

Solvent Basicity, A Study of Kamlet–Taft *β* **and Gutmann** *DN* **Values Using Computationally Derived Molecular Properties**

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Abstract

Solvent basicity is recognized as playing a major role in solvation and is included, through empirical basicity parameters, in linear free energy relationships that account for the efects of changes in solvent on chemical reactions. It is reasonable to postulate that the basicity of a solvent molecule refects some combination of its molecular properties. In the present study, density functional calculations using the B3LYP functional, and Hartree–Fock calculations have been used to calculate the partial atomic charges (using the Hirshfeld and CM5 models), orbital energies, polarizabilities, dipole moments and quadrupolar amplitudes for over one hundred molecules for which there are experimental values for two basicity parameters, Kamlet and Taft's hydrogen bond acceptor strength, *β*, and Gutmann's donor number, *DN*, a measure of Lewis basicity. Regression of the experimental *β* and *DN* values against molecular descriptors refecting the above molecular properties yields a remarkably consistent picture. For both parameters the values for alcohols and amines lie systematically off of the regression lines through the remaining compounds, which include alkanes, aromatics, halogenated alkanes and aromatics, esters, carbonates, carboxylic acids, ketones, ethers, nitriles, phosphates, sulfdes and sulfates. Independent of the calculation method or method of estimating the partial atomic charges, both experimental *β* and *DN* are essentially determined by two molecular properties: the charge on the most negative atom of the molecule and the molecular orbital from which charge donation would occur. The regression results using any of the fours sets of descriptors (refecting the two calculation methods and two methods of charge estimation) are remarkably similar for *β* and *DN* supporting the view that these are measures of the same "basicity".

Keywords Solvent basicity · Kamlet–Taft *β* · Gutmann *DN* · Computational chemistry

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1 Introduction

Basicity and acidity are among the core concepts in solution chemistry. The earliest approaches to acidity and basicity, due to Arrhenius [\[1\]](#page-15-0) and to Brønsted [\[2\]](#page-15-1) and Lowry [\[3](#page-15-2)], focused on the proton acidity. Lewis [\[4,](#page-15-3) [5](#page-15-4)] subsequently broadened the idea of acid–base chemistry to include, for example, the binding of ligands, as Lewis bases, to metal ions, acting as Lewis acids. While proton basicity, as reflected in pK_a values and Lewis basicity as refected in the binding constants of metal–ligand complexes are diferent, it is likely that they both refect some fundamental "basicity" of the moiety.

The general importance of basicity in solutions is widely recognized and it is one of the properties universally included in linear free energy type equations, such as those due to Kamlett and Taft [\[6\]](#page-15-5), for the correlation of chemical parameters with molecular properties. Thus, a number of experimental solvent parameters relating to solvent basicity have been developed [\[7,](#page-15-6) [8](#page-15-7)] of which Gutmann's donor number [[9\]](#page-15-8), *DN*, and Kamlet and Taft's hydrogen bond acceptor basicity [[10](#page-15-9)], *β*, are commonly used.

The development of computational methods and the availability of increasing computer power have opened the possibility of calculating, as opposed to measuring, values of these basicity parameters or replacing them with molecular descriptors generated computationally. A number of computational studies have been reported, commonly these have involved the calculation of pK_a values of acids $[11–17]$ $[11–17]$ $[11–17]$ or the correlation (and prediction) of experimental basicity parameters with computationally derived molecular descriptors [[18](#page-15-12)[–20\]](#page-15-13). In principle, either approach can provide insight into the origins of a moiety's basicity, from the relative contributions of the diferent descriptors used.

The present study involves the correlation of experimental basicity parameters with computationally derived molecular descriptors; however, it is not directed to the prediction of the solubility parameters but, rather, to explore which molecular properties lead to a moiety's basicity. The experimental parameters considered are Kamlet and Taft's hydrogen bond acceptor parameter, *β*, and Gutmann's donor number, *DN*.

2 Basicity Parameters

It is worthwhile considering the basicity scales and whether they measure the same "basicity" of a molecule.

Gutmann's *DN* was originally defned as the absolute value of the molar enthalpy of interaction of the base with antimony pentoxide, a very strong Lewis acid, with the reaction carried out in dilute solutions with dichloroethane as solvent. In efect it was intended as a measure of the Lewis basicity of an isolated or very weakly solvated, molecule of the base [\[9\]](#page-15-8).

In contrast, Kamlet and Taft's *β* was defned as the diference between the shifts in the absorbance maximum of two dyes, which difered in that one had an acidic proton [\[10\]](#page-15-9). In this case the measurements were carried out on dilute solutions of the dye with the base as solvent. Thus, β was intended to be a measure of the hydrogen bond basicity, or hydrogen bond acceptor strength, of the base as solvent.

So the scales difer in two ways, the *DN* scale being a measure of Lewis basicity while *β* was intended to be a measure of hydrogen bond acceptor strength. The two scales also difer in that the *DN* was measured for an isolated base molecule in a weakly interacting solvent while β was a property of the bulk liquid.

In carrying out this work we have used the *DN* and β values listed in Marcus's review [[7\]](#page-15-6). This review presents data for around one hundred solvents where both *β* and *DN* values are available and we restricted this study to those compounds. To bring the scales into approximate correspondence we have divided the *DN* values by 37, which makes the *DN** for hexamethylphosphoramide equal to its β value (1.05).

$$
DN^* = \frac{DN}{37} \tag{1}
$$

It is worth noting at the outset that both the *β* and *DN** values show essentially no evidence of steric hindrance. Thus, *β* and *DN** depend essentially on the principal functional group of the base. If steric efects were important than one would observe a systematic decrease in the basicity measures as larger side-groups are introduced. This is generally not the case, as is clear from Table [1](#page-3-0) where the *β* and *DN** values for diferent groups of molecules, with varying sizes of side-groups, are listed.

It is also clear from Table [1](#page-3-0) that the β and DN^* values are in remarkably good agreement except for several amines, where the *DN** values are systematically higher. This is confirmed by Fig. [1](#page-5-0) where the DN^* values are plotted against the β values. Marcus reports a value 0.76 for the correlation coefficient (R^2) of this plot for the 110 compounds for which he reports values [[7\]](#page-15-6); however, if the values for simple alkyl amines (butyl-, diethyl-, triethyl and tributyl-amine) are excluded, R^2 for the remaining 106 compounds is 0.86 and removing all of the amines, anilines and pyridines from the correlation raises \mathbb{R}^2 to 0.92 (97 data points).

Thus, despite their diferent formulations, *β* and *DN* (or *DN**) appear to be measures of the same "basicity" of solvents; the only clear exception being nitrogen bases.

3 Computational Details

Since the focus of this work is to understand the relationship between the measures of basicity and molecular properties of the bases, calculations were carried out on isolated molecules rather than in the presence of a reaction feld.

It seemed important to assess the reliability of the calculated molecular properties and so calculations were carried out using Hartree–Fock and density functional methods (using the B3LYP functional). All calculations were carried out using the Gaussian 09 suite of programs [\[21\]](#page-15-14). The structures of the molecules were optimized using both methods and the molecular properties recovered for the minimized structures.

Initially calculations were calculated using the $6-31G(d,p)$ and $6-311G(2d,2p)$ basis sets and Mulliken partial charges were used. However, it is clear the Mulliken charges are highly sensitive to the basis set used and so don't provide a suitable basis for analyses of the solvent parameters. Thus, the calculations were repeated and Hirshfeld and CM5 partial charges were recovered.

To observe the efect of basis set on the molecular properties, density functional calculations were carried out for DMSO using the B3LYP functional and nine basis sets ranging from $6-31G(d,p)$ to $6-311++(3df,2p)$ and including Dunning's aug-CC-pVTZ and aug-cc-pVQZ. These calculations show that the Mulliken partial charges vary widely and non-monotonically with changes in basis set (partial charges on the S=O oxygen atom are − 0.699, − 0.463 and − 1.121 a.u. for the 6–31G(d,p), 6–311++(3df,2p) and aug-cc-pVQZ basis sets, respectively). In contrast, the Hirshfeld and CM5 partial charges are relatively

Table 1 Comparison of *β* and *DN* values for bases with a common functional group but difering side-groups

insensitive to basis set and show reasonable convergence for the more complete basis sets (Hirshfeld partial charges for the S=O oxygen atom are -0.401 , -0.385 , -0.385 , -0.392 and − 0.389 a.u. for the 6–31(d,p), 6–311+(3df,2p), 6–311++(3df,2p), aug-CC-pVTZ and aug-cc-pVQZ basis sets, respectively).

To ensure that the results were general, rather than specifc to DMSO, calculations were carried out using both the density functional (B3LYP functional) and Hartree–Fock methods and the 6–311+G(3df,2p) and aug-cc-pVTZ basis sets for *n*-hexane, *m*-xylene, ethanol, DMSO and *N*,*N*-dimethyl formamide, DMF. This showed that the Hirshfeld and CM5 partial charges were method dependent but not basis set dependent, at least for these basis sets. Thus, calculations were carried out using both density functional and Hartree–Fock methods but only using the 6–311G+(3df,2p) basis set, which was computationally less demanding than the aug-cc-pVTZ basis set.

The molecular properties recovered were the Hirshfeld and CM5 partial charges on the most negative and most positive atoms, the polarizability, dipole moment, quadrupolar

Fig. 1 Plot of *DN** against *β*: light blue circles, alkanes and aromatics; dark blue squares, halogenated alkanes and aromatics; orange circles, esters and carbonates; green circles, carboxylic acids; purple circles, ketones; black diamonds, ethers; red triangles, nitriles; dark green squares, RS, RS=O, RP=O; dark blue circles, amides; light brown triangles, water alcohols and polyols; grey triangles, pyridines; brown squares, amines and anilines (Color fgure online)

amplitude^{[1](#page-5-1)} of the molecule and the energies of the filled, donor, and unfilled, acceptor, orbitals. Plots of the polarizabilities, dipole moments and quadrupolar amplitudes from the Hartree–Fock calculations $(6-311G+(3df,2p)$ basis set) against those from the density functional calculations are linear so that, for these, the choice of calculation method in immaterial. This is not the case for the orbital energies, shown for the occupied donor orbitals in Fig. [2,](#page-6-0) where the values from the Hartree–Fock calculations generally fall on two lines when plotted against the density functional results, one line through the nitriles, alkanes and aromatic compounds (including halogenated compounds) and the second line passing through the values for most of the other compounds.

Similar plots of the Hirshfeld derived partial charges calculated using the Hartree–Fock method against those from the density functional method are also linear, while those for the CM5 derived charges show small deviations for some classes of compounds. However, when CM5 derived charges are plotted against Hirshfeld derived charges, as in Fig. [3](#page-7-0) where the negative atom partial charges from the density functional calculations are plotted, it is found that the data lie on several lines, depending on the functional group.

For each molecular property a molecular descriptor, Q_x , was constructed as:

$$
Q_X = \frac{(X - X_{\min})}{(X_{\max} - X_{\min})}
$$
\n(2)

¹ The quadrupolar amplitude is calculated as $A = \sqrt{\sum q_{ij} q_{ij}}$ $i = x, y, z \neq j = x, y, z$ where the q_{ij} are the components of the traceless quadrupole.

Fig. 2 Plot of the donating orbital energies *E*(OMO) calculated using the Hartree–Fock method against those from the density functional method: light blue circles, alkanes and aromatics; dark blue squares, halogenated alkanes and aromatics; orange circles, esters and carbonates; green circles, carboxylic acids; purple circles, ketones; black diamonds, ethers; red triangles, nitriles; dark green squares, RS, $RS = O$, $RP = O$; blue circles, amides; light brown triangles, water alcohols and polyols; grey triangles, pyridines; brown squares, amines and anilines (Color figure online)

where *X* represents the molecular property and the subscripts max and min refer to the maximum and minimum calculated values of *X* (note that for the negative charge X_{max}) is the largest negative charge, for example). This gives a series of descriptors that vary between zero and unity, making comparison of their relative importance straightforward.

Because of the diferences in the *E*(OMO) values calculated using the Hartree–Fock and density functional methods and those between the Hirshfeld and CM5 based partial atomic charges, both the *β* and *DN** values were analysed using descriptors derived from both computational methods and from both the Hirshfeld and CM5 based partial atomic charges.

All of the molecular properties recovered from the quantum mechanical calculations and the experimental β and DN^* values are provided in the supplementary material. The molecular descriptors recovered from the DF calculations using the CM5 derived charges are also listed there.

4 Analysis of *β* **and** *DN******

The approach adopted assumes linear relationships between the basicity parameters and the molecular descriptors; thus we write:

$$
\beta = \beta_0 + \sum a_X Q_X \tag{3}
$$

Fig. 3 Plot of the CM5 derived partial charges on the most negative atom against the Hirshfeld derived values, calculated using the density functional method; light blue circles, alkanes and aromatics; dark blue squares, halogenated alkanes and aromatics; orange circles, esters and carbonates; green circles, carboxylic acids; purple circles, ketones; black diamonds, ethers; red triangles, nitriles; dark green squares, RS, RS=O, RP=O; blue circles, amides; light brown triangles, water alcohols and polyols; grey triangles, pyridines; brown squares, amines and anilines (Color figure online)

$$
DN^* = DN^{*0} + \sum b_X Q_X \tag{4}
$$

where Q_X are molecular descriptors and the a_X and b_X are the related coefficients.

The molecular properties recovered for the minimized chemical structures are largely straightforward; thus, the molecular polarizability, dipole moment and quadrupolar amplitude are unambiguous.

In considering the partial charges on atoms the situation is simple except in the cases of alkanes where the most negative atoms are the carbon atoms and so are not directly available to neighbouring molecules; in these cases, the net charge on the CH*n* moiety was taken (these are reported by Gaussian). For aromatic compounds this wasn't necessary, presumably because the carbon atom partial charges are available from above or below the ring.

The question of which orbital's energy is taken is more complex. As an example, the nitriles all have very similar *β* of *DN*^{*} values and for the simple alkyl nitriles the highest occupied molecular orbital (HOMO) is the CN π -bonding orbital but in benzyl cyanide and benzonitrile the first and second HOMOs are the benzene ring π -bonding orbitals and the third HOMO, which is the CN π -bonding orbital, was taken as the donating orbital. Similar situations arise in a few other cases; thus, the HOMO of chloroethanol is associated with the Cl atom and the second HOMO with the O atom and the HOMO of tetramethyl urea is associated with the N atoms and the second HOMO, which is on the $C=O$, was taken as the donating orbital.

	DF, CM5		HF, CM5		DF. Hir		HF, Hir	
	Value	p value	Value	p value	Value	p value	Value	p value
β values								
R^{2a}	0.74		0.72		0.69		0.72	
F	43		38		34		39	
β^{0b}	-0.31	2×10^{-3}	-0.40	8×10^{-5}	-0.39	2×10^{-4}	-0.42	3×10^{-5}
a_{q-}	0.78	1×10^{-12}	0.75	3×10^{-9}	0.75	4×10^{-9}	0.81	1×10^{-9}
$a_{\text{E(OMO)}}$	0.69	8×10^{-13}	0.70	2×10^{-9}	0.67	2×10^{-10}	0.73	1×10^{-10}
a_{DP}	0.02	7×10^{-1}	0.01	9×10^{-1}	-0.24	2×10^{-3}	-0.24	8×10^{-3}
$a_{\rm p}$	0.04	6×10^{-1}	-0.03	8×10^{-1}	0.10	3×10^{-1}	0.12	2×10^{-1}
$a_{\rm QP}$	0.03	5×10^{-1}	0.08	4×10^{-1}	0.01	6×10^{-1}	0.00	1×10^{0}
a_{q+}	0.13	2×10^{-1}	0.06	3×10^{-1}	0.37	9×10^{-4}	0.24	5×10^{-7}
a_{EUMO}	-0.22	1×10^{-1}	0.05	8×10^{-1}	0.01	1×10^{0}	0.06	7×10^{-1}
DN^* values								
R^2	0.71		0.80		0.55		0.57	
F	39		60		20		21	
$DN^{\ast 0}$	-0.43	8×10^{-4}	-0.28	4×10^{-3}	-0.68	2×10^{-5}	-0.39	2×10^{-3}
b_{q-}	0.98	7×10^{-9}	1.15	1×10^{-15}	0.31	1×10^{-1}	0.72	2×10^{-4}
$b_{E(OMO)}$	0.74	2×10^{-9}	0.59	9×10^{-11}	1.00	1×10^{-8}	0.80	4×10^{-10}
$b_{\rm DP}$	-0.03	6×10^{-1}	-0.09	2×10^{-1}	-0.10	4×10^{-1}	-0.24	7×10^{-2}
$b_{\rm P}$	0.29	2×10^{-2}	0.22	5×10^{-2}	0.27	1×10^{-1}	0.28	1×10^{-1}
$b_{\rm QP}$	-0.22	6×10^{-2}	-0.30	4×10^{-3}	-0.06	7×10^{-1}	-0.15	3×10^{-1}
b_{q+}	0.10	4×10^{-1}	0.05	6×10^{-1}	$0.62\,$	3×10^{-4}	0.58	7×10^{-4}
$b_{\text{E(UMO)}}$	-0.10	6×10^{-1}	-0.16	4×10^{-1}	0.36	1×10^{-1}	0.16	6×10^{-1}

Table 2 Results of the regression of all β and DN^* with the seven molecular descriptors

DF and HF indicate that the molecular descriptors were derived from density functional and Hartree–Fock calculations and Hir and CM5 that *Q*q− and *Q*q+ were from Hirshfeld and CM5 charge calculations, respectively; bold values show apparent statistical significance ($p \le 0.05$), intercepts are not highlighted as they are inevitable

 ${}^{a}R^{2}$ is the correlation coefficient of the regression, corrected for the number of variables and F the F test result

b Descriptors derived using Eq. [2](#page-5-2) from molecular properties: *Q*q− and *Q*q+ from the partial charges on the most negative and most positive atoms, respectively (see text); \dot{Q}_{DP} , Q_P and Q_{OP} from the molecular dipole moment, polarizability and quadrupolar amplitude, respectively; $Q_{E(OMO)}$ and $\tilde{Q}_{E(UMO)}$ from the energies of the flled donor and unflled acceptor orbitals, respectively (see text)

In general, use of the ring π -bonding orbitals of aromatic compounds led to calculated β and DN^* that were much too large and, in all cases, the highest non-ring orbital was used. This result seems counter-intuitive but may refect the fact that the ring π -bonding orbitals are diffuse, with the electrons bound by several C nuclei. This is likely specifc to this case, which involves the basicity of molecules with hard donor atoms.

The procedure adopted to analyze the β and DN^* data was to begin by carrying out a multiple regression of all of the values, ftting them to all seven of the molecular descriptors. The regression was repeated after the removal of descriptors for which the p-values of the coefficients indicated that they were statistically insignificant. This is shown in Tables 2 and [3](#page-9-0) which give the results of the regression all of the β and *DN** values (106 data)

	DF, CM5		HF, CM5		DF, Hir		HF, Hir	
	Value	p value						
β values								
R^2	0.74		0.73		0.69		0.73	
$\mathbf F$	149		138		61		70	
β^{0a}	-0.32	4×10^{-9}	-0.37	9×10^{-9}	-0.33	1×10^{-6}	-0.35	1×10^{-7}
a_{q-}	0.80	9×10^{-20}	0.85	5×10^{-22}	0.77	2×10^{-10}	0.82	8×10^{-13}
$a_{E(OMO)}$	0.65	3×10^{-13}	0.64	1×10^{-10}	0.68	1×10^{-11}	0.74	1×10^{-12}
a_{DP}					-0.27	4×10^{-4}	-0.27	3×10^{-4}
$a_{\rm p}$								
$a_{\rm OP}$								
a_{q+}					0.33	1×10^{-3}	0.23	5×10^{-7}
$a_{\text{E(UMO)}}$								
DN^* values								
R^2	0.70		0.79		0.53		0.54	
\mathbf{F}	124		129		60		42	
DN^{*0}	Value	p value						
b_{q-}	-0.41	4×10^{-9}	-0.27	2×10^{-6}	-0.43	9×10^{-6}	-0.30	4×10^{-4}
$b_{E(OMO)}$	0.93	6×10^{-16}	1.09	2×10^{-24}			0.36	2×10^{-3}
b_{DP}	0.81	6×10^{-12}	0.65	2×10^{-14}	1.20	2×10^{-17}	0.93	1×10^{-14}
$b_{\rm P}^{a}$								
$b_{\rm QP}$								
b_{q+}			-0.22	2×10^{-2}				
$b_{\text{E(UMO)}}$					0.66	2×10^{-5}	-0.60	2×10^{-4}

Table 3 Results of the regression of all β and *DN** with the statistically significant molecular descriptors

All abbreviations as in Table [2](#page-8-0)

^aIn a subsequent regression, using only Q_{q-} , $Q_{E(OMO)}$ and Q_{P} , the p value for *b*_P was>0.05 and this was taken as statistically insignifcant and the regression was repeated using only *Q*q− and *Q*E(OMO)

against all seven descriptors and against those with statistically significant coefficients, respectively.

There is a diference between the regressions using the CM5 and Hirshfeld based partial atomic charges. Thus, for the β values, regressions using the CM5 partial charges return only two signifcant descriptors, *Q*q−, based on the partial charge of the most negative atom, and $Q_{E(OMO)}$, based on the energy of the donating orbital. The regressions of the DN^* values return these descriptors as significant but also return significance for Q_P , based on the molecular polarizability, for the density functional derived values and for Q_{OP} , based on the molecular dipoles, for the Hartree–Fock calculations.

In contrast, regressions of the β values using Hirshfeld charges, in addition to the dependences on Q_{q-} and $Q_{E(OMO)}$, show statistically significant coefficients for Q_{q+} , based on the partial charge of the most positive atom, and for Q_{DP} . In the case of DN^* , the regressions show statistically significant coefficients for Q_{q+} and, for the density functional results, the dependence on Q_{q-} is lost (p=0.3).

When the β values calculated using the solvent descriptors and the coefficients in Table [3](#page-9-0) are plotted against the experimental values it becomes clear that the calculated

Fig. 4 Plot of calculated against experimental β values, with β_{calc} values calculated using the coefficients in Table [3](#page-9-0) based on density functional calculations and CM5 derived partial charges. Symbols: light blue circles, alkanes and aromatics; dark blue squares, halogenated alkanes and aromatics; orange circles, esters and carbonates; green circles, carboxylic acids; purple circles, ketones; black diamonds, ethers; red triangles, nitriles; dark green squares, RS , $RS = O$, $RP = O$; blue circles, amides; light brown triangles, water alcohols and polyols; grey triangles, pyridines; brown squares, amines and anilines; the solid red line represents perfect agreement (Color figure online)

values for the alcohols and primary or secondary amines lie on lines quite diferent from that through the values for the other compounds. This is shown in Fig. [4](#page-10-0), which compares the experimental β values with those calculated from the descriptors recovered from the density functional calculations and the CM5 based partial charges using the coefficients in Table [3](#page-9-0).

The plots of values of β calculated using the other coefficients in Table [3](#page-9-0) show similar patterns, with the calculated values for the alcohols and aniline or amines with NH hydrogens are systematically out of agreement with the experimental values.

In the case of the *DN** values the same pattern is observed except that, in these cases, the values for the amines, anilines and pyridines lie off the line through the data for the other systems. Given the fact that, in contrast to most compounds, the *DN** values of several of these nitrogen bases are significantly higher than their β values (see Fig. [1\)](#page-5-0), it is perhaps not surprising that there isn't good agreement between the calculated and experimental *DN** values.

In view of the consistency of these results the β and *DN** values were regressed with the values for the alcohols and NH hydrogen bases removed from the *β* data set and those of the alcohols and amines, anilines and pyridines removed from the *DN** data set. The results are shown in Tables [4](#page-11-0) and [5](#page-12-0) which give the results of the regressions of the *β* and *DN*^{*} values (84 and 77 data, respectively) against all seven descriptors and against those with statistically significant coefficients, respectively.

	DF, CM5		HF, CM5		DF, Hir		HF, Hir	
	Value	p value	Value	p value	Value	p value	Value	p value
β values ^a								
R^2	0.84		0.84		0.78		0.84	
$\mathbf F$	61		64		43		64	
$\beta^{0 b}$	-0.28	2×10^{-4}	-0.47	2×10^{-8}	-0.30	4×10^{-4}	-0.47	1×10^{-8}
a_{q-}	0.99	1×10^{-15}	0.837	2×10^{-15}	0.68	9×10^{-11}	0.88	3×10^{-17}
$a_{E(OMO)}$	0.52	4×10^{-11}	0.55	2×10^{-10}	0.54	1×10^{-9}	0.54	1×10^{-10}
a_{DP}	0.01	9×10^{-1}	0.10	9×10^{-2}	$-\,0.06$	3×10^{-1}	0.10	1×10^{-1}
$a_{\rm p}$	0.05	5×10^{-1}	0.06	4×10^{-1}	0.16	7×10^{-2}	0.07	3×10^{-1}
$a_{\rm OP}$	-0.01	8×10^{-1}	0.02	8×10^{-1}	0.00	1×10^{0}	-0.07	8×10^{-1}
a_{q+}	0.09	4×10^{-1}	0.00	1×10^{0}	0.01	9×10^{-1}	-0.02	8×10^{-1}
$a_{\rm E(UMO)}$	-0.18	1×10^{-1}	0.39	7×10^{-2}	0.04	7×10^{-1}	0.38	7×10^{-2}
DN^* values ^b								
R^2	0.67		0.87		0.68		0.80	
F	23		70		25		43	
$DN^{\ast 0}$	-0.38	7×10^{-4}	-0.43	3×10^{-7}	-0.36	4×10^{-3}	-0.26	5×10^{-3}
b_{q-}	0.75	9×10^{-5}	1.00	2×10^{-16}	0.66	8×10^{-5}	0.82	3×10^{-12}
$b_{E(OMO)}$	0.59	3×10^{-7}	0.43	1×10^{-11}	0.65	1×10^{-6}	0.35	3×10^{-6}
b_{DP}	0.04	6×10^{-1}	0.04	5×10^{-1}	-0.16	9×10^{-2}	-0.04	6×10^{-1}
$b_{\rm P}$	0.19	1×10^{-1}	0.23	8×10^{-3}	0.05	7×10^{-1}	0.20	5×10^{-2}
$b_{\rm QP}$	-0.04	7×10^{-1}	-0.14	4×10^{-2}	0.03	8×10^{-1}	-0.14	1×10^{-1}
$b_{\mathbf{q}+}$	0.26	5×10^{-2}	0.23	8×10^{-3}	0.31	7×10^{-2}	0.09	5×10^{-1}
$b_{E(UMO)}$	$-\,0.09$	6×10^{-1}	0.32	1×10^{-1}	0.05	8×10^{-1}	0.30	2×10^{-1}

Table 4 Results of the regression of *β* and *DN** with some groups of molecules removed, the seven molecular descriptors

All abbreviations as in Table [2](#page-8-0)

a *β* values for alcohols and amines or anilines with N–H hydrogens removed from the data set (84 data regressed)

b *DN** values for alcohols, amines, anilines and pyridines removed from the data set (77 data regressed)

The results shown in Tables [4](#page-11-0) and [5](#page-12-0) are clear and essentially consistent. Thus, for the *β* values, all four regressions indicate that only the dependences on *Q*q− and *Q*E(OMO) are statistically signifcant. This is also true for the *DN** values, except for the regression using the Hartree–Fock and CM5 charge derived molecular descriptors, where the dependences on $Q_{\rm P}$, Q_{DP} and $Q_{\text{q+}}$ are marginally significant, with p values of 0.01, 0.03 and 0.01, respectively, as compared to Q_{q-} and $Q_{E(OMO)}$ for which the p values are 9×10^{-20} and 2×10^{-12} , respectively.

The β and DN^* values calculated using the four sets of descriptors and the coefficients in Table [5](#page-12-0) are compared to the experimental values in Fig. [5](#page-13-0).

5 Discussion

It is clear from Fig. [1](#page-5-0) and Table [1](#page-3-0) that *β* or *DN** are closely aligned, indicating that, in these cases at least, the hydrogen and Lewis basicities are very similar. The nitrogen bases may be an exception to this, since there is poor agreement between β or DN^* for these.

	DF, CM5		HF, CM5		DF, Hir		HF, Hir	
	Value	p value						
β values								
R^2	0.80		0.84		0.77		0.78	
$\mathbf F$	168		223		144		149	
β^0	-0.31	2×10^{-12}	-0.35	1×10^{-12}	-0.23	4×10^{-7}	-0.33	5×10^{-9}
a_{q-}	0.98	1×10^{-22}	0.93	2×10^{-25}	0.59	1×10^{-16}	0.63	1×10^{-19}
$a_{E(OMO)}$	0.51	1×10^{-12}	0.56	2×10^{-12}	0.60	4×10^{-13}	0.69	9×10^{-14}
a_{DP}								
$a_{\rm P}$								
$a_{\rm OP}$								
a_{q+}								
a _{E(UMO)}								
DN^* values								
R^2	0.67		0.86		0.67		0.79	
$\mathbf F$	77		96		82		140	
DN^{*0}	-0.27	2×10^{-5}	-0.35	2×10^{-8}	-0.26	3×10^{-5}	-0.14	2×10^{-4}
b_{q-}	0.83	3×10^{-10}	1.01	9×10^{-20}	0.56	6×10^{-9}	0.68	8×10^{-19}
$b_{E(OMO)}$	0.58	1×10^{-7}	0.45	2×10^{-12}	0.69	2×10^{-8}	0.43	7×10^{-9}
b_{DP}								
$b_{\rm P}$								
$b_{\rm QP}$			0.21	1×10^{-2}				
$b_{\mathbf{q}+}$			0.15	3×10^{-2}				
$b_{\rm E(UMO)}$			0.22	1×10^{-2}				

Table 5 Results of the regression of β and *DN** with the statistically significant molecular descriptors

All abbreviations as in Table [2](#page-8-0)

This is borne out by the results of the regressions, which show that, in both cases, only the descriptors refecting the partial charge on the most negative atom, *Q*q−, and that reflecting the energy of the charge donating orbital, $Q_{E(\text{OMO})}$, have meaningful statistical significance.

As can be seen from Table [5,](#page-12-0) the results are surprisingly consistent over all of the regressions. Thus, the average value of the intercept is 0.28 with those for the β and DN^* values being 0.31 and 0.26, respectively, with relatively little dependence on the calculation method or the method used to estimate the partial atomic charges.

Perhaps surprisingly, given the diferences in the orbital energies from the density func-tional and Hartree–Fock calculations (see Fig. [2\)](#page-6-0), the coefficients recovered for $Q_{E(ONO)}$ from the regressions are also substantially independent of the calculation method. The average coefficient recovered for $Q_{E(\text{OMO})}$ is 0.56 with the values for the for the *β* and *DN** values being 0.59 and 0.54, respectively.

There are differences for the coefficients recovered for Q_{q-} , reflecting the differences in the Hirshfeld and CM5 based partial charges (see Fig. [3\)](#page-7-0); however, there is consistency between the values recovered from the regressions of the β and *DN** data with these averaging 0.94 and 0.62 for descriptors based on the CM5 and Hirshfeld charge models, respectively; again, these are substantially independent of the calculation method.

Fig. 5 Plots of calculated against experimental β values, with β_{calc} values calculated using the coefficients in Table [5.](#page-12-0) Symbols: light blue circles, alkanes and aromatics; dark blue squares, halogenated alkanes and aromatics; orange circles, esters and carbonates; green circles, carboxylic acids; purple circles, ketones; black diamonds, ethers; red triangles, nitriles; dark green squares, RS , $RS = O$, $RP = O$; blue circles, amides; the solid red line represents perfect agreement. **a** Density functional calculations and CM5 derived partial charges. **b** Hartree–Fock calculations and CM5 derived partial charges. **c** Density functional calculations and Hirshfeld derived partial charges. **d** Hartree–Fock calculations and Hirshfeld derived partial charges (Color fgure online)

The fact that the alcohols and nitrogen bases don't ft on the regression line through the other classes of compounds indicates that there are factors not accounted for in the present treatment. The liquid alcohols and amines are hydrogen bonded liquids, which could impinge on their β values but, in principal, the *DN** values are measured for individual molecules where hydrogen bonding shouldn't be a factor. In practice, this distinction between *β* and *DN** is commonly lost and donor numbers are determined using proxy experiments where, for example, the NMR [\[22\]](#page-16-0) or visible [[23](#page-16-1)] spectra of a probe molecule are measured in diferent liquid solvents and the donor number is estimated from the variation of the measured property with donor numbers for other solvents. In these cases, the values determined are properties of the liquid solvent and need not coincide with the property of the isolated molecule.

The nitrogen bases have previously been recognized as difering from the other, commonly oxygen, bases. For example, Popov pointed out very early that pyridine behaved as a weaker base than is indicated by its donor number [[24](#page-16-2)]. This is clearly refected in Fig. [1](#page-5-0), where the *DN** values of several nitrogen bases are far higher than would be expected from their *β* values.

We currently have no explanation for why these compounds differ so strongly from the others for which data are available and will reserve further consideration of this to a later paper.

For the remaining compounds, including nitriles, a number of conclusions can be drawn. Thus, the *β* and *DN** values are essentially diferent measures of the same molecular property and are substantially determined by the magnitude of the negative charge on the most negative atom in the molecule and the energy of the orbital from which charge donation will occur. Perhaps surprisingly, given what one commonly reads, there is no detectable influence of the dipole moment of the solvent molecule nor of its polarizability on β and *DN**.

The relative importances of Q_{q-} and $Q_{E(OMO)}$ are made ambiguous by the differences of the partial atomic charges recovered using the Hirshfeld and CM5 methods (see Table [5](#page-12-0) for example). Thus, with Q_{q-} based on CM5 charges the contribution of $Q_{E(OMO)}$ is around half of that from *Q*q− while the contributions seem to be approximately equal when *Q*q− values are calculated using Hirshfeld charges.

Figure [5a](#page-13-0)–d compare the β values calculated using the four sets of descriptors with the experimental data; the corresponding graphs comparing the calculated *DN** with the experimental values are essentially similar and are provided in the supplementary material.

Consideration of Table [5](#page-12-0) suggests that there is no clear "best method" for calculating the molecular properties, with the R^2 and F values being fairly consistent for the β and DN^* values, except for the *DN** values calculated using the Hartree–Fock method and CM5 derived charges, where the mild signifcances of the quadrupole amplitude, charge on the most positive atom and energy of the accepting (unoccupied) orbital likely afect the statistical results.

It is clear from Fig. [5](#page-13-0)a–d that the values calculated for the nitriles (red triangles) are sensitive to both the calculation method and model used to derive the partial atomic charges, lying on the line through the other values for the DF calculations and CM5 charges but clustering below the line with DF calculations and/or Hirshfeld derived charges. Of course, the values for the other groups of compounds are also shifted by changes in the calculation method or source of partial charges, resulting in the relatively small variations in \mathbb{R}^2 and F.

The present results don't allow the choice of either a preferred calculation method or preferred model for estimating the partial atomic charges.

6 Conclusions

Regression of the experimental *β* and *DN** values against the molecular descriptors recovered from the density functional and Hartree–Fock calculations, with the partial atomic charges estimated using the Hirshfeld and CM5 models yield a remarkably consistent picture.

In both cases the calculated values for the alcohols and some nitrogen bases lie systematically of of the regression line through the alkanes, aromatics, halogenated alkanes and aromatics, esters, carbonates, carboxylic acids, ketones, ethers, nitriles, phosphates, sulfdes and sulfates. The reason for the diferences between the results for the alcohols and amines and the other solvents isn't clear.

Both *β* and *DN** are substantially determined by two molecular properties: the charge on the most negative atom of the molecule and the molecular orbital from which charge donation would occur. The apparent relative importance of these properties difers, depending on the method of charge estimation, but is consistent between *β* and *DN** for either method. The last point strongly indicates that *β* and *DN** are essentially measures of the same basicity, despite the diferences in their initial formulation.

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