



# The use of titanium oxide/polyethylene glycol nanocomposite in sorption of $^{134}\text{Cs}$ and $^{60}\text{Co}$ radionuclides from aqueous solutions

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## Abstract

Titanium dioxide/polyethylene glycol ( $\text{TiO}_2/\text{PEG PNC}$ )-nanocomposite was prepared using the wet chemical method. Physico-chemical characterization of  $\text{TiO}_2/\text{PEG PNC}$  is studied by TEM, FTIR, XRD, DTA-TGA, particle size distribution, and pore size analysis.  $\text{TiO}_2/\text{PEG PNC}$  used for sorption of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides. The  $\text{TiO}_2/\text{PEG PNC}$  sorption monolayer capacities towards  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides at pH 5 and 25 °C is numerically equal to  $163.28 \pm 10.98$ , and  $330.16 \pm 41.60 \text{ mg g}^{-1}$ , respectively. The kinetic of the sorption reaction is applicable with a pseudo-second-order model. The sorption reaction is favorable and endothermic.

**Keywords** Titanium dioxide · Nanocomposite · Sorption · Radioactive waste

## Introduction

Nano-sized materials are a new solid that takes a large portion of attention in recent years due to its special properties (such as small size (1–100 nm), numerous specific surface area [1–3]). Thus, the nano-materials are able to provide a selective high sorption capacity towards trace mineral ions.

A previous study showed that  $\text{TiO}_2$  nanoparticles could adsorb heavy metal ions [4] and rare earth elements [5]. The disadvantage in using nanometal oxides as a sorbent is the agglomeration due to van der Waals interactions [6] as a result for the increase in surface area, which makes metal oxide particles unstable. Thus, the metal oxide may lose selectivity, mechanical strength, and high adsorption capacity. To overcome this disadvantage, polymeric supports, with a large surface area, adjustable surface chemistry, perfect mechanical hardness, and pore size distribution, could be used for metal oxides immobilization [6, 7].

Polyethylene glycol (PEG) is a hydrophilic polymer capable of creating a uniform surface, smooth coating and well-defined particles [8], as it reduces cracked surface formation in the immobilizer system [9]. Most reports on nano  $\text{TiO}_2$  immobilized with PEG have been identified to

enhance photosynthesis due to porosity effect and greater specific surface area [10, 11]. Trapalis et al. [12] found that as the weight percent of PEG introduced in the  $\text{TiO}_2$  film increases, the porosity consequently increases. However, no detailed study was conducted on the sorption behavior of  $\text{TiO}_2$  immobilized with PEG towards radioactive waste.

A large amount of radioactive wastewater has been produced in conjunction with the advances in nuclear industry.  $^{90}\text{Sr}$ ,  $^{134}\text{Cs}$ , and  $^{60}\text{Co}$  are the most important radionuclides in low-level aqueous wastes in terms of a possible dose of humans [13–15]. Adsorption of radionuclides from their solutions is one of the various steps used in the treatment of radioactive liquid-waste using suitable adsorbent, (activated and impregnated carbon, clays, alumina silicates, organic, and inorganic gels and others, have been reported) [16–22].

Therefore, this work aims to prepare  $\text{TiO}_2/\text{PEG PNC}$  and explain the physicochemical characteristics using FTIR, TEM, X-ray diffraction, DTA-TG, particle size distribution, and pore size analysis. The sorption of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  on  $\text{TiO}_2/\text{PEG PNC}$  is studied. Optimization of the reaction conditions such as (pH, shaking time, sorbent concentration, and temperature have been investigated. Moreover, the specifications of the sorption reaction as kinetics mechanism, isotherms models, and thermodynamic parameters are studied.

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## Experimental

### Chemicals

All chemicals used were of (AR) and were used without additional purification. Titanium tetra isopropyl orthotitanate ( $C_{12}H_{28}O_4Ti \geq 97\%$ ) obtained from Merck Germany, Isopropyl alcohol ( $C_3H_8OH \geq 99.7\%$ ) obtained from Prolabo, England. Ammonium hydroxide ( $NH_4OH$ ) 33% from Edwic El-Nasr, Egypt. Polyethylene glycol 1500, H ( $OCH_2CH_2$ )<sub>n</sub> OH Extra Pure Obtained from Kosdaq. China. Dehydrated alcohol, absolute ethanol  $C_2H_5OH$ , 99.9% obtained from International Company for Sup. & MED. Industries, Egypt.

Hydrochloric acid (HCl) and sodium hydroxide (NaOH) were obtained from El-Nasr Co. (ADWIC), Egypt, used to adjust the pH of the solutions. Cesium chloride (CsCl) and cobalt chloride ( $CoCl_2$ ) were purchased from Merck, (Germany). For all experiments, (DDW) double-distilled water was used for the preparation of solutions.

The radionuclides of two elements ( $^{134}Cs$  and  $^{60}Co$ ) were produced by irradiation of cesium chloride and cobalt chloride powders in the Second Egyptian Research Reactor (ET-RR-2). The initial activity were 42.2 KBq/L, and 14.3 KBq/L for  $^{134}Cs$  and  $^{60}Co$  radionuclides respectively.

A stock solution of ( $^{134}Cs$  and  $^{60}Co$ ) were prepared by dissolving a certain amount of cesium and cobalt salts in

double-distilled water and spiked with the  $^{134}Cs$  and  $^{60}Co$  radionuclides. These solutions were kept as stock radioactive solutions for all experiments.

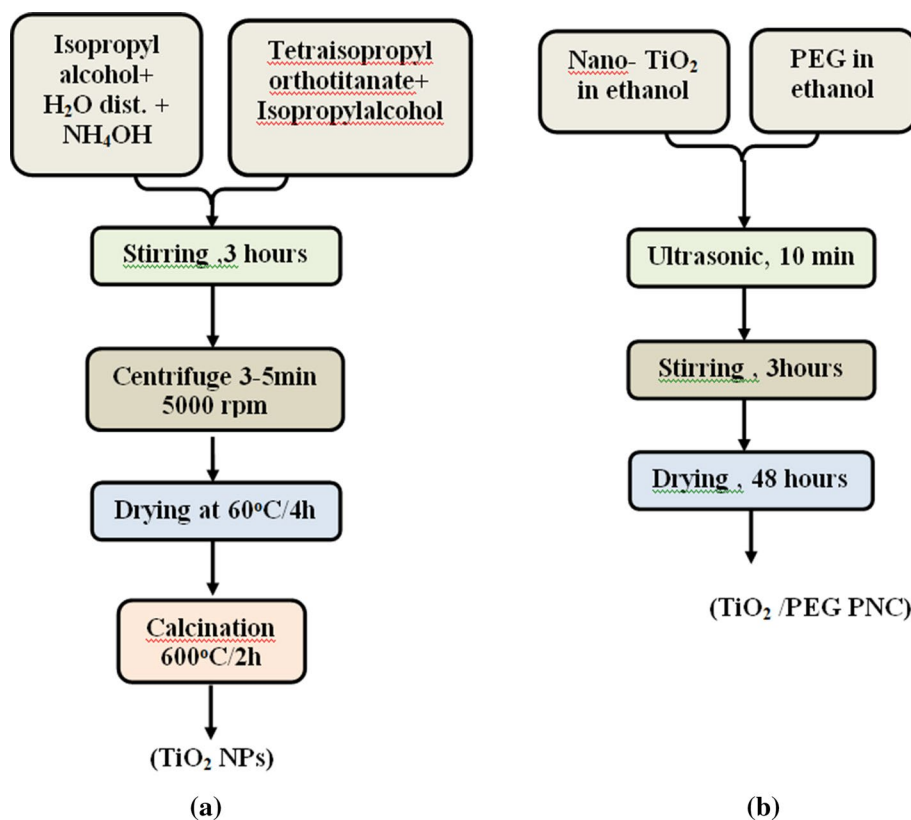
### Preparation of nano-sized $TiO_2$ powder ( $TiO_2$ NPs)

Nano-sized  $TiO_2$  is prepared by the sol–gel hydrolysis technique using titanium tetra isopropyl orthotitanate as a precursor. The preparation technique includes the hydrolysis of alkoxide (tetra isopropyl orthotitanate) to form sol and then the gel phase is formed after polymerization of sol using a catalyst [23]. The flow chart in Fig. 1a summarizes the steps for  $TiO_2$  NPs preparation.

### Preparation of $TiO_2$ /PEG nanocomposite ( $TiO_2$ /PEG PNC)

The 1:1 PEG/ $TiO_2$  nanocomposite was prepared using a wet chemical technique [24] where PEG was adsorbed on the  $TiO_2$  surface. 5 g of polyethylene glycol in 20 ml ethanol and added drop wisely to a solution of 5 g of the calcined nano- $TiO_2$  powder. The mixture was lied in ultrasonic for 10 min. The whole mixture was stirred for 3hours. The gelatin was dried at 80 °C for 48 h. The flow chart in Fig. 1b summarizes the steps for  $TiO_2$ /PEG PNC preparation.

**Fig. 1** Flow chart for preparation of **a**  $TiO_2$  NPs and **b**  $TiO_2$ /PEG PNC



## Instruments and apparatus

The scanning electron microscope (SEM) combined with energy-dispersive X-ray spectroscopy and electron backscatter diffraction (SEM, FEI Quanta FEG-250, and EDX). The transmission electron micrograph image (TEM), for the particle size was recorded on a TEM, JEM2100, and Jeol.s.b, Japan. The X-ray diffraction (XRD) in a Philips X'PERT multipurpose X-ray diffractometer with copper emission lines. Thermal properties of the samples studied using thermo gravimetric analysis (TGA) performed on a Perkin Elmer TGA6 instrument. The sample was heated from 298 to 973 K with a heating rate of 283 K/min under a nitrogen atmosphere with a flow rate of 20 mL/min. Fourier transform infrared (FT-IR) spectra of the samples were recorded using an IR spectrometer with Fourier transformation (Thermo Nicolet Nexus FT-IR, Waltham, MA, USA). The particle size of the prepared samples determined using Zetasizer Nano-Zs, MALVERN, UK. Pore size distribution and corresponding porosity of the prepared powders investigated applying mercury intrusion porosimetry technique with the aid of Pore-sizer chromatech 9320, USA. The activity of radionuclides have been measured radiometrically by high resolution (7.5%) NaI (TI) detector model 802-3X3, Canberra, USA.

## Sorption batch studies

0.05 g of the TiO<sub>2</sub>/PEG PNC with (100 mg L<sup>-1</sup>) of the solution labeled with <sup>134</sup>Cs and <sup>60</sup>Co radionuclides at various time range (1–120 min), temperatures 25 °C, 40 °C, and 60 °C, and optimum pH. The activity of both radionuclides was determined and the amount of radionuclides,  $q_t$  (mg g<sup>-1</sup>), was calculated from the following equation:

$$q_t = \frac{A_0 - A_t}{A_0} \times C_0 \times \frac{V}{m} \quad (1)$$

where ( $A_0$  and  $A_t$ ) are the activity of the solution at initial and any time  $t$ , respectively, ( $C_0$ ) is the initial concentration of ions, ( $V$ ) is the volume of the solution (10 mL), and ( $m$ ) is the weight of adsorbent (0.05 g).

## Sorption isotherm studies

Sorption isotherm studies of <sup>134</sup>Cs and <sup>60</sup>Co radionuclides [25] were investigated at different concentrations (50–300 mg L<sup>-1</sup>) onto the prepared materials by adding a certain weight of the sorbent (0.05) to solution of ions labeled by the radionuclides for 30 min. The pH value of the solution was adjusted at (5 ± 0.1). Different isotherm

models such as Langmuir and Freundlich isotherm models were studied.

## Results and Discussion

### Characterization of the prepared nanocomposite

#### SEM and TEM measurement

Figure 2a represents the dispersion of TiO<sub>2</sub> and PEG in TiO<sub>2</sub>/PEG PNC. There is neither phase separation nor cracking in the prepared composite but a rough and fractured surface is obtained [24, 26]. The white nanoparticles are constituted of TiO<sub>2</sub> NPs and the dark surrounding area is constituted of the organic matrix of PEG.

Figure 2b shows a TEM analysis of TiO<sub>2</sub>/PEG PNC with a significant presence of nanoparticles reveals [27]. The obtained image is mostly composed of aggregates of hexagonal and irregular particles with a particle size below 20 nm. The aggregation attributes to the sol–gel preparation method.

#### Particle size statistics and porosity

The particle size statistics is represented in Fig. 3. The sample were ground in the mill and dispersed ultrasonically in non polar solvent and water for TiO<sub>2</sub>/PEG PNC and TiO<sub>2</sub> NP, respectively.

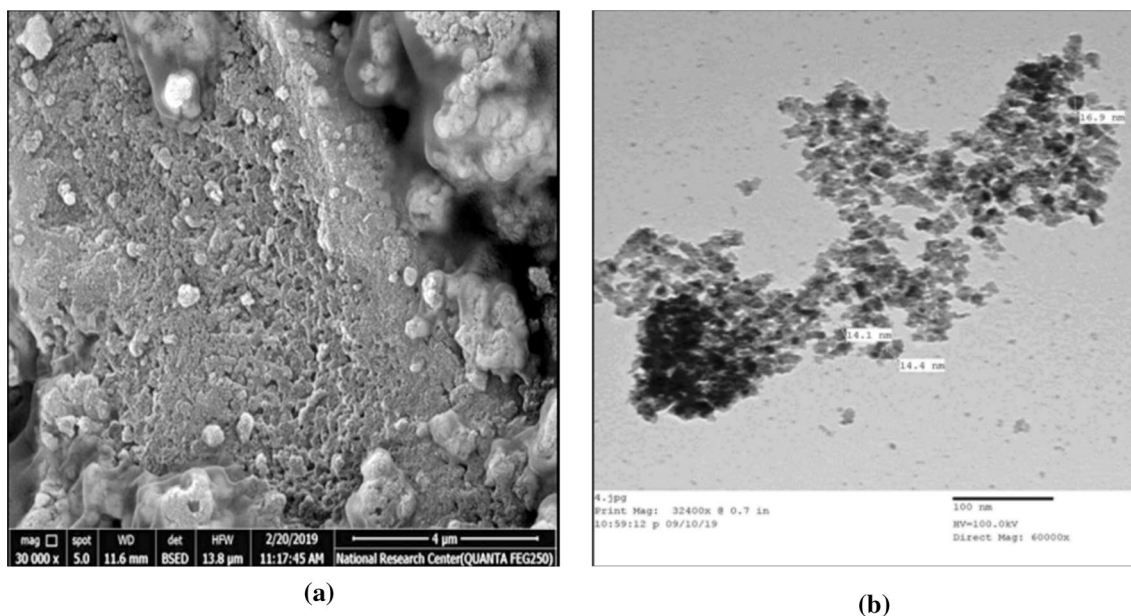
The nanocharacter appears in TiO<sub>2</sub> particles while; the particle size distribution varies between nano-size to fine for TiO<sub>2</sub>/PEG PNC. The increase in particle size is due to the chemical adsorption of PEG molecules onto TiO<sub>2</sub> [28].

The porosity and pore parameters of TiO<sub>2</sub>/PEG PNC were illustrated in Table 1. The porous structure of TiO<sub>2</sub>/PEG PNC is clarified as the porosity is 32.78%, TiO<sub>2</sub>/PEG PNC porosity strongly depends on the amount and molecular weight of PEG [12, 29].

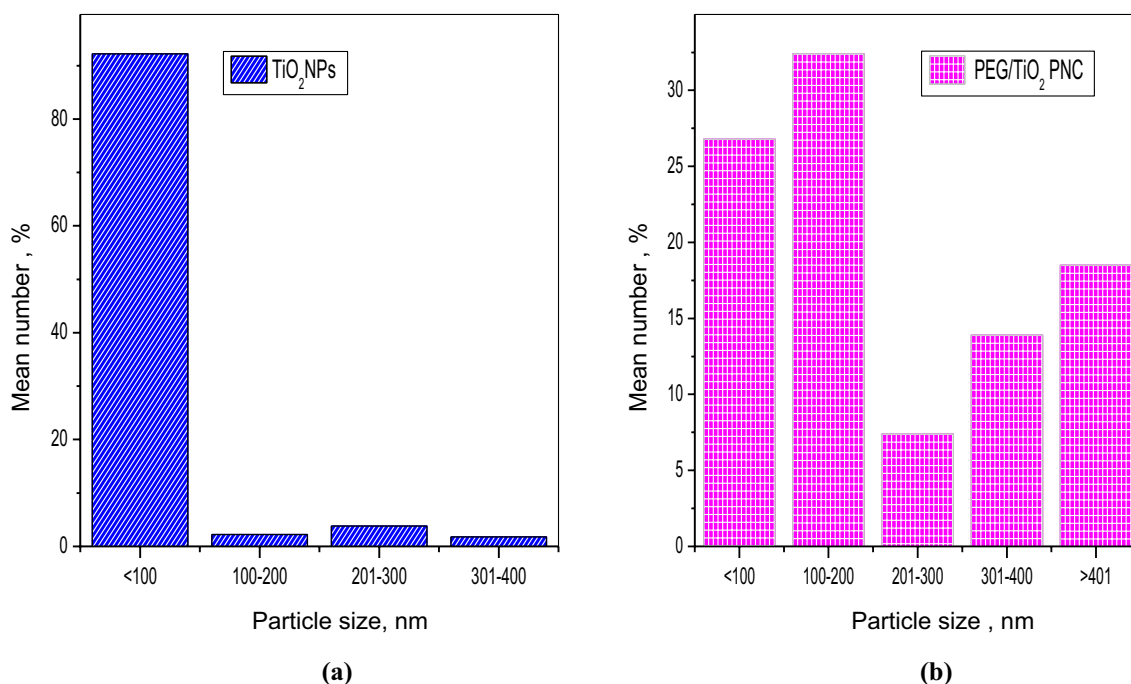
#### FT-IR analysis

Figure 4a, b shows a sequence of FT-IR spectra for TiO<sub>2</sub> NPs and TiO<sub>2</sub>/PEG PNC respectively. Figure 4a represents the spectrum of TiO<sub>2</sub> NPs, clearly shows bands at 3862 cm<sup>-1</sup>, 2979 and 2901 cm<sup>-1</sup>, assigned to the stretching vibration of the hydroxyl group O–H of the TiO<sub>2</sub> NPs. The presence of the O–H group belongs to the remaining water/humidity molecules in the crystals lattice of the TiO<sub>2</sub> sample. The band observed around 1633 cm<sup>-1</sup>, corresponding to bending modes of water Ti–OH; a strong noticeable peak at 1051 cm<sup>-1</sup> related to Ti–O modes [30, 31].

The FT-IR spectrum of TiO<sub>2</sub>/PEG PNC is given in Fig. 4b, a considerable change represents in the spectrum



**Fig. 2** **a** SEM and **b** TEM image of  $\text{TiO}_2/\text{PEG PNC}$



**Fig. 3** Particle size distribution of **a**  $\text{TiO}_2$  NPs and **b**  $\text{TiO}_2/\text{PEG PNC}$

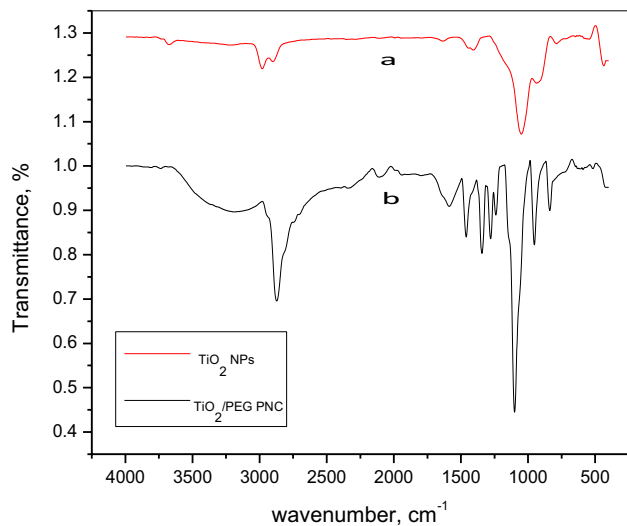
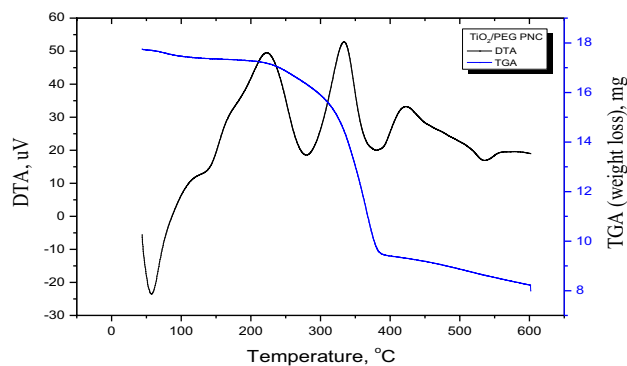
where new bands appear due to the presence of PEG. A strong peak around  $1099\text{ cm}^{-1}$  attributable to C–C and C–O stretching vibrations. A sharp peak at  $2872\text{ cm}^{-1}$  is also observed, corresponding to C–H stretching vibration; while the peak  $3862\text{ cm}^{-1}$  in  $\text{TiO}_2$  NPs for O–H disappears. This change confirms the chemically adsorption of PEG onto  $\text{TiO}_2$  [28, 31, 32].

### Thermal analysis

Figure 5 shows that  $\text{PEG}/\text{TiO}_2$  PNC had an approximate two endothermic peak at  $\sim 60\text{ }^\circ\text{C}$  and  $144\text{ }^\circ\text{C}$  with initial weight loss 2.5% attribute to the evaporation of absorbed water and ethanol [28]. Started from  $280\text{ }^\circ\text{C}$  till  $539\text{ }^\circ\text{C}$ , three endothermic peaks with total weight loss 51% are attributed to

**Table 1** Porosity and pore parameters for TiO<sub>2</sub>/PEG PNC

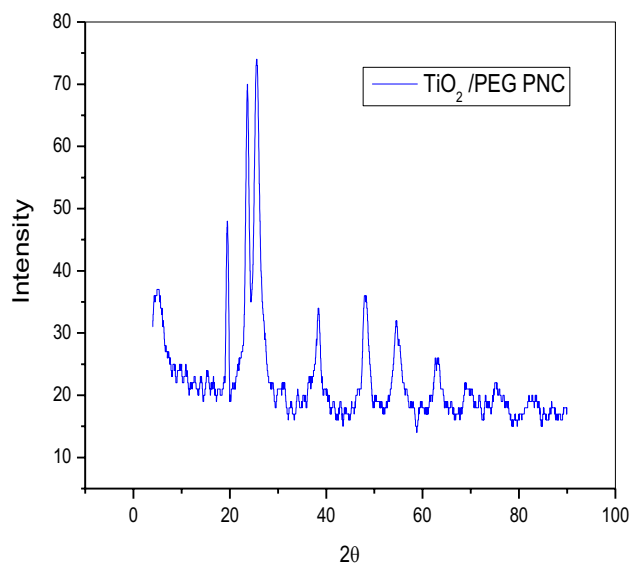
Sample	Pore size parameters			
	Average pore diameter (nm)	Porosity (%)	Bulk density (g/mL)	Apparent density (g/mL)
TiO <sub>2</sub> /PEG PNC	257.1	32.78	0.8405	1.2503

**Fig. 4** FT-IR spectra for: (a) TiO<sub>2</sub> NPs, and (b) TiO<sub>2</sub>/PEG PNC**Fig. 5** TGA and DTA for the synthesized TiO<sub>2</sub>/PEG PNC

organic matter degradation of PEG in TiO<sub>2</sub>/PEG PNC [28, 31].

### X-ray diffraction (XRD)

The result of XRD analysis of TiO<sub>2</sub>/PEG PNC is represented in Fig. 6 and listed in Table 2. The crystallite structure of the nanocomposite is clarified through the intensity of

**Fig. 6** XRD profiles of the TiO<sub>2</sub>/PEG PNC**Table 2** XRD results of TiO<sub>2</sub>/PEG PNC

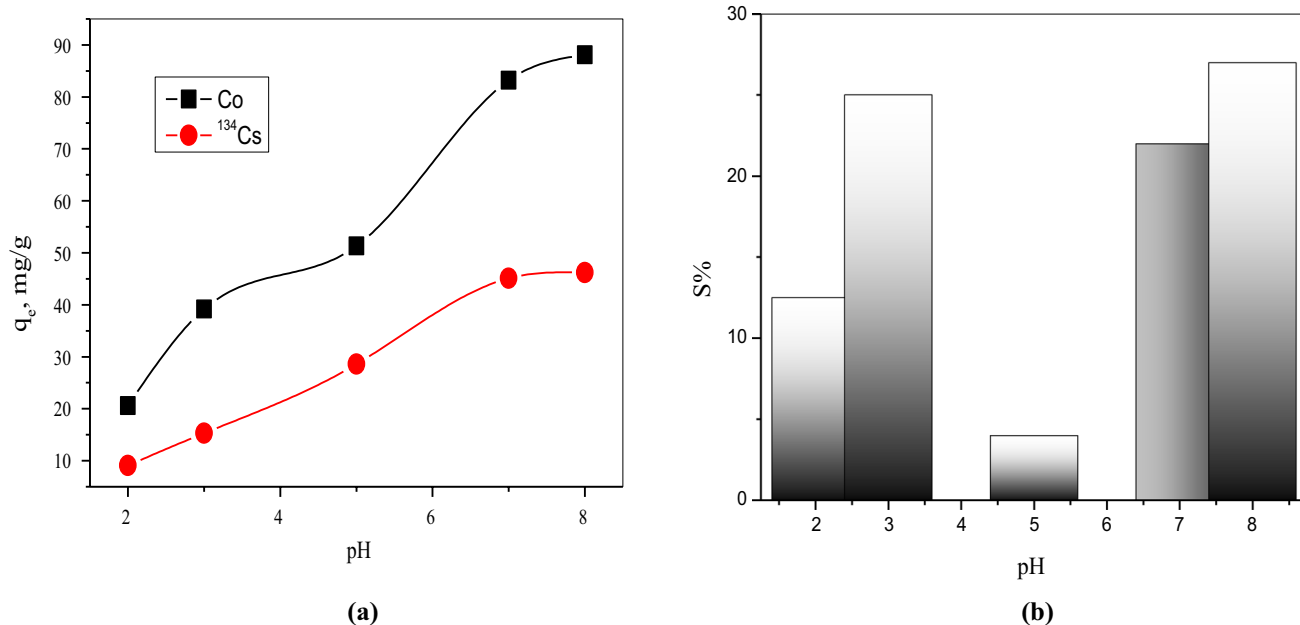
Samples	XRD results		
	2θ	d-spacing (Å)	FWHM (deg)
TiO <sub>2</sub> /PEG PNC	25.56	3.48	1.12
	23.62	3.76	0.73
	19.49	4.55	0.54

XRD peaks while the broad diffraction peaks indicate very small size crystallite. For TiO<sub>2</sub>/PEG PNC. The diffraction angle,  $2\theta = 25.5$  [35] confirms TiO<sub>2</sub> anatase structure, while  $2\theta = 23.62, 19.49$  confirms crystalline phase of PEG [24].

### Sorption studies

#### The effect of pH

Figure 7a shows the effect of pH on the amount adsorbed ( $q_e$ ) of <sup>134</sup>Cs and <sup>60</sup>Co radionuclides, different experiments were performed in the pH range 1–8. The sorption of both radionuclides is pH-dependent. The amount adsorbed of <sup>134</sup>Cs and <sup>60</sup>Co increase with increasing pH. At higher pH values,  $[H^+]$  is low and the negative charge on the surface of the composite will increase enhancement the attraction forces among the surface of the composite and radionuclides increase, so the amount adsorbed of the radionuclides will increase. At lower pH values, the concentration of  $[H^+]$  is high and competes the sorption of Cs and Co radionuclides on the surface of the composite and so decrease the amount adsorbed of these radionuclides [33].

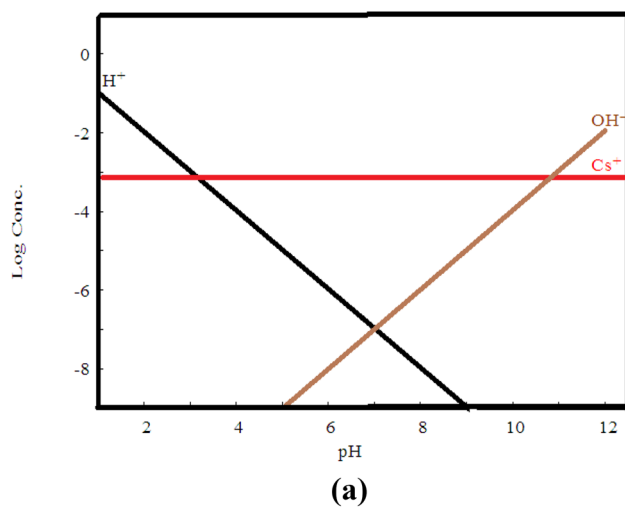


**Fig. 7** **a** Effect of pH on the amount of adsorbed of  $^{134}\text{Cs}$ ,  $^{60}\text{Co}$  on  $\text{TiO}_2/\text{PEG}$  PNC at room temperature and **b** stability of prepared  $\text{TiO}_2/\text{PEG}$  PNC powder in different pH

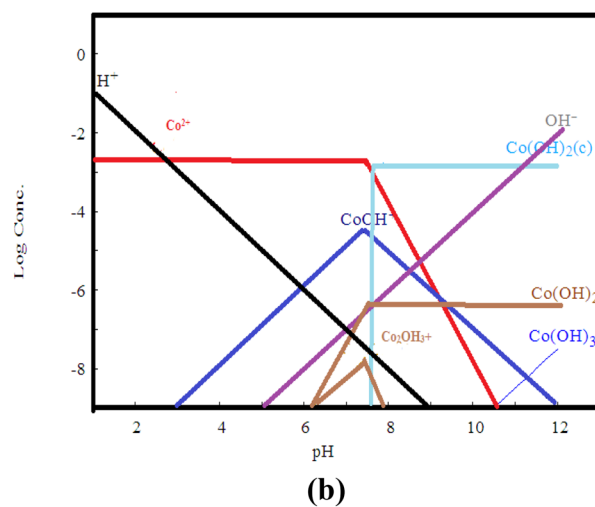
The speciation diagram of  $\text{Cs}^+$  and  $\text{Co}^{2+}$  ions at different pH values in aqueous solution is shown in Fig. 8 using Hydra/Medusa chemical equilibrium software [34]. As pH increases, hydrolysis precipitation most probably would start due to the formation of various hydro complexes in aqueous solution [35].

At initial metal ions concentration,  $50 \text{ mg L}^{-1}$ , room temperature and different pH values (1–12). From Fig. 8a it is clear that the monovalent cesium ( $\text{Cs}^+$ ) is the dominant species at all pH ranges. It is obvious that in Fig. 8b, the divalent species,  $\text{Co}^{2+}$ , is the dominant cobalt species at pH below 8, at the pH values  $> 8$ , the cobalt ion was precipitated as  $\text{Co}(\text{OH})_2$ . So, the removal of cobalt below the

$[\text{Cs}^+]_{\text{TOT}} = 0.37 \text{ mM}$



$[\text{Co}^{2+}]_{\text{TOT}} = 0.84 \text{ mM}$



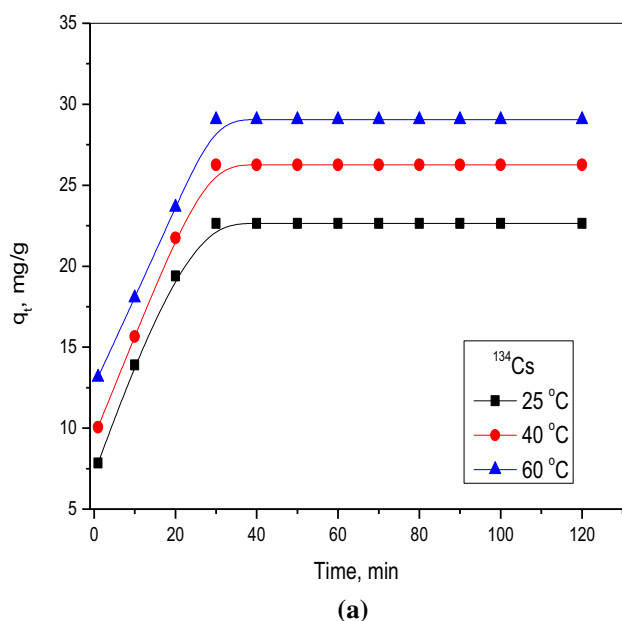
**Fig. 8** Speciation of: **a** cesium and **b** cobalt ions at different pH and room temperature

pH < 8 is due to the sorption process but at a higher value of pH the hydrolysis of  $\text{Co}^{2+}$  [35], leading to the formation of  $[\text{CoOH}]^+$  and  $\text{Co}(\text{OH})_2$ , therefore, the precipitation process is the predominant mechanism at the higher pH values. So all the sorption experiments were carried out at pH 5 [35]. The result of chemical stability tests is shown in Fig. 7b. The prepared powder material was highly stable at pH 5 with weight loss of about 4%, and it witnessed considerable weight loss of 22, 25 and 27% at pH values 3, 7 and 8, respectively. In light of these findings, further experiments were performed in a solution of pH 5 to avoid any possible hydroxide precipitation and also ensure usage of the material in its most stable state.

The pH- distribution coefficient relation is shown in Table 3. The results obtained showed that  $K_d$  is pH-dependent. As the pH increases,  $k_d$  will increase for both radionuclides confirming the increase in amount sorbed of radionuclides as the pH increase.

**Table 3** Distribution coefficients ( $K_d$ ) of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides sorbed by  $\text{TiO}_2/\text{PEG PNC}$  at different pH

pH	$K_d$ (ml/g)	
	$^{134}\text{Cs}$	$^{60}\text{Co}$
2	20.02	51.89
3	36.13	128.95
5	80.11	210.78
7	164.29	990.27
8	171.75	1480.67



## Effect of shaking time & temperature

The effect of shaking time on the sorption behavior of the studied radionuclides at temperatures 25 °C, 40 °C, and 60 °C is represented in Fig. 9. A certain weight (0.05 g) of the prepared nanocomposite and optimum pH 5. The results indicated that the sorption process was fast and equilibrium was reached within 30 min sorbents. The rapid radionuclides sorption onto  $\text{TiO}_2/\text{PEG PNC}$  sorbents can be explained by the availability of active sites on sorbent surfaces. The percent uptake was found to be 45.3, 52.5 and 58.1% for  $\text{Cs}^+$  ions, and 83.3, 87.3 and 94.5% for  $^{60}\text{Co}$  respectively. The amounts sorbed of  $^{134}\text{Cs}$  radionuclide at equilibrium is 22.65, 26.25 and 29.05  $\text{mg g}^{-1}$  at 25 °C, 40 °C and 60 °C respectively while the sorbed amounts of  $^{60}\text{Co}$  radionuclide at equilibrium is 41.65, 43.75 and 47.25  $\text{mg g}^{-1}$  at 25 °C, 40 °C and 60 °C respectively.

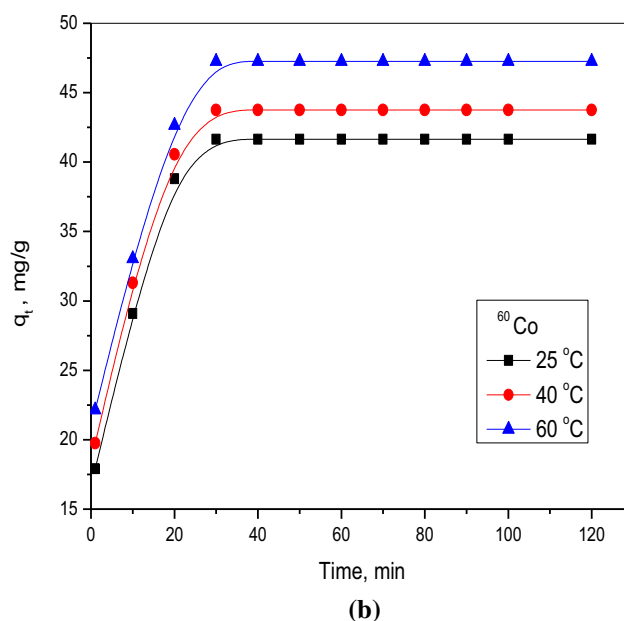
## Sorption kinetics modeling

Kinetic models are used to determine the rate of sorption reaction and to investigate the mechanism of the sorption process.

The pseudo-first-order model was studied by applying the Non-linear pseudo-first-order Eq. (2) [36]:

$$q_t = q_e (1 - e^{-k_1 t}) \quad (2)$$

where  $q_e$  ( $\text{mg g}^{-1}$ ), and  $q_t$  ( $\text{mg g}^{-1}$ ), are the quantities of metal ion sorbed at equilibrium and at time  $t$ , respectively, and  $k_1$  ( $\text{min}^{-1}$ ), is the rate constant of the first-order equation.



**Fig. 9** Effect of contact time on the amount sorbed of **a**  $^{134}\text{Cs}$  and **b**  $^{60}\text{Co}$  onto  $\text{TiO}_2/\text{PEG PNC}$  at different temperatures, pH 5 and  $V/m = 200 \text{ mL/g}$

The pseudo-second-order non-linear equation is expressed as [36]:

$$q_t = \frac{k_2 q_e^2 t}{1 + k_2 q_e t} \quad (3)$$

where  $k_2$  is a rate constant of the second-order model (g/mg·min). Figure 10 illustrates the fitting of the relation and the value of  $k_2$  and  $q_e$  were determined and listed in Table 4. The pseudo-second-order equation is used with the assumption that the interaction between the adsorbate and adsorbent material is due to the chemisorption process.

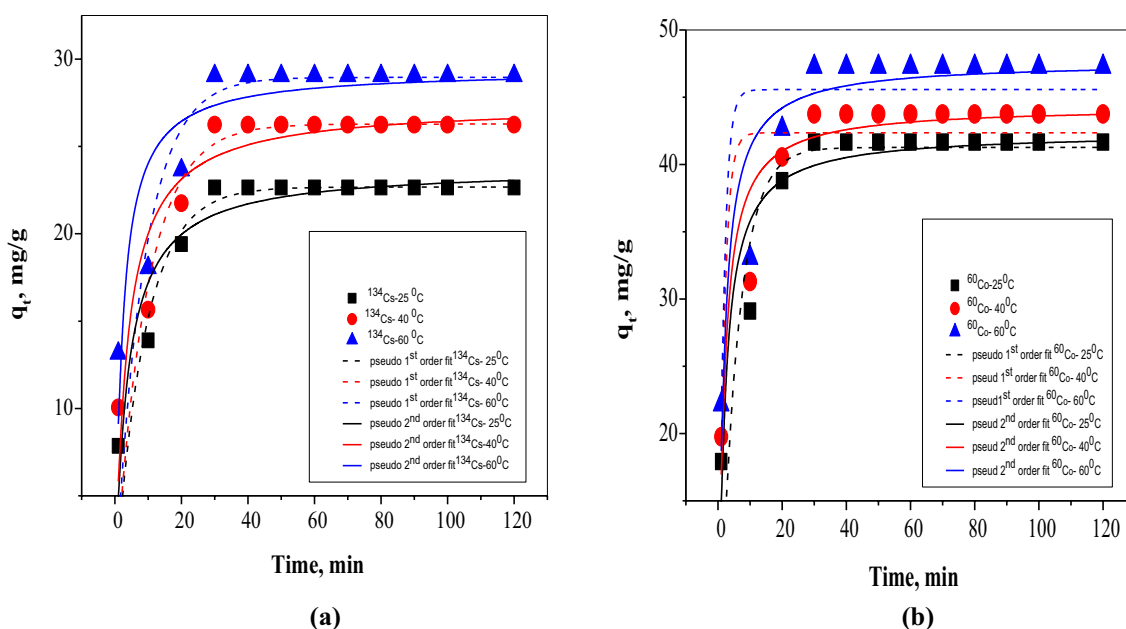
Figure 10 expressing the relation fitting. Table 4 illustrated the values of  $q_e$ ,  $k_1$ ,  $k_2$  and the correlation coefficient ( $R^2$ ) of both radionuclides at three different temperatures. The values of the calculated capacity of the sorbed

radionuclides at equilibrium  $q_e$  (cal.) must be in identity with the values of the experimental data  $q_e$  (exp.).

The values of  $q_e$  (cal.) are commensurate with the results of  $q_e$  (exp.) for both pseudo-first and pseudo-second-order. But, the high values of  $R^2$  for pseudo-second-order elucidate that the sorption of  $^{60}\text{Co}$  and  $^{134}\text{Cs}$  radionuclides on  $\text{TiO}_2/\text{PEG}$  obeys pseudo-second-order kinetics. This fact shows that the pseudo-second-order model is the predominant model and the sorption process can be controlled by the chemical sorption process.

### Equilibrium isotherm studies

The adsorption isotherm describes the relationship between the amount of sorbate on the sorbent at equilibrium,  $q_e$ , and the concentration of dissolved sorbate in the liquid,  $C_e$ . Fig. 11 shows the plots between the amount of  $^{134}\text{Cs}$  and



**Fig. 10** Non-linear form fitting of pseudo-first order and pseudo-second order plots for the sorption of **a**  $^{134}\text{Cs}$  and **b**  $^{60}\text{Co}$  radionuclides onto  $\text{TiO}_2/\text{PEG}$  PNC at different temperatures

**Table 4** Calculated parameters of the studied kinetic models for adsorption of  $^{60}\text{Co}$  and  $^{134}\text{Cs}$  onto  $\text{TiO}_2/\text{PEG}$  PNC

Radionuclide	Temperature (°C)	First-order kinetic parameters			$q_{e(\text{exp})}$ (mg/g)	Second-order kinetic parameters		
		$k_1$ (min <sup>-1</sup> )	$q_e$ (cal.) (mg/g)	$R^2$		$k_2$ ( $\times 10^{-3}$ ) (g/mg min)	$q_e$ (cal.) (mg/g)	$R^2$
$^{134}\text{Cs}$	25	0.1049 ± 0.02	22.67526 ± 0.6384	0.8529	22.65 ± 0.33	0.01099 ± 0.0033	23.78652 ± 0.73825	0.89402
	40	0.10523 ± 0.02	26.28254 ± 0.87304	0.7882	26.25 ± 0.37	0.00984 ± 0.0035	27.4166 ± 0.9976	0.84426
	60	0.11436 ± 0.03	28.95577 ± 1.15955	0.6166	29.025 ± 0.39	0.01531 ± 0.0060	29.38326 ± 1.02265	0.76869
$^{60}\text{Co}$	25	0.17702 ± 0.05148	41.27 ± 1.29	0.7165	41.65 ± 1.21	0.01283 ± 0.00322	42.378 ± 0.9152	0.89219
	40	0.60763 ± 0.16473	42.358 ± 1.135	0.7457	43.75 ± 1.27	0.01398 ± 0.0034	44.30962 ± 0.90048	0.8907
	60	0.65071 ± 0.1853	45.56 ± 1.313	0.6994	47.25 ± 1.29	0.01357 ± 0.0037	47.62535 ± 1.0883	0.85676



$^{60}\text{Co}$  radionuclides sorbed at equilibrium  $q_e$ , onto the papered  $\text{TiO}_2/\text{PEG PNC}$  and the initial metal ion concentrations  $C_o$ . The concentration of metal ions ranges 50–300 mg/L. From the Figure, it is observed that the amount sorbed of each radionuclide was increased with the increase of the initial concentration of the metal ions and temperature.

### Langmuir and Freundlich isotherm models

The non-linear form of the Langmuir model can be expressed as the following [37]:

$$q_e = \frac{q_m b C_e}{1 + b C_e} \quad (4)$$

where  $q_m$  is the monolayer sorption capacity ( $\text{mg g}^{-1}$ ),  $b$  is the constant related to the free energy of sorption ( $b \propto e^{-\Delta G/RT}$ ) and  $C_e$  is the equilibrium metal ion concentration.

Also, the non-linear form of the Freundlich model can be expressed in Eq. (5) as the following [37]

$$q_e = k_f C_e^{1/n} \quad (5)$$

where,  $k_f$  is the Freundlich adsorption capacity coefficient ( $\text{mg g}^{-1}$ ),  $1/n$  is the adsorption intensity

Figure 12 represents non-linear form fitting of Langmuir isotherm and Freundlich models of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides sorption onto  $\text{TiO}_2/\text{PEG PNC}$ . On the basis of the parameters obtained from the Langmuir model (Table 5), the maximum sorption capacities of  $\text{TiO}_2/\text{PEG PNC}$  towards

$^{134}\text{Cs}$  and  $^{60}\text{Co}$  were calculated to be  $163.28 \pm 10.98$ , and  $330.16 \pm 41.60 \text{ mg g}^{-1}$ , respectively at  $25^\circ\text{C}$ . The sorption capacity of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  onto  $\text{TiO}_2/\text{PEG PNC}$  and the energy of sorption increased with temperature. The available active sites of  $\text{TiO}_2/\text{PEG PNC}$  increase as the temperature is raised, consequently the sorption capacity will increase.

Also, the numerical of  $1/n < 1$  suggested that  $\text{TiO}_2/\text{PEG PNC}$  sorption reactions towards  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  are favorable.

From the tabulated parameters, comparing the correlation coefficients of Langmuir isotherm model ( $R^2 \geq 0.981$  for  $^{134}\text{Cs}$  and  $R^2 \geq 0.957$  for  $^{60}\text{Co}$  radionuclide) with the correlation coefficients of Freundlich isotherm model ( $R^2 \geq 0.98$  for  $^{134}\text{Cs}$  and  $R^2 \geq 0.98$  for  $^{60}\text{Co}$  radionuclide), indicating that the Freundlich isotherm model is more applicable.

Temkin model:

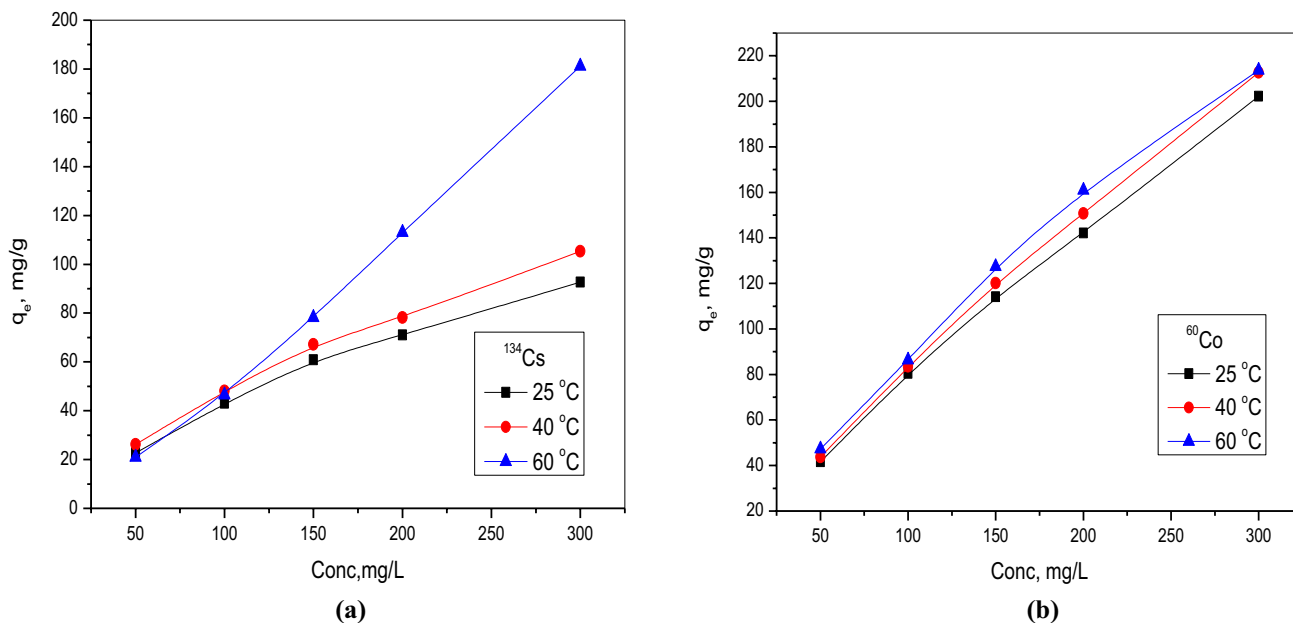
Temkin isotherm linear form is given by Eq. (6) [38].

$$q_e = RT \ln K_T + RT/b C_e \quad (6)$$

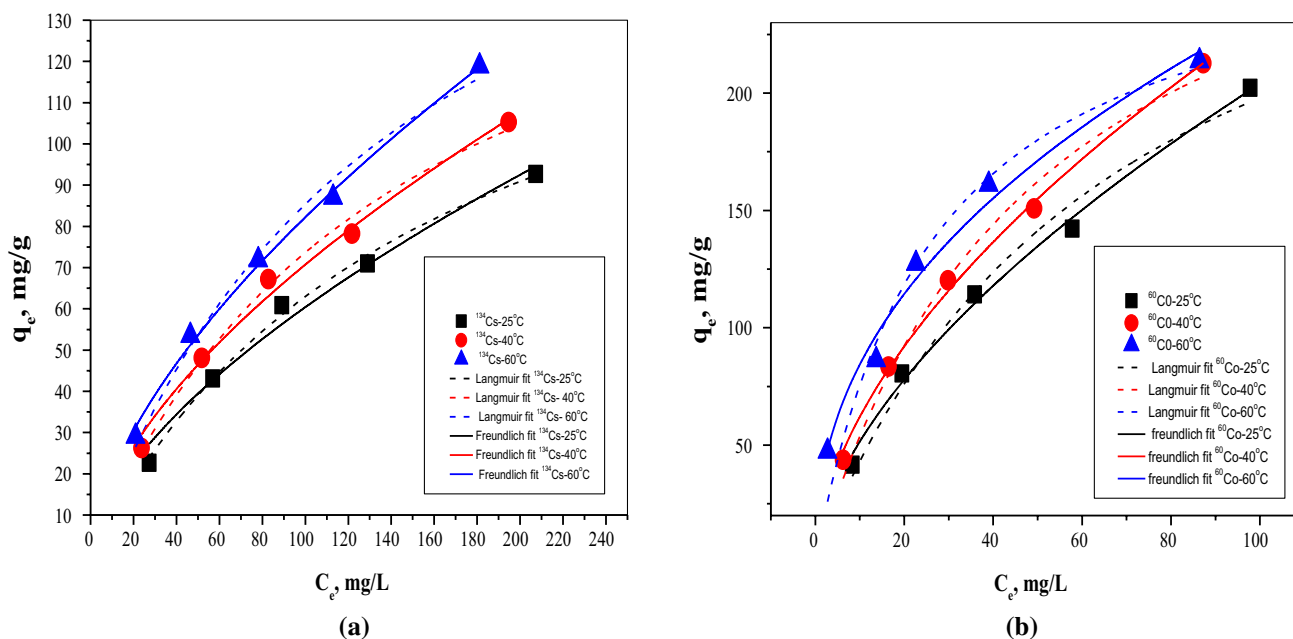
where,  $K_T$  is the equilibrium binding constant ( $\text{L mol}^{-1}$ ), the adsorption heat is ( $b$ ), Fig. 13 represents Temkin isotherm plot. Table 6 shows the values of parameters and  $R^2 \geq 0.96$  for  $^{134}\text{Cs}$  and  $\geq 0.92$  for  $^{60}\text{Co}$ .

### Effect of metal-ion Interference

The sorption interference of specific ions on  $\text{TiO}_2/\text{PEG PNC}$  was studied. The sorption mixture of Na (I), Sr (II) and Fe



**Fig. 11** Effect of metal ion concentrations on the amount sorbed of **a**  $^{134}\text{Cs}$  and **b**  $^{60}\text{Co}$  onto  $\text{TiO}_2/\text{PEG PNC}$  at pH 5, different temperatures, and  $V/m=200 \text{ mL/g}$



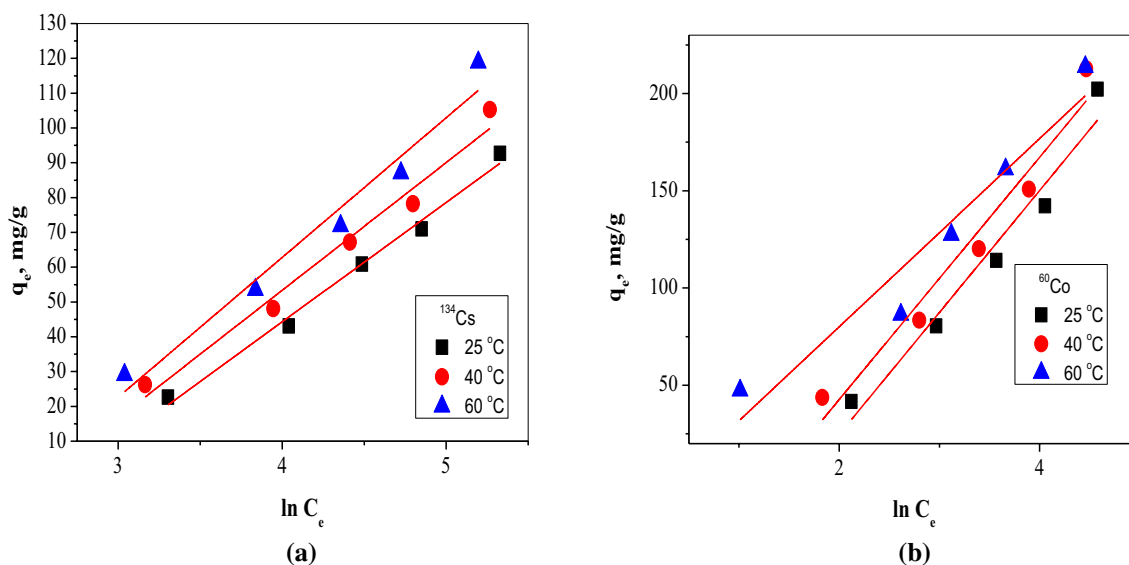
**Fig. 12** Non-linear form fitting of Langmuir isotherm and Freundlich models of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides sorption onto  $\text{TiO}_2/\text{PEG}$  PNC at different temperatures

**Table 5** The values of parameters of Langmuir and Freundlich isotherm models for adsorption ions onto  $\text{TiO}_2/\text{PEG}$  PNC:

Metal ion	Temperature (°C)	Langmuir isotherm model			Freundlich isotherm model		
		$Q^{\circ}$ (mg/g)	$B$ (L/mg)	$R^2$	$K_f$ (mg/g)	$n$	$R^2$
$^{134}\text{Cs}$	25	$163.28742 \pm 10.98998$	$0.00627 \pm 7.62406\text{E-}4$	0.9946	$3.56131 \pm 0.93513$	$1.62666 \pm 0.1433$	0.98
	40	$180.76351 \pm 15.5883$	$0.00688 \pm 0.00108$	0.9908	$4.31702 \pm 0.80847$	$1.64698 \pm 0.1061$	0.98
	60	$207.83712 \pm 22.50746$	$0.00697 \pm 0.00135$	0.9871	$4.80804 \pm 0.54776$	$1.62199 \pm 0.0634$	0.99
$^{60}\text{Co}$	25	$330.16995 \pm 41.60667$	$0.01497 \pm 0.00356$	0.9805	$12.98732 \pm 1.5734$	$1.67238 \pm 0.0824$	0.99
	40	$328.34516 \pm 34.84246$	$0.01955 \pm 0.00413$	0.9830	$16.74114 \pm 1.37129$	$1.75795 \pm 0.063$	0.99
	60	$275.25992 \pm 31.31084$	$0.0378 \pm 0.01064$	0.9576	$30.6344 \pm 4.2989$	$2.27373 \pm 0.188$	0.98

(III) were studied.; Contact time was 2 h with 0.05 g of sorbent dosage. It was shown that the presence of the monovalent, divalent and trivalent ions greatly affect the sorption of both  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides. The sorption capacities of  $\text{TiO}_2/\text{PEG}$  PNC towards  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  increase in the order the  $^{60}\text{Co} > ^{134}\text{Cs}$ . In presence of  $50 \text{ mg L}^{-1}$  of Sr (II),

the amount sorbed from  $83.3$  to  $9.5 \text{ mg g}^{-1}$  and from  $45.3$  to  $1.9 \text{ mg g}^{-1}$  for  $^{60}\text{Co}$  and  $^{134}\text{Cs}$ , respectively. This might be due to the influence of ionic potential and ionic radius [39]. Figure 14 represents the metal-ion interfering effect on  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides onto  $\text{TiO}_2/\text{PEG}$  PNC.



**Fig. 13** Temkin isotherm plots of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides sorption onto  $\text{TiO}_2/\text{PEG PNC}$  at different temperatures, pH 5 and  $V/m=200\text{ mL/g}$

**Table 6** The values of parameters of the Temkin isotherm model for  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides sorption onto  $\text{TiO}_2/\text{PEG PNC}$ :

Metal ion	Temperature (°C)	Temkin isotherm model		
		<i>b</i>	$K_T(\text{L mol}^{-1})$	$R^2$
$^{134}\text{Cs}$	25	$72.23 \pm 1.44$	$0.066 \pm 0.0005$	0.99
	40	$68.639 \pm 1.56$	$0.078 \pm 0.0007$	0.97
	60	$68.975 \pm 1.89$	$0.087 \pm 0.0008$	0.96
$^{60}\text{Co}$	25	$39.503 \pm 0.91$	$0.201 \pm 0.001$	0.95
	40	$40.444 \pm 0.95$	$0.268 \pm 0.004$	0.95
	60	$57.217 \pm 0.98$	$0.707 \pm 0.008$	0.92

### Thermodynamic studies

The sign of the free energy, ( $\Delta G^\circ$  kJ/mol, determines the favorability of the sorption process.  $\Delta G^\circ$  is calculated with Eq. (7) aid.

$$\Delta G^\circ = -RT \ln K_c \tag{7}$$

where, the universal gas constant is  $R$  ( $8.314\text{ J K}^{-1}\text{ mol}^{-1}$ ), Temperature is  $T$  (K), and the equilibrium constant of the

sorption process is  $K_c$ . The values of other thermodynamic parameters such as  $\Delta H^\circ$  (kJ/mol (and  $\Delta S^\circ$  (J/mol K) have been calculated using the following Eq. (8).

$$\ln K_c = \Delta S^\circ / R - \Delta H^\circ / RT \tag{8}$$

Figure 15 shows the plot between  $\ln K_c$  and  $1/T$ . The values of  $\Delta H^\circ$  are positive emphasize an endothermic sorption reaction of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides onto  $\text{TiO}_2/\text{PEG PNC}$  as shown in Table 7. Also, the positive values of  $\Delta S^\circ$  indicate an increase in the randomness at the sorbent/radionuclides interface and a good affinity of sorbents towards the radionuclide [40].

### Conclusion

$\text{TiO}_2/\text{PEG PNC}$  was successfully prepared by wet-chemical method and physic-chemically characterized by some analytical techniques such as (TEM), (FTIR), (XRD), (DTA-TGA), particle size distribution, and pore size analysis.  $\text{TiO}_2/\text{PEG PNC}$  used for sorption of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides from aqueous solutions at pH 5. The equilibrium was reached after about 30 min. Pseudo second order model is applicable with

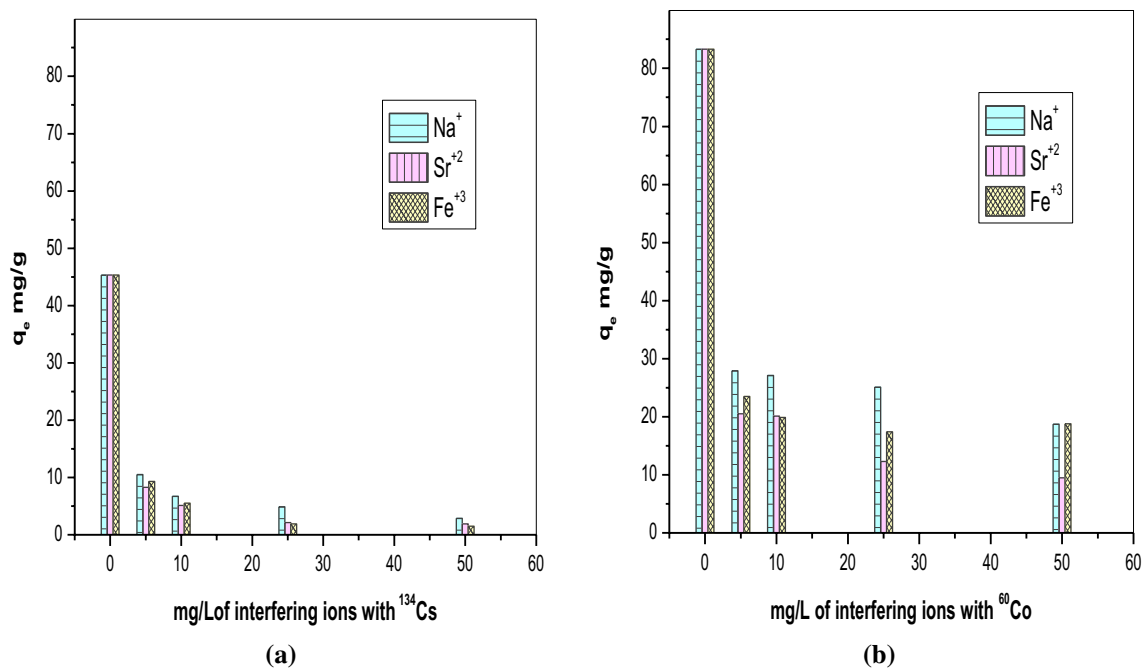


Fig. 14 Metal-ion interfering effect on a <sup>134</sup>Cs and b <sup>60</sup>Co radionuclides sorption onto TiO<sub>2</sub>/PEG PNC

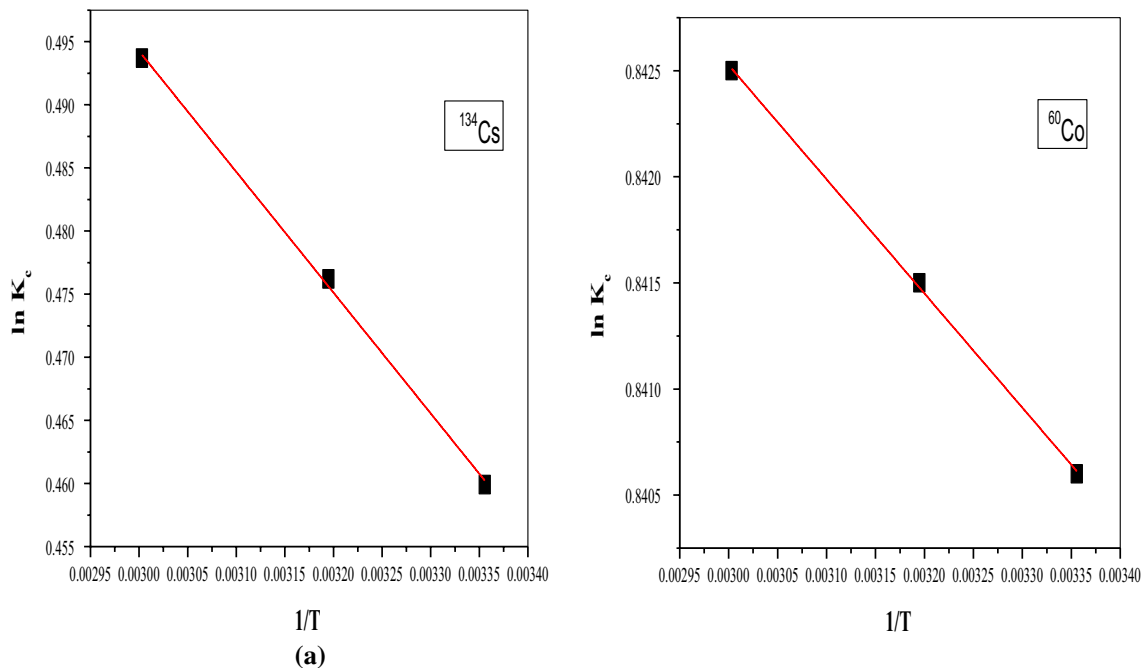


Fig. 15 Thermodynamic plot for the sorption of a <sup>134</sup>Cs and b <sup>60</sup>Co radionuclides onto TiO<sub>2</sub>/PEG PNC

**Table 7** Thermodynamic parameters for the sorption of <sup>134</sup>Cs and <sup>60</sup>Co radionuclides onto TiO<sub>2</sub>/PEG PNC:

Radionuclides	$\Delta G^\circ$ , J/mol			$\Delta H^\circ$ (J/mol)	$\Delta S^\circ$ , (J/mol K)
	298 K	313 K	333 K		
<sup>134</sup> Cs	$-1137 \pm 22.1$	$-1237.1 \pm 20.6$	$-1364 \pm 23.78$	$794.17 \pm 10.3$	$6.484 \pm 0.9$
<sup>134</sup> Co	$-2079 \pm 24.4$	$-2186 \pm 30.7$	$-2328 \pm 29.9$	$44.66 \pm 3.2$	$7.12 \pm 1.6$

the sorption reaction mechanism. The monolayer capacities (at pH 5 and 25 °C) of  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides on  $\text{TiO}_2/\text{PEG PNC}$  were found to be  $163.28 \pm 10.98$ , and  $330.16 \pm 41.60 \text{ mg g}^{-1}$ , respectively. The thermodynamic studies explain favorability and endothermic nature of the sorption process. Therefore,  $\text{TiO}_2/\text{PEG PNC}$  could be used as an efficient sorbent for  $^{134}\text{Cs}$  and  $^{60}\text{Co}$  radionuclides. The study demonstrates that interference with co-metals is an important factor for consideration in  $\text{TiO}_2/\text{PEG PNC}$  sorption application.

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