



# Measurements of specific heat capacity of common building materials at elevated temperatures: a comparison of DSC and HDA

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## Abstract

The objective of this study is to investigate how the specific heat capacity ( $c_p$ ) value of a material changes with respect to temperature and heating rate of that material. In-depth knowledge in the variation of  $c_p$  will provide a better knowledge of the thermo-physical properties of these materials and will increase the capabilities and fidelity of computational fluid dynamics (CFD)-based fire modelling. The models and simulations are reliant on input data gained through experimentation and this allows for the present study to provide such input data and trends, which are useful in understanding how fires respond in different situations. The value of  $c_p$  in relation to the rate of temperature change has been measured using differential scanning calorimetry (DSC) and hot disk analysis (HDA). This study encapsulates the determination of  $c_p$  values, trends and equations for poly(methyl methacrylate), pinewood, pinewood char, and two fabrics: cotton and wool. The  $c_p$  values were found to increase with the sample temperature and for the two fabrics; they vary with the change in heating rate. The derived equations show that  $c_p$  values from DSC and HDA are comparable. To include these relationships in CFD-based fire models, a set of suggestions have been made.

**Keywords** DSC · Hot disk analyser · Specific heat capacity · PMMA · Pinewood · Fabric

## List of symbols

$\beta_s$	Heating rate ( $\text{K min}^{-1}$ )
$C$	Specific heat ( $\text{J g}^{-1} \text{K}^{-1}$ )
$c_p$	Specific heat capacity ( $\text{J g}^{-1} \text{K}^{-1}$ )
$c_{p,a}$	Apparent Specific heat capacity ( $\text{J g}^{-1} \text{K}^{-1}$ )
$c_r$	Specific heat capacity of reference sample ( $\text{J g}^{-1} \text{K}^{-1}$ )
$\frac{dH}{dt}$	Heat flow to the sample (mW)
$\frac{dH_r}{dt}$	Heat flow to the reference material (mW)
$H$	Enthalpy (J)
$m$	Mass (g)
$m_o$	Sample mass (g)
$m_r$	Reference mass (g)

$p$	Pressure constant
$Q$	Heat flow (J)
$\Delta Q$	Change in heat flow (mW)
$T$	Temperature ( $^{\circ}\text{C}$ or K)
$\Delta T$	Change in temperature ( $^{\circ}\text{C}$ or K)

## Introduction

Fire models and simulations are much more cost-effective in determining important factors that contribute to fire behaviour, prevention, suppression and control. Full and medium-scale experimentation in compartment fire testing, however, is cost prohibitive. This constraint therefore requires the use of numerical fire modelling which needs input parameters from a controlled miniature and/or bench-scale testing environment to gather fundamental experimental data. It is imperative that the data from experimental testing and analysis are able to validate models of fire behaviour [1]. More accurate predictions of fire can lead to a better understanding of the associated fire risk and reliable fire prevention and systems can be implemented to reduce the risk. This is economically beneficial for insurers, building owners and clients, who would

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benefit from a reduction in fire damage subsequently reducing the cost of a fire incidence.

Poly(methyl methacrylate) (PMMA), pinewood, cotton and wool are some of the common materials that are used throughout the building and manufacturing industry. These materials have a wide range of uses and are found in diverse environments in which they are typically clustered. In instances where these materials are exposed to a fire situation, the surrounding temperature varies as the fire grows or declines and the materials can be heated with different heating rates. With regard to the heating rate of the material, the accurate measurement of specific heat capacity ( $c_p$ ), among other thermo-physical and flammability parameters, is required for input values for computational fluid dynamics (CFD)-based fire models such as fire dynamic simulation (FDS) [2] to improve fidelity. A variation in heating rate is known to have an effect on the thermo-physical properties of different materials [3, 4], and  $c_p$  has an influence on many thermo-physical processes that occur during a fire including ignition point, phase change and chemical interactions during pyrolysis. The  $c_p$  value is useful when determining regions of thermal activation, volatilization and pyrolysis; therefore, studies are needed to focus on estimating  $c_p$  of the materials. In CFD-based fire simulations, it is crucial that accurate input values are used including variations in terms of temperature, heating rate, heat flux, etc. [5]. Small scale testing can be used to accurately determine the  $c_p$  value of the materials as a prerequisite for simulation but also to verify if these simulations are predictive of large fires [6].

The  $c_p$  value can be determined using numerous methods with varying degrees of accuracy and sources of errors with different calorimetry instruments [7] including the differential scanning calorimeter (DSC) and hot disk analyser (HDA) apparatus. These instruments can provide a range of thermo-physical data for a wide range of materials and are readily commercially available. The DSC can provide quantitative and qualitative data on transitions of materials with temperature, heating rate, degradation environment and can be used to estimate  $c_p$ , thermal conductivity ( $k$ ), latent heat, transition temperature and enthalpy [4, 7]. However, the DSC requires significant effort in post-processing the raw data to obtain  $c_p$  and  $k$  values. Moreover, the thermal behaviour of the material studied is normally compared with a reference material such as sapphire making the process time-consuming and expensive. The HDA instrument can be used to determine the thermal diffusivity,  $k$  and  $c_p$  and its companion software provides these values readily. The primary variance between the two instruments is that the DSC gives  $c_p$  as a function of both heating rate and temperature, whereas the HDA provides the data as a function of temperature only. Differential thermal analysis (DTA) is another technique closely related to the

DSC; however, the DSC can provide greater accuracy and is the preferred method of determining  $c_p$  [8].

Although literature exists on the effect of temperature on PMMA and various species of pinewood, there are few reports of the effect of heating rate on pinewood char, cotton and wool [9]. Goodrich [9] observed that there are substantial difficulties with materials of a similar nature to cotton and wool which may account for the lack of conclusive research in this particular area.

For some materials, especially those undergoing endothermic reactions, heating rates higher than  $5 \text{ K min}^{-1}$  are recommended for thermal analysis [10] and are considered to be macroscopic heating rates. Therefore, in the present study,  $c_p$  was measured as a function of the rate of temperature change for heating rates of 50, 100 and  $200 \text{ K min}^{-1}$  with these high heating rates likely to occur in building fires. Using DSC measurements, raw data were obtained using the sapphire method [11] and  $c_p$  was calculated using post-processing in MATLAB. Using the same materials, experiments using HDA equipment were performed where the sample was heated in an oven until a thermocouple attached to the sample showed that it reached the desired temperature then the  $c_p$  value was measured at that temperature. The data from both sets of apparatus were used to develop possible equations for use in fire engineering applications and also within fire modelling algorithms.

## Materials and methods

### Concept of specific heat capacity determination using DSC

$c_p$  is the amount of thermal energy (J) that is required to change the temperature of 1 g of material by 1 K at constant pressure and expressed in  $\text{J g}^{-1} \text{ K}^{-1}$ . Thermodynamically,  $c_p$  is determined by the equation:

$$c_p = \left( \frac{\partial H}{\partial T} \right)_p \quad (1)$$

where  $H$  is enthalpy;  $T$  is temperature of the system;  $p$  is the pressure constant.

The derivation of  $c_p$  can also be expressed as:

$$c_p = \frac{\delta Q}{dT} \cdot \frac{1}{m} \quad (2)$$

where  $Q$  is heat;  $m$  is mass. The amount of energy or heat that is exchanged for the change in temperature from  $T_1$  to  $T_2$  for a given mass  $m$  and specific heat  $c_p(T)$  is determined by the equation:

$$Q = m \int_{T_1}^{T_2} c_p(T) dt \quad (3)$$

The characteristic equation that is used to determine the  $c_p$  from DSC is:

$$c_p = \frac{\Delta Q}{\Delta T} \quad (4)$$

Equation (4) can be utilized using the DSC curves of the heat flow and physical quantity.

Taking into account the heating rate,  $c_p$  can be calculated using the following formula:

$$c_p = \frac{1}{m_o \cdot \beta_s} \cdot \frac{dH}{dt} \quad (5)$$

where  $\beta_s$  is the heating rate of the sample;  $m_o$  is the sample mass;  $\frac{dH}{dt}$  is the blank curve corrected heat flow to the sample. The sample is required to be stable throughout the heating range in order to determine the specific heat.

Depending on the method used to determine  $c_p$ , if a sample or known reference material is used, then  $c_p$  is calculated by:

$$c_p = \frac{m_r}{m_o} \cdot \frac{dH/dt}{dH_r/dt} \cdot c_r \quad (6)$$

where  $m_r$  is the reference mass;  $c_r$  is the specific heat capacity of the reference mass;  $\frac{dH_r}{dt}$  is the heat flow of the reference. The temperature range for this study was selected up to which no thermal degradation (mass loss) occurs in order to avoid a mass correction for the evaluation of the  $c_p$ . Thermogravimetric analysis data from a previous study [12] and a concurrent study [13] show that PMMA, pine and cotton have minimal mass loss up to 300 °C and for wool up to 275 °C. Therefore, only results up to these regions are evaluated.

The concept and experimental technique to obtain HDA data can be found in [5, 12]. It should be noted that HDA does not require calibration since the Kapton sensor infused with nickel wire is calibrated by the manufacturer. The data affected by the contact sensor resistance lie in the nonlinear region at the start of the experiment and is thus automatically removed from the calculation of material properties [14]. The following sections describe the DSC method for obtaining the  $c_p$ .

## Obtaining $c_p$ using DSC

### Sample preparation

The samples of PMMA were crushed into small granules approximately 1 mm<sup>2</sup> or smaller. Pinewood dust and parings of approximately 0.6–1 mm<sup>2</sup> were used. The cotton and wool samples were cut into small fragments ranging between 0.5 and 1.2 mm<sup>2</sup>. Sample masses between 1.3 and 4.2 mg were used to ensure that the DSC could obtain a suitable

measurement signal. The sample weights also ensured the crucibles were not over filled which potentially could have hindered the measurement of heat flow. Aluminium crucibles of 40 µL capacity were used in a Mettler Toledo DSC instrument [15]. Weighing errors were minimized with the use of a microbalance. Additionally, samples were reweighed when consistency between samples varied. The samples were placed in a conditioning unit prior to being encapsulated in the crucibles to reduce the moisture content in the materials, and also to verify the affect that moisture content has on materials when determining  $c_p$ . The relative humidity of the conditioning unit where the samples were kept was approximately 50% at 23 °C.

### Experimental/operating procedure

The DSC instrument was fully calibrated by the indium standard prior to sample measurements [16]. During the measurement, an inert atmosphere was created under a nitrogen flow of 50 mL min<sup>-1</sup>. This represents an atmosphere in the absence of air which occurs during flaming combustion thus preventing air reaching the burning material. The sapphire method for  $c_p$  determination was used as this method produces an accuracy that is within ± 2% [10, 12]. This method has been experimentally noted to have a variation of ± 5% for the value of sapphire material [17].

A “baseline” or blank measurement was performed for each heating rate (50, 100 and 200 K min<sup>-1</sup>) in order to determine the signal bias in the system. This was obtained by determining the response of both crucibles when empty and allows for the signal bias to be removed from the data. A reference test for each heating rate was performed to ascertain the difference between the sapphire reference material with well-defined known specific heat values and the experimental sample. All of the results obtained were blank curve corrected and performed in triplicate.

There are two predominant methods of sealing the sample crucibles, namely without lid pinholes [4, 18], and with pinhole pierced lids [19]. Rath et al. [20] compared the use of an open pan and one with a lid pinhole and found that the presence of the lid affected both the heat flow and exothermic thermal effect of the sample. Other studies have also shown the effect of heating rate on samples and also the uncertainty of the results from DSC [4, 21, 22]. From these studies, it appears that the pinhole lid has a minimal effect depending on whether gasses are released from the sample during the heating process. The test material and the reference were placed into individual aluminium crucibles which were then sealed with pierced lids. The data from the DSC were recorded and then analysed using MATLAB in order to obtain the  $c_p$  from the data. Taking into account the uncertainty of sample mass, variations between samples and

DSC accuracy [21, 23], the standard error was estimated to be  $\pm 3\text{--}5\%$ .

## Results and discussion

With all four materials, we either observe moisture evaporation or phase transition (such as melting) or both. Such physical phenomenon involves enthalpy changes which are not part of the specific heat capacity. In the literature [24], a combination of the specific heat capacity and additional enthalpy changes are described as “apparent specific heat capacity” and herein we have used  $c_{p,a}$  and have plotted “apparent specific heat capacity” in Figs. 1–7. However, the equations of  $c_p$  were determined from data and trends of the experimental data excluding enthalpy changes. The equation type has been selected for fire engineering purposes and CFD-based fire modelling simulations. Fire engineering has been emphasized over computer simulations, as fire engineers are more reliant on desktop computational methods since they typically do not have access to extensive experimental data resources and simulation computation. This has therefore limited the calculations to linear and polynomial equations.

### PMMA

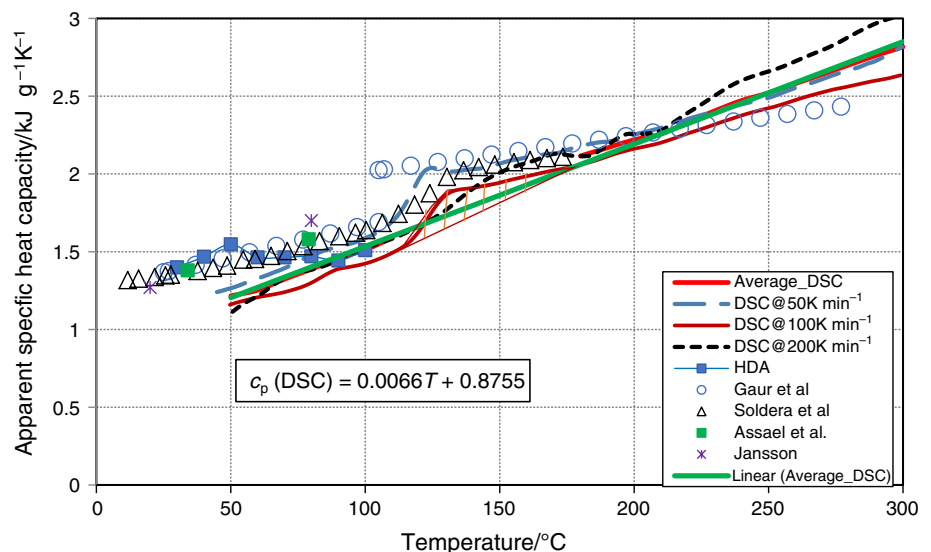
Figure 1 shows the  $c_{p,a}$  of PMMA tested between 25 and 300 °C at different heating rates between 50 and 200 K min<sup>-1</sup>. However, the data below 70 °C for 200 K min<sup>-1</sup> and 45 °C for 100 K min<sup>-1</sup> are excluded due to uncertainty in the initial measurement.

It can be observed that between 120 and 145 °C, there is a peak in all  $c_{p,a}$ —temperature profiles which is an indication of transition from a solid state to a molten state. As an example, the phase transition enthalpy for 100 K min<sup>-1</sup> profile is shown by the hatched pattern and this shows the difference between the specific heat capacity and the apparent specific heat capacity. This transition was also observed by Gaur et al. [25] and Soldera et al. [26] as shown in Fig. 1. For this reason, the  $c_p$  values are obtained using HDA up to 100 °C as the equipment is only designed to obtain the data from a solid state where no phase change of material or significant degradation of material takes place. The  $c_p$  values from HDA are also plotted in Fig. 1 and the data between two apparatus are markedly comparable. The  $c_p$  values from the DSC (excluding phase transition range) have been averaged as the heating rates ranged from 50 to 200 K min<sup>-1</sup> and the averaged profile is presented in Fig. 1. Undertaking a least squares analysis, we obtain a relationship presented as Eq. (7), where  $T$  is in °C:

$$c_p(\text{DSC}) = 0.0066T + 0.8755 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 1.0) \quad (7)$$

This equation follows the  $c_p$  profile obtained for 200 K min<sup>-1</sup> prior to melting, and after melting, the equation follows the  $c_p$  profile obtained for 50 K min<sup>-1</sup>. Both HDA data and Eq. (7) (averaged  $c_p$  from DSC) are compared with other literature studies. Data from Assael et al. [27] and Jansson [28] show linear relationships, and their values are close to the values obtained in the current study. Prior to and after melting, linear relationships are also observed by Gaur et al. [25] and Soldera et al. [26]. Overall literature values are close to those in the current study.

**Fig. 1** Apparent specific heat capacity variance of PMMA. The hatched pattern shows exemplar phase transition enthalpy as well as the difference between the specific heat capacity and the apparent specific heat capacity



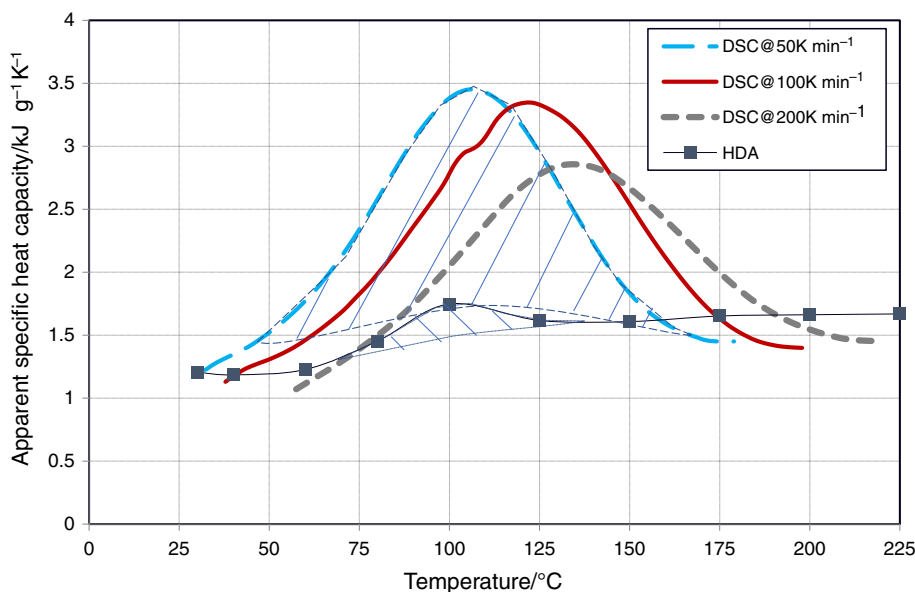
### Pinewood: virgin and char

Figures 2 and 3 show the  $c_{p,a}$  values of virgin pinewood. A peak bordering 100 °C in the HDA data represents a moisture affected region with similar peaks more pronounced in the DSC data. At lower heating rates, the peaks are higher although they occur over a smaller temperature range. As the water evaporates at 100 °C, we can assume that these regions are affected by moisture content and its evaporation. Figure 2 shows that this region is affected by evaporation which ends between 170 °C at a heating rate of 50 K min<sup>-1</sup> (moisture evaporation enthalpy is shown by hatched pattern) and 217 °C at a heating rate of 200 K min<sup>-1</sup> for the data

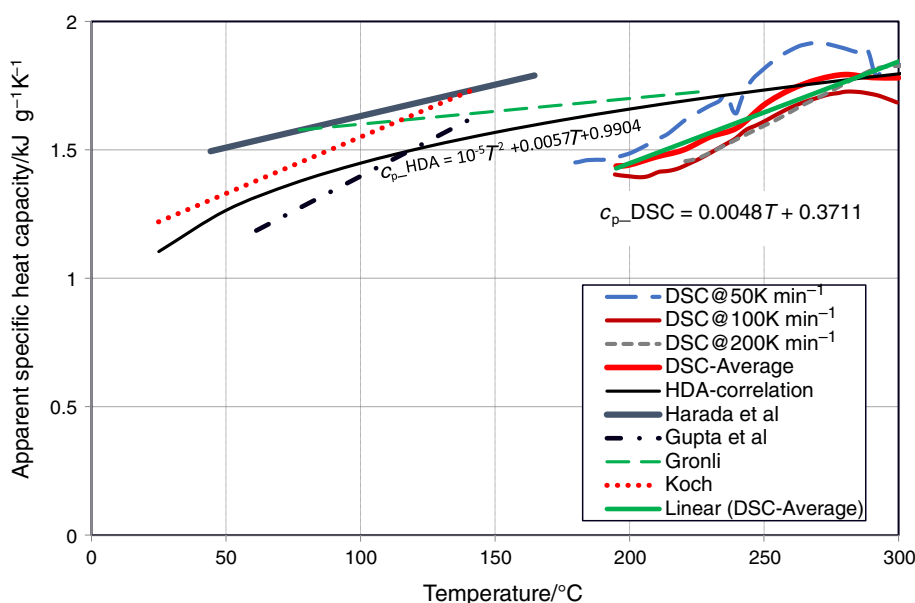
obtained using the DSC. Above these temperatures, the  $c_p$  value increases with temperature.

In Fig. 3, data beyond the moisture affected region is represented up to 300 °C. The  $c_p$  value changes with the rate of heating are apparent within one thermal set, comprising data of 50–200 K min<sup>-1</sup>. The values in 100 and 200 K min<sup>-1</sup> are close to each other in relative terms, and the values of 50 K min<sup>-1</sup> are higher which may be due to the effect of thermal transport. The sudden drop at 240 °C for the data obtained at 50 K min<sup>-1</sup> can be attributed to pressure from vapour being released from the timber causing the seal and pinhole on the crucible lid to widen. This sudden endothermic peak in the data accounts for the shape of the graph.

**Fig. 2** Apparent specific heat capacity variance of pinewood (moisture influenced region). The hatched pattern shows exemplar moisture evaporation enthalpy



**Fig. 3** Apparent specific heat capacity without moisture evaporation region of pinewood





In Fig. 3, literature data [29–32] from dry wood are also presented although it should be noted that Gupta et al. [29] used a DSC to measure the  $c_p$  at 5 K min<sup>-1</sup> heating rate. Moreover, the literature data [29–31] are only reported up to 140 °C, whereas the current study values are extended to 300 °C. From 160 to 300 °C, the  $c_p$  values from the DSC have been averaged (without endothermic data) with the profile presented in Fig. 3 and a relationship presented as Eq. (8) is obtained undertaking a least squares analysis, where  $T$  is in °C:

$$c_p(\text{DSC}) = 0.004T + 0.6554 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.94) \quad (8)$$

Equation (9) can be derived from the HDA data (excluding the data within the moisture affected region) [5], where  $T$  is in °C:

$$c_p(\text{HDA}) = -10^{-5} + 0.0057T + 0.9904 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.98) \quad (9)$$

The DSC data could not be compared with the literature data since up to 170 °C, the data are moisture affected. Yet, the HDA appears to be comparable with the literature data giving us confidence in our experimental procedure. Literature values show similar trends that conform to the current data given for different species of timber. They show the values at lower temperature ranges that are not affected by the moisture evaporation region and can be attributed to using completely dry wood for experiments. It should be noted that a diverse range of timbers exist and that even variation exists within the same species of timber.

Figure 4 shows the  $c_{p,a}$  of pinewood char tested where the samples were superfluous from larger scale testing. The time taken between testing allowed moisture to penetrate the samples by the time DSC tests were conducted and this is observed

in the results obtained. The enthalpy change in the moisture affected region can be observed in Fig. 4 for the DSC experiments. Moisture evaporation enthalpy for the 50 K.min<sup>-1</sup> profile, as an example, is shown as hatched pattern which can be considered the difference between the specific heat capacity and the apparent specific heat capacity. Since the HDA data are not affected by moisture, this data shows an overall increase in  $c_p$  with increasing temperature with the data from either side of the moisture region presented in Fig. 4.

Increasing linear relationships with temperature proposed by Gupta et al. [29], Gronli et al. [31] and Koufopoulos et al. [33] are presented in Fig. 5 along with the current study data (moisture affected DSC data are excluded). At the lower end of the temperature range, the data from the aforementioned studies show that values that are comparable to the HDA data of flat-pine char obtained are more aligned with the literature data. From the HDA data, Eqs. (10–11) were derived [5], where  $T$  is in °C:

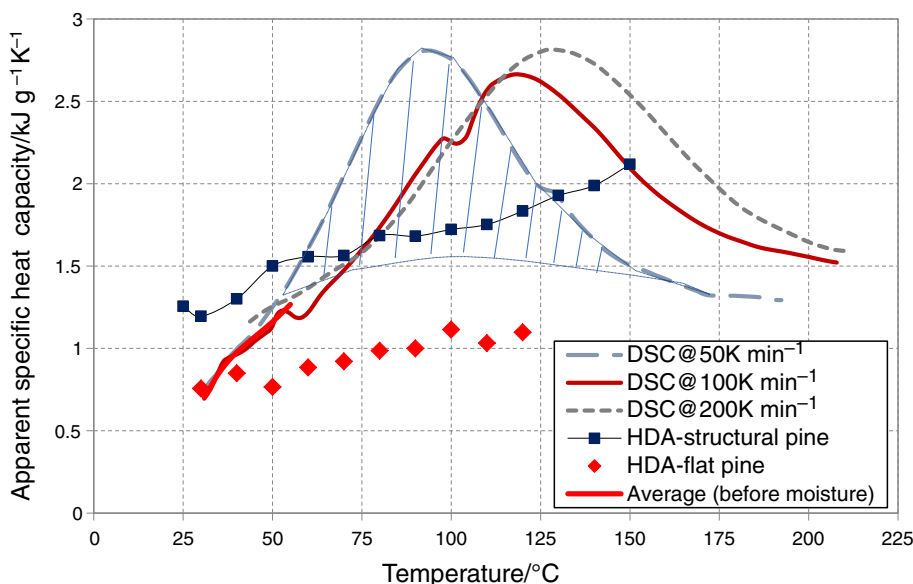
$$\begin{aligned} \text{Structural pine } c_p(\text{HDA}) &= 0.00655 T \\ &+ 1.0897 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.96) \end{aligned} \quad (10)$$

$$\text{Flat pine } c_p(\text{HDA}) = 0.00394T + 0.6456 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.83) \quad (11)$$

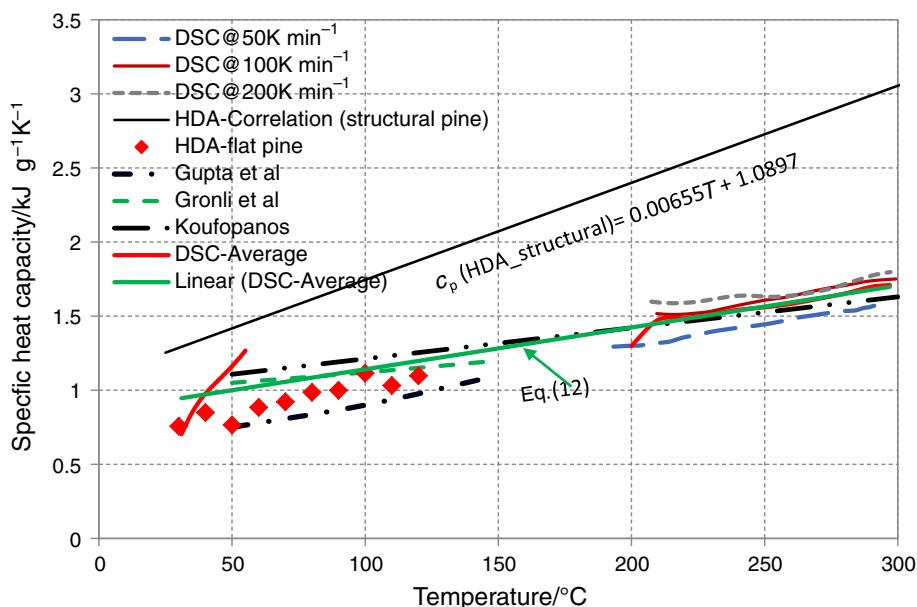
The DSC data show that between 50 and 200 K min<sup>-1</sup>, the effect of heating rate (thermal transport) on  $c_p$  is not significant. The empirical relations that were observed between temperature and  $c_p$  outside the area affected by moisture evaporation are presented in Fig. 5 with Eq. (12) determined:

$$c_p = 0.0028 T + 0.8587 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.88) \quad (12)$$

**Fig. 4** Variation of  $c_{p,a}$  (DSC data) and  $c_p$  (HDA data) with temperature for pine char. The hatched pattern shows exemplar moisture evaporation enthalpy



**Fig. 5** Variation in  $c_p$  for pinewood char excluding the moisture affected region



Extrapolation of the data obtained by Koufopoulos et al. [33] and Gupta et al. [29] shows consistency with the DSC data of the present study. In this case, the data of Koufopoulos et al. [33] run almost equivalent with Eq. (12).

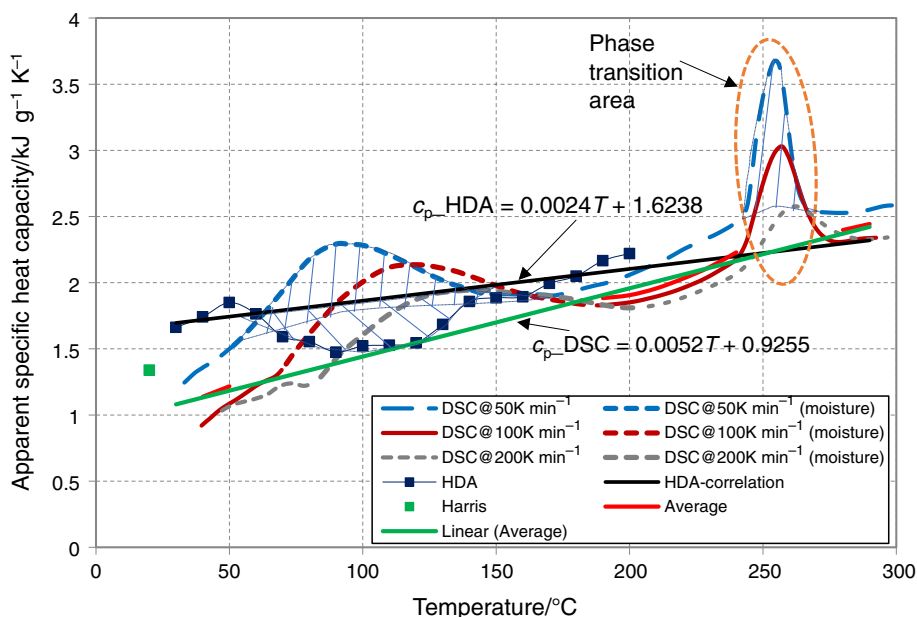
**Cotton and wool fabrics**

Figure 6 shows variation in the  $c_{p,a}$  for cotton and similar to pinewood, the moisture content results in enthalpy change in the vicinity of 100 °C. The region of moisture evaporation can be observed in Fig. 6, though this is a subtle representation. The sudden spike in  $c_p$  values observed at around 260 °C for all heating rates can be attributed to the phase

transition occurring in the cellulose structures within the cotton [34]. In all cases, this is a significant but not unexpected spike since the cellulose content of cotton is around 90% [35]. As an example, moisture evaporation and phase transition enthalpy for 50 K min<sup>-1</sup> profile are shown as hatched patterns and these show the difference between the specific heat capacity and the apparent specific heat capacity.

The HDA data are also plotted in Fig. 6 and a steadily increasing trend in the  $c_p$  is observed after the moisture evaporation region (hatched pattern) was removed. The HDA data generally conform to the same characteristic trend present for the DSC with  $c_p$  values that are comparable. A literature value for cotton from Harris [36] at lower

**Fig. 6** Variation of apparent specific heat capacity for cotton. The hatched pattern shows exemplar moisture evaporation and phase transition enthalpy as well as the difference between the specific heat capacity and the apparent specific heat capacity



temperature is presented in Fig. 6 which falls slightly above the range of the DSC values, but below HDA, for values at the lowest temperatures presented.

To obtain a quantitative trend, the data related to the moisture evaporation and phase transition regions were removed. Then, from 40 to 290 °C, the  $c_p$  values from the DSC have been averaged for the heating rates 50–200 K min<sup>-1</sup>. It can be observed that the  $c_p$ –temperature profiles from these three heating rates are close to each other implying that the effect of thermal transport is not significant. This averaged profile is also presented in Fig. 6 and Eq. (13) [where  $T$  is in °C] was obtained by a least square's regression analysis:

$$c_p(\text{DSC}) = 0.0052 T + 0.9255 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.99) \quad (13)$$

Similarly, Eq. (14) was derived from the HDA data [5] where  $T$  is in °C:

$$c_p(\text{HDA}) = 0.0024 T + 1.6238 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.78) \quad (14)$$

Figure 7 shows the variation of  $c_{p,a}$  for wool tested using both the DSC and HDA apparatus, though HDA experiments were not conducted beyond 200 °C. Wool is affected by moisture evaporation in the same manner as cotton and pinewood. Both the DSC and HDA data show that shortly after the initiation of heating, the moisture affected region is apparent. Phase transition regions are observed in the DSC data which can be attributed to the decomposition within the fibres of wool or swelling decrystallisation of various types of amino acids present in wool [30, 31]. This can also contribute to the secondary peak and linear increase observed as the acids break down into base constituents above the temperature of 225 °C [37, 38]. Similar to the cotton data presented in Fig. 6, the moisture evaporation and phase

transition enthalpy for the 50 K.min<sup>-1</sup> profile are shown as hatched patterns.

To obtain a quantitative trend, all DSC data were analysed excluding the moisture evaporation and phase transition. The DSC obtained  $c_p$  values were averaged over all three heating rates data in three regions: (i) from 25 to 68 °C, (ii) from 180 to 240 °C and (iii) from 260 to 275 °C. Undertaking a least squares analysis of the average profile, the relationship obtained is presented in Eq. (15) for the DSC data and in Eq. (16) for the HDA data [5], where  $T$  is in °C:

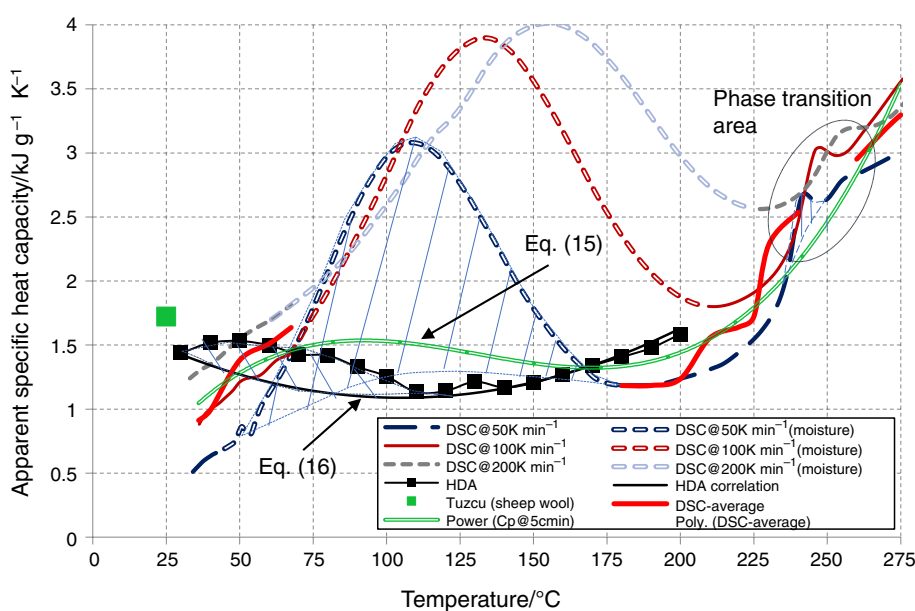
$$c_p(\text{DSC}) = 9 \times 10^{-7} \times T^3 - 0.000355 T^2 + 0.04237 T - 0.06137 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.94) \quad (15)$$

$$c_p(\text{HDA}) = 6 \times 10^{-5} \times T^2 - 0.0126 T + 1.85 \text{ kJ g}^{-1} \text{ K}^{-1} (r^2 = 0.91) \quad (16)$$

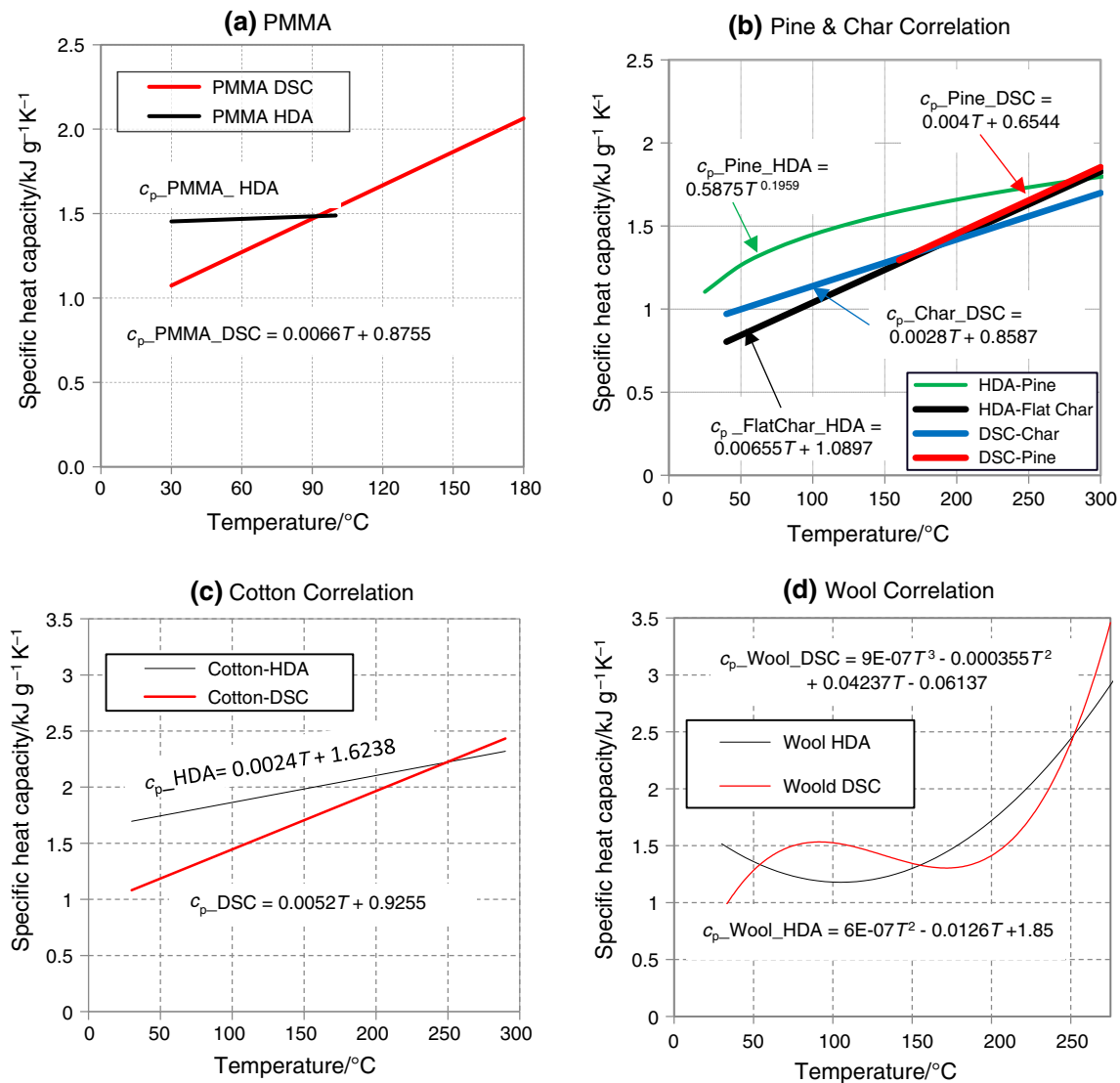
In general, the data from both test apparatus are comparable except at low temperatures. Figure 7 also presents a comparative literature value for sheep wool as reported by Tuzcu [39] which is slightly higher than the values from the current study although it should be noted that this literature data did not take into account temperature or heating rate. It can be observed that while the heating rate varied, before and after the moisture evaporation region (until the phase transition occurs),  $c_p$  values differ considerably implying significant effect of thermal transport.

A summary of the correlations developed for the tested materials is presented in Fig. 8 and in general, it can be observed that as the temperature increases there is an increase in the  $c_p$  values. Moreover, the difference between HDA and DSC measurements are not substantial. For each material, at a specific temperature, the values intersect and

**Fig. 7** Variation of apparent specific heat capacity for wool. The hatched pattern shows exemplar moisture evaporation and phase transition enthalpy as well as the difference between the specific heat capacity and the apparent specific heat capacity







**Fig. 8** Correlations of  $c_p$  for **a** PMMA, **b** pinewood, virgin and char, **c** cotton and **d** wool with temperature

moving away from this intersection point, the difference increases. The maximum difference ranges for PMMA, pine, pine char, cotton and wool are  $\pm 0.6$ ,  $\pm 0.3$ ,  $\pm 0.2$ ,  $\pm 0.6$  and  $\pm 0.7$   $\text{kJ kg}^{-1} \text{K}^{-1}$ . In the supplementary material, a method is recommended to enable the optimized use of the data.

## Conclusions

The  $c_p$  values of common building materials tested with DSC and HDA apparatus are presented in this study with their trends determined with respect to temperature. The primary objective is to use the obtained  $c_p$  values in CFD-based

fire simulations for fire engineering and research purposes. While the HDA measurement did not involve changes in heating rate, DSC measurements were conducted at heating rates of 50, 100 and 200  $\text{K min}^{-1}$  as these are likely to occur in substantial fires. DSC materials were roughly measured over a temperature range of 25–300  $^{\circ}\text{C}$  except for wool which was measured up to 275  $^{\circ}\text{C}$ . HDA measurements were conducted over the temperature ranges 30–100  $^{\circ}\text{C}$  for PMMA, 30–225  $^{\circ}\text{C}$  pinewood, 25–150  $^{\circ}\text{C}$  for char and 30–200  $^{\circ}\text{C}$  for cotton and wool.

Of all the materials tested, PMMA was the only material not affected by moisture content and pine, cotton and wool all showed phase transitions at  $\sim 125$   $^{\circ}\text{C}$ ,  $\sim 260$   $^{\circ}\text{C}$  and  $\sim 245$   $^{\circ}\text{C}$ , respectively. For similar materials, literature

data were generally comparable to the data obtained in the current study although typically at lower temperatures. This further supports the results obtained at higher temperatures and at different heating rates in the current study.

The DSC measurements of  $c_p$  values did not change significantly for PMMA and pine char between heating rates adopted in this study. For pine and cotton, slight decreases in  $c_p$  with increased heating rates are observed. On the other hand, wool  $c_p$  values considerably increased as the heating rate increased. The effect of thermal transport varies due to chemical composition, physical and structural properties. It is also noted that the materials have different fibrous and cellulose structures.

Analysis of the DSC and HDA  $c_p$  values for the various materials studied enabled the development of empirical relationships. The relationships were developed from regions where phase changes were not occurring, and regions not affected by moisture evaporation. The relationships show that the difference between HDA and DSC are not substantial. These relationships can be used as input values for CFD-based fire simulations and models and all materials except for wool showed a linear increase of  $c_p$  values with increasing temperature. A second- and third-order curvilinear increase was observed for the  $c_p$  values with HDA and DSC measurement for wool. Some suggestions are made, in the supplementary material, for including these relationships in CFD-based fire models. The enhanced accuracy of the data will assist in providing higher fidelity simulations of fire scenarios which can be utilized in order to develop improved designs for reducing fire risk.

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## Compliance with ethical standards

**Conflict of interest** The authors report no conflict of interest in this study.

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