

# A three-stage novel framework for efficient and automatic **glaucoma classifcation from retinal fundus images**

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## **Abstract**

Glaucoma is one of the leading causes of visual impairment worldwide. If diagnosed too late, the disease can irreversibly cause severe damage to the optic nerve, resulting in permanent loss of central vision and blindness. Therefore, early diagnosis of the disease is critical. Recent advancements in machine learning techniques have greatly aided ophthalmologists in timely and efficient diagnosis through the use of automated systems. Training the machine learning models with the most informative features can signifcantly enhance their performance. However, selecting the most informative feature subset is a real challenge because there are  $2<sup>n</sup>$  potential feature subsets for a dataset with n features, and the conventional feature selection techniques are also not very efficient. Thus, extracting relevant features from medical images and selecting the most informative is a challenging task. Additionally, a considerable feld of study has evolved around the discovery and selection of highly infuential features (characteristics) from a large number of features. Through the inclusion of the most informative features, this method has the potential to improve machine learning classifers by enhancing their classifcation performance, reducing training and testing time, and lowering system diagnostic costs by incorporating the most informative features. This work aims in the same direction to propose a unique, novel, and highly efficient feature selection (FS) approach using the Whale Optimization Algorithm (WOA), the Grey Wolf Optimization Algorithm (GWO), and a hybridized version of these two metaheuristics. To the best of our knowledge, the use of these two algorithms and their amalgamated version for FS in human disease prediction, particularly glaucoma prediction, has been rare in the past. The objective is to create a highly infuential subset of characteristics using this approach. The suggested FS strategy seeks to maximize classifcation accuracy while reducing the total number of characteristics used. We evaluated the efficacy of the proposed approach in classifying eye-related glaucoma illnesses. In this study, we aim to assist professionals in identifying glaucoma by utilizing a proposed clinical decision support system that integrates image processing, soft-computing algorithms, and machine learning, and validates it on benchmark fundus images. Initially, we extract 65 features from the 646 retinal fundus images in the ORIGA benchmark dataset, from which a subset of features is created. For two-class classifcation, diferent machine learning classifers receive the elected features. Employing 5-fold and 10-fold stratifed crossvalidation has enhanced the generalized performance of the proposed model. We assess performance using several well-established statistical criteria. The tests show that the

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suggested computer-aided diagnosis (CAD) model has an F1-score of 97.50%, an accuracy score of 96.50%, a precision score of 97%, a sensitivity score of 98.10%, a specifcity score of 93.30%, and an AUC score of 94.2% on the ORIGA dataset. To demonstrate its excellence, we compared the suggested approach's performance with other current state-ofthe-art models. The suggested approach shows promising results in predicting glaucoma, potentially aiding in the early diagnosis and treatment of the disease. Furthermore, realtime applications showcase the proposed approach's suitability, enabling its deployment in areas lacking expert medical practitioners. Overburdened expert ophthalmologists can use this approach as a second opinion, as it requires very little time for processing the retinal fundus images. The proposed model can also aid, after incorporating required modifcations, in making clinical decisions for various diseases like lung infection and, diabetic retinopathy.

**Keywords** Feature selection · Soft-computing algorithms · Image classifcation · Medical data · Glaucoma diagnosis · Machine learning · Hybrid approach

## **1 Introduction**

Over the last ten years, there has been a signifcant increase in interest in biomedical research. The signifcant amount of clinical and healthcare data generated as a result of technological advancements in medical research may help to explain this. Healthcare professionals who use this data to improve patient care are immensely intrigued by its potential. This information essentially promotes improved illness diagnosis and, as a result, better healthcare services. The biomedical data come from many diferent sources, are widely accessible, and include a large spectrum of information. However, it is often impractical to handle vast volumes of data manually. Therefore, people use data mining techniques to enhance existing data analysis methods and extract more profound and valuable insights from the data. Real-world datasets have a variety of traits or properties. It is possible that not all of these characteristics will be necessary to extract useful data from the databases. When certain machine learning or data mining approaches process the data, the presence of non-informative properties in the data does not enhance the learning algorithm's efectiveness. In reality, these characteristics may sometimes make the learning algorithm perform worse while also lengthening the training period. As a result, it is crucial to carefully choose the ideal collection of characteristics for a methodical approach. Through the use of fewer features and lower training costs, this endeavor seeks to improve and maintain the performance of the underlying learning algorithm. Furthermore, the reduced proportions of the features would necessitate a lower quantity of storage space. Feature selection (FS) is one of the data pre-processing methods often used in data mining and machine learning applications [[1\]](#page-56-0). The sizeable amount of high-dimensional data produced by modern technologies has made FS a crucial step in the data pre-processing process. Duplicate, irrelevant, and noisy properties in high-dimensional data can severely impact the accuracy of classifcation. Scholars use it when datasets may contain duplicated and unimportant data. By removing superfuous features, FS reduces dimensionality and improves classifcation accuracy. We can describe it as an optimization issue, aiming to enhance or sustain classifcation performance by selecting the optimal feature collection. Basically, there are three diferent feature selection approaches [\[2](#page-56-1)]: flter model, wrapper model, and embedded model. When there are more features (characteristics), it becomes computationally

expensive to use exhaustive subset search techniques to fnd the right feature subset. This can be attributed to the exponential increase in the number of potential feature subsets. For the dataset with N features, there are a total of  $2<sup>N</sup>$  possible feature subset options. The FS procedure is a challenging combinatorial issue. We must use an FS approach to select the subset that exhibits the best performance. Research has demonstrated that metaheuristic algorithms excel in combinatorial tasks [\[3\]](#page-56-2). In order to quickly locate the almost ideal feature subset, the metaheuristic algorithms have the capacity to investigate  $2^N$  possible feature subsets.

The Branch and Bound method use a monotonic evaluation function and has a low time complexity [\[4\]](#page-56-3). Because it is unable to handle large amounts of data, designing an evaluation function is very difficult. Other methods that may be used in this situation include scatter search and greedy search, according to  $[5, 6]$  $[5, 6]$  $[5, 6]$ . Many of these algorithms face challenges in avoiding local optima and incur signifcant computational burdens [[7\]](#page-56-6). Because of their ability to efficiently find ideal solutions, FS methods based on evolutionary algorithms have gained popularity in recent years. In order to efficiently and reliably provide solutions for optimization issues, evolutionary algorithms make use of biological notions of evolution [\[8](#page-56-7)]. The term "chromosome" refers to each possible result. A chromosome contains a gene, a piece of structural DNA that determines the presence or absence of a certain characteristic. A gene's value may be either 1 or 0, with 1 indicating the existence of a certain feature and 0 indicating its absence. We use the population to compile a complete list of viable solutions. A contender is a popular term for a chosen option. A candidate's chosen ftness value from the population infuences their performance. As the candidate's ftness value rises, so does their performance. Through the use of genetic procedures like crossover and mutation, a small number of candidates increase population diversity [[9](#page-56-8)].

Consequently, researchers have noted the use of evolutionary algorithms in diagnosing various ailments, with the aim of improving patient care through efficient and timely pre-diction. Researchers [\[12\]](#page-56-9) used the augmented shuffled frog leaping algorithm to predict illnesses such as lung cancer and colon tumors, among others. Similar to [[13](#page-56-10), [14](#page-56-11)] covered the particle swarm optimization (PSO) technique for predicting lung cancer. Furthermore, [[10](#page-56-12)] used the gravitational search-based algorithm (GSA) developed in [\[11\]](#page-56-13) to forecast illnesses including breast cancer, heart disease, and dermatological problems. In recent years, the grasshopper optimization algorithm (GOA) [[15](#page-56-14)], has become a very potent optimization tool. This technique replicates the natural foraging behaviour of a group of grasshoppers. The method is successful because it successfully strikes a good balance between exploration and exploitation, thereby limiting trapping in local optima. The experimental results presented in [[15](#page-56-14)] provide additional proof that the GOA can either increase or decrease the average ftness of a population of randomly generated search agents over the course of iterations, depending on whether the goal is to maximize or minimize ftness. The researchers are also employing several widely recognized optimization algorithms, such as PSO [[13](#page-56-10)], Bat Algorithm [[16](#page-56-15)], States of Matter Search [\[17\]](#page-56-16), Cuckoo Search [[18](#page-56-17)], Flower Pollination Algorithm [\[19\]](#page-56-18), Firefly Algorithm [[20](#page-57-0)], GSA [\[10\]](#page-56-12), and Genetic Algorithm [[21](#page-57-1), [22\]](#page-57-2).

Meta-heuristic algorithms that draw their inspiration from nature have become wellknown in recent years as effective answers to difficult real-world issues. These algorithms have shown astounding performance and efficacy. These algorithms may make use of the population's vast knowledge in order to get the best results. These algorithms include the Elephant Herd Optimizer [\[23\]](#page-57-3), Moth Search Algorithm [[24](#page-57-4)], Cuckoo Search Algorithm [[25](#page-57-5)], Monarch Butterfly Optimisation [[26](#page-57-6), [27\]](#page-57-7), Elephant Herding optimization algorithm [[28](#page-57-8)], Krill Herd [[29](#page-57-9)] and Teaching learning-based algorithm [\[30\]](#page-57-10). Numerous optimisation issues, including complex design issues, node localization in wireless sensor networks,

fault diagnosis, economic load dispatch, high-performance computing, high-dimension optimisation problems, image matching, and the knapsack problem, are commonly solved using these algorithms  $[31–39]$  $[31–39]$  $[31–39]$ . Various methods have been shown to be dependable and efficient in resolving various problems. Additionally, a number of academics have tried to use stochastic approaches to address feature selection problems. These techniques include genetic algorithms [[21](#page-57-1)], simulated annealing [[40](#page-57-13)], tabu search [[41](#page-57-14)], bacterial foraging optimization algorithm  $[42]$  $[42]$  $[42]$ , and artificial bee colonies  $[43]$  $[43]$  $[43]$ . Researchers  $[44, 45]$  $[44, 45]$  $[44, 45]$  $[44, 45]$  $[44, 45]$  have used a record-to-record trip approach based on fuzzy logic to address rough set attribute reduction issues. According to [\[46\]](#page-57-19), the method entails thinking of attributes as graph nodes in order to build a graph model. To solve the feature selection issue, one can implement ant colony optimization approach to choose the nodes [\[47\]](#page-57-20). Proposed an FS method based on artifcial bee colonies and diferential evolution. Authors verifed the method using ffteen data-sets from the UCI collection. Previous research [\[48,](#page-57-21) [49\]](#page-58-0) has used the Ant Lion Optimizer (ALO) as a feature selection model. The Flower Pollination Algorithm (FPA) [\[51\]](#page-58-1), the Dragonfy Algorithm [\[52\]](#page-58-2), and the Grey Wolf Optimizer (GWO) are modern algorithms that have efectively solved FS issues. Researchers have used a salp swarm algorithm (SSA) based on chaos to improve feature selection [\[50,](#page-58-3) [53\]](#page-58-4). The authors also employed a competent crossover strategy [[55](#page-58-5)] to enhance the SSA's ability to handle the FS difficulty. In order to find optimality, the authors' work [\[51\]](#page-58-1) presented a hybrid GWO-ALO algorithm that combines the global search powers of GWO with the exploitation capabilities of ALO. Recent research [[54](#page-58-6)] employed the whale optimization approach (WOA) as a feature selection technique. Scholars have also combined the approaches of simulated annealing (SA) and WOA [[52](#page-58-2)] to investigate feature subsets and choose the best feature set. The fndings of this work contribute to the body of evidence showing that, when tested on benchmark image datasets, GWO, WOA, and their hybrid algorithms provide competitive results. These algorithms are good at locating key characteristics. These factors have led to the use of these three techniques in the feld of feature selection for the classifcation of glaucoma, globally spreading an eye-related disease.

Glaucoma (Fig. [1\)](#page-3-0) is a medical disorder that has the potential to harm the eye's optic nerve. Over time, the issue gets worse. Experts believe a large buildup of pressure inside the eye is the main cause of the incident. The elevated intraocular pressure has harmed the optic nerve. The brain receives visual information from the optic nerve. Glaucoma's increasing pressure over time can cause considerable damage that can lead to vision loss, including permanent impairment and the potential development of total blindness. Regaining lost vision might be difficult. Lowering intraocular pressure has the potential to help



<span id="page-3-0"></span>**Fig. 1** Figure depicting normal eye and glaucomatous eye

restore vision. In modern times, people in their 40s and older frequently sufer from this condition, but those aged 55 and above are the most commonly afected. Because glaucoma can take many different forms, it can be difficult to track how the disease is changing and could even advance undetected.

The eye contains the fuid known as aqueous humor. It normally comes out of a meshlike duct in a typical person. The blockage in the duct causes the eye to continuously produce fuid, which accumulates over time. The medical community is still researching the cause of the channel obstruction, making it a hereditary problem. Inappropriate use of the drainage angle. The accumulation of fuid causes the pressure inside the eye to rise. We refer to the pressure within the eye as intraocular pressure (IOP) damage to the optic nerve. Millions of incredibly tiny nerve fbers make up the optic nerve. In many aspects, it is similar to various electric cables made up of countless tiny wires. Any human will become more prone to developing blind spots that impair vision when these nerve fbers start to deteriorate over time. These blind zones are rarely noticeable unless a person has lost a signifcant amount of their visual nerve fbers. Simple causes of glaucoma include a minor wound, an infection, or any other type of damage that causes obstruction of blood vessels in an average person's eye. Although it is extremely rare, there are situations when eye surgery may be used to treat another issue.

Glaucoma, the second most common cause of blindness worldwide (after cataract), is a common chronic disorder that poses a serious risk to ocular health [\[56\]](#page-58-7). The World Health Organization (WHO) estimates that glaucoma affects 65 million people globally [[57](#page-58-8)]. People sometimes refer to glaucoma as the "silent theft of sight" [\[58\]](#page-58-9) due to its irreversible nature and the absence of symptoms in its early stages. Even though there is no known cure for glaucoma at this time, early detection and the right care may greatly help patients avoid visual loss and lower their risk of becoming blind. Clinical settings commonly use the measurement of intraocular pressure (IOP) to detect glaucoma. IOP is a well-known glaucoma symptom. This disorder has the potential to have negative consequences such as optic nerve injury, abnormalities in the visual feld, and eventually blindness [\[59\]](#page-58-10). Therefore, glaucoma evaluation considers IOP as a crucial signal. The IOP of certain people with glaucoma, however, may decrease within the normal range, making this technique inefective [\[60\]](#page-58-11). As a result, relying solely on IOP measurement may result in missed detection of these specifc situations. Conducting optic nerve head (ONH) tests, which require clinical ophthalmologists to evaluate glaucoma using retinal pictures, is another frequently used technique for glaucoma screening [[61](#page-58-12)]. Ophthalmologists routinely manually improve the retinal picture throughout the glaucoma screening procedure and make diagnoses based on their experience and domain-specifc knowledge. The inefectiveness and length of the diagnostic procedure render the two approaches listed above unsuitable for population screening. As a result, the development of an automated glaucoma screening system is both very advantageous and necessary for a broad and early diagnosis of the problem. However, the development of digital retinal image processing and artifcial intelligence has made it feasible to perform automated glaucoma screening. Large-scale screening can benefit from this method due to its reliable accuracy and efficiency. Pathological signs of glaucoma often include an expanded optic cup and degradation of the retinal nerve margin [[62](#page-58-13), [63](#page-58-14)]. The ONH is the primary cause of these abnormal symptoms. As a result, the ONH evaluation is an important method for glaucoma screening. Clinical measurement analysis and image-based feature analysis are the two main groups of automated glaucoma diagnostic techniques that use fundus pictures. The term "clinical measurement analysis" refers to the evaluation of certain geometric features related to glaucoma, such as the ratio of the optic cup to disc (CDR) [[64](#page-58-15)], the diameter of the optic disc [\[65\]](#page-58-16), and the area of the optic cup. The most important of these traits, as recognized by clinical ophthalmologists, is the CDR, which shows a substantial link with glaucoma screening. An observer may quickly recognize the optic disc (OD) in a color retinal picture because of its distinctive appearance as a bright yellow oval area. It may be challenging to see the optic cup (OC), located in the middle of the OD and distinguished by its brilliant oval or circular shape. The remaining peripheral portion of the optic disc is referred to as the neuroretinal rim, with the exception of the optic cup area. A bigger CDR indicates a higher possibility of developing glaucoma, and conversely, a smaller CDR predicts a lower probability, as shown in Fig. [1.](#page-3-0) This observation is based on clinical experience and domain knowledge. Researchers have developed numerous automated glaucoma diagnosis techniques, many of which rely on clinical traits such as the CDR. A few recent state-of-the-art research and the most current methods that academics have developed for glaucoma prediction are shown in Table [1](#page-6-0) below.

Examining fundus images requires the time-consuming and computationally complex processing of large amounts of data. Expert ophthalmologists analyze the subject's fundus images to confrm the disease. The observation takes time and is subject to error due to its intra-observability. Moreover, there is always a scarcity of expert medical practitioners. Hence, an artifcial intelligence-based computer-aided diagnosis (CAD) system is today's need. To achieve better results from CAD systems, efective approaches necessitate feature collection, selection, and organization as critical components of comprehensive data analysis. Glaucoma is a complex illness, and various features have to be analyzed from the patient's retinal fundus image, which makes the confrmation of this disease and distinguishing between healthy and glaucomatous eyes a very challenging task. The hybrid approach improves the accuracy and usefulness of fnding glaucoma in fundus pictures by combining Grey Wolf Optimization (GWO) and the Whale Optimization Algorithm (WOA). This makes it possible to create reliable and highly efficient CAD system.

If this chronic illness is not found in its early stages, it might cause permanent blindness. There are several manual scanning techniques, but they are costly, time-consuming, and require the assistance of specialists in these felds. It's critical to use image processing, feature selection, and machine learning-based classifcation models to identify the illness sooner in order to prevent such detrimental efects. All of these procedures have been used in this work to classify images from the ORIGA benchmark dataset. Three nature-inspired metaheuristic algorithms—GWO, WOA, and integration of these two—are used in the fundamental process of selecting the most important features (the hybrid model presented from our side is the original scientifc contribution). The empirical study presented the research that identifes the optimal and most efective features required for the diagnosis of a prevalent eye disease glaucoma. The study concludes by demonstrating exceptional performance and outcomes.

Using the most recent artifcial intelligence techniques, researchers have attempted to develop a very effective diagnosis system for eye-related disorders [\[104](#page-60-0)[–107](#page-60-1)]. This recent article presents the Fundus-DeepNet system [[104](#page-60-0)] where the proposed approach uses deep learning to classify many eye illnesses by merging feature representations from two fundus images. The intricate dataset Ophthalmic Image Analysis-Ocular Disease Intelligent Recognition (OIA-ODIR), which includes numerous fundus images displaying eight diferent eye illnesses, has undergone extensive testing. Ophthalmologists and other eye experts can diagnose and determine the appropriate course of treatment for a range of retinal disorders by using the author's suggested approach for segmenting and extracting clinically meaningful information from the retinal blood vessels  $[105]$ . Next study rigorously evaluates and categorizes approaches for identifying veins and arteries in fundus images as either automatic or semi-automatic [[106\]](#page-60-3). In the subsequent study rigorously evaluates and

<span id="page-6-0"></span>





categorizes approaches for identifying veins and arteries in fundus images as either auto-matic or semi-automatic [[107\]](#page-60-1).

#### **1.1 Motivation and the novelty in the work**

This study introduces a novel hybrid FS algorithm, termed GWOWOA, which combines the Grey Wolf Optimization Algorithm (GWO) with the Whale Optimization Algorithm (WOA). The study comprehensively investigates three FS algorithms—GWO, WOA, and GWOWOA—for glaucoma classifcation tasks using fundus retinal images belonging to the ORIGA benchmark dataset. Multiple experiments were conducted on this well-established glaucoma dataset. The objective is to enhance glaucoma classifcation accuracy, robustness, and scalability using a fundus image dataset. Initially, 65 features belonging to fve vital categories were extracted using self-created, handcrafted coding scripts. Additionally, the study evaluates six classifers: support vector machine, random forest, logistic regression, XGBoost, catboost, and ensemble of all fve. Evaluation metrics include accuracy, precision, sensitivity, specifcity, F1-score, Kappa score, MCC, and ROC analysis. Our approach is compared against recent FS brave-new-ideas based approaches, showing improvements in feature selection process, classifcation accuracy, and other performance measuring parameters. Our suggested approach offers an exploration-exploitation balance that enhances the algorithms' ability to identify relevant features while optimizing computational efficiency. By leveraging optimization capabilities alongside feature importance estimation, the hybrid approach can yield robust and generalizable FS results. The objective of combining the algorithms for FS in glaucoma classifcation using a fundus image dataset is to identify the most relevant features associated with this disease. These algorithms aim to improve the accuracy of glaucoma classifcation by selecting a subset of informative features while reducing dimensionality and removing irrelevant or redundant genes from the dataset. The goal is to enhance the performance of ML classifers by focusing on the most discriminative features for accurate glaucoma diagnosis and prognosis. The novelty of this paper stems from the introduction of a three-phase hybrid classifcation model, combining feature extraction, feature selection, and fnally two-class classifcation using machine learning classifers that are trained on these selected features. This hybrid approach ofers a unique solution to the challenge of FS in glaucoma classifcation using a fundus image dataset. This novel algorithm addresses the limitations of existing methods and aims to improve the accuracy and efficiency of glaucoma classification models. The GWOWOA algorithm introduces a novel approach for determining feature importance in glaucoma classifcation. Its utilization marks a departure from traditional methods and promises improved performance in identifying relevant features from the ORIGA dataset. These three algorithms, while not previously employed in the realm of glaucoma detection using fundus image datasets, present a promising avenue for optimizing FS. Its novel approach to optimization offers potential improvements in the efficiency and accuracy of FS processes. Additionally, the incorporation of these algorithms underscores the importance of exploring innovative techniques to enhance cancer classifcation models and advance research in the feld. We have implemented 5-fold and 10-fold cross-validation approaches in this work. Convergence curves and the efect of population size are some of the characteristics of the in-depth analysis performed in this work, which are rarely observed in recent state-of-the-art articles. The novelty of this research stems from several key contributions aimed at advancing glaucoma classifcation from the fundus image dataset. The results generated from our approach are highly auspicious; our proposed clinical decision support system requires less human intervention, has a robust nature, high reliability, and is fast-responding in nature.

In a nutshell, highlighting points of this work are as follows:

- After conducting a thorough analysis of the current literature, it is evident that there is vast potential for improving features and features count in the feld of glaucoma detection. This study presents a new feature selection technique called the hybrid GWOWOA, which combines the strengths of the GWO and the WOA. This technique has the ability to remove irrelevant features from the feature space, thereby improving classifcation accuracy and reducing computing costs. This proposed algorithm represents a signifcant innovation and scientifc contribution from the author. With our current understanding, we are pioneering the use of these algorithms to detect glaucoma, efectively addressing a major research gap in the feld.
- This work presents a novelty by applying three feature selection algorithms to select the most infuential features, along with highly in-depth experimentation and analysis. We have conducted a comprehensive set of experiments using the ORIGA benchmark dataset, covering various tests. In addition, this research provides a comprehensive analysis of various characteristics to demonstrate the efectiveness of the proposed methodology. By including the analysis of confusion measures and ROC curves, we have thoroughly evaluated the performance of six machine learning classifers. The current assessment involved calculating eight metrics used to measure efficiency. These metrics are important for assessing the efectiveness of the classifers' performance. This study highlights the importance of timing in the development of a soft-computing approach and the training and testing of a machine learning model, as demonstrated by the execution of a 5- and 10-fold cross-validation method.
- In this work thorough experimentation and analysis accompany the selection process, showcasing a highly professional approach. This study aims to showcase the researchers the most informative features required for the screening of this disease along with a highly reliable and efective clinical decision support system for professionals specializing in ophthalmology. Furthermore, our main objective is to offer a software-driven solution that can assist in addressing the decrease in human visual acuity by enabling quick, efective, and accurate identifcation of ocular infections. The tool demonstrates a high level of professionalism by allowing for customization to connect with mobile and wearable medical devices. This makes it suitable for use in environments where there may be a shortage of skilled medical professionals.

The rest of the paper is organized as follows: Section 2 is dedicated to proposed approach mentioning dataset, methodology along with the algorithms applied; Section 3 depicts the computed results in tabular format and graphical format in detailed fashion along with discussion on the results and the comparison of the suggested approach with recent state-of-the-art published studies. Finally, section 4 concludes the work.

#### <span id="page-11-0"></span>**Table 2** Description of Dataset



#### <span id="page-11-1"></span>**Table 3** Description of features extracted from dataset images



## **2 Proposed approach**

### **2.1 Dataset and the details about features extracted**

The dataset used in this empirical study is ORIGA\_ALL\_FEATURES dataset. The Table [2](#page-11-0) given below provides the information about the dataset.

The dataset created by extracting 65 features (Table [2\)](#page-11-0) from ORIGA images [[103](#page-60-4)] contains 646 instances i.e., 646 rows of data. The dataset contains 66 columns, out of which the 65 columns are features and the last column is the classifcation column. The last column is the column with heading (glaucoma) which contains discrete data. The data is either 0 or 1. Here, 0 represents the person does not have glaucoma while 1 represents that the person has glaucoma. In 646 instances of data, we have 166 instances containing 1 s while the other 480 instances contain 0 s. Table  $3$  present the list and Table [4](#page-12-0) depicts short description about extracted features.



<span id="page-12-0"></span>**Table 4** List and short definition of the extracted features **Table 4** List and short defnition of the extracted features



#### **2.1.1 Structural features (cup diameter, disk diameter, cup to disk ratio, RIM, DDLS)**

Prior to determining the cup-to-disc ratio, it is necessary to segment the optic disc and optic cup. In this procedure, the area of interest (ROI) is extracted from the input fundus image. The ROI is further subdivided into Red, Green, and Blue channels. The Red component is suitable for optic disc segmentation because to the abundance of information for disc area in the red channel, whereas the Green component is appropriate for optic cup segmentation due to the presence of the appropriate optic cup region in the green channel. Thus, the entire procedure is described with the assistance of Fig. [2](#page-14-0), which itself is self-explanatory.

## **2.1.2 GLCM features**

The gray-level co-occurrence matrix (GLCM), also known as the gray-level spatial dependency matrix, is a mathematical process of analyzing texture that recognizes the spatial association of pixels. The GLCM functions describe an image's texture by measuring how frequently pairs of pixels with unique values and in a given spatial relationship appear in an image, generating a GLCM, and extracting statistical measures from this matrix. The size of matrix  $M_k \times M_k$ , which describes the second-order joint likelihood of a mask-bound image feld defned a.

 $(x(l, n), \lambda, \theta)$ . The  $(l, n)$  th element of matrix represents number of times the combined levels *l* and *m* occurs in two pixels within the image separated by distance *λ* along angle  $\theta$ . Now, let *I* be a small positive num  $x(l, n)$  is the co-occurrence matrix for  $\lambda = 1$  and angle  $\theta$ .  $x_p(l) = \sum_{n=1}^{M_k} x(l, n)$  is marginal row probability.  $x_q(n) = \sum_{n=1}^{M_k} x(l, n)$  is marginal row probability.  $\eta_p$  is the grey level intensity of  $x_p$ .  $\eta_q$  is the grey level intensity of  $x_q$ .  $\sigma_p$  and  $\sigma_q$  are the standard deviation of  $x_p$  and  $x_q$ . For each degree, the GLCM final value is



<span id="page-14-0"></span>**Fig. 2** Sample for extraction optic cup and optic disc from Retinal fundus image



<span id="page-15-0"></span>**Table 5** Shortlisted and extracted GLCM features

calculated, and the mean of these values is returned. Horizontally the values of *θ* are 0∘ ,the diagonally it represent 45<sup>∘</sup> and 90<sup>∘</sup> in vertical direction. Finally, the resulting matrix is calculated with the functionality described below. Table [5](#page-15-0) presents the shortlisted GLCM features.

#### **2.1.3 Gray level run length matrix (GLRM)**

The GLRM is a matrix that provides details regarding textural features for analyzing an object's texture. It's known as a line of pixels in a specifc direction with the same intensity values. The sum of such pixels is referred to as the grey level run length, and the number of times it occurs is referred to as the run length value. In GLRM, *x*(*l*,*n*| *θ*) the (*l*,*n*)*th* element defines the number of runs with gray level *l* and *n* in the image along  $\theta$ . Now let  $M_k$ be the discrete value of intensity in the image.  $M<sub>r</sub>$  be the discrete run lengths in the image.  $M_p$  be the voxels number in the image.  $M_r(\theta)$  is the number of runs along angle  $\theta$ . Table [6](#page-16-0) presents the shortlisted GLRM features.

#### **2.1.4 First order statistical (FoS) features**

FoS features can often used to evaluate an image's texture by the computation of an image histogram showing the likelihood of a pixel appearing in an image. These characteristics rely only on individual pixel values and not on the relationship with the pixels nearby. The first order histogram estimate is given by  $p(c) = \frac{N(c)}{K}$ . Here c represents the grey level in the image, *K* is the total number of pixels in the neighbourhood window centered around the expected pixel and *N*(*c*) is the number of pixels of gray value c in the window  $0 \le c \le M - 1$ .

The FoS characteristics are widely used as described below: mean, standard variation, variance, curtosis, skewness and entropy. Table [7](#page-17-0) presents the shortlisted FoS features.

#### **2.1.5 Discrete wavelet transforms (DWT) features**

The transformation of wavelets is the division of data, operators or functions into diferent frequency components and the analysis of each with a resolution corresponding to a scale. Here, Wavelet transforms the picture into four distinct elements, i.e. approximation, horizontal, diagonal and vertical. Approximation variable is used for scaling and three for localization. For images, separate wavelet Transform with One-Dimension flter bank is added to rows and columns of each channel. Here for p rows and q columns, we have suppose the scaling function  $I_{m, p, q}(r, s)$  and for translation function  $\mathcal{Q}^l_{m, p, q}(r, s)$  in Equation () and (). The Horizontal

<span id="page-16-0"></span>

<span id="page-17-0"></span>

high-pass channels, vertical high-pass channels and diagonals high pass channels are  $\zeta^H(r,s)$ ,  $\zeta^V(r,s)$ ,  $\zeta^D(r,s)$ . All these important channels are extracted from  $I_{m,n,q}(r,s)$  scaling function.

$$
\mathfrak{S}_{m,p,q}(r,s) = 2^{m/2} \mathfrak{S}(2^m r - p, 2^m s - q) \tag{1}
$$

$$
\mathcal{C}_{m,p,q}^l(r,s) = 2^{m/2} \mathcal{C}(2^m r - p, 2^m s - q)l = \{H, V, D\}
$$
 (2)

Here the three main components of wavelets are diagonal (D), horizontal (H) and vertical (V).

For the image  $f(r, s)$  of the size p,q, The discrete wavelet transform is as follows:

$$
W_{\mathfrak{F}}(j_0, p, q) = \frac{1}{\sqrt{pq}} \sum_{r=0}^{p-1} \sum_{s=0}^{q-1} f(r, s) \mathfrak{F}_{j_0, p, q}(r, s)
$$
(3)

$$
W_{\mathfrak{F}}(j_0, p, q) = \frac{1}{\sqrt{pq}} \sum_{r=0}^{p-1} \sum_{s=0}^{q-1} f(r, s) \mathcal{G}_{m, p, q}^l(r, s), l = \{H, V, D\}
$$
(4)

 $j_0$  is an arbitrary starting scale and  $W_1(j_0, p, q)$  coefficient define an approximation of  $f(r, s)$ at scale  $j_0$ . The  $W^l_{\wp}(m, p, q)$  coefficients add horizontal, vertical and diagonal details for scales  $m \ge j_0$ . We normally let  $j_0 = 0$  and select  $p=q=2^m$  so that  $m = 0, 1, 2, \ldots$ .m-1.

Below is a short mathematical representation of the traits that were retrieved.

1. **CDR (Cup Disc Ratio) –**The eye is considered normal. The formula to calculate CDR is: *Dia*\_*of* \_*Cup*

$$
Cup\_Disc\_Ratio = \frac{Dia\_of\_Disc}{Dia\_of\_Disc}
$$
 (5)

2. **GLCM (Grey Level Co-occurrence Matrix) –**Grey level Co-occurrence Matrix *S*(*o*,*t*): *Dia*\_*of* \_*Disc*

$$
S_m(o) = \sum_{t=1}^{P_k} S(o, t)
$$
 (6)

$$
S_n(o) = \sum_{t=1}^{P_k} S(o, t)
$$
 (7)

$$
S_{m+n}(k) = \sum_{o=1}^{P_k} \sum_{t=1}^{P_k} S(o, t)
$$
 (8)

$$
A_{mn1} = -\sum_{o} \sum_{t} S(o, t) \log \left\{ S_m(o) S_n(t) \right\} \tag{9}
$$

$$
A_{mn2} = -\sum_{o} \sum_{t} S(o, t) \log \left\{ S_m(o) S_n(t) \log \left\{ S_m(o) S_n(t) \right\} \right\}
$$
(10)

$$
SRE = \frac{\sum_{l=1}^{s_g} \sum_{m=1}^{p_r} \frac{p(l,m|\theta)}{m^2}}{p_r(\theta)}
$$
(11)

Here  $p(l,m)$ ,  $(l,m)^{th}$  element define the number of run with grey level *l* and length *m* in the image.

**LRE (Long Run Emphasis)** 
$$
- LRE = \frac{\sum_{l=1}^{s_g} \sum_{m=1}^{p_r} p(l, m | \theta) . m^2}{p_r(\theta)}
$$
(12)

## 4. **GLU (Grey Level Uniformity) –**

$$
g(i,j) = 255 - \frac{g(i,j) - g_{\min}}{g_{\max} - g_{\min}}
$$
(13)

- 5. where  $g_{\text{max}}$  and  $g_{\text{min}}$  correspond to the maximum and minimum gray levels respectively and the whole range of gray levels is 255–0.
- 6. **DDLS (Disc Damage Likelihood Scale)-**

$$
Disc\_dam\_Like\_Scale = \frac{Rim\_of\_Width}{Diameter\_of\_Disc}
$$
 (14)

7. **Bicoherence-**

$$
c(w_1, w_2) = \frac{E_M \left[M(w_1)M(w_2)M^*(w_1 + w_2)\right]}{\sqrt{E_M \left[\left|M(w_1)M(w_2)\right|^2\right]M_X \left[\left|X(w_1 + w_2)\right|^2\right]}} = \left|X(w_1, w_2)\right| e^{j\phi(X(w_1, w_2))}
$$
\n(15)

 $|X(w_1, w_2)|$  is a magnitude feature and  $e^{j\phi(X(w_1, w_2))}$  is a phase feature.

8. **Energy** $energy = \sum_{i=1}^{N_k} \sum_{j=1}^{N_k} p(i,j)^2$  (16) ∑*Nk*  $p(i,j)^2$ 

*j*=1

9. **Homogenity–**

hom 
$$
op = \sum_{i=1}^{N_k} \sum_{j=1}^{N_k} \frac{p(i,j)}{1+|i-j|^2}
$$
 (17)

10. **Correlation-**

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$$
correlation = \sum_{i=0}^{M-1} \sum_{j=0}^{M-1} \frac{\{i \times j\} \times p(i,j) - \{\mu_x \times \mu_y\}}{\sigma_x \times \sigma_y}
$$
(18)

#### 11. **Contrast-**

$$
contr = \sum_{i=1}^{N_g} \sum_{j=1}^{N_g} (i,j)^2 p(i,j)
$$
 (19)

12. **Dissimilarity (dissi)**-

$$
dissi = \sum_{i=1}^{N_g} \sum_{j=1}^{N_g} |i - j| p(i, j)
$$
 (20)

13. **Entropy-**

$$
ENTROPY = -\sum_{i=0}^{G-1} \sum_{j=0}^{G-1} P(i,j) \times \log(P(i,j))
$$
\n(21)

#### **2.2 Methodology implemented in this work**

Using the ORIGA\_ALL\_FEATURES dataset, the suggested approach here assists in determining if an individual has glaucoma or is healthy. This dataset includes information from 646 cases that was retrieved from snapshots in both the glaucomatous and normal conditions. There are 65 characteristics in the provided ORIGA dataset. The presented dataset has to be normalized since it contains several characteristics with diferent values. Some characteristics have values that are less than 0 while others have values that are larger than 50 k. The dataset must be normalized as a result. A sklearn pre-processing module called Standard Scaler was used to normalize the dataset. Normalization is a criterion that machine learning estimators must often meet. The estimators could perform poorly if the data are not normalized. After normalizing the dataset, we provide the specifed optimizer list the dataset's dimensions, population size, and number of iterations. Then, after carrying out their tasks, these optimizers provide us the ftness value at each iteration along with a list of features they've chosen from among all the features in the dataset. Following the return of a list of chosen features, machine learning analysis is conducted utilizing a variety of machine learning estimators on the supplied list of chosen features from the dataset. These numerous estimators pick up on new dataset characteristics, making predictions that are then measured by a variety of performance criteria. The outcomes are documented for further analysis.

#### **2.2.1 Objective function**

The objective Function used for the Grey Wolf Optimizer is Rastrigin Function.

Mathematical implementation of Rastrigin Function-:

$$
f(x) = \sum_{i=1}^{n} \left[ x i^2 - 10 \cos(2\pi x i) + 10 \right]
$$
 (22)

The Rastrigin function is mainly used as a performance test problem for optimization algorithms. It is basically a non-linear multimodal function was frst proposed in 1974. The Rastrigin function has many local minima it is because the optimization algorithms have to be run from multiple starting points Rastrigin function has only one global minimum, and all other local minimums have value greater than global minimum.

#### **2.3 Recent advances in optimization**

In this research [[93](#page-59-12)], a binary version of the Coyote Optimisation Algorithm (COA) called Binary COA (BCOA) was suggested. It was used to choose the best feature subset for classifcation by utilising a wrapper model's hyperbolic transfer function. In this manner, a classifcation algorithm's performance evaluation was used to determine which features to include. Lévy Arithmetic Algorithm is an improved metaheuristic optimisation method that uses the Lévy random step [\[94\]](#page-59-13). Arithmetic operators solve many optimisation problems in Arithmetic Optimisation Algorithm. Its linear search capabilities may prevent ideal solutions, causing stagnation. This paper introduces the Lévy Arithmetic Algorithm by merging the Arithmetic Optimisation Algorithm and the Lévy random step to improve search capabilities and reduce processing demands. Ten CEC2019 benchmark functions, four real-world engineering issues, and microgrids with renewable energy integration Economic Load Dispatch were evaluated. Next study introduces an optimisation method for plate-fn heat exchangers (PFHEs) that aims to minimise the entropy generating units. The method used is Adaptive Diferential Evolution with Optional External Archive (JADE) and a modifed version called Tsallis JADE (TJADE) [[95](#page-59-14)]. Plate-fn heat exchangers possess significant attributes, including elevated thermal conductivity and efficiency, as well as a substantial heat transfer surface area relative to their volume. These characteristics result in reduced space and energy requirements, weight, and cost. Additionally, the design of plate-fn heat exchangers can consider various geometric and operational parameters.

GPOA, which integrates GOA and POA, is used to segment lesions and train U-Net to identify diferent types of lesions [\[96\]](#page-59-15). The image and vector-based features of fundus images are extracted after fipping, rotation, shearing, cropping, and translating fundus images. Exponential Gannet Pelican Optimisation Algorithm-trained Deep Q Network (DQN) detects diabetic retinopathy. Equivalently Weighted Moving Average (EWMA), Gannet Optimisation Algorithm (GOA), and Firefy Optimisation Algorithm (FFA) form the EGFOA. This study presents a new and enhanced frefy algorithm (IFA) that utilises a Gaussian distribution function for the optimal chiller loading design [\[97\]](#page-59-16). The study demonstrates the efectiveness of the proposed method by conducting two case studies. These studies compare the results of the developed model using IFA with those of traditional frefy algorithm and other optimisation methods found in literature. The study focuses on the optimisation problem of minimising energy consumption in multi-chiller systems. The objective function is to reduce energy consumption, and the optimum parameter to achieve this is the partial loading ratio of each chiller. Chiller loading optimisation strategies have been presented recently [[98](#page-59-17)]. In general, the optimisation problem minimises chiller energy use while meeting cooling demand. Continuous parameters optimisation problems can be solved efficiently with the CSA (cuckoo search algorithm). CSA relies on cuckoo species' obligate brood-parasitic behaviour and birds' and fruit fies' Lévy fying. Its early studies suggest it could outperform existing algorithms. This research presents a diferential operator (DCSA) CSA technique for optimal chiller loading design [[98](#page-59-17)]. Next study proposes a modifed grasshopper optimisation technique for non-linear wireless channel equalisa-tion [[99](#page-59-18)]. Although grasshopper optimisation algorithm (GOA) is efficient, it gets caught in local optima after some iterations due to swarm diversity loss. GOA includes no provision to maintain elite grasshoppers detected at each index, which weakens its exploitation and convergence rate. This research modifes GOA in three ways to overcome its limitations. Inefficient search regions are detected by a threshold setting. Lévy Flight is combined with the basic GOA to increase grasshopper swarm diversity, and the greedy selection operator preserves exceptional grasshoppers at every index. The modifed grasshopper optimisation algorithm (MGOA) outperforms metaheuristic methods. This study introduces a cheetahbased optimisation algorithm (CBA) that incorporates the social behaviour of these ani-mals [[100](#page-59-19)]. The proposed CBA is tested against seven well-known optimizers using three diverse benchmark problems. Lastly, the study provides insights into research issues and directions in the CBA design. In  $[101]$  scholars proposed a beta distribution and natural gradient local search-based modifed social spider optimisation (SSO) (MSSO) to improve SSO performance. The MSSO's performance is tested using Loney's solenoid benchmark and a brushless direct current motor benchmark to compare the SSO with the proposed MSSO. In the next study, authors presented a meerkat optimisation algorithm (MOA) by mimicking their natural behaviour  $[102]$  $[102]$ . Meerkat survival techniques, whose sentinel system allows them to switch behaviour patterns, inspired MOA. Some mathematical aspects of meerkat optimisation algorithm were proven, and classical optimisation test functions verify MOA's advantages. MOA solves real-world engineering issues with constraints, proving its efficacy and excellence.

#### **2.4 Rationale behind selecting GWO and WOA**

The Grey Wolf Optimization (GWO) algorithm is an optimization algorithm that draws inspiration from the social behaviour of grey wolves. It is a population-based approach that aims to fnd optimal solutions. A wide range of optimization problems, including feature selection in machine learning tasks, have utilized it. Researchers widely regard this method as the preferred choice for selecting features from a large set of retinal fundus images for glaucoma diagnosis. Its key properties include exploration and exploitation, efficiency, a population-based approach, adaptability, robustness to noise, and parallelizability. In summary, the GWO algorithm shows great potential for selecting features from retinal fundus images for glaucoma diagnosis. Its ability to balance exploration and exploitation, along with its efficiency, adaptability, robustness, and parallelizability, make it a highly professional choice. These dynamic characteristics (Leader-Follower Hierarchy, Exploration and Exploitation, Dynamic Search Intensity, Encouragement of variation and Local and Global Search) of the GWO allow for efective feature selection from a sizable set of original features in the context of diagnosing human diseases. In order to efficiently uncover pertinent features for illness detection while managing the complexity of high-dimensional feature spaces, GWO combines local and global search algorithms, encourages diversity, and strikes a balance between exploration and exploitation.

The Whale Optimization Algorithm (WOA) is an optimization algorithm that draws inspiration from the social behaviour of humpback whales. It has been utilized for a wide range of optimization problems, including feature selection. Practitioners widely recognize this method as the best option for selecting features from a large set of retinal fundus images, which is crucial for diagnosing human diseases like glaucoma. Its notable features include thorough exploration and exploitation, a population-based approach, a dynamic search strategy, high efficiency, and the ability to perform both global and local searches. In general, the WOA shows great potential for feature selection from a large feature set extracted from retinal fundus images for human disease, such as glaucoma diagnosis. Its exploration-exploitation balance, population-based approach, dynamic search strategy, efficiency, global and local search capabilities, and robustness to noise all contribute to its promise. The WOA's various dynamic properties, such as its ability to balance exploration and exploitation, update encircling prey dynamically, establish a leader-follower hierarchy, adapt the search space dynamically, and maintain diversity, all contribute to its efectiveness in selecting features for human disease diagnosis from large sets of original features. WOA possesses several characteristics that allow it to efficiently traverse the complex feature space, detect significant features, and enable precise diagnosis of human diseases.

#### **2.5 GWO‑WOA hybrid**

The hybrid algorithm comprising the two implemented soft-computing algorithms (GWO and WOA) is proposed with an intention that the properties of these two algorithms may enhance the performance, then the individual case, overall, in a joint venture by collaborating each other [[81](#page-59-21), [82,](#page-59-22) [83](#page-59-23), [84](#page-59-24)]. GWO-WOA is predicted to increase the WOA Algorithm's performance. The given method applies the GWO leadership ranking to the WOA's bubble net attacking strategy. The proposed algorithm selects three best candidate solutions from the entire search agents, the first level alpha $(\alpha)$ , the second and third levels in the group beta $(\beta)$ and delta $(\delta)$ , and the other search agents will adjust their positions in accordance with the positions of the best search agents to improve the performance of the WOA algorithm. Overall, for the purpose of screening human diseases, the hybrid algorithm that combines WOA and GWO's dynamic qualities allow for efective feature selection from sizable original feature sets. The hybrid algorithm dynamically adjusts search intensity, incorporates efficient convergence mechanisms, and uses a variety of exploration and exploitation strategies to efficiently navigate the high-dimensional feature space and identify relevant features with high accuracy and efficiency.

Table [8](#page-22-0) illustrates the parameters and their corresponding values applied in this hybridized algorithm. Humpback whales use two ways to swim around their prey, as previously indicated. The mathematical model that has been proposed for updating whale positions and the following mathematical representation of this during optimization utilising GWO's leadership hierarchy is shown below using various equations. Using a bubble-net attack strategy, they use of the hierarchy to update the position of whales.

GWO Equations:

$$
M = |N \cdot \eta p(m) - \eta(m)| \qquad (23)
$$



<span id="page-22-0"></span>**Table 8** Parameter Settings of hybrid algorithm

$$
\eta(m+1) = \eta p(m) - \kappa \cdot M \tag{24}
$$

$$
\kappa = 2 \cdot \psi(m) \cdot \text{ran1} - \psi(m) \tag{25}
$$

$$
N = 2 \cdot \text{ran2} \tag{26}
$$

$$
M\alpha = | N1 \cdot \eta \alpha - \eta(m) |
$$
  
\n
$$
M\beta = | N2 \cdot \eta \beta - \eta(m) |
$$
  
\n
$$
M\delta = | N3 \cdot \eta \delta - \eta(m) |
$$
\n(27)

$$
\eta i1(m) = \eta \alpha(m) - \kappa i1 \cdot M\alpha(m)
$$
  
\n
$$
\eta i2(m) = \eta \beta(m) - \kappa i2 \cdot M\beta(m)
$$
  
\n
$$
\eta i3(m) = \eta \delta(m) - \kappa i3 \cdot M\delta(m)
$$
\n(28)

$$
\eta(m+1) = \frac{\eta i 1(m) + \eta i 2(m) + \eta i 3(m)}{3}
$$
\n(29)

Whale Equations

$$
\eta(m+1) = M' \cdot e^{bl} \cdot \cos(2\pi l) + \eta * (m) \tag{30}
$$

<span id="page-23-0"></span>
$$
M' = \mid \eta * (m) - \eta(m) \mid \tag{31}
$$

$$
\eta(m+1) = \eta * (m) - \kappa \cdot M, \text{ if } p < 0.5
$$
\n
$$
\eta(m+1) = M' \cdot e^{bl} \cdot \cos(2\pi l) + \eta * (m), \text{ if } p \ge 0.5
$$
\n
$$
(32)
$$

$$
M = |N \cdot \eta_{rand} - \eta| \tag{33}
$$

$$
\eta(m+1) = \eta_{rand} - \kappa \times M \tag{34}
$$

The following is a formula for GWO leadership: Humpback whales have a shrinking encircling mechanism utilising to update their position using Eq. ([29\)](#page-23-0).

**Mathematical model and algorithm for optimization** Spiral updating position: To update the position of humpback whales on a spiral path, use the formula below.

$$
M'_{\alpha} = \begin{vmatrix} \eta_{\alpha}(m) - \eta(m) \\ \eta_{\beta}(m) - \eta(m) \end{vmatrix}
$$
  
\n
$$
M'_{\beta} = \begin{vmatrix} \eta_{\beta}(m) - \eta(m) \end{vmatrix}
$$
 (35)

$$
\eta_1(m) = \eta_a(m) + M'_a \cdot e^{\chi \varphi} \cdot \cos(2\pi \varphi)
$$
  
\n
$$
\eta_2(m) = \eta_\beta(m) + M'_\beta \cdot e^{\chi \varphi} \cos(2\pi \varphi)
$$
  
\n
$$
\eta_3(m) = \eta_\delta(m) + M'_\delta \cdot e^{\chi \varphi} \cdot \cos(2\pi \varphi)
$$
\n(36)

And now

$$
\eta(m+1) = \frac{\eta 1 + \eta 2 + \eta 3}{3} \tag{37}
$$

### **2.5.1 Pseudo code**

The pseudo code for the proposed HWGO algorithm can be built in the following steps:

Step 1: Create the search agent's initial population.

Step 2: Determine the value of the objective function for each search agent.

Step 3:  $\eta_{\alpha}$ = The most suitable candidate.

Step 4:  $\eta_{\beta}$ = The second possible solution.

Step 5:  $\eta_{\delta=}$  The Third candidate solution.

Step 6: While (m < Max number of iterations).

Step 7: for  $i = 1$  to number of each search agent.

```
Step 8: Make a change to control parameter (κ, N, ψ,l and q).
```
Step 9: If<sub>1</sub>i =  $(q< 0.5)$ ,

Step 10: if<sub>2</sub> ( $|k|$  < 1).

Step 11: Update the search agent's position by (24).

Step 12: else If<sub>2</sub> ( $|\kappa| > 1$ ).

Step 13: Pick a search agent at random (*ηrand*).

- Step 14: Update the search agent's position by (29).
- Step 15: end if<sub>2</sub>.

Step 16: else if<sub>1</sub> ( $q$ >=0.5).

- Step 17: Update the position of the search agent by (32).
- Step 18: end if<sub>1</sub>.
- Step 19: end for.
- Step 20: Check to see whether any search agents have left the search space.
- Step 21: Calculate the value of each search agent's objective function.
- Step 22: Update the position of *ηα*, *ηβ* and*ηδ*.
- Step 23  $m = m + 1$
- Step 24: end while
- Step 25: return *ηα*.

**Variables used in the algorithm** *ηα*: The best candidate solution.

- *ηβ*: The second candidate solution.
- *ηδ*: The Third candidate solution.
- *q*: random number in [0,1].
- $\varphi$ : random number in [−1,1].

*χ*:The shape of the logarithmic spiral is defned by this constant.

- *η*: Humpback whale position vector.
- m: used for iterations.

### **2.5.2 Flowchart**

Figure [3](#page-25-0) depicts the hybrid algorithm and Fig. [4](#page-26-0) represents the diagrammatic representation of the whole suggested process for efficient glaucoma classification.



<span id="page-25-0"></span>**Fig. 3** Flowchart of the GWOWOA hybrid algorithm

## **3 Implementation, results and comparison**

## **3.1 Hardware and software**

All the experiments have been performed on a machine with Intel Core i5-8250U (8 Gen) at 1.60–1.80 GHz, 8 GB RAM and 64-bit Operating System. Language and the platform used was Python (version 3.7) and Jupyter Notebook. NumPy, Pandas, Seaborn, Matplotlib, Time, Random, Sklearn, and Math libraries were used. Within the python programming language used for coding, diferent libraries used are NumPy (Version 1.24.1) and Pandas (Version 2.0.3). In this work, normalization have been performed (using min-max approach) during data processing phase.



<span id="page-26-0"></span>**Fig. 4** Diagrammatic representation of the proposed framework for efficient glaucoma classification

#### **3.2 Performance measuring indicators and evaluation metrics**

The machine learning models, trained using the features identifed by soft-computing feature selection methods, present their results and fndings in this subsection. The objective of this training was to classify benchmark fundus images into two categories: healthy individuals and those with glaucoma. The confusion matrix, as shown in Table [9](#page-27-0) and Fig. [5](#page-27-1), is a performance metric used in machine learning classifcation tasks with multiple potential outputs. The table displays four unique combinations of actual and forecasted values. The confusion matrices measure roughly two by two. People often use this chart to demonstrate a specifc classifcation network's performance. The confusion matrix includes four values: true positive (TP), false positive (FP), true negative (TN), and false negative (FN). We have some confusion matrices that provide insights into the binary classifcation task of identifying positive cases of glaucoma. This empirical study includes a range of performance

<span id="page-27-1"></span><span id="page-27-0"></span>

assessment metrics, including F1-score, specifcity, accuracy, precision, sensitivity, Kappa, MCC, and AUC. We primarily use TP, TN, FP, and FN. False positive, or FP, occurs when a test result indicates the presence of a condition in people who do not actually have it. Based on the results, it appears that the individual is in excellent health. Regrettably, this prediction proves to be inaccurate and resembles a false alarm, a result that falls short of our initial expectations. Conversely, TP, or true positive, signifes that the individual indeed has glaucoma, which is the desired result. Similarly, FN represents a patient who shows signs of a specifc illness, but the diagnostic test produces a negative result. It is evident that the patient has tested positive for glaucoma, which is a very serious condition. On the other hand, TN refers to individuals who do not have an infection and therefore receive a negative test result. Figure [5](#page-27-1) displays the confusion matrix for the proposed work, with "negative" (0) indicating normal and "positive" (1) indicating glaucoma.

The main metrics for assessing diagnostic accuracy are recall and sensitivity. We determine recall by dividing the number of true positives by the sum of true positives and false negatives, and we represent the true positive rate with sensitivity. The assessment evaluates machine learning's accuracy in predicting the occurrence of glaucoma infection. The proportion of correct rejections to the overall number of evaluations is equivalent to the combination of sensitivity and the occurrence of incorrect rejections. We calculate accuracy by dividing the number of true negatives by the sum of true negatives and false positives. The measure of specifcity determines the ratio of correctly predicted negative cases, while the measure of sensitivity calculates the ratio of correctly predicted positive cases. Studies have shown that machine learning algorithms can provide accurate medical reports for individuals without glaucoma infections. We defne recall as a count of precise results. How closely a sample matches the target determines its accuracy. The F1-score is a method that takes into account both the accuracy and recall of the model to calculate a single number, known as the harmonic mean. The precision level of a measurement determines its accuracy in relation to the fnal result. Precision can be calculated by determining the ratio of true positives to the total of true positives and false positives. Precision is the most crucial measure for assessing the accuracy of the classifer model. The technique calculates the proportion of accurately defned images to the overall number of images in the dataset  $[108]$  $[108]$ . The scores for sensitivity and specificity are reliable indicators of performance accuracy. We use the Matthews correlation coefficient (MCC) as a metric to evaluate the accuracy of binary classifications. It provides a fair assessment by considering TP, TN, FP, and FN, even when the classes have diferent sizes. It plays a vital role in predicting human diseases using machine learning. It offers a comprehensive evaluation measure that considers the balance between sensitivity and specifcity in a meticulous manner. This facilitates model selection and optimisation while also ensuring their clinical applicability. The kappa score, also known as Cohen's kappa coefficient, serves as another statistical measure to evaluate the performance of machine learning models. This is particularly advantageous for assessing models used in classifcation tasks with categorical outcomes. The calculation determines the level of agreement between the anticipated and observed categories, taking into consideration the possibility of coincidental agreement. The kappa score is crucial in machine learning for predicting human diseases. The kappa score is a valuable indicator for predicting human diseases using machine learning techniques. It enables comparisons between models in terms of their performance and clinical utility. Furthermore, it serves as a measure of agreement that considers the potential for random concurrence.

The ROC curve is a visual representation of how well a classifcation model performs when it comes to adjusting classifcation thresholds. A ROC curve illustrates the correlation between the rates of true positive, false positive, and true negative at various classifcation thresholds. ROC analysis is a reliable method for accurately categorising glaucoma. The ROC curve is a visual representation of the classifcation's characteristics, showing the relationship between sensitivity and 1-specifcity. It provides valuable information about the measurement's sensitivity. A partially independent vector refers to the feld that exists below the curve. The ROC curve is a visual representation that illustrates the relationship between the true positive rate and the false positive rate. The ROC quantifes the level of distinction among various groups, demonstrating the model's ability to accurately categorize and examine these groupings. As the true positive rate increases, both the true positive and false positive rates will also increase in proportion. We evaluate the model's performance by computing the area under the receiver operating characteristic curve, which is a two-dimensional area that extends from the point (0,0) to (1,1). The model used to classify diferent groups is known as the area under the curve (AUC), indicating a higher level of excellence [\[109](#page-60-7)]. We expect the AUC to be 1.0, signifying fawless performance. A value of 0 would indicate a lack of predictive power, while a value of 0.5 would suggest that the model performs no better than random guessing. This is an all-encompassing measure of achievement at every level of acknowledgement.

$$
Sensitivity = \frac{True \text{ positives}}{True \text{ Positives} + False \text{ Negative}} \tag{38}
$$

$$
Specificity = \frac{True \ negative}{True \ Negatives + False \ positive}
$$
\n(39)

$$
Recall = \frac{\text{True positives}}{\text{True Positives} + \text{False Negatives}}
$$
(40)

$$
Precision = \frac{True \text{ positives}}{True \text{ positives} + False \text{ Positive}} \tag{41}
$$

 $Accuracy =$  True positives + True Negatives<br>True Positives + False Negatives + True Negatives

$$
(42)
$$

$$
F1 - Score = 2 * \frac{(\text{Precision} * Recall)}{(\text{Precision} + Recall)}
$$
(43)

**Parameters values for implemented machine learning models** The following values are fnalized for diferent parameters belonging to various ML classifers which have shortlisted for this work.

Random Forest Classifer:

n\_estimators=100, max\_depth:None, min\_samples\_split:2, min\_samples\_leaf:1,max\_ features:"auto ", max\_leaf\_nodes: None,max\_sample:None.

Logistic Regression:

Penalty=l2,  $C=1.0$ , fit\_intercept\_scaling=1, class\_weight=None, random\_ state=None, solver='lbfgs', max\_iter=100, multi\_class='auto' verbose=0 warm\_ start=False  $n$  jobs=None.

Decision Tree Classifier:<br>Criterion = 'gini' splitter = 'best' Max depth=None,min samples leaf=1,  $min\_weight\_fraction = 0.0,$  max $__feature = None, random\_state = None,$  max $__leaf$  $nodes = None$ ,  $min\_impurity\_decrease = 0.0$ ,  $class\_weight = None$ .

KNN:

 $N_{\text{neighbours}} = 5$ , weights  $=$  'uniform', algorithm  $=$  'auto', leaf<sub>size</sub>  $= 30$ , metric='minkowski',metric\_rarams=None,n\_jobs=None.

Support Vector Machine:

 $C=1.0$ , kernel = 'rbf', degree = 3, gamma = 'scale', coef $0=0.0$ , shrinking = True prob $ability = False$ ,  $tol = 0.001$ ,  $cache\_size = 200$ ,  $class\_weight = None$ , verbose = False, max\_ iter=−1,decision\_function='ovr',break\_ties=False,random\_state=None.

#### **3.3 Results**

We have compressed all of the GWO and WOA results into one comparative table ( Table [10\)](#page-30-0), which shows the overall best results of the entire experimental process. We have compressed all the results of GWO and WOA into a single comparative table due to space constraints and the large number of results we can display. If any reader is interested in seeing these results in detail, we can share them via email (Table [10](#page-30-0)).



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### **3.3.1 Results of hybrid GWOWOA algorithm**

Here are the results of the hybrid GWOWOA algorithm when we have provided the dataset **ORIGA\_ALL\_FEATURES** to the particular code. We have performed the experiment on population size (5, 10, 15, 20) and recorded ftness values on iterations (100, 200, 300, 400, and 500). Due to space constraints, we have shown convergence curves for population sizes 10 and 20 only. Tables [11](#page-33-0), [12,](#page-34-0) [13,](#page-35-0) [14](#page-36-0), [15](#page-37-0), [16,](#page-38-0) [17,](#page-39-0) [18](#page-40-0), [19](#page-41-0), [20,](#page-42-0) [21](#page-43-0), [22](#page-44-0) show the results generated through the features selected through the hybrid algorithm. Table [23](#page-45-0) compiles all previous tables to present the overall best results of the experimentation process. We present the confusion matrix and convergence curve related to these experiments in Figs. [6](#page-46-0), [7](#page-46-1), [8](#page-47-0), [9,](#page-47-1) [10,](#page-48-0) [11,](#page-48-1) [12](#page-48-2), [13](#page-49-0), [14,](#page-50-0) [15.](#page-50-1)

The column features selected shows the number of features that have been selected from the total features in the dataset at each individual iteration and the ftness value calculated at that iteration.

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**Convergence evaluation for population 10** The convergence behaviour of Hybrid Grey Wolf Optimizer and Whale Optimization Algorithm is evaluated over the objective function (Rastrigin Function) with population 10 for iterations (100, 200, 300, 400, and 500) and the curves are given below.

The column features selected shows the number of features that have been selected from the total features in the dataset at each individual iteration and the ftness value calculated at that iteration.

The column features selected shows the number of features that have been selected from the total features in the dataset at each individual iteration and the ftness value calculated at that iteration.

**Convergence evaluation for population 20** The convergence behaviour of Hybrid Grey Wolf Optimizer and Whale Optimization Algorithm is evaluated over the objective function (Rastrigin Function) with population 20 for iterations (100, 200, 300, 400, and 500) and the curves are given below.

## **3.4 Discussion**

The WOA's convergence curves indicate stepwise fuctuation in the early iterations, but very modest variability after a specifc number of iterations. The WOA's convergence curves converge swiftly, and we are now exploiting the search space's dimensions to obtain the optimal result. The switching continues until they have exploited the entire search space. As the iteration progresses to the termination condition, the falling trend of these convergence curves illustrates a population of whales working together to improve results by updating their positions to a much better one. The WOA algorithm features a better balance between exploration and exploitation, which leads to improved convergence. Because the WOA is optimized for a multimodal function, it has similar convergence behavior. As a result, the convergence behavior is consistent across populations.

<span id="page-33-0"></span>



<span id="page-34-0"></span>**Table 12** Results along with best confusion matrix and AUC curve observed with 5-Fold with population size 5

<span id="page-35-0"></span>



<span id="page-36-0"></span>**Table 14** The results for the hybrid algorithm when the experiment performed on population 10 for iterations (100, 200, 300, 400, and 500)

Table 14 The results for the hybrid algorithm when the experiment performed on population 10 for iterations (100, 200, 300, 400, and 500)

<span id="page-37-0"></span>



<span id="page-38-0"></span>**Table 16** Results along with best confusion matrix and AUC curve observed with 10-Fold with population size 10

<span id="page-39-0"></span>



<span id="page-40-0"></span>**Table 18** Results along with best confusion matrix and AUC curve observed with 5-Fold with population size 15

<span id="page-41-0"></span>

<span id="page-42-0"></span>

<span id="page-43-0"></span>



<span id="page-44-0"></span>**Table 22** Results along with best confusion matrix and AUC curve observed with 10-Fold with population size 20

Table 23 Overall best results of the whole experiment process **Table 23** Overall best results of the whole experiment process

<span id="page-45-0"></span>OVER ALL BEST RESULTS OVER ALL BEST RESULTS





<span id="page-46-0"></span>**Fig. 6** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 5 and cross validation was 5-fold



<span id="page-46-1"></span>**Fig. 7** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 5 and cross validation was 10-fold

The GWO's convergence curves show high fuctuations in the frst iteration and very low variations after a certain number of iterations. The convergence curves of the GWO converge quickly as they have explored the whole search space and then started exploitation in the dimensions of the search space, fnding the best result. The cycle continues until the search space yields the optimal feature set. The descending trend of these convergence curves depicts the population of wolves that are in collaboration, improving results by updating their positions to a much better one as the iteration moves to the termination condition. The descending trend of these convergence curves depicts the population of wolves that are in collaboration, improving results by updating their positions to a much better one as the iteration moves to the termination condition. The GWO algorithm exhibits superior convergence, suggesting a superior equilibrium between exploration and exploitation. Hence, the convergence behavior is similar for diferent populations.

The convergence curves of the hybrid of GWO and WOA are much better than those of the Grey Wolf Optimizer and the Whale Optimizer because the hybrid's convergence curves do not converge as quickly as those of the Whale Optimizer, indicating that it has a



<span id="page-47-0"></span>**Fig. 8** Convergence curves for WOA algorithm when population size was 15



<span id="page-47-1"></span>**Fig. 9** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 10 and cross validation was 5 fold



<span id="page-48-0"></span>**Fig. 10** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 10 and cross validation was 10-fold



<span id="page-48-1"></span>**Fig. 11** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 15 and cross validation was 5-fold



<span id="page-48-2"></span>**Fig. 12** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 15 and cross validation was 10-fold



<span id="page-49-0"></span>**Fig. 13** Convergence curves for hybrid algorithm when population size was 20

good exploration capability, but it exploits the data using the Whale Optimizer's bubble net attacking method. The curves are the fnest compromise between exploration and exploitation. The curves of the hybridized version algorithm are asymptotic due to the use of an objective function. The algorithm updates the search agents' placements, calculates their ftness values, and selects the best search agent based on the falling trend of these convergence curves. The Grey Wolf Optimizer's wolves, primarily the Alpha, Beta, and Delta, serve as search agents in the hybrid version of GWO and WOA, providing excellent exploration capabilities, while the whale's bubble net attacking style enhances prey exploitation.

The proposed approach uses three diferent algorithms—GWO, WOA, and a hybrid approach that incorporates the traits of both algorithms. The three implemented soft-computing algorithms perform the optimization on the dataset ORIGA\_ALL\_FEATURES, selecting the most informative features out of a total of 65 features. The primary aim of



<span id="page-50-0"></span>**Fig. 14** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 20 and cross validation was 5-fold



<span id="page-50-1"></span>**Fig. 15** Confusion matrix of best classifer and the combined ROC curves for hybrid algorithm population size was 20 and cross validation was 10-fold

these methods is to narrow down the initial feature set, which serves as the input for various machine learning classifers. The key goal is to correctly divide the two distinct types of subject-fundus photographs. We administered multiple distinct tests as part of a comprehensive investigation, using all three methods. Every experiment shares a similar objective function. The experimental framework shows a population size ranging from 5 to 20, with increments occurring at regular intervals of 5. We evaluate the population's performance by gradually altering the number of iterations, which ranges from 100 to 500 with increments of 100. The classifer then receives the attributes (features) of the instance exhibiting the smallest value of the objective function, without examining or accounting for the remaining four incidences in the research. The tables above indicate that we must gather a minimum of 23 features and a maximum of 40. As a result, the degree of feature reduction is highly variable, ranging from 65% (equal to 23 out of 65) to a maximum of 40 obtained after the evaluation, which is 35% of the maximum possible score of 65 features. In order to determine the execution's time, a precise inspection of two diferent perspectives is required. The demonstration also includes the temporal element of iteration in soft computing techniques. After that, an investigation into the temporal specifcations for the development and assessment of machine learning models will take place. For this current work, we select and implement six machine learning classifiers. The first five ML classifers are classical, and the sixth one is the ensemble of all fve. We assess the efectiveness of classifers using a variety of metrics, including accuracy, sensitivity, specifcity, and precision. Additionally, the F1-Score, Kappa-Score, Matthews Correlation Coefficient (MCC), and Area under the Curve (AUC) are used. According to the examination of medical images, each of these metrics is essential to the prognosis of human disorders. Research investigations rarely examine all of these calculations simultaneously.

We assess the model's performance by calculating the percentage of accurate predictions compared to the total number of predictions made. We obtain the accuracy rate by dividing the total number of predictions by the number of accurate forecasts. One of the most important performance indicators is the measure of accuracy, and our fndings in this particular area deserve attention. The accuracy has signifcantly increased in the hybrid algorithm's integration with the Ensemble classifer, rising to an auspicious rate of 96.55%. The GWO case has an accuracy of 95.6%, the WOA case has an accuracy of 95.2%, and the hybrid case has the lowest accuracy rate at 93.1%, which is also very satisfactory. The hybrid algorithm selected features that achieved an accuracy rate of more than 90% in all situations. Therefore, we can conclude that this study's strategy exhibits a signifcant level of accuracy. Sensitivity is a key concept in the measuring feld, particularly in terms of a test's capacity to correctly identify people who actually have the ailment. In clinical contexts, we refer to the "detection rate" as the percentage of individuals who receive a positive test result for a specifc illness among those who actually have the condition. A diagnostic test with 100% sensitivity will reliably identify and label every patient with the specifc illness as positive. According to the results of the GWO study's sensitivity fndings, the SVM model has the highest score, 0.981. In a situation like this, WOA records the highest sensitivity score, up to 0.974. Using a ML classifer allows the hybrid models to achieve their highest sensitivity score, precisely 0.973.

The idea of specifcity has to do with how well a diagnostic test can distinguish between those who are in excellent health and don't exhibit any symptoms. The term "specifcity" refers to the proportion of people who test negative for a particular ailment even when they do not have the disease. A positive outcome suggests a higher probability of the disease being present. A test with the highest level of specifcity would correctly identify healthy people by returning a negative result. On the other hand, a test with less than full specifcity would unambiguously rule out the existence of the condition. Because individuality is so important, it is imperative to carefully evaluate the factors that lead to its development. When implementing the SVM model, WOA has the highest value of 0.933. The best GWO value is 0.921. The hybrid technique's fnding, which also uses these classifers, reveals a maximum value of 0.903. We use the harmonic mean of accuracy and recall to derive the F1-score, which ofers a fair evaluation of the classifer. The F1 score is a well-known performance statistic for assessing the efectiveness of classifcation models. We specifcally designed the evaluation to assess accuracy, taking into account both the potential negative and positive efects of incorrect results. The maximum F1-score for the integration of the GWO-CatBoost classifer and Hybrid-Ensemble is 0.975; also, the maximum F1-score for the WOA is equivalent to 0.967. Precision, a quantitative measurement, assesses the proportion of correctly identifed positive cases compared to the total number of instances classifed as positive. It is possible to accurately determine the prevalence of glaucoma in a population using a number of viable methods. Furthermore, the degree of precision closely correlates with the quantity of pertinent data points. When starting medication for a patient who, according to our theoretical framework, has glaucoma-like symptoms but not the actual clinical condition, it is crucial to exercise caution. When integrating GWO with RF at their respective maximum values, the optimal combination for precision values is 0.976. Our proposed hybrid algorithm achieves superior accuracy and F1-Score compared to other benchmark approaches. When it comes to measuring precision, sensitivity, F1-score, kappa score, and MCC performance, GWO even slightly outperforms the proposed hybrid algorithm.

There are equivalent sets of sensitivity and specifcity values for each diagnostic threshold. We generated a Receiver Operating Characteristic (ROC) curve, a graphic depiction of paired data points, using the dataset. The x-axis represented specifcity, while the y-axis represented sensitivity. Both the AUC calculation and the receiver operating characteristic (ROC) curve analysis can assess a test's capacity to discriminate between groups. The test shows increasing discriminating ability in diferentiating between impacted and unafected scenarios as the curve slowly approaches the top left corner and the region beneath it grows. The integral of the curve ranges from 0 to 1, which is a valid indicator of the test's efectiveness. An ideal diagnostic test has an AUC of 1, while an area of 0.50 describes a non-selective zone of the test. The AUC is a regularly used metric for assessing a test's diagnostic accuracy. Additionally, we have calculated the AUC values, which serve as indicators of successful outcomes in the specifc study setting. As the number gets closer to 1.000, the overall quality of the output shows a discernible improvement. The combination of the SVM classifer and the GWO achieved the best AUC value of 0.943, which was also the best result of the WOA algorithm. The hybrid strategy showed the highest AUC score of 0.938. The AUC metric shows that the SVM classifer performs admirably. The fndings include numerous important metrics, including receiver operating characteristic (ROC) curves for each instance, confusion matrices, and estimates of the Matthews correlation coefficient (MCC) and Kappa scores for each experiment. We also compute and show execution time, along with other key performance measurement parameters.

#### **3.5 Comparison with the current best practices**

A comparison of the suggested method to the most cutting-edge glaucoma prediction methods is shown in Table [24.](#page-53-0) The comparison table that is shown demonstrates how well the methods used in this study performed in terms of detecting glaucoma when compared to earlier research. With an accuracy of up to  $96.5\%$  efficacy in recognising glaucoma when compared to earlier research, the offered table provides strong evidence that the suggested approach is reliable and profcient in categorising fundus pictures. The performance's sensitivity and specifcity are encouraging, as are other metrics. When compared to the other 18 techniques indicated in Table [24](#page-53-0) that were published in or after 2018, our performance shows exceptional results. Our approach, which makes use of machine learning and soft computing techniques, has proven to be more successful than deep learning approaches in a few situations. It is important to keep in mind that in certain cases, the datasets used to evaluate the other approaches may be diferent.

## **4 Conclusion**

It is commonly acknowledged that feature selection (FS) is a crucial pre-processing step in modelling. FS main goal is to get rid of pointless features so that the learning model performs better by using the right number of features. This is important in the feld



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of biomedical research, particularly in illness databases, where it has been noted that patients' various characteristics are captured, and a wrong diagnosis might have serious repercussions. To address this issue, we have proposed a pioneering method for FS. Our approach employs three algorithms derived from nature to identify the most signifcant traits. The suggested approach selects limited features while maintaining a high degree of classifcation accuracy. We have applied this approach to the ORIGA collection of glaucoma images, accessible to the general public. This investigation focuses on glaucoma, the second most common cause of vision loss in people. The only way for people to protect themselves from the negative efects of glaucoma is through timely identifcation to reduce the risk of vision loss as well as initiating the treatment. Using both 5-fold cross-validation and 10-fold cross-validation procedures, several machine learning classifers were trained and tested on the features selected through soft-computing computing. To fully explore the occurrence of glaucoma, we extract a mix of several classes of features, such as clinical measurement features and image-based features (e.g., statistical features). This strategy seeks to greatly improve the glaucoma screening classifer's accuracy by accumulating extensive evidence for glaucoma discrimination. Our glaucoma screening approach surpasses other available recent approaches in terms of accuracy, sensitivity, and specifcity, according to experimental results derived from the ORIGA dataset. The soft-computing algorithms' accuracy rate was 95%, while the hybrid method's accuracy rate exceeded that of the individual algorithms by more than 96%. In contrast to many other current approaches taken into consideration in this comparison, the acquired fndings show greater performance. Therefore, we can regard the suggested novel methodology as an appropriate and reliable technique for automated glaucoma screening in a variety of clinical scenarios. To illustrate our strategy's resilience, we want to use high-dimensional datasets in the future. In our future endeavors, we want to use the suggested technique in a variety of clinical and real-world situations. As a result, we will be able to improve classifcation accuracy and get more exact results. We can observe, formulate, and analyze this two-class classifcation problem as a mutiobjective problem, where the two conficting objectives aim to maximize accuracy while minimizing the number of features. Similarly, we can add more objectives and transform the problem into multiple objective problems, each with more than two objectives. We can compute and suggest multiple solutions using Pareto fronts, enabling researchers and those in need to select the ones that best suit their needs.

The extremely favourable outcome shows that hospitals in remote locations with a shortage of expert medical practitioners can deploy the proposed system. Additionally, it serves as a second opinion, alleviating the burden on overworked, experienced, and senior ophthalmologists. The approach, which is highly efficient and affordable, aids humanity by successfully classifying images of humans as healthy or infected, thereby initiating the best treatment as soon as possible, mitigating (slowing down) the spread of the disease, and preventing humans from losing their visibility permanently. The suggested system can seamlessly integrate with the Internet of Things, providing the human race with Internet of Medical Things functionalities. From patient images, the suggested method can also predict the presence of other diseases like skin cancer, breast cancer, and diabetic retinopathy.

This empirical study's validation of the proposed approach on a medium-sized dataset is one of its major limitations. Validation on multiple datasets, or a combination of diferent medium- or small-size datasets, will increase confdence in the suggested approach. We could have extracted a larger number of features from this fundus image dataset. Extracting more features might impact the performance of the approach.

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**Data availability** "The datasets analyzed during the current study are easily and publically available in the internet's repository," We also confrm that data will be available on demand.

## **Declarations**

**Competing interests** "The authors have no relevant fnancial or non-fnancial interests to disclose. The authors declare that they have no known competing fnancial or personal relationships that could be viewed as infuencing the work reported in this paper".

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