



Marshall-Olkin distributions: a bibliometric study

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Abstract

Recently, there has been a growing interest among statistical researchers to develop new probability distributions, adding one or more parameters to previously existing ones. In this article, we describe a bibliometric analysis carried out to show the evolution of various models based on the seminal model of (Marshall and Olkin, *Biometrika*. 1997). This method allows us to explore and analyze large volumes of scientific data through performance indicators to identify the main contributions of authors, universities, and journals in terms of productivity, citations, and bibliographic coupling. The analysis was performed using the Bibliometrix R-package tool. The sample of analyzed data was based on articles indexed in the main collection of the Web of Science and Scopus between 1997 and 2021. This work also includes an overview of the methodology used, the corresponding quantitative analyses, a visualization of networks of collaboration and co-citations, as well as a description of the topic trends. In total, 131 articles were analyzed, which were published in 67 journals. Two journals published 17% of the manuscripts analyzed in this work. We identified 238 separate authors who have participated in the development of this research topic. In 2020, 49% of the authors presented new distributions, where their proposed models included up to six parameters. The publications were grouped into 20 collaborative groups of which Groups 1 and 2 are dominant in the development of new models. Thus, 24% of the publications analyzed belong to two researchers who lead these two groups. To show the flexibility of the new distributions, the authors apply their models using at least two sets of real-world data to show their potentiality. This article gives a broad overview of different generalizations of the Marshall-Olkin model and will be of great help to those interested in this line of research.

Keywords Bibliometric analysis · Marshall-Olkin distribution · Parameter estimation methods

Mathematics Subject Classification 60E05 · 62E15 · 62F10

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Introduction

Marshall and Olkin (1997) introduced a method for adding a parameter to a distributions family through application to the exponential and Weibull with the purpose of obtaining new distributions. This procedure aims to develop new distributions with greater flexibility in modeling various data types. According to the authors, if $\bar{F}(x)$ is denoted as a survival function of a continuous random variable X , then the mechanism of adding parameter α , results in another survival function $\bar{G}(x)$ defined by,

$$\bar{G}(x, \alpha) = \frac{\alpha \bar{F}(x)}{1 - (1 - \alpha)\bar{F}(x)}, \quad -\infty < x < \infty, \quad \alpha > 0, \quad (1)$$

where the probability density function (PDF) and the cumulative distribution function (CDF) corresponding to Eq. (1) are:

$$g(x, \alpha) = \frac{\alpha f(x)}{[1 - (1 - \alpha)\bar{F}(x)]^2}, \quad -\infty < x < \infty, \quad \alpha > 0, \quad (2)$$

and

$$G(x, \alpha) = \frac{F(x)}{[1 - (1 - \alpha)\bar{F}(x)]}, \quad -\infty < x < \infty, \quad \alpha > 0, \quad (3)$$

where $f(x)$ is the PDF corresponding to $\bar{F}(x)$.

On the other hand, the hazard rate function of the Marshall–Olkin extended distribution is given by

$$h(x; \alpha) = \frac{r(x)}{1 - (1 - \alpha)\bar{F}(x)}, \quad (4)$$

where $r(x) = \frac{f(x)}{\bar{F}(x)}$, which is the hazard rate function of the baseline distribution.

Marshall and Olkin called the additional parameter “tilt parameter” since the hazard rate of the new family is shifted below ($\alpha > 1$) or above ($0 < \alpha \leq 1$) of the hazard rate of the underlying distribution. In other words, for all $x \geq 0$, $h(x) \leq r(x)$ when $\alpha > 1$, if $0 < \alpha \leq 1$ then $h(x) \geq r(x)$.

From the seminal work of Marshall and Olkin (1997), many researchers have introduced new distributions or generalized some existing distributions to model a real data set’s behavior. The main objective of proposing, extending, or generalizing models is to explain how a data set behaves in lifetime analysis, survival times, failure times, and reliability analysis. Furthermore, the proposed models have been applied in areas such as medicine, public health, biology, physics, computer science, finance and insurance, engineering, industry, communications, among others (Jayakumar & Sankaran, 2019a, 2019b; Nassar et al., 2019; Rondero-Guerrero et al., 2020).

For instance, better modelling of reliability analysis of system components is increasingly important in virtually all sectors of manufacturing, engineering, and administration. Indeed, reliability engineering studies the ability of a device to function without failures in order to predict or estimate the risk of failure. That is, it studies the capacity of a component or system to function during a specific time or over an interval of time (Ricardo P. Oliveira et al., 2021). Therefore, the use or application of different lifetime distributions has become more critical due to the global dynamics of trade. Because globally there is a

growing variety of products and increasing focus on quality control more companies are under pressure to perform reliability analysis of their products to understand failure and survival rates. In addition, statistical lifetime distributions have grown in fields such as biological sciences, life tests, and medicine since they can predict disease behaviors, in particular control measures and mitigation in response to the social impact of epidemics and pandemics.

Although, Ricardo P. Oliveira et al. (2021), Algarni (2021), and Eghwerido et al. (2021) mention that lifetime probability distributions such as Weibull, exponential, Lindley, and Weibull exponential distribution, among others, can be used to model the data, in many cases they do not provide a good fit for modeling phenomenon with non-monotone failure rates, such as bathtub upside down failure shaped. For this reason, many researchers have developed new, more flexible models in the last decade.

That is why this article aims to analyze publications related to the new distribution models or generalizations of existing distributions that derive from the seminal work of Marshall and Olkin (1997) through a bibliometric approach. For this bibliometric study, we focus on publications found in Web of Science (core collection) and Scopus databases. In addition, this study considers several bibliometric indicators related to authors, journals, and articles. The paper presents various bibliometric techniques using open-access software “Rstudio” of “R” to mapping collaboration and co-citation networks. The contribution of this work to the body of literature lies in:

- Describing how the contribution by Marshall and Olkin (1997) in developing new distributions in terms of publications, authors, and journals is organized and advanced. As well as identify bibliometric trends.
- Presenting the main characteristics of the new distributions or distribution families.

Materials and method

Bibliometric analysis is a type of quantitative analysis used to classify and report bibliographic data on a particular research topic. In other words, it is used to measure the impact of journals, identify authors, and detect new research lines. This type of analysis involves the mathematical and statistical treatment of scientific publications and their respective citations. Bibliometric analysis results provide relevant information about the level of activity (research) that exists among authors, organizations or countries, as well as the evolution of research topics (Cancino et al., 2019; Ferreira, 2018; Lei & Xu, 2020).

We chose a bibliometric study because it develops a systematic, transparent, and reproducible process of identifying relevant manuscripts. In addition, a series of techniques are applied to evaluate scientific production through objective and quantitative indicators of bibliographic data (Krainer et al., 2020). The protocol used for this bibliometric analysis is shown in Fig. 1. This process begins by establishing the research topic and then continues with four sequential stages that provide sufficient evidence on the contribution and development of scientific knowledge (development or generalization of new distributions).

Also, in this protocol, two main categories of analysis are considered: performance analysis and scientific mapping. The first one aims to present a descriptive analysis of the following parameters: authors, journals, institutions, and articles. The second focuses on

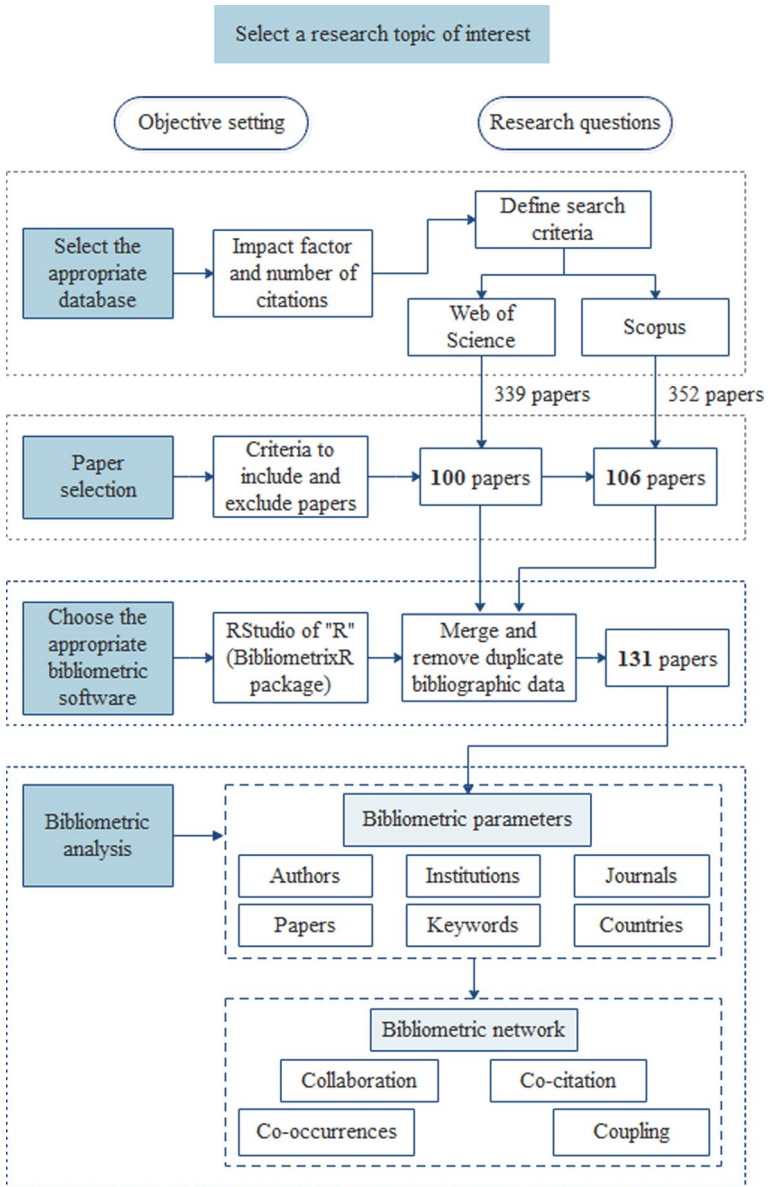


Fig. 1 Protocol for the bibliometric study

mapping bibliometric networks to explore the interrelationship between authors and references (Ruggeri et al., 2019).

The “RStudio” software was used with the Bibliometrix 3.0.1 package. This package is appropriate for bibliometric and scientometric studies because it provides users with

a greater degree of control over modifying and adjusting the input and output data (Aria & Cuccurullo, 2020).

Data collection

Oorschot et al. (2018) and Ruggeri et al. (2019) state that to guarantee the documents' maximum quality be analyzed, it is vital to use the Web of Science database (core collection) since the validity of any bibliometric analysis depends mostly on selecting the publications. The authors indicate that Web of Science meets the highest standards in terms of impact factor and number of citations. On the other hand, Lei and Xu (2020) mention that another database with high-quality standards is the Scopus database. According to Lei and Xu, Scopus is the world's largest peer-reviewed journal abstract and citation database.

Therefore, to achieve the objective of this study, the Web of Science (main collection) and Scopus databases were both selected. Data collection was carried out beginning on April 30, 2021. For the Web of Science database, the following search string was used: Topic (Marshall-Olkin), Publication Years (2021–1997), and Document Types (Article). The results of this search produced 339 articles. To verify the coherence of the subject matter of each manuscript, each one of them was analyzed. Through this process, 239 documents were removed from the database, resulting in a dataset of 100 documents.

The SCOPUS database was obtained with the following search string: Article title, Abstract, Keywords (Marshall-Olkin), Year (2021–1997), and Document Type (Article). The result was 352 articles. For this database, the same Web of Science process was carried out to verify the coherence of the subject matter of each manuscript, which resulted in 106 documents.

Finally, to combine the bibliographic data Web of Science and Scopus, and eliminate the duplicate data (duplicate articles), the “mergeDbSources” function of the Bibliometrix package was used (Aria & Cuccurullo, 2020), where a total of 131 articles were ultimately obtained for bibliometric analysis.

Bibliometric analysis

In this section, a quantitative analysis of the articles composing the database is presented and discussed. We carried out a descriptive analysis considering the following parameters: authors, journals, institutions, and articles. Secondly, we conducted a bibliometric network analysis considering collaboration and co-citation networks.

Of the 131 articles analyzed, 238 authors participated in the development of the publications. Collaboration between authors is the key to the development of new models. Table 1 shows that eight papers were each written by only one author. The rate of collaboration between authors is 1.8. The main information about the bibliometric data is shown in Table 1.

Annals and trends

Table 2 presents an overview of the annual scientific production from 1997 to April 21, 2021. As shown in the table, from 1997 to 2011, there were only six publications related to new classes or generalizations of distributions based on the seminal work by

Table 1 Main information about bibliometric data

Parameter	<i>N</i>
Papers	131
Authors	238
Sources (Journals)	67
Keywords plus	244
Author's keywords	366
References	3505
Authors of multi-authored papers	226
Authors of single-authored papers	12
Average citations per papers	6.191
Papers per author	0.55 (131/238)
Authors per papers	1.82 (238/131)
Collaboration Index	1.9 (226/(131–12))

Table 2 Annual Scientific Production

Year	TP	TC	ATC	CY	ATCY	TCR	ACR	NA
2004	1	1	1	17	0.06	20	20	1
2007	2	167	83.5	14	5.96	23	11.5	5
2008	1	36	36	13	2.77	17	17	2
2010	1	33	33	11	3	26	26	3
2011	1	16	16	10	1.6	18	18	3
2013	5	110	22	8	2.75	101	20.2	11
2014	3	20	6.67	7	0.95	98	32.67	11
2015	5	74	14.8	6	2.47	114	22.8	14
2016	15	86	5.73	5	1.15	385	25.66	45
2017	17	82	4.82	4	1.21	496	29.17	52
2018	9	60	6.67	3	2.22	239	26.55	33
2019	22	61	2.77	2	1.39	523	23.77	68
2020	37	64	1.72	1	1.73	1099	29.70	118
2021	12	1	0.08	0	–	346	28.83	42

Indicators in the table: TP: Total papers number; TC: Total citation number; ATC: Average TC per article (TC/TP); CY: Citable years; ATCY: Average TC per year (ATC/ CY); TCR: Total cited references; ACR: Average cited references (TCR/TP); NA: Number of authors.

Marshall and Olkin, (1997). Table shows that from 2013 to 2015, an interest in developing new probability distributions began. From 2016 to date, there has been a significant increase in the publication of new distribution models. In terms of the number of total citations (TC) and the number of average citations per article (ATC), the most cited manuscripts correspond to the year 2007, although in that year there were only two publications. However, interest in this research topic increased significantly since 2016. Regarding the number of authors, there is an upward trend from 2013 to date, as shown in Table 2.

The main authors, most influential articles and journals

Table 1 showed that, in this analyzed database, 238 authors have written about new distributions or have extended a distribution class. This section presents the most productive authors, those with five or more publications. Under this consideration, 12 researchers were identified, as Table 3 shows. These 12 authors are ordered by the number of publications from highest to lowest. Cordeiro G. is the author who has contributed the most to the development of new distributions with a total of 17 publications, followed by Afify A. with 14 articles. Regarding the total number of citations, the most cited authors are Cordeiro G. (123), Al-Awadhi F. (105), Alkhalfan L. (105), Ghitany M. (105), Yousof H. (101), and Afify A. (97).

On the other hand, one of the objectives among the scientific community (researchers) is to achieve a significant and recognized impact through their publications. One way of assessing the impact of an author is by considering where and how often their work is cited. That is, author-level metrics are citations metrics that measure the bibliometric impact of authors individually. Table 3 presents three metrics that measure the impact of the authors analyzed here. As seen in Table 3, Cordeiro G. is in the first position of two of the three indices presented (h-index and g-index), and Yousof H. has the highest level in the m-index.

Another aspect of a bibliometric analysis is to identify the most influential documents in the development of new distributions. As shown in the Table 4, the document by Ghitany et al. (2007) is the most cited in the database, with a total of 105 citations. The authors of this article present a new variant of “the extended family of Marshall and Olkin distributions,” where they introduce the Lomax distribution to generate a new model. A significant aspect of the publications shown in Table 4 is that two articles were each written by a single author; the other eight papers were collaborations.

Of the different document types available on scientific platforms or databases, journals are considered the most important means of communication, and it is one of the most

Table 3 Most Relevant Authors

Authors	TP	Institutions	h-index	g-index	m-index	TC	PY-start
Cordeiro G	17	Federal University of Pernambuco	7	11	0.875	123	2014
Afify A	14	Benha University	6	9	1.000	97	2016
Jayakumar K	8	University of Calicut	3	7	0.214	57	2008
Yousof H	8	Benha University	7	8	1.167	101	2016
Alizadeh M	6	Persian Gulf University	3	6	0.429	43	2015
Kundu D	6	Indian Institute of Technology Kanpur	3	6	0.333	44	2013
Almetwally E	5	Delta University of Science and Technology	2	4	1.000	17	2020
Hamedani G	5	Marquette University	4	5	0.667	53	2016
Jamal F	5	The Islamia University Bahawalpur	1	1	0.200	4	2017
Ozel G	5	Hacettepe University	2	3	0.333	15	2016
Saboor A	5	Kohat University of Science & Technology	3	5	0.429	45	2015
Sankaran K	5	University of Calicut	2	2	0.333	9	2016

PY-start: Publication Start Year

Table 4 The 10 most cited documents

Paper	Year	Author/s	TC	ATCY
Marshall-Olkin Extended Lomax Distribution and Its Application to Censored Data	2007	Ghitany ME, Al-Awadhi FA, Alkhalaf LA	105	6.690
A new class of bivariate distributions and its mixture	2007	Sarhana MA, Balakrishnan N	62	4.133
On a generalization to Marshall-Olkin scheme and its application to Burr type XII distribution	2008	Jayakumar K, Mathew T	36	2.571
The Marshall-Olkin Fréchet distribution	2013	Krishna E, Jose KK, Alice T, Ristić MM	34	3.777
Marshall-Olkin q -Weibull distribution and max-min processes	2010	Jose KK, Naik SR, Ristić MM	33	2.750
A new extension of the Birnbaum-Saunders distribution	2013	Lemonte AJ	31	3.440
The beta Marshall-Olkin family of distributions	2015	Alizadeh M, Cordeiro GM, Brito ED, Demétrio CGB	29	4.140
Marshall-Olkin Generalized Exponential Distribution	2015	Ristić MM, Kundu D	21	3.000
A New Extension of Weibull Distribution with Application to Lifetime Data	2017	Dey S, Sharma KV, Mesfoui M	20	4.000
Marshall-Olkin extended log-logistic distribution and its application in minification processes	2013	Gut W	20	2.222

widely used sources among the scientific community. Therefore, a journal works as an official means to record scientific and academic findings publicly; that is, it is considered as a scientific and social institution that indicates aspects such as the contribution and prestige of researchers (authors), the disciplines of the most influential scientists, and the most productive institutions, countries, and publishers.

Table 5 shows the journals that have two or more publications in this database. As shown in the table, the journal “Communications in Statistics-Theory and Methods” ranks first in the number of articles and citations, with 13 and 156, respectively. However, the journal “Statistical Papers” has the highest proportion of citations per paper (3 papers and 85 citations). On the other hand, journal quality can be determined by the impact factor (in this case, the relationship between the number of articles and the sum of the citations of these articles). In this bibliometric analysis, the journal with the highest impact factor is “Journal of King Saud University – Science”, followed by “Journal of Computational and Applied Mathematics”, and “Statistical Papers”.

Bibliometric networks

Network analysis is a technique widely used in bibliometrics and scientometrics studies. Bibliometric networks generally consist of nodes, which may be authors (researchers), universities, countries, journals, keywords or references, and links representing the relationships between them. In each case, the corresponding bibliometric network represents a set of documents for study or analysis. The software used in this work allows the following bibliometric networks to be created and represented visually: Collaboration Networks, Co-citation Networks, Coupling Networks, and Co-occurrences Networks.

The mapping method in Bibliometrix 3.0.1 package consists of three stages: (1) standardization method, (2) type of network, and (3) clustering algorithm of the nodes in the

Table 5 The most productive international journals

Source	NP	TC	h_index	g_index	m_index	IF	5-IF
Communications in Statistics-Theory and Methods	13	156	5	12	0.277	0.612	0.606
Pakistan Journal of Statistics and Operation Research	9	38	3	6	0.50	ESCI	ESCI
Annals of Data Science	6	26	3	5	0.6	GS	GS
Journal of Statistical Theory and Applications	6	11	2	2	0.28	ESCI	ESCI
Communications in Statistics: Simulation and Computation	4	13	2	3	0.28	0.651	0.651
Advances and Applications in Statistics	4	0	0	0	0.00	ESCI	ESCI
Hacettepe Journal of Mathematics and Statistics	4	44	3	4	0.42	0.679	0.787
Journal of King Saud University-Science	4	16	3	4	1	3.819	–
Mathematics	4	20	3	4	1.5	1.747	–
Journal of Computational and Applied Mathematics	3	31	3	3	0.37	2.037	1.994
Statistica	3	18	2	3	0.333	ESCI	ESCI
Statistical Papers	3	85	3	3	0.21	1.433	1.247

IF: Impact factor; 5-IF: 5-year impact factor; ESCI: Emerging Sources Citation Index, GS: Google Scholar.

network. To visualize bibliometric networks, the “net2VOSviewer” function of the Bibliometric 3.0.1 package was used to export the obtained networks to the “VOSviewer” software (Aria & Cuccurullo, 2020). The collaboration network and co-citation network for this work are presented below.

Collaboration network

This analysis allows for identifying the level of collaboration of published research from three different approaches: authors, institutions, and countries. This analysis type aims to investigate the level of collaborative strength of research in a specific field.

Concerning co-authorship relationships, Table 1 shows that 12 of the 238 authors are listed as sole authors. That is, 91% of the articles in this database were published by co-authorship. Figure 2 shows the collaboration network between authors. The most collaborative authors, in terms of publications, are represented as larger nodes. In Fig. 2, it can be seen that the largest node is for Cordeiro G. and Afify A., which shows the most articles and the total strength of the link. The above is consistent with Table 3. On the other hand, 20 research clusters were identified, represented by different colors, where it can be observed that the research clusters of Afify A., Ozel G., Jamal F., Yousof H., Alizadeh M., and Nasir M. are closely collaborating with Cordeiro G. The rest of the researchers show a lower weight in publications and collaborative links. Thus, the clusters are distributed

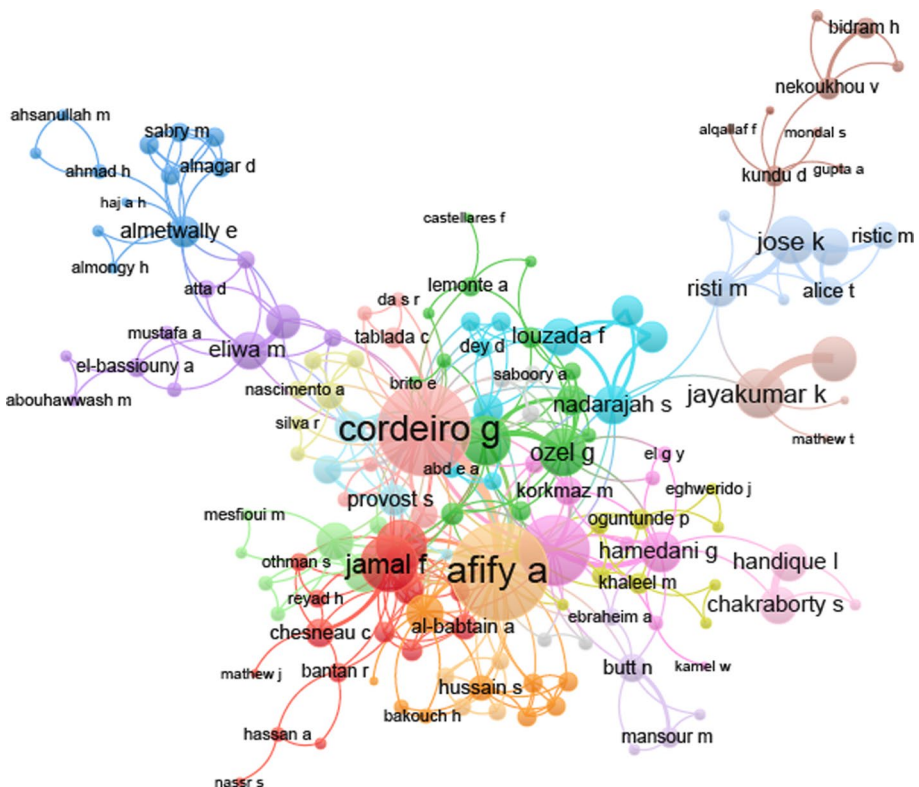


Fig. 2 Collaboration networks: co-authorship

separately, where some are barely connected with one researcher, and others have no connection or collaboration with other research clusters.

Co-citation network

According to Ruggeri et al. (2019), they mention that citation analysis is a bibliometric technique proposed by Small, (1973) that aims to represent through a network the structure of a set of documents that are commonly cited among themselves. In other words, the more times two papers are cited together, the stronger their association, which allows us to infer in some way that the authors’ research is significantly related (they belong to the same research field).

In Fig. 3, the co-citation network of references is presented. The database recorded a total of 3,505 cited references. In Fig. 3, the 200 references with the most significant citation nodes are shown, indicating that these articles are the most frequently cited in publications related to the development of new distributions. The most cited reference is the seminal work by Marshall and Olkin, (1997); this allows us to infer that this article represents the central knowledge base for developing new distributions, and it is also congruent with the study objective of this work. On the other hand, of the 131 articles analyzed, it is observed that the manuscript of Jayakumar and Mathew, (2008) is the most cited within the local citations.

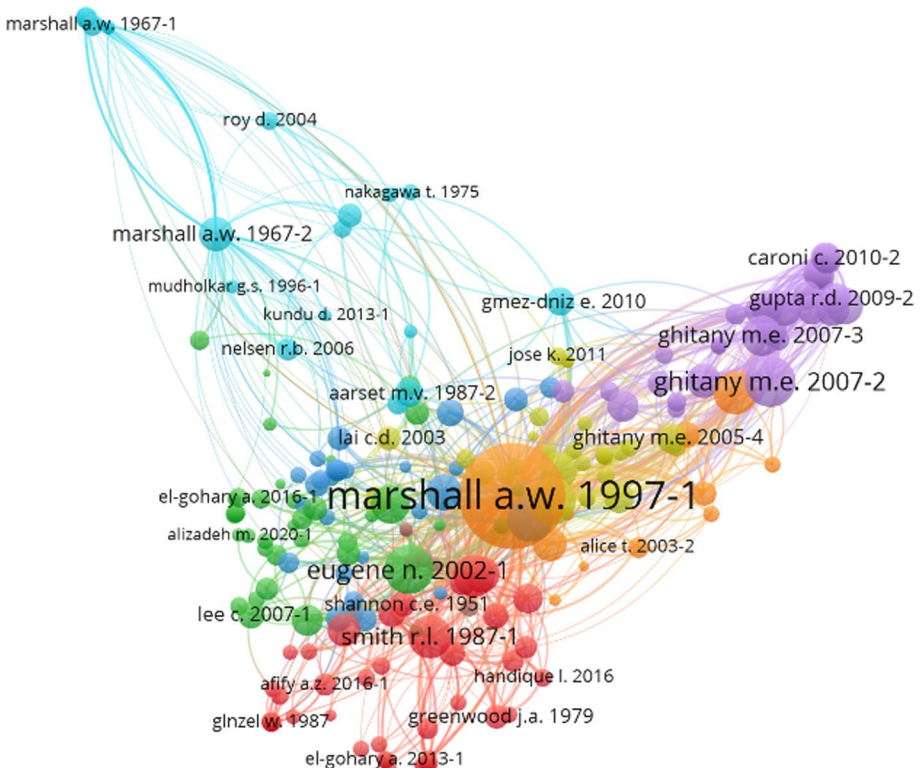


Fig. 3 Co-citation network: references

Main findings of the bibliometric analysis

According to the database, in the last six years, mainly researchers in statistics, mathematics, and engineering have developed new distributions or have generalized and extended the existing models to increase the distributions' versatility. The popular and most used distributions such as the exponential, gamma, Normal, and Weibull, among others, are very limited in their characteristics and cannot show great flexibility. For this reason, many authors have used different techniques to build new models. According to El-Morshedy et al. (2020), the main reasons for these new models are:

- To build heavy-tailed distributions to be able to model real data.
- To make the kurtosis more flexible compared to the baseline model(s).
- To generate distributions with symmetric, left-skewed, right-skewed, or reversed-J shape.
- To provide more flexibility in the cumulative distribution function and the hazard rate function.
- To provide a better fit than models generated under the same baseline distribution.

Another relevant point considered by the articles was the method for estimating the parameters of the model. Ninety-five percent of the papers presented a method for estimating the parameters of their model. The rest of the manuscripts did not present this point. The predominant method was that of maximum likelihood; 124 articles used this method. Also, 13 manuscripts applied the Bayesian estimation method. Other methods used to estimate parameters were the maximum product spacing, the least-squares method, and the interval estimation method.

The main topics addressed in the manuscripts are survival function, hazard function, mean residual life, Renyi entropy, moments, moment generating function, quantile function, order statistics, stochastic orderings, estimation method, simulation, and applications. Of the 131 works, 91 of the articles mention that they used software to find the values of the parameters in the different simulations and applications of the proposed models. Seventy-one manuscripts used the open-source software "R." They also used other software such as Maple, Matlab, Mathematical, SAS, Python, Mathcad, Mathematica, and Ox matrix programming language. The rest of the papers did not mention what software they used.

Ninety-one percent of the publications illustrate the proposed model's practical importance by applying it to a real data set to show the new distribution's potential and flexibility. The data used are adjusted to the proposed model and compared with other existing models. For comparison purposes, the authors calculate some goodness-of-fit statistics such as Akaike information criterion (AIC), consistent Akaike information criterion (CAIC), Bayesian information criterion (BIC), Hannan-Quinn information criterion (HQIC), Anderson Darling (AD), Cramér-von Mises Criterion (CVMC), Kolmogorov-Smirnov (KS) statistic, and corresponding p-values. An important aspect to note about the authors' data used to show the new distributions' application is that 109 articles take data from other publications with reference years from 1965 to 2011.

Some of the data used correspond to failure times of mechanical or electrical components, waiting times in banks, survival times due to tuberculosis infection, survival times in cancer patients, strength tests for glass fibers, number of deaths from vehicle accidents, fatigue times of 6061 T6 Aluminum Coupons, wind speed measured at 20 m height,

remission times in cancer patients, tension at break of carbon fibers, GDP growth (% per year), nicotine measurements, equipment or device failure rate, fatigue fracture, monthly tax income, sports, assess the risks associated with earthquakes that occur near a nuclear power plant (distances, in miles, to the nuclear power plant and the epicenter of the earthquake), call times, average annual growth rate of carbon dioxide, maximum annual flood discharges, average maximum daily rainfall for 30 years, vehicular traffic, lifespan (in km) of front disk brake pads on randomly selected cars, marital status and divorce rates, and length of relief times of patients who received an analgesic. Consider that each of the models proposed in this database will serve as a possible model to others available through the literature to model another real-life data set.

One of the main characteristics of the new distributions or generalizations is the number of parameters added to the model to provide greater flexibility in modeling specific applications or data. Table 6 shows the name and number of parameters in each of the models proposed in the 131 articles analyzed. As can be seen in the table, 9.2% of the distributions only consider two parameters, 45% work with three parameters, 35.1% consider four parameters, 8.4% model with five parameters, and 2.3% (3 articles) are considering a distribution with six parameters, which was proposed by Handique and Chakraborty, (2017a, 2017b), Yousof et al. (2016), and Jose et al. (2011).

Clearly, from the empirical applications of the models analyzed in this bibliometric study, the results reported by the authors show that the new proposed distributions, which are generalizations of Marshall and Olkin, (1997), produce better results than other models that are already known and widely applied.

Conclusion

The main objective of this manuscript was to present a bibliometric analysis on distribution functions that have been developed from the seminal work of Marshall and Olkin (1997) over twenty-four years from 1997 and 2021. The Bibliometrix package was used through the R software for data mining and analysis and bibliometric network mapping. This process made it possible to identify the main trends and contributions in this line of research.

Two research repositories, Web of Science and Scopus, were used to compile the database of 131 articles. Some of the most relevant findings that contribute to the current literature are the new distributions adding one or two parameters to the baseline models or the previous generalizations. There are distributions where up to six parameters are involved in achieving greater flexibility in the proposed models. The maximum likelihood method is predominant for estimating parameters; in 124 articles, this method is used. However, other methods such as the maximum product spacing, the least-squares method, and the interval estimation method have been used in recent years to estimate parameters. On the other hand, the main topics addressed in the publications are survival function, hazard function, mean residual life, Renyi entropy, moments, moment generating function, quantile function, order statistics, stochastic orderings, and estimation method. In addition, in order to show the advantages of the proposed models, 91% of the analyzed publications carried out simulations and applications to real data to ratify and show the competitiveness of the new distributions that are being constituted.

Finally, we note that more than 90% of the distributions analyzed in this work are generalizations or extensions of models already existing in the literature. Thus, it follows that the different structures that have been used to model distributions will be combined

Table 6 Families of distributions

Author(s)	Distribution	Parameters
Ricardo P.Oliveira et al. (2021)	Bivariate Lindle distributions of Marshall–Olkin type	3
Algarni (2021)	Extended generalized Lindley Distribution (EGLD)	3
Hassan and Nassr (2021)	Marshall–Olkin inverse power Lomax (MOIPL) distribution	4
Eghwerido et al. (2021)	alpha power Marshall–Olkin–G (APMO–G) family of distributions	4
Almetwally et al. (2021)	Marshall–Olkin alpha power Weibull (MOAPW) distribution	4
Shoab et al. (2021)	Marshall–Olkin generalized inverse Lindley (MOGIL)	3
Al-Babtain et al. (2021)	Marshall–Olkin Burr–R (MOB–R) family	3
Wang et al. (2021)	new logarithmic (NL) family	3
Haq et al. (2021)	Marshall–Olkin modified Burr III (MOMBIII) distribution	4
Almongy et al. (2021)	Marshall–Olkin alpha power Lomax (MOAPL) distribution	4
Fawzy et al. (2021)	Marshall–Olkin Rayleigh Lomax (MORL) distribution	3
A. Z. Afify et al. (2021)	Marshall–Olkin odd Burr III–G (MOOB–G) family	4
Ricardo Puziol de Oliveira et al. (2020)	trivariate Marshall–Olkin–Weibull (TMOW) distribution	5
A. Z. Afify and et al. (2020a, 2020b)	Marshall–Olkin transmuted–G (MOT–G) family	3
Almetwally and Haj Ahmad (2020)	Marshall–Olkin Alpha Power Pareto (MOAPP)	3
Tahir et al. (2020)	Kumaraswamy–Weibull (NKwW) distribution	4
Mathew and Chesneau (2020)	Marshall–Olkin LBM (MOLBM) distribution	2
Saboor et al. (2020)	Bivariate Exponentiated Fréchet (BvEF) distribution	4
Al-Moffeh et al. (2020)	generalized Ramos–Louzada (GRL) distribution	2
Khaleel et al. (2020)	Marshall–Olkin Topp Leone–G (MOTL–G) family of distributions	4
R. Bantan et al. (2020a, 2020b)	generalized Marshall–Olkin inverse Lindley (GMOIL) distribution	3
Mathew (2020)	Marshall–Olkin Length Biased Lomax (MOLBL) distribution	3
A. Z. Afify and et al. (2020a, 2020b)	Marshall–Olkin power generalized Weibull (MOPGW) distribution	4
Mondal and Kundu (2020)	absolutely continuous bivariate inverse Weibull (ACBIW) distribution	4
R. A. R. Bantan et al. (2020a, 2020b)	ratio exponentiated general (RE–G) family of distributions	4

Table 6 (continued)

Author(s)	Distribution	Parameters
A. Z. Afify and Alizadeh (2020)	OddD-Lindley (OddDLi) distribution	4
Nwezza and Ugwuowo (2020)	OddD-Weibull (OddDW) distribution	5
V. Garcia et al. (2020)	Marshall-Olkin Gumbel- Lomax (MOG-L) distribution	5
Al-babtain et al. (2020)	generalised Marshall-Olkin exponential (GMOE)	3
Alghamedi et al. (2020)	Marshall-Olkin binomial-exponential2 (MOBE-2) distribution	3
El-Morshedy et al. (2020)	Alpha Power Transformed extended exponential (APTEE) distribution	3
H.,A.,H.,Ahmad and Almetwally (2020)	bivariate Burr X-G (BBX-G) family	4
Gillariose and Tomy (2020)	MO generalized Pareto (MOGP) distribution	3
Da Silva et al. (2020)	MOE power Lomax (MOEPL) distribution	4
Oluyede et al. (2020)	transmuted Marshall-Olkin extended Lomax (TMOELx) distribution	4
Ahmed et al. (2020)	Marshall-Olkin Log-logistic Erlang-Truncated Exponential (MOLLoGETE) distribution	4
Cui et al. (2020)	Topp Leone Marshall Olkin- Weibull (TLMO-W) distribution	4
Khalil and Kamel, (2020)	Marshall Olkin Weibull (NMOW) distribution	3
Raffiq et al. (2020)	Marshall-Olkin generalized Weibull (MOGW) distribution	3
Usman and Ahsan (2020)	Marshall and Olkin inverted Nadarajah-Haghighi (MOINH) distribution	3
Yari et al. (2020)	Marshall-Olkin extended inverted Kumaraswamy (MOEIK) distribution	3
Khosa et al. (2020)	Marshall-Olkin Gompertz Makeham Distribution (MOGM)	5
Ricardo Puziol de Oliveira and Achcar (2020)	new extended-F (NE-F) family	3
Eltehiwy (2020)	bivariate discrete generalized Rayleigh (BDGR) distribution	3
Alqallaf and Kundu, (2020)	Logarithmic inverse Lindley (LIL) distribution	2
Elbatal and Elgarhy (2020)	bivariate inverse generalized exponential (BIGE) distribution	4
Hamdeni and Gasmi (2020)	Kumaraswamy Marshal-Olkin length-biased exponential (KMOLBE) distribution	4
Eliwa and El-Morshedy, (2020)	Marshall-Olkin generalized defective Gompertz distribution (MO-GDGD)	4
Rondero-Guerrero et al. (2020)	bivariate discrete inverse Weibull (BDsIW) distribution	4
	Generalized Potenciada Uniform Distribution (GPUD)	3

Table 6 (continued)

Author(s)	Distribution	Parameters
Hussain et al. (2019)	Exponential Negative Binomial (ENB-X) family of distributions	5
Jayakumar and Sankaran, (2019a)	truncated Discrete Linnik Weibull (DLW) distribution	5
Javed et al. (2019)	Marshall-Olkin Kappa (MOK) distribution	4
Handique et al. (2019)	The Exponentiated Generalized Marshall-Olkin (EGMO-G) family of distribution	4
M.,Korkmaz et al. (2019a, 2019b)	Weibull Marshall-Olkin-G (WMO-G) family	3
Kundu and Nekoukhou (2019)	bivariate discrete Weibull (BDW) distribution	4
Tablada and Cordeiro (2019)	beta Marshall-Olkin Lomax (BMOL) distribution	4
Ghosh et al. (2019)	unit-Marshall-Olkin extended exponential (UMOEE)	2
Nassar et al. (2019)	Marshall-Olkin alpha power (MOAP) family	2
George and Thobias (2019)	Kumaraswamy Marshall-Olkin-Exponential (KwMO-E) distribution	4
Haq et al. (2019)	Marshall-Olkin length-biased exponential (MOLBE) distribution	2
Shahen et al. (2019)	bivariate exponentiated Modified Weibull (BEMW) distribution	4
Mansoor et al. (2019)	Marshall-Olkin Logistic-Exponential (MOLE) distribution	3
Basheer (2019)	Marshall Olkin alpha power inverse exponential (MOAPIE) distribution	3
Cordeiro Prataiviera et al. (2019)	MOE-Flexible Weibull (MOE-FW) distribution	4
Krishnan and George (2019)	Marshall-Olkin Weibull truncated negative binomial(MOWTNB) distribution	4
Jayakumar and Sankaran (2019b)	Exponential intervened Poisson (EIP) distribution	3
Marinho et al. (2019)	Nadarajah-Haghighi geometric (NHG) distribution	3
Khalil et al. (2019)	Burr X exponentiated Weibull (BrXEW) model	3
Cordeiro, Mansoor et al. (2019)	Harris extended Lindley (HEL) distribution	3
Shalabi (2019)	bivariate generalized Lindley (BGL) distribution	2
Jamal et al. (2019)	Marshall-Olkin Odd Lindley G family of distributions (MOOL-G)	3
Jayakumar and Sankaran (2018)	truncated discrete Mittag-Leffler family of distributions	2
Shakhatreh (2018)	extended log-logistic (ELL) distribution	3
Balakrishnan et al. (2018)	Marshall-Olkin generalized exponential (MOGE) models	3

Table 6 (continued)

Author(s)	Distribution	Parameters
M.,Ç.,Korkmaz et al. (2018)	Marshall-Olkin Generalized G Poisson family	3
Barriga et al. (2018)	Marshall-Olkin generalized gamma (MOGG) distribution	4
Mansour et al. (2018)	Exponentiated Marshall-Olkin Fréchet (EMOFr) distribution	5
A. Z. Afify et al. (2018)	Marshall-Olkin additive Weibull (MOAW) distribution	5
Cakmakyapan et al. (2018)	Kumaraswamy Marshall-Olkin Log-Logistic (KMOLL) distribution	5
Yousof et al. (2018)	Marshall-Olkin generalized-G (MOG-G) family	3
Handique and Chakraborty (2017a)	Beta Kumaraswamy Marshall-Olkin-G (BKwMO-G) family of distributions	5
Handique and Chakraborty (2017b)	Beta Generalized Marshall-Olkin Kumaraswamy-G (BGMOKw-G) family of distribution	6
Benkhalifa (2017)	Marshall-Olkin extended generalized Lindley (MOEGL) distribution	3
Yaghoobzadeh (2017)	Generalized Marshall-Olkin Gompertz (GMOG) distribution	4
Jayakumar and Sankaran (2017)	Generalized Exponential Truncated Negative Binomial (GETNB) distribution	4
Rocha et al. (2017)	Marshall Olkin-extended Weibull (MOeW) distributions	3
Dey et al. (2017)	Alpha power transformed Weibull (APTW) distribution	3
MirMostafae et al. (2017)	Marshall-Olkin extended generalized Rayleigh (MOEGR) distribution	3
Cordeiro et al. (2017)	Marshall-Olkin exponentiated Burr XII (MOEBXII) distribution	4
Kundu and Gupta (2017)	bivariate inverse Weibull (BIW) distribution	4
Handique et al. (2017)	Marshall-Olkin Kumaraswamy-G (MOKw-G) family of distributions	3
Jamal et al. (2017)	Marshall-Olkin Burr X (MOBX) family	4
Alizadeh et al. (2017a, 2017b)	odd log-logistic Marshall-Olkin-Lindley (OLLMO-L) distribution	3
H.,H.,Ahmad et al. (2017)	Marshall-Olkin Extended Weibull distribution (MOEW)	3
Alizadeh, MirMostafae et al. (2017)	odd log-logistic Marshall-Olkin power Lindley (OLLMO-PL) distribution	4
I.,E.,Okorie et al. (2017a, 2017b)	Modified Power function (MPF) distribution	2
Idika E.,Okorie et al. (2017a, 2017b)	Marshall-Olkin generalized Erlang-truncated exponential (MOGETE) distribution	3
Alawadhi et al. (2016)	Marshall-Olkin extended two-parameter bathtub (MOETPBT) distribution	3
Castellares and Lemonte (2016)	Marshall-Olkin extended Kumaraswamy (MOE-Kw) distribution	3

Table 6 (continued)

Author(s)	Distribution	Parameters
Alshangiti et al. (2016)	extended generalized inverted exponential distribution (EGIED)	3
V.,J.,García et al. (2016)	Marshall–Olkin lognormal distribution (MOLN)	3
Okasha and Kayid (2016)	M–O generalized linear exponential (M–OGLE) distribution	4
Rocha et al. (2016)	Marshall–Olkin Gompertz distribution	2
Saboor and Pogany (2016)	Marshall–Olkin inverse Gaussian distribution	3
Lemonte et al. (2016)	Marshall–Olkin variant of the Provoist gamma–Weibull distribution (MOP _g W)	4
Yousof et al. (2016)	Marshall–Olkin Nadarajah–Haghighi (MONH) distribution	3
El-Bassiouny et al. (2016)	Kumaraswamy transmuted Marshall–Olkin Fréchet (Kw-TMOF) distribution	6
Hamid Bidram et al. (2016)	bivariate exponentiated generalized Weibull–Gompertz distribution (BEGWGD)	3
Kamel et al. (2016)	generalized geometric (EGG) distribution	3
Cordeiro et al. (2016)	Uniform Truncated Negative Binomial (UTNB) distribution	3
W. M. Afify (2016)	Kumaraswamy exponential–Weibull (KwEW) distribution	5
Jayakumar and Sankaran, (2016)	Marshall–Olkin flexible Weibull distribution	3
Alizadeh et al. (2015)	Generalised Uniform distribution (GUD)	2
Ristić and Kundu (2015)	beta Marshall–Olkin (BMO) family	4
Pogany et al. (2015)	Marshall–Olkin Generalized Exponential (MOGE) distribution	3
H.,Bidram et al. (2015)	Marshall–Olkin Exponential–Weibull (MOEW) distribution	4
Jayakumar and Girish Babu (2015)	extended exponentiated Weibull (EEW) distribution	4
Alshangiti et al. (2014)	Generalized Symmetric Double Weibull (GSDW) distribution	4
Santos-Neto et al. (2014)	M–O extended modified Weibull distributions (M-OEMW)	4
Krishna et al. (2013)	The Marshall–Olkin extended Weibull (MOEW) family of distributions	3
Gui (2013)	Marshall–Olkin Fréchet Distribution (MOFR)	3
Nadarajah et al. (2013)	Marshall–Olkin Log-Logistic distribution (MOLLDD)	3
Lemonte, (2013)	exponential-truncated negative binomial (ETNB) distribution	3
	Marshall–Olkin extended Birnbaum–Saunders distribution (MOEBS)	3

Table 6 (continued)

Author(s)	Distribution	Parameters
Jose et al. (2014)	Marshall–Olkin Extended Exponential distribution (MOEE)	2
Jamalizadeh and Kundu, (2013)	weighted Marshall–Olkin bivariate exponential (WMOBE) distribution	4
Jose et al. (2011)	type 2 Marshall–Olkin bivariate Weibull distribution	6
Jose et al. (2010)	Marshall–Olkin q-Weibull distribution (MO-q-W)	4
Jayakumar and Mathew (2008)	Marshall–Olkin semi-Burr (MOSB) distribution	3
Sarhan and Balakrishnan (2007)	new bivariate distribution (NBD)	2
Ghitany et al. (2007)	Marshall–Olkin extended Lomax (MOEL) distribution	3
Yeh (2004)	Marshall–Olkin type multivariate Pareto distributions (GMOP)	2,3,4

or expanded, and new models will be developed that will make it possible to analyze the behavior of different data sets related to real-world problems.

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