RESEARCH PAPER

The effect of nanoparticle concentration on the rheological properties of paraffin-based $Co₃O₄$ ferrofluids

S. Masoud Hosseini • E. Ghasemi • A. Fazlali • Dale E. Henneke

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Abstract A series of ferrofluids were made using oleic acid-capped $Co₃O₄$ (cobalt oxide) nanoparticles in liquid paraffin by a high-energy milling/sonication method. The average physical size of the dry $Co₃O₄$ nanoparticles was determined to be 21 nm by measuring the peak broadening of the (311) crystal plane from X-ray diffraction data of the nanopowder. The results of measurements by an alternative gradient force magnetometer indicated that the dry nanoparticles were paramagnetic. The prepared colloids were characterized by dynamic light scattering and found to contain

S. M. Hosseini Unit of Residue Fluidized Catalytic Cracking (RFCC), Emam Khomeini Petroleum Refinery, Shazand, Iran

S. M. Hosseini - A. Fazlali Department of Chemical Engineering, Faculty of Engineering, Arak University, Arak, Iran e-mail: a-fazlali@araku.ac.ir

E. Ghasemi Institute for Colorants, Paint and Coating (ICPC), 1668814811 Tehran, Iran e-mail: eghasemi@iust.ac.ir

D. E. Henneke (\boxtimes) Department of Chemical Engineering, University of Waterloo, Waterloo, Ontario, Canada e-mail: henneke@uwaterloo.ca

aggregated nanoparticles having between 51 and 835 individual particles per aggregate. The rheological properties of these ferrofluids were then studied using a standard rotating rheometer, both in the presence and absence of an externally applied magnetic field. Magnetoviscous and thixotropic effects on the ferrofluids viscosity were studied as both the nanoparticle concentration and the applied magnetic field was varied. Nanoparticle aggregation and its effect on the rheological properties of these ferrofluids is discussed (i.e. the interactions between nanoparticles and aggregates). At nanoparticle concentrations above 30 wt%, a combined thixotropic/magnetoviscous effect on the fluids viscosity was observed. The ferrofluids exhibited a thixotropic behaviour with little magnetoviscous effect at more dilute nanoparticle concentrations, 25 wt%.

Keywords $Co₃O₄$ nanoparticles \cdot Cobalt oxide nanoparticles - Paramagnetic nanofluids - Viscosity - Nanoparticle interactions

Introduction

A magnetic nanofluid or ferrofluid is a stable suspension of magnetic nanoparticles, such as $Fe₃O₄$ (iron oxide, magnetite) (Ghasemi et al. 2008), CoFe₂O₄ (cobaltferrite) (Didukh et al. [2002](#page-5-0)), Mn–Zn (manganese–zinc ferrites) (Arulmurugan et al. [2006\)](#page-5-0), Co–Zn (cobalt–zinc ferrites) (Arulmurugan et al. 2005), Li₂O–Fe₂O₃ (lithium ferrite) (van der Meer et al. [2009\)](#page-6-0) in a liquid base.

S. M. Hosseini

Department of Research and Technology, Emam Khomeini Petroleum Refinery, Shazand, Iran e-mail: s.masoudhoseini@gmail.com

The base liquid can be polar or non-polar, but for the nanoparticle to remain unagglomerated, the nanoparticle surface must be covered with a suitable capping agent (Charles [2002](#page-5-0)). The capping agent, typically a surfactant, maintains the stability of the colloid even when a highgradient magnetic field is applied (Bolshakova et al. [2005\)](#page-5-0). Ferrofluids are commonly used in industrial applications and in the field of medicine (Scherer and Figueiredo Neto [2005](#page-6-0); Rosenweig [1985\)](#page-6-0). The rheological properties of ferrofluids are an important area of study and enable new applications for ferrofluids to be developed. Magnetic fields have been found to cause nanoparticles of magnetic materials to form chains and aggregates within the ferrofluid, which affect the macroscopic properties of the fluid for even dilute suspensions (Zubarev et al. 2002; Morozov and Shliomis [2002](#page-6-0); Zubarev and Iskakova [2003](#page-6-0); Ivanov and Kantorovich [2003;](#page-6-0) Odenbach and Störk [1998\)](#page-6-0). It has also been found that the particle size distribution affects the interactions between particles (Odenbach and Raj [2000;](#page-6-0) Blanco-Mantecon and O'Gray [2006](#page-5-0)), but particleto-particle interactions have not been considered in current theoretical descriptions for the dynamic properties of ferrofluids (Zubarev 2002; Odenbach [2002\)](#page-6-0). A variety of models have been developed to describe how particle concentration affects the viscosity of colloidal suspensions. The first theory for dilute, mono-sized, colloids was presented by Einstein [\(1906](#page-5-0)):

$$
\eta_s = \eta_l (1 + K_H \phi) \tag{1}
$$

where η_s is the viscosity of the suspension, η_l is the viscosity of the base fluid, K_H is the shape factor for the particles ($K_H = 2.5$ for spherical particles) and ϕ is the volume fraction of particles in suspension. The effect of particle size on a fluids viscosity is not considered in the Einstein model, but the model does account for particle shape and the concentration of particles in the suspension. Equation (1) is only valid for dilute colloids where particle-to-particle interactions do not occur. As the particle concentration of the colloid increases, the likelihood of particle-to-particle interactions occurring is likewise increased. As such, a correction to the Einstein equation is made for concentrated colloidal suspensions as follows (Hunter [2001](#page-6-0)):

$$
\eta_s = \eta_l (1 + 2.5\phi_h + 6.2\phi_h^2) \tag{2}
$$

where ϕ_h is the hydrodynamic volume fraction. Chow [\(1993](#page-5-0)) presented a theoretical analysis for the effective fluid viscosity of concentrated suspensions by taking particle interactions into account, but this analysis is limited to low-shear viscosity colloids:

$$
\frac{\eta}{\eta_o} = \exp(\frac{2.5\phi_h}{1 - \phi_h}) + \frac{A\phi_h^2}{1 - A\phi_h^2 \phi_m}
$$
(3)

where $\phi_{\rm m}$ is the maximum hydrodynamic volume fraction, and A is the coupling coefficient between the particles $(A = 4.67$ for fluids where there is no interaction between particles). The Krieger–Dougherty model (Hunter [2001\)](#page-6-0) describes the change in viscosity for concentrated suspensions as particle concentration is varied:

$$
\eta = \eta_s \left(1 - \frac{\phi_h}{\phi_m} \right)^{-\eta \phi_m} \tag{4}
$$

where η is the intrinsic viscosity. For spherical particles, the intrinsic viscosity was found to be between 2.5 and 2.925.

Previously, the authors investigated the rheological properties of a paraffin-based γ -Fe₂O₃ ferrofluids that were prepared by a milling method (Hosseini et al. [2010\)](#page-5-0). In this study, we determined the effect of concentration on the rheological properties and magnetoviscous effect of $Co₃O₄$ ferrofluids; little work on the rheological properties of such ferrofluids can be found in the literature.

Experimental

Materials

A Co3O4 magnetic nanoparticle powder having a mean particle size less than 50 nm was obtained from Aldrich. Pure liquid paraffin was provided by Arman Sina, and the oleic acid (OA), used as a nanoparticle capping agent, was obtained from Merck. All of the chemicals used in this study were analytical grade and were used as delivered.

Preparation of the nanoparticle ferrofluid

Ferrofluids were prepared by mixing 20 g of $Co₃O₄$ nanopowder with 50 cc of OA. The OA was added to the nanoparticles as a capping agent and to improve the dispersion of nanoparticles in the prepared ferrofluids. OA has been successfully used previously for $Fe₂O₃$ nanoparticles to ensure that the nanoparticles remain unagglomerated during testing (Ghasemi et al.

[2008\)](#page-5-0). The mixture was then milled in a Fritsch Pulverisette model planetary mill for 5 h to ensure that the particles are well capped. A series of stable nanoparticle suspensions in liquid paraffin having different particle concentrations were then made by: (1) adding an appropriate amount of paraffin and OA; (2) mechanically mixed them; and (3) sonicating the suspension in an ultrasonic bath (Fritsch Ultrasonic, laborette 17, frequency: 5,060 Hz) for 10 min.

Characterization of the nanoparticle ferrofluid

The dry $Co₃O₄$ nanoparticles were characterized using a Philips PW 1800 X-ray diffractometer equipped with a copper source and a nickel filter ($\lambda = 1.5418$ Å) in a continuous scan mode from 5° to 90° with a scanning rate of 0.02° per second. The average size of the crystallites was calculated from X-ray line broadening using Scherrer's formula (Scherrer [1918\)](#page-6-0):

$$
D = \frac{0.9 \cdot \lambda}{\beta \cdot \cos(\Theta)}\tag{5}
$$

where D is the average crystalline size, λ is the X-ray wavelength, β is the angular line width of halfmaximum intensity, and Θ is the Bragg angle in degrees. For the (311) peak of the dry nanoparticle sample, β was found to be 0.76 \degree resulting in a mean nanoparticle size of 21 nm. Magnetization measurements were carried out using an alternative gradient force magnetometer (local AGFM: model 155) at room temperature. The size distributions of the ferrofluids were measured using a Malvern 3000 Dynamic Light Scattering (DLS) system. The rheological properties of the prepared ferrofluids were measured using a MCR300 rheometer made by Physica Anton Paar GmbH. In this system, a plate– plate spindle (PP25-MRD, diameter $= 1.95$ cm) was employed for all of the measurements with a sample volume of 0.3 mL. A magnetic field was applied at vertical direction to the sample during the tests. Using a Peltier and water circulation system, the temperature of samples was controlled during the measurements with a precision of ± 0.01 °C.

Results and discussion

Figure 1 shows the X-ray powder diffraction spectra of the dry Co_3O_4 nanopowder. All of the peaks observed in this scan correspond to the $Co₃O₄$ phase. An average crystallite size of 21 nm was calculated by measuring the peak broadening of the (311) crystal plane for $Co₃O₄$. These results are consistent with the reported size of the material from the manufacturer $(i.e. < 50 \text{ nm})$. All of the peaks are relatively sharp which indicates that the material is crystalline and relatively pure.

A hysteresis curve for the dry $Co₃O₄$ nanoparticles obtained from the magnetometer is shown in Fig. 2. In this plot it can be seen that the $Co₃O₄$ nanoparticles exhibit a paramagnetic behaviour and have a saturation magnetization of 0.45 emu/g. From this figure, it is clear that the magnetization curve increases continuously as the applied magnetic field strength is increased. For superparamagnetic behaviour it is common to plot M versus $\frac{1}{H}$ and assume that M is equal to M_s when the applied field is off, $H = 0$. Using this method, the approximated value for M_s is 0.45 emu/g.

Fig. 1 X-Ray diffraction pattern of the dry $Co₃O₄$ nanopowder

Fig. 2 Magnetometer hysteresis loop for dry $Co₃O₄$ Powder

These saturation magnetization values are considerably less than what has been reported for γ -Fe₂O₃ (82 emu/g, particle diameter $\lt 16$ nm) and Fe₃O₄ (70 emu/g, particle diameter $\lt 16$ nm) (Sun and Zeng) [2002\)](#page-6-0). As such, a weaker magnetoviscous effect can be expected in the prepared ferrofluids compared to $Fe₂O₃$ and $Fe₃O₄$ nanoparticle-based ferrofluids.

The DLS measurement of the 40 wt% ferrofluid suspension is shown in Fig. 3. This measurement is representative of the other ferrofluid suspensions and shows that the mean hydrodynamic particle size is 146 nm with hydrodynamic diameters varying between 95 and 240 nm. The number of nanoparticles in the aggregates can be estimated using a spherical agglomerate model:

$$
n = k \left(\frac{D}{d}\right)^3 \tag{6}
$$

where d is the mean particle size, D is the hydrodynamic particles size and k is the particle packing factor. In this model it is assumed that: (1) the particles and aggregates are spherical; (2) the nanoparticles are symmetric; and (3) the nanoparticles form a densely packed structures. Using this model, with an average nanoparticle size of 21 nm, a mean hydrodynamic size of 146 nm, and a packing factor of 0.74, the average number of particles per aggregate is calculated to be 338. When considering the lower and upper limits of the DLS size ranges (95 and 240 nm), the number of nanoparticles is 51 to 835 per aggregate.

A plot showing the viscosity of the ferrofluids versus shear rate is shown in Fig. 4. Regardless of the concentration of $Co₃O₄$ nanoparticles in the ferrofluid, all of these suspensions exhibit a shear-thinning behaviour. This behaviour has been observed in ferrofluids using other base fluids and magnetic nanoparticles. It has been hypothesized that the

Fig. 3 DLS results for 40 wt%, OA capped, 21 nm, $Co₃O₄$ particles in liquid paraffin

Fig. 4 Viscosity of the prepared ferrofluid versus shear rate

behaviour is due to the presence of weak bonds between particles. These weak bonds are thought to be responsible for the shear-thinning effect (Odenbach [2002\)](#page-6-0). As the shear rate increases, the existing weak particle-to-particle bonds are progressively broken and the viscosity decreases. As the particle concentration is reduced, the particle-to-particle interactions also become weaker. As such, for dilute ferrofluids (i.e. those with ≤ 5 wt% nanoparticles) at shear rates greater than $100 s^{-1}$, a relatively constant value is observed. These constant values indicate that the fluid has changed from a shear-thinning to a Newtonian fluid behaviour.

In Fig. 5, the effect of the nanoparticle concentration on the ferrofluids viscosity is shown at a shear rate of $120 s^{-1}$. Using the models that have been

Fig. 5 Comparison between experimental data and theoretical models describing viscosity versus particle volume fraction. No magnetic field was applied to these fluids $(H = 0 \text{ A})$

previously described, the theoretical values of the fluid viscosity versus particle concentration are also shown in this figure (Fig. [5\)](#page-3-0). It is clear that these models do not accurately predict the experimentally obtained values for ferrofluids at higher particle concentrations (i.e. at hydrodynamic volume fractions $\geq 0.04 \ \%_{V/V}$). Since these models do not account for particle-toparticle interactions, this result is not entirely surprising at these higher particle concentrations. A relatively high shear rate was used to reduce the interactions between aggregated particles. In this figure, it is clear that, in spite of such a large shear rate, there is large difference between the measured fluid viscosity and the viscosities calculated by the previously mentioned models. This indicates that there are strong interactions between the aggregated particles. At lower nanoparticle concentrations (≤ 0.024 % $_{\rm V/V}$), there is fairly good agreement between the measured values and the theoretical model, which indicates that there are weaker particle-to-particle interactions at lower nanoparticle concentrations.

Thixotropic fluids exhibit viscosities that are time dependent (Mezger [2002\)](#page-6-0). Thixotropic behaviour in a fluid arises when weak bonds between particles or molecules in a fluid begin to form (e.g. van der Waals forces). The effect of these weak bonds significantly impacts the viscous nature of the fluid and cannot be disregarded in thixotropic fluids. Figure 6 shows the variation in viscosity over time at a constant shear rate of 5 s^{-1} . In this case, a relatively small shear rate of $5 s⁻¹$ was used to show the effect of particle interactions with time. At nanoparticle concentrations less than 20 wt% the viscosity does not vary over time, but at higher concentrations it increases. The prepared ferrofluids exhibit a thixotropic behaviour that increases over time for nanoparticle concentrations greater than 20 wt%. The thixotropic behaviour is pronounced at 30 and 40 wt% and it is clear that the higher nanoparticle concentration of these ferrofluids leads to more particle-to-particle interactions. Since the nanoparticles were capped and stabilized using OA before the suspensions were made, a steric barrier is expected to be present on the individual nanoparticles. The authors did not anticipate that these ferrofluids would exhibit thixotropic behaviour. To describe such phenomenon it can be presumed that either: (1) some of the nanoparticles have not been covered completely with OA or (2) the nanoparticle aggregates are broken apart by shearing and begin to re-aggregate over time.

Fig. 6 Viscosity of the prepared ferrofluids versus time

The surface charge of $Co₃O₄$ nanoparticles capped by OA chains exhibit van der Waals forces, which is confirmed by the aggregated structures observed in the DLS measurements.

In Fig. 7, the change in ferrofluid viscosity as a function of magnetic field strength is shown. This figure shows the magnetoviscous effect of the ferrofluids at various nanoparticle concentrations. For the dilute ferrofluids $($30 \text{ wt}\%$), there is not an increase$ in viscosity as the magnetic field is applied. At higher particle concentrations (30 and 40 wt%), an appreciable increase in the viscosity can be seen. In the case of 40 wt%, the increase in the viscosity at higher field strengths confirms that the magnetic field induces further aggregation of the nanoparticles (i.e. either

Fig. 7 Effect of an external magnetic field on the viscosity of the ferrofluid at a shear rate of 5 s^{-1}

Fig. 8 Viscosities of the prepared ferrofluids with a magnetic field applied and in the absence of an applied field

chains of aggregates form, there is further aggregation of the already existing nanoparticle aggregates, or both). At this concentration, the viscosity increases 61 % in a field having a strength of 91 kA/m. This value is smaller than the increase of 400 % that was observed for Fe3O4-based ferrofluids (Ghasemi et al. 2008) and the 150 % increase that was found for γ - $Fe₂O₃$ -based ferrofluids (Hosseini et al. 2010). Although $Co₃O₄$ nanoparticles exhibit weak paramagnetism compared to these other materials, the magnetoviscous effect is still seen at higher nanoparticle concentrations. Even when there is a small proportion of aggregated structures in a ferrofluid, a strong magnetoviscous effect is often observed (Odenbach [2002\)](#page-6-0).

The effect of nanoparticle concentration on the viscosity of the prepared ferrofluids in the presence and absence of a magnetic field $(H = 40 \text{ kA/m})$ can be seen in Fig. 8. For nanoparticle concentrations greater than 30 wt%, the viscosity increases whether or not an applied magnetic field is present. For concentrations greater than 20 wt%, the viscosity of the ferrofluid shows a definite increase when the magnetic field is applied. At lower nanoparticle concentrations, the magnetic field does not effectively change the rheology of the system.

Conclusions

Stable OA capped, $Co₃O₄$ nanoparticle-paraffin ferrofluids were prepared using a milling method. The effect of nanoparticle concentration on the rheological properties of the prepared ferrofluids was then investigated. The experimental results show that these ferrofluids are non-Newtonian fluids with a shearthinning behaviour in either the absence or presence of a magnetic field. Both nanoparticle aggregation and concentration affect the rheological behaviour of these ferrofluids. It has been surmised that van der Waals and an externally applied magnetic field affect the aggregation of and interaction between the nanoparticles. A combined thixotropic/magnetoviscous effect was observed for concentrated preparations of the ferrofluid, >30 wt%. At more dilute concentrations, \leq 25 wt%, the rheological properties of the prepared ferrofluids exhibited a thixotropic behaviour with little magnetoviscous effect.

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References

- Arulmurugan R, Vaidyanathan G, Sendhilnathan S, Jeyadevan B (2005) CoZn ferrite nanoparticles for ferrofluid preparation: study on magnetic properties. J Phys B 363:225–231
- Arulmurugan R, Vaidyanathan G, Sendhilnathan S, Jeyadevan B (2006) MnZn ferrite nanoparticles for ferrofluid preparation: study on thermalmagnetic properties. J Magn Magn Mater 298:83–94
- Blanco-Mantecón M, O'Gray K (2006) Interaction and size effects in magnetic nanoparticles. J Magn Magn Mater 296:124–133
- Bolshakova I, Bolshakov M, Zaichenko A, Egorov A (2005) The investigation of the magnetic fluid stability using the devices with magnetic field microsensors. J Magn Magn Mater 289:108–110
- Charles SW (2002) The preparation of magnetic fluids. In: Odenbach S (ed) Ferrofluids: magnetically controllable fluids and their applications. Springer, Berlin, pp 3–18
- Chow TS (1993) Viscosities of concentrated dispersions. Phys Rev E 48:1977–1983
- Didukh P, Greneche JM, Slawska-Waniewska A, Fannin PC, Casas LI (2002) Surface effects in CoFe_2O_4 magnetic fluids studied by Mössbauer spectrometry. J Magn Magn Mater 242–245:613–616
- Einstein A (1906) Berichtigung zu meiner Arbiet ''Eine neue Bestimmung der Moleküldimensionen". Ann Phys 19:289–291
- Ghasemi E, Mirhabibi A, Edrissi M (2008) Synthesis and rheological properties of an iron oxide ferrofluid. J Magn Magn Mater 320:2635–2639
- Hosseini SM, Fazlali A, Ghasemi E, Ahmadi Moghaddam H, Salehi M (2010) Rheological properties of a γ -Fe₂O₃

paraffin-based ferrofluid. J Magn Magn Mater 322(23):3792–3796

- Hunter RJ (2001) Foundations of colloid science. Oxford University Press Inc., New York, pp 190–196
- Ivanov AO, Kantorovich SS (2003) Structure of chain aggregates in ferrocolloids. J Colloid 65(2):189–200
- Mezger TG (2002) The rheology handbook. Vincentz, Hannover
- Morozov MI, Shliomis MI (2002) Magnetic fluid as an assembly of flexible chains. In: Odenbach S (ed) Ferrofluids: magnetically controllable fluids and their applications. Springer, Berlin, pp 162–184
- Odenbach S (2002) Magnetoviscous effects in ferrofluids. Springer-Verlarg, Berlin
- Odenbach S, Raj K (2000) The influence of large particles and agglomerates on the magnetoviscous effect in ferrofluids. J Magnetohydrodyn 36:312–319
- Odenbach S, Störk H (1998) Shear dependence of field-induced contributions to the viscosity of magnetic fluids at low shear rates. J Magn Magn Mater 183:188
- Rosensweig RE (1985) Ferrohydrodynamics. Cambridge University Press, New York
- Scherrer P (1918) Bestimmung der Größe und der inneren Struktur von Kolloidteilchen mittels Röntgenstrahlen. Nachrichten von der Gesellschaft der Wissenschaften zu Göttingen. Math Phys Kl 2:98
- Scherer C, Figueiredo Neto AM (2005) Ferrofluids: properties and applications. Braz J Phys 35(3A):718–727
- Sun S, Zeng H (2002) Size-controlled synthesis of magnetite nanoparticles. J Am Chem Soc 124:8204–8205
- van der Meer J, Bardez I, Bart F, Albouy P-A, Wallez G, Davidson A (2009) Dispersion of $Co₃O₄$ nanoparticles within SBA-15 using alkane solvents. J Microporous Mesoporous Mater. 118:183–188
- Zubarev AY (2002) Statistical physics of non-dilute ferrofluids. In: Odenbach S (ed) Ferrofluids: magnetically controllable fluids and their applications. Springer, Berlin, pp 143–161
- Zubarev AY, Iskakova LY (2003) On the theory of structural transformations in magnetic fluids. Colloid J 65(6): 703–710
- Zubarev AY, Odenbach S, Fleisher J (2002) Rheological properties of dense ferrofluids. Effect of chain-like aggregates. J Magn Magn Mater. 252:241–243