



# Anonymous biometrics-based authentication with key agreement scheme for multi-server environment using ECC

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Received: 6 February 2018 / Revised: 12 May 2019 / Accepted: 21 May 2019 /

Published online: 24 June 2019

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## Abstract

The rapidly evolving communication technology has now made it easy for people to enjoy kinds of online services over the insecure public internet. However, with convenience, ensuring data security as well as user privacy and authentication is particularly important and urgent. In view of this, this work presents a new biometrics-based three-factor authentication with key agreement scheme for multi-server environment using ECC. The formal authentication proof using BAN logic confirms that the new scheme can achieve mutual authentication and agree on a common session key; and the heuristic cryptanalysis shows that the new scheme provides perfect forward secrecy, preserves user anonymity and secures against various known security vulnerabilities. Furthermore, the performance evaluation demonstrates that our scheme is efficient.

**Keywords** Elliptic curve cryptography · Multi-server · Biometrics · Authentication · Three-factor · Smart-card

## 1 Introduction

The advancement of network and communication technologies has brought more and more offline services online, and people are now enjoying high-efficiency online services such as e-health, e-commerce and e-government, etc. However, these online services are provided over the insecure public internet, where adversaries can easily perform some attacks, like privacy violating, impersonation attack, replay attack, man-in-the-middle attack, etc. To deal with these security challenges, authentication with session key agreement protocol is deployed to ensure

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that only certified users can enjoy services, only the legitimate service providers can be accessed, and the exchanged critical information is secured by encryption with the negotiated session key.

## 1.1 Related works

In recent years, numerous authentication schemes have been designed to maintain secure communications between the remote users and the servers over the internet. Many smart-card based two-factor authentication schemes [4, 8, 9, 12, 17, 20, 21, 23, 24] were proposed in which the elliptic curve cryptography (ECC) was applied to establish security since ECC can provide the same level of security with far less key size and faster computing speed. However, all these schemes are only applicable to single-server environment and many of them have been found vulnerable to various attacks. Compared with single-server environment, multi-server environment has the obvious advantage that it enables users to access various application servers with one account. To adapt to the security requirements of multi-server environment, several kinds of authentication schemes [1, 3, 5, 6, 10, 11, 13, 15, 16, 18, 19, 22, 25] with respect to multi-server environment have therefore been presented.

In 2013, Yoon and Yoo [25] presented a biometrics-based multi-server authentication scheme using ECC, while Kim et al. [15] proved that this scheme is prone to the offline password guessing attack, and an improvement for this scheme was presented. Later, Chuang et al. [6] came up with an anonymous biometrics-based authentication scheme with respect to multi-server environment, while Mishra et al. [18] soon proved that this scheme was prone to the server spoofing, smart-card stolen and impersonation attacks, and they put forward a new scheme. However, Lu et al. [16] soon proved that Mishra et al.'s new scheme was not to secure against the forgery and server masquerading attacks, and they redesigned an authentication scheme for multi-server environment using asymmetric cryptography. Nevertheless, Lu et al.'s new scheme was soon identified by Chaudhry et al. [5] to be vulnerable to the impersonation attack.

Afterwards, Odelu et al. [19] put forward a new biometrics-based multi-server authentication scheme on the basis of He and Wang's scheme [10] with the aim to eliminate its security weaknesses. Later, Shen et al. [22] came up with a multi-server authentication scheme not preserving user anonymity. Later, Amin et al. [1] proposed an anonymity preserving authentication scheme for multi-server telemedicine information system using ECC, but very recently, their scheme was found by Irshad et al. [11] to be vulnerable to the offline password guessing and impersonation attacks. Recently, Chandrakar and Om [3] presented an anonymous three-factor authentication scheme for multi-server environment using ECC; and Jangirala et al. [13] presented a dynamic identity based multi-server authentication scheme. However, like the schemes [6, 18], Jangirala et al.'s scheme doesn't employ asymmetric cryptographic primitives to ensure security either. Thus, it fails to provide the forward secrecy.

## 1.2 Motivation and contributions

By investigating the related existing schemes, it can be found that various weaknesses are still within many of them. To ensure that remote users can enjoy online services and exchange critical data securely, this work designs a new robust biometrics-based authentication scheme based on previous researches for multi-server environment. The proposed scheme preserves user's biometrics template privacy by employing the fuzzy extractor [7], and the formal authentication proof by Burrows-Abadi-Needham (BAN) logic [2] shows that the new scheme

can effectively realize mutual authentication and agree on a common session key. Besides, the heuristic security discussion in this paper demonstrates that our scheme can preserve user anonymity, provide perfect forward secrecy and protect users from various known security loopholes such as impersonation attack, replay attack, denial of service attack, and offline password guessing attack, etc. In addition, since our scheme has the advantage in network architecture design, i.e. the registration center in our scheme will no longer participate in the subsequent user-server session key negotiation processes after completing the user authentication, thus greatly reducing computation and communication costs in the authentication with key agreement phase. Hence, besides the security attributes, our new scheme has advantages over other relevant schemes in terms of computation and communication costs.

### 1.3 Organizations

The rest of this article is arranged as follows. Section 2 describes the necessary preliminaries. Section 3 introduces our new biometrics-based authentication with key agreement scheme for multi-server environment. The authentication proof by BAN logic is presented in Section 4; the security analysis of the proposed scheme is presented in Section 5; and the performance evaluation is presented in Section 6. Finally, conclusions are given in Section 7.

## 2 Preliminaries

This section briefly lists the notations used throughout this work, and introduces the essential notion and definitions of ECC and the fuzzy extractor.

### 2.1 Notation guide

The meaning of the frequently used notations in this paper is shown in Table 1.

**Table 1** Notations & descriptions

Notations	Descriptions
$RC$	the registration center
$n, p$	two sufficiently large prime numbers
$F_p$	a prime finite field
$x$	the master secret key of $RC$
$E_p(a, b)$	an non-singular elliptic curve $E$ over $F_p$ , defined by $y^2 = x^3 + ax + b \pmod{p}$
$G$	a base point over $E_p(a, b)$ with prime order $n$
$P_{pub}$	the public key of $RC$
$U_i$	the $i$ th user
$S_j$	the $j$ th server
$ID_i, pw_i, B_i$	$U_i$ 's identity, password, biometrics
$SID_j$	$S_j$ 's identity
$Z_n$	the interval $[1, n - 1]$
$H(\cdot), h(\cdot)$	two secure one-way hash functions
$\oplus$	the bitwise XOR operation
$\parallel$	the concatenation operation
$\Delta t$	the preset threshold
$SC_i$	$U_i$ 's smart card

## 2.2 Elliptic curve over a prime field $F_p$

Let the symbol  $E_p(a, b)$  denote an elliptic curve  $E$  over a prime finite field  $F_p$ , defined by the non-singular elliptic curve equation:  $y^2 = x^3 + ax + b \pmod p$ ,  $a, b \in F_p$  with the *discriminant*:  $\Delta = 4a^3 + 27b^2 \pmod p \neq 0$ . That is,

$$E_p(a, b) = \{(x, y): x, y \in F_p, y^2 = x^3 + ax + b \pmod p, \Delta = 4a^3 + 27b^2 \pmod p \neq 0, a, b \in F_p\} \cup \{\mathcal{O}\}.$$

The scalar multiplication over  $E_p(a, b)$  defined as  $tP = P + P + \dots + P$  ( $t$  times).

A point  $P$  has order  $n$  if  $nP = \mathcal{O}$  for the smallest integer  $n > 0$ , where  $\mathcal{O}$  is the extra point called infinity point.

**Definition 1** Elliptic curve discrete logarithm problem (ECDLP) is defined as follows: Given  $P \in E_p(a, b)$  with order  $n$  and  $Q = kP \in E_p(a, b)$ , it is infeasible to derive the integer  $k \in [1, n - 1]$ .

**Definition 2** Computational Diffie-Hellman problem (CDHP) is defined as follows: Given  $P, aP, bP \in E_p(a, b)$ , it is intractable to compute  $abP \in E_p(a, b)$ .

## 2.3 Fuzzy extractor

Fuzzy extractor [7] is used to extract a uniform random string  $\sigma_i$  from the inputted biometrics template  $B_i$  in an error-tolerant way, which means  $\sigma_i$  can be derived each time with a noisy biometrics template  $B_i^*$  and an auxiliary string  $\theta_i$  if  $B_i^*$  is reasonably similar to the original  $B_i$ . A fuzzy extractor comprises two procedures, namely, the probabilistic generation procedure *Gen* and the deterministic reproduction procedure *Rep*. More concrete descriptions are as follows:

- (1)  $(\sigma_i, \theta_i) = \text{Gen}(B_i)$  means when receiving the inputted biometrics  $B_i$ , *Gen* outputs a uniform random string  $\sigma_i$  and an auxiliary string  $\theta_i$ .
- (2)  $\sigma_i = \text{Rep}(B_i^*, \theta_i)$  means *Rep* can recover  $\sigma_i$  with the noisy biometrics  $B_i^*$  and the corresponding random auxiliary string  $\theta_i$  when  $\text{dis}(B_i^*, B_i) < \Delta t$ , where *dis* represents the distance function and  $\Delta t$  is the error threshold.

## 3 Our proposed scheme

This section presents our new biometrics-based authentication with key agreement protocol for multi-server environment, which comprises the following four phases.

### 3.1 System initialization phase

The registration center *RC* first takes the following steps to initialize the system parameters.

- (1) *RC* selects a non-singular elliptic curve  $E_p(a, b)$  with a large prime order  $n$ , and a base point  $G$  with the order  $n$  over  $E_p(a, b)$ .
- (2) *RC* selects two cryptographic hash functions:  $H : \{0, 1\}^* \rightarrow Z_p^*$ ,  $h : \{0, 1\}^* \rightarrow Z_p^*$ .

- (3)  $RC$  generates its private key  $x \in \mathbb{Z}_n^*$  which should be kept secret strictly, and then computes its public key  $P_{pub} = x \cdot G$ .
- (4)  $RC$  publishes the system parameters  $\{E_p(a, b), G, n, P_{pub}, H(\cdot), h(\cdot)\}$ .

### 3.2 Registration phase

The registration phase of our scheme comprises the following two phases.

#### 3.2.1 Server registration phase

To deploy a new server  $S_j$  to be a legal server, the following steps also shown in Fig. 1 need to be executed.

- (1)  $S_j$  selects its identity  $SID_j$  and transmits it to  $RC$  via a secure channel.
- (2)  $RC$  generates a random number  $r_j$  and computes the secret key  $k_j = h(SID_j || x || r_j)$ , then stores  $\{SID_j, r_j\}$  into its security database and transmits  $k_j$  back to  $S_j$  via a secure channel, where  $x$  is the system private key.
- (3) Upon receiving  $k_j$ ,  $S_j$  keeps it secretly.

#### 3.2.2 User registration phase

To be a legal user,  $U_i$  needs to take the following steps also shown in Fig. 2, to register in  $RC$ .

- (1)  $U_i$  inputs his/her identity  $ID_i$ ,  $pw_i$  and imprints  $B_i$  on a sensor.
- (2)  $U_i$  computes  $(\sigma_i, \theta_i) = Gen(B_i)$ ,  $MP_i = h(pw_i || \sigma_i)$  and transmits  $ID_i, MP_i$  to  $RC$  by a secure channel.
- (3) Upon receiving  $ID_i$  and  $MP_i$ ,  $RC$  checks the validity of  $ID_i$  and whether  $h(ID_i)$  exists in  $RC$ 's user database. If not,  $RC$  stores  $h(ID_i)$  in its user database and computes  $r_i = h(ID_i || x)$   $k_i = r_i \oplus MP_i$ ,  $v_i = H(ID_i || r_i || MP_i)$ , where  $x$  is the system private key, and then  $RC$  stores  $\{k_i, v_i, H(\cdot), h(\cdot)\}$  into a smart-card  $SC_i$  and returns it back to  $U_i$ ; otherwise  $RC$  aborts the procedure.
- (4) After receiving  $SC_i$ ,  $U_i$  stores  $\theta_i$  into  $SC_i$ .

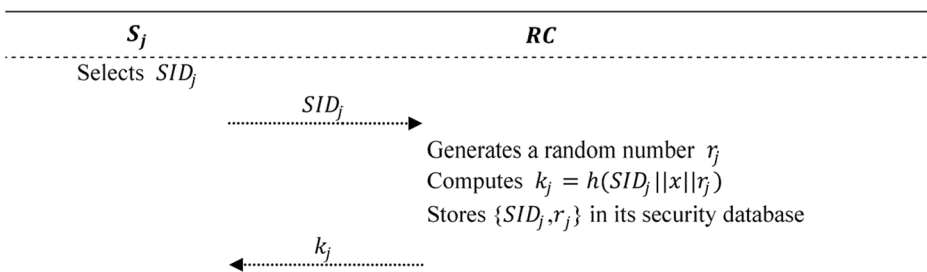


Fig. 1 Server registration phase

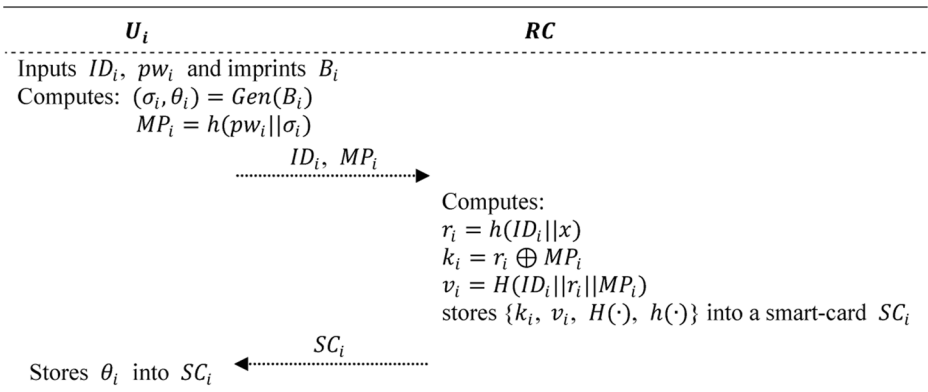
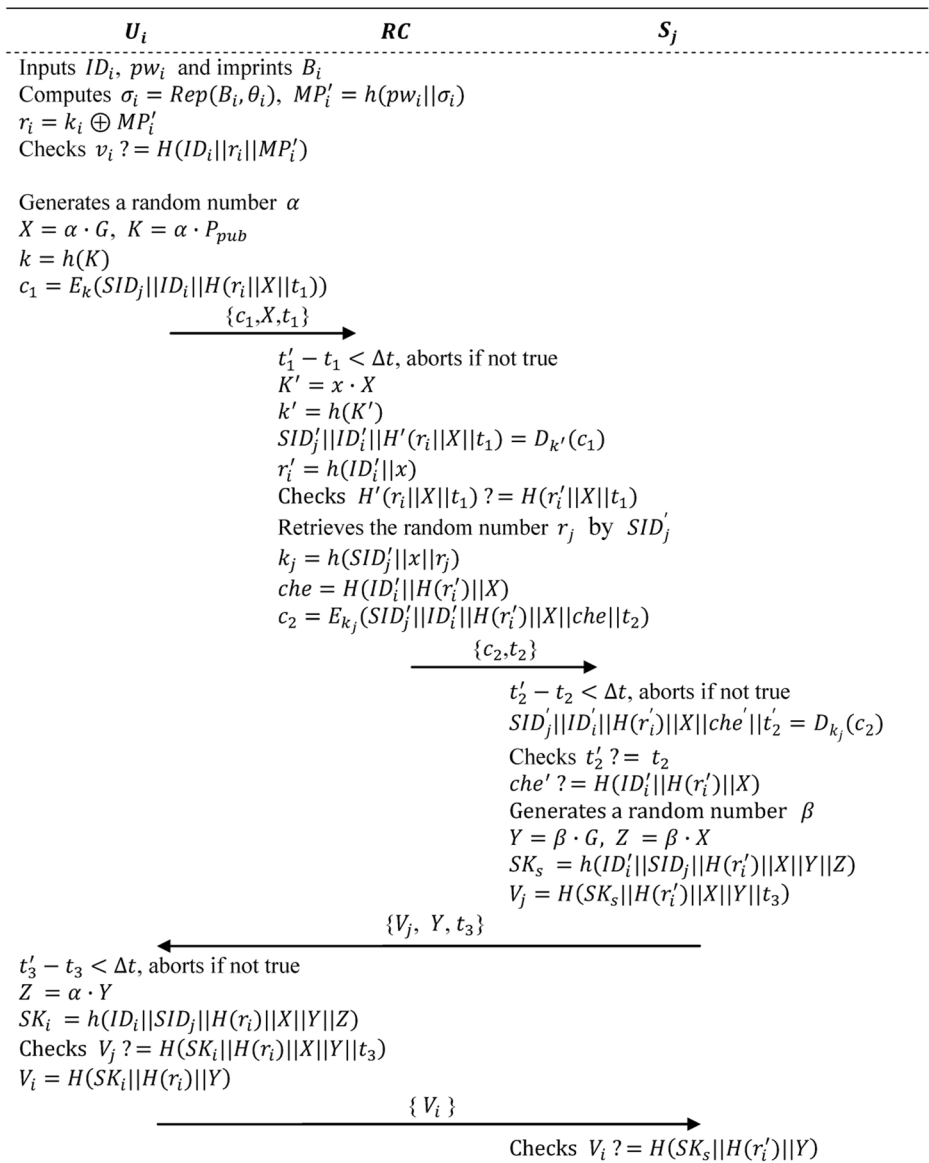


Fig. 2 User registration phase

### 3.3 Login and mutual authentication with key agreement phase

Assume that a remote user  $U_i$  wants to enjoy online services from  $S_j$ , then, he/she needs to perform the following steps to accomplish the mutual authentication processes and agree on a session key for encrypting the subsequent communications over the insecure public channel as shown in Fig. 3.

- (1)  $U_i$  inserts his/her smart-card  $SC_i$  into a card reader, then inputs  $ID_i, pw_i$ , and imprints  $B_i$  at a sensor.
- (2)  $SC_i$  computes  $\sigma_i = Rep(B_i, \theta_i)$ ,  $MP'_i = h(pw_i || \sigma_i)$ ,  $r_i = k_i \oplus MP'_i$ , and checks whether  $v_i = H(ID_i || r_i || MP'_i)$  holds. If not,  $SC_i$  rejects  $U_i$ , otherwise,  $SC_i$  generates a random number  $\alpha$  to compute  $X = \alpha \cdot G$ ,  $K = \alpha \cdot P_{pub}$ ,  $k = h(K)$ ,  $c_1 = E_k(SID_j || ID_i || H(r_i || X || t_1))$ , where  $t_1$  is the current timestamp of  $U_i$ , and sends  $\{c_1, X, t_1\}$  to  $RC$ .
- (3) Upon receiving the message  $\{c_1, X, t_1\}$ ,  $RC$  gets its current timestamp  $t'_1$  and checks whether  $t'_1 - t_1 < \Delta t$  holds. If not,  $RC$  aborts the procedure, otherwise,  $RC$  computes  $K' = x \cdot X$ ,  $k' = h(K')$ ,  $SID'_j || ID'_i || H'(r_i || X || t_1) = D_{k'}(c_1)$ ,  $r'_i = H(ID'_i || x)$  and checks whether  $H'(r_i || X || t_1) = H(r'_i || X || t_1)$  holds. If not,  $RC$  aborts the procedure; otherwise,  $RC$  retrieves the random number  $r_j$  by  $SID'_j$  and computes  $k_j = h(SID'_j || x || r_j)$ ,  $che = H(ID'_i || H(r'_i) || X)$ ,  $c_2 = E_{k_j}(SID'_j || ID'_i || H(r'_i) || X || che || t_2)$  and sends  $\{c_2, t_2\}$  to  $S_j$ .
- (4) Upon receiving the message  $\{c_2, t_2\}$ ,  $S_j$  gets its current timestamp  $t'_2$  and checks whether  $t'_2 - t_2 < \Delta t$  holds. If not,  $S_j$  aborts the procedure, otherwise, computes  $SID'_j || ID'_i || H(r'_i) || X || che || t'_2 = D_{k_j}(c_2)$  and checks whether  $t'_2 = t_2$  and  $che' = H(ID'_i || H(r'_i) || X)$  hold. If not,  $S_j$  aborts the procedure, otherwise, generates a random number  $\beta$  to compute  $Y = \beta \cdot G$ ,  $Z = \beta \cdot X$ ,  $SK_s = h(ID'_i || SID_j || H(r'_i) || X || Y || Z)$ ,  $V_j = H(SK_s || H(r'_i) || X || Y || t_3)$  where  $t_3$  is the current timestamp of  $S_j$ , and sends  $\{V_j, Y, t_3\}$  to  $U_i$ .
- (5) Upon receiving the message  $\{V_j, Y, t_3\}$ ,  $U_i$  gets its current time stamp  $t'_3$  and checks whether  $t'_3 - t_3 < \Delta t$  holds. If not,  $U_i$  aborts the procedure, otherwise, computes  $Z = \alpha \cdot Y$ ,  $SK_i = h(ID_i || SID_j || H(r_i) || X || Y || Z)$  and checks  $V_j = H(SK_i || H(r_i) || X || Y || t_3)$ ; if not,  $U_i$  aborts the procedure, otherwise, accepts  $SK = h(ID_i || SID_j || H(r_i) || X || Y || Z)$  as the session key, then, computes  $V_i = H(SK_i || H(r_i) || Y)$  and sends  $\{V_i\}$  to  $S_j$ .



**Fig. 3** Login and mutual authentication with key agreement phase

- (6) Upon receiving the message  $\{V_i\}$ ,  $S_j$  checks  $V_i ? = H(SK_s || H(r'_i) || Y)$ . If not,  $S_j$  aborts the procedure, otherwise,  $S_j$  accepts  $SK = h(ID_i || SID_j || H(r_i) || X || Y || Z)$  as the session key for subsequent communications.

### 3.4 Password change phase

A legal user  $U_i$  may for security reasons need to change the old password  $pw_i$ , and then, he/she just needs take the following steps without connecting to  $RC$  or  $S_j$ .

- (1)  $U_i$  inserts his/her smart card  $SC_i$  into a card reader, then inputs  $ID_i, pw_i$  and imprints  $B_i$  at a sensor.
- (2)  $SC_i$  computes  $\sigma_i = Rep(B_i, \theta_i)$ ,  $MP'_i = h(pw_i \parallel \sigma_i)$ ,  $r_i = k_i \oplus MP'_i$ , and checks whether  $v_i = H(ID_i \parallel r_i \parallel MP'_i)$  holds. If not,  $SC_i$  rejects  $U_i$ ; otherwise,  $SC_i$  asks  $U_i$  to input new password  $pw_i^*$ .
- (3) Upon receiving  $pw_i^*$ ,  $SC_i$  computes  $MP_i^* = h(pw_i^* \parallel \sigma_i)$ ,  $k_i^* = k_i \oplus MP_i \oplus MP_i^*$ ,  $v_i^* = H(ID_i \parallel r_i \parallel MP_i^*)$  and replaces  $k_i, v_i$  with  $k_i^*, v_i^*$ , respectively.

### 4 Authentication proof by BAN logic

This section formally proves that our new scheme can achieve mutual authentication with session key agreement by BAN logic [2]. Detailed proof is as follows.

• **BAN logic notations:**

- $P \mid \equiv X$ : The principal  $P$  believes  $X$ .
- $\#(X)$ : The formula  $X$  is fresh.
- $P \Rightarrow X$ :  $P$  has jurisdiction over  $X$ .
- $P \mid \sim X$ :  $P$  once said the statement  $X$ .
- $P \mid \triangleleft X$ :  $P$  sees the statement  $X$ .
- $(X, Y)$ :  $X$  or  $Y$  is one part of the  $(X, Y)$ .
- $\{X\}_K$ :  $X$  is encrypted with the key  $K$ .
- $(X)_K$ :  $X$  is hashed with the key  $K$ .
- $\langle X \rangle_K$ :  $X$  is combined with the key  $K$ .
- $P \xrightarrow{K} Q$ :  $P$  and  $Q$  use the shared session key  $K$  to communicate, and  $K$  will never be discovered by any principal except  $P$  and  $Q$ .

• **BAN logic rules:**

- *Rule(1)*: Message-meaning rule:  $\frac{P \mid \equiv P \xrightarrow{K} Q, P \mid \triangleleft \{X\}_K}{P \mid \equiv Q \mid \sim X}$
- *Rule(2)*: Nonce-verification rule:  $\frac{P \mid \equiv \#(X), P \mid \equiv Q \mid \sim X}{P \mid \equiv Q \mid \equiv X}$
- *Rule(3)*: Jurisdiction rule:  $\frac{P \mid \equiv Q \Rightarrow X, P \mid \equiv Q \mid \equiv X}{P \mid \equiv X}$
- *Rule(4)*: Freshness-conjunction rule:  $\frac{P \mid \equiv \#(X)}{P \mid \equiv \#(X, Y)}$

• **Establishment of security goals:**

- *Goal 1*:  $S_j \mid \equiv U_i \xrightarrow{H(r_i)} S_j$ .
- *Goal 2*:  $U_i \mid \equiv S_j \mid \equiv U_i \xrightarrow{SK_s} S_j$ .
- *Goal 3*:  $U_i \mid \equiv U_i \xrightarrow{SK_s} S_j$ .
- *Goal 4*:  $S_j \mid \equiv U_i \mid \equiv U_i \xrightarrow{SK_i} S_j$ .
- *Goal 5*:  $S_j \mid \equiv U_i \xrightarrow{SK_i} S_j$ .



• **Idealized the proposed scheme**

$$\begin{aligned}
 M_1 (U_i \rightarrow RC) &: \left\{ \{SID_j, ID_i, H(r_i || X || t_1)\}_k, X, t_1 \right\} \\
 M_2 (RC \rightarrow S_j) &: \left\{ \left\{ SID'_j, ID'_i, U_i \xleftrightarrow{H(r_i)} S_j, X, che, t_2 \right\}_{k_j} \right\}, t_2 \\
 M_3 (S_j \rightarrow U_i) &: \left\{ \left( U_i \xleftrightarrow{SK_s} S_j, X, Y, t_3 \right)_{H(r_i)}, Y, t_3 \right\} \\
 M_4 (U_i \rightarrow S_j) &: \left\{ \left( U_i \xleftrightarrow{SK_i} S_j, Y \right)_{H(r_i)} \right\}
 \end{aligned}$$

• **Hypotheses of the proposed scheme**

$$\begin{aligned}
 H_1 &: U_i | \equiv \#(X = \alpha \cdot G) \\
 H_2 &: S_j | \equiv \#(Y = \beta \cdot G) \\
 H_3 &: S_j | \equiv \#(t_2) \\
 H_4 &: U_i | \equiv U_i \xleftrightarrow{H(r_i)} S_j \\
 H_5 &: S_j | \equiv S_j \xleftrightarrow{k_j} RC \\
 H_6 &: S_j | \equiv RC \Rightarrow U_i \xleftrightarrow{H(r_i)} S_j \\
 H_7 &: U_i | \equiv S_j \Rightarrow U_i \xleftrightarrow{SK_s} S_j \\
 H_8 &: S_j | \equiv U_i \Rightarrow U_i \xleftrightarrow{SK_i} S_j
 \end{aligned}$$

• **The proof of our proposed scheme**

– According to  $M_2$ , we have

$$S_1 : S_j \triangleleft \left\{ SID'_j, ID'_i, U_i \xleftrightarrow{H(r_i)} S_j, X, che, t_2 \right\}_{k_j}$$

– According to  $S_1, H_5$  and *Rule(1)*, we have

$$S_2 : S_j | \equiv RC | \sim \left\{ SID'_j, ID'_i, U_i \xleftrightarrow{H(r_i)} S_j, X, che, t_2 \right\}$$

– According to  $S_2, H_3, Rule(4)$  and *Rule(2)*, we have

$$S_3 : S_j | \equiv RC | \equiv \left\{ SID'_j, ID'_i, U_i \xleftrightarrow{H(r_i)} S_j, X, che, t_2 \right\}$$

– According to  $S_3$ , we have

$$S_4 : S_j | \equiv RC | \equiv U_i \xleftrightarrow{H(r_i)} S_j$$

- According to  $S_4$ ,  $H_6$  and *Rule(3)*, we have

$$S_5 : S_j | \equiv U_i \xleftrightarrow{H(r_i)} S_j \quad (\mathbf{Goal\ 1})$$

- According to  $M_3$ , we have

$$S_6 : U_i \triangleleft \left( U_i \xleftrightarrow{SK_s} S_j, X, Y, t_3 \right)_{H(r_i)}$$

- According to  $S_6$ ,  $H_4$  and *Rule(1)*, we have

$$S_7 : U_i | \equiv S_j | \sim \left( U_i \xleftrightarrow{SK_s} S_j, X, Y, t_3 \right)$$

- According to  $H_1$ , *Rule(4)*,  $S_7$  and *Rule(2)*, we have

$$S_8 : U_i | \equiv S_j | \equiv \left( U_i \xleftrightarrow{SK_s} S_j, X, Y, t_3 \right)$$

- According to  $S_8$ , we have

$$S_9 : U_i | \equiv S_j | \equiv U_i \xleftrightarrow{SK_s} S_j \quad (\mathbf{Goal\ 2})$$

- According to  $H_7$ ,  $S_9$  and *Rule(3)*, we have

$$S_{10} : U_i | \equiv U_i \xleftrightarrow{SK_s} S_j \quad (\mathbf{Goal\ 3})$$

- According to  $M_4$ , we have

$$S_{11} : S_j \triangleleft \left( U_i \xleftrightarrow{SK_i} S_j, Y \right)_{H(r_i)}$$

- According to  $S_5$ ,  $S_{11}$  and *Rule(1)*, we have

$$S_{12} : S_j | \equiv U_i | \sim \left( U_i \xleftrightarrow{SK_i} S_j, Y \right)$$

- According to  $H_2$ , *Rule(4)*,  $S_{12}$  and *Rule(2)*, we have

$$S_{13} : S_j | \equiv U_i | \equiv \left( U_i \xleftrightarrow{SK_i} S_j, Y \right)$$

- According to  $S_{13}$ , we have

$$S_{14} : S_j | \equiv U_i | \equiv U_i \xleftrightarrow{SK_i} S_j \quad (\mathbf{Goal\ 4})$$

- According to  $H_8$ ,  $S_{14}$  and *Rule(3)*, we have

$$S_{15} : S_j | \equiv U_i \xleftrightarrow{SK_i} S_j \quad (\mathbf{Goal\ 5})$$

## 5 Security analysis

This section demonstrates how our scheme accomplishes perfect security requirements and resists all well known attacks in the heuristic way. Detailed analysis is as follows.

### 5.1 Perfect forward secrecy

The negotiated session key is  $SK = h(ID_i \| SID_j \| H(r_i) \| X \| Y \| Z)$  in our scheme, where  $X = \alpha \cdot G$ ,  $Y = \beta \cdot G$ ,  $Z = \alpha\beta \cdot G$ ,  $\alpha$  and  $\beta$  are randomly generated in every session by  $U_i$  and  $S_j$  respectively. If an adversary  $A$  tries to derive  $\alpha$  and  $\beta$  by  $X = \alpha \cdot G$  and  $Y = \beta \cdot G$ , then  $A$  has to resolve the ECDLP, which is well-known impossible. Meanwhile, the session key  $SK$  is obviously independent of the system private key  $x$ , so even if  $x$  is leaked to  $A$ , he/she cannot get any information about the former established session keys. Thus, our scheme provides perfect forward secrecy.

### 5.2 User anonymity

In our scheme,  $U_i$ 's original identity  $ID_i$  together with other parameters are first encrypted by  $k$  and transmitted to  $RC$ , where  $k = h(K)$  and  $K = \alpha \cdot P_{pub}$  are dynamic for that  $\alpha$  is randomly generated in every session. Then, the  $ID_i$  is encrypted by  $RC$  with the shared secret key  $k_j = h(SID_j \| x \| r_j)$  between  $RC$  and  $S_j$ , and the cipher text is transmitted to  $S_j$ . For an adversary  $A$ , if he/she wants to derive  $ID_i$ , then he/she has to get  $K$  or  $k_j$ , which further requires him/her to get the system private key  $x$  or solve the ECDLP ( $X = \alpha \cdot G$ ) to obtain  $\alpha$ . Obviously, that is impossible. So, our scheme preserves user anonymity.

### 5.3 Impersonation attack

In our scheme, a patient  $U_i$  must be first authenticated by  $RC$  before accessing to  $S_j$ , so if an adversary  $A$  wants to impersonate  $U_i$ , he/she has to pass the verification test performed by  $RC$ . Thus,  $A$  must try to compute  $r_i = h(ID_i \| x)$ , which requires  $A$  to obtain  $U_i$ 's  $ID_i$  and the system private key  $x$  at the same time. Obviously, that is impossible. Another way to deceive  $RC$  is to obtain  $U_i$ 's  $ID_i$ ,  $pw_i$ , biometrics  $B_i$ , and smart-card  $SC_i$  simultaneously, which is also obviously impossible. Analogously, for an illegal  $S_j$ , without the secret  $k_j$ , it cannot get the parameter  $H(r'_i)$ , and thus it cannot forge the valid message  $V_j = H(SK_s \| H(r'_i) \| X \| Y \| t_3)$  to deceive  $U_i$ . So, the impersonation attack is infeasible in our scheme.

### 5.4 Replay attack

A legal user  $U_i$ 's previous login message  $\{c_1, X, t_1\}$  may be intercepted by an adversary  $A$ , then  $A$  may try to replay the old message to  $RC$ , but  $RC$  will reject  $A$  for  $t'_1 - t_1 > \Delta t$  will hold. Further,  $A$  may modify the timestamp  $t_1$  to satisfy the condition  $t'_1 - t_1 < \Delta t$ , but  $RC$  will also reject  $A$  for the validation equation  $H'(r_i \| X \| t_1) \neq H(r'_i \| X \| t_1)$  embedded with the original timestamp  $t_1$ . If  $t_1$  is modified,  $H'(r_i \| X \| t_1) \neq H(r'_i \| X \| t_1)$  will hold, then  $RC$  will reject  $A$ . Analogously,  $A$  cannot replay the old messages exchanged between  $RC/U_i$  and  $S_j$  to deceive the participants. So, the replay attack is infeasible in our scheme.

### 5.5 Man-in-the-middle attack

For an adversary  $A$  to perform the man-in-the-middle attack, he/she needs to establish independent connections with the legal participants and replay messages between them, making them mistaken that they are talking directly to each other. Thus,  $A$  needs to successfully deceive  $U_i$  and  $S_j$  at the same time, which further requires  $A$  to obtain  $H(r_i) = H(h(ID_i \| x))$  or  $k_j = h(SID_j \| x \| r_j)$ , and then  $A$  has to get the system private key  $x$ , which is obviously impossible. So, the man-in-the-middle attack is infeasible in our scheme.

### 5.6 Stolen-verifier attack

In our scheme,  $RC$  just stores  $h(ID_i)$  which is useless to an adversary  $A$ , moreover,  $RC$  and  $S_j$  don't store  $U_i$ 's  $pw_i$  and biometrics  $B_i$  at all. Thus, even if  $A$  breaks into  $RC$  or  $S_j$ , there are no useful authentication credentials for him/her to steal. So, the stolen-verifier attack is infeasible in our scheme.

### 5.7 Privileged insider attack

In our scheme,  $U_i$ 's password  $pw_i$  and biometrics  $B_i$  never leave the user side, and only in the registration phase does  $U_i$  send  $MP_i = h(pw_i \| \sigma_i)$  to  $RC$ , which is embedded with his/her password  $pw_i$ . It is obvious that the password  $pw_i$  is protected by one-way hash function with the random string  $\sigma_i$  derived by  $(\sigma_i, \theta_i) = Gen(B_i)$ . Thus, it is impossible for an insider to get  $U_i$ 's password  $pw_i$  and biometrics  $B_i$  throughout our scheme. So, the privileged insider attack is infeasible in our scheme.

### 5.8 Denial of service attack

In our scheme, before launching the login message, the legality of a user  $U_i$  is first verified by the smart-card  $SC_i$  by checking whether  $v_i = H(ID_i \| r_i \| MP_i')$  holds, where  $r_i = k_i \oplus MP_i$ ,  $MP_i' = h(pw_i \| \sigma_i)$ ,  $\sigma_i = Rep(B_i, \theta_i)$ . If not,  $SC_i$  will directly reject  $U_i$ . In other words, only when  $U_i$  is first authenticated by  $SC_i$  locally, the login message is sent to  $RC$ . Besides, there is no information needed to be synchronized for  $SC_i$ ,  $S_j$  and  $RC$  in each session. So, the denial of service attack is infeasible in our scheme.

### 5.9 Offline password guessing attack

Suppose that an adversary  $A$  has got  $U_i$ 's smart-card  $SC_i$  by some means, and extracted the stored parameters  $k_i$ ,  $v_i$  and  $\theta_i$  from  $SC_i$  by side-channel attacks, then, to guess  $U_i$ 's password  $pw_i$  by the equation  $v_i = H(ID_i \| r_i \| MP_i)$ , where  $MP_i = h(pw_i \| \sigma_i)$ ,  $A$  has to obtain  $U_i$ 's biometrics  $B_i$  to compute  $\sigma_i$  by  $\sigma_i = Rep(B_i, \theta_i)$ , which is almost impossible. So, the offline password guessing attack is infeasible in our scheme.

## 6 Performance evaluation

We've chosen the recent biometrics based authentication schemes [1, 10] for comparison since they have the same technology backgrounds with our scheme, i.e. all are biometrics based

**Table 2** Security comparison

	Scheme		
	[10]	[1]	Our
Authentication with session key agreement	✓	✓	✓
Perfect forward secrecy	✓	✓	✓
User anonymity	✓	✓	✓
Impersonation attack resistance	✗	✗	✓
Replay attack resistance	✓	✓	✓
Man-in-the-middle attack resistance	✓	✓	✓
Stolen-verifier attack resistance	✓	✓	✓
Privileged insider attack resistance	✓	✓	✓
Denial of service attack resistance	✗	✓	✓
Offline password guessing attack resistance	✓	✗	✓

using ECC as the cryptographic foundation. Moreover both the schemes were designed for generic multi-server environments rather than a specific application environment, which are consistent with ours from the design goal. So, this section compares our proposed scheme with them in security, computation and communication costs aspects. Table 2 shows these schemes’ abilities to resist the identified attacks, which signifies the robustness of our proposed scheme over the others. To conveniently evaluate our scheme with other relevant schemes in the aspects of computation and communication costs, we assume that the length of identity, timestamp, hash digest and an elliptic curve point are 64, 64, 160 and 320 bits respectively, and use the following notations to depict time complexities of different operations:

- $T_m$ : the time for executing elliptic curve scalar point multiplication
- $T_s$ : the time for executing symmetric encryption/decryption operation
- $T_h$ : the time for executing hash function
- $T_G$ : the time for executing the fuzzy extractor operation  $Gen$

According to the experimental results of Kilinc and Yanik [14],  $T_m$ ,  $T_s$  and  $T_h$  approximately take 2.226, 0.0046 and 0.0023 ms respectively. And we here assume that the time complexity of  $Gen(\cdot)$  is the same with the elliptic curve scalar point multiplication. Then, the detailed comparison of the computation and communication costs of registration phase and

**Table 3** Computation and communication costs comparison of the registration phase

scheme	User registration		Server registration	
	$U_i$	$RC$	$S$	$RC$
Computation cost:				
[10]	$T_G$	$2T_h$	–	$T_h$
[1]	–	$T_m + 2T_h$	–	$T_h$
Our	$T_G + T_h$	$2T_h$	–	$T_h$
Communication cost:				
[10]	224 bits		224 bits	
[1]	288 bits		224 bits	
Our	224 bits		224 bits	

**Table 4** Computation and communication costs comparison of the AKA phase

	Scheme		
	[10]	[1]	Our
Computation cost:			
$U_i$	$3T_m + 7T_h$	$4T_m + 1T_s + 7T_h$	$3T_m + 1T_s + 7T_h$
$S_j$	$3T_m + 5T_h$	$4T_m + 2T_s + 5T_h$	$2T_m + 1T_s + 3T_h$
$RC$	$2T_m + 9T_h$	$3T_m + 1T_s + 6T_h$	$1T_m + 2T_s + 6T_h$
Total cost	$8T_m + 21T_h$	$11T_m + 4T_s + 18T_h$	$6T_m + 4T_s + 16T_h$
Execution time	17.856 ms	24.546 ms	13.411 ms
Communication cost:	3520 bits	1792 bits	1408 bits

authentication with key agreement (AKA) phase between our scheme and the others are demonstrated in Tables 3 and 4. According to Table 3, we can see that the computation and communication costs of registration phase are almost the same in all schemes. According to Table 4, our proposed scheme consumes the lowest computation cost of 13.411 ms and communication cost of 1408 bits in the AKA phase, while the scheme [10] bears the average computation cost of 17.856 ms and communication cost of 3520 bits, and the scheme [1] bears the average computation cost of 24.546 ms and communication cost of 1792 bits. So, in the light of the fact demonstrated in Tables 2, 3 and 4, it can be concluded that our new scheme has advantages over the others, whether in terms of security and functionalities or computation and communication costs.

## 7 Conclusions

This work presents our biometrics-based mutual authentication with session key agreement scheme for multi-server environment. The security analysis demonstrates that our scheme has perfect security features and can resist various known attacks. The performance evaluation shows that our new scheme is more efficient in the aspects of computation cost and communication cost, for the  $RC$  no longer participates in the subsequent user-server session key negotiation processes after it authenticates the user, and thus reducing the computation and communication costs. Hence, it can be said that our new scheme is a more suitable authentication key exchange protocol for multi-server environment.

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