

ULTIMA: Magnetic Field Dependence of the Calibration Factor

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Abstract ULTIMA is a project which proposes to use superfluid ^3He as a sensitive medium for direct dark matter search. In this paper we report on new, detailed calibrations of our bolometric cells as a function of the magnetic field. An influence on the order of 20% on the peak height after an energy deposition is observed for magnetic fields up to 330 mT. Simultaneous measurements of neutron capture and heater events, releasing both a well defined energy, show that the effect is similar for both, and that it is possible to maintain a good calibration by an appropriate correction.

Keywords Superfluid ^3He · Bolometry · Magnetic field dependence

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1 Introduction

The basic building block of our bolometers is a closed cell with a small orifice, immersed into and filled with superfluid ^3He at very low temperatures. At temperatures $T \approx 0.15 T_C$, where T_C is the superfluid transition temperature, the heat capacity of the ^3He is small enough that if one measures the temperature inside the cell, this can be used for detecting elementary particle events, with the superfluid ^3He being the target material [1, 2].

A substantial advantage of this type of bolometer is the possibility to calibrate it by direct heating of the quasiparticles by a mechanical moving object. For the purpose

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of both, thermometry and heating, we have used Vibrating Wire Resonators (VWR). VWR thermometers at ultra low temperatures are well studied objects [3, 4]. For the calibrated heat pulses we have used a second VWR also located in the cell [5]. The direct calibration procedure makes this type of bolometers a very special particle detector, as it does not rely on a relative or “theoretical” calibration.

Until now, the magnetic field dependence of this calibration was considered to be negligible. New measurements show that with fields up to 330 mT, the calibration factor changes by as much as 20%. Even if under usual working conditions the magnetic field is limited to about 120 mT, for precise calibrations, magnetic field corrections thus have to be applied.

2 Bolometric Calibration by Heater Pulses

The bolometrical cells are 0.13 cm^3 copper boxes filled with superfluid ^3He and linked to an outer ^3He reservoir by a small orifice. The temperature inside the cell is monitored by a Vibrating Wire Resonator (VWR). A VWR is a fine superconducting NbTi wire, bent into semi-circular shape and oscillating perpendicular to its plane, driven by the Laplace force. The damping of the VWR is dominated by the interaction with the quasiparticle gas, whose density exponentially depends on temperature. A frequency sweep over the resonance thus delivers a Lorentzian whose FWHM $W(T)$ contains the information about the temperature. In the zero field limit, $W(T)$ writes [6]

$$W(T) = \alpha \exp(-\Delta/k_B T), \quad (1)$$

where Δ is the superfluid gap at zero temperature and zero field, and α a prefactor which depends on properties of the VWR and the liquid (for details see Ref. [6]). For to obtain this equation, the contributions of quasiparticles incoming from all different directions \hat{k} have to be integrated. At zero field, where the dispersion relation is isotropic, the integral is analytic and the above result is obtained. For finite magnetic field, the superfluid gap deforms [7] and to get the corresponding relation $W(T, B)$, a correction has to be applied to the above formula. The theoretical magnetic field dependence $W(T, B)$ has not yet been determined, but measurements done in Lancaster [8] give experimental evidence that for non zero field, W indeed increases.

After a heating event caused for example by a cosmic particle, the temperature inside the cell will suddenly rise, and then go back to its initial temperature by thermalisation via the hole. A method used to simulate such an event is to introduce by a second VWR a well known energy by mechanical friction [2, 9] (see Fig. 1) For small enough pulses, the height of the resulting peak (H , in Hz) is proportional to the heat injected (E), and we can define the calibration coefficient as $\sigma = H/E$. A detailed calculation [5] shows that this calibration coefficient is proportional to the temperature derivative of $W(T)$, $W'(T)$ and inversely proportional to the heat capacity ($C(T)$):

$$\sigma = \frac{1}{C(T)} \frac{dW(T)}{dT} = \frac{1}{C(T)} W'(T). \quad (2)$$

Fig. 1 (Color online) Example of a typical heater pulse. The heater wire is excited during a short time (80 ms) with a current I (inset, red bold line). The VWR starts to move and induces a voltage U (inset, black dashed line). The total energy E injected is obtained as the integral of the electric power: $E = \int UI dt$. At the same time, an increase of the resonance width of the VWR thermometer can be observed (black circles). The peak shape is well understood and can be fitted (red line). After some corrections [5], the peak height divided by the energy gives the calibration factor σ

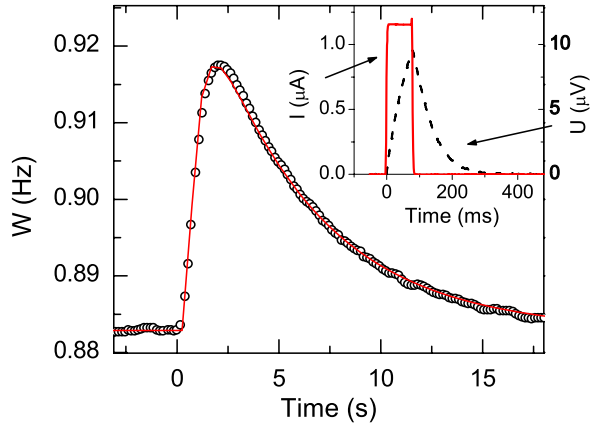
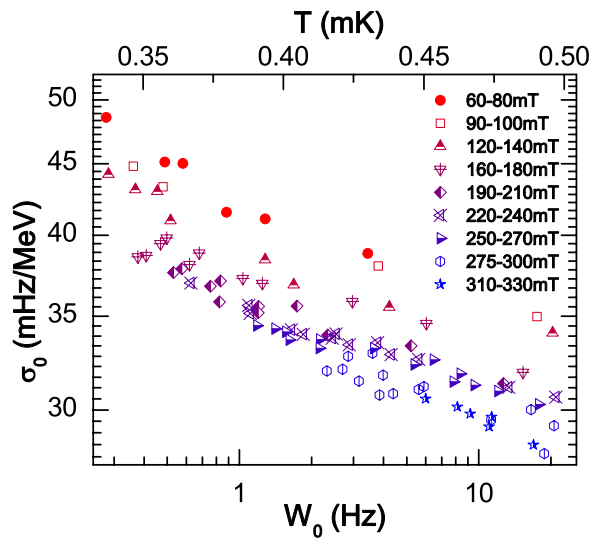


Fig. 2 (Color online) Calibration factor for different baseline widths and magnetic fields (29.3 bar). The exact conversion between $W(T, B)$ and the temperature is only known for $B = 0$ T, so that the temperature scale on the top only has indicative character. For constant magnetic field, the expected $1/\sqrt{T}$ dependence is found



The heat capacity is dominated by the quasiparticle gas. As the total number of quasiparticles strongly depends on the gap, a distortion of the gap should modify this term too, so that the magnetic field dependence of the calibration coefficient is the result of both factors, C and W' , depending on magnetic field.

For zero field, the temperature dependence for both factors is known, and a remarkable feature of this kind of bolometer is that the exponential temperature dependence cancels, and a weak $1/\sqrt{T}$ dependence is expected, meaning that the calibration factor does not change much over the temperature range of interest.

3 Magnetic Field Dependence

The working temperatures down to 130 μK are reached using a nuclear demagnetisation cryostat. We use a Lancaster style nuclear stage, so that the experimental cells are in the main coil, and the magnetic field is the final field of the demagnetisation. This in turn means that changing the field without changing the temperature is impossible. Changing the temperature at constant field can be done by heating, e.g. using a third VWR, but due to the huge solid liquid thermal boundary resistance (Kapitza resistance), thermalisation after such heating takes too long time (>3 h). The most efficient method which was found was to change the magnetic field stepwise and measure at the resulting temperature. Figure 2 presents the results from calibration pulses, all taken during one demagnetisation run. The data are taken at different “baseline widths”, i.e. the equilibrium VWR width W_0 observed between events. Each point corresponds to a total of 25 heater pulses with different heating powers. The calibration factor σ is then taken as the slope in the peak height-energy plot. It can be clearly seen that the magnetic field has a systematic influence. The magnetic field dependence of σ for a constant temperature would be interesting for a quantitative study of this phenomena, but unfortunately no independent thermometry exists in this temperature range, and the field correction for the VWR width is not known. In Fig. 3, σ^{-1} as function of magnetic field is plotted for three different baseline widths. This graph as well as similar graphs for other W_0 show linear behavior, with almost the same slope for the different temperatures. All experimental results can thus be well described by

$$\sigma(W, B) = \frac{\beta}{\sqrt{T(W)}} \cdot \frac{1}{1 + \gamma B}, \quad (3)$$

where β is a constant which depends on superfluid ^3He parameters and the VWR geometry, $T(W)$ is the temperature as obtained using the zero field formula (1), and γ a phenomenological constant. At 29.3 bar we find $\gamma(29.3 \text{ bar}) = 1.25 \pm 0.09 \text{ T}^{-1}$.

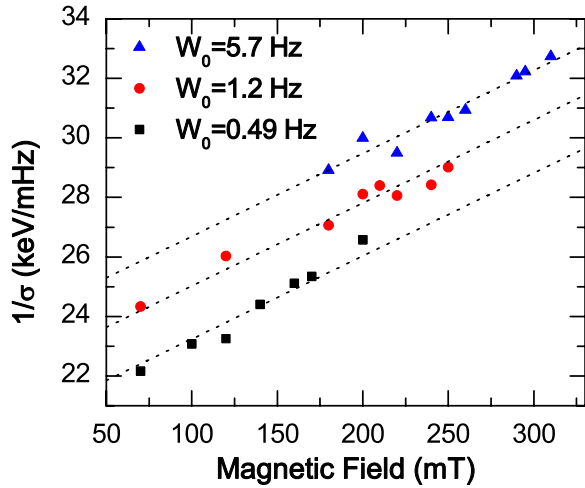
4 Discussion

The presented results were taken at 29.3 bar, because at higher pressures, the superfluid transition temperature T_C is higher ($T_C(29.3 \text{ bar}) = 2.43 \text{ mK}$) and a higher field range can be measured. Measurements at lower pressures qualitatively show the same behavior.

The linear dependence in B for constant baseline width is at first very surprising, especially because one expects for symmetry reasons a quadratic correction in field for both, the specific heat and the resonance width of the VWR. Preliminary numerical simulations however show that under certain conditions, quadratic field corrections for constant temperatures can lead to a linear correction of calibration factor for constant baseline width. More detailed simulations are still a work in progress.

A second method which can be used for calibration is to use a neutron source for the production of nuclear capture reactions. This reaction releases a well defined energy of about 764 keV, of which about 652 keV are transferred to heat. Using this

Fig. 3 (Color online) $1/\sigma$ for three different, almost constant baseline widths W_0 . Similar graphs at different W_0 indicate that for the whole measured range 0.2 to 20 Hz, $1/\sigma$ is linear with magnetic field strength: $\sigma(W_0 = cst) \propto 1/(1 + \gamma B)$. The precision is not sufficient to conclude whether or not γ varies with W_0 but in any case, the dependence is rather weak



second method and applying at the same time heater pulses demonstrates that the influence of the magnetic field is not limited to heater pulses. This is a very important observation for the ULTIMA project, as it shows that the influence of the magnetic field introduces an additional correction factor which needs to be considered, but that it does not prevent achieving a proper energy calibration.

To conclude, we observed a magnetic field dependence of the calibration factor. While a complete numerical understanding is still missing, a phenomenological characterisation is possible. Accounting for this effect opens the way for a future dark matter detector with an accurate energy resolution.

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