

Meridional Motion and Reynolds Stress from Debrecen Photoheliographic Data

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Abstract The Debrecen Photoheliographic Data catalogue is a continuation of the Greenwich Photoheliographic Results providing daily positions of sunspots and sunspot groups. We analyse the data for sunspot groups focussing on meridional motions and transfer of angular momentum towards the solar equator. Velocities are calculated with a daily shift method including an automatic iterative process of removing the outliers. Apart from the standard differential rotation profile, we find meridional motion directed towards the zone of solar activity. The difference in measured meridional flow in comparison to Doppler measurements and some other tracer measurements is interpreted as a consequence of different flow patterns inside and outside of active regions. We also find a statistically significant dependence of meridional motion on rotation velocity residuals confirming the transfer of angular momentum towards the equator. Analysis of horizontal Reynolds stress reveals that the transfer of angular momentum is stronger with increasing latitude up to about $40°$, where there is a possible maximum in absolute value.

Keywords Sunspots · Rotation · Velocity fields · Photosphere

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1. Introduction

The Debrecen Photoheliographic Data (DPD) catalogue was started as a continuation of the Greenwich Photographic Results (GPR). Royal Greenwich Observatory ceased its photoheliographic program in 1977 and the International Astronomical Union commissioned Debrecen Observatory, Hungary, to continue the project (Wayman, [1980\)](#page-12-0). The DPD catalogue is also supplemented by solar images from other observatories (for details see Baranyi, Győri, and Ludmány, [2016\)](#page-10-0) to fill in the gaps in the Debrecen observations.

The GPR dataset represents one of the most valuable resources in studying the behaviour of the Sun over long time periods. It comes as no surprise that various portions of the dataset were used in a large number of papers studying solar rotation (Newton and Nunn, [1951;](#page-11-0) Ward, [1965,](#page-12-1) [1966;](#page-12-2) Balthasar and Wöhl, [1980](#page-10-1); Arevalo *et al.*, [1982](#page-10-2); Balthasar, Vázquez, and Wöhl, [1986](#page-10-3); Brajša *et al.*, [2002](#page-10-4), [2004](#page-10-5); Ruždjak *et al.*, [2004,](#page-12-3) [2005\)](#page-12-4). Often the dataset was extended into the future by using observations by the Solar Observing Optical Network of the United States Air Force/National Oceanic and Atmospheric Administration (SOON/USAF/ NOAA) (Pulkkinen and Tuominen, [1998a;](#page-11-1) Javaraiah, [2003;](#page-11-2) Zuccarello and Zappalá, [2003;](#page-12-5) Javaraiah, Bertello, and Ulrich, [2005](#page-11-3); Brajša *et al.*, [2007](#page-10-6); Javaraiah, [2010;](#page-11-4) Sudar *et al.*, [2014\)](#page-12-6). Pulkkinen and Tuominen ([1998a\)](#page-11-1) also extended the analysis into the past by using observations made by Carrington and Spörer. Observations of sunspots from other observatories were also used: *e.g.*, Kanzelhöhe (Lustig, [1983\)](#page-11-5), Mt. Wilson (Gilman and Howard, [1984\)](#page-11-6), Mitaka (Kambry and Nishikawa, [1990\)](#page-11-7), Kodaikanal (Gupta, Sivaraman, and Howard, [1999\)](#page-11-8), and Abastumani (Khutsishvili, Gigolashvili, and Kvernadze, [2002](#page-11-9)).

The transport of angular momentum towards the solar equator, necessary for maintaining the observed solar differential rotation profile, is often attributed to Reynolds stresses which result from mutual dependence between meridional motions and rotation velocity residuals (Rüdiger, [1980;](#page-12-7) Canuto, Minotti, and Schilling, [1994](#page-10-7); Pulkkinen and Tuominen, [1998b](#page-11-10)). Motions of only a few ms^{-1} in both velocity components are sufficient to generate horizontal Reynolds stress of the order of several 10^3 m² s⁻², which is sufficient to maintain the observed solar rotation profile (Schröter, [1985](#page-12-8), and the references therein). Actual observations show the required value of several 10^3 m² s⁻² for horizontal Reynolds stress (Ward, [1965;](#page-12-1) Belvedere *et al.*, [1976;](#page-10-8) Schröter and Wöhl, [1976](#page-12-9); Gilman and Howard, [1984;](#page-11-6) Pulkkinen and Tuominen, [1998b;](#page-11-10) Vršnak *et al.*, [2003](#page-12-10); Sudar *et al.*, [2014\)](#page-12-6). Ward ([1965\)](#page-12-1), Gilman and Howard ([1984\)](#page-11-6), Pulkkinen and Tuominen ([1998b](#page-11-10)), Vršnak *et al.* ([2003\)](#page-12-10), and Sudar *et al.* ([2014\)](#page-12-6) also showed that the absolute value of horizontal Reynolds stress increases with latitude up to about 30◦ where there is a possible maximum.

Velocity components of the Reynolds stress (meridional motions and rotation velocity residuals) are also a subject of investigation. Howard and Labonte ([1980\)](#page-11-11) found a cyclic pattern of alternating faster and slower rotation bands with a period of \approx 11 years. Further confirmation of these torsional oscillations was reported by Ulrich *et al.* ([1988](#page-12-11)), Howe *et al.* ([2000\)](#page-11-12), Haber *et al.* ([2002\)](#page-11-13), and Basu and Antia ([2003\)](#page-10-9). Recently, Sudar *et al.* [\(2014](#page-12-6)) tried to find a similar pattern in sunspot groups velocity data, but were unable to detect such a signal when folding all solar cycles to one phase diagram. Doppler measurements show meridional flow directed towards solar poles on all latitudes (Duvall, [1979](#page-10-10); Howard, [1979;](#page-11-14) Hathaway, [1996](#page-11-15); Zhao and Kosovichev, [2004;](#page-12-12) Kosovichev and Zhao, [2016](#page-11-16)). Most of the time the flow was of the order of 20 m s⁻¹, but episodes of significantly larger flow have also been detected (Hathaway, [1996\)](#page-11-15). Sometimes almost no meridional flow (Lustig and Wöhl, [1990\)](#page-11-17) or even opposite flow (Pérez Garde *et al.*, [1981\)](#page-11-18) was detected in Doppler data. Various tracers, such as sunspots, sunspot groups, small magnetic features, coronal bright points (CBPs) and solar plages, were also used to measure the meridional motion. Sunspots

and sunspot groups were most frequently used and most of the results show flow outward from the centre of the solar activity (Tuominen and Virtanen, [1984](#page-12-13); Howard and Gilman, [1986;](#page-11-19) Howard, [1991a;](#page-11-20) Kambry *et al.*, [1991](#page-11-21); Wöhl and Brajša, [2001](#page-12-14)). Recently, however, Sudar *et al.* [\(2014\)](#page-12-6) reported flow which is almost exactly the opposite. Similar flow to Sudar *et al.* ([2014\)](#page-12-6) was found by Howard [\(1991b\)](#page-11-22) by tracing solar plages. Komm, Howard, and Harvey ([1993\)](#page-11-23) and Snodgrass and Dailey [\(1996](#page-12-15)) used small magnetic features as tracers and found similar, but still in some aspects mutually different, results. Komm, Howard, and Harvey ([1993\)](#page-11-23) found poleward flow at all latitudes with a maximum amplitude of about 10 m s[−]1, while Snodgrass and Dailey [\(1996](#page-12-15)) obtained a flow which is directed out of the centre of solar activity with poleward flow at higher latitudes with similar amplitude to that of Komm, Howard, and Harvey [\(1993](#page-11-23)). Analysing the motion of CBPs, Sudar *et al.* [\(2016](#page-12-16)) detected poleward meridional flow for all latitudes with an amplitude of about 30 m s⁻¹.

The main focus of this paper is to analyse the meridional motion revealed by tracing sunspot groups over the solar surface with DPD, which has never been used before for this purpose. We also attempt to explain the wide variety of results for meridional flow in Section [4](#page-7-0) in a consistent way. Another very important aspect of this work is to confirm that Reynolds stress is the main generator of the observed solar rotation profile as already suggested by a number of previous theoretical and empirical papers.

2. Data and Reduction Methods

Our dataset is created from positions and times of sunspot groups measured in $DPD¹$ $DPD¹$ $DPD¹$ (Baranyi, Győri, and Ludmány, [2016;](#page-10-0) Győri, Ludmány, and Baranyi, [2017\)](#page-11-24) during a period from 1974 to 2016. Positions of sunspot groups are typically determined once per day. We use the daily change in position of each sunspot group to calculate both meridional and rotational speeds:

$$
\omega_{\rm rot} = \frac{\Delta \text{CMD}}{\Delta t},\tag{1}
$$

$$
\omega_{\text{mer}} = \frac{\Delta b}{\Delta t},\tag{2}
$$

where Δ CMD is the difference between central meridional distances (CMD) and Δb is the difference in latitude of two consecutive positions of the sunspot group in time Δt (usually 1 day).

This results in 59 090 data points for each speed. Rotation speeds are transformed from synodic to sidereal values (Skokic´ *et al.*, [2014\)](#page-12-17). Assigning particular latitude, *b*, to each velocity is not as straightforward as it seems. With two measurements of position to calculate one velocity, we could use the latitude of the first or the second measurement. Even average latitude seems like a possible candidate. However, as Olemskoy and Kitchatinov [\(2005](#page-11-25)) pointed out, an uneven distribution of sunspots (or any other kind of tracer) in latitude creates a problem with some of the possible choices. They have shown that the gradient of the latitudinal distribution can create false meridional flows if the latitude of the second measurement is used. The simplest way to avoid this problem is to use the latitude of the first measurement and this is the choice we make (Sudar *et al.*, [2014,](#page-12-6) [2015](#page-12-18), [2016](#page-12-16)).

Determination of the position of a sunspot on the limb can introduce large errors due to projections effects. In addition, Arevalo *et al.* [\(1982](#page-10-2)) found that the calculated rotation

¹See <http://fenyi.solarobs.csfk.mta.hu/en/databases/DPD/>.

profile changes, depending on the cut-off longitude. Wöhl [\(1983\)](#page-12-19) also reported that the determined rotation velocities are larger for smaller cut-off longitudes. Such changes were attributed to Wilson depression by Balthasar and Wöhl [\(1983](#page-10-11)). Therefore we limit the dataset to \pm 58 \degree in CMD which alleviates these problems (Stark and Wöhl, [1981](#page-12-20); Balthasar *et al.*, [1986\)](#page-10-12). Nevertheless, outliers resulting from misidentification of sunspot groups in subsequent measurements or other errors are still present, so we use an iterative filtering method similar to the one used in Sudar *et al.* [\(2016](#page-12-16)). In the first step we calculate the solar rotation profile:

$$
\omega(b) = A + B \sin^2(b),\tag{3}
$$

where b is the latitude, and then we calculate the rotation velocity residuals by subtracting the individual rotational speeds from the average rotation profile given by Equation ([3](#page-3-0)). In the next step we calculate the lower quartile, Q_1 , and upper quartile, Q_3 , for rotation velocity residuals and finally remove the so-called hard outliers which lie outside of the range:

$$
[Q_1 - k(Q_3 - Q_1), Q_3 + k(Q_3 - Q_1)], \qquad (4)
$$

where we choose $k = 3.5$. Since outliers could potentially influence the calculated rotation profile, we use the remaining dataset to recalculate the solar rotation profile. The new rotation profile changes the values of rotation velocity residuals which then need to be checked for outliers. This process continues iteratively until no data points are outside of the interquartile range (Equation (4) (4)). In the end we obtain a dataset consistent with the calculated rotation profile and with outliers removed. In each iteration we also remove the outliers in meridional velocity using the same form of the interquartile range. The process converges very fast and only four iterations were necessary in our case. Outlier limits turn out to be ±4*.*5◦ day[−]¹ and ±2*.*1◦ day[−]¹ for rotation velocity residuals and meridional velocities, respectively.

After removing the outliers we end up with 53 283 data points. The best fit rota-tion profile is shown in Figure [1](#page-3-2) where the coefficients of the profile (Equation (3) (3)) are $A = 14.5011 \pm 0.0081° \text{ day}^{-1}$ and $B = -2.540 \pm 0.073° \text{ day}^{-1}$. In the same figure we also show average values of $\omega(b)$ in 2°-wide bins in latitude. The error bars shown in Fig-ure [1](#page-3-2) become fairly large for $b > 35^\circ$, which is a consequence of the fact that sunspots rarely appear above this latitude. In terms of expansion in Gegenbauer polynomials (Snod-grass and Howard, [1985\)](#page-12-21) the rotation profile coefficients become $A_G = 13.993° \text{ day}^{-1}$ and $B_{\rm G} = -0.51^\circ \,\rm day^{-1}$.

Figure 2 Meridional flow, v_{mer} as a function of latitude, *b*, is shown with black squares with error bars. Averaging bins are 5◦ wide in latitude. On the left hand side we show all data folded into one hemisphere where meridional velocity is asymmetrically transformed for southern latitudes. In this part of the plot positive values indicate motion towards the poles $(+P)$. On the right hand side of the plot meridional velocities are not transformed and we show both hemispheres. Positive values indicate motion towards the northern solar pole $(+N)$.

In the rest of the paper we use only residual rotation velocities and meridional velocities which are transformed from angular values to their linear counterparts taking into account the latitude of the first measurement. The conversion factor, with $R_{\odot} = 6.96 \times 10^8$ m, is 140*.*6 ms[−]¹ day*(*◦*)*[−]1, while rotation velocity residuals are additionally multiplied with the cosine of latitude. Additionally, meridional speeds are symmetrised, so that negative value of meridional speed reflects motion towards the equator for both solar hemispheres. This is achieved by transforming calculated meridional speeds with $v_{\text{mer}} = -\partial b/\partial t$ for the southern solar hemisphere, where we assign negative values to *b* for southern latitudes.

3. Results

In Figure [2](#page-4-0) we show the dependence of the meridional flow on latitude, *b*. Black squares with error bars depict average meridional flow in 5◦ bins of latitude. We can see that for −15◦ *<* $b < 15°$ meridional flow is towards the solar poles. In the right hand side of the plot we see that at the equator meridional flow is $\approx 0 \text{ m s}^{-1}$ and that the flow is asymmetrical around the equator. At mid-latitudes meridional flow becomes zero again on both hemispheres and probably turns to flow towards the equator at even higher latitudes. Similar behaviour was found by Sudar *et al.* ([2014\)](#page-12-6) who also concluded that the latitude at which the flow becomes zero is the centre of solar activity defined by the latitudinal distribution of sunspots for each phase of the solar activity cycle.

On the other hand, by using Doppler line shifts, most researchers found poleward flow of about 20 m s^{-1} for all latitudes (Duvall, [1979](#page-10-10); Howard, [1979;](#page-11-14) Hathaway, [1996\)](#page-11-15). Similar values were found by using high-resolution magnetograms (Komm, Howard, and Harvey, [1993\)](#page-11-23) and by applying time–distance helioseismology (Zhao and Kosovichev, [2004](#page-12-12)). Moreover, by using coronal bright points (CBP) as tracers, Sudar *et al.* [\(2016](#page-12-16)) found poleward meridional flows everywhere except at the equator where the flow was zero. This discrepancy in meridional flow between sunspot measurements and other observations is discussed in the next section.

Average values of the rotation velocity residuals, Δv_{rot} , in bins of 5[°] in latitude, *b*, are shown in Figure [3](#page-5-1) with solid squares with error bars. No significant deviation from $\Delta v_{\text{rot}} = 0$ can be detected.

One important feature of the solar rotation profile is that lower latitudes rotate faster than higher latitudes which implies that most of the angular momentum of the Sun is located in the zones around the equator. Therefore, it is reasonable to assume that there must be some mechanism which transfers angular momentum towards lower latitudes. By studying the relationship between meridional velocities, v_{mer} , and rotation velocity residuals, Δv_{rot} , we can directly observe if this is what is really happening. The relationship between the two velocities is shown in Figure [4.](#page-5-2) We also show the best linear fit to the data with the solid line, obtaining the following relation:

$$
v_{\text{mer}} = (-0.0876 \pm 0.0021) \Delta v_{\text{rot}} + (1.01 \pm 0.34) \text{ m s}^{-1}. \tag{5}
$$

The slope in Equation ([5](#page-5-0)) is statistically significant when compared with its uncertainty (relative error \approx 2.4%) which shows that on average the two values are not independent. The fact that the slope is negative shows that on average the angular momentum is indeed transferred from higher to lower latitudes. In a previous study, using the sunspot group data from the GPR and the SOON/USAF/NOAA obtained in the period 1878 – 2011, Sudar *et al.* ([2014\)](#page-12-6) found a very similar value for the slope *(*−0*.*080 ± 0*.*002*)*.

Reynolds stress is thought to be the main generator of the differential rotation on the Sun (Rüdiger, [1980;](#page-12-7) Pulkkinen and Tuominen, [1998b](#page-11-10)) which works against the diffusive decay.

The covariance of meridional velocities and rotation velocity residuals, $q = \langle \Delta v_{\text{rot}} v_{\text{mer}} \rangle$, is the horizontal component of the Reynolds stress tensor and in Figure [5](#page-6-2) we show its dependence on latitude. Values of q in 10 \degree bins in latitude, b , are shown as solid squares with error bars. We can see that the average value of q is negative for all latitudes meaning that there is a net angular momentum transfer towards lower latitudes. This picture might seem to be in conflict with Figures [2](#page-4-0) and [3](#page-5-1), which show the average behaviour of v_{mer} and Δv_{rot} with respect to latitude, *b*. However, we must remember that the average of the product is not equal to the product of the average, i.e. $q = \langle v_{\text{mer}} \Delta v_{\text{rot}} \rangle \neq \langle v_{\text{mer}} \rangle \langle \Delta v_{\text{rot}} \rangle$. Negative values of *q* actually imply that v_{mer} and Δv_{rot} are not mutually independent variables and that the relationship between them must be similar to the one given in Equation ([5\)](#page-5-0).

Sudar *et al.* [\(2014](#page-12-6)) introduced an empirical exponential cut-off function which describes the decreasing trend of $q(b)$ from the equator to higher latitudes and allows for a possible minimum. In this work we simplify the form of this relationship by requiring that the function is perfectly asymmetric around zero $(q(b) = -q(-b))$ leading to the expression:

$$
q = c_1 b e^{-c_3 b^2}.
$$
\n⁽⁶⁾

This choice is justified by the appearance of the function *q* in Figure 10 in Sudar *et al.* ([2014\)](#page-12-6), Figure 15 in Canuto, Minotti, and Schilling ([1994\)](#page-10-7), and also by the fact that Sudar *et al.* ([2014\)](#page-12-6) found that the value of parameter e_2 in their model was 69 ± 80 ms⁻². The function is plotted in Figure [5](#page-6-2) with a thick solid line. In the same plot we also shade the area defined by errors of the coefficients c_1 and c_3 (Table [1\)](#page-6-1). Using the errors of the coefficients we can also calculate the depth and location of the minimum in the $q(b)$ plot with their respective errors by using the method of error propagation. The minimum is thus located at $b_{\text{min}} = (42.3 \pm 8.3)$ ° with a value of $q(b_{\text{min}}) = (4250 \pm 880)$ m² s⁻². A similar result was obtained by Sudar *et al.* ([2014](#page-12-6)) who suggested that the $q(b)$ relationship has a minimum $(q \approx -3000 \text{ m s}^{-2})$ around 25 – 30°. We do not consider the difference between the two results to be significant, especially considering the scarcity of sunspots at higher latitudes where the minimum is supposed to be.

4. Discussion

The rotation profile calculated in this work is almost identical to the result obtained by Sudar *et al.* ([2014\)](#page-12-6) who also analysed the rotation by tracing sunspot groups albeit for a different time period and different observing stations. So, the DPD series proves to be a rather good continuation of the GPR dataset. For a more thorough comparison of solar rotation profiles obtained by different methods we refer the reader to Wöhl *et al.* ([2010\)](#page-12-22) and Sudar *et al.* ([2015\)](#page-12-18).

In Figure [3](#page-5-1) we show the average of rotation velocity residuals, Δv_{rot} , as a function of latitude, *b*. This plot should not be confused with the torsional oscillation pattern, because torsional oscillations show deviations from the mean velocity in time. When we average these variations over a long time, as we do in Figure [3](#page-5-1), such a plot is more indicative of the quality of the fit of the solar rotation profile function (Equation [\(3\)](#page-3-0)). In this context, we can say that, apart from the bin at $b = 2.5^\circ$, the average value of Δv_{rot} is zero. We are not sure if the slight discrepancy from this rule at $b = 2.5^\circ$ is of any significance.

The most interesting are the results for the meridional flow (Figure [2](#page-4-0)) because they are the most controversial. A quote by Hathaway [\(1996\)](#page-11-15) is perhaps the most illustrative of the problem: "Unfortunately, previous measurements of the Sun's meridional circulation have produced a bewildering array of results that appear to be of no help at all in constraining theory." On one hand we have sunspot measurements (and other features closely associated with sunspots such as plages) which show opposite flows on opposite sides of the centre of the solar activity and on the other hand we have Doppler measurements which predominately show poleward motion for all latitudes, regardless of the centre of the solar activity. There are also tracers, such as CBPs (Sudar *et al.*, [2016\)](#page-12-16), which also show average poleward motion everywhere of approximately the same amplitude as Doppler measurements. Small magnetic features analysed with different methods by Komm, Howard, and Harvey ([1993\)](#page-11-23) and Snodgrass and Dailey ([1996\)](#page-12-15) showed different behaviour around the centre of solar activity for meridional motion.

So, if we measure the same phenomenon with different techniques, how can we consistently interpret these differing results? First of all there is an internal problem with tracer measurements where some authors (Tuominen and Virtanen, [1984](#page-12-13); Howard and Gilman, [1986;](#page-11-19) Howard, [1991a](#page-11-20); Kambry *et al.*, [1991](#page-11-21); Wöhl and Brajša, [2001](#page-12-14)) reported a flow out of the centre of activity, while others detected a flow towards the centre of activity (Howard, [1991b](#page-11-22); Sudar *et al.*, [2014\)](#page-12-6). This difference can probably be explained by an easy-to-make error: assuming that it is irrelevant to which latitude one assigns the observed meridional velocity. Olemskoy and Kitchatinov [\(2005](#page-11-25)) demonstrated and Sudar *et al.* ([2014](#page-12-6)) later verified that it is necessary to assign the latitude of the first measurements due to the uneven distribution of tracers in latitude. Otherwise one would obtain almost exactly opposite and false flow. Technically it is possible to use the latitude of the last measurement of position, but the velocity would have to be weighted taking into account the frequency of tracers at the starting latitude. Since the tracer distribution can also vary during the solar cycle, the second method turns out to be very complicated compared to the neat trick of assigning the latitude of the first measurement. As a consequence we take the results by Sudar *et al.* [\(2014](#page-12-6)) as a reference model for sunspot measurements which are also confirmed by the results for meridional flow in this paper (Figure [2](#page-4-0)). However, we must point out that Sivaraman *et al.* ([2010\)](#page-12-23), who also used first latitude as a reference point, found a flow which is directed towards the solar equator for all latitudes. What we find intriguing in their results is that it appears that meridional flow is not zero at the equator, which is especially noticeable for the Mt. Wilson data they used. On the right hand side of our Figure [2](#page-4-0) we can see that the

average meridional motion is ≈ 0 which makes the motion clearly asymmetrical on the two solar hemispheres.

Small magnetic features were also used as tracers by past authors and although their latitudinal distribution is not the same as the one for sunspots we encounter the same problem. Their distribution overall falls from the equator towards the poles, but it also has peaks around centres of solar activity (Harvey, [1993\)](#page-11-26). Such a distribution gradient can create false flows out of the centre of activity in a similar manner as with sunspots, if proper care of assigning latitude was not taken. In this context we can explain the results by Snodgrass and Dailey [\(1996](#page-12-15)), but the meridional flow measured by Komm, Howard, and Harvey [\(1993](#page-11-23)) still requires some explanation. First we note that the amplitude of meridional motion in their work was about 10 m s⁻¹ which is substantially lower than most Doppler measurements and analysis of CBP data, so it is possible that their result was also influenced just by the overall drop in distribution of tracers towards the poles where the velocity resolution was not sufficient to be influenced by the peaks near centres of activity. Of course, it is also possible that they measured the real flow and that the fairly low amplitude they obtained is consistent with the wide range of possible variations mentioned by Hathaway [\(1996](#page-11-15)).

Analysing the flow in the upper convective zone with time–distance helioseismology Zhao and Kosovichev [\(2004](#page-12-12)) found mostly poleward meridional flow (their Figure 3a). However, when they subtracted the flow from Carrington Rotation 1911 which occurred during the solar minimum year 1996 they obtained the *residual* meridional flow (their Figure 3b) which in all important aspects looks the same as the meridional flow we see in this work (Figure [2](#page-4-0)) and in Figure 3 in Sudar *et al.* [\(2014](#page-12-6)). Applying ring-diagram analysis to GONG Dopplergrams González Hernández *et al.* ([2008\)](#page-11-27) also found residual meridional flows very similar to our meridional flow (their Figures 4 and 5). Moreover, map plots of residual meridional motion in González Hernández *et al.* [\(2008](#page-11-27)) (their Figure 6) and González Hernández *et al.* [\(2010](#page-11-28)) (their Figure 3) look a lot like a similar map plot for meridional motion of sunspot group data in Sudar *et al.* [\(2014](#page-12-6)) (their Figure 2).

The key in understanding why residual meridional flow in Doppler measurements looks like total meridional motion in sunspot groups measurements is in appreciating that sunspot groups do not cover all of the solar surface, but are limited to active regions. When Zhao and Kosovichev [\(2004](#page-12-12)) subtracted the meridional flow measured during the solar cycle minimum when active regions rarely appear they obtained the residual flow dominated by the motion in and around active regions and that is the area where sunspot groups are found. Therefore, it is perfectly understandable why Zhao and Kosovichev [\(2004](#page-12-12)) found that their residual meridional flows in the period from 1997 – 2002 converge towards activity belts with the magnitude of $2 - 8$ m s⁻¹ in both solar hemispheres just as we see in our total meridional flow (Figure [2\)](#page-4-0). By analysing sunspot group data we get no information as regards the dominant poleward meridional flow outside of the active regions. Even the analysis of CBP data (Sudar *et al.*, [2016\)](#page-12-16) supports this hypothesis, because detection of CBPs with the segmentation algorithm above bright active regions is almost impossible. As a result, Sudar *et al.* [\(2016](#page-12-16)) found the dominant poleward meridional motion originating outside of the active regions.

An alternative to our hypothesis is that the anchor depth of magnetic features plays a role in the meridional flow pattern. Anchor depth has been used as an explanation for differences in rotation rates measured by different tracers and different observing methods. A useful overview of this problem is given in Beck ([2000\)](#page-10-13). The rotation rate of surface features are usually connected to depth corresponding to the rotation rate obtained with helioseismology. In general larger features are associated with larger depths, but there are exceptions like for example recurrent sunspot groups. It is logical to assume that the meridional flow of surface features also depicts the motion of deeper layers which is what Sivaraman *et al.* [\(2010](#page-12-23)) concluded based on observing different size sunspot groups. Further work on meridional flow at different depths, possibly in connection with the phase of the solar cycle, is still necessary to shed more light on the subject.

Another interesting question is how does this difference between sunspot group data and CBP data affect the observed horizontal Reynolds stress. Sunspot group measurements (Ward, [1965;](#page-12-1) Gilman and Howard, [1984;](#page-11-6) Sudar *et al.*, [2014\)](#page-12-6) show a fairly large negative value of $q \approx -3000$ m² s⁻² located near 30° in latitude. A slightly larger value at higher latitude is also found in this work. Canuto, Minotti, and Schilling [\(1994](#page-10-7)) already confirmed that this result is in agreement with the theoretical curve using only standard values for parameters in solar conditions. On the other hand, analysis of CBP data by Sudar *et al.* ([2016\)](#page-12-16) yields a highly uncertain value of only $q \approx -1500$ m² s⁻² around 25°. The time period covered in Sudar *et al.* [\(2016](#page-12-16)) is less than six months in the rising phase of the solar cycle, but we do not think that the phase of the solar cycle is the cause of such a low value of *q* in CBP data. Sudar *et al.* [\(2014](#page-12-6)) showed a map of *q* versus latitude and phase of the solar cycle and found that the locations and depth of the horizontal Reynolds stress, *q*, are persistent at least from the beginning of the solar cycle until well past the solar activity maximum. In the declining phase of the solar cycle, the latitudinal distribution of sunspots prevents making a firm conclusion about the behaviour of *q*. So, we suggest that the horizontal Reynolds stress is stronger in and around active regions which means that most of the angular momentum transfer towards the equator takes place in these areas. Another possibility is that the height of the tracers also plays a role, or in other words that Reynolds stress is less pronounced in the layers above the photosphere. This would also imply that CBPs are not firmly rooted to the photosphere and we do not consider this to be very likely.

5. Conclusion

We analyse the motion of sunspot groups obtained by Debrecen Observatory in the period 1974 – 2016. The calculated solar rotation profile is in agreement with other authors especially those investigating also sunspot groups. This shows that the DPD catalogue is an adequate successor of the GPR dataset.

The observed meridional motion is typical for the sunspot groups, but different from Doppler and CBP measurements. We suggest that the difference lies in the fact that sunspot groups are located within active regions where the meridional motion is different than outside of those areas. This idea is supported by *residual* meridional flow obtained by subtracting the dominant poleward meridional flow in Doppler data which then looks almost the same as the total meridional flow we see when analysing sunspot group data. Canuto, Minotti, and Schilling ([1994](#page-10-7)) derived a model of Reynolds stress which is driven by buoyancy which acts as a source of convective turbulence. If we take into account that in strong magnetic fields within sunspots convection is inhibited, it might be possible that the velocity components of the horizontal Reynolds stress are also affected and, therefore, show different behaviour in and outside of active regions.

The horizontal Reynolds stress calculated in this work confirms the results in all important aspects obtained by Sudar *et al.* ([2014\)](#page-12-6) who used data from different observatories. The latitudinal behaviour of the horizontal Reynolds stress shows the transport of angular momentum towards the equator everywhere, increasing in absolute value from the equator to a possible maximum value somewhere around $25 - 40°$, which is also consistent with earlier studies based on sunspot data (Ward, [1965](#page-12-1); Belvedere *et al.*, [1976;](#page-10-8) Schröter and Wöhl, [1976;](#page-12-9) Gilman and Howard, [1984](#page-11-6); Pulkkinen and Tuominen, [1998b](#page-11-10)). By comparing the horizontal

Reynolds stress obtained with sunspot group data and CBP data we suggest that larger values of horizontal Reynolds stress, and consequently angular momentum transfer, are found within active regions. Analysis of meridional motion and horizontal Reynolds stress values with CBP data as a function of proximity to active regions might prove or disprove this hypothesis.

Measurements of the latitudinal dependence of the covariance of rotation velocity residuals and meridional flow presented in this work strongly suggest that the Reynolds stress is the dominant mechanism which explains the observed characteristics of the solar differential rotation. The observed horizontal Reynolds stress is consistent with the transport of angular momentum towards the solar equator both qualitatively (correct sign) and quantitatively (absolute value). On the other hand, the model of axisymmetric meridional circulation, which could also produce transfer of the angular momentum towards the equator, is strongly disfavored because it requires surface meridional motions in the direction towards the solar equator (Gilman, [1981;](#page-11-29) Stix, [1989](#page-12-24); Foukal, [2013\)](#page-11-30), which contradicts the observations in the present and other papers.

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