

Performance enhancement of the power penalty in DWDM FSO communication using DPPM and OOK modulation

Ebrahim Eld. Elsayed1 · Bedir B. Yousif2 · Mahmoud M. Alzalabani1

Received: 16 December 2017 / Accepted: 22 May 2018 / Published online: 26 June 2018 © Springer Science+Business Media, LLC, part of Springer Nature 2018

Abstract

This paper presents the design and performance enhancement of the power penalty (PP) in a dense wavelength division multiplexing based on free space optical communication (FSOC) link using digital pulse position modulation (DPPM) and on–of keying (OOK) modulation. Such a system has a high performance, low cost, robust and power efficient, reliable, excessive fexibility, and higher data rate for access networks. The system performance is evaluated for an 8-channel wavelength-division-multiplexing for hybrid fber FSOC system at 2.5 Gbps on widely accepted modulation schemes under various atmospheric turbulence (AT) regimes conditions. The performance of system is introduced in terms of PP, bit-error rate (BER), transmission distance and the average received optical power. The numerical results shows that the improvement of the PP using DPPM modulation of 0.2–3.0 dB for weak turbulence (WT) regimes for BER of 10^{-6} and above 20, 25 dB for strong turbulence (ST) regimes are reported for BER of 10^{-6} and 10^{-9} , as respectively (depending on the AT level). Further, we develop of improvement the PP caused by multiple-access interference about 6.686 dB which is predicted for target BER of 10−9 in WT and 1 dB at target BER of 10−6 in ST when the 8 user are active on the system of optical network units. Additionally, the optical power budget and margin losses of a system are calculated with diferent link length. The proposed approach of DPPM merges superiority with higher enhancement of PP about 0.8 dB for BER equal 10−9 at FSO link length l_{fso} =2000 m compared to OOK at 1 dB for WT. An improvement of 2 dB is observed using the DPPM scheme over an OOK due to capability of detect pulses under background noise conditions with increased receiver sensitivity.

Keywords Atmospheric turbulence (AT) · FSO communication (FSOC) · DWDM · Power penalty $(PP) \cdot DPPM \cdot Outage$ probability $(OUP) \cdot Amplified$ spontaneous emission (ASE)

 \boxtimes Ebrahim Eld. Elsayed engebrahem16@gmail.com

Electronic supplementary material The online version of this article [\(https://doi.org/10.1007/s1108](https://doi.org/10.1007/s11082-018-1508-y) [2-018-1508-y\)](https://doi.org/10.1007/s11082-018-1508-y) contains supplementary material, which is available to authorized users.

Extended author information available on the last page of the article

1 Introduction

Although linking communication in free space optical (FSO) spectrum instead of the radio one allows ignoring license requirements, improving security, and transmitting data with a broad spectrum, optical technologies carrier can have access to a good network where they could potentially provide huge bandwidth but it sufers from fuctuations in temperature and pressure that occur in the atmosphere regularly (Chan [2006](#page-33-0); Shapiro and Harney [1980](#page-34-0)). Free-space optical communication (FSOC) includes many improvements as an opportunity to defeat the limitation in capacity of radio frequency (RF) , such as easy-to-install, difficult to intercept and license-free. As a result the FSOC performance is even restricted for deep-distance links owing to these obstacles. FSOC using a dense-wavelength-division multiplexing (DWDM) can enhance the number of channels with support from a performance high capacity to reach (32 channel \times 40 Gbps) and are easy to increase a data rate into the FSO for the long-distance data transmission (Ciaramella et al. [2009\)](#page-33-1). FSOC, it is a realistic proposition, which construct a wavelength-division multiplexing (WDM) optical access networks (OAN) in the distribution link since both optical fber (OF) and FSO systems adopt an identical transmission wavelengths and network components (Ciaramella et al. [2009](#page-33-1)). There are three types of WDM that are commonly used: coarse WDM (CWDM), dense WDM (DWDM) and broadband WDM. DWDM is a new technology which multiplexes multiples (optical carrier signals) over a singular medium by applying diferent signals with huge channel capacity and the wavelength range from 1539 to 1565 nm is the most commonly located in conventional band (C-band) and contribute in reducing bandwidth usage and can support capacity to reach Terabits per second and are easily to increase a data rate into the FSO (Ciaramella et al. [2009](#page-33-1)). The feasibility of WDM FSO networks has been demonstrated experimentally. Passive-optical networks (PON) are the most important competitors for the OAN, where the general network replace the copper on the basis of network access technologies (Karp et al. [1988](#page-33-2); Ramaswami and Sivarajan [2002](#page-34-1)).

DWDM is the next generation of dissemination of hybrid fber FSOC (HFFSOC) based access network which ofers higher bandwidth (Manor and Arnon [2003;](#page-34-2) Arnon [2003\)](#page-33-3). A common spacing in DWDM is 25, 50, 100, or 200 GHz with channel count leading up to 128 or higher channels at distances of several thousand kilometers from the amplifcation and regeneration along such a routing. For each optical network unit (ONU), a fxed wavelengths is installed in DWDM-PON and thus a high transfer bandwidth available more full utilize of the in the optical domain (Ansari and Zhang [2013](#page-33-4); Zuo and Phillips [2009](#page-34-3)). DWDM-PON systems ofer greater security and increase bandwidth and less loss compared to time division multiplexing/multiple access (TDM/TDMA) (Ciaramella et al. [2009](#page-33-1); Aladeloba et al. [2013](#page-33-5); Killinger [2002](#page-34-4); Monroy and Tangdiongga [2002](#page-34-5)). Optical amplifer (OA) is important is according to the deep-distances in the free space optics. WDM systems is well reported an Interchannel Crosstalk (ICC) in Ramaswami and Sivarajan [\(2002\)](#page-34-1). The efects of atmospheric turbulence (AT) accentuated ICC have been investigated in for WDM FSO network (Aladeloba et al. [2013\)](#page-33-5).

When the signal pathways and crosstalk are turbulent independently beyond being physically quite specifc so that mutual strength may close tentatively or even considerably exceeds the signal strength in spite of the long-time average signal (LTAS) to crosstalk ratio that resulted a turbulence accentuation of ICC. On–off keying (OOK) and digital pulse position modulation (DPPM) are the most modulation format of AT using intensity of photon. DPPM one concerning the modulation method has supreme power efficiency compared according to OOK (Aladeloba et al. [2012a](#page-33-6), [b,](#page-33-7) [c](#page-33-8); Aldibbiat et al. [2005](#page-33-9); Ghassemlooy et al. [2013](#page-33-10)). It has been successfully implemented in the OF, satellite, terrestrial for FSO and deep space optical communication. These profts come at the expenditure of higher channel bandwidth demands. DPPM has with success been applied in OF, inter-satellite and deep FSOC and could be a robust competition for terrestrial FSO network (Ghassemlooy et al. [2013](#page-33-10); Phillips et al. [1996](#page-34-6)). Several researches show that DPPM is ftted to FSOC systems wherever dispersion is negligible and it's a lot of power efective schemes compared to OOK (Aladeloba et al. [2012a](#page-33-6), [b,](#page-33-7) [c;](#page-33-8) Ghassemlooy et al. [2013\)](#page-33-10). DPPM offer a better error rate performance and a good average received optical power (AROP) requirement efficiency that is critical in obliging with eye safety limitations (Aldibbiat et al. [2005](#page-33-9); Ghassemlooy et al. [2013](#page-33-10)). DPPM satisfes its merits but however at the cost of a bandwidth expansion. Development of the PON idea and a variety of architectures are viable in DWDM. Diferent wavelengths from several laser light sources in the system raise the problem optical ICC. In DWDM PON, ICC and naturally, unless the wavelength narrow spacing in particular, it will feature a purely amount of contribution to the intensities and no interferometric contribution. Optical amplifers (OAs) are required for the long haul FSO propagation distances. The optical amplifers improve the strength of signal on the cost of an amplifed spontaneous emission (ASE) noise that limits the system performance (Abtahi et al. [2006\)](#page-33-11).

The reminder paper is structured as follows. Section [2](#page-2-0) illustrated the network structure and architecture for DWDM-PON/HFFSOC. Section [3](#page-4-0) assessed the AT channel modeling. Section [4](#page-5-0) introduces the bit-error rate (BER) analysis. Section [5](#page-8-0) presents the BER evaluations for DWDM-PON/HFFSOC systems. The numerical results are presented and discussed in Sect. [6.](#page-16-0) Section [7](#page-28-0) discusses the validations of power penalty compared to the other published papers. Finally, further discussions, conclusions and the future work of research are presented in Sect. [8.](#page-30-0)

2 Network structure and architecture

Figure [1](#page-3-0) shows a schematic representation of the planned DWDM-PON based HFFSOC system. The network components encompass a transmitter module which involves of laser for optical signal (OS) generation, a laser driver (LD) and the input data signal and DPPM modulator (DPPM Mod) and receiver modulator with created of a photodetector (PD), flter, and feeder fber, OA, electrical amplifer (EA), and the comparator circuit (CC) for system decision. Dynamic tracking of a threshold is not needed with DPPM, unlike for some OOK systems. DWDM-PON/HFFSOC relies on multiplexing of the user on incorporating fber infrastructure employing a specifc wavelength for every terminal. This approach creates a virtual link from a point-to-point (POP), which permits full duplex communication with optical bit rates severally of the traffic induced by different users. An erbium doped-fiber amplifier (EDFA) with multihop DWDM/relaying are employed for long-distance from the optical line terminator (OLT) to the ONU. Due to the physical of the perfection of demultiplexer (demux) in OLT to move upstream or each Remote Node (RN) for the transfer of downstream an ICC occurs. The efect of AT-emerged ICC in DWDM-PON incorporated with HFFSO a network was investigated in Monroy and Tangdiongga [\(2002](#page-34-5)). In upstream functional system (UFS) diagram where the ONU transmitter for each transmit OS on wavelengths $\lambda_1, \lambda_2, \lambda_N$, where *N* is the ONU numbers corresponding toward the diameter D_{RX} of Receiver Collecting Lenses (RCLs) at the RN and consist of an Optical Band-Pass Filter (OBPF) as shown in Fig. [1a](#page-3-0). Each ONU in the UFS has a dedicated independent POP data link to the OLT with a specifc fxed optical wavelength as shown in Fig. [1a](#page-3-0). In the downstream functional system (DFS) diagram, *N* separates transmitter applying to each ONU on a specifc wavelength a POP fashion as shown in Fig. [1](#page-3-0)b. However,

Fig. 1 A proposed DWDM-PON based hybrid fber FSOC (HFFSCOC)system for the fnal distribution stage, with an OA located at the RN (Case A) or at the OLT demux input (Case B). ONUs will be distributed at diferent angles around the RN **a** Upstream functional system diagram, **b** Downstream functional system diagram, **c** Downstream transmission system (DTS) diagram and **d** Upstream transmission system (UTS) diagram

to reduce fber nonlinearity, then maximum OLT transmits a power lower than 10 dBm. To restrict background ambient light the downstream collecting lens (CLs) can also include an OBPF as shown in Fig. [1b](#page-3-0), while the demux naturally performs the OBPF within the upstream direction. Downstream ICC resulted from the imperfection of the RN demux, but this is not emerged by the AT. Thus, the technique is intensity modulated/direct detection (IM/DD) signal is obtained directly. The downstream transmission system (DTS) diagram RCLs may include an OBPF shown in Fig. [1c](#page-3-0) to limit background surround light, while the demux inherently precedes the OBPF in the upstream direction. The properties of the CLs used in the tracking and pointing subsystem would vary depending on the FSO link length. In the upstream transmission system diagram (UTS), each ONU has a dedicated specifc laser fxed wavelength for a POP optical link to the OLT as illustrated in Fig. [1d](#page-3-0). Depending on the FSO link length we choose the suitable lenses in the tracking and pointing subsystem. We use the optimal threshold, frequency spacing and optical wavelengths in OOK modulation of our calculations at the same assumptions for the downstream and upstream transmission. A fber collimator is used to couples arranged wavelength from each RN RCL through a short length of fber as in Abtahi et al. [\(2006](#page-33-11)) to the Multiplexer (mux). To enhance the signal power through the OF an optical preamplifer of Noise Figure (NF) and Gain (G) can be placed at the RN output. By using an automatic tracking and pointing system, the transmitter divergence angle (TxDA) can be narrowed dimension enough with divergence angle≪1 mrad to achieve the alignment with adjusting the focal lengths and position of the lenses, which allows a collect larger proportion of transmitted power and secure transmission.

3 Atmospheric turbulence channel modeling

Atmospheric scintillation takes place due to the heat diference between the earth's surface and pressure caused refractive index variations of the atmosphere along the data link channel, leading to speedy change of the received signal, divergence in degree of continuity of the OS and too insufficient BER. These implements of conflict, weak, moderate, and strong are described utilizing the Probability Density Function (pdf) of Gamma–Gamma (GG) and given as (Andrews et al. [2001](#page-33-12); Andrews and Phillips [2005;](#page-33-13) Majumdar [2005](#page-34-7); Khalighi et al. [2009;](#page-34-8) Al-Habash et al. [2001](#page-33-14))

$$
p_{GG}(h_Z) = \frac{2(\alpha\beta)^{(\alpha+\beta)/2}}{\Gamma(\alpha)\Gamma(\beta)} h_Z^{((\alpha+\beta)/2)-1} K_{\alpha-\beta} \left(2\sqrt{\alpha\beta h_Z}\right); \quad h_Z > 0,
$$
 (1)

where $h_z = h_d$ or h_i is the attenuation owing to AT for the required signal (h_{sig}) or interfere (h_{int}) , α and β are the effective quantity of large and small scale eddies due to the scattering process respectively, $K_n(\cdot)$ is a modified Bessel Function (MBF) (second kind, order *n*), and $\Gamma(\cdot)$ is the Gamma function. The signal and interferer (SAI) travels independently over physically separate pathways in the UTS and then have uncorrelated disturbance; hence, their GG pdfs are each dealt with independently. The parameter α and β are given as (Andrews et al. [2001](#page-33-12); Andrews and Phillips [2005](#page-33-13); Majumdar [2005;](#page-34-7) Khalighi et al. [2009;](#page-34-8) Al-Habash et al. [2001](#page-33-14))

$$
\alpha = \left\{ \exp \left[\frac{0.49 \sigma_R^2}{\left(1 + 0.65 \, d^2 + 1.11 \sigma_R^{12/5} \right)^{7/6}} \right] - 1 \right\}^{-1},\tag{2}
$$

 \mathcal{D} Springer

$$
\beta = \left\{ \exp \left[\frac{0.51\sigma_R^2 \left(1 + 0.69\sigma_R^{12/5} \right)^{-5/6}}{1 + 0.9d^2 + 0.62d^2\sigma_R^{12/5}} \right] - 1 \right\}^{-1},\tag{3}
$$

$$
d = \sqrt{kD_{RX}^2 / 4l_{fso}} \tag{4}
$$

where d is the normalized RCLs, C_n^2 is the refractive index structure (RINS) parameter (ranging from $\approx 1 \times 10^{-17}$ m^{-2/3} to $\approx 1 \times 10^{-13}$ m^{-2/3}), l_{fso} is the FSO channel length, $k = 2\pi/\lambda$ is the wave number and λ is the wavelength are given as Andrews and Phillips ([2005\)](#page-33-13), Majumdar [\(2005](#page-34-7)), Khalighi et al. ([2009\)](#page-34-8) and Al-Habash et al. ([2001\)](#page-33-14). Table [1](#page-5-1) presents the turbulence conditions regimes for FSO link length $(l_{fso}) = 1000$ m come from C_n^2 . The Rytov variance (RVAR) distinguishes the various link turbulence regimes σ_R^2 , if the resulting $\sigma_R^2 < 1$, we have weak turbulence (WT); if $\sigma_R^2 \approx 1$, we have Moderate Turbulence (MT) and if $\sigma_R^2 > 1$; we have strong turbulence (ST), and if saturated turbulence $\sigma_R^2 \to \infty$ are given as from (Andrews and Phillips [2005;](#page-33-13) Khalighi et al. [2009](#page-34-8))

$$
\sigma_R^2 = 1.23 \, C_n^2 \, k^{7/6} l_{\text{fso}}^{11/6} \tag{5}
$$

4 Bit error rate (BER) analysis

The BERs conditional under the hypothesis of separate signal and ICC for UTS and DTS, the average turbulence which accentuated ICC BER of given specifc transmitter powers for the OS and ICC (Aladeloba et al. [2013\)](#page-33-5)

$$
\overline{BER} = \int_0^\infty \int_0^\infty BER\left(h_{sig}, h_{int}\right) p_{GG, sig}\left(h_{sig}\right) p_{GG, int}\left(h_{int}\right) dh_{sig} dh_{int},\tag{6}
$$

where $p_{GG,sig}(h_{sig})$ and $p_{GG,int}(h_{int})$ are respectively, the SAI GG-pdfs each with various value α , β and σ_R^2 as written in Manor and Arnon ([2003\)](#page-34-2), Phillips et al. ([1996\)](#page-34-6), Abtahi et al. ([2006\)](#page-33-11) and Andrews et al. ([2001\)](#page-33-12). Using Gaussian beam approximation (GBA) methods, the BER dependent on (h_{sig}) and (h_{int}) for UTS with single ICC (Aladeloba et al. [2013\)](#page-33-5)

$$
BER(h_{sig}, h_{int}) = \frac{1}{4} erfc\left(\frac{Q(h_{sig}, h_{int})}{\sqrt{2}}\right)
$$
 (7)

$$
Q(h_{sig}, h_{int}) = \frac{i_{1,0}(h_{sig}, h_{int}) - i_{0,1}(h_{sig}, h_{int})}{\sigma_{1,0}(h_{sig}, h_{int}) + \sigma_{0,1}(h_{sig}, h_{int})}
$$
(8)

$$
i_{d_{sig}} d_{int}(h_{sig}, h_{int}) = i_{d_{sig}} (h_{sig}) + i_{d_{int}} (h_{int})
$$
 (9)

where $i_{d_{sig}, d_{int}}(h_{sig}, h_{int})$ is the outputs for signal $(d_{sig} = zero \text{ or one})$ and interferer $(d_{int} =$ zero or one) of decision circuit (DC). where $i_{d_{sig}, d_{int}}(h_{sig}, h_{int})$ is the resulting signal $i_{d_{sig}}(h_{sig}) + i_{d_{int}}(h_{int}) = (d_{sig} =$ zero or one) and interferer $(d_{int} =$ zero or one) current at the DC are written as (Aladeloba et al. [2013\)](#page-33-5), $i_{d_{sig}}(h_{sig}) = \alpha d_{sig} R P_{R, sig}(h_{sig})$ and $i_{d_{int}}(h_{int}) = \alpha d_{int} RP_{R,int}(h_{int})$ is SAI current for data one and zero, are, respectively. $P_{R,sig}$ and $P_{\text{R int}}$ are the instantaneous and interferer AROP, respectively. *r* is the extinction ratio and $R = \eta q / E$ is the responsivity (in A/W), η is the PD quantum efficiency, q is the electron charge, $E = h\nu$ is the photon energy, *h* is Planck's constant and ν is the optical frequency. The total OLT Thermal Receiver Noise Variance (TRNVAR) $\sigma_{d_{sig}, d_{int}}^2$ is the summa-

tion of the shot noise signal, amplifed spontaneous emission (ASE) shot noise, signal-ASE Beat Noise (ASEBN), and ASE–ASE beat noise variance, given respectively in Eqs. ([10](#page-6-0)–[13](#page-6-1)). An integrate-and-dump receiver is assumed at the DC with electrical bandwidth $B_e = 1/2 T_b$, $T_b = 1/ R_b$ and R_b is the data rate, $B_e = R_b/2$, m_t is ASE noise polarization states and ASE Noise (ASEN) Power Spectral Density (PSD) in a single ploarization state. B_0 is the optical bandwidth:

$$
\sigma_{\text{shot-d}_{\text{sig}},d_{\text{int}}}^{2} = 2q i_{d_{\text{sig}},d_{\text{int}}}(h_{\text{sig}},h_{\text{int}})B_{e}, \qquad (10)
$$

$$
\sigma_{shot,ASE}^2 = 2m_t B_o N_o q R B_e, \qquad (11)
$$

$$
\sigma_{\rm sig-d_{\rm sig},d_{\rm int}-ASE}^2 = 4\text{RN}_\circ i_{\rm d_{\rm sig},d_{\rm int}}(h_{\rm sig}, h_{\rm int})B_{\rm e},\tag{12}
$$

$$
\sigma_{ASE-ASE}^2 = 2m_t R^2 N_o^2 B_o B_e. \tag{13}
$$

4.1 Upstream transmission system

For the overall performance evaluations, it is assumed to have signal multiplexer/demultiplexer losses L_{mix} and L_{demux} (\leq 3.5 dB) (Monroy and Tangdiongga [2002](#page-34-5)), a contiguous-channel additive loss $L_{\text{max.contiguous}}$ (typically > 30 dB), and non-a contiguous-channel additive loss $L_{\text{mix,non-contionous}}$ (generally > 35 dB). Equations $(6-13)$ $(6-13)$ $(6-13)$, can be employed for the system of specifc computations. The Single Crosstalk (SC) channel is relevant a predominant interferer occurs (e.g., in some slightly DWDM network). There is also the probability of systems where some transportation channel is FSOC and OF. At PDs of the OLT photodiodes for the required SAI is given for the AROP, respectively, by equation written in (Aladeloba et al. [2013](#page-33-5))

$$
P_d(h_d) = GP_{u_{T,d}} h_d L_{fso,d} L_{bs,d} n_{c,d} L_{\text{mu}x} L_{fiber} L_{\text{demux}},\tag{14}
$$

 \mathcal{D} Springer

$$
P_i(h_i) = GP_{u_{T,i}} h_i L_{fso,i} L_{bs,i} \eta_{c,i} L_{max} L_{fiber} L_{demux} L_{demux,XT},
$$
\n(15)

where G is gain optical amplifier, $L_{demux,XT}$ is the crosstalk (XT) i.e. additional losses (above L_{demux}) the interferer has when connected onto the OS photodiode by the demuliplexer. $P_{u_{T,d}}$ and $P_{u_{T,i}}$ are the signal and interferer of ONU transmitting powers, respectively

$$
L_{\text{fso}} = 10^{(-\alpha_{\text{fso}} l_{\text{fso}}/10)}\tag{16}
$$

$$
L_{fiber} = 10^{(-\alpha_{fiber}I_{fiber}/10)}\tag{17}
$$

where L_{fso} and L_{fiber} (OFL) are the FSO and OF Losses where α_{fiber} and α_{fso} are the attenuation coefficients of OF and FSO, respectively, (in dB/km). l_{fiber} is the channel length for OF in (km). The nominal demux loss $L_{demux}/$ multiplexer (mux) loss L_{max} is about 3.5 dB (Monroy and Tangdiongga 2002), while the interferer's demux loss $L_{\text{demux,XT}}$ is the other loss that interferer experiences upon connecting to the required signal wavelength port, and also defines the signal-to-crosstalk ratio (C_{XT}) (in the case when the input signal power (SIGP) and crosstalk power (CXTP) are corresponding. Under weather conditions, signal attenuation is higher intense and the FSOC length is limited. The beam spreading loss L_{bc} in the FSOC link for the desired SAI can be calculated from (Andrews and Phillips [2005;](#page-33-13) Majumdar [2005\)](#page-34-7)

$$
L_{bs} = \left(\frac{D_{RX}}{\theta l_{fso}}\right)^2\tag{18}
$$

and η_c is the coupling loss for both the SAI is determined from Dikmelik and Davidson ([2005\)](#page-33-15). In the UTS Case A, the obtained ASEN PSD in the single polarization state at the photodiode can be written as $N_{\text{o}}/A = 0.5 (NFG - 1) h v L_{\text{fiber}} L_{\text{demux}}$ where *G* and *NF* are the OA gain and noise figure, respectively. Various qualities of N_{\circ} rise depending on the OA stand, while in Case B, the collected ASEN PSD as can be written as $N_{\circ} = N_{\circ OA} L_{\text{demux}, XT}.$

4.2 Downstream transmission system

The downstream ICC is not emphasized disturbance, as rejecting wavelength change shape on σ_R^2 it passes through the same atmospheric direction as the signal. In the DTS Case A, the received ASEN in the original emission state at the PD is expressed as N_{\circ} _{*OA*} = 0.5 (*NFG* – 1) $h \nu L_{demux} L_{fso} L_{bs}$, but in Case B, the obtained ASEN PSD, it is given as $N_0 = N_0 O_A L_{demux, XT}$ (Aladeloba et al. [2013](#page-33-5)). The AROP at the ONU photodiodes for required SAI is presented, respectively, as written in (Aladeloba et al. [2013;](#page-33-5) Mbah et al. [2016\)](#page-34-9)

$$
P_{d_{R, sig}}(h_Z) = GP_{d_{T,d}} h_Z L_{fso} L_{bs} L_{muX} L_{fiber} L_{demux}
$$
\n(19)

$$
P_{i_{R,in}}(h_Z) = GP_{d_{T,i}} h_Z L_{fso} L_{bs} L_{muX} L_{fiber} L_{demux} L_{demux,XT}
$$
 (20)

where $P_{d_{T,d}}$ and $P_{d_{T,i}}$ are the respective downstream OLT transmitter power of SAI.

5 BER evaluations for hybrid DWDM PON FSOC systems

This section includes evaluations the BER for hybrid DWDM-PON/FSOC in DPPM and OOK modulation. DWDM-FSO technology is a key component of next generation needs designed and simulated to serve as Long Reach Passive Optical Network (LR-PON) for achieving higher rate, immense capability, and allows operators to deliver high information measure to multiple using one wavelength of upstream transmission and another wavelength for upstream transmission. DWDM PON is linked a multi-wavelengths optical line terminator to optical network units over an interconnecting OF system. The optical line terminator is one of the foremost necessary of the network. It provides an interface between core network and PON network. OA positioning with two other sources of amplifer location is Case A at RN and at the OLT Case B. In the UST Case A, the ASEN expertise loss owing to feeder OF attenuation and OLT demux loss, while in the UST Case B, the ASEN sufers from OLT demux losses in OLT only. In some Cases the position of the UST OA may also no longer do enough distinction to the overall performance, considering that the optical signal-to-noise ratio (OSNR) range by way of only approximately 4 dB among Case A and Case B (for 20 km OF). In the DTS Case A, the ASEN sufers RN demux losses, AT power loss, and beam divergence spreading loss, while in the DTS Case B, the ASEN moreover experiences OF attenuation feeder fber. ONU is access services. For both DTS and UTS areas directions, the OLT connected with ONUs via *N* intermediate relays $(R_i, i=1, 2... N)$ $(R_i, i=1, 2... N)$ $(R_i, i=1, 2... N)$, together with RN. Table 2 is a key parameter used in the calculations (Aladeloba et al. [2013;](#page-33-5) Mbah et al. [2016\)](#page-34-9) and [present]. Forward error correction (FEC) is able to much better performance. Note, however, that the proper relation between the LTAS BER before and after the forward error corrections would take the FEC to enter the analysis, e.g., within Eq. ([6\)](#page-5-2). Dispersion and nonlinear efectiveness at OF are rejected for

	Parameters Description	Values in Aladeloba et al. (2013)	Values in Mbah et al. (2016)	Present work
R _h	Binary data rate	2.5 Gbps	2.5 Gbps	2.5 Gbps
B_{α}	Demux or OBPF channel bandwidth	60 GHz	76 GHz	60 GHz
λ	Desired signal wavelength	1550 nm	1550 nm	1550 nm
θ_{XT}	Transmission divergence angle	0.2 mrad	0.2 mrad	0.2 mrad
D_{RX}	Receiver Cls diameter	13 mm	13 mm	17 mm [Present]
\mathbf{r}	Extinction ratio	10dB	10dB	10dB
η	Quantum efficiency	0.8	0.8	1 [Present]
NF	Amplifier noise figure	4.77 dB	4.77 dB	4.77 dB
$l_{\rm fso}$	Maximum FSO link length	2 km	2 km	4 km [Present]
l_{fiber}	Feeder fiber length	$20 \mathrm{km}$	$20 \mathrm{km}$	$20 \mathrm{km}$
α_{fiber}	Feeder fiber attenuation	0.2 dB/km	0.2 dB/km	0.2 dB/km
$\alpha_{\rm fso}$	Atmospheric channel attenuation [clear air]	0.2 dB/km	0.2 dB/km	0.2 dB/km
m_{t}	ASE noise polarization states	2	\overline{c}	2
G	Optical preamplifier gain	30 dB	30 dB	30 dB
L_{demux}	Signal mux/demux loss	3.5 dB	3.5 dB	3.5 dB

Table 2 Key parameters used in the calculations

a 20 km feeder, only particularly minor Power Penalties (PP). The RCL diameter option (13 mm) well reported in Aladeloba et al. ([2013\)](#page-33-5), Mbah et al. ([2016\)](#page-34-9) and Vetelino et al. ([2007\)](#page-34-10) but we assume the RCL diameter (17 mm) is coherent with this work and signal mux/demux loss L_{demux} (3.5 dB) (Monroy and Tangdiongga [2002;](#page-34-5) Lee et al. [2006](#page-34-11)). OOK modulation in DWDM FSOC is the oftenest performance generally used IM/DD. This approach provides an easy implementation and minimum cost (Badar and Jha [2017](#page-33-16)). Seeks to beat the irreducible Error Floors (EFs) of OOK have directed on the study of adaptive detection threshold (ADT). For calculating the require average received power, there is no single equation at a fxed BER by maintaining the BER at a fxed value and restructure the code for fnding the BER to be able to calculate the average power that can give the fxed BER. This can be done using the root fnding technique. Basically to fnd an average power value that will result in a BER value above the fxed BER value and another average power value that will result in a BER value below the fxed BER value. Then use the average power that gave the higher and lower BER values as the upper and lower limit of the root fnding search and then keep dissecting the space in between those two limits until get the approximate average power that can give the fxed BER.

5.1 DPPM crosstalk modeling

The DPPM format is achieving a significant improvement in power efficiency. The DPPM modulation ofers greater channel bandwidth requirements. DWDM DPPM format, is simple case of a single contiguous interferer However, the evaluations accentuated ICC, where, M bits is the frame assigned with the raw DR R_b , are assigned to a frame, where each block of *b* bits is mapped to one of M feasible symbols (s_0, s_1, s_M) where $n=2^M$ equalsized time slots t_s=M/nR_b, where T_b = 1/R_b, where M is referred to as the Coding Level (COL). For illustration, at the binary DR of 2.5 Gbps, DPPM Frames (DPPMF) for $M=2$ include four slots, $t_s = 2$ T_b /4, $t_s = 2/4 \times 2.5$ GHz = 1/5 GHz, each and therefore the pulse in each DPPMF shows a 2-bit word transferred at a slot rate of 5 GHz. For $M=4$ contain = 16 slots shows example of time-waveforms of an OOK Non-Return-to-Zero (NRZ) and the equivalent 16-DPPM signal $(M=4)$ (Mbah et al. [2014\)](#page-34-12). Systems bandwidth increases with rising COL and proper spacing is needed between the wavelengths for operations with signifcant COL, OSs encompass not alone data signal but also background noises and SAI with the AROP of background power P_b and power transmitter P_t int. The Means and Variances (MEAVAR) of the random variables, both are describing the conjunction over the slot that consists of particularly the Signal Pulse (SP), especially Crosstalk Pulse (CP), both SP and CP pulses and no pulses (i.e. empty slot) are determined and, respectively, the general equations for the UTS are derived in $(21–25)$ $(21–25)$, the equations for the DTS are regain by changing the losses due to AT for the required SAI (h_d, h_i) with h_Z written as (Aladeloba et al. [2012a,](#page-33-6) [b](#page-33-7), [c](#page-33-8); Mbah et al. [2014\)](#page-34-12).

$$
\mu_{X_{sig,im}}(h_d, h_i) = \frac{LRqN_o}{t_s} + Gq\left(sigRP_d(h_d) + int R_i P_i(h_i) \right) \tag{21}
$$

$$
\sigma_{X_{sig,int}}^2(h_d, h_i) = \sigma_{th}^2 + \left(\frac{\left(\text{LRq}^2 N_{\circ} \left(1 + \text{LRq}^2 N_{\circ} \right)\right)}{t_s^2}\right) + Gq^2 \left[\begin{array}{c} \left(R + 2R^2 N_{\circ}\right) \frac{\text{sig} P_d(h_d)}{t_s} \\ + \left(R_i + 2R_i^2 N_{\circ,i}\right) \frac{\text{int} P_i(h_i)}{t_s} \end{array}\right] \tag{22}
$$

where sig/int = 0 or 1 relying on the existence of SP/CP pulse in slot. σ_{th}^2 is TRNVAR of DPPM, $L = B_{\circ} m_t t_s$ is the product of temporal and spatial modes (Aladeloba et al. [2012a](#page-33-6), b , [c\)](#page-33-8), B_0 is the demultiplexer or OBPF channel bandwidth, and m_t is the number of ASEN polarization states. The ASEN for PSD in a specifc polarization state at the photodiode is N_o . MEAVAR have been obtained with modifications to account for crosstalk–ASEBN afecting the interferer and the needed signal experiences the same ASEN at the OA output (Aladeloba et al. [2012a](#page-33-6), [b,](#page-33-7) [c\)](#page-33-8)

$$
P_{we(l,r)}(h_d, h_i) \ge \prod_{\substack{j=1 \ j \neq sig \, slot}}^{n} P\left(X_{1,int} > X_j \, | \, h_d, h_i\right) \tag{23}
$$

where Xj is the non-signal slot $X_{0,int}$ contents (Mbah et al. [2014](#page-34-12))

$$
P_{we(l,r)}(h_d, h_i) \le 1 - \left(1 - P\left(X_{0,0} > X_{1,int} \,|\, h_d, h_i\right)\right)^{n-1-(l-r)} 1 - P\left(X_{0,1} > X_{1,int} \,|\, h_d, h_i\right)\right)^{l-r} \tag{24}
$$

Assuming that the random variables $X_{1,int}$ and $X_{0,int}$ are Gaussian, the expression $P(X_{0,int} > X_{1,int} | h_d, h_i)$ using GBA is of the general form (Mbah et al. [2014\)](#page-34-12)

$$
P\left(X_{0,int} > X_{1,int} | h_d, h_i\right) = 0.5erfc\left(\frac{\mu_{X_{1,int}}(h_d, h_i) - \mu_{X_{0,int}}(h_d, h_i)}{\sqrt{2\left(\sigma_{X_{1,int}}^2(h_d, h_i) + \sigma_{X_{0,int}}^2(h_d, h_i)\right)}}\right)
$$
(25)

The BERs conditional for the UTS and DTS on the turbulence and crosstalk frame overlap, respectively are given as

$$
BER_{U_l}(h_d, h_i, n_1) = p_{f(l)}(n_1) \frac{n}{2(n-1)} \times (p_{s(l)}(1) P_{we(l,1)}(h_d, h_i) + p_{s(l)}(0) P_{we(l,0)}(h_d, h_i))
$$
\n(26)

$$
BER_{D_l}(h_Z, n_1) = p_{f(l)}(n_1) \frac{n}{2(n-1)} \times (p_{s(l)}(1)P_{we(l,1)}(h_Z) + p_{s(l)}(0)P_{we(l,0)}(h_Z))
$$
 (27)

where $p_{f(l)}(n_1)$ is the probability of *l* CP shooting the Single Frame (SF). Also $p_{s(l)}(r)$ is the probability of *r* out of *l* CP shooting the single slot are calculated the same as in Mbah et al. [\(2014](#page-34-12)). $P_{we(l,1)}(h_d, h_i)$ and $P_{we(l,0)}(h_d, h_i)$ are calculated using Eq. ([24](#page-10-1)) for $r = 1$ and 0 which represent probability error for interfere and the desired signal for diferent turbulent regimes in the UTS. Also $P_{we(l,1)}(h_z)$ and $P_{we(l,0)}(h_z)$ are computed using Eq. ([24](#page-10-1)) where SAI for the same AT channel link in the DTS. The total BER in the existence of the turbulence and crosstalk for UTS and DTS determined using Eqs. [\(26\)](#page-10-2), ([27](#page-10-3)) respectively

$$
\overline{BER}_U = \int_0^\infty \int_0^\infty \frac{1}{n} \sum_{n_1=0}^{n-1} \sum_{l=0}^2 BER_{U_l}(h_d, h_i, n_1) p_{GG,d}(h_d) p_{GG,i}(h_i) dh_d dh_i \tag{28}
$$

$$
\overline{BER_D} = \int_0^\infty \frac{1}{n} \sum_{n_1=0}^{n-1} \sum_{l=0}^2 BER_{D_l}(h_Z, n_1) p_{GG,d}(h_Z) dh_Z
$$
(29)

 \mathcal{D} Springer

The SF and crosstalk with fxed mis-alignment, ([28](#page-10-4)) and ([29](#page-10-5)) are modifed to eliminate conditions of averaging over all values for the UTS and DTS of (n_1) .

5.2 Error foors analysis in the case of adaptive and fxed detection thresholds

This section includes the analytical mathematical model of the EFs that rely on OOK with adaptive and fxed detection threshold modulation for a general depiction of functional DWDM-FSO links. The result obtained proved a further improvement with the modifed OOK is used to eliminate the EFs that occurs in the case of the (Signal with AT, Interferer with No AT (TurbuSi, XT)). The resulting of analysis the EF are outlined in Table [3,](#page-12-0) where $K_{\alpha-\beta}$ (·) denotes the MBF of the second kind with order $\alpha-\beta$ (Yang et al. [2016\)](#page-34-13).

5.2.1 Mathematical model derivation of OOK with adaptive detection threshold

BER
$$
(P_{R,sig}(1)) = \frac{1}{4} \text{erfc}\left(\frac{2(r-1)RP_{R,sig}(1)/(r+1)}{2 q B_e R P_{R,sig}(1) + \sigma_{th}^2}\right)
$$
 (30)

In the second one, it has the form

$$
BER = \frac{1}{4} \int_{0}^{\infty} \text{erfc}\left(\frac{2(r-1) R \cdot P/(r+1)}{2q B_{e} R \cdot P + \sigma_{th}^{2}}\right) p_{GG}\left(\frac{P}{P_{R,\text{sig}}(1)}\right) dP
$$
(31)

where

$$
p_{GG}\left(\frac{P}{P_{R,\text{sig}}(1)}\right) = \frac{2\left(\alpha\beta\right)^{(\alpha+\beta)/2}}{\Gamma\left(\alpha\right)\Gamma\left(\beta\right)} \left(\frac{P}{P_{R,\text{sig}}(1)}\right)^{((\alpha+\beta)/2)-1} K_{\alpha-\beta} \left(2\sqrt{\alpha\beta \frac{P}{P_{R,\text{sig}}(1)}}\right)
$$
(32)

Finally, in the last case the dependence is the following:

$$
BER = \frac{1}{4} \int_{0}^{\infty} erfc\left(\frac{2(r-1)R \cdot P(1-1/C_{XT})}{2qB_{e}R \cdot P(1+1/C_{XT}) + \sigma_{th}^{2}}\right) p_{GG}\left(\frac{P}{P_{R,sig}(1)}\right) dP \quad (33)
$$

Here, the major challenge consists in taking integrals in the right hand sides of the Eqs. ([31](#page-11-0)) and [\(33\)](#page-11-1) properly. To fnd correct values for the integral limits in these equations, one should examine the dependence that is the following as written in (Andrews and Phillips [2005;](#page-33-13) Mbah et al. [2016](#page-34-9); Al-Habash et al. [2001](#page-33-14))

$$
p_{GG}(h_Z) = \frac{2(\alpha \beta)^{(\alpha+\beta)/2}}{\Gamma(\alpha)\Gamma(\beta)} h_Z^{((\alpha+\beta)/2)-1} K_{\alpha-\beta} (2\sqrt{\alpha \beta h_Z}); \quad h_Z > 0,
$$
 (34)

where h_Z is the attenuation owing to AT.

10−¹²

Since

$$
\int_{0^{-12}}^{3} p_{GG}(h_z) dh_z = 0.9725 \tag{35}
$$

Table 3 pdf and error foor terms for diferent atmospheric turbulence channel models. (Reproduced with permission from Yang et al. [2016](#page-34-13)) ♪ \cdot \overline{a} i, ϵ l, \cdot or ϵ ϵ $\ddot{}$ ् $\ddot{}$

With performing the integration in Eqs. ([31\)](#page-11-0) and ([33](#page-11-1)) from $10^{-12} \cdot P_{R,\text{sig}}(1)$ to $3 \cdot P_{R,\text{sig}}(1)$ one can count on the accuracy that does not exceed a few percent. For instance, one can try 10^{-12} for the lower limit and 10^{-3} for the upper one. However, the arbitrary choice of limits can lead to the normalization of GG pdf that does not equal to 1 exactly. Therefore, one can introduce the normalization constant *A* in this function

$$
p_{GG}\left(\frac{P}{P_{R,sig}(1)}\right) = \frac{2(\alpha\beta)^{\frac{(\alpha+\beta)}{2}}}{\Gamma(\alpha)\Gamma(\beta)} A\left(\frac{P}{P_{R,sig}(1)}\right)^{((\alpha+\beta)/2)-1} \times K_{\alpha-\beta} \left(2\sqrt{\alpha\beta \frac{P}{P_{R,sig}(1)}}\right)
$$
(36)

5.2.2 OOK with fxed detection threshold

The received signal $(r = \xi I + N)$ in the low state, where *N* (noise PSD) and $I_s = \xi I$ optical received independent and ξ is low and high offset that result from use with r (Yang et al. 2016), since I_s , N are assumed to be independent.

$$
f(r|s_0) = \frac{1}{\xi} f_1\left(\frac{r}{\xi}\right) * f_N(r) = \int_0^\infty \frac{1}{\sqrt{2\pi}\sigma_x} exp\left(-\frac{\left(ln\frac{x}{\xi} + \frac{\sigma^2}{2}\right)^2}{2\sigma^2}\right) \times \frac{1}{\sqrt{2\pi}\sigma_y} exp\left(\frac{(r-x)^2}{2\sigma_y^2}\right) dx\tag{37}
$$

where * symbolize for the convolution process, and $f_N(r) = \frac{1}{\sqrt{2\pi}\sigma_y} exp\left(\frac{(-r)^2}{2\sigma_y^2}\right)$ $2\sigma_y^2$ λ denotes the

noise pdf. For a given fixed detection threshold (FDT) T_{th} , the false alarm probability P_F and the miss probability P_M can be respectively is given by (Yang et al. [2016](#page-34-13))

$$
P_F = \int_{T_{th}}^{\infty} f(r|s_0) dr = \int_{T_{th}}^{\infty} \left(\frac{1}{\xi}\right) f_I\left(\frac{r}{\xi}\right) * f_N(r) dr \tag{38}
$$

$$
P_M = \int_{-\infty}^{T_{th}} f(r|s_1) dr = \int_{0}^{T_{th}} \left(\frac{1}{2+\xi}\right) f_l\left(\frac{r}{2+\xi}\right) * f_N(r) dr.
$$
 (39)

Assuming that p_1 shows a priori probability that "1" is sent, i.e., $p_1 = 1/2$ means "0"s and "1"s are equally likely to be sent, one can write that the BER for OOK using FDT T_{th} as

$$
P_e = (1 - p_1)P_F + p_1 P_M \tag{40}
$$

where T_{th} is FDT, P_F and P_M , $Q_{(x)} = \frac{1}{\sqrt{2\pi}}$ ∞ ∫ *x* $e^{-\frac{t}{2}}dt$ is the Gaussian Q-function in fixed and unoptimized detection threshold.

5.3 Mathematical model of power penalty

This section is mainly dealt with the deterioration led to by the optical crosstalk, PP can be referred to as the devaluation othe diference of Optical Power (OP) level between the "1" and the "0" states and this is expressed in the following equation (Gyselings et al. [1999](#page-33-17))

$$
\varepsilon_{x} = \left\{ \frac{P((t_{1})|d_{s}(t_{1}) = 1 - P((t_{0})|d_{s}(t_{0})) = 0)}{A^{2}/2} \right\}
$$
(41)

where $P((t_1)|d_s(t_1) = 1)$ is the OP in case "1" and the $P((t_0)|d_s(t_0)) = 0$ is the OP in case "zero". The PP will be:

$$
P_x = -10. \log \{ \varepsilon_x \} \tag{42}
$$

In general terms, the spectral emission from a typical LD agrees fairly well to a Gaussian distribution, which then provides a direct analytic explanation for operation in any model. Corresponding to Gaussian placement in the analytical model, the MEAVAR for a random variable will be:

$$
E[\varepsilon_X] = 1 \tag{43}
$$

$$
var[\varepsilon_{X}] = \sum_{i}^{N} \delta_{i}
$$
 (44)

Since $E[\epsilon_X]$ and $var[\epsilon_X]$ calculate the mean and variance of a random variable, respectively. With GA distribution, considered the following:

$$
BER = P\left[\varepsilon_{\text{X}} \le \left(1 - 6\sqrt{\sum_{i=1}^N \delta_i}\right)\right] = 10^{-9}
$$
\n(45)

Here the purpose of as a model of beneft for determining the certainty for the penalty analysis. But this is not automatically an assurance need for actual system design, as this model does not actually have to correspond with the generally employed BER amount of value at 10^{-9} . However, with this level of assurance for calculating crosstalk (XT) penalty:

$$
P_x = -10. \log \left(1 - 6 \sqrt{\sum_{i=1}^{N} \delta_i} \right) \tag{46}
$$

where P_x represents the PP of AROP signal, (N) is the number of XT elements and δ_i is the XT coupling coefficient. Equation (46) (46) (46) shows the PP to the obtained OS in the process where the optical receiver noise is controlled by thermal noise. But for further exact evaluation if the detection is signal spontaneous beat noise dominated ([47](#page-14-1)) the equation will be

$$
P_x = -5. \log \left(1 - 6 \sqrt{\sum_{i=1}^{N} \delta_i} \right) \tag{47}
$$

The Eqs. [\(46\)](#page-14-0) and [\(47\)](#page-14-1) have been employed for investigating the implementation proceeds as designs for PP of the DWDM FSOC.

5.4 Optical power budget analysis

The mean to OAN distance is optical power budget (OPB) the amount of light possible to produce at OF link. OFL or overall attenuation is the amount of the losses of each individual component between a transmitter and receiver including fber, couplers and other optical devices and splices. The losses are relative to the transmitter output power and infuences the required receiver input power. Power margin, P_{MA} , represents the amount of power available after deducting linear and nonlinear span losses from the power budget (Ng et al. [2010\)](#page-34-14)

Power Budget
$$
(P_B)
$$
 = Minimum transmitter Power (P_{TMIN})
– Minimum Receiver Sensitivity (P_{RMIN}) (48)

Link Margin
$$
(P_S)
$$
 = (Fiber Attenuation × Km) – (Splice Loss × No. Splices)
+ (Connector Loss × No. Connectors) (49)

Power Margin
$$
(P_{MA})
$$
 = Power Budget (P_B) – Link Margin (P_S) – Safety Margin (50)

Fiber link loss dimensions must be given out utilizing a laser source and a power meter in both ways on each fber span to insure that the original network loss is less than the budgeted loss. In this design, the minimal transmitter power and minimal receiver sensitivity is set as 0 and − 44 dBm. The possible power or power budget for the constructed plan is 44 dBm For performance estimates it is taken up to have signal mux/demux loss L_{mix} and L_{demux} (≤3.5 dB), contiguous channel other loss L_{demux; contiguous} (typically>30 dB), and non-contiguous-channel additional loss $L_{demux; non-contiguous}$ (typically > 35 dB) (Monroy and Tangdiongga [2002\)](#page-34-5).

Here is the calculation OPB:

Power Budget =
$$
T_X
$$
 Power – R_X Sensitivity – LLosses
\n
$$
T_X
$$
 Power = 0 dBm
\n
$$
R_X
$$
 Sensitivity = -44 dBm

(52) Losses = (8−channel Multiplexer∕Demultiplexer1 loss) + (8−channel Multiplexer∕Demultiplexer2 loss) = 38 dB

OPB = T_xPower−R_xSensitivity−Losses = 0 dBm−(− 44 dBm)−38 dB = 6 dB (53)

5.5 Maximum link distance calculations in DWDM FSO network

After checking the power budget for OF link, we can apply the amount to determine the maximum distance that the network can support. The estimation equation is presented as below.

Power Budget = Buffer Distance∕Fiber Attenuation (54)

Then we will determine the maximum supported distance of FSO link. Here we have the amount for the OF attenuation in Table [2](#page-8-1) (0.2 dB/km). The distance is:

$$
Distance = (6 dB - 2 dB)/0.2 dB/km = 20 km \tag{55}
$$

5.6 Outage probability

The Outage Probability (OUP) is thus achieved by summing the collective pdf around the region that the BER of target is smaller than the instantaneous BER (InstBER) and is given as (Aladeloba et al. [2012a,](#page-33-6) [b](#page-33-7), [c](#page-33-8), [2013;](#page-33-5) Mbah et al. [2017](#page-34-15))

$$
P_{OUT}(I_d, I_l) = \int \int \int_{R_x} p_{x_d, x_l}(I_d, I_l) \langle I_d \rangle, \langle I_l \rangle dI_d dI_l \tag{56}
$$

where R_X is the region in (I_d, I_l) space where $BER_{inst}(I_d, I_l) > BER$ target. Equation ([56](#page-16-1)) could be simplifed further as (Mbah et al. [2014](#page-34-12), [2017\)](#page-34-15),

$$
P_{OUT}(\langle I_d \rangle, \langle I_l \rangle) = \int\limits_0^\infty \int\limits_0^{I_{dI}(I_l)} p_{X_d}(I_d, \langle I_d \rangle) p_{X_l}(I_l, \langle I_l \rangle) dI_d I_l = \int\limits_0^\infty p_{X_l}(I_l, \langle I_l \rangle) \left[\int\limits_0^{I_{dI}(I_l)} p_{X_d}(I_d, \langle I_d \rangle) dI_d \right] dI_l
$$
\n(57)

where the threshold instantaneous of irradiance $I_{dT}(I_l)$ is required to obtain a BER_{inst} equals to the BER purpose and is rely on the interferer spontaneous irradiance. The system instantaneous BER is dependent on the interferer and instantaneous irradiances of the signal (I_d, I_l) (Aladeloba et al. [2012a,](#page-33-6) [b](#page-33-7), [c](#page-33-8)),

$$
BER_{inst}(I_d, I_l) = \frac{1}{4} erfc\left(\frac{Q(I_d, I_l)}{\sqrt{2}}\right)
$$
\n(58)

$$
Q(I_d, I_l) = \frac{i_{1,0}(I_d, I_l) - i_{0,1}(I_d, I_l)}{\sigma_{1,0}(I_d, I_l) + \sigma_{0,1}(I_d, I_l)}
$$
(59)

6 Numerical results and discussion

Power penalty, BER required OS transmission power results are performed utilizing speci-fications reported in Table [2.](#page-8-1) DPPM COL with $M=2$ is used for all computations to control the bandwidth extension down while yet retaining the attractive qualities of DPPM. The required optical power applied to in this work represents the transmitter power at the OLT for DTS and ONU for UTS power of 20 dBm is deemed reliable for FSO transmission system around the 1550 nm wavelength region. Refractive index structure constant ranging from $C_n^2 = 1 \times 10^{-17}$ to 1×10^{-13} m^{-2/3} are used for FSOC link length of 0–2500 m, corresponding to RVAR (σ_R^2) range of 0 to 10.6811 and covering all the AT regimes. Aperture Averaging (AA) is integrated in the turbulence model for scintillation mitigation through the operation of Eqs. ([2](#page-4-1)) and [\(3\)](#page-5-3). Amplifer concentration-based implements, fber dispersion, and other non-linearities are ignored in the analysis, and a proper extinction ratio is assumed for the OOK calculations. Results in terms of AROP are given to conclude the behavior for different schemes of DWDM FSO system. The TRNVAR σ_{th-OOK} with

 $R_b = 2.5$ Gbps is back determined employing the DPPM bandwidth using the DPPM bandwidth extension factor $B_{exp} = 2^M/M$ (Sibley [1995\)](#page-34-16) and $\sigma_{th-DPPM}^2 = B_{exp} \sigma_{th-OOK}^2$. The thermal noise current is taken as $(7 \times 10^{-7} A)$ with sensitivity -23 dBm at BER of 10^{-12} (Ramaswami and Sivarajan [2002](#page-34-1)). For the calculation, we assume that the bandwidth for the multiplexer/demultiplexer channel bandwidth is 60 GHz, with 3.5 dB insertion loss and a contiguous channel spacing of 100 GHz in the C-band of the ITU (International Telecommunication Union) Grid Sector. Numerical results are presented the analysis of ICC for all the cases (1) No Interferer, No AT Si); (2) Signal with AT, No Interferer (TurbuSi); (3) Signal with AT, Interferer with No AT (TurbuSi,XT); (4) Signal with Interferer, No AT (Si,XT); and (5) Signal with No AT, Interferer with AT (Si, TurbuXT). The WT and ST conditions for FSO link length $l_{fso} = 1000$ m come from $C_n^2 = 8.4 \times 10^{-15}$ m^{-2/3} and $C_n^2 = 1 \times 10^{-13}$ m^{-2/3}, respectively. We considered an optically preamplified receiver without any other losses, to clearly the efects of crosstalk alone.

Figure [2](#page-18-0) depicts the results of our calculations with the analysis AT that accentuated ICC [present]. As one can see in Fig. [2](#page-18-0), BER versus average received optical power (dBm) for AT regimes with no amplifier when (a) C_{XT} =30 [dB] (Aladeloba et al. [2013\)](#page-33-5), (b) C_{XT} =15 dB [present] and (c) C_{XT} =25 dB [present]. The Error Floor (EF) that occurs in the case of Si, TurbuXT because the demux Contiguous Channel Rejection Ratio (CCRR) $L_{\text{demux} \,XT}$ reduced the power of turbulent interferer. The ER starts once the SIGP and CXTP are sufficiently high that the noises are very unlikely to cause a reverse threshold crossing. In Fig. [2](#page-18-0) shows all the cases of BER foors, in the ST cases the TurbuSi,XT BER floors when C_{XT} =30 dB, and while in WT the TurbuSi,XT and Si,TurbuXT both EF when C_{XT} =15 dB and C_{XT} =25 dB that rises with Turbulence Strength (TS), [present]. For illus-tration, in Fig. [2a](#page-18-0) with C_{XT}=30 dB shows EF TurbuSi,XT with C_n²=1 × 10⁻¹³ m^{-2/3} in ST cases while the TurbuSi,XT and Si,TurbuXT both error floor when C_{XT} =15 dB as shown in Fig. [2b](#page-18-0). Also, when $C_{YT} = 25$ dB shows both the EF TurbuSi, XT and Si, TurbuXT but in the Si,TurbuXT case occurs at much lower BERs for WT as seen in Fig. [2c](#page-18-0).

Figure [3](#page-19-0) shows BER versus average received optical power (dBm) for turbulence regimes with an amplified case when (a) C_{XT} = 30 dB (Aladeloba et al. [2013](#page-33-5)), (b) C_{XT} = 15 dB [present] and (c) $C_{XT} = 25$ dB [present]. The Crosstalk XT effects is small without AT (as shown by the Si,TurbuXT BER curves in Fig. [3a](#page-19-0) and b and c) where the dependencies BER on AROP for all the mentioned cases that presented in Aladeloba et al. [\(2013](#page-33-5)) where in Fig. [3b](#page-19-0) with $C_{XT} = 15$ dB, the EF at BER of 10^{-7} and in Fig. [3c](#page-19-0) $C_{XT} = 25$ dB shows the EF at considerable lower BER of 10^{-11} [present]. To understand the EF of AT ICC, the case of Si,TurbuXT can increase to 1 value so {crosstalk become 1, data 0} is greater than {crosstalk 0, data 1} when h_{int} is higher from h_{sig} , when value a data rate is faster from turbulence leading to EF this occur when $h_{int} > h_{sig}$. In the case of TurbuSi,XT same case Si,TurbuXT except POP attenuation of the signal. The EF occurs when AT has increased the interfering $h_{int} > h_{sig}$. FEC can bring about much better performance. Note, however, that the actual link between the LTAS power BER before and after the FEC would require the FEC to enter the analysis. FEC would improve largely the procedure in handling with EF and increasing the feasible target BER. Times of CXTP is huger than the SIGP leads to the turbulent, there is a perfect detection of crosstalk of BER for the signal, so the error floor is easily provided by $0.5 \times$ prob (CXTP $>$ SIGP). The BER use where the EFs occur is thus worked out by both the TS and the demux Channel Rejection Ratio (CRR) (which precisely deals with the CXTP). Before the error foors occur, the process BER operation is defned by turbulence (ASEBN, ASEN, ASE-shot etc.) and an increase in the Signal-to-Noise-Ratio (SNR) of the system improves the BER. Similarly, at low power, the infuences the signal and worsens BER. Turbulent conditions considered

² Springer

 $\frac{1}{2}$

are $C_n^2 = 1e - 17 \text{ m}^{-2/3}$ $C_n^2 = 1e - 15 \text{ m}^{-2/3}$, and $C_n^2 = 1e - 13 \text{ m}^{-2/3}$. If the resulting σ_R^2 < 1, we have WT; if $\sigma_R^2 \approx 1$, we have moderate and if $\sigma_R^2 > 1$; we have ST.

Figure [4](#page-20-0) shows the PP (dB) for a interferer demux CRR $L_{demux,XT}$ at $l_{fso} = 1500$ m and $C_n^2 = 1e - 16 \text{ m}^{-2/3}$ which presented in Mbah et al. ([2016\)](#page-34-9), (b) interferer demux channel rejection L_{demux,XT} at $l_{\text{fso}} = 2000 \text{ m}$ and $C_n^2 = 1e - 17 \text{ m}^{-2/3}$ [present]. Figure [4](#page-20-0)a shows

 \mathcal{D} Springer

the DPPM PP about of 0.2 −0.7 dB for WT are reported for BER about $10^{-3} - 10^{-9}$, respectively of $C_n^2 = 1e - 16 \text{ m}^{-2/3}$ and $l_{\text{fso}} = 1500 \text{ m}$ which is presented in Mbah et al. ([2016\)](#page-34-9), while in Fig. [4b](#page-20-0) shows the PP for the OOK system be upper than DPPM for WT with $C_n^2 = 1e - 17 \text{ m}^{-2/3}$ and $l_{fso} = 2000 \text{ m}$ where the DPPM PP about 0.2 –0.8 dB at BER about $10^{-3} - 10^{-9}$ for WT, respectively [present] while the OOK about 0.3 -1.0 dB at BER about $10^{-3} - 10^{-9}$ for WT. Comparing Fig. [4a](#page-20-0), b we show the enhancement of the PP from $l_{\text{fso}} = 1500$ to 2000 m at 0.2 –0.8 dB of BER about $10^{-3} - 10^{-9}$ for WT, respectively. The proposed approach of DPPM merges higher enhancement of PP about 0.8 dB for BER 10^{-9} at distance 2000 m compared to OOK at 1 dB for WT [present]. Figure [5](#page-21-0) shows the PP (dB) for a the UTS as a function of $(C_n^2 m^{-2/3})$, with $(L_{\text{demux, XT}} = 35 \text{ dB})$ $(L_{\text{demux, XT}} = 35 \text{ dB})$ $(L_{\text{demux, XT}} = 35 \text{ dB})$ b interferer demux CRR $(L_{\text{demux, XT}})$. Figure 5a shows the OOK is lower PP compared to the DPPM modulation under MT to ST. As shown in Fig. [5](#page-21-0)a with NINT of the DPPM PP is greater than the OOK by 0.2 dB and increasing to 0.5 dB as the TS. OOK requires lower PP than DPPM for all values of $C_n^2 = 1e - 13 \text{ m}^{-2/3}$. The DPPM sensitivity has been reduced over OOK systems in the presence of AT as given in Aladeloba et al. ([2012a](#page-33-6), [b](#page-33-7), [c\)](#page-33-8), without interferers. The distinction between the PP of both

systems is reduction of turbulence in the existence of interferers. We use the Power Control (PC) from the RN to monitor and control of the OLT with estimation each ONUs distance from the RN in order to determine the required transmit power from such distance to

Fig. 5 Power penalty (dB) for **a** the upstream as function of the refractive index structure constant $\left(C_n^2 m^{-2/3}\right)$ at $L_{\text{demux,XT}} = 35 \text{ dB}$, **b** interferer demux channel rejection ratio (CCR) $(L_{\text{demux,XT}})$ (dB)

achieve the defned quality of service (QoS). In implementing PC, the system determines the required transmitter power (P_{TXmin}) independent of the net link path loss to achieve the set QoS or BER. Figure [5](#page-21-0)b shows the CRR loss $(L_{\text{demux, XT}})$ (dB) versus the PP. In this section, it has been provided a methodology for calculating the PP side by side in the presence of the Dominant Signal Noise (DSN) dependent noise has been presented (Phillips [2007\)](#page-34-17). It can be seen in Fig. [5](#page-21-0)b, the PP that dominated by thermal noise higher than the PP signal received from thermal noise. Signals received at each station of the system and two cases, this means that the PP of each case also has diferent values depending on the situation, when the DSN and spontaneous noise when the signal is dominated by a diferent PP. Using a mathematical model, the results shown in Table [4.](#page-22-0)

The curves DTS BER appears for a Single Interferer (SINT) as both ST and WT is shown in Fig. 6 of the signal and interferer FSO link lengths of 2500 m. Figure 6 shows that the DTS required OP (dBm) (BER of 10^{-6}) as a function of the length of the link FSO (a) $L_{\text{demux, XT}} = 30$ dB, (b) $L_{\text{demux, XT}} = 15$ dB, $l_{\text{fso}} = 2500$ m with OOK and DPPM for the No Interferer (NINT) and SINT cases. For Case A, with signal and crosstalk transmit same the powers. In Fig. [6](#page-23-0)a both the NINT and SINT cases have very similar to the transmission power required as a result of the high signal to crosstalk ratio (and no AT-ICC). The result of Fig. [6](#page-23-0), its coverage of all turbulent cases from weak to moderate and

strong turbulence. In the case of strong turbulence $C_n^2 = 1 \times 10^{-13} \text{ m}^{-2/3}$, and increasing the AROP. In Fig. [6a](#page-23-0), the interferer demux rejection is 30 dB and both SAI are at the same distance from the RN. Numerical result shows that the downstream AROP (dBm) at BER of 10^{-6} in OOK is higher from DPPM. Also in Fig. [6](#page-23-0) shows AROP increased with the C_n^2 and FSO link length. Generally, as the FSO link length increases, the AROP increases, since the attenuation, scattering, beam losses spreading and scintillation increase, when $C_n^2 = 1 \times 10^{-13} \text{ m}^{-2/3}$. For first case, the NINT and SINT transmitted power in same time, for second case that the NINT and SINT transmitted with high C_{XT} to obviate the effects AT accentuated ICC seen Fig. [6](#page-23-0)a. Figure [6](#page-23-0)b shows the crosstalk efect becomes notice-able, though not dramatically (Aladeloba et al. [2013](#page-33-5)) and $L_{demux,XT} = 15$ dB is lower demux or indigent demux. From Fig. [6](#page-23-0), if the power was transferred to be a high value as 0 dBm, it can overcome the efects of turbulence for all systems are considered except $C_n^2 = 1 \times 10^{-13}$ m^{-2/3} and *l*_{fso} > 1500m in case of the single interferer. In Fig. [6](#page-23-0), if the T_x was fixed OLT power in the 0 dBm (to reduce non-linear fiber), it can be used to infer FSO link lengths of about 1500 m can be used for the case of ST condition. In Case B, amplifers placed at the OLT transmitter quite similar results not shown are obtained in Case A, above due to the low loss of fber. However, for Case B is low allowed transmitter about -10 dBm (Ramaswami and Sivarajan [2002](#page-34-1)) due to the integrity of the fiber. RVAR σ_R^2 is constant for a specific curve and the T_x power for the SAI are supposed to be the same, so only the demux CCRR loss $(L_{demux, XT})$ is accountable for the crosstalk. The effect of crosstalk is seen to be small without turbulence even for a demux with poor CCRR (15 dB).

Figure [7](#page-24-0) shows the UTS required transmitted OP (dBm) (BER of 10[−]6) as a function of the FSO link length (a) $L_{demux, XT} = 30$ dB, (b) transmitter divergence angle $\theta_{XT} = 0.2$ mrad, $l_{\rm fo}$ = 2500 m with OOK and DPPM for the no interferer and SINT cases. The result of Fig. [7](#page-24-0) covered for all the cases in turbulent from WT to MT and ST. Figures [6a](#page-23-0) and [7](#page-24-0)a, it can be seen that the required transmit power is higher in the UTS case by about 7 dBm when $C_n^2 = 1 \times 10^{-13} \text{m}^{-2/3}$ and $l_{\text{fso}} = 2500$. The results show that the UTS required transmitted optical power (dBm) at BER of 10[−]⁶ in OOK is higher from DPPM. Demux CCRR values typically≤−15 dB and≥−45 dB have been investigated in Yu and Neilson [\(2002](#page-34-18)), Maru et al. ([2007\)](#page-34-19), Hirano et al. ([2003\)](#page-33-18) and are considered. Thus, it is remarkable for a good designer of PON to determine the closest distance to the RN each ONU should be in order to achieve the required system performance with appropriate consideration to the demux CCRR $L_{demux, XT}$. For example, using a $L_{demux, XT}$ of 30 dB as seen in Fig. [7](#page-24-0)a when the user interfering is 1000 m from the RN required and then the required ONU cannot

$L_{\text{demux,XT}}$		Power penalty		
Signal dominated by thermal noise	Signal spontaneous beat noise dominated	Signal dominated by thermal noise	Signal spontaneous beat noise dominated	
-35	-35	0.49	0.245	
-33	-33	0.6264	0.3132	
-31	-31	0.8045	0.4023	
-29	-29	1.04	0.5198	
-27	-27	1.355	0.6775	
-25	-25	1.787	0.8938	

Table 4 Numerical results when the signal is dominated by a diferent power penalty

be more than 1500 m ONU of RNs for the target BER to be met at all regimes for WT, MT and ST. To avoid some of the problems of AT, may be included PC algorithm in the system to monitor each ONU power transmission relative to the distance from the RN provides that the same receptor is the ability to RCL for each user, as shown in the design. If the ONU is required in the 2500 m away from the RN mode, and then for another ONU interferer to be in the 1000 to RN, a demux with CCR higher than 45 dB is required so that the target BER is reached for all turbulence regimes as seen in Fig. [7](#page-24-0)a. The ONU transmits power can be up to 10 dBm to fulflls the eye-safety condition for a C-band wave-length range (Aladeloba et al. [2013](#page-33-5); Mbah et al. [2016](#page-34-9)). When the TxDA (θ_{XT}) and the C_n^2 increases since the AROP clearly increased as shown in Fig. [7b](#page-24-0). The non-tracking with the transmission beam of relatively large differences θ_{XT} for > 1 mrad, more powerful than the tracking systems will be required. For the automatic pointing and tracking, the system with *≪* 1mrad to be narrow and allow with the pointing and tracking for safely collecting a large proportion of the transmitted energy. It can provide information about the location of the receiver. The tracking system is also pointing jitter errors (Aladeloba et al. [2012a](#page-33-6), [b,](#page-33-7) [c\)](#page-33-8) not included here. To achieve a BER of 10⁻⁶ and *l*_{fso} of 1500 by using small transmission divergence angle (about 0.12 mrad). The results show the impact of ICT on the UTS through the evaluation of BER versus AROP (dBm) within the transmission distance of 2500 m with

 $L_{\text{demux XY}}$ = 30 dB, for different FSO link lengths from the interferer to the RN d_{int} , using good demux ($L_{\text{demux, XT}}$ =30 dB). If a good demux device is used Fig. [7](#page-24-0) at BER=10⁻⁶, the effect of crosstalk is negligible as AROP stays the same in both cases of $d_{int} = d_{sig}$.

Figure [8,](#page-25-0) shows the required OP (dBm) for the UTS as a function of RINS constant $(C_n^2 m^{-2/3})$ and interferer demux channel rejection L_{demux,XT} (dB) at $l_{\text{fso}} = 2000$ m. The result as for target BERs concerning 10^{-9} , 10^{-6} , and 10^{-3} , in accordance with remain met at entire AT regimes, the system requires demux with a CCRR better or equalize in accordance with 46 dB, 33 dB, and 17 dB, respectively. However, to get a BER regarding 10[−]⁹ would need great OP (above 25 dB). FEC carried out between most recent realistic systems, function at BER about 10⁻³ is becoming appropriate and demultiplexers along 18 dB rejection is effortlessly available.

Figure [9](#page-25-1) shows the PP (dB) for the UTS as a function of the RINS constant $(C_n^2 m^{-2/3})$ at $C_n^2 = 1e - 17 \text{ m}^{-2/3}$ and interferer demux CRR L_{demux,XT}(dB) at $l_{\text{fso}} = 250 \text{ m}$. The result shows that the PP for the DPPM system tends in conformity with keep lower than that on the OOK system. Obtained results in Fig. [9](#page-25-1) shows that the PP for DPPM about 2.0 −3.0 dB and 2.0 –4.0 dB for WT are reported of BER about $10^{-3} - 10^{-6}$ and $10^{-3} - 10^{-9}$, respectively. As shown in Fig. [9,](#page-25-1) an interferer that is closer to the RN more crosstalk to other users

further away, even at below value $(C_n^2 m^{-2/3})$. Thus, in the non-attendance of PC, user stationing should be dealt with as an essential design specifcation.

Figure [10](#page-26-0) shows the result of OUP in the existence of a single turbulent interferer for a DWDM FSO OOK system compared to a situation where there is no interferer. The system outage offers with different RINS (C_n^2) , demultiplexer CCRR $(L_{demux,XT})$ and RL aperture diameter are examined for an FSO channel length $(l_{\rm fo})$ of 2000 m for both SAI. With the presence of the interferer, outage foors analogous to the EFs obtained for BER evaluations in Aladeloba et al. ([2013](#page-33-5)), Mbah et al. [\(2016](#page-34-9)) occur where the floor position shifts with change in C_n^2 and $L_{demux,XT}$ respectively in Fig. [10](#page-26-0)a, b. Figure [10c](#page-26-0) shows that AA which is a commonly used AT mitigation technique (Vetelino et al. [2007\)](#page-34-10) improves the OUP of the system. As seen in Fig. [10](#page-26-0)c, increasing the RL aperture diameter from 1.55 to 2.55 cm decrease the OUP of the system with turbulence-affected interferer from 10^{-6} to about 10^{-9} at about 27 dBm/ cm² mean irradiance.

To further support up this point, in Fig. [11,](#page-26-1) we show a plot concerning the Required Mean Irradiance (RMI) to obtain InstBER overall performance target about 10⁻⁶ then 10[−]³ with including fxed OUP values regarding both 10[−]⁶ or 10[−]³ and RMI to achieve average BER aims regarding of 10^{-6} and 10^{-3} for a DWDM FSOC system (Mbah et al.

Fig. 10 Outage Probability (OUP) versus Mean Irradiance for a turbulent system (FSO link length = 2000 m) **a** for different values of C_n^2 at $L_{demux,XT} = 35$ dB, **b** for different values of $L_{demux,XT}$ at $C_n^2 = 1 \times 10^{-13}$ m^{-2/3}, **c** for different values of RL aperture diameter at $L_{demux,XT} = 35$ dB and $C_n^2 =$

Fig. 11 Required Mean Irradiance (RMI) as a function of the FSO link length to achieve instantaneous BER targets with fxed Outage Probability (OUP) values and average BER targets at L_{demux,XT} = 35 dB and
 $C_n^2 = 1 \times 10^{-13}$ m^{-2/3}

[2017\)](#page-34-15). From the end results proven of Fig. [11](#page-26-1) it is seen that with $L_{\text{demux,XT}} = 35$ dB and $C_n^2 = 1 \times 10^{-13}$ m^{-2/3}, the RMI to attain a target InstBER of 10⁻⁶ with OUP target of 10⁻³ for all links of FSO transmission considered. This shows so extra transmitter power is required according to enhance OUP for a given a partial InstBER target than in accordance with enhance the InstBER a given OUP target. This shows that the transmitter power more is required to improve the OUP for a given InstBER target than to improve InstBER for a specified OUP target. From the result shown in Fig. [11](#page-26-1) it is seen that with $L_{\text{demux}XT}=35 \text{ dB}$ a and $C_n^2 = 1 \times 10^{-13} \text{m}^{-2/3}$, the RMI to obtain a target InstBER of 10^{-3} with OUP target of 10⁻⁶ is greater than RMI to achieve a target InstBER of 10⁻⁶ with OUP target of 10[−]³ for all FSO lengths considered (Mbah et al. [2017\)](#page-34-15). This shows that more transmitter power is required to improve OUP for a given InstBER target than to improve the Inst-BER for a given OUP target. For example, at 2000 m in Fig. [11,](#page-26-1) extra 2.66 $(dBm/cm²)$ is required to improve the instantaneous BER from 10^{-3} to 10^{-6} at fixed OUP of 10^{-3} , while it takes additional 14.23 dBm/cm² to improve the OUP from 10^{-3} to 10^{-6} at fixed InstBER of 10⁻³. The values *α* and *β*, are analyzed at $l_{\text{fso}} = 1000$ m, ($\alpha = 4.2739$), ($\beta = 3.1606$) at $C_{n_0}^2$ =1 × 10⁻¹³ m⁻²/³, RVAR σ_R^2 = 1.9910 and we calculated the total OLT receiver value $(\sigma_{\text{th}}^2 = 98 \times 10^{-14} \text{ A})$ as seen in Fig. [12.](#page-27-0) The bit is sampled and compared with ADT. For OOK-NRZ signaling assumed here, the Kalman filtering method (Chen et al. [2008](#page-33-19)) represents a realistic adaptive approach to achieving near the optimal threshold for each instantaneous power level, and such an optimal is assumed. All noises and scintillation due to vulnerability to refractive index fuctuations arising of variation air temperature, pressure (Dar and Jha [2017](#page-33-20); Kaushal et al. [2017\)](#page-33-21) are analyzed. The results show BER foors of the interchannel crosstalk are analyzed for WT and ST in this study. Table [5](#page-28-1) show the calculations results of α and β and RVAR σ_R^2 at $l_{\text{fso}} = 1000$ m. Typical values of σ_R^2 , α and β used for modelling WT, MT, ST and Saturated Turbulence regimes are shown in Table [6](#page-28-2) (Ghassemlooy et al. [2013;](#page-33-10) Andrews and Phillips [2005](#page-33-13); Aladeloba et al. [2012a](#page-33-6), [b](#page-33-7), [c](#page-33-8); Popoola and Ghassemlooy [2009](#page-34-20)). The PP induced by Multiple Access Interference (MAI) only (i.e. relative to when one ONU is active on the required wavelength) for individual object BER values is shown in Fig. [13.](#page-28-3) The implement of MAI is less prominent at ST conditions with a maximum PP contribution of about 1 dB when the 8 ONUs are active and at target BER of 10⁻⁶. The effect of MAI is more prominent at WT conditions and for C_n^2 of 1×10^{-16} m^{-2/3}, a PP of about 6.686 dB is concluded for target BER of 10⁻⁹ when the 8 user are active on the system of ONUs.

Parameters Turbulence regimes Weak $\left(\sigma_{\rm R}^2 < 1\right)$ **Moderate** $\left(\sigma_{\rm R}^2\approx 1\right)$ te Strong ($\sigma_R^2 > 1$) **Saturated** $(\sigma_R^2 \to \infty)$ $\sigma_{\rm R}^2$ R 0.2 1.6 3.5 25 *a* 11.651 4.027 4.226 8.048 *β* 10.122 1.911 1.362 1.032

7 Validations

 $l_{\text{fso}} = 1500 \text{ m}$

As an analytical approach, it is certain to examine and evaluate the validity of PP results using DPPM and OOK. Figure [14](#page-29-0) show PP (dB) for the UTS as a function of RINS $(C_n²)$ at BER of 10^{-6} , l_{fso} = 2000 m and L_{demux,XT} = 35 dB. Unlike the non-AT WDM DPPM versus OOK crosstalk results in Mbah et al. ([2014\)](#page-34-12). For this purpose, we performed the PP results are shown in Fig. [14](#page-29-0) that the OOK system has slightly lower PP compared to the DPPM system under moderate-to-ST. The presented result show enhancement of the PP using DPPM at *l*_{fso}=2000 m above 20 dB for ST regimes are reported for BER of 10⁻⁶ as shown in Fig. [14](#page-29-0), with no interferer the DPPM PP is greater than the OOK by 0.1 dB, and when the TS increases, the PP reached to 0.5 dB. The diference between the PP of both Mbah et al. (2016) (2016) and [present] that the DPPM system tends to be closer to the OOK system at 26.65 dB system. The results show that the DPPM PP is greater than the OOK PP by 0.2 and increase to 0.5 at $l_{\text{fso}} = 1500$ m that presented in Mbah et al. [\(2016](#page-34-9)).

Next, Fig. [15](#page-29-1) illustrates BER of the designed system operating (4-Pulse Position Modulation (PPM) versus Ps, for the DTS with diferent turbulence strengths. Within the total distance of 4 km, the BER work is regularly worsened when the when the turbulence becomes stronger (i.e., higher C_n^2). With only one relay (N), the required P_s to attain BER of 10⁻⁹ are 10.2 dBm, 7.5 dBm, and 4.2 dBm corresponding to C_n^2 of 10⁻¹⁴m^{-2/3}, $7.5 \times 10^{-15} \text{m}^{-2/3}$, and $5 \times 10^{-15} \text{m}^{-2/3}$, respectively [present]. With two relays, the BER performance is significantly improved compared to the case when relay $(N=1)$, the performance improvements when N=2 are 8 dB, 7 dB, and 6 dB for C_n^2 of 10^{-14} m^{-2/3}, 7.5×10^{-15} m^{-2/3}, and 5×10^{-15} m^{-2/3}, respectively [present]. While N=1, the required P_s to obtain BER of 10⁻⁶ are 10.5 dBm, 7.5 dBm, and 4.5 dBm corresponding to C_n^2 of 10^{-14} m^{-2/3}, 7.5×10^{-15} m^{-2/3}, and 5×10^{-15} m^{-2/3} as published in Trinh et al. [\(2016](#page-34-21)). With two relays (N), the BER performance is significantly improved. More specifically, compared to the case when $N=1$, the performance improvements when $N=1$, the performance improvements when $N=2$ are 8 dB, 7 dB, and 6 dB for C_n^2 of 10^{-14} m^{-2/3}, 5×10^{-15} $\text{m}^{-2/3}$, and $5 \times 10^{-15} \text{ m}^{-2/3}$.

Fig. 15 Comparison between Downstream transmission: BER versus the average transmitted power per information bit P_s, with 4-PPM, $R_b = 1$ Gbps, $L_{demux,XT} = -30$ dB, and l_{fso} = 4 km, for different turbulence strengths $C_n^2 m^{-2/3}$ that presented in Trinh et al. ([2016,](#page-34-21) Present)

8 Conclusions

A hybrid fber and DWDM FSO network using OOK and DPPM have been investigated in this paper. The performance evaluation under the impacts of turbulence-accentuated ICC on the system is done. The novel approach of DPPM took advantage to all DWDM HFFSO network and is simple implementation with integrating of hybrid fber free space optical communication to form a low-cost, fexible, greater bandwidth and huge channel capacity, reliable with higher date rate optical network. The DPPM and OOK scheme at coding level of 2, DPPM gives about 2 dB in required average power over the OOK. Numerical result shows the improvement of the power penalty with OOK and DPPM modulation. The DPPM is a higher power efficient, powerful and results for greater-connection network. These improvements achieved in DPPM format on the price of higher channel bandwidth requires. Depending on the turbulence level, power penalties of 0.2–3.0 dB for WT regimes, and above 20 dB ST regimes are reported for a BER of 10⁻⁶. The PP that dictated by thermal noise greater than the power penalty that dominated spontaneous beat noise. The optical received signal spontaneous more accurate than optical received signal by thermal noise. The results of this paper should be appropriate for choosing DPPM modulation to enhancement the PP in DWDM FSO communication. Finally, FEC would further largely the procedure in handling with error foors and correcting the feasible target BER.

Acknowledgements Support from University Mansoura, Faculty of Engineering, Electrical Communication Department is gratefully acknowledged.

Appendix

This turbulence accentuated interchannel crosstalk efect is considered for the cases are written as Aladeloba et al. ([2013](#page-33-5))

The signal with turbulence but the interferer does not

To do so Eqs. ([6](#page-5-2)[–13\)](#page-6-1) are used in an optically preamplifed case [gain G, ASE PSD at the amplifier output], the ASE power spectral density (PSD) is $N_0 = 0.5 (NFG - 1)$ E where *G* and *NF* are the OA gain and noise figure, respectively, with no amplifier $(G=1)$. Then $P_{R, sig}(h_{sig}) = GP_{inst.size}(h_{sig})$ where $P_{inst.size}(h_{sig})$ is the instantaneous received signal power and thus $P_{\text{int,sig}}(1)$ is also the turbulence-free average received power $(ThbncFrp_{sig})$ of the input signal at the optical preamplifier. $P_{R, \text{int}} = GP_{int}$, is fixed by setting a signal-to-crosstalk ratio $C_{XT} = P_{R,sig}(1)/P_{int}$ where P_{int} is also the crosstalk optical signal power.

The interferer experiences turbulence, but not the signal

 $P_{R, int}(h_{int}) = GP_{inst, int}(h_{int})$, where $P_{inst, int}(h_{int})$ is the instantaneous received interferer power and thus $P_{R, sig} = GP_{sig}$ is fixed by setting a signal-to-crosstalk ratio $C_{XT} = P_{sig} / P_{R, int}(1)$, where $P_{R, int}(1)$ is also the turbulence-free average received interferer power $(\overrightarrow{TrblncFrp_{int}})$ and P_{sig} is the (non-turbulent) optical signal power.

Algorithms

See Table [7](#page-31-0).

Table 7 MATLAB code to calculate the value of (Trb ln cFrP)

```
%% define constants 
Rb=2.5*10^9;mt=2;eta=1;
c=2.998*10^8;h=6.626*10^(-34);lambda=1.55*10^(-6);r=10;B0=60*10^9;Be=Rb/2;
q=1.60218*10^(-19);
\overline{G}=1; E=h*c/lambda; 
N0=0;capitalr=eta*q/E; 
sigma2shotASE=2*mt*B0*N0*q*capitalr*Be; 
sigma2ASEASE=2*mt*(capitalr*N0)^2*B0*Be; 
signal2th=2*49*10^(-14);prec=[];
\frac{1}{1}her=[];
for ii=1:1:101 
 prec(ii)=-30+(ii-1)*8.3/100; 
 p(ii)=10^(-3)*10^(prec(ii)/10);
    \frac{1}{2}sigma2shot1=2*q*2*r/(r+1)*capitalr*p(ii)*Be;
    sigma2shot0=2*q*2/(r+1)*capitalr*p(ii)*Be;
 sigma2sigASE1=4*capitalr*N0*2*r/(r+1)*capitalr*p(ii)*Be;
 sigma2sigASE0=4*capitalr*N0*2/(r+1)*capitalr*p(ii)*Be; 
     sigma1=sqrt(sigma2shot1+sigma2sigASE1+sigma2shotASE+sigma2ASEASE+sigma2th);
    sigma0=sqrt(sigma2shot0+sigma2sigASE0+sigma2shotASE+sigma2ASEASE+sigma2th);
    curent0(ii)=2/(r+1)*capitalr*p(ii);
    current(iii)=2*r/(r+1)*cabilr*b(ii);qq(ii)=(current(ii)-current(iii))/(sigma0+signal); arg4ber=qq(ii)/sqrt(2); 
    ber(ii)=erfc(arg4ber)/2;
    lber(ii)=log10(ber(ii));end 
% ploting the dependences 
hold on
plot(prec,lber,'r'); 
%axis([20 30 -10^(-1) 10^(-1)]) 
%set(hPlot, 'LineWidth', 2);
%NF=4.77; 
 %F=10^{\circ} (NF/10) \cdot\frac{10}{6} = 10^(30/10);
$NO=0.5*(F*G-1)*E;%Lc=1-dblquad('dinteg', 1,1,0,0);
%alphafso=0.0002; 
lfso=1000;
%capitalLfso=10^(-alphafso*lfso);
%alphafiber=0.0002; 
%lfiber=20000; 
%capitalLfiber=10^(-alphafiber*lfiber); 
DRX=0.017;
%theta=0.0002; 
%capitalLbs=(DRX/(theta*lfso))^2;
%capitalLdemux=10^(0.35); 
%capitalLmux=10^(0.35); 
\frac{10^{18}}{20} = 10^(-3)*10^(8/10);
c2n=1.0e-13; 
k=2*pi/lambda; 
sigmaR2=1.23*c2n*k^(7/6)*lfso^(11/6); 
d=sqrt(k*DRX^2/(4*lfso)); 
alpha=1/(exp(0.49*sigmaR2/(1+0.65*d^2+1.11*sigmaR2^1.2)^*(7/6))-1);beta=1/(exp(0.51*sigmaR2*(1+0.69*sigmaR2^1.2)^(-5/6)/(1+0.9*d^2+0.62*(d^2)*sigmaR2^1.2))-1);
x=[];
v=[];
x=10^(-12):(10^(-3)-10^(-12))/2000:10^(-3);
prec1=[]; 
lberwtrb=[]; 
for ii=1:1:101 
     prec1(ii)=-30+(ii-1)*50/100; 
    p1(i) = 10^(-3)*10^(prec1(ii)/10); %*capitalLfso*capitalLbs*Lc*capitalLmux*capitalLfiber*capitalLdemux); 
     for iii=1:1:2001 
    hsig(iii)=x(iii)/p1(ii);
```
Table 7 (continued)

```
pgg(iii)=2*(alpha*beta)^((alpha+beta)/2)/(gamma(alpha)*gamma(beta))*(hsig(iii))^((alpha+beta)/
2-1)*besselk(alpha-beta, 2*sqrt(alpha*beta*hsig(iii)));
 sigma2shot1=2*q*2*r/(r+1)*capitalr*x(iii)*Be; 
 sigma2shot0=2*q*2/(r+1)*capitalr*x(iii)*Be; 
 sigma2sigASE1=4*capitalr*N0*2*r/(r+1)*capitalr*x(iii)*Be; 
 sigma2sigASE0=4*capitalr*N0*2/(r+1)*capitalr*x(iii)*Be; 
 sigma1=sqrt(sigma2shot1+sigma2sigASE1+sigma2shotASE+sigma2ASEASE+sigma2th);
      sigma0=sqrt(sigma2shot0+sigma2sigASE0+sigma2shotASE+sigma2ASEASE+sigma2th);
     current0tub(iii)=2/(r+1)*capitalr*x(iii);curent1tub(iii)=2*r/(r+1)*capitalr*x(iii);qq1(iii)=(curent1tub(iii)-curent0tub(iii))/(sigma0+sigma1);
     area4ber = qq1(iii)/sqrt(2);
 ber1(iii)=erfc(arg4ber)/2; %Lc*capitalLmux*capitalLfiber*capitalLdemux); 
 y(iii)=pgg(iii)*ber1(iii); 
       end
       berwtrb(ii)=trapz(x, y); 
      shift=1ber(1)-loq10(berwtrb(1));lberwtrb(ii)=log10(berwtrb(ii))+shift;end 
TrblncFrP=10^(-shift) 
%ber2(1)=ber1(1)/pgg(1); 
\text{Biber2}(1) = \text{load10}( \text{ber2}(1));%berint=[];%hsigint=[]; 
%for ii=2:1:1001
   % for iii=1:1:ii 
      % berint(iii)=ber1(iii); 
     % hsigint(iii)= hsig(iii);
      % end 
    % ber2(ii)=trapz(hsigint, berint); 
    % lber2(ii)=log10(ber2(ii));
    % end
```
BER comparison of the impact of two crosstalk sources and a single crosstalk source of equivalent power

See Fig. [16](#page-32-0).

Fig. 16 BER comparison of the impacts of two crosstalk sources and a single crosstalk source of equivalent power in a turbulent FSO DWDM DPPM system with coding level $M = 2$, $l_{fso, int} = 2000$ m and signal-to-crosstalk ratio $L_{demux,XT}$ (eprints.nottingham. ac.uk). (Reproduced with permission from Mbah et al. [2014\)](#page-34-12)

References

- Abtahi, M., Lemieux, P., Mathlouthi, W., Rusch, L.A.: Suppression of turbulence-induced scintillation in free-space optical communication systems using saturated optical amplifers. J. Lightw. Technol. **24**, 4966–4973 (2006)
- Aladeloba, A.O., Phillips, A.J., Woolfson, M.S.: DPPM FSO communication systems impaired by turbulence, pointing error and ASE noise. In: 14th International Conference on Transparent Optical Networks (ICTON), Coventry, UK (2012)
- Aladeloba, A.O., Phillips, A.J., Woolfson, M.S.: Performance evaluation of optically preamplifed digital pulse position modulation turbulent free-space optical communication systems. IET Optoelectron. **6**(1), 66–74 (2012a)
- Aladeloba, A.O., Phillips, A.J., Woolfson, M.S.: Improved bit error rate evaluation for optically preamplifed free-space optical communication systems in turbulent atmosphere". IET Optoelectron. **6**(1), 26–33 (2012b)
- Aladeloba, A.O., Woolfson, M.S., Phillips, A.J.: WDM FSO network with turbulence-accentuated interchannel crosstalk. OSA/IEEE **5**(6), 641–651 (2013)
- Aldibbiat, N.M., Ghassemlooy, Z., McLaughlin, R.: Indoor optical wireless systems employing dual header pulse interval modulation (DH-PIM). Int. J. Commun. Syst. **18**(3), 285–305 (2005)
- Al-Habash, M.A., Andrews, L.C., Phillips, R.L.: Mathematical model for the irradiance probability density function of a laser beam propagating through turbulent media. Opt. Eng. **40**, 1554–1562 (2001)
- Andrews, L.C., Phillips, R.L.: Laser Beam PropagationThrough Random Media, 2nd edn. SPIE, Bellingham, WA (2005)
- Andrews, L.C., Phillips, R.L., Hopen, C.Y.: Laser Beam Scintillation with Applications. SPIE Press, Bellingham, WA (2001)
- Ansari, N., Zhang, J.: Media Access Control and Resource Allocation for Next Generation Passive Optical Networks. Springer, Berlin (2013)
- Arnon, S.: Optical wireless communications. In: Driggers, R.G. (ed.) Encyclopedia of Optical Engineering, pp. 1866–1886. Marcel Dekker, Inc., New York (2003)
- Badar, N., Jha, R.K.: Performance comparison of various modulation schemes over free space optical (FSO) link employing Gamma-Gamma fading model. Opt. Quantum Electron. **49**, 192 (2017). [https://doi.](https://doi.org/10.1007/s11082-017-1025-4) [org/10.1007/s11082-017-1025-4](https://doi.org/10.1007/s11082-017-1025-4)
- Chan, V.W.S.: Free-space optical communications. IEEE/OSA J. Lightw. Technol. **24**(12), 4750–4762 (2006)
- Chen, C., Yang, H., Jiang, H., Fan, J., Han, C., Ding, Y. (2008) Mitigation of turbulence-induced scintillation noise in free-space optical communication links using Kalman flter. In: IEEE Congress on Image and Signal Processing, China, Hainan, vol. 5, pp. 470–473 (2008)
- Ciaramella, E., Arimoto, Y., Contestabile, G., Presi, M., D'Errico, A., Guarino, V., Matsumoto, M.: 1.28 terabit∕s (32×40 Gbit∕s) WDM transmission system for free space optical communications. IEEE J. Sel. Areas Commun. **27**, 1639–1645 (2009)
- Dar, A.B., Jha, R.K.: Chromatic dispersion compensation techniques and characterization of fber Bragg grating for dispersion compensation. Opt. Quantum Electron. **49**, 108 (2017). [https://doi.org/10.1007/](https://doi.org/10.1007/s11082-017-0944-4) [s11082-017-0944-4](https://doi.org/10.1007/s11082-017-0944-4)
- Dikmelik, Y., Davidson, F.M.: Fiber-coupling efficiency for free-space optical communication through atmospheric turbulence. Appl. Opt. **44**(23), 4946–4952 (2005)
- Ghassemlooy, Z., Popoola, W., Rajbhandari, S.: Optical Wireless Communications—System and Channel Modelling with MATLAB, 1st edn. CRC Press, London (2013)
- Gyselings, T., Morthier, G., et al.: Crosstalk analysis of multiwavelength optical cross connects. IEEE J. Lightw. Technol. **14**, 1423–1435 (1999)
- Hirano, A., Miyamoto, Y., Kuwahara, S.: Performances of CSRZ-DPSK and RZ-DPSK in 43-Gbit/s/ch DWDM G.652 single-mode-fber transmission. In: Optical Fiber Communications Conference, pp. 454–456 (2003)
- Karp, S., Gagliardi, R.M., Moran, S.E., Stotts, L.B.: Optical Channels: Fibers, Clouds, Water and the Atmosphere. Plenum, New York (1988)
- Kaushal, H., Jain, V. K., Kar, S.: Free Space Optical Communication, 1st edn. In: Optical Networks. (2017). <https://doi.org/10.1007/978-81-322-3691-7>
- Khalighi, M., Schwartz, N., Aitamer, N., Bourennane, S.: Fading reduction by aperture averaging and spatial diversity in optical wireless systems. J. Opt. Commun. Netw. **1**(6), 580–593 (2009)
- Killinger, D.: Free space optics for laser communication through the air. Opt. Photon. News **13**(10), 36–42 (2002)
- Lee, C.H., Sorin, W.V., Kim, B.Y.: Fiber to the home using a PON infrastructure. J. Lightw. Technol. **24**, 4568–4583 (2006)
- Majumdar, A.K.: Free-space laser communication performance in the atmospheric channel. J. Opt. Fiber Commun. Rep. **2**, 345–396 (2005)
- Manor, H., Arnon, S.: Performance of an optical wireless communication system as a function of wavelength. Appl. Opt. **42**(21), 4285–4294 (2003)
- Maru, K., Mizumoto, T., Uetsuka, H.: Demonstration of fat-passband multi/demultiplexer using multi-input arrayed waveguide grating combined with cascaded Mach-Zehnder interferometers. J. Lightw. Technol. **25**(8), 2187–2197 (2007)
- Mbah, A.M., Walker, J.G., Phillips, A.J.: Performance evaluation of digital pulse position modulation for wavelength division multiplexing FSO systems impaired by interchannel crosstalk. IET Optoelectron. **8**(6), 245–255 (2014)
- Mbah, A.M., Walker, J.G., Phillips, A.J.: Performance evaluation of turbulence-accentuated interchannel crosstalk for hybrid fbre and free space optical wavelength division multiplexing systems using digital pulse position modulation. IET Optoelectron **10**(1), 11–20 (2016)
- Mbah, A.M., Walker, J.G., Phillips, A.J.: Outage probability of WDM free-space optical systems afected by turbulence-accentuated interchannel crosstalk. J. Phillips IET Optoelectron. **11**(3), 91–97 (2017)
- Monroy, I.T., Tangdiongga, E.: Crosstalk in WDM Communication Networks. Kluwer Academic, Norwell, MA (2002)
- Ng, B., Ab-Rahman, M.S., Premadi, A., Jumari, K.: Optical power budget and cost analysis in PON-based *i*-FTTH. Res. J. Inf. Technol. **2**, 127–138 (2010)
- Phillips, A.J.: Power penalty for burst mode reception in the presence of interchannel crosstalk. IET Optoelectron. **1**, 127–134 (2007)
- Phillips, A.J., Cryan, R.A., Senior, J.M.: An optically preamplifed intersatellite PPM receiver employing maximum likelihood detection. IEEE Photon. Technol. Lett. **8**(5), 691–693 (1996)
- Popoola, W.O., Ghassemlooy, Z.: BPSK Subcarrier intensity modulated free-space optical communications in Atmospheric turbulence. J. Lightw. Technol. **27**(8), 967–973 (2009)
- Ramaswami, R., Sivarajan, K.N.: Optical Networks—A Pratical Perspective, 2nd edn. Academic, London (2002)
- Shapiro, J.H., Harney, R.C.: Burst-mode atmospheric optical communication. In: Proceedings of National Telecommunication Conference, pp. 27.5.1–27.5.7 (1980)
- Sibley, M.J.: Optical Communications: Components and Systems, 2nd edn. Macmillan Press Ltd, London (1995)
- Trinh, P.V., Dang, N.T., Thang, T.C., Pham, A.T.: Performance of all-optical amplify- and-forward WDM/ FSO relaying systems over atmospheric dispersive turbulence channels. IEICE Trans. Commun. **99**(6), 1255–1264 (2016)
- Vetelino, F.S., Young, C., Andrews, L., Recolons, J.: Aperture averaging efects on the probability density of irradiance fuctuations in moderate-to-strong turbulence. Appl. Opt. **46**(11), 2099–2108 (2007)
- Yang, L., Song, X., Cheng, J., Holzman, J.F.: Free-Space optical communications over lognormal fading channels using OOK with fnite extinction ratios. IEEE Access **4**, 574–584 (2016)
- Yu, C.X., Neilson, D.T.: Difraction-grating-based (de)multiplexer using image plane transformations. IEEE J. Sel. Top. Quantum Electron. **8**(6), 1194–1201 (2002)
- Zuo, T.J., Phillips, A.J.: Performance of burst mode receivers for optical digital pulse position modulation in passive optical network application. IET Optoelectron. **3**(3), 123–130 (2009)

Afliations

Ebrahim Eld. Elsayed1 · Bedir B. Yousif2 · Mahmoud M. Alzalabani1

Bedir B. Yousif bedir.yousif@gmail.com

Mahmoud M. Alzalabani mmalzalabani@yahoo.com

- ¹ Electronics and Communications Department, Faculty of Engineering, Mansoura University, Mansoura 35516, Egypt
- ² Electrical Engineering Department, Faculty of Engineering, Kafrelsheikh University, Kafrelsheikh 35514, Egypt