

Growth curve analysis of asymptomatic and symptomatic meningiomas

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Abstract Meningiomas sometimes appear to stop growing after attaining a large size. Commonly used exponential growth models do not reflect this phenomenon. We attempted to find the best curve to simulate their growth. Fifty-two patients with meningioma were followed up for 3.1–21.7 years (mean 7.5 years) with four or more imaging studies each. Thirty-one patients had asymptomatic tumors. The other 21 patients with residual or recurrent tumor were followed up after surgery. Time–volume curves for each tumor were plotted. Nonlinear regression analyses were performed against power, exponential, logistic, and Gompertzian curves. Time–volume curves corresponded to the Gompertzian and logistic growth curves better than to power or exponential curves. When simulating time–volume curves with Gompertzian curves, the majority of benign meningiomas began to slow their growth before patient age of 80 years. Twenty-three of 31 asymptomatic meningiomas had already passed the inflection point before diagnosis. In contrast, this happened less frequently in symptomatic tumors. Especially, all six atypical meningiomas continued to grow quasi-exponentially. Sigmoid curves that approach a plateau were better descriptors of the growth of benign meningiomas than were curves of

unlimited growth. However, atypical meningiomas were unlikely to slow their growth.

Keywords Growth kinetics · Magnetic resonance imaging · Meningioma · Volumetry

Introduction

Meningiomas usually grow slowly with a long initial asymptomatic phase, and may remain silent until the patient's death. The incidence of asymptomatic meningioma found at autopsy is 1–2.3% [1–3]. On the other hand, the incidence of symptomatic meningiomas found in population-based studies is 2–4 per 100,000 person-years [4–6]. These results imply that only a small proportion of meningiomas become symptomatic. Actually, only 3–6% of clinically detected asymptomatic meningiomas later become symptomatic [7–9]. This may be due to slow growth of incidentally found asymptomatic meningiomas. Another explanation might be that meningiomas may stop growing at some point, and a key difference between symptomatic and asymptomatic tumors may be their size when they stop growing.

Figures for the proportion of asymptomatic meningiomas which were found to be growing when they were discovered have varied from 11% to 100% [7–15]. This wide range of rate figures is due to differences between measurement methods and the length of follow-up periods. Exact volumetric measurement using image-analysis software usually showed higher rates of tumor growth than calculations using diameter as a growth indicator. Even among studies based on exact volumetry, very few of them set a cutoff point for discriminating between growing and nongrowing tumors in view of measurement error [10, 16].

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As the growth rate of a tumor directly affects the patient's prognosis and therapeutic options, many investigators have attempted to find a model for meningioma growth [9, 12–14, 16–21]. Most of these studies were based on the hypothesis that each meningioma grows at a constant rate. One long-term observation in a limited number of cases revealed that meningiomas showed three growth patterns, namely exponential, linear, and no growth [16]. Other observations including 70 cases for a mean follow-up period of 3.3 years supported that idea [10]. However, both of these studies raise the possibility that these growth patterns may change in the long term; exponentially growing tumors may decelerate their growth and even stop growing. If this is true, it may not be appropriate to use a linear or exponential curve to predict the growth of meningiomas in the long term. Better understanding of the growth kinetics of the tumor is of paramount importance for choice of more successful strategies. We attempted to analyze the growth of meningiomas using various curves to find the best growth model.

Materials and methods

Because growth analysis requires multiple imaging studies over a sufficiently long period, we studied patients with meningiomas that were followed up without radiation therapy, with four or more radiological studies over more than 3 years. We examined the clinical records of patients with meningioma during the period between 1980 and 2004 at the Department of Neurosurgery, Shiga University of Medical Science and during the period between 2001 and 2004 at the Division of Neurosurgery, Shizuoka Cancer Center. Neurofibromatosis cases were excluded. We identified 52 patients, 13 men and 39 women; their median age was 57.6 years at their first imaging study, and the mean follow-up period was 7.7 years (range 3.1–21.7 years). Of those 52, 31 had asymptomatic tumors, and the other 21 were postoperative patients with residual or recurrent tumors; of those 21, 6 had atypical meningioma while the other 15 had benign meningioma. In the 21 patients with residual or recurrent tumors, 5 (that is, 4 atypical and 1 benign) had undergone macroscopically total resection; the volumes of the tumors immediately after macroscopically total resection were defined as equal to 0.1 cm^3 , as in two previous studies [18, 19]. A further five patients underwent another surgery during the follow-up. Tumor growth in those patients was analyzed both after the first surgery and after the second surgery separately, yielding data for two growth curves each. In each of those five cases the growth curve for the longer follow-up period was used for statistical analysis. The majority of cases had at least one plain computed

tomography (CT) scan, although nonenhanced scans were not employed in volume analysis.

Tumors were classified by histology according to the World Health Organization (WHO) classification system [22].

Measurement of tumor volume

Images obtained from CT scanning or magnetic resonance imaging (MRI) were taken into a computer system. Although MRI was used for analysis in most cases, CT scanning was mainly employed in three cases. The tumor area in each slice was measured using NIH image software 1.62, and the tumor volume was calculated by the slice thickness of the image. Each volume was measured three times, and the mean value was calculated. Any change less than 8.2% between the initial and the last volume was considered as no change because the mean standard deviation was 4.1% of the calculated volume using this method [16].

Curve fitting

We tested four representative growth curves for analysis of meningioma growth (Fig. 1). Exponential growth is the most commonly used tumor growth model. In this model, the cells divide at a constant rate with constant cell loss, and increase perpetually. The power law is a growth model that shows various shapes of growth curves such as root, linear, and parabolic curves. This group of curves exhibits unlimited growth with various changes in the growth rate. Another class of growth models consists of sigmoid curves such as the logistic and Gompertzian curves. These show quasi-exponential proliferation followed by gradually decelerating growth rate. The point at the beginning of deceleration is called the inflection point, after which the curve approaches a plateau.

A time–volume curve was plotted for each tumor. Nonlinear regression analysis against power, exponential, logistic, and Gompertzian growth curves (Fig. 2, equations shown in the Appendix) were performed using Statistica 4.1 (StatSoft, Tulsa, OK, USA). The correlation coefficients (R) and coefficients of determination (R^2) were calculated. In the Gompertzian and logistic analysis of the time–volume curves, inflection points were calculated from the equation in the Appendix. Patient age at the inflection point was compared with patient age at the first imaging study and at last follow-up, to find whether and when each tumor began to slow its growth. In the previous study, the deceleration of growth speed of benign meningiomas appeared to be related to tumor age [16]. We attempted to analyze patient age when the tumor began to slow its growth (inflection point) using Kaplan–Meier method.

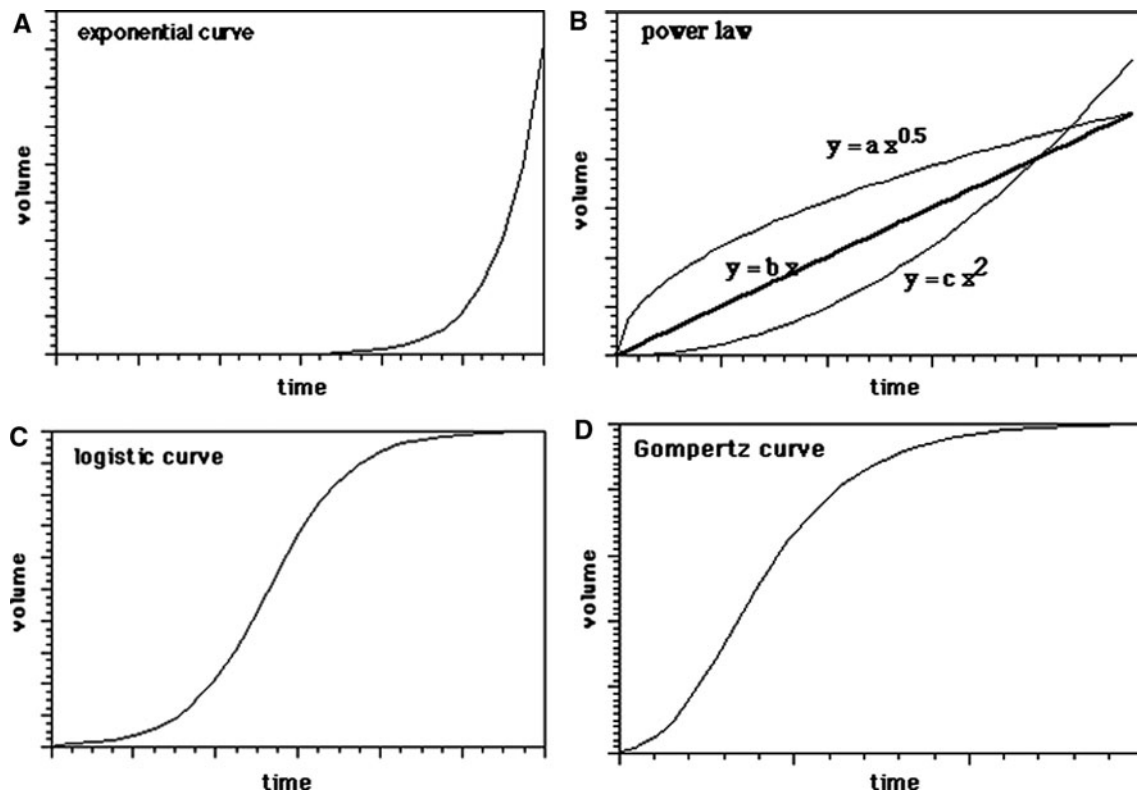


Fig. 1 Four growth curves for analysis of meningioma growth: **a** exponential curve, **b** power curves, **c** logistic curve, and **d** Gompertzian curve

Statistical methods

Statistical analyses were performed using Statistica 4.1 (StatSoft, Tulsa, OK, USA) and Stata version 11.1 (StataCorp LP, College Station, TX, USA). Coefficients of determination were summarized by their quartiles for all cases ($N = 44$), and separately for benign tumors ($n = 38$) and atypical tumors ($n = 6$). Quartiles were estimated by linear interpolation between neighboring sample values as necessary. Comparisons were made between model types (exponential, power, logistic, and Gompertzian) by Wilcoxon's signed-rank test. Comparisons were made for all tumors, and separately for benign tumors and atypical tumors. Bonferroni's inequality was used to adjust P -values for multiple comparisons.

We analyzed patient age at the inflection point using a Kaplan–Meier method. Patients who had not passed the inflection point at last follow-up were censored in the analysis.

Results

Of the 52 patients with meningioma, 44 patients' tumors displayed measurable growth during the observation period covered in this report. Summary statistics for coefficients of determination of curve fits for those 44 tumors are shown in

Tables 1 (all tumors), 2 (benign tumors only), and 3 (atypical tumors only). For all tumors (Table 1), as well as for the subset of nonmalignant meningiomas (Table 2), median R^2 was higher for logistic and Gompertzian model types than for exponential and power. R^2 for power model type was higher than that for exponential. In terms of R^2 , logistic and Gompertzian models fitted equally well to longitudinal measurements of tumor volume. For the subset of atypical meningiomas (Table 3), a statistically significant difference in R^2 between model types was not detected.

One example of growth of a benign recurrent meningioma, with the longest follow-up in this series, is shown in Fig. 2. The meningioma enlarged about eight times during the first 79 months, and less than twice during the next 89 months. The time–volume curve was fitted by a Gompertzian curve or a logistic curve better than by a power or exponential curve.

Because patient age at the inflection point calculated from Gompertzian curves correlated highly with those from logistic curves ($R = 0.98$, $P < 0.000001$) (Fig. 3) and the mean ages were almost equal (60.6 ± 11.2 versus 59.8 ± 11.7 years), we performed the following analysis using the data from Gompertzian curves. Kaplan–Meier analyses of the inflection point in each patient indicated that the majority of benign meningiomas begin to slow their growth before the age of 80 years (Fig. 4). In contrast,

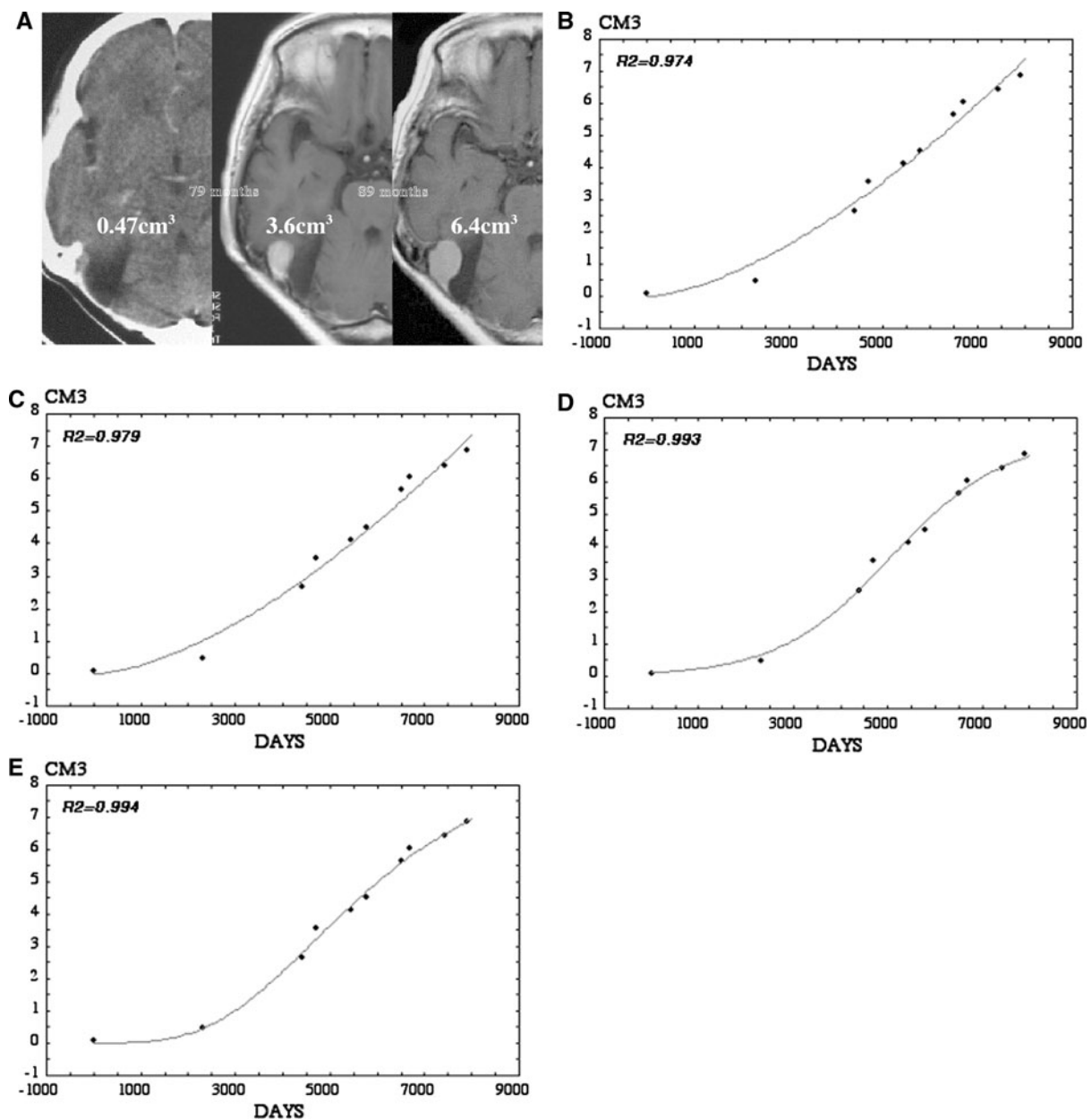


Fig. 2 a Sequential MR images of a recurrent meningioma in a patient with the longest follow-up. The meningioma enlarged about eightfold during the first 79 months, but less than doubled during the

next 89 months. Curve fitting to exponential (b), power (c), logistic (d), and Gompertzian curve (e)

atypical meningiomas never decelerated their growth (log-rank test, $P = 0.04$, Fig. 4).

Of tumors with calcification, eight showed no growth, as their mean volume change was measured at 2.8% over the mean 5.7 years. Their growth curves were considered to be in the plateau phase of the Gompertzian or logistic curve. Of the 31 asymptomatic meningiomas, 23 had already passed their inflection point (and 8 of those had stopped growing) before diagnosis, and 3 more passed their inflection point during the mean follow-up period of 5.7 years. Of the 15 symptomatic but benign meningiomas, 6 passed their

inflection point before diagnosis, and 5 more did so during the mean follow-up period of 9.9 years. Asymptomatic meningiomas had passed the inflection point before diagnosis more frequently than had symptomatic benign meningiomas (χ^2 -test, $P = 0.025$). However, Kaplan–Meier analyses showed no difference of patient age at inflection point between symptomatic and asymptomatic meningiomas (log-rank test, $P = 0.53$, Fig. 5). This was partly due to older age at diagnosis in patients with asymptomatic meningiomas (64.5 ± 9.6 years old) than those with symptomatic benign ones (52.2 ± 11.0 years

Table 1 Coefficients of determination (all meningiomas, $N = 44$)

Regression model	Percentile		
	25th	50th (median)	75th
Exponential	0.87	0.95	0.96
Power	0.86	0.96	0.99
Logistic	0.93	0.98	0.99
Gompertzian	0.93	0.98	0.99

Paired comparisons (Wilcoxon’s signed-rank test)	
Comparison	Bonferroni-adjusted P -value
Exponential versus power	0.005
Exponential versus logistic	<0.001
Exponential versus Gompertzian	<0.001
Power versus logistic	<0.001
Power versus Gompertzian	<0.001
Logistic versus Gompertzian	1.0

Table 2 Coefficients of determination (benign meningiomas, $n = 38$)

Regression model	Percentile		
	25th	50th (median)	75th
Exponential	0.82	0.94	0.97
Power	0.89	0.96	0.99
Logistic	0.93	0.98	0.99
Gompertzian	0.93	0.98	0.99

Paired comparisons (Wilcoxon’s signed-rank test)	
Comparison	Bonferroni-adjusted P -value
Exponential versus power	<0.001
Exponential versus logistic	<0.001
Exponential versus Gompertzian	<0.001
Power versus logistic	<0.001
Power versus Gompertzian	<0.001
Logistic versus Gompertzian	0.44

old) (Mann–Whitney U test, $P = 0.0008$). In contrast, none of the atypical meningiomas passed the inflection point.

Discussion

We showed that the growth curves of meningiomas fitted the sigmoid Gompertzian and logistic curves with high R^2 . We previously reported that meningiomas matched three growth patterns, namely exponential, linear, and no growth [16]. Some cases showed changes in apparent growth pattern from exponential to linear and from linear to no growth. In this study, the sigmoid growth model could fit all these changes with one equation, and seems useful for

Table 3 Coefficients of determination (atypical meningiomas, $n = 6$)

Regression model	Percentile		
	25th	50th (median)	75th
Exponential	0.91	0.98	1.00
Power	0.74	0.89	1.00
Logistic	0.93	0.97	1.00
Gompertzian	0.93	1.00	1.00

Paired comparisons (Wilcoxon’s signed-rank test)	
Comparison	Bonferroni-adjusted P -value
Exponential versus power	0.70
Exponential versus logistic	1.0
Exponential versus Gompertzian	1.0
Power versus logistic	0.45
Power versus Gompertzian	0.70
Logistic versus Gompertzian	1.0

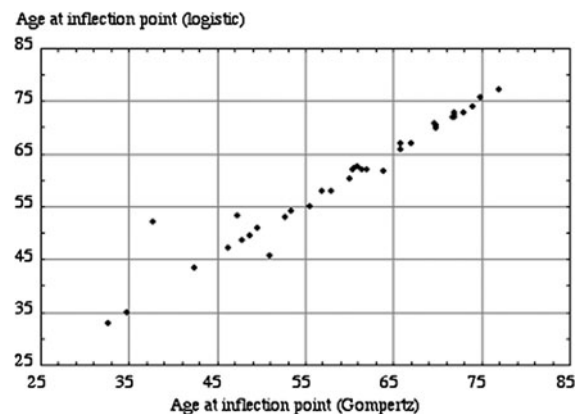


Fig. 3 Relationship between calculated age at the inflection point from Gompertzian and logistic curves ($R = 0.983$, $P < 0.000001$)

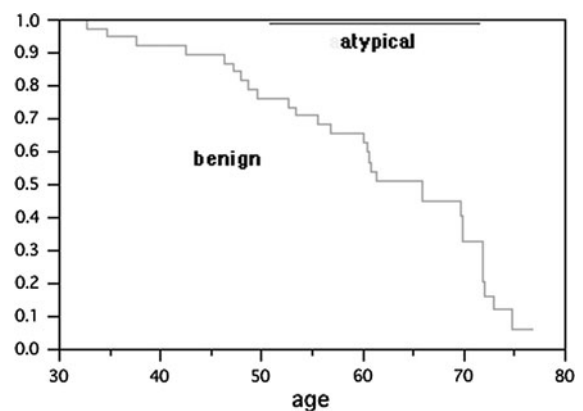


Fig. 4 Kaplan–Meier analysis of patient age at the inflection point. Atypical meningiomas are unlikely to pass the inflection point compared with benign meningiomas (log-rank test, $P = 0.04$). Atypical: atypical meningioma; benign: benign meningiomas

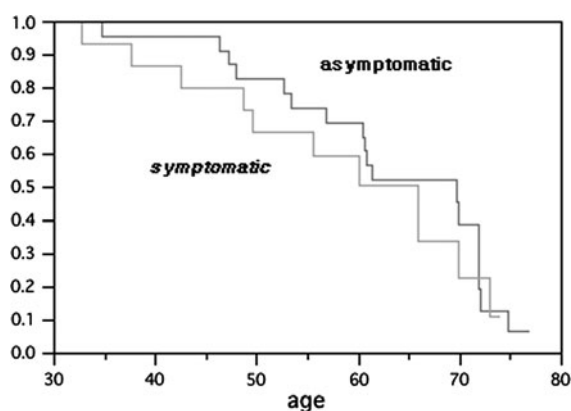


Fig. 5 Kaplan–Meier analysis of patient age at the inflection point: no difference was found between patients with asymptomatic and symptomatic benign meningiomas (log-rank test, $P = 0.53$)

describing the growth of meningiomas. This model is in accordance with the previous observations that meningiomas in the elderly grow more slowly than those in younger people [9, 11–13, 23].

This study demonstrated that growth speed of benign meningiomas might change in the long term. In this context, application of the proper growth model is indispensable for prediction of growth and for decision-making in treatment. Especially, it is very important to know the time when tumors begin to slow their growth (the inflection point). It is expected that a tumor with Gompertzian growth can grow as much as 2.7 times larger after its inflection point. In this study, 26 of 31 incidental meningiomas passed their inflection point before or during the observation period. This explains why most of the incidental meningiomas were found to grow slowly and remain asymptomatic. Although the growth of atypical meningiomas was fitted well by the pre-inflection regions of the Gompertzian and logistic curves, it is unlikely that atypical or anaplastic meningiomas slow their growth spontaneously. The sigmoid curve can be adapted to the growth of tumors that would not have an inflection point, by setting a large value for the inflection point.

Most studies on growth analysis using sigmoid curves utilized cell lines [24–27]. Application of this model to clinical neoplasms has been attempted using historical clinical data [28–30]. In benign tumors, the whole processes are difficult to observe during the follow-up period. In fact, for the mean follow-up period of 7.7 years, we were able to observe both the exponential and decelerating growth phase in only eight tumors. Shorter follow-up may reveal only an apparently exponential, linear, or no-growth phase.

Several biological and biophysical hypotheses have been proposed to explain why the sigmoid growth model is

a good descriptor of the biological growth of tumors [24, 25, 31–33]. All of these studies are based on the idea that the tumor volume saturates when the tumor becomes larger. The larger the tumor, the more likely the proliferating cells are to become quiescent, and the less likely the quiescent cells are to re-enter the proliferation cycle. In this context, growth should accelerate again when the volume is reduced by surgery [34]. However, the growth rate of benign meningiomas slowed even when the size became smaller after surgical removal [16]. When comparing patient age at the inflection point among those with asymptomatic and symptomatic meningiomas, they did not differ when the latter experienced surgical removal. Thereafter, it appears that the deceleration of growth of benign meningiomas correlates with tumor or patient age. This means that the mechanism of growth saturation in meningiomas would be different from that of experimental tumors *in vitro* and *in vivo*.

This study has several limitations. This was a retrospective study that enrolled selected patients. The design of this study might have included a bias toward selecting tumors which were not growing. However, the incidence of tumor growth among the asymptomatic meningiomas in this series (74.2%) was not lower than in previous reports. Moreover, the finding that even symptomatic tumors with recurrence or regrowth showed growth deceleration in the long run supports the idea of the sigmoid growth model for benign meningiomas. Another limitation of this study arises from the errors of volume measurement. Tumors of small size are apt to pose problems of partial volume effect and slice thickness of the images. If more exact measurement were possible, then a more precise prediction in an early phase might be made. Although we employed Gompertzian and logistic curves as a sigmoid function, there are other forms of sigmoid equations [32]. If more precise measurement becomes possible, it may be determined which is the best descriptor of tumor growth.

Growth may not be self-limiting when benign meningiomas acquire malignant change. However, the reported incidence is low. Schiffer et al. [35] stated that only 2 of 53 recurrent meningiomas progressed from benign to atypical. None in our present series showed malignant change of grade 1 meningioma.

Estimation of growth in the present method has limitations, and a long follow-up period is necessary. Further study may reveal definite radiological or clinical features that distinguish tumors that have passed the inflection point. Calcification of a tumor may be one such candidate. Elucidation of the mechanism of the self-limiting growth model may make it possible to predict the plateau volume and inflection point from a surgical specimen.

Conclusions

We have presented for the first time the applicability of a self-limiting growth model for simulation of benign meningioma growth. Benign meningiomas may pass the inflection point and approach their plateau volume in the long run, while atypical meningiomas are not likely to do so. This difference may be one reason for the lower recurrence rate in benign meningiomas than in higher-grade ones even after incomplete surgery. Further refinement of the methodology and elucidation of the mechanism should enable us to predict growth of meningiomas more precisely and simply.

Appendix

Growth curve equations used in this article are shown below, where α , β , and γ are constants, and $V(t)$ is the volume at time t .

Exponential curve : $V(t) = \alpha\beta^t + \gamma$

Power curve [28] : $V(t) = (\alpha t(1 - \beta) + \gamma)^{1/\beta}$

The power curves show rapid increase of volume when $0 < \beta < 1$, linear growth when $\beta = 0$, and gradual deceleration when $\beta < 0$.

Logistic curve : $V(t) = \gamma / (1 + \alpha \exp(-\beta t))$

Gompertzian curve : $V(t) = \alpha \exp(-\beta \exp(-\gamma t))$

Inflection point : $T_i = (\ln(\alpha/\beta))/\beta$

T_i was described as days after the initial observation time. A negative T_i value indicates that the inflection point was before the initial imaging study. However, if T_i is beyond the observation period, the tumor was still growing quasi-exponentially.

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