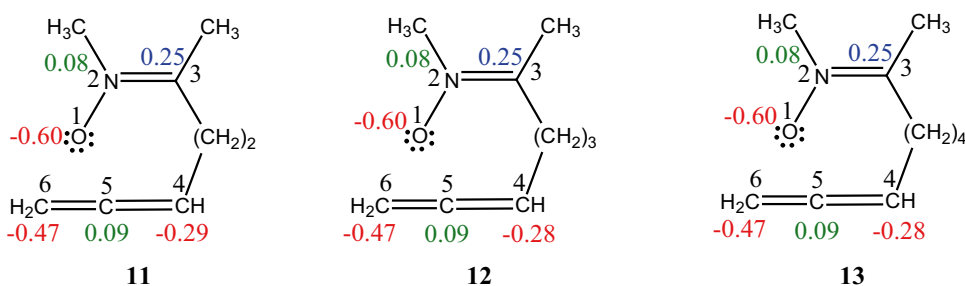


Table 1 B3LYP/6-31G(d) calculated electronic chemical potential μ , chemical hardness η , global electrophilicity ω and global nucleophilicity N , in eV at the ground state of the allenic nitrones **11**, **12** and **13**

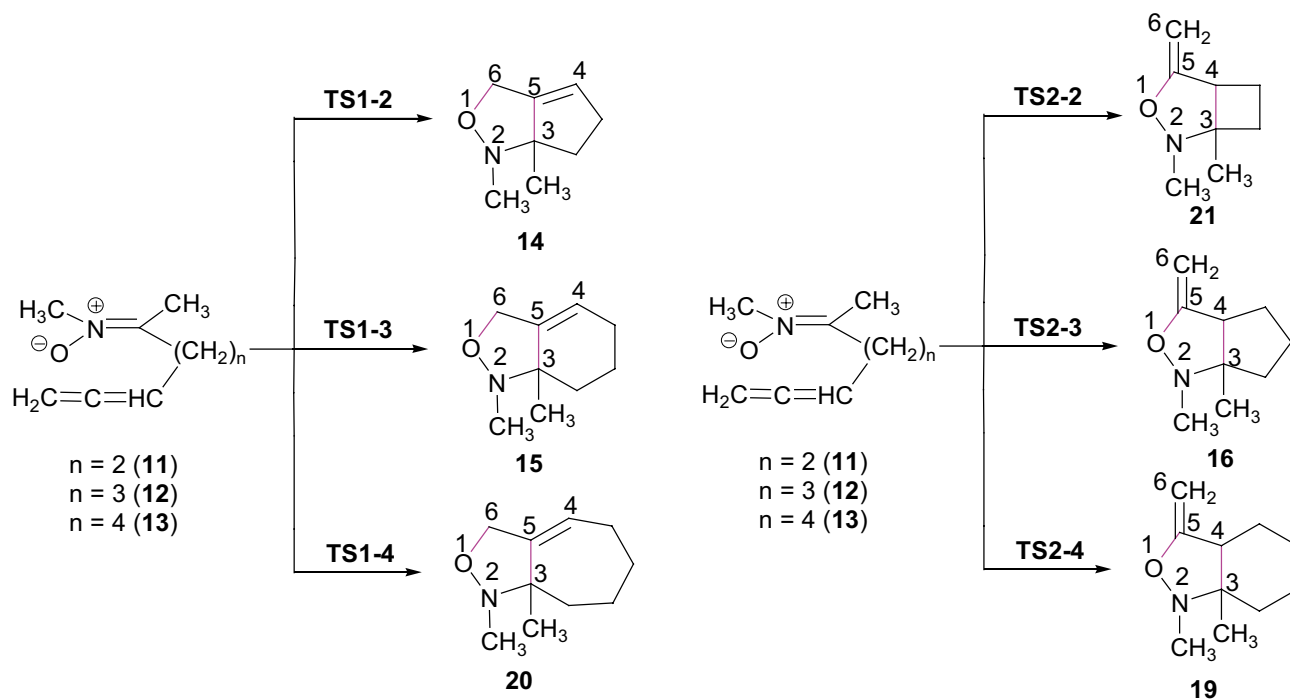
	μ	η	ω	N
11	-2.83	5.06	0.79	3.75
12	-2.78	5.17	0.74	3.75
13	-2.75	5.22	0.72	3.75

Exploring the potential energy surface along the IM32CA reactions of the allenic nitrones **11–13**

Herein, the two feasible reaction channels associated with the IM32CA reactions of allenic nitrones **11–13** involving the addition of the nitrono moiety to the terminal C5-C6 double bond and to the internal C4-C5 double bond have been studied (Scheme 4).

Search for the stationary points along these reaction paths allowed locating the reagents, only one TS and the bicyclic adduct in each case, suggesting one-step mechanism. The TSs and adducts associated with the addition along the C5-C6 and C4-C5 double bonds are respectively prefixed as **TS1** and **TS2**, followed by **2**, **3** and **4** respectively indicating the number of CH₂ groups separating the nitrono and the allenic function. Thus, **TS1-2**, **TS1-3** and **TS1-4** are the TSs associated with the addition of the nitrono moiety of the reagents **11**, **12** and **13** along the C5-C6 double bond respectively leading to the bicyclic adducts **14**, **15** and **20**, while **TS2-2**, **TS2-3** and **TS2-4** are associated with

the addition of nitrono moiety of the reagents **11**, **12** and **13** along the C4-C5 double bond respectively leading to the bicyclic adducts **21**, **16** and **19**. The relative energies, enthalpies, entropies and free energies in ethanol of the TSs and adducts are given in Table 2. The total thermodynamic data are gathered in the Supplementary Information. The studied IM32CA reactions are exergonic, with reaction free energies between -17.3 and -35.1 kcal mol⁻¹, suggesting kinetic control and show activation free energies between 22.2 and 34.9 kcal mol⁻¹, consistent with the πw -type character. Some appealing conclusions can be derived from the relative free energies. (1) For the IM32CA reaction of nitrono **11**, the activation free energy of **TS1-2** associated with addition along the C5-C6 bond is lowered by 5.9 kcal mol⁻¹ relative to that of **TS2-2** associated with the addition along the C4-C5 bond. This is in complete agreement with the experimental results [10] showing exclusive formation of the unsaturated bicyclic isoxazolidine **14**. (2) The activation free energy of **TS1-2** is lowered than that of **TS1-3** and **TS1-4** by 4.3 and 12.7 kcal mol⁻¹ suggesting that the addition of the nitrono moiety to the terminal C5-C6 double bond of the allenic function is relatively more feasible when the nitrono and the allene groups are separated by two methylene units. (3) For the IM32CA reaction of nitrono **13**, the activation free energy of **TS2-4** associated with addition along the C4-C5 bond is lowered by 7.7 kcal mol⁻¹ relative to that of **TS1-4** associated with the addition along the C5-C6 bond. This is in complete



Scheme 4 Studied reaction paths for the IM32CA reactions of allenic nitrones

Table 2 MPWB1K/6-311G(d,p) relative energies in gas phase and the relative energies, enthalpies, entropy and free energies in ethanol at 298.15 K, in kcal·mol⁻¹, of TSs and cycloadducts for the IM32CA reactions of allenic nitrones **11**, **12** and **13**

TS	$\Delta E/$ gas phase	$\Delta E/$ ethanol	$\Delta H/$ ethanol	$\Delta S/$ ethanol	$\Delta G/$ ethanol	Product	$\Delta E/$ gas phase	$\Delta E/$ ethanol	$\Delta H/$ ethanol	$\Delta S/$ ethanol	$\Delta G/$ ethanol
TS1-2	16.9	19.6	18.5	-12.4	22.2	14	-33.3	-29.7	-28.4	-15.5	-23.8
TS2-2	23.6	26.7	25.4	-9.2	28.1	21	-25.8	-21.5	-21.1	-12.7	-17.3
TS1-3	18.5	22.4	21.7	-16.3	26.5	15	-42.2	-37.1	-35.2	-20.8	-29.0
TS2-3	15.1	19.1	18.2	-16.6	23.2	16	-44.6	-39.6	-38.2	-18.6	-32.6
TS1-4	25.4	29.7	29.1	-19.6	34.9	20	-40.4	-34.8	-32.5	-25.6	-24.9
TS2-4	17.8	21.9	21.1	-20.4	27.2	19	-49.8	-44.5	-42.7	-25.5	-35.1

agreement with the experimental results showing exclusive formation of the bicyclic isoxazolidine **19** [10]. (3) These unimolecular IM32CA reactions show negative relative entropies of the TSs between -9.2 and -20.4 kcal mol⁻¹ and that of the adducts are between -12.7 and -25.6 kcal mol⁻¹. Note that the relative entropies of **19** and **20** differ by 0.1 kcal mol⁻¹, that of **15** and **16** differ by 2.2 kcal mol⁻¹ and that of **14** and **21** differ by 2.8 kcal mol⁻¹ suggesting the influence of ring size on the entropy differences of the two possible adducts. Inclusion of thermodynamic correction decreases the activation enthalpies by 0.6–1.3 kcal mol⁻¹ relative to the activation energies, while the reaction enthalpies are increased by 0.4–1.9 kcal mol⁻¹ relative to the reaction energies.

The MPWB1K/6-311G(d,p) optimized geometries of the TSs in ethanol are shown in Fig. 3, with the bond distances between the four interacting atomic centres, GEDT and the imaginary frequencies in gas phase and ethanol are given in Table 3. The distances between the C–C interacting centres

are greater than 2.0 Å, and that between the C–O interacting centres are greater than 1.9 Å suggesting that the formation of new C–C and C–O covalent bond formation has not been started at the TSs, considering the formation of C–C bonds at 1.9–2.0 Å and the C–O bonds at 1.7–1.8 Å [13]. This is in complete agreement with the ELF and AIM studies (“[ELF and AIM topological analyses of the electron density at the TSs associated with the IM32CA reactions](#)” section). Note that **TS2-2**, **TS2-3** and **TS2-4** associated with the addition along the C4–C5 double bond are more asynchronous and relatively more advanced compared to **TS1-2**, **TS1-3** and **TS1-4** associated with the addition along the C5–C6 double bond.

The GEDT [34] allows evaluating the flux of electron density at the TSs and hence the polar character. GEDT values above 0.2 e are associated with polar reactions, while those below 0.1 e are the non-polar ones. Accordingly, the calculated GEDT values at the TSs are given in Table 4. In both gas phase and ethanol, the GEDT values are between

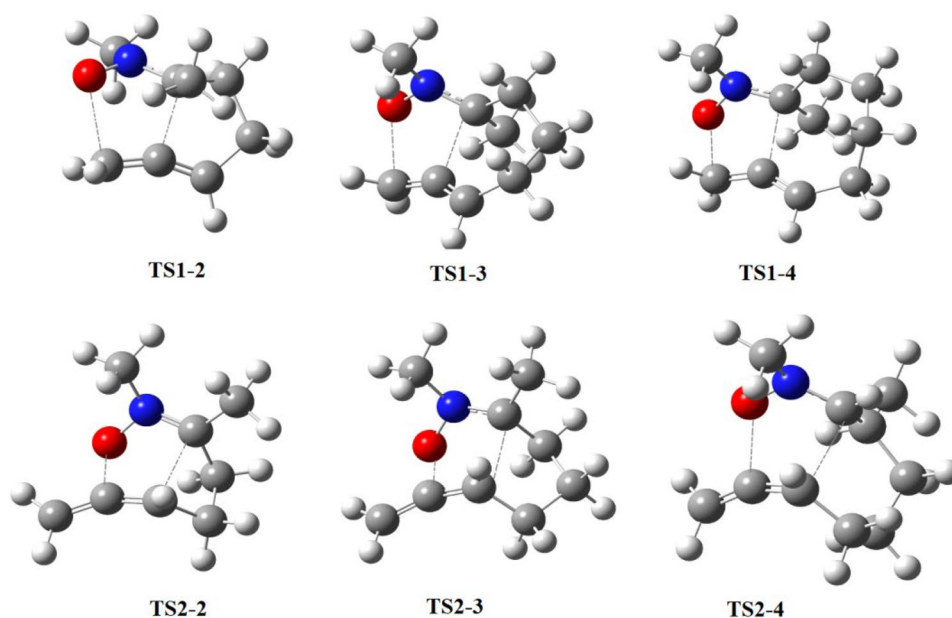
Fig. 3 MPWB1K/6-311G(d,p) optimized geometries of the TSs in ethanol

Table 3 MPWB1K/6-311G(d,p) calculated forming bond distances (Å), imaginary frequencies (cm^{-1}) at optimized TSs and GEDT in average number of electrons associated with the IM32CA reactions of allenic nitrones **11**, **12** and **13**

TS	Gas phase			Imaginary frequency	Ethanol			Imaginary frequency
	$d_{\text{C-O}}$	$d_{\text{C-C}}$	GEDT		$d_{\text{C-O}}$	$d_{\text{C-C}}$	GEDT	
TS1-2	2.229	2.036	0.01	−499.996	2.238	2.009	0.01	−515.975
TS2-2	1.908	2.226	0.04	−476.925	1.903	2.197	0.04	−496.903
TS1-3	2.169	2.169	0.04	−459.460	2.191	2.136	0.03	−487.604
TS2-3	1.989	2.295	0.04	−551.980	2.000	2.254	0.03	−572.059
TS1-4	2.096	2.274	0.05	−493.542	2.112	2.233	0.05	−515.339
TS2-4	2.063	2.267	0.06	−474.143	2.071	2.228	0.05	−492.057

0.01 and 0.06 e, indicating non-polar character allowing the classification of these zw -type 32CA reactions as the null electron density transfer (NEDF) [60] type. The predicted non-polar character is consistent with the calculated high activation parameters associated mainly with the rupture of the C–C double bond revealed from the ELF topological analysis along the reaction paths (“[Revealing the molecular mechanism and flux of electron density along the reaction paths associated with the IM32CA reactions of the allenic nitrones 11 and 13](#)” section).

Revealing the molecular mechanism and flux of electron density along the reaction paths associated with the IM32CA reactions of the allenic nitrones **11** and **13**

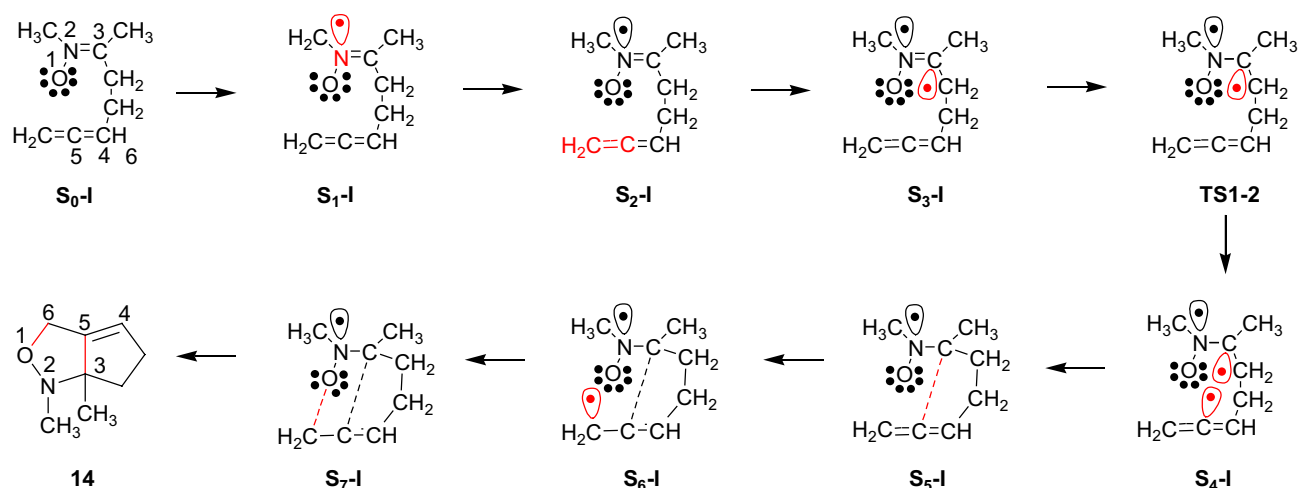
The bonding evolution theory (BET) [35] is a quantum chemical methodology to establish the molecular mechanism of a chemical reaction by studying the nature of electronic rearrangement along a reaction path. The bonding changes are analyzed topologically and energetically within the MEDT perspective, allowing a complete understanding of the bonding changes and the origin of the energy profile. Herein, the molecular mechanism of the preferred reaction paths for the IM32CA reaction of the allenic nitrones **11** and

13, leading to the adducts **14** and **19**, is studied. The complete BET studies are given in the Supplementary material. In this section, we explain the appealing conclusions arising from these BET studies in a chemical fashion.

(1) The molecular mechanism associated with the IM32CA reactions of the allenic nitrones **11** and **13** are represented in Schemes 5 and 6 respectively. The IM32CA reaction of **11** can be topologically characterized by eight differentiated phases while that of **13** by seven topological phases. (2) For the IM32CA reaction of **11**, the starting structure of the phases is denoted as $S_0\text{-I}$, $S_1\text{-I}$, $S_2\text{-I}$, $S_3\text{-I}$, $S_4\text{-I}$, $S_5\text{-I}$, $S_6\text{-I}$ and $S_7\text{-I}$, and for that of **13** is represented as $S_0\text{-II}$, $S_1\text{-II}$, $S_2\text{-II}$, $S_3\text{-II}$, $S_4\text{-II}$ and $S_5\text{-II}$. (3) For the IM32CA reaction of **11**, $S_1\text{-I}$ is associated with the creation of non-bonding electron density at N2 nitrogen with energy cost (EC) of $15.4 \text{ kcal}\cdot\text{mol}^{-1}$, $S_2\text{-I}$ is associated with the rupture of C5-C6 double bond with energy cost (EC) of $16.2 \text{ kcal}\cdot\text{mol}^{-1}$, $S_3\text{-I}$ is associated with the formation of *pseudoradical* centre at C3 with energy cost (EC) of $16.6 \text{ kcal}\cdot\text{mol}^{-1}$ and **TS1-2** with the EC of $16.9 \text{ kcal}\cdot\text{mol}^{-1}$ belongs to *Phase-III*. Therefore, the activation energy associated with this IM32CA reaction is related to the formation of non-bonding electron density at N2 nitrogen, rupture of C5-C6 double bond and the creation of *pseudoradical* centre at C3 carbon. The subsequent phases are related to the

Table 4 ELF valence basin populations at the MPWB1K/6-311G(d,p) optimized gas phase TSs associated with the IM32CA reactions of the allenic nitrones **11**, **12** and **13**

	TS1-2	TS1-3	TS1-4	TS2-2	TS2-3	TS2-4
V(O1)	2.95	2.95	2.94	2.94	2.95	2.95
V'(O1)	2.88	2.88	2.87	2.90	2.88	2.89
V(N2,O1)	1.29	1.31	1.30	1.24	1.26	1.28
V(N2,C3)	2.51	2.55	2.66	2.93	2.93	2.95
V(C5,C6)	3.55	3.57	3.03	1.87	1.88	1.88
V'(C5,C6)				1.90	1.91	1.89
V(C4,C5)	1.89	1.90	1.87	3.20	3.23	3.27
V'(C4,C5)	1.84	1.84	1.83			
V(N2)	1.31	1.24	1.19	1.32	1.32	1.25
V(C3)	0.39	0.36	0.36			
V(C5)			0.59			
V(C4)				0.45	0.37	0.38

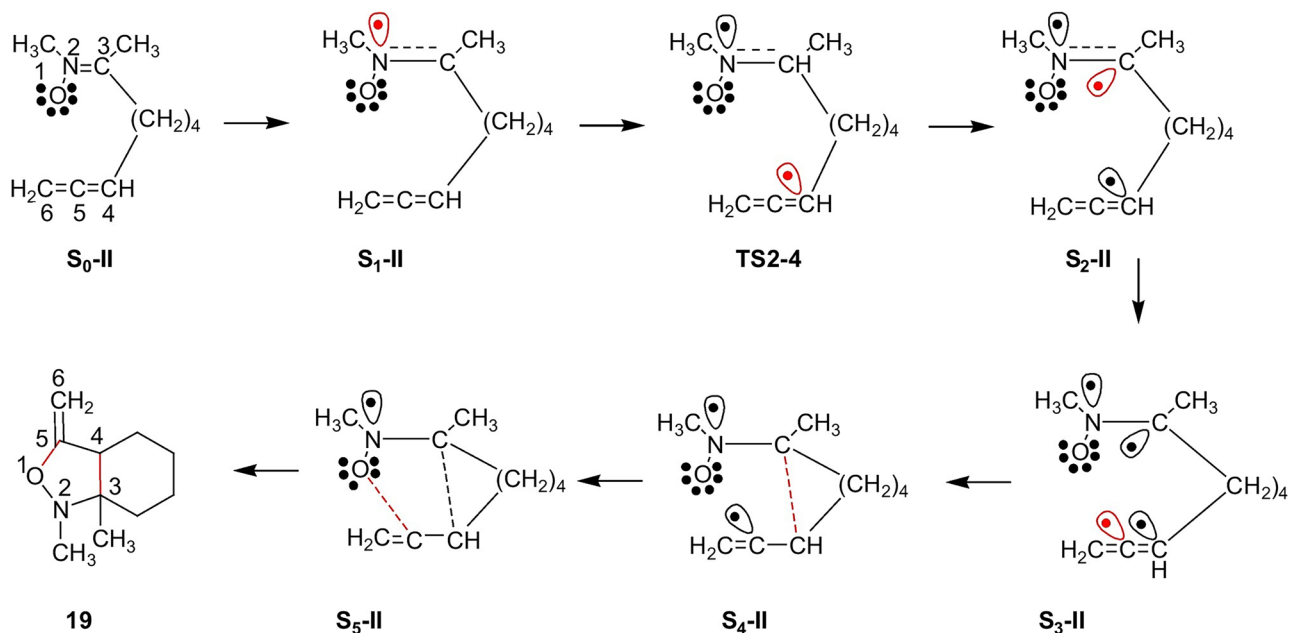


Scheme 5 Simplified representation of the molecular mechanism of the reaction path associated with the IM32CA reaction of allenic nitrene **11** leading to adduct **14** arising from the topological analysis of the ELF

creation of *pseudoradical* centre at C5 (**S₄-I**), formation of C3-C5 single bond (**S₅-I**), creation of *pseudoradical* centre at C6 (**S₆-I**) and finally the formation of O1-C6 single bond (**S₇-I**). The ELF localization domains of these structures are given in Fig. 4. The formation of second O1-C6 bond begins when the first C3-C5 bond formation has been completed by 94%, suggesting two-stage one-step mechanism.

(4) For the IM32CA reaction of **13**, **S₁-II** is associated with the creation of non-bonding electron density at N2 nitrogen and rupture of the C4-C5 double bond with energy

cost (EC) of 17.2 kcal·mol⁻¹, **TS2-4** is associated with the formation of *pseudoradical* centre at C4 with energy cost (EC) of 17.8 kcal·mol⁻¹. Therefore, the activation energy associated with this IM32CA reaction is related to the formation of non-bonding electron density at N2 nitrogen, rupture of C4-C5 double bond and the creation of *pseudoradical* centre at C4 carbon. The subsequent phases are related to the creation of *pseudoradical* centre at C3 (**S₂-II**), creation of *pseudoradical* centre at C5 (**S₃-II**), formation of C3-C4 single bond (**S₄-II**) and finally the formation of



Scheme 6 Simplified representation of the molecular mechanism of the reaction path associated with the IM32CA reaction of allenic nitrene **13** leading to adduct **19** arising from the topological analysis of the ELF

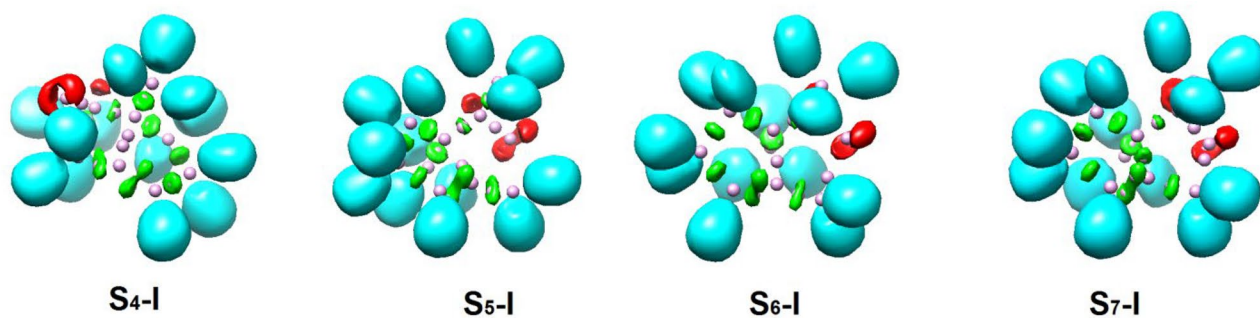


Fig. 4 MPWB1K/6-311G(d,p) ELF localization domains of **S₄-I**, **S₅-I**, **S₆-I** and **S₇-I** associated with the formation of C3-C5 and O1-C6 bonds in the IM32CA reaction of allenic nitrene **11** (protonated)

basins are shown in blue, monosynaptic basins in red, disynaptic basins in green and the core basins in black colour (isovalue = 0.85). The ELF attractors are shown in pink colour

O1-C5 single bond (**S₅-II**). The ELF localization domains of these structures are given in Fig. 5. The formation of second O1-C5 bond begins when the first C3-C4 bond formation has been completed by 77%, suggesting asynchronous one-step mechanism for this IM32CA reaction. (5) The minimal GEDT along the reaction path to reach the TSs establishes non-polar character of these IM32CA reactions consistent with the high activation energies.

ELF and AIM topological analyses of the electron density at the TSs associated with the IM32CA reactions

Finally, the ELF topological analysis at the TSs involved in the 32CA reactions was performed. The relevant valence basin populations are given in Table 4 and the ELF localization domains are shown in Fig. 6. **TS1-2**, **TS1-3** and **TS1-4** associated with the addition along the C5-C6 bond of the allenic nitrenes **11**, **12** and **13** present similar ELF topology, and that of **TS2-2**, **TS2-3** and **TS2-4** associated with the addition along the C4-C5 bond show similitude in

the electronic structure. All six TSs show the presence of V(N2) monosynaptic basin integrating 1.19–1.32 e associated with the accumulation of non-bonding electron density at N2 nitrogen, which is not found in the allenic nitrenes **11–13**. The ELF of **TS1-2**, **TS1-3** and **TS1-4** shows the formation of V(C3) monosynaptic basin integrating 0.36–0.39 e associated with the presence of *pseudoradical* centre at C3, which is not found in **TS2-2**, **TS2-3** and **TS2-4**. Note that to create the *pseudoradical* centre at C3 carbon and non-bonding electron density at N2 nitrogen, the N2-C3 bonding region at **TS1-2**, **TS1-3** and **TS1-4** experiences depopulation between 1.27 e and 1.41 e relative to the separated reagents, while this depopulation is between 0.98 e and 1.01 e at **TS2-2**, **TS2-3** and **TS2-4**, since the non-bonding electron density at N2 nitrogen is only formed in these three TSs. The N2-O1 bonding region is also depopulated between 0.12 e and 0.15 e at **TS1-2**, **TS1-3** and **TS1-4** and between 0.15 e and 0.20 e at **TS2-2**, **TS2-3** and **TS2-4** to contribute for the accumulation of non-bonding electron density at the N2 nitrogen. Interestingly, **TS1-4** shows the presence of V(C5) monosynaptic basin integrating 0.59 e

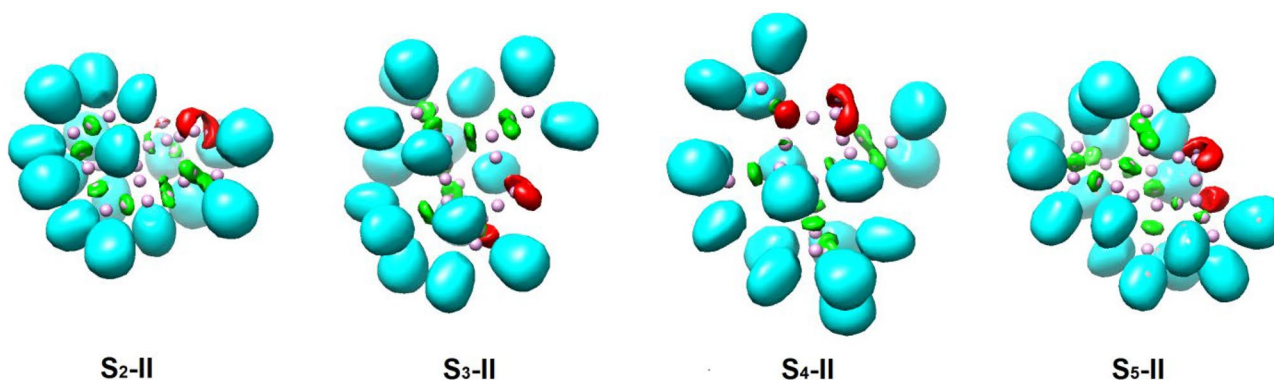


Fig. 5 MPWB1K/6-311G(d,p) ELF localization domains of **S₂-II**, **S₃-II**, **S₄-II** and **S₅-II** associated with the formation of C3-C4 and O1-C5 bonds in the IM32CA reaction of allenic nitrene **13** (protonated)

basins are shown in blue, monosynaptic basins in red, disynaptic basins in green and the core basins in black colour (isovalue = 0.85). The ELF attractors are shown in pink colour

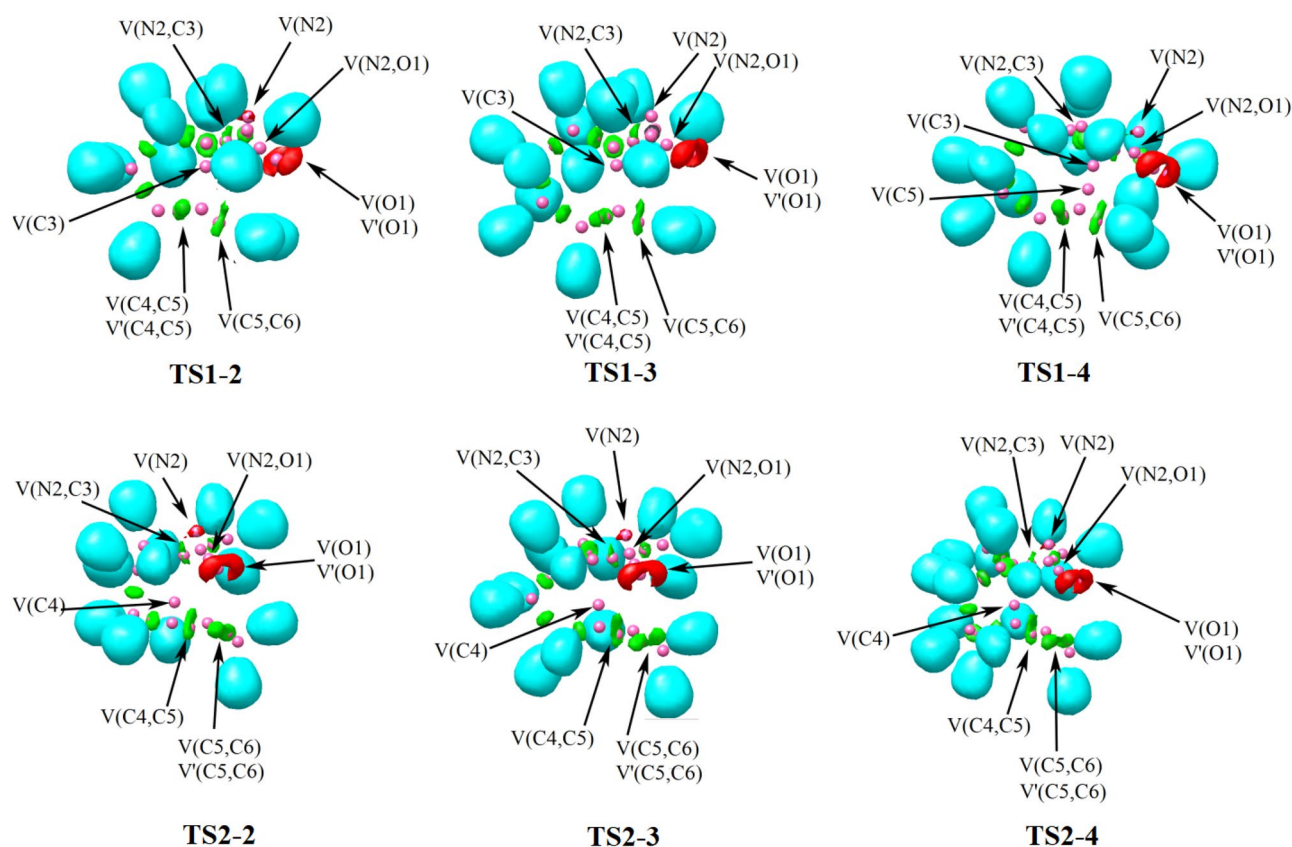


Fig. 6 MPWB1K/6-311G(d,p) ELF localization domains of the TSs associated with the IM32CA reactions of nitrones **11**, **12** and **13** (protonated basins are shown in blue, monosynaptic basins in red, disynaptic basins in green and the core basins in black colour (isovalue = 0.85))

deriving electron density from the C4-C5 bonding region, while no such change in electronic structure is observed in **TS1-2** and **TS1-3**. On the other hand, **TS2-2**, **TS2-3** and **TS2-4** show the presence of V(C4) monosynaptic basin integrating 0.45 e, 0.37 e and 0.38 e respectively associated with the formation of *pseudoradical* centre at C4 carbon, the electron density of which comes from the depopulation of the C4-C5 bonding region along the reaction path. Note that the addition along the C5-C6 and C4-C5 bonds

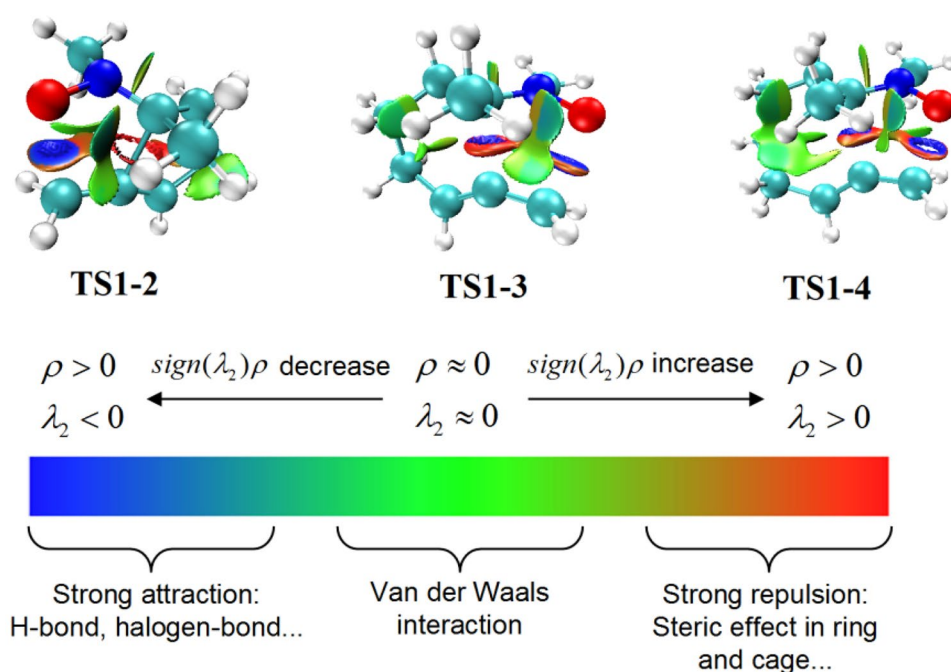
of the allenic nitrones show varied pattern of changes in electron density and accordingly follow different molecular mechanism. Finally, the absence of disynaptic basins associated with the formation of new covalent bonds reveal early nature of these TSs in each case in which the new covalent bonds have not been started.

The topological analysis of the AIM was performed to characterize the interatomic interactions at the TSs. The AIM parameters, namely the total electron density ρ and

Table 5 Total electron density, ρ (a.u.), Laplacian of electron density $\nabla^2\rho(r_c)$ (a.u.) of **BCP1** and **BCP2** at the TSs associated with the IM32CA reactions in gas phase and in ethanol

	Gas phase				Ethanol			
	BCP1 (C–C)		BCP2 (C–O)		BCP1 (C–C)		BCP2 (C–O)	
	ρ	$\nabla^2\rho(r_c)$	ρ	$\nabla^2\rho(r_c)$	ρ	$\nabla^2\rho(r_c)$	ρ	$\nabla^2\rho(r_c)$
TS-12	0.082	0.025	0.048	0.104	0.086	0.019	0.047	0.102
TS-22	0.058	0.062	0.088	0.141	0.060	0.059	0.089	0.140
TS-13	0.064	0.037	0.052	0.117	0.068	0.033	0.050	0.112
TS-23	0.053	0.042	0.074	0.140	0.056	0.039	0.073	0.138
TS-14	0.053	0.042	0.060	0.130	0.057	0.039	0.058	0.126
TS-24	0.055	0.043	0.064	0.132	0.059	0.041	0.063	0.130

Fig. 7 NCI isosurfaces (isovalue = 0.5), in the range $-0.04 < \text{sign}(\lambda_2)\rho < 0.04$ a.u., of **TS1-2**, **TS1-3** and **TS1-4**



the Laplacian of electron density $\nabla^2\rho(r_c)$, at the bond critical points **BCP1** and **BCP2** associated respectively with the forming C–C and C–O bonds are given in Table 5. The total electron density ρ less than 0.1 au and the positive Laplacian of electron density indicate non-covalent interactions in each case, consistent with the ELF topological analysis and the forming bond distances greater than 2.0 Å. The NCI isosurfaces at **TS1-2**, **TS1-3** and **TS1-4** represented in Fig. 7 show green isosurfaces at the interatomic regions, indicative of weak non-covalent interactions.

Conclusion

The *zw*- type intramolecular 32CA reactions of allenic nitrones **11**, **12** and **13** experimentally reported by Lebel and Banucci [10] have been studied within MEDT at the MPWB1K/6-311G(d,p) computational level. The topological analysis of the ELF of the nitrones **11**, **12** and **13** allows establishing their zwitter-ionic structure. Analysis of the global reactivity indices defined within CDFT classifies the nitrones as strong nucleophiles and marginal electrophiles. These IM32CA reactions follow non-concerted one-step mechanism with asynchronous TSs. In the allenic nitrone **11**, the nitrone and allenic frameworks are separated by two methylene groups and the addition is energetically preferred along the C5-C6 double bond, while for the allenic nitrone **13**, in which the nitrone and allenic frameworks are separated by four methylene groups, the addition takes place exclusively along the C4-C5 double bond of the allene. This study allows understanding the cyclization selectivity

in intramolecular 32CA reactions of allenic nitrones. The molecular mechanism revealed from the bonding evolution theory predicts varied changes in the electron density along the reaction paths associated with the IM32CA reactions of the nitrones **11** and **13**. However, in each case, the early TSs are located in which the formation of new C–C and C–O covalent bonds have not been started.

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Author contribution All authors contributed to the study conception and design. Data collection and analysis were performed by Barsali Banerjee under the supervision of Nivedita Acharjee. The draft of the manuscript was written and subsequently reviewed by Barsali Banerjee, Nivedita Acharjee and Debnath Palit. All authors read, reviewed and approved the final manuscript.

Data availability All datasets generated during and/or analyzed during the current study are available from the corresponding author on reasonable request.

Code availability Not applicable.

Declarations

Conflict of interest The authors declare no competing interests.

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