



Manifestation of Magnetic Characteristics of Zinc Ferrite Nanoparticles Using the Langevin Function

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Received: 16 July 2020 / Accepted: 17 October 2020 / Published online: 7 November 2020
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Abstract

Zinc ferrite (ZnFe_2O_4) nanoparticles were prepared by chemical co-precipitation method. Structural characterization was performed using X-ray diffraction (XRD) and transmission electron microscopy (TEM). Formation of spinel phase was confirmed from XRD studies. Crystallite size and lattice constant of the prepared sample were calculated. TEM images reveal spherical-shaped particles with nanosized distribution. Room temperature magnetic hysteresis loop was recorded using vibrating sample magnetometer (VSM). The magnetization loops exhibit a very narrow loop and behave like superparamagnetic nature. Using the Langevin function, the magnetic behaviour of the prepared nanoparticles was investigated. From the curve fitting, saturation magnetization and reduced magnetization were determined. As-prepared sample was further annealed at three different temperatures namely 800 °C, 1000 °C, and 1200 °C for 2-h duration. The effects of annealing on the structural and magnetic properties were further investigated using XRD and VSM. The observed results on the magnetic characteristics of ZnFe_2O_4 and applicability of the Langevin function are being discussed.

Keywords Magnetization curves · Zinc ferrite · Superparamagnetism · Langevin function · Spinel ferrites

1 Introduction

Magnetic materials occupy an important place in different technological developments. They are extensively investigated and being applied in different fields such as memory devices, biomedical applications, polluted water treatment technologies, and microwave devices [1–3]. Bringing them to various applications requires a good knowledge of their characteristic properties which necessitates the detail understanding of the magnetization curves. Different researchers reported theoretical models with an attempt to describe different kinds of magnetic materials [4–6]. On the other hand, these models are being tested and applied to a variety of materials by many experimentalists [7–11]. It includes different forms of law of approach to saturation magnetization, the Langevin function for paramagnetic and superparamagnetic materials. They are reported to be used to investigate the magnetic characteristics of different kinds of magnetic materials. Fine magnetic nanoparticles

arouse great interest to researchers because of their superparamagnetic properties and hence their applicability of different areas. Among them, ZnFe_2O_4 nanoparticles are also reported to be an important one having superparamagnetic properties. ZnFe_2O_4 belongs to the category of spinel ferrites which occupies an important class of magnetic materials [1, 12]. Spinel ferrites have a unit cell composed of 32 oxygen atoms in a cubic closest packing, leaving behind two interstitial sites, namely the tetrahedral (A) and octahedral (B) sites available for the cations. Normally, for ZnFe_2O_4 , Zn^{2+} occupies A sites and hence belongs to the category of normal spinel ferrites. Different synthesis routes such as solid state method, sol gel, auto-combustion, hydrothermal, and co-precipitation method have been reported for the synthesis of spinel ferrites [13–17]. Their properties in general are reported to be dependent on their synthesis methods as well as other processing conditions such as pH of the reaction, and heat treatment temperature and duration [17–19].

In this work, we investigate the structural and magnetic properties of fine nanoparticles of ZnFe_2O_4 along with the effect of annealing temperature on their characteristic properties. Also, we report studies on the magnetization data using the Langevin function and determination of the intrinsic magnetic parameters associated with them.

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2 Experimental Details

2.1 Materials and Method

Zinc ferrite nanoparticles were prepared by a simple coprecipitation method. The starting materials were zinc (II), chloride (dry ZnCl_2), iron (III), chloride anhydrous (FeCl_3), and sodium hydroxide (NaOH). Aqueous solution of 0.5 M MnCl_2 and 1 M FeCl_3 was mixed at 60 °C with continuous stirring. It was then added to 0.6 M NaOH solution which was initially heated at 80 °C with continuous stirring. The solution was maintained at 85 °C for 1 h. The precipitate obtained was centrifuged and washed several times with distilled water and dried at 80 °C. Then, the product so obtained was grounded into fine powders. Furthermore, the sample was annealed at three different temperatures, namely 800 °C, 1000 °C, and 1200 °C, for 2 h in open air. The sample was then finally subjected to different characterizations.

2.2 Characterization

The phase structure of the prepared ZnFe_2O_4 was studied by X-ray diffraction (XRD) with $\text{Cu-K}\alpha$ radiation. TEM images for as-prepared sample were recorded with a TEM 200 kV (JEM-2100). The magnetic study was carried out using vibrating sample magnetometer (VSM Lakeshore 7410). All the abovementioned measurements were conducted at room temperature.

3 Result and Discussion

3.1 XRD

The XRD patterns of the prepared ZnFe_2O_4 nanoparticles are presented in Fig. 1. It confirms the formation of spinel phase of ZnFe_2O_4 corresponding to the standard reference pattern ICDD-01-070-6491. The average crystallite size, D , was calculated using the Scherrer formula

$$D = \frac{k\lambda}{\beta \cos\theta} \quad (1)$$

where λ is the wavelength of the X-ray used, k is a constant related to the shape of the particles, and β being full width at half maximum of the diffraction peak. Instrumental broadening was determined using standard silicon powder. The corrected full width at half maximum value, β , was determined using the relation $\beta^2 = \beta_o^2 - \beta_i^2$, where β_o and β_i are observed full width at half maximum and full width at half maximum due to instrumental broadening respectively. Taking $\lambda = 0.15406$ nm, $k = 0.9$, and using β of the most intense peak in the XRD pattern, average crystallite sizes were

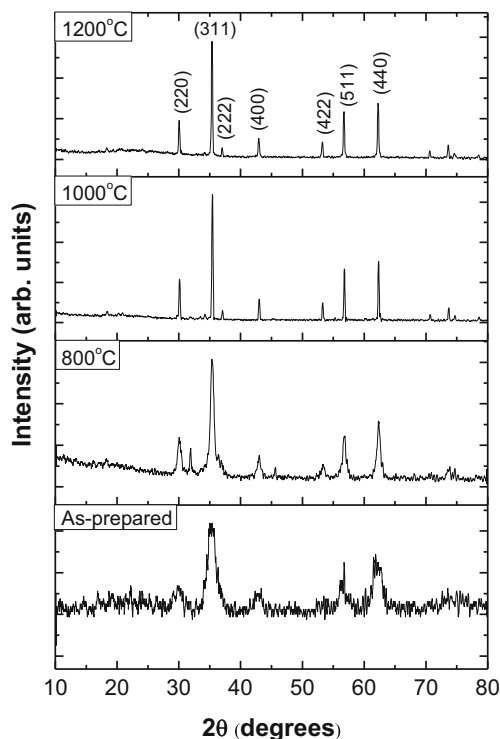


Fig. 1 XRD pattern of as-prepared and annealed ZnFe_2O_4 nanoparticles

calculated which are listed in Table 1. It was found to be 7 nm for as-prepared and 21, 103, and 106 nm for annealed at 800, 1000, and 1200 °C, respectively. The characteristic broad peaks of the XRD pattern of as-prepared ZnFe_2O_4 also depict its nanosized distribution. On annealing and also with increasing annealing temperature, a remarkable increase in the average crystallite size characterized with narrow and intense peaks can be seen. Using five most intense peaks from the XRD data, lattice constant, a , were determined using the equation

$$a = d \sqrt{h^2 + k^2 + l^2} \quad (2)$$

where d is the inter planer spacing and h , k , and l being the miller indices of the diffraction peaks. The calculated values of lattice constant are given in Table 1. Lattice constant of as-prepared sample shows a larger value as compared to the annealed samples. This may have arisen due to the size effects as owing to its nanosized nature, the structural perturbation may have resulted. Similar results have also been found in the literature [20]. Also, a remarkable contribution may come from the variation in the cationic distribution. It is reported that ZnFe_2O_4 in nanoregime is found to have mixed spinel structure while in bulk has normal spinel structure. The processing parameters like annealing temperature have an impact on the cation distribution and hence lattice constant of ZnFe_2O_4 . The combined effects of the above mentioned factors may have resulted in the variation of lattice constant of ZnFe_2O_4 with different annealing temperature.

Table 1 Crystallite size (nm), lattice constant (Å), M_s (emu/g), H_c (Oe), M_r (emu/g), magnetic moment, μ (μ_B), R^2 , and χ^2 values of as-prepared and annealed $ZnFe_2O_4$ nanoparticles

Annealing temperature (°C)	Crystallite size (nm)	Lattice constant (Å)	M_s (emu/g)	H_c (Oe)	M_r (emu/g)	Magnetic moment, μ (μ_B)	R^2	χ^2
As-prepared	7	8.512	13.30 ± 0.12	38	0.01	550	0.999	0.007
800	21	8.410	9.15 ± 0.07	58	0.03	739	0.999	0.006
1000	103	8.404	4.46 ± 0.05	58	0.02	676	0.998	0.002
1200	106	8.416	3.72 ± 0.07	69	0.02	530	0.998	0.001

3.2 TEM Studies

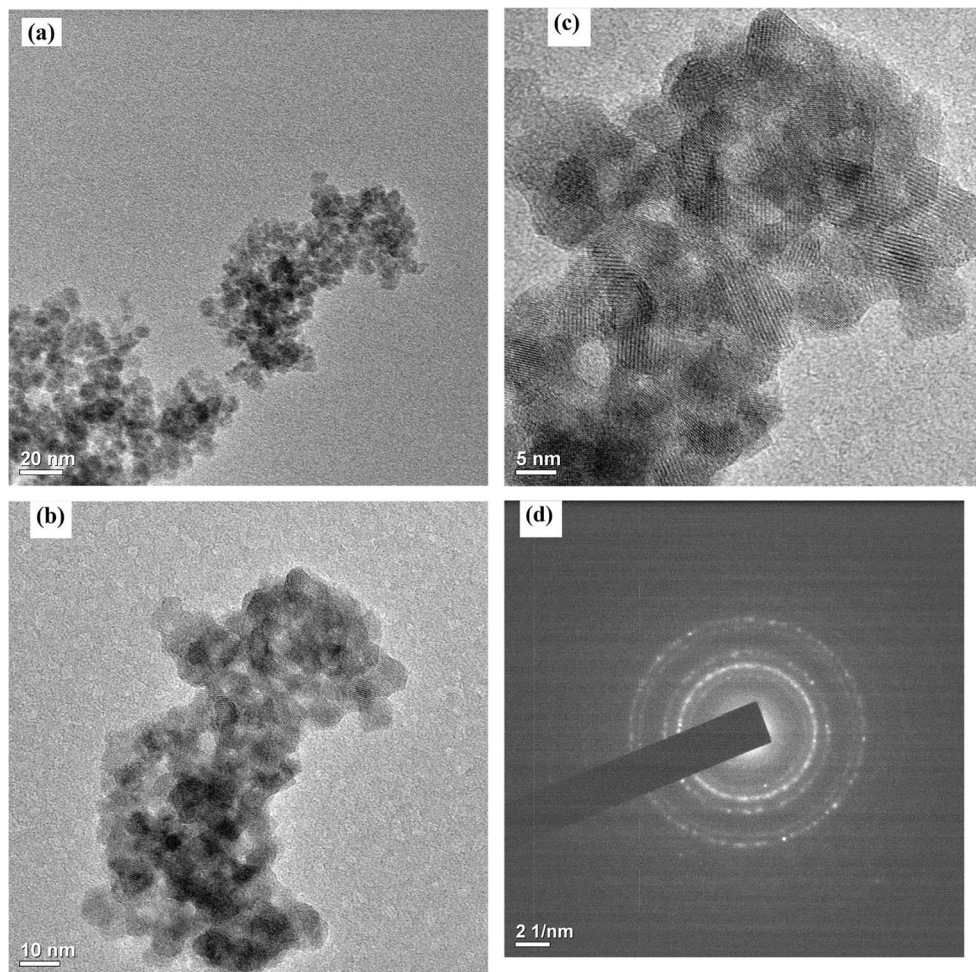
Bright field TEM images at different magnification of the as-prepared $ZnFe_2O_4$ are shown in Fig. 2(a–d). The micrographs depict the formation of almost spherical nanoparticles around an average size of 10 nm. So, the average size is found to be approximately in agreement with the crystallite size obtained from the XRD studies. Lattice fringes of the individual crystallites are also observed in high-resolution image (Fig. 2(c)) depicting the crystalline nature of the nanoparticles. The selected area electron diffraction (SAED) pattern is shown in Fig. 2(d). It can be seen that the SAED pattern consists of spots and rings which clearly

indicates the polycrystalline nature of the prepared $ZnFe_2O_4$ nanoparticles as the rings and spots are resulted from the random orientation of the crystallites of the nanoparticles [21].

3.3 Magnetic Studies

Room temperature magnetization loops of $ZnFe_2O_4$ are shown in Fig. 3. The values of coercivity, H_c , and retentivity, M_r , of the prepared samples obtained from the magnetization loops are listed in Table 1. All the prepared samples possess small values of retentivity lying in the range of 0.01 to 0.03 emu/g. Coercivity of the prepared samples increases with the increase in annealing

Fig. 2 TEM images at different magnification (a)–(c) and selected area electron diffraction pattern (d) of as-prepared $ZnFe_2O_4$ nanoparticles



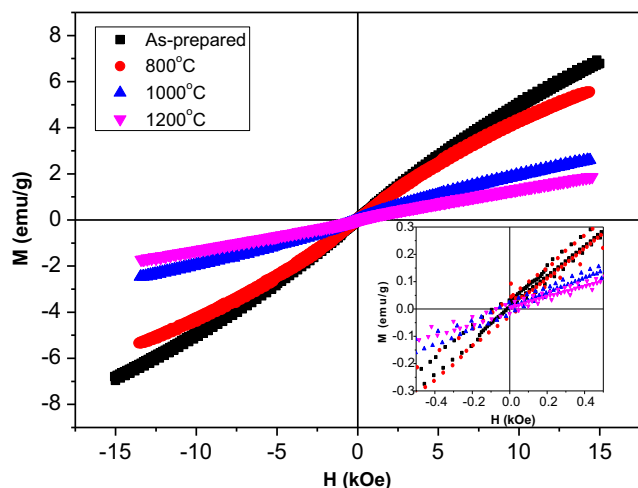


Fig. 3 MH loops of as-prepared and annealed ZnFe_2O_4 nanoparticles

temperature. It may be readily understood in terms of variation of size of prepared samples. Coercivity of nanoparticles has a striking dependence on their size. As the size decreases, coercivity increases in the multi-domain region, reaches a maximum at a critical diameter where particles become single domain and then decrease with further decrease in the size [4]. On the other hand, this observed behaviour gives an indication of the prepared

samples in the single-domain regime. It can be seen that magnetization loops exhibit very narrow loops. As-prepared sample exhibits higher magnetization as compared to annealed samples and magnetization decreases with increasing annealing temperature. On annealing and also with the increase of annealing temperature, the magnetization loops exhibit a transition of slightly S-shaped (in the case of as-prepared) to a linear nature (in the case of annealed) can be observed. To further investigate the nature of the magnetic characteristics, the magnetization data is fitted with the Langevin function which is usually described as

$$M = M_s \left[\coth \left(\frac{\mu H}{k_B T} \right) - \left(\frac{k_B T}{\mu H} \right) \right] \quad (3)$$

where μ , k_B , H , T , and M_s being the reduced magnetic moment, Boltzmann constant, applied magnetic field, temperature, and saturation magnetization, respectively [22, 23].

Magnetization data fitted with the Langevin function are shown in Fig. 4(a–d). It can be clearly seen that the magnetization data of ZnFe_2O_4 fits well with the Langevin function. The goodness of fitting parameters R^2 and χ^2 values along with the fitted parameters are given in Table 1. The closeness of the R^2 value to unity confirms the good fitting of the experimental data with the Langevin equation. Excellent fitting of the magnetization data

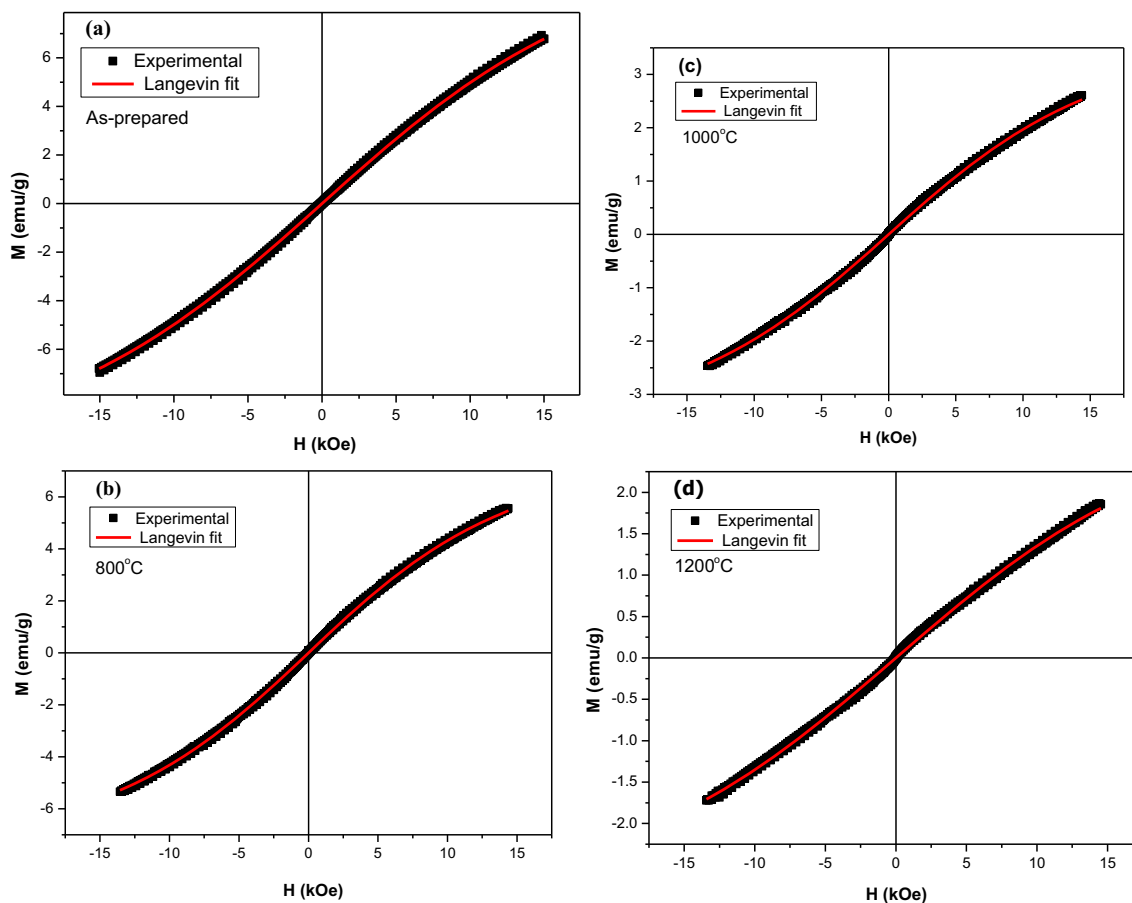


Fig. 4 (a)–(d) Fitting of magnetization data of as-prepared and annealed ZnFe_2O_4 nanoparticles using the Langevin function

with the Langevin function implies that prepared nanoferrites behave like superparamagnetic or paramagnetic nature. Basically, paramagnetic materials possess very weak magnetic moments but in the absence of an external magnetic field, they do not retain any net magnetization because of the randomizing thermal effects. With response to an external applied field, their magnetization curves are characterized by a weak positive and linear magnetization and on removal of the field, magnetization becomes zero. Superparamagnetic materials are usually considered a system of widely spaced or isolated and non-interacting single-domain particles such that magnetic moments of the particles act independently along with instability of magnetization due to thermal agitation. Similar to paramagnetic materials, thermal energy randomizes the magnetization in superparamagnetic materials in the absence of an applied field. However, on application of an external field, they tend to align along the field direction with a much higher magnetization value compared to paramagnetic materials. Owing to its similar behaviour with paramagnetic materials, the Langevin function is reported to be applied to study the magnetization curves of superparamagnetic materials [23, 24]. It is found to apply in different types of materials such as antiferromagnetic nickel oxide nanoparticles, CaFe_2O_4 , Fe_3O_4 , and composites of bismuth ferrites and nickel zinc ferrites [22, 23, 25, 26]. From the curve fitting, saturation magnetization and reduced magnetic moment were determined and are given in Table 1. It can be seen that saturation magnetization decreases with increasing annealing temperature. The observed result may be understood in terms of cation distribution of ZnFe_2O_4 . It has been reported that ZnFe_2O_4 in bulk form belongs to the category of normal spinel ferrite in which Zn^{2+} ions occupy tetrahedral (A) sites and trivalent Fe^{3+} ions occupy octahedral (B) sites of the spinel structure which is usually represented as $(\text{Zn}_1)_\text{A} [\text{Fe}_2]_\text{B} \text{O}_4$ and behaves like paramagnet [27, 28]. However, in the case of ZnFe_2O_4 nanoparticles, partial occupancy of Fe^{3+} in A sites occurs that is $(\text{Zn}_{1-x}\text{Fe}_x)_\text{A} [\text{Zn}_x\text{Fe}_{2-x}]_\text{B} \text{O}_4$ and hence results in an enhanced magnetic moment [27, 28]. Upon the increase in the inversion degree x , the magnetization value changes and hence ferrimagnetic behaviour of nanocrystalline ZnFe_2O_4 . Although the cationic distribution strongly depends on the synthesis method and the processing conditions, it is commonly reported that the low-temperature preparation methods usually have higher inversion degree and hence higher saturation magnetization [20]. The reduced magnetic moment is expressed as the product of volume of the particle and the saturation magnetization [22]. And for spherical particles of diameter D , it is usually given by

$$\mu = \frac{4}{3} \pi \left(\frac{D}{2}\right)^3 M_s \quad (4)$$

Reduced magnetic moment of prepared ZnFe_2O_4 nanoparticles was found to be in the range 530–739 μ_B . An irregular trend in reduced magnetic moment with variation of annealing

temperature can be seen. This may have resulted from two competitive factors as saturation magnetization decreases while size increases with increasing annealing temperature.

Ideally speaking, coercivity is zero for superparamagnetic nanoparticles, but may not be necessarily zero in the case of real samples which are also reported by many researchers [25, 26, 29–31]. In addition, negligible coercivity is not the only criteria for superparamagnetism, but well-fitting of magnetization data with the Langevin function is an indicator of superparamagnetism which is also reported by different researchers [29, 30, 32]. Also, in the case of annealed samples, coercivity is not zero, but their linear characteristics, well-fitting to the Langevin function, negligible retentivity depicts paramagnetic behaviour. Very small values of retentivity (in the range of 0.01–0.03 emu/g) and well-fitting of the Langevin function was common in all the samples but differences in saturation magnetization values ($M_s = 13.30 \pm 0.12$ for as-prepared and $M_s = 3.72 \pm 0.07$ for 1200 °C annealed ZnFe_2O_4) were observed. This implies a clear transition from superparamagnetic to paramagnetic nature of ZnFe_2O_4 samples on annealing and with increasing annealing temperature.

4 Conclusion

Spinel phase ZnFe_2O_4 nanoparticles were successfully synthesized by a low-temperature co-precipitation method. Average crystallite size of the as-prepared ZnFe_2O_4 calculated using XRD was found to be 7 nm. TEM reveals spherical-shaped nanoparticles. On subjecting to annealing temperature of 800, 1000, and 1200 °C, crystallite size increases to 21, 103, and 106 nm, respectively. Coercivity was observed to be increased with the increase of annealing temperature. Increase in coercivity with increasing size of the prepared nanoparticles gives an indication of the prepared samples in the single-domain regime. Excellent fitting of magnetization data with the Langevin function was observed for all the prepared samples. Saturation magnetization and reduced magnetic moment were obtained from the curve fitting. Saturation magnetization decreases with increasing annealing temperature which may have arisen due to change in the inversion degree of the cation distribution. As-prepared samples seem to possess a superparamagnetic behaviour which transforms to paramagnetic one with increasing annealing temperature. The overall results show that magnetization data of ZnFe_2O_4 nanoparticles can be successfully described by the Langevin function.

Acknowledgements Elangbam Chitra Devi is thankful to the University Grants Commission, New Delhi, India, for the award of Dr. D.S. Kothari Post-Doctoral Fellowship (Award No. F. 4-2/2006(BSR)/PH/18-19/0090). Authors are grateful to CIF, IIT Guwahati for VSM measurements and SAIF, NEHU for TEM measurements.

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