ORIGINAL RESEARCH

Evaluating the hydrogen chemisorption and physisorption energies for nitrogen-containing single-walled carbon nanotubes with different chiralities: a density functional theory study

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Received: 7 October 2013 / Accepted: 21 November 2013 / Published online: 5 December 2013 - Springer Science+Business Media New York 2013

Abstract The hydrogen adsorption energies for nitrogencontaining carbon nanotubes (N-CNTs) and for bare carbon nanotubes were calculated using the density functional theory methods at the B3LYP/6–31-G(d) level, including dispersion force corrections. The N-CNTs were finite saturated and non-saturated single-walled carbon nanotubes that contained one or more pyrimidine units, the relative positions of which defined the different configurations of the nanotube. The chemisorption of atomic hydrogen to a full exocyclic monolayer of *zigzag*, *armchair*, and *chiral* N-CNTs was studied as a function of the structural parameters. Zigzag N-CNTs of any configuration, with a larger number of nitrogen atoms, a small diameter and a small length, are more reactive compared to chiral and armchair N-CNTs. The presence of nitrogen in the carbon nanotubes enhances their reactivity to chemisorb atomic hydrogen, showing exothermic energy values. In contrast,

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J. Alvarez e-mail: jose.alvarez@usach.cl the physisorption of molecular hydrogen was endothermic for most of the studied saturated N-CNTs, even when including corrections for van der Waals interactions. The endothermicity was greatest for *zigzag* nanotubes, then decreased for chiral nanotubes and decreased again for armchair nanotubes. In general, the endothermicity decreased for longer nanotubes, which have larger diameters, and a small number of nitrogen atoms. The results of this study suggest that, with saturated bare carbon nanotubes, saturated, and unsaturated N-CNTs could potentially have a higher capacity as hydrogen-storage media than the corresponding unsaturated carbon nanotubes.

Keywords Hydrogen chemisorption energies - Physisorption · Nitrogen-doped nanotubes · Chirality - Saturated nanotubes - Dispersion forces

Introduction

Carbon nanotubes likely represent one of the most versatile structures of our time, and recent research has been conducted to find new applications for these promising compounds $[1-4]$. One application is hydrogen storage $[5, 6]$ $[5, 6]$ $[5, 6]$ $[5, 6]$, which is necessary to safely use hydrogen, for example, as a renewable source of clean energy. A material is expected to fulfill the requirement proposed by the US Department of Energy, that is, a gravimetric target of 5.5 wt% by 2015 [\[7](#page-10-0)], to be suitable as a hydrogen-storage medium.

Carbon nanotubes have been extensively investigated as hydrogen uptake media, with reported values between 0.2 and 10 wt% [[8–10\]](#page-10-0). Many theoretical and experimental critical analyses have been published considering molecular and atomic hydrogen adsorption $[6, 11-17]$ $[6, 11-17]$ $[6, 11-17]$. The general

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consensus is that bare carbon nanotubes, as such, are not a promising hydrogen-storage media.

An important point to consider for hydrogen adsorption is the presence of heteroatoms, with the goal of modifying the electronic density of the nanotube surface. For example, it is known that carbon nanotubes with a small nitrogen content have increased conductivity [[18,](#page-10-0) [19](#page-10-0)]. The presence of nitrogen in the carbon nanotubes decreases their toxicity [\[20](#page-10-0)] and adds a number of useful properties [\[21–23](#page-10-0)], possibly from the induced charge that forms in the vicinity of the nitrogen. With respect to the synthesis of nitrogendoped carbon nanotubes, chemical vapor deposition with pyridine as the nitrogen source and acetylene as the carbon source can be selectively performed with either sp^2 or sp^3 nitrogen atoms and with different nitrogen levels [\[24–27](#page-10-0)].

Research on the interaction of N-CNTs with atomic and molecular hydrogen using density functional theory (DFT) $[28-30]$ and molecular dynamics $[30, 31]$ $[30, 31]$ $[30, 31]$ $[30, 31]$ has arrived at contradictory results because the comparisons of these methods were conducted in completely different systems. For example, the physisorption of one molecule of hydrogen on the external surface of zigzag and armchair N-CNTs exhibits a hydrogen molecular adsorption energy that is significantly smaller for a pristine carbon nanotube [\[29](#page-10-0)] using DFT. The same unfavorable situation is found when evaluating the chemisorption of one atom of hydrogen on the external surface of the N-CNTs compared with the pristine nanotube [[29\]](#page-10-0). However, the opposite results are found when calculating the hydrogen physisorption energy for N-decorated nanotubes (as opposed to N-substituted nanotubes) using DFT and molecular dynamics, resulting in a calculated adsorption energy of -80 meV [\[30](#page-10-0)]. This energy level indicates a potentially high hydrogen-storage capacity. Alternatively, studies of molecular hydrogen dissociative adsorption using density functional methods indicate a reduced barrier when an (8,0) carbon nanotube is doped with nitrogen [[28\]](#page-10-0). Studies using DFT to evaluate the hydrogen chemisorption energy of N-CNTs with a high nitrogen content at 100 % hydrogen coverage suggest that saturated N-CNTs are stable and that N-CNTs could be used as effective media for the storage of hydrogen [\[32](#page-11-0)]. However, there are no systematic studies concerning the effect of the structural parameters on the hydrogen-storage capacity of these nitrogenated carbon nanotubes. Hydrogen physisorption has not yet been reported for saturated N-CNTs.

In this work, we theoretically investigated both the relative reactivity of N-CNTs against atomic hydrogen chemisorption and the relative reactivity of saturated N-CNTs against molecular hydrogen physisorption to evaluate how structural parameters cooperate with the goal of optimizing the hydrogen-storage capacity of these N-CNTs.

Methods

For all simulations, finite open nanotubes were used, and the dangling bonds at the edges were saturated with hydrogen. The N-CNT structures were built using Hamada indices with HyperTube [[33\]](#page-11-0), a specific algorithm implemented as a script embedded in HyperChem [\[34](#page-11-0)]. Saturated and non-saturated carbon nanotubes were created by choosing the appropriate option in the HyperTube interface. Nitrogen atoms were added by replacing either a C atom (for non-saturated structures) or a CH unit (for saturated tubes) so that after two substitutions (following the pattern –N1–C2–N3–C4–C5–C6–), a pyrimidine-like ring was formed. The next two substitutions, forming a second pyrimidine ring, were located in the opposite position of the same carbon layer. Different configurations were characterized according to the rotation angle between opposite pyrimidine rings to yield S , O , M , and P configurations for rotation angles (θ) of 0° , 60° , 120° , and 180° , respectively. (The O, M , and P names were chosen related to the ortho, meta, and para positions of disubstituted benzene rings, with the pyrimidine carbon atom C2 as a reference, as shown in Fig. [1\)](#page-2-0). All of the structures were first optimized with AM1 (Austin Model 1, semi empirical, as installed in HyperChem) and were then further optimized using the DFT method with Jaguar v7.8 [[35\]](#page-11-0) at the B3LYP/6–31G(d) theoretical level [\[36](#page-11-0), [37\]](#page-11-0). DFT calculations have been commonly used for studying nanotube structures [\[12](#page-10-0), [13,](#page-10-0) [32,](#page-11-0) [38–40](#page-11-0)]. They have also been widely used for the study of non-covalent stacking [\[41](#page-11-0)], producing good results for the structure and the relative energies for different isomer conformations (even without considering the typical DFT underestimation) [\[42](#page-11-0)]. DFT calculations have also been used to explain conductivities for wideband-gap semiconductors and oxides [\[43](#page-11-0)]. To accurately account for the van der Waals (vdW) interactions, selfconsistent field (SCF) energies of fully exo-hydrogenated N-CNTs and their corresponding inside-hydrogen physisorption systems were corrected for dispersion forces using the DFT-D3 method developed by Grimme et al. [\[44](#page-11-0)] and implemented in the electronic structure program ORCA 2.9 for the B3LYP functional [[45\]](#page-11-0) (B3LYP-D3 functional). Some of the N-CNTs-hydrogen molecules systems were randomly chosen to perform a dispersion force correction for the SCF energies using the DFT-non-local method [[46,](#page-11-0) [47](#page-11-0)] (a more expensive method than DFT-D3 because the DFT-non-local method needs the converged electron density to compute the dispersion energy of the non-local term), with results that differ very little from the DFT-D3 correction [vdW term in expression (2) (2) ; see Table [1\]](#page-2-0), thus validating the calculation method and the use of the corrected B3LYP energies. The evaluation of the participation weight of the hydrogen molecules' interaction alone over

the total vdW correction resulted in a low value of approximately 6 kcal/mol for an 8-carbon layer zigzag (8,0) N-CNT with four nitrogen atoms and nine interior hydrogen molecules. For the verification and characterization of energy minima, harmonic vibrational frequency calculations for optimized geometries at the same level of DFT were performed and they all resulted in real values. No symmetry constraints were applied.

The hydrogen chemisorption energy, Er, was calculated as follows:

$$
Er = E_{N-CNT(ch)} - E_{N-CNT} - nE_H,
$$
\n(1)

where $E_{N-CNT(ch)}$ and E_{N-CNT} are the total energies for N-CNT with and without the chemisorbed hydrogen, respectively; n is the number of chemisorbed hydrogen atoms; and E_H is the hydrogen atom energy. Full coverage exo-hydrogenation of a hydrogen monolayer was considered. A negative value of Er indicates that hydrogen chemisorption is a favorable process, that is, the corresponding nanotube shows a good reactivity for chemisorbing hydrogen and that the fully saturated nanotube is stable.

Hydrogen physisorption energy, Eph, was calculated according to expression (2) as follows:

$$
Eph = (E(ch+ph)-E(ch)) - hEH2 + vdW,
$$
\n(2)

where $E_{(ch + ph)}$ and $E_{(ch)}$ are the total energies for the saturated N-CNTs with and without physisorbed molecular hydrogen, respectively; h is the number of physisorbed hydrogen molecules; $E_{H₂}$ is the total energy of a hydrogen molecule, all of which are calculated at the same level of DFT; and, vdW corresponds to the contribution of dispersion energy from van der Waals interactions among hydrogen molecules and nanotube systems, as calculated by the DFT-D3 method. A positive value of Eph indicates that the hydrogen physisorption process is endothermic.

The notation used in this work is the following. First, the type of nanotube is specified according to the chirality

Table 1 Differences between the values of the vdW term of expression (2) calculated by the DFT-D3 and the DFT-nonlocal methods $[\Delta \text{vdW}(d\text{ftd}3-n)]$ employed in the evaluation of the hydrogen physisorption energy for some N-CNTs

Type	Number of H_2 molecules	AvdW $(dftd3-nl)$ (Ha)	AvdW $(dftd3-nl)$ (eV)
$(4,4)$ P-4N-H	2	-0.0005	-0.014
$(4,4)P-4N-H$	4	-0.0007	-0.019
$(4,4)P-4N-H$	5	-0.0010	-0.026
$(4,4)P-4N-H$	8	0.0023	0.063
$(4,0)M-4N-H$	\mathfrak{D}	-0.0093	-0.253
$(8,0)$ S-8N-H	2	-0.0002	-0.007
$(8,0)$ S-8N-H	3	-0.0003	-0.007
$(8,0)$ S-8N-H	7	-0.0018	-0.048

indices (n, m) . Second, the configuration according to the rotation angle between opposite pyrimidine groups is indicated by the corresponding symbol $(S, O, M, \text{or } P)$. Third, the number of nitrogen atoms present in the nanotube (4N, 8N, etc.) is indicated by a hyphen. When necessary, a character H separated by a hyphen is added to indicate that a saturated nanotube is present. Finally, the number of carbon layers (cl) added, when needed, is indicated by 8cl, 12cl, 16cl, and so on. For example, a chiral carbon nanotube with a P configuration having 4 nitrogen atoms that is fully exo-hydrogenated is denoted as (6,3)P-4N–H. If the nanotube contained five hydrogen molecules physisorbed inside, then, instead of the final H, the characters $5H_2$ are added, and the compound is written as $(6,3)P-4N-5H_2$.

Results and discussion

Fig. 1 Examples of the S , O , M and P configurations of the N-CNTs are shown in (a), (b), (c), and (d), respectively, where the disposition of the C2 carbon atom for the posterior pyrimidine ring is obtained after a rotation of 0° , 60° , 120° , and 180 $^{\circ}$. N atom *blue*, C atom *gray*, H atom white (Color figure online)

Hydrogen adsorption is a process that takes place through the interaction of the hydrogen atom and the adsorbent material to form covalent bonds (chemisorption) or the

interaction of molecular hydrogen and the adsorbent material to form non-covalent bonds (physisorption). In this section, we present the results for both hydrogen atom chemisorption energies and hydrogen molecule physisorption energies for N-CNTs as well as the effects on the energy values of structural parameters, such as the diameter, length, chirality, configuration, and the number of nitrogen atoms in the nanotubes. In the first part of the section, the hydrogen chemisorption energy results for bare carbon nanotubes and for N-CNTs are presented to characterize the effect of each of the named parameters, although most of the parameters are interrelated. At the end of the section, the results for hydrogen physisorption energies are presented.

Hydrogen chemisorption energy

Chemisorption energy, Er, measures the energy involved in the adsorption of hydrogen atoms to the $sp²$ C atoms to form covalent C–H bonds. In that process, the hybridization of the nanotube C atoms is changed from sp^2 to sp^3 . The C–N bond lengths exhibited for the C2 atom that were in the range of $1.37-1.42$ Å for the N-CNTs (Fig. 2; in agreement with the 1.42 \AA reported for the average C–N bond length for nitrogen-doped armchair carbon nanotubes [[48\]](#page-11-0)) were changed to be in the range of $1.45-1.48$ Å for the saturated N-CNTs. An exothermic Er value [see expression ([1\)](#page-2-0)] indicates that energy is released during hydrogen chemisorption. The value of Er measures how easily such a reaction occurs and the stability of the product of the reaction. In general, an exothermic Er indicates that the formation of the saturated nanotube is a favorable process. A larger exothermic value indicates that the corresponding non-saturated nanotube is a good hydrogen adsorbent.

In this work, a single layer of 100 % hydrogen external coverage (which is energetically more favorable [\[49](#page-11-0)] than internal hydrogenation) was considered for chemisorption. Larger nanotubes will adsorb a greater number of hydrogen atoms. To make them comparable, a value of Er/H was used to represent the energy associated with the chemisorption per hydrogen atom for the analyzed nanotube.

Nanotube diameter effect

The diameter has been reported as a parameter that strongly affects the hydrogen adsorption energy of carbon nanotubes [\[12](#page-10-0), [13,](#page-10-0) [50–52](#page-11-0)]. The hydrogen chemisorption energy generally decreases as the nanotube diameter decreases, such that small-diameter carbon nanotubes are more reactive to chemisorb hydrogen than those with larger diameters. This phenomenon can be understood in terms of the higher curvature of the small-diameter nanotubes. The calculations in this study for bare carbon nanotubes at 100 % coverage show the same trend, with endothermic values for the nanotubes with diameters larger than 7.0 \AA , such as $(5,5)$, $(6,6)$, and $(6,4)$ nanotubes, and exothermic values for nanotubes with diameters smaller than 6.5 Å , as shown in Fig. [3](#page-4-0) (for 0 nitrogen atoms). All of the nanotubes tested for the data presented in Fig. [3](#page-4-0) have an S configuration and are listed in order of increasing diameter, from 3.7 to 9.2 Å. For example, for a $(6,6)$ armchair carbon nanotube with a diameter of 8.2 \AA , the Er/ H value is 0.122 eV, and for a (3,3) carbon nanotube with a diameter of 4.3 \AA , the Er/H value is -0.957 eV. The same reactivity trend was reported previously with an unfavorable endothermic chemisorption energy value of 0.965 eV for a (6,6) armchair carbon nanotube at full exo-hydrogenation using gradient-corrected DFT [\[11](#page-10-0)]. Our results

Fig. 2 Bond lengths obtained for one of the pyrimidine rings of an optimized (5,5)S-4N nanotube at the B3LYP/6–31G(d) level

indicate the same hydrogen chemisorption energy trend for armchair, chiral, and zigzag carbon nanotubes, with greater exothermic values observed for nanotubes with smaller diameters. Different results have been reported for the chemisorption of one H atom on the sidewall of the nanotube. Even though armchair carbon nanotubes present the same trend, with values of Er/H (calculated at the B3LYP/6–31G(d) level of DFT) from -53.5 to -38.8 kcal/mol $(-2.32$ to -1.68 eV) for $(3,3)$ and $(6,6)$ nanotubes of nine carbon layers, respectively, [[12\]](#page-10-0), zigzag carbon nanotubes show a different trend, with values of -85 kcal/mol (-3.7 eV) and -95 kcal/mol (-4.1 eV) for $(5,0)$ and $(9,0)$ nanotubes, respectively $[51]$ $[51]$.

The Er/H for N-CNTs also depends on the diameter, with exothermic values observed for all of the nanotubes studied. The smaller-diameter N-CNTs are the most reactive to atomic hydrogen chemisorption. The results presented in Fig. 3 indicate that this trend is valid for armchair, chiral, and zigzag N-CNTs. For example, the Er/H values, for $(4,0)$, $(6,0)$, and $(8,0)$ zigzag N-CNTs with four nitrogen atoms that have diameters of 3.7, 5.5, and 7.5 Å, are -0.96 , -0.5 , and -0.4 eV, respectively. The results show that a global diameter effect on atomic hydrogen chemisorption energies remains the same, regardless of either the nanotube chirality or the presence of nitrogen. An Er/H value of -1.34 eV for N-CNTs with smaller diameters (\sim 3 Å), calculated at the same level of DFT [\[32](#page-11-0)], confirms the observed trend described above.

Effect of the number of nitrogen atoms in the nanotube

The results of this study indicate that, in general, the Er/H decreases (i.e., it is more favorable) when the carbon nanotube contains nitrogen, presenting smaller values as the number of nitrogen atoms in the N-CNTs increases (the

Fig. 3 Hydrogen chemisorption energy per chemisorbed hydrogen atom calculated at the B3LYP/6–31G(d) level versus the number of nitrogen atoms in the corresponding zigzag, chiral, and armchair carbon nanotube represented in green, red and blue, respectively, with symbols that indicate a decreasing diameter order: *triangle* $>$ *diamond* $> square > circle$ (Color figure online)

Er/H decreases by approximately 0.03 eV for each nitrogen atom added to the structure), with the exception of those nanotubes that have the smallest diameters (3.7 Å) , which also have the most exothermic Er/H values (-0.98 eV) and are almost insensitive to the presence of nitrogen (see Fig. 3).

N-CNT configuration effect

In Fig. 4, the hydrogen chemisorption energy results for *zigzag* N-CNTs with diameters greater than 3.7 Å and containing four and eight nitrogen atoms are presented. These results exhibit no strong dependence on the configuration of S, O, M, or P (different rotation angles). For $(6,0)$ and (4,0) N-CNTs with four nitrogen atoms, Er/H is -0.56 and -0.97 eV, respectively, for any configuration. For (8,0) N-CNTs that have four and eight nitrogen atoms, Er/ H is approximately -0.37 and -0.5 eV, respectively, regardless of configuration. The data in Fig. 4 also confirm that hydrogen chemisorption is an energetically more favorable process when the N-CNT diameter decreases and when the number of nitrogen atoms in the N-CNT increases, consistent with the reported DFT calculations for *zigzag* N-CNTs with diameters of \sim 3 Å and a nitrogen content $>30 \%$ [[32\]](#page-11-0).

N-CNT chirality effect

A chirality effect on the hydrogen chemisorption energies for N-CNTs was illustrated by the data. Zigzag N-CNTs exhibit the most exothermic Er/H values and are, therefore, the most reactive to hydrogen chemisorption, as shown in Fig. 3. For example, the Er/H values for the (6,0), (6,2), and (4,4) nanotubes with four nitrogen atoms (and a diameter of 5.5 Å) are -0.5 , -0.38 , and -0.32 eV, respectively. The same trend is found for the larger

Fig. 4 Hydrogen chemisorption energies per hydrogen atom at the B3LYP/6–31G(d) level for zigzag N-CNTs with four and eight nitrogen atoms versus the rotation angle that represents the different configurations (i.e., 0° , 60° , 120° , and 180° represent S, O, M, and P configurations, respectively)

diameter N-CNTs, that is, the Er/H values for (8,0), (6,3), and (5,5) N-CNTs with four nitrogen atoms (and a diameter of \sim 7.5 Å) are -0.4, -0.23, and -0.16 eV, respectively. Therefore, the predicted order of the reactivity of N-CNTs for hydrogen chemisorption is $zigzag > chiral > armchair$. The same chirality effect was also observed for bare carbon nanotubes, as shown in Fig. [3.](#page-4-0)

N-CNT length effect

The N-CNT length depends on the number of carbon layers constituting the nanotube. However, for N-CNTs with the same number of carbon layers, the same number of nitrogen atoms and a similar diameter, their lengths depend upon nanotube chirality. For example, the (8,0), (6,3), and $(5,5)$ N-CNTs with molecular formulae $C_{60}N_4H_{16}$, $C_{78}N_4H_{20}$, and $C_{76}N_4H_{20}$, respectively, all of which have eight carbon layers, four nitrogen atoms and 7.5 Å diameters [structures $(a-c)$ in Fig. 5], have 7.1, 7.4, and 8.5 \AA lengths, respectively (measured from C to C). When these nanotubes are completely saturated [structures (d–f) in Fig. 5], their lengths are 6.9, 7.2, and 8.8 Å, respectively. Maintaining most of the N-CNT characteristics constant, it appears that the N-CNT length increases in the order of $zigzag < chiral < armchair$. Interestingly, this order is the inverse of the N-CNT reactivity to hydrogen chemisorption, as was established above.

In Fig. [6](#page-6-0), the hydrogen chemisorption energies for armchair N-CNTs that only differ in their lengths [(4,4)S-8cl with an 8.5 \AA length and $(4,4)S-12c$ l with a 13.3 \AA length] as a function of the number of nitrogen atoms are compared. The data show that the number of nitrogen atoms has a significant effect on the exothermicity of the hydrogen chemisorption reaction for armchair N-CNTs and that the effect is more pronounced for shorter nanotubes. Er/H decreases as the number of nitrogen atoms increases from 0 to 8; the exothermicity is nearly 0.15 eV higher for the N-CNTs, which are approximately 5 Å shorter (8 carbon layer vs 12 carbon layers). This difference is better appreciated in N-CNTs with a higher number of nitrogen atoms. That is, the shorter N-CNTs appear to be more favorable for full hydrogen chemisorption than the longer ones, regardless of the number of nitrogen atoms contained in the nanotube. This trend coincides with the reported results computed at the B3LYP/6–31G(d) level for the chemisorption of one hydrogen atom on the sidewalls of $(4,4)$ single-walled carbon nanotubes $[12]$ $[12]$ $[12]$. The tendency for shorter N-CNTs to be more favorable for chemisorption could explain in part why the zigzag N-CNTs are the most reactive. A further confirmation of the greater reactivity of zigzag N-CNTs compared with the other chiralities is shown in Fig. 6 for $(6,0)S-12cl$ N-CNTs (which have the same configuration and the same number of carbon layers as well as the similar diameters as the (4,4)S-12cl

Fig. 6 Variation of the chemisorption energies per adsorbed H atom at the B3LYP/6–31G(d) level for (4,4) armchair N-CNTs of different lengths and for $(6,0)$ *zigzag* N-CNTs versus the number of nitrogen atoms

nanotubes), which show nearly 0.25 eV higher exothermicity than the (4,4)S-12cl N-CNTs. Therefore, chirality appears to affect hydrogen chemisorption energies for N-CNTs more than length does.

Hydrogen physisorption energy

In the case of physisorption, a non-covalent interaction between the nanotube and the molecular hydrogen inside the nanostructure occurs. The energy involved in the physisorption of molecular hydrogen inside the nanotube, Eph, is calculated using equation [\(2](#page-2-0)), which incorporates a correction for dispersion forces, as explained above. The energy associated with the physisorption of a single hydrogen molecule is called Eph/H2. Hydrogen physisorption is performed over fully saturated N-CNTs (i.e., N-CNTs that have been submitted to exo-hydrogenation at 100 % coverage) without involving any change of the hybridization of the nanotube C atoms. All of the calculated values of the hydrogen physisorption energies for N-CNTs are endothermic (except for the small-diameter (4,4) armchair nanostructures containing one or two hydrogen molecules). A high value of $Eph/H₂$ indicates that hydrogen physisorption requires more energy and that the resulting (nanotube- H_2) system is less stable. A good hydrogen-storing material should be able to release hydrogen in a controlled manner, without requiring much added energy. For this reason, such a material should have an exothermic Eph/H_2 that is not far from 0 eV. An ideal range for the hydrogen binding energy to carbon nanotubes that allows for reversible hydrogen storage at ambient conditions has been reported as $0.1-0.5$ eV/H₂ [[6](#page-10-0), [53](#page-11-0)]. Several thermodynamic estimations of the binding energy of H2 molecules for reversible storage are almost in the same range, that is, $0.16-0.4$ eV/molecule $[54-56]$.

In Table [2,](#page-7-0) a comparative summary of the hydrogen chemisorption energies and the hydrogen physisorption energies for a number of different systems that were studied, with the corresponding diameters and vdW corrections, are presented including the total hydrogen content. As the data in Table [2](#page-7-0) illustrates, non-covalent interactions contribute significantly to the hydrogen physisorption energies. The B3LYP-D3 method used in this work was recently found to be one of the most accurate methods available for treating intermolecular interactions when tested on several databases of non-covalently interacting dimers with the C-DCP, which is a new dispersioncorrecting potential developed by DiLabio et al. [\[57](#page-11-0)] for the modeling of C–C bond-making/bond-breaking chemistry.

The data in Table [2](#page-7-0) show a significant difference in physisorption energies between the small-diameter (4,0) and the larger-diameter (8,0) N-CNTs. The physisorption endothermicity is substantially higher in the (4,0) N-CNTs compared with the $(8,0)$ structures. In the case of the $(8,0)$ N-CNTs, a marked deviation in the physisorption endothermicity was observed in the S configuration (rotation angle equal to zero) compared with the rest of the configurations. However, the smaller-diameter (4,0) N-CNTs do not follow the same trend as the larger-diameter nanotubes, and the deviations in the physisorption endothermicities in this case are less significant between configurations. The effect of configuration is more evident when comparing the Eph/H₂ values for $(8,0)$ N-CNTs when different numbers of H_2 molecules are absorbed. For the O and P configurations, the endothermicity of hydrogen physisorption increases as the number of physisorbed hydrogen molecules increases, which is the opposite of the situation for the S configuration. This finding can be attributed to the different polarization of the nanotube structure from the effect caused by the disposition of the nitrogen atoms in the structure, which in turn affects the electrostatic interactions between hydrogen and the nanotube.

The number of nitrogen atoms has a uniform influence on the hydrogen physisorption energy of the smallerdiameter (4,0) zigzag N-CNTs, with smaller values of endothermicity for nanotubes with a smaller number of nitrogen atoms (i.e., the $(4,0)$ -4N-3H₂ nanotube compared with the $(4,0)$ -8N–3H₂ nanotube in Table [2\)](#page-7-0). In contrast, the number of physisorbed hydrogen molecules inside the nanotube primarily influences the larger-diameter (8,0) N-CNTs.

Data in Fig. [7](#page-8-0) indicate that the nanotube configuration does not significantly affect the hydrogen physisorption energy for smaller-diameter armchair N-CNTs and is in agreement with the results found for the zigzag N-CNTs. In addition, the data in Fig. [7](#page-8-0) for the (4,4)S-4N–H-12cl nanotubes are within the ideal range mentioned above for hydrogen storage and when compared with shorter (4,4)S-4N–H-8cl nanotubes, indicate that nanotube length has a

Hydrogen physisorption energies (E_{ph}), hydrogen physisorption energies per inside-adsorbed H₂ molecule (E_{ph} /H₂) calculated by DFT-D3 methods at the B3LYP/6–31G(d) level for the mentioned saturated N-CNTs at different inside-number of physisorbed hydrogen molecule. Contribution of dispersion energy from vdW interactions and total hydrogen content for the nanotube-H2 systems

significant effect on the endothermicity of hydrogen physisorption, with smaller endothermic $Eph/H₂$ values for longer N-CNTs. In Fig. [8](#page-9-0) optimized structures of $(4,4)$ S- $4N-8H_2-12c1$ and $(8,0)S-4N-20H_2-12c1$ are presented. These findings seem reasonable because longer nanotubes have more room to allocate the hydrogen molecules inside the tubes and thus repulsion between the hydrogen molecules remains at a low level. This behavior differs from that observed in the case of hydrogen chemisorption energies for N-CNTs of comparable size, where hydrogen remains bonded to the outside of the nanotube and many hybridization changes take place.

In Table [2](#page-7-0), the hydrogen physisorption energy results for $(5,5)$, $(6,3)$, and $(8,0)$ N-CNTs with the same characteristics (i.e., S configuration, four nitrogen atoms, 7.5 A diameter, and eight carbon layers), except for topological chirality, are compared. These results show that chirality has a strong effect on physisorption endothermicity. For three physisorbed H_2 molecules or more, the *armchair* N-CNTs exhibit $Eph/H₂$ values within the ideal range for a reversible hydrogen-storage medium [\[6](#page-10-0), [53](#page-11-0), [55](#page-11-0), [56](#page-11-0)]. For all of the configurations, it is observed that endothermicity increases in the order of *armchair* \langle *chiral* \langle *zigzag* and also increases when the number of physisorbed H_2

Fig. 7 Variation of the physisorption energies per adsorbed H_2 calculated by DFT-D3 methods at the B3LYP/6–31G(d) level for saturated (4,4) armchair N-CNTs of different configurations and different lengths, as a function of the number of adsorbed H_2 molecules

molecules increases. The polarizability of armchair N-CNTs on one hand and the repulsion between H_2 molecules on the other hand could explain this behavior. These findings for N-CNTs are in excellent agreement with the DFT calculations for $(5,5)$, $(6,4)$, and $(8,2)$ carbon nanotubes that employed the local density approximation [\[14](#page-10-0)].

Fig. 8 N-CNT structures optimized at the B3LYP/6–31G(d) level for (a) $(4,4)$ S-4N-8H₂-12cl and (b) $(8,0)$ S-4N-20H₂-12cl (nanotubes had both stoichiometry $C_{124}N_4H_{140}$ before the hydrogen physisorption process took place). Lateral and front views are presented. N atom blue, C atom gray, H atom white (Color figure online)

However, for one or two physisorbed H_2 molecules, the N-CNTs show a completely different behavior. Armchair and zigzag N-CNTs exhibit Eph/H_2 values for one physisorbed H_2 molecule that are much more endothermic than for the rest of the cases. This result is not unusual and has been observed for hydrogen chemisorption energies calculated at the B3LYP/6–31G(d) level for (5,5) armchair carbon nanotubes with 9 and 15 carbon layers [\[12](#page-10-0)]. Chiral N-CNTs exhibit a more conservative variation of the Eph/ H2 values for the entire range of physisorbed molecular hydrogen. A different situation has been reported for the hydrogen physisorption energy of a single hydrogen molecule on the outer surface of carbon nanotubes where no chirality effect was detected using DFT calculations [\[52](#page-11-0)].

Therefore, the best energy values for the inside-hydrogen physisorption of saturated N-CNTs are exhibited by longer *armchair* N-CNTs with larger diameters and a small number of nitrogen atoms. Bare saturated carbon nanotubes have better hydrogen physisorption energy values than saturated N-CNTs. Furthermore, the wt% total content of hydrogen for saturated carbon nanotubes decreases with nitrogen substitution (see Table [2\)](#page-7-0). For example, a saturated (5,5) carbon nanostructure with five physisorbed H_2 molecules exhibits Eph/H₂ = -0.068 eV and 10.3 wt% hydrogen for a bare carbon nanotube, but changes to Eph/ $H_2 = 0.337$ eV and 9.9 wt% hydrogen for N-CNTs with four nitrogen atoms (both structures have the same configuration and length).

Conclusions

The reactivity of the finite N-CNTs of different chiralities for the adsorption of hydrogen was investigated using the DFT and DFT-D3 methodology at the B3LYP/ 6–31G(d) level. Smaller diameter carbon nanotubes with or without the presence of nitrogen are more reactive for chemisorbing atomic hydrogen, regardless of chirality. The presence of nitrogen enhances this trend and, accordingly, the Er/H decreases by approximately 0.03 eV for each nitrogen atom added to the structure, except for the most reactive nanotubes with diameters of 3.7 Å , the reactivity of which is not dependent on nitrogen content. The configuration of the N-CNTs had no significant influence on the N-CNT reactivity. In contrast, the chirality of N-CNTs was found to be an important factor that affects their reactivity to hydrogen chemisorption in the order of zigzag $> chiral > armchair$. The same trend was found for the hydrogen chemisorption of bare carbon nanotubes. The nanotube length was also found to affect the reactivity of N-CNTs, with shorter structures being the most reactive to hydrogen chemisorption.

Therefore, the structures that have higher exothermic values for hydrogen chemisorption energies per hydrogen atom are zigzag N-CNTs, which have more favorable values for nanotubes with smaller diameters and lengths and with an increased number of nitrogen atoms. This finding is in agreement with reported values for even smaller diameter N-CNTs [\[32](#page-11-0)].

In contrast, hydrogen physisorption energies for N-CNTs exhibit endothermic values for most of the studied N-CNTs, with nanotubes of larger diameters having lower endothermic values of $Eph/H₂$. The vdW correction term represented an important contribution to the hydrogen physisorption energies. In addition, the diameter has a significant effect on hydrogen physisorption energies. For example, the N-CNTs with diameters of less than 4 Å showed no dependence on the configuration of the N-CNTs, the number of nitrogen atoms, or the number of physisorbed H_2 molecules. The hydrogen physisorption energies for larger-diameter N-CNTs are

less endothermic and depend on the length, the number of nitrogen atoms, the nanotube configuration and the number of physisorbed H2 molecules inside the N-CNTs, with more favorable values for longer N-CNTs that have a smaller number of nitrogen atoms and a reduced number of physisorbed H_2 molecules. For three or more physisorbed H_2 molecules, the endothermicity of the hydrogen physisorption for saturated N-CNTs decreases in the chirality order of $zigzag > chiral > armchair$. Therefore, for saturated N-CNTs, the longer armchair nanotubes with large diameters and a small number of nitrogen atoms are the most reactive to hydrogen physisorption and, according to their energy values, have a high potential capacity as hydrogen-storage media along with the fully saturated bare carbon nanotubes.

Acknowledgments This work was partially supported by the Direction of Scientific and Technological Research DICYT-USACH Project Nr. 061342CF and by the Sociedad de Desarrollo Tecnológico SDT-USACH project Nr. CIA 2981. In addition, the central cluster of the Faculty of Chemistry and Biology and the VRID of the University of Santiago de Chile are acknowledged for allocating computational resources.

Conflict of interest The authors declare that they have no conflict of interest.

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