

Optimizing the Electricity Consumption with a High Degree of Flexibility Using a Dynamic Tariff and Stackelberg Game

Simona-Vasilica Oprea¹ · Adela Bâra¹ · George Adrian Ifrim²

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Abstract

Recent advancements in the sensor industry, smart metering systems and communication technology have led to interesting electricity consumption optimization opportunities that contribute to both peak reduction and bill savings and better integration of flexible appliances (including e-mobility). In combination with advanced tariffs, there has been a promising demand side management strategy devised from different perspectives: consumers interested in cost minimization, retailers and grid operators interested in peak minimization or hybrid solutions which reduce the costs to the extent of a certain peak level. In this paper, we propose an optimization algorithm that is significantly enhanced by a Stackelberg-type dynamic nonzero-sum game in which the consumers optimize and send their 24-h consumption schedules to the electricity retailer and receive the hourly tariff rates until their savings and the Flattening Index are maximized. Thus, it has been demonstrated that the oneiteration optimization is not as rewarding as the proposed game-optimization algorithm and that the results are heavily influenced by the degree of flexibility of the appliances. The algorithm is tested and validated using a large real input dataset, recorded at 15-min interval for a period of one year from a small residential community that consists of 11 modern houses with more than 300 appliances and high flexibility in terms of shifting, and the results highlight the consumers' gain, FI and peak to average ratio indicators.

Keywords Optimization algorithm · Game theory · Smart meters · Advanced tariff

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Simona-Vasilica Oprea simona.oprea@csie.ase.ro

¹ Department of Economic Informatics and Cybernetics, The Bucharest University of Economic Studies, no. 6 Piaţa Romană, Bucharest, Romania

² Department of Automatic Control and Electrical Engineering, Dunărea de Jos University, no. 47 Domnească, Galați, Romania

h	Hour, $h = \overline{1, 24}$
Н	Hour for shifting, $H = \overline{1, 24}$
A^h	Action or consumption of all consumers at hour h
A^h_{\cdot}	Hourly electricity consumption of a consumer <i>i</i>
A^{h}_{\cdots}	Hourly electricity consumption of an appliance <i>i</i> that belongs to con-
ij	sumer i
\mathbf{PA}^{h}	Hourly consumption of all programmable appliances that belong to con-
11 i	sumer <i>i</i>
PASW ^h	Hourly consumption of all shiftable without interruption appliances that
in o m _i	belong to consumer <i>i</i>
PASI ^h	Hourly consumption of all shiftable interruptible appliances that belong
i nor _i	to consumer i
MA.	Maximum hourly consumption imposed as a shifting condition to avoid
WIT L _i	new neaks
C.	Electricity cost for consumer <i>i</i>
C_i^0	Initial electricity cost for community (unontimized)
C^0	Initial electricity cost for consumer <i>i</i> (unoptimized)
	Daily cost of programmable interruptible appliance i
CW	Daily cost of programmable non-interruptible appliance i
CW CW	Daily cost for a possible shift of a non-interruptible appliance i
D_{A}	Daily exist for a possible sint of a non-interruption appriance <i>j</i>
TDA	Vector of total hourly consumption of all consumers
IDA	TDA $-\int \Delta h = \frac{1}{2} \frac{2h}{24}$
R	$DA = \{n, n = 1, 2\pi\}$ Consumer's <i>i</i> utility function
R R	Retailer's utility function
G G	Community gain
G	Consumer's gain
$h_{\text{offpeak_rate}}$	Tariff rate for off-neak hours
th _{peak_rate}	Tariff rate for peak hours
th _{shoulder_rate}	Tariff rate for day hours
$t^{h_{\text{rate}}}$	Tariff rate for a specific hour of consumption, $t^{h_{\text{rate}}} \in \{t^{h_{\text{peak}_{\text{rate}}}}, t^{h_{\text{offpeak}_{\text{rate}}}}\}$
	$t^{h}_{\text{shoulder_rate}}$
t ^h	Tariff rate for a specific hour of consumption that is a function of A^h
a. b. c	Coefficients of the tariff rate
DSM	Demand side management
FI	Flattening index
k.	Vector of the operating hours of appliance <i>i</i>
α	Vector of the hourly consumption of appliance <i>i</i>
Lk.	Length of vector k, representing the total operating hours of appliance i
PAR	Peak to average ratio
k_{a}^{h}	Vector of hours from which consumption of an interruptible appliance
SI	will be shifted
NPA	Non-programmable appliance
NPA ^h	Hourly total consumption of all NPA for consumer <i>i</i>
i	

Abbreviations

RES	Renewable energy sources
N_i^h	Hourly total consumption of NPA for consumer <i>i</i>
sN_i	Sorted N _i
PA	Programmable appliance that can be an interruptible or non-interruptible
	appliance
$PACM_i$	Constraints matrix $(24xm)$ for PA of consumer <i>i</i>
PACM ^h	Element of matrix PACM,
SI	Shiftable interruptible appliance
SI,	Matrix of SI appliances of consumer <i>i</i>
SI_{ii}^{h}	Element of matrix SI,
tSI_i	Temporary matrix of SI appliances of consumer <i>i</i>
ŚŴ	Shiftable without interruption or non-interruptible appliance
SW_{ii}^h	Hourly consumption of a SW appliance
SWA _{ii}	Matrix with all possible shifts of an appliance <i>j</i>
SWA ^h _{iiH}	Element of matrix SWA _{ii}
ToU	Time-of-use tariff
th	Threshold for shifting
j	A programmable appliance
j_{mCW}	SW Appliance with the lowest cost selected for shifting
j_{mCI}	SI appliance with the lowest cost selected for shifting
m	Number of PA
m_{SW}	Number of SW appliances
m _{SI}	Number of SI appliances
mCW	Minimum cost of SW
mCI	Minimum cost of a SI appliance
n	Number of consumers
niter	Number of iterations, iter = $\overline{1, \text{niter}}$
DLC	Direct load control
MILP	Mixed integer linear programming
IoT	Internet of Things
DER	Distributed energy resources
EV	Electric vehicle

1 Introduction

To avoid the onerous demands on power plants at peak, imbalances between electricity generation and consumption, and also costly grid investment, retailers and even grid operators [26] conceive advanced tariffs to encourage the consumer to shift flexible appliances and significantly improve PAR and FI indicators. They are usually nonlinear cost functions that ensure consistent lower bounds and a profit for the designers [8] or related to the contribution of the consumer to the peak/off-peak consumption [20]. Thus, the consumers are motivated to optimize their electricity consumption as long as their savings are substantial. On the one hand, a *fixed* time-of-use (ToU) tariff that probably does not always follow the load curve is not an efficient tool especially on the mid-run and long run [6], because it does not overlap with the inherent changes in consumers' behavior. The lack of overlapping between daily load curve and a *fixed* ToU tariff is frequent as the load curve varies for seasonal reasons. It is even more frequent from region to region because ToU tariff peak and off-peak rates are calculated considering peak and off-peak hours at the national level. However, regional load shape could be different as the peak takes place at different time intervals (hours) than at the national level. On the other hand, a *flexible* over time or dynamic tariff that is adjusted according to the consumption level has the potential to stimulate consumers to shift the operation of their appliances to the lower tariff rates [29].

Nonetheless, when a high degree of flexibility is available, there are some risks to be encountered such as the swaying of the appliances from peak to off-peak hours. These situations can be handled by providing a constraint matrix or, in its absence, the shifting condition needs to be adapted to avoid the incidence of new peaks. The shifting condition could be true as long as the new peak is lower than daily average consumption. Consequently, massively swaying the appliances from peak to off-peak hours is prevented. Most of the research studies do not address this issue as they usually consider a small number of flexible appliances.

In a classic optimization process, the operation of the flexible appliances is shifted in one iteration only according to a fixed ToU tariff [14–16, 21–23]. On the other hand, in a game-optimization process, the tariff is created daily based on the total consumption schedule of the community that represents a signal and the consumers optimize the consumption using local computational resources [17, 18] or even mobile phones. Then, they send the schedules to the retailer, who recomputes the tariff according to the new total consumption and so on, until there is no shift that improves the utility functions of both consumers and retailer [2–4, 17, 18, 30].

The two approaches have advantages and disadvantages, yet the benefits of the game-optimization process prevail. The main advantages of the first, classic approach, are its simplicity and the low computational requirements, while the advantage of the second, game-optimization approach, consists in being more transparent for consumers and bringing more incentives for shifting and adjusting the tariff to maximize FI. Thus, the second approach is more complex, but the optimization in multiple iterations could be an automatic process that uses machine learning with direct load control (DLC) [7], Internet of Things (IoT) and other mechanisms that ease the process and improve its effectiveness.

In this paper, we propose an optimization algorithm enhanced by an advanced tariff and a Stackelberg-type dynamic nonzero-sum game which emphasizes significant insights into the flexibility degree of the appliances as we use in simulation a large real consumption dataset from 11 complex and modern houses with a high degree of flexibility. The proposed algorithm minimizes the consumers' cost and avoids the creation of new peaks that could appear as a consequence of the high degree of flexibility.

The current paper is structured in five main sections as follows: the first section is an introduction regarding the goal of our research, and the second section is a literature review briefly describing the current stare-of-art. In the third section, we propose a game theory approach to iteratively optimize the electricity consumption and avoid new peaks. The fourth and fifth sections are organized around simulations, results and conclusion, respectively.

2 Literature Survey

Game theory in the consumption optimization process has previously been approached from various perspectives. Optimization problems using game theory are studied in [1, 3–5, 13, 14, 25]. Usually, the privacy of the consumers is assured by a minimal information exchange between consumers and retailer as the retailer does not need to know sensitive information about consumers' preferences and appliances. The proposed solutions in similar, previous research, decreases the cost, but the results show a lack of validation, as they are not extended for a longer interval (e.g., a one-year period). For instance, one day of simulation with a built scenario including a high energy demand is presented in [4]. In our study, the sensitive information related to consumers' preferences and detailed consumption of appliances are not revealed as the optimization is performed at the consumers' level. Furthermore, the proposed algorithm is tested and validated using a large dataset of records and its implementation is performed for one day and also for one year, thus proving the sustainability of the results.

An interesting game-optimization study using a community storage facility is carried out in [8] showing a cost reduction of almost 10% and also a significant PAR reduction with a hybrid combination of a real-time and ToU tariff. Since each consumer is modeled in the laboratory with a small number of appliances and constrained operation hours, the swaying effect discussed in our paper is ignored. The results given for a winter and summer day are chosen as representative. However, aspects related to the flexibility degree of the appliances and the implementation of the solution are not disclosed in similar studies, including [8].

A one-leader, as a virtual supplier, and *n* followers, as electricity consumers, represent the players of a Stackelberg game to identify the optimal consumption strategy [30]. A real-time price system is implemented to perform simulations. Although the daily payment has been reduced by almost 21%, the results lack validation as the simulations are not repeated for a longer period. Furthermore, the simulation included only a few appliances that are easily handled at the centralized level of the retailer, while an increasing number could lead to significant delays. Also, the swaying effect of appliances from peak to off-peak hours that could occur in real operation is not considered in [5, 30].

Several types of Stackelberg nonzero-sum game, theory and applicability of this game are described in [24], emphasizing their static and dynamic perspectives. This early study highlighted valuable conclusions regarding Stackelberg strategy, conditions for the existence of Stackelberg solution and the relation with Nash solution. Also, for a dynamic game, the conditions for the existence of a Stackelberg solution are identified. A couple of examples are presented to demonstrate the solution concept.

Moreover, the Stackelberg game models the interactions between distributed energy resources (DER) owners and an aggregator [15], comparing two ways of

DER owners participation in the wholesale electricity market: direct participation or via an aggregator and quantifying the benefits of using the price of aggregation. The results demonstrated that DER owners are better-off if they cooperate with an aggregator due to its profit-maximizing strategy. By comparison, in our paper, it is shown that the consumers benefit more from interacting with the electricity aggregator or retailer.

A mixed integer linear programming (MILP) problem using a game theory approach is solved in [2], focusing on the communication packet error rate on the optimization process. The results show interesting insights into the impact of the communication issues on the actions of the consumers and retailer. Also, MILP problems with a signaling game integrating local RES are approached in [31]. Its drawback is that it considers a limited number of appliances and a small testing interval of analyses that have not been extended over a longer period.

A game model that includes the EVs charging schedule and the impact on the electricity price are analyzed in [17, 18]. The optimal schedule of EVs using the driving data from the Danish National Travel Surveys considers the battery loading at low-consumption hours leading to a reduced PAR. This research focused more on the randomness of the EV charging schedule [27] and proved to be robust to price forecast errors. To increase the efficiency, DLC managing flexible appliances such as air-conditioning and heating systems could be embedded in DSM [19] using game-optimization algorithms [11, 12]. Such a DLC method, with a multi-objective particle swarm optimization algorithm, calculates multiple local optimization solutions [7] and has been tested at the experimental level using a simulator. With this method, the consumption is not only shifted, but also reduced by means of DLC. A difference between this study and the current research is that non-programmable appliances, for example, refrigerators, freezers (using their cooling inertia) and lighting are considered controllable. We took such appliances as non-controllable since the consumers' acceptance to control such appliances might be limited; thus, their potential to reduce the costs was not taken into account. Furthermore, another advantage of our study consists in splitting the programmable appliances into interruptible and non-interruptible ones. This approach is realistic as some appliances are shiftable, but they do not support interruption.

With consideration to the points raised above, in this paper, we propose an optimization algorithm enhanced by an advanced flexible tariff and a Stackelberg-type dynamic nonzero-game that increases the optimization potential of the consumers. Our main contributions are:

- A game-optimization algorithm that maximizes FI that represents the utility function of the retailer using flexible tariff rates that depends on the community hourly consumption;
- A cost optimization algorithm that minimizes the daily electricity cost considering both interruptible and non-interruptible programmable appliances and calculates the optimal consumption schedules;
- Involving numerous flexible appliances from real consumption dataset that can have various restricted operation hours that may lead to swaying effect of appliances from peak to off-peak hours depending on the hourly tariff rate. Such

effect is discussed and handled with an additional shifting condition to prevent the occurrence of new peaks;

- The proposed optimization mechanism is transparent to the consumers, provides incentives for shifting programmable appliances and does not disclose sensitive information regarding the consumers' privacy (preferences and consumption details) as the optimization takes place at the consumers' level;
- The algorithm is tested and validated with a large dataset recorded for one year.

3 Game Theory Approach

A game is usually characterized by several elements: *players*—electricity residential consumers, that forms a community, and retailer; *actions* or decisions or strategies regarding the consumption level and tariffs; *rewards* or utility functions that can be related to the electricity cost or the peak related indicators. The game *equilibrium* is found when a set of actions is better than any other set of actions leading to the end of the game. Thus, a Stackelberg-type dynamic nonzero-sum game explains the interaction between a retailer and the electricity consumers as shown in Fig. 1 and in the following paragraphs.

Most of the time, the optimization is performed in one iteration: the retailer conceives the tariff and the consumers optimize the consumption accordingly. But the advanced charging system has been created dependent on the total consumption level; thus, it is unlikely to get the minimum electricity cost at the first iteration of the optimization process. Considering that the consumers behave rationally, they will continue to optimize the operating schedule of their appliances as long as the cost declines. Also, using a quadratic cost function, the retailer adjusts the tariff rates at the consumption level in order to flatten the peak.

A Stackelberg-type dynamic nonzero-sum game in which the strategies are announced sequentially describes the iterative interactions between players: the consumers, on the one hand, as followers and electricity retailer as leader, on the other hand. The leader has a tariff structure that is calculated according to the



Fig. 1 Flows between electricity consumers and retailer

consumption forecast. In this game, considering the initial tariff structure, the consumers send the initial consumption schedules (not optimized) to the retailer, who aggregates the total consumption, calculates the hourly tariff rates based on the community's hourly consumption and sends them to the consumers. The strategy of the leader consists in a set of messages sent as an array of tariffs: $ToU = \{t^{h_{rate}}\}, \forall h = \overline{1, 24}$. The consumers will play or act according to the tariff that is sent by the retailer. Then, the consumers will reschedule their programmable appliances (taking actions) according to the tariff rates to lower the electricity cost. The strategy of the consumer consists in the hourly consumption vector, DA_i that represents the daily actions of a consumer *i*. Thus, the utility functions are defined for both leader and followers: $R_{ret}(TDA, ToU)$ and $R_i(DA_i, ToU)$, where TDA is the total daily actions. Therefore, the retailer will devise the tariff signal to flatten the peak and encourage the consumers to shift the operation of their appliances to those hours with lower rates.

The optimization problem is formulated for both retailer and consumers to select the optimal strategy in the following paragraphs.

A. The strategy of the retailer is to create tariff rates to minimize the peak consumption.

Considering that each consumer has a specific hourly consumption A_i^h , the array of the hourly consumption for an interval of 24 h represents the DA_i. Thus, the sum of the hourly actions of all consumers represents the total consumption that a retailer should provide:

$$TDA = \left\{ A^h | A^h \in \mathbb{R}, A^h \ge 0 \right\}, \ \forall h = \overline{1, 24}$$

$$\tag{1}$$

where A^h is the total consumption of all consumers at hour *h*.

$$A^{h} = A_{1}^{h} + A_{2}^{h} + \dots + A_{n}^{h} = \sum_{i=1}^{n} A_{i}^{h}$$
(2)

Consequently, TDA is obtained by adding up DA_i of all consumers; thus, the retailer's utility function (R_{ret}) is to minimize the peak consumption of the community.

$$R_{\text{ret}}(\text{TDA}, \text{ToU}) = \min\left(\max\left(A^{h}\right)\right), \forall h = \overline{1, 24}$$
(3)

A couple of indicators are calculated to measure the retailer's reward and the performance of the proposed algorithm. FI is the ratio between the average consumption and the consumption at peak, whereas PAR is the ratio between the squared consumption at peak and the squared mean consumption. Thus, the retailer's utility function can be assimilated with the peak reduction that is described by the two indicators: FI and PAR.

$$FI = \frac{\left(\sum_{h=1}^{24} A^{h}\right) / 24}{\max_{h=1,24} A^{h}}$$
(4)

$$PAR = \frac{\left(\max_{h=1,24} A^{h}\right)^{2}}{\left(\left(\sum_{h=1}^{24} A^{h}\right)/24\right)^{2}}$$
(5)

The optimization objective for the retailer in case of FI indicator can be expressed as follows:

$$\max R_{\rm ref}({\rm TDA},{\rm ToU}) = \max {\rm FI}$$
(6)

The peak minimization that is measured by FI is obtained by applying a ToU tariff that influences the hourly consumption of the community A^h .

The fixed ToU tariffs have been implemented at the beginning of the DSM strategies [9]. At most, they have performed well in the first months of implementation; then, they have failed to improve the demand response because the shape of the tariff and the load curve differ significantly as a consequence of the consumers changing their behavior. Therefore, a flexible design of ToU tariff is defined as a quadratic cost function depending on the hourly consumption:

$$t^{h} = f\left(A^{h}\right) = a \times \left(A^{h}\right)^{2} + b \times A^{h} + c \tag{7}$$

where *a*, *b*, *c* are coefficients characteristic for the residential consumers. The typical values for these coefficients are: a = 0.00295, b = -0.0417 and c = 0.711, but they are slightly adjusted according to the consumption level and market price [10].

Using (7), we have set the rates depending on the hourly consumption of the community at peak, day and off-peak hours. The tariff vector ToU has three components corresponding to peak, off-peak and the remaining hours. The peak tariff rate is calculated as the average of tariff rates t^h for peak hours (between 17 and 21) extracted from the load curve. The off-peak tariff rate is calculated as the average of tariff rates t^h for off-peak hours (between 1 and 4, and 24). The shoulder tariff rate is calculated as the average of tariff rates t^h for the remaining hours.

$$\text{ToU} = \left\{ t^{h_{\text{rate}}} \middle| t^{h_{\text{rate}}} > 0, \ t^{h_{\text{rate}}} \in \left\{ t^{h_{\text{peak_rate}}}, t^{h_{\text{offpeak_rate}}}, t^{h_{\text{shoulder_rate}}} \right\} \right\}, \ \forall \ h = \overline{1, 24}$$
(8)

$$t^{h_{\text{offpeak}_{rate}}} = \text{mean}(t^h), \forall h = \overline{1, 4} \text{ and } h = 24$$
 (9)

$$t^{h_{\text{shoulder_rate}}} = \text{mean}(t^{h}), \forall h = \overline{5, 16} \text{ and } h = \overline{22, 23}$$
 (10)

$$t^{h_{\text{peak_rate}}} = \text{mean}(t^{h}), \forall h = \overline{17, 21}$$
(11)

Deringer

Thus, the feasible strategy set of the retailer is represented by the vector of ToU tariff calculated according to (7-11).

B. The equilibrium strategy of the consumer is to minimize the daily electricity cost by choosing a set of strategies represented by the hourly consumption A_i^h given the tariff rates sent by the retailer. Based on the tariff rate $t^{h_{rate}}$, the electricity cost for a consumer *i* is given by the following equation:

$$C_i = \sum_{h=1}^{24} A_i^h \times t^{h_{\text{rate}}}$$
(12)

where C_i —the electricity cost for a consumer *i*;

 $t^{h_{\text{rate}}}$ the tariff rate for a specific hour of consumption.

Thus, the consumer's utility function or reward R_i :

$$R_i(\mathrm{DA}_i, \mathrm{ToU}) = C_i = \sum_{h=1}^{24} A_i^h \times t^{h_{\mathrm{rate}}}, \forall i = \overline{1, n}$$
(13)

where *n* is the number of consumers.

The action (strategy) of a consumer *i* for hour *h*, A_i^h , consists in the consumption of all appliances that operate at a specific hour *h*.

$$A_i^h = NPA_i^h + PA_i^h \tag{14}$$

The appliances are classified into: non-programmable appliances (NPAs) and programmable appliances (PAs). For optimization purposes, PAs are further classified into shiftable interruptible (SI) and shiftable without interruption (SW) appliances. Thus, the operation of SW cannot be split over non-consecutive hours due to their intrinsic characteristics.

$$PA_i^h = PASI_i^h + PASW_i^h = \sum_{j=1}^m A_{ij}^h$$
(15)

$$A_{i}^{h} = NPA_{i}^{h} + \sum_{j=1}^{m} A_{ij}^{h}$$
(16)

One of SW is the washing machine since once it starts, it has to operate until the washing program finishes; otherwise, the clothing could become stale in the tub or some machines simply do not allow the interruption. Among PAs, SI appliances are usually more numerous and more flexible for shifting. NPAs are usually considered as total. Although NPAs do not shift, they are an important segment of the hourly consumption that must be part of the optimization process.

The electricity consumption optimization process starts with the modeling of the set of constraints. The consumption operating hours of PA are set by the consumers. It forms the programmable appliances constraints matrix $PACM_i$, defined by each consumer *i*.

$$PACM_{i} = \left\{ PACM_{ij}^{h} \right\}, \ \forall i = \overline{1, n}; \ j = \overline{1, m}; \ h = \overline{1, 24}$$
(17)

$$PACM_{ii}^h \in \{0, 1\}$$

where 1 means that the appliance *j* can operate at hour *h*, and 0 otherwise.

Each consumer aims to minimize his daily cost under the constraints imposed by the operating conditions of the appliances defined in the matrix $PACM_i$. Therefore, the optimization objective can be expressed as follows:

$$\min R_i (\mathrm{DA}_i, \mathrm{ToU}) = \min C_i = \min \sum_{h=1}^{24} A_i^h \times t^{h_{\mathrm{rate}}}, \forall i = \overline{1, n}$$
(18)

The feasible strategy set of each consumer *i* is represented by $DA_i = \{A_i^h | A_i^h \in \mathbb{R}, A_i^h \ge 0\}$, where A_i^h is calculated according to (16), each appliance *j* being restricted by PACM_{ij}^h \in \{0, 1\}.

To measure the cost reduction at each iteration of the game, relative to the initial unoptimized schedule, the consumer's gain (G_i) (as the percentage of the cost reduction) can be calculated at the consumer level.

$$G_i = 100 - \frac{C_i \times 100}{C_i^0}$$
(19)

Furthermore, the cost reduction or the consumers' gain (G) at the community level is the percentage of the aggregated cost reduction relative to the unoptimized schedule.

$$G = 100 - \frac{\sum_{i=1}^{n} C_i \times 100}{\sum_{i=1}^{n} C_i^0}$$
(20)

where C_i^0 is the initial cost and C_i is the cost after the optimization for consumer *i*.

The community gain is also important for the retailer as it highlights the satisfaction of the consumers.

Stackelberg strategy is the optimal strategy for the retailer (leader) if the consumers schedule their appliances optimally. Thus, the Stackelberg equilibrium is attained in an iterative exchange of messages that stops when the leader finds the best combination of ToU tariff rates that maximizes his utility function and provides the optimal operation solution for programmable appliances. The leader strategy that is to maximize FI is the leader's equilibrium strategy. Then, the followers minimize their daily costs by choosing the best response to the leader's equilibrium strategy that is the optimal operation of the programmable appliances. Thus, the Stackelberg equilibrium is characterized by both optimal strategies from which players do not deviate. Let us denote the optimal set of strategies (*) as:

$$(ToU^*, TDA^*) = \arg \max R_{ret}(TDA, ToU),$$
 (21)

$$TDA^* = \left\{ A^{(*)h} | A^{(*)h} = \sum_{i=1}^n A_i^{(*)h} \right\}, \forall h = \overline{1, 24},$$
(22)

$$A_i^{(*)h} = \arg\min R_i (\mathrm{DA}_i, \mathrm{ToU}) = \arg\min \sum_{h=1}^{24} A_i^h \times t^{\mathrm{h_{rate}}}, \forall i = \overline{1, n},$$
(23)

To summarize, the consumers send their daily consumption schedule (not optimized) to the retailer that created an initial tariff structure. Considering the aggregated consumers' schedules, the retailer computes the tariff rates and sends them to the consumers. Each consumer minimizes the cost and obtains the optimal daily consumption schedule. If it is different from the previous schedule, it is sent to the retailer that computes a new tariff until maximum value of FI is obtained in a definite number of iterations established by retailer. This mechanism is explained in detail in Sects. 3.1 and 3.2.

3.1 Cost Minimization Algorithm

The cost optimization algorithm is built upon the community day-ahead optimization algorithms [23]. The significant difference consists in the objective function of the algorithms and the iterative process proposed in the current research. The community day-ahead optimization algorithms in [23] target the flattening of the electricity consumption vector by shifting the consumption of the programmable appliances toward the hours less loaded and, when several fixed ToU tariffs are implemented, the reduction of the electricity cost is also achieved. The newly developed cost minimization algorithm aims to obtain the lowest cost for the consumers by shifting the consumption toward the hours with the cheapest rates. The off-peak $t^{h_{offpeak,rate}}$, shoulder $t^{h_{shoulder,rate}}$ and peak rates $t^{h_{peak,rate}}$ are iteratively calculated with the dynamic ToU tariff described in (7)–(11). The higher the hourly consumption, the higher the rate; thus, the flattening of the consumption vector is a result of the tariff rates.

The cost optimization algorithm is designed to manage the programmable appliances: both the non-interruptible (SW) and the interruptible ones (SI).

3.1.1 Optimization Algorithm for SW

The cost optimization algorithm for SW shifts the consumption to lower rate hours so that the consumer *i* obtains the lowest cost, by following the next steps:

- 1. *Define the input block.* The algorithm extracts for each house (consumer) *i* the following input:
 - The vector with the total hourly consumption of NPA for consumer *i*, NPA_i^h \in NPA_i, with $h = \overline{1, 24}$ and $i = \overline{1, n}$. Let us consider N_i a vector with the hourly consumption of the appliances that will not be further rescheduled.

Initially, N_i sums the consumption of all NPA because they cannot be shifted. Then, other appliances will be added after their optimal operation schedule is calculated; thus, they will not be further rescheduled.

- The matrix with the consumption of programmable non-interruptible appliances, SW_i, with SW^h_{ij} \in SW_i, $h = \overline{1, 24}$, $i = \overline{1, n}$ and $j = \overline{1, m_{SW}}$. The algorithm for SW runs first because they are more restricted (as they have more operation constraints). SW are not allowed to operate at any hour due to constraints imposed by the consumer. Thus, to find the optimal solution, PACMⁱ_i constraints matrix, with elements PACM^h_{ij} $\in \{0, 1\}$, has to be provided by each consumer *i* depending of their preferences.
- 2. Generate all possible shifts of an appliance *j*. The first appliance in SW is selected and all possible shifts are generated through a circular shift function. Therefore, there are 24 possibilities denoted by $H = \overline{1, 24}$, but not all are feasible because of the constraints included into PACM_i. The combinations that are not feasible are replaced with non-numeric elements. This creates a new matrix, SWA_{ij}, with SWA^h_{iiH} \in SWA_{ij} with 24×24 dimension.
- 3. Calculate the cost of all possible shifts of an appliance *j*. For each shift in SWA_{*ij*}, the cost is calculated using the tariff rates. The hourly costs are summed to obtain the daily cost for each possible shift. Thus, a vector CW_{*ijH*} that has the dimension 1×24 is obtained (also without numeric elements for the unfeasible shifts): $\frac{24}{24}$

$$CW_{ijH} = \sum_{h=1}^{n} SWA_{ijH}^{h} \times t^{h_{rate}}, \forall h, H = \overline{1, 24}.$$

- 4. *Calculate the minimum cost.* Steps 2 and 3 are repeated until the daily cost of all *SW* is calculated. By adding a row for each appliance *j*, we obtain a matrix with $m_{SW} \times 24$ dimension. The lowest cost from CW_{*ijH*} is calculated as mCW and the appliance with the lowest cost, j_{mCW} , is selected for shifting. The best feasible solution is the one with the consumption at the lower rate hours.
- 5. Update SW_i and N_i. The appliance that gave the minimum cost at the previous step is added to matrix N_i and removed from the matrix SW_i. The new SW_i matrix has the dimension $(m_{SW} 1) \times 24$.
- 6. *Return to step 2*. The optimization process is repeated until SW_i is dimensionless (or has no numerical elements).

To have a better view on its implementation, Fig. 2 shows the flowchart of the cost optimization algorithm for SW.

3.1.2 Optimization Algorithm for SI

After the consumption of all SW is optimized, SI appliances are processed. The algorithm for SI shifts the electrical consumption at the hours with the lowest rate, by following the next steps for each consumer *i*:

1. Define the input block—it is the same as described above and can be a common step for both types of *PA*. Besides the NPA and SW, a matrix with the consumption of *SI* for consumer *i*, SI_{*i*}, $(SI_{ii}^h \in SI_i, j = \overline{1, m_{SI}})$ must be extracted.



Fig. 2 The flowchart of the cost optimization algorithm for SW

2. Find the consumption of appliance *j* from SI_{*i*}. The algorithm must find the initial scheduled hours for appliance *j* in order to shift its consumption. To avoid shifting exceptionally low consumptions, a threshold, th, can be defined here (SI^{*h*}_{*ii*} > th).



Fig. 3 The flowchart of the cost optimization algorithm for the SI

 k_j is the vector that holds the hours from which appliance j will be shifted and α_j is the vector of the consumption of j for the scheduled hours.

- 3. Sort vector N_i and ToU. The vector with the total hourly consumption of the NPA and the optimal operation schedule of SW (denoted with N_i in Sect. 3.1.1) must be sorted by the lowest rate of ToU. Since there are only three rates (i.e., off-peak, shoulder and peak rates), the vector N_i and ToU can be double sorted in ascending order. This way, the consumption of SI is first shifted at the hour with the lowest consumption of the lowest rate. The sorted vector N_i will be denoted sN_i .
- 4. Shift appliance j according to the matrix $PACM_i$. Because not all hours are feasible, the $PACM_i$ will be verified before shifting. The consumption of appliance j from α_j will be shifted if $PACM_{ij}^h = 1$ where h represents the first available hour in sN_i . This step continues for all hours in k_j meaning that it will be repeated Lk_j times, where Lk_j is the length of vector k_j . If there is no feasible solution for shifting the appliance j, its consumption remains unshifted. At this step, a temporary matrix tSI_i will hold the shifted consumption.
- 5. *Calculate the cost for appliance j*. Based on the same tariff rates, the cost of the newly shifted consumption is calculated. The resulted hourly costs are summed up, and the daily cost for *j* is obtained as CI_{*ii*}.
- 6. Find the minimum cost. The cost is calculated for each appliance and concatenated, CI_{ij} becoming a vector of $1 \times m_{SI}$. This is done by repeating the steps 2 to 5 for each appliance. The minimum of CI_{ij} (mCI) can then be found, meaning that the appliance that has the lowest cost will be shifted first.
- 7. Update N_i and SI_i . The appliance that has been shifted is added to the matrix N_i and removed from SI_i .
- 8. *Return to step 2*. The optimization process is reiterated until the SI_i is dimensionless (or until it has no numerical elements).

For a detailed illustration, Fig. 3 presents the optimization algorithm of SI.

3.2 Game-Optimization Algorithm

The results of the cost optimization algorithm are iteratively enhanced by the flexible ToU tariff calculated according to (7)–(11) implemented in a game theory approach. Since the cost optimization algorithm shifts the consumption of the PA toward the hours with the lowest rates, new peaks could be created if the flexibility degree of the PA is high. The search of the optimal solution should be thus constrained, based on the consumers' preferences or on retailer's capacity to obtain the flattened consumption vector for which he is willing to offer cost reductions. The cost optimization algorithm is run individually, for each house. Thus, the sensitive consumption data are not disclosed, and the optimization process is more transparent for consumers. Since the tariff is devised as a function of the consumption level of the community, the community cost reduction (G) is monitored. Consequently, the optimization algorithm performs the following steps:



Fig. 4 The flowchart or the game-optimization algorithm

1. *Define the input block*—the game theory algorithm requires the vector of hourly consumption of all consumers, TDA, which is the sum of the daily action arrays



Fig. 5 The structure of the appliances at house level (a) and community level (b)



Fig. 6 The number of appliances at house level (a) and monthly community consumption level (b)

 (DA_i) that is initially unoptimized and coefficients, *a*, *b*, *c* for the tariff function. The retailer imposes a maxim number of iterations—*niter*.

- 2. Calculate the initial tariff rates, cost, FI and PAR. Based on the TDA previously calculated, the initial tariff rates and cost of the unoptimized dataset, C^0 , are calculated. The FI and PAR are also calculated on the unoptimized total consumption vector.
- 3. Optimize the cost of each house (consumer) *i*. The optimization algorithm for each house in the community performs the optimization individually. The optimization minimizes the electricity costs using the ToU tariff built upon the initial TDA and calculates the individual gains G_i , using (19).



Fig. 7 The typical daily load curve at the community level

- 4. *Calculate the new* TDA. The retailer aggregates the optimized consumption of each house, obtaining the new vector TDA.
- 5. *Calculate FI*. The *FI* and *PAR* are calculated (using (14) and (15)) on the new optimized TDA to evaluate the degree of flattening obtained after optimization. Also, to measure the community cost reduction and evaluate the consumers' satisfaction, the community gain, *G*, is calculated using (20).
- 6. *Return to step 2*. The optimization is repeated until the leader equilibrium strategy is obtained meaning that FI is maximized. For this strategy, the followers' equilibrium strategy is also obtained as their daily consumption is optimized according to the algorithm proposed in Sects. 3.1.1 and 3.1.2. The flowchart of the game-optimization algorithm is presented in Fig. 4.

The game-optimization algorithm is implemented, and the performance indicators defined in (4), (5), (19), (20) are calculated.



Fig. 8 The total consumption of the community before (left) and after (right) optimization on 24-h datasets with no constraints on the PA shifting hours

Table 1 T	he gains after	the optimiza	tion of a 2.	4-h datas(et with n	to constrai	nt									
Iteration	foffpeak_rate	$t^{\rm shoulder_rate}$	tpeak_rate	G	FI	$G_{ m A}$	$G_{\rm B}$	$G_{\rm C}$	G_D	$G_{\rm E}$	$G_{\rm F}$	G_G	$G_{\rm H}$	$G_{\rm I}$	GJ	$G_{\rm K}$
1	0.19	0.23	0.56	25.28	0.51	3.74	25.73	1.06	13.28	16.19	39.92	16.02	7.38	2.17	43.14	42.89
2	0.61	0.21	0.20	31.96	0.43	10.42	26.18	16.25	34.40	21.53	46.14	19.02	22.07	1.32	49.87	46.54
3	0.19	0.21	0.81	18.43	0.45	-2.58	24.63	-17.26	0.42	4.17	34.48	11.42	-4.75	- 6.08	37.71	38.48
4	0.67	0.21	0.19	31.75	0.42	9.62	26.08	13.87	34.46	19.44	46.00	20.99	21.52	-0.89	49.98	46.51
5	0.19	0.21	0.88	15.39	0.47	-4.75	23.19	-22.87	-3.74	0.51	33.41	2.73	-8.47	-8.30	35.86	37.08

4 Simulations and Results

4.1 Community Input Data

In simulations, we consider a small community that consists of 11 complex houses [28], with more than 300 appliances individually measured. The structure of the appliances for each house is shown in Fig. 5a, whereas the structure of the appliances at the community level is displayed in Fig. 5b. House G is the most flexible followed by houses F, D and K and that have more than 60% flexible load. It also shows a high potential of flexibility. The number of appliances, by type, and the consumption level per month are given in Fig. 6. The highest consumption was recorded in November and January,

The typical daily load curve is shown in Fig. 7 as it influences the tariff set by the retailer. It shows the morning and evening peak and the night/afternoon valleys. Also, it shows a high potential for shifting the operation of flexible appliances at the community level.

Starting from peaks, shoulders and valleys of the daily curve, the initial ToU tariff shape can be designed. In this particular case study, the off-peak hours with the lowest rates are 24 and between 1 and 4 in the morning, the average hours (shoulder) are between 5 and 16, and 22 and 23, the peak hours with the highest rates are between 17 and 21. Classifying and timely updating the hours is important as the rates heavily influence the consumers to shift the operation of their appliances from peak to off-peak hours. Also, the level of rates is significant as they reflect the consumption level.

4.2 Simulations and Results

All the algorithms are tested and validated on 24-h and one-year datasets. As stated above, the cost minimization tends to create new peaks by unrestrictedly shifting the consumption of the *PA* toward the hours with the lowest rates. This



Fig. 9 The total consumption of the community before/after optimization with customers' preferences

Table 2 C	ommunity gai	ins after the ol	ptimization	of a 24-h	dataset v	vith const	umers' pre	sferences								
Iteration	$t^{ m off}$ peak_rate	$t^{\rm shoulder_rate}$	tpeak_rate	G	FI	G_{A}	$G_{\rm B}$	$G_{\rm C}$	G_{D}	$G_{\rm E}$	$G_{\rm F}$	G_{G}	$G_{\rm H}$	$G_{\rm I}$	ਓ	G_{K}
1	0.19	0.23	0.56	15.22	0.61	1.41	4.80	1.06	12.85	16.03	2.59	11.46	6.49	2.17	39.67	36.02
2	0.35	0.22	0.28	26.37	0.70	10.05	18.32	19.92	28.12	26.11	37.19	18.13	22.48	8.99	45.14	28.29
3	0.23	0.25	0.26	28.76	0.51	6.71	23.78	21.51	26.24	26.50	38.07	21.94	20.49	8.28	44.17	38.36
4	0.39	0.22	0.24	28.70	0.52	10.00	18.64	20.74	29.29	25.96	36.73	17.88	23.26	8.11	44.98	42.71
5	0.19	0.28	0.25	28.45	0.64	4.35	20.03	20.24	24.68	26.23	40.00	20.97	17.96	6.82	46.13	40.77

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Fig.10 Individual consumption before (left) and after optimization (right) on a 24-h dataset with consumers' preferences



Fig. 11 The total consumption of the community before/after optimization with retailer's constraints

is different from other studies as most of them use a small number of appliances. Since the game-optimization algorithm is enhanced by the dynamic ToU tariff, which iteratively calculates the rates based on the total electrical consumption of the community TDA, new peaks could be created and the algorithm cannot converge toward an optimal solution. Figure 8 shows the electrical consumption of the community before and after optimization. The 24-h dataset corresponds to a summer day that has the consumption peak at 19:00. Five iterations of the game-optimization algorithm are performed, and the results are displayed in Table 1 in terms of rates, community gain, FI and the individual gains for each house. The dataset in Fig. 8 corresponds to the fifth and last iteration. The FI of the unoptimized data is 0.41 and does not significantly improve as it can be seen in Table 1. The peaks migrate from the day to night hours repeatedly (see the rates in Table 1). Even though the gains can be as high as ~ 32% (e.g., iteration 2 and 4), the Flattening Index is not convenient for the retailer and the constraints must

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Iteration	$t^{ m offpeak_rate}$	$t^{ m shoulder_rate}$	$t^{ m peak_rate}$	G	FI	$G_{ m A}$	$G_{ m B}$	$G_{\rm C}$	$G_{ m D}$	G_{E}	G_{F}	$G_{ m G}$	$G_{ m H}$	G_{I}	G_{J}	$G_{\rm K}$
	0.19	0.23	0.56	10.09	0.64	3.74	12.87	1.06	13.28	1.41	13.25	16.02	7.38	1.36	5.50	13.17
5	0.27	0.22	0.35	26.16	0.78	6.53	27.53	16.78	25.44	19.59	31.35	22.39	19.86	8.97	32.02	37.53
	0.20	0.27	0.27	27.45	0.56	2.33	22.25	20.57	27.08	24.31	37.08	23.44	19.77	7.03	40.55	36.29
4	0.26	0.22	0.37	25.42	0.80	6.74	26.73	15.70	24.53	18.27	29.84	22.60	19.08	8.68	29.79	37.97
2	0.21	0.26	0.26	28.12	0.66	7.17	25.76	20.98	27.06	24.82	36.13	21.70	20.29	7.57	41.11	36.88

Table 3 Community gains after the optimization of a 24-h dataset with retailer's constraints



Fig. 12 The total consumption of the community before (left) and after (right) optimization on one-year datasets of with no constraints

be imposed. Therefore, if the PACM has only ones, that indicates the maximum flexibility of the *PA*, the swaying effect of the peak will be encountered. Thus, this matrix reflects the consumers' preferences and should have zeros as well.

The consumer can impose his consumption preferences through the PACM to increase his comfort (e.g., to restrict the functioning of noisy appliances during the night). As there is no real information about the *PA* constrains and their number is very high, it is assumed that approximately 20% of the operating hours (approximately 5 h per day) are restricted in the PACM randomly. These constraints allow obtaining a considerably better flattening of the consumption vector over the first 5 iterations, as presented in Fig. 9 and Table 2. It can be also observed that no house registers negative gains compared to the unoptimized dataset (compare Table 1 with Table 2). The FI reaches up to 0.7 (and in some other simulations even more) without a substantial loss in gain. Figure 10 shows the individual consumption of the houses in the community for a better insight into the optimization algorithm at the house level.

If restrictions from the customers are not available, or if they are not consistent enough to ensure a desired flattening of the consumption vector, the retailer can create and impose certain constraints in the optimization algorithm or shifting conditions that can be activated when required. Therefore, the retailer can stop the creation of new peaks by imposing a maximum hourly consumption, MA_i , on the optimized individual DA_i vector. This constraint $(A_i^h < MA_i)$ is more likely to be imposed for *SI* since they can be easily shifted at the hour with the lowest rate, regardless of consumption. Before shifting, the optimization algorithm verifies if the new total consumption of a certain hour is higher than MA_i . If $A_i^h \ge MA_i$, the algorithm restricts the hour in the PACM_i and thus, the next position of sN_i is evaluated at step 4 in Sect. 3.1.2. Therefore, MA_i could be an optional restriction of the optimization problem. If MA_i is too low, the optimization process will be very restricted and only few appliances will be shifted. On the other hand, if MA_i is too high, the optimization will remain unconstrained. For the simulations presented below, we consider MA_i as twice the average of the hourly consumption of

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Table 4 Yearly avera	ige gains and t	otal cost after	optimization v	with no constr-	aints						
	G_{A}	$G_{ m B}$	$G_{\rm C}$	G_{D}	$G_{\rm E}$	$G_{ m F}$	G_{G}	$G_{\rm H}$	G_{I}	G_{J}	G_{K}
Average gains (%)	5.01	7.08	5.37	7.35	4.95	17.50	5.77	4.78	4.86	15.09	17.90
Optimal cost (f)	1470.22	1968.09	1486.96	2839.25	3030.93	2600.62	7742.97	1516.40	1458.67	2192.21	2932.35



Fig. 13 The total consumption of the community before (left) and after (right) optimization on one-year datasets with consumers' constraints

each house. But the shifting condition is at the retailer's convenience and could be also imposed as long as the new peak is lower than daily average consumption. Figure 11 shows the community consumption before and after optimization with constraints imposed by retailer; the results consist in a particularly good FI of up to 0.8. Table 3 presents the first 5 iterations of the game-optimization algorithm in terms of rates, total gain, FI and individual gains.

Not all daily consumption profiles look similar, some days have 2 peaks (one in the morning and one in the evening) and others only one peak (in the evening). To investigate the result of the game-optimization algorithm on a bigger time interval, the algorithm is run for a one-year dataset with no constraints. Figure 12 shows the results obtained by displaying the annual hourly averages. The *FI* of the unoptimized dataset is 0.67 and of the optimized set 0.68 (*PAR* decreased from 2.25 to 2.18), indicating the need for constraints. Table 4 shows the average annual gains for each house and the total cost after optimization. The different gains between the houses reside in the individual consumption profile and flexibility.

Figure 13 shows the annual hourly averages after optimization with constraints from the customers ($\sim 20\%$ restricted hours). In this case, the average FI can be as high as 0.83 (PAR = 1.46), while the gains are similar (as presented in Table 5).

Simulations are performed also for the case when the retailer imposes the constraints to prevent the occurrence of the new peaks (see Fig. 14 showing the annual hourly averages for this case). The average FI after optimization is 0.77 (PAR = 1.7).

Tables 5 and 6 present the average gains and the costs after optimization for both cases of constraints. The results are slightly better when the consumers impose their preferences and can be further improved by redesigning the $PACM_{i}$.

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Table 5 Yearly avera	ige gains and t	otal cost after	optimization v	vith consumer	s' constraints						
	$G_{ m A}$	$G_{ m B}$	$G_{\rm C}$	G_{D}	$G_{ m E}$	G_{F}	$G_{ m G}$	$G_{ m H}$	$G_{\rm I}$	$G_{\rm J}$	G_{K}
Average gains (%)	4.74	6.10	6.39	4.37	5.39	11.25	4.98	5.06	6.01	11.64	12.37
Optimal cost (E)	1486.84	2015.50	1481.83	3017.48	3034.23	2869.23	7849.92	1521.25	1453.17	2318.56	3176.83



Fig. 14 The total consumption of the community before (left) and after (right) optimization on one-year datasets with retailer's constraints

5 Conclusion

A reliable game-optimization algorithm has been designed to achieve the best reward for a community of 11 houses with numerous appliances, implementing a dynamic ToU tariff. The cost optimization algorithm addresses both types of programmable appliances: non-interruptible and interruptible. The dynamic ToU tariff iteratively calculates the off-peak, shoulder and peak rates based on the total hourly consumption of the community, assigning higher rates at high consumption level, discouraging the peak consumption. The calculated rates are input for the optimization algorithm which provides a solution to minimize the cost by shifting the consumption of the programmable appliances toward hours with lower rates. Because the ToU tariff rates are calculated based on the total hourly consumption array, the algorithm enhances the cost minimization by repetitive optimization, providing, as a result, cost reductions of up to 30%. The simulations without constraints, seen as the highest flexibility degree, lead to new peaks which translates into the need to impose constraints. The simulations have been performed with certain customers' preferences ($\sim 20\%$ restricted hours of operation) or with constrains imposed by the retailer (in case the consumers preferences are not available) which limit the shifting flexibility degree of the programmable appliances. The Flattening Index can go as high as 0.83. As future work, as the optimization in multiple iterations is more complex, it could be performed and implemented as an automatic process that uses machine learning with direct load control (DLC), Internet of Things (IoT) and other mechanisms that ease the process and improve its effectiveness.

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Table 6 Ye	

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6.13 2492.65

4.23 1481.11

3.89 1539.64

4.13 7914.29

7.07 3005.21

3.60 3092.67

4.83 1507.29

3.63 2066.38

2.49 1521.89

Average gains (%) Optimal cost (E)

3061.92 3.22

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References

- Atzeni, I., Ordóñez, L.G., Scutari, G., Palomar, D.P., Fonollosa, J.R.: Demand-side management via distributed energy generation and storage optimization. IEEE Trans. Smart Grid. 866–876 (2013). https://doi.org/10.1109/TSG.2012.2206060
- [2] Belhaiza, S., Baroudi, U.: A game theoretic model for smart grids demand management. IEEE Trans. Smart Grid. 1386–1393 (2015). https://doi.org/10.1109/TSG.2014.2376632
- [3] Chouikhi, S., Merghem-Boulahia, L., Esseghir, M.: Energy demand scheduling based on game theory for microgrids. IEEE Int. Conf. Commun. 1–6 (2018). https://doi.org/10.1109/ICC.2018.84224 10
- [4] Chouikhi, S., Merghem-Boulahia, L., Esseghir, M., Snoussi, H.: A game-theoretic multi-level energy demand management for smart buildings. IEEE Trans. Smart Grid. 6768–6781 (2019). https://doi.org/10.1109/TSG.2019.2911129
- [5] Dong, X., Li, X., Cheng, S.: Energy management optimization of microgrid cluster based on multiagent-system and hierarchical Stackelberg game theory. IEEE Access. 206183–206197 (2020). https://doi.org/10.1109/access.2020.3037676
- [6] Eid, C., Koliou, E., Valles, M., Reneses, J., Hakvoort, R.: Time-based pricing and electricity demand response: existing barriers and next steps. Util. Policy 15–25 (2016). https://doi.org/10. 1016/j.jup.2016.04.001
- [7] Evora, J., Hernandez, J.J., Hernandez, M.: A MOPSO method for direct load control in smart grid. Expert Syst. Appl. 7456–7465 (2015). https://doi.org/10.1016/j.eswa.2015.05.056
- [8] Fernandez, E., Hossain, M.J., Nizami, M.S.H.: Game-theoretic approach to demand-side energy management for a smart neighbourhood in Sydney incorporating renewable resources. Appl. Energy 245–257 (2018). https://doi.org/10.1016/j.apenergy.2018.09.171
- [9] Gellings, C.W.: Evolving practice of demand-side management. J. Mod. Power Syst. Clean Energy 1–9 (2017). https://doi.org/10.1007/s40565-016-0252-1
- [10] Jacquot, P.:Game theory and optimization methods for decentralized electric systems. University PARIS-SACLAY, Institut Polytechnique de Paris. Accessed from http://www.cmap.polytechni que.fr/~paulin.jacquot/content/thesis/manuscript.pdf (2019)
- [11] Jacquot, P., Beaude, O., Gaubert, S., Oudjane, N.: Demand response in the smart grid: The impact of consumers temporal preferences. In: 2017 IEEE International Conference on Smart Grid Communications, SmartGridComm 1–7 (2017). https://doi.org/10.1109/SmartGridComm. 2017.8340690 (2018)
- [12] Jacquot, P., Beaude, O., Gaubert, S., Oudjane, N.: Demand side management in the smart grid: An efficiency and fairness tradeoff. In: 2017 IEEE PES Innovative Smart Grid Technologies Conference Europe, ISGT-Europe 2017—Proceedings. 1–7 (2017). https://doi.org/10.1109/ISGTEurope. 2017.8260265
- [13] Jamil, A., Alghamdi, T.A., Khan, Z.A., Javaid, S., Haseeb, A., Wadud, Z., Javaid, N.: An innovative home energy management model with coordination among appliances using game theory. Sustainability (Switzerland) 1–23 (2019). https://doi.org/10.3390/su11226287
- [14] Khaled A, Mariola N, Subhonmesh Bose, T.B.: The impact of aggregating distributed energy resources on electricity market efficiency. In: 2019 53rd Annual Conference on Information Sciences and Systems (CISS). Baltimore, MD, USA, IEEE (2019)

- [15] Khalid, A., Javaid, N., Mateen, A., Ilahi, M., Saba, T., Rehman, A.: Enhanced time-of-use electricity price rate using game theory. Electronics (Switzerland) 1–26 (2019). https://doi.org/10. 3390/electronics8010048
- [16] Li, X., Yang, H., Yang, M., Yang, G.: Flexible time-of-use tariff with dynamic demand using artificial bee colony with transferred memory scheme. Swarm Evol. Comput. 235–251 (2019). https://doi.org/10.1016/j.swevo.2019.02.006
- [17] Liu, L., Chang, Z., Guo, X., Mao, S., Ristaniemi, T.: Multiobjective optimization for computation offloading in fog computing. IEEE Internet Things J. 283–294 (2018). https://doi.org/10. 1109/JIOT.2017.2780236
- [18] Liu, Z., Wu, Q., Huang, S., Wang, L., Shahidehpour, M., Xue, Y.: Optimal day-ahead charging scheduling of electric vehicles through an aggregative game model. IEEE Trans. Smart Grid. 5173–5184 (2018). https://doi.org/10.1109/TSG.2017.2682340
- [19] Onile, A.E., Machlev, R., Petlenkov, E., Levron, Y., Belikov, J.: Uses of the digital twins concept for energy services, intelligent recommendation systems, and demand side management: a review. Energy Rep. 997–1015 (2021). https://doi.org/10.1016/j.egyr.2021.01.090
- [20] Oprea, S.V., Bara, A.: Setting the time-of-use tariff rates with NoSQL and machine learning to a sustainable environment. IEEE Access. 25521–25530 (2020). https://doi.org/10.1109/ACCESS. 2020.2969728
- [21] Oprea, S.V., Bara, A., Cebeci, M.E., Tor, O.B.: Promoting peak shaving while minimizing electricity consumption payment for residential consumers by using storage devices. Turk. J. Electr. Eng. Comput. Sci. 3725–3737 (2017). https://doi.org/10.3906/elk-1606-152
- [22] Oprea, S.V., Bâra, A., Ifrim, G.: Flattening the electricity consumption peak and reducing the electricity payment for residential consumers in the context of smart grid by means of shifting optimization algorithm. Comput. Ind. Eng. 125–139 (2018). https://doi.org/10.1016/j.cie.2018.05.053
- [23] Oprea, S.V., Bâra, A., Ifrim, G.A., Coroianu, L.: Day-ahead electricity consumption optimization algorithms for smart homes. Comput. Ind. Eng. 382–401 (2019). https://doi.org/10.1016/j.cie.2019. 06.023
- [24] Simaan, M., Cruz, J.B.: On the Stackelberg strategy in nonzero-sum games. J. Optim. Theory Appl. 533–555 (1973). https://doi.org/10.1007/BF00935665
- [25] Sohrabi, M.K., Azgomi, H.: A survey on the combined use of optimization methods and game theory. Arch. Comput. Methods Eng. 59–80 (2020). https://doi.org/10.1007/s11831-018-9300-5
- [26] Tör, O.B., Cebeci, M.E., Koç, M., Teimourzadeh, S., Atli, D., Oprea, S.V., Bara, A.: Peak shaving and technical loss minimization in distribution grids: a time-of-use-based pricing approach for distribution service tariffs. Turk. J. Electr. Eng. Comput. Sci. 1386–1404 (2020). https://doi.org/10. 3906/elk-1907-30
- [27] Tushar, M.H.K., Zeineddine, A.W., Assi, C.: Demand-side management by regulating charging and discharging of the EV, ESS, and utilizing renewable energy. IEEE Trans. Ind. Inform. 117–126 (2018). https://doi.org/10.1109/TII.2017.2755465
- [28] UMassTraceRepository, Smart* Data Set for Sustainability.: http://traces.cs.umass.edu/index.php/ Smart/Smart. Accessed 20 May 2020 (n.d.)
- [29] Yang, L., Dong, C., Wan, C.L.J., Ng, C.T.: Electricity time-of-use tariff with consumer behavior consideration. Int. J. Prod. Econ. 402–410 (2013). https://doi.org/10.1016/j.ijpe.2013.03.006
- [30] Yu, M., Hong, S.H.: A real-time demand-response algorithm for smart grids: a Stackelberg game approach. IEEE Trans. Smart Grid. 879–888 (2016). https://doi.org/10.1109/TSG.2015.2413813
- [31] Zhu, Z., Lambotharan, S., Chin, W.H., Fan, Z.: A game theoretic optimization framework for home demand management incorporating local energy resources. IEEE Trans. Ind. Inf. 353–362 (2015). https://doi.org/10.1109/TII.2015.2390035

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