



# Weakly Radio-Frequency Negative Permittivity of Poly(vinylidene fluoride)/Ti<sub>3</sub>SiC<sub>2</sub> MAX Phase Metacomposites

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## Abstract

While metal or carbon materials served as conductive phase in fabricating metamaterials or metacomposites have been widely investigated, MAX phases could provide alternative route. In this paper, Poly(vinylidene fluoride)/Ti<sub>3</sub>SiC<sub>2</sub> MAX phase metacomposites with different Ti<sub>3</sub>SiC<sub>2</sub> content were fabricated. Electrical and dielectric properties of metacomposites were analyzed. Percolating phenomenon was observed over the percolation threshold ( $f_c$ ). Below  $f_c$ , ac conductivity spectra were explained by Jonscher's power law, indicating hopping conduction behavior. Above  $f_c$ , ac conductivity of composites follows Drude model, suggesting the metal-like conductive behavior. Weakly negative permittivity behavior was observed and explained by Lorentz and Drude model, suggesting the combinative contribution of induced electric dipole resonance and low-frequency plasmonic oscillation. The impedance performance of composites were also clarified by Nyquist plots and equivalent circuit analysis, manifesting the capacitive-inductive shift of composites. This work presented a novel route to metacomposites with weakly negative permittivity which greatly benefitted the practical applications of MAX phase in metacomposites.

**Keywords** Negative permittivity · Metacomposites · MAX phase · Metamaterials · PVDF

## 1 Introduction

The percolating theory was brought up initially in disordered systems to analyze sudden change of physical properties, broadening its application in heterogeneous materials. The percolation transition was generally presented in heterogeneous multicomponent composites. Actually, filler in composites was gradually contacted with each other

leading to a continuous cluster throughout the composites when increasing filler content approaches  $f_c$  [1]. Accompanied with microstructure changing, percolative composites also underwent sudden change in some physical properties. For instance, positive/negative permittivity was tuned by controlling the functional phase content below/above  $f_c$ . Therefore, metacomposites with negative permittivity can be designed and fabricated following the percolative composite route.

Metamaterials with negative permittivity  $\epsilon'$  have been extended into multiple novel applications which hardly can be realized by conventional materials [2]. Specifically, applications in perfect lens, invisible cloaking, wireless power transfer (WPT), magnetic resonance imaging and colossal permittivity materials [3] have been developed due to their exotically physical properties (e.g., negative refraction index, reversed Doppler effect and Vavilov–Cherenkov effect). In fact, the fascinating performance of metamaterials generally originates from their artificial and periodical metal structures (split-ring resonators, fishnets, wires or cut-wire pairs) [4–6]. Great achievements of metamaterials have been reported in recent years, some characteristics of metamaterials can be summarized.

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For example, in order to tune the negative electromagnetic parameters, shape, size or geometric arrangement in metamaterials should be redesigned, leading to complex constructing process [3, 6–9]. Besides, anisotropic electromagnetic response in metamaterials will usually trigger an adverse impact when applied in electronics [10]. Metacomposites with random functional units were promising candidates to broaden the scope of metamaterials [11, 12], which can be fabricated by typical and traditional preparation technology of materials and could be designed on the basis of percolation theory.

When constructing metacomposites, metallic fillers (e.g., Fe, Ni, Cu or Ag) were usually served as conductive functional phases hosted in insulating matrixes. Negative parameters corresponding to the chemical composition and microstructure of metacomposites could be easily tuned [13, 14]. Negative permittivity could also be observed in metacomposites consisting of metallic alloys or amorphous alloys (e.g.,  $\text{Fe}_{50}\text{Ni}_{50}$ ,  $\text{FeNiMo}$  or  $\text{Fe}_{78}\text{Si}_9\text{B}_{13}$ ) [15–17]. However, development of metal-based metacomposites were limited by the excessive power loss in composites and electromagnetic interference (EMI) to surrounding metal electronics [15, 18]. Under this circumstance, we presented a new route to metacomposites by consisting of nonmetallic conductive functional phases, “MAX” phases.  $\text{M}_{n+1}\text{AX}_n$  phase was a group of layered ternary materials, where  $n$  is 1, 2 or 3, M is an early transition metal, A is an A-group element, and X is either C or N. MAX phases have triggered tremendous attentions due to their promising applications in structural reinforced ceramic matrix composites (CMCs), battery electrodes materials and supercapacitors [19–21]. MAX phases presented combination properties in metal and ceramic, including high-temperature oxidation resistance, damage tolerance, machinability, great electrical conductivity, and excellent irradiation/corrosion resistance [22–30]. Among all the MAX phases,  $\text{Ti}_3\text{SiC}_2$  exhibits great electrical conductivity and structural performance which makes it a promising candidate for preparing metacomposites [19]. Poly(vinylidene fluoride) (PVDF) was a semicrystalline thermoplastic polymer with high piezo- and pyroelectric coefficients, great thermal and chemical resistance. PVDF has been employed into percolative composites with colossal permittivity by containing functional phases (e.g.,  $\text{BaTiO}_3$ , PZT) [31–51]. Therefore, PVDF and  $\text{Ti}_3\text{SiC}_2$  MAX phase was selected as matrix and functional phase respectively to fabricate percolative metacomposites towards negative permittivity.

In this work,  $\text{Ti}_3\text{SiC}_2$ /PVDF metacomposites with different  $\text{Ti}_3\text{SiC}_2$  content were prepared. The electrical and dielectric properties were investigated at radio frequency range (20 MHz–1 GHz). The different variation trends of ac conductivity spectra verified the percolation threshold. Negative permittivity behavior was observed in composites

above  $f_c$ . Equivalent circuit models were applied to analyze the impedance response of  $\text{Ti}_3\text{SiC}_2$ /PVDF composites.

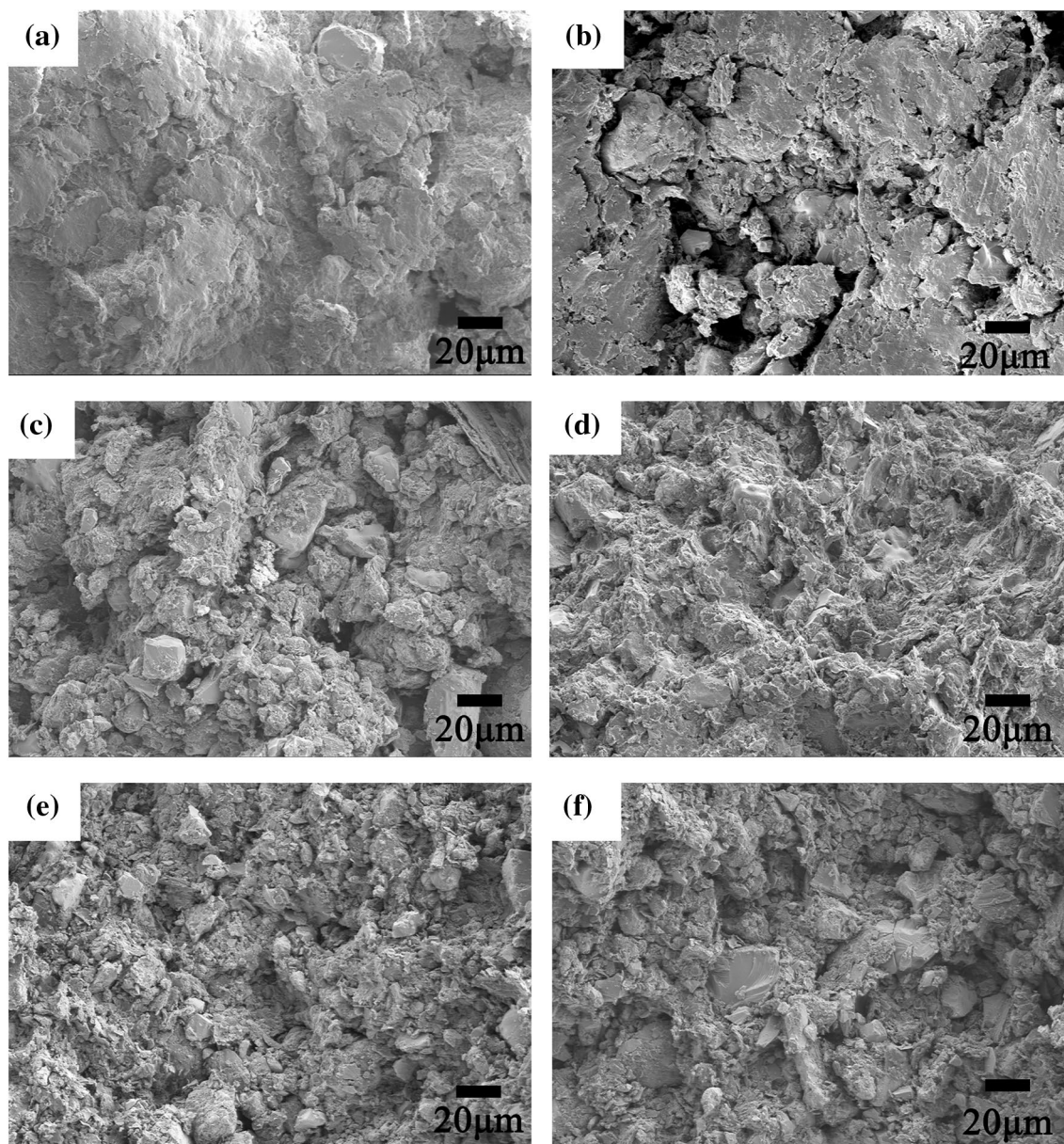
## 2 Materials and Methods

$\text{Ti}_3\text{SiC}_2$  (purity > 98%, average size ~ 44  $\mu\text{m}$ ) were purchased from Haoxinano Technology Co., Ltd. Poly(vinylidene fluoride) were acquired from Shenzhen Boyi Plastic Raw Material Co., Ltd. The composites with  $\text{Ti}_3\text{SiC}_2$  content of 10 wt%, 30 wt%, 50 wt%, 60 wt%, 70 wt%, 80 wt%, and 85 wt% were prepared by blending and compression molding procedure. Field emission scanning electron microscopy (FESEM) and X-ray diffractometer (XRD) with Cu  $K_\alpha$  radiation were applied to characterize microstructure and phase composition of composites. The electrical and dielectric properties of composites was tested by Agilent E4991A precision impedance analyzer. The detailed testing and calculating process was presented in Supplementary Information.

## 3 Results and Discussion

### 3.1 Microstructure and Composition Characterization

Figure 1 shows SEM images of  $\text{Ti}_3\text{SiC}_2$ /PVDF metacomposites at different  $\text{Ti}_3\text{SiC}_2$  filling content. The isolated  $\text{Ti}_3\text{SiC}_2$  particles are randomly distributed in PVDF matrix. As increasing  $\text{Ti}_3\text{SiC}_2$  content, the  $\text{Ti}_3\text{SiC}_2$  particles gradually interconnect with each other leading to the formation of three-dimensional (3D) conductive networks in  $\text{Ti}_3\text{SiC}_2$ /PVDF composites (85 wt%). Figure 2 shows XRD patterns of  $\text{Ti}_3\text{SiC}_2$  and  $\text{Ti}_3\text{SiC}_2$ /PVDF composites with different  $\text{Ti}_3\text{SiC}_2$  content. The XRD pattern of PVDF materials was indexed by  $\alpha$ ,  $\beta$ , and  $\gamma$  crystal phases of PVDF. The peak at  $18.4^\circ$  was corresponding to the  $\alpha$ -phase. The peaks of  $20.8^\circ$  and  $26.6^\circ$  indicated the  $\beta$ -phase superposition and  $\gamma$ -phase diffraction respectively. As increasing  $\text{Ti}_3\text{SiC}_2$  content, the diffraction peaks of PVDF were wakening while the diffraction peaks of  $\text{Ti}_3\text{SiC}_2$  were enhancing. FT-IR experiments of raw PVDF materials were performed as shown in Fig. 3a. The FT-IR spectra showed the typical absorption peaks of  $\alpha$ -phase,  $\beta$ -phase, and  $\gamma$ -phase of PVDF at about  $613\text{ cm}^{-1}$ ,  $488\text{ cm}^{-1}$  and  $841\text{ cm}^{-1}$ , respectively. The bending of C–C–C is observed at  $1071\text{ cm}^{-1}$ , and the peak of  $\text{CH}_2$  appears at  $1403\text{ cm}^{-1}$ . Figure 3b shows the simultaneous DSC/TGA curves of PVDF raw materials measured at heating rate 10 K/min in air. As temperature rising, the weight of PVDF materials kept unchanged below  $350^\circ\text{C}$  and then starting losing weight. DSC curve shows an endothermic peak at about  $380^\circ\text{C}$  and an exothermic peak at about  $485^\circ\text{C}$  which could be attributed to the decomposition of



**Fig. 1** SEM images of  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  metacomposites with  $\text{Ti}_3\text{SiC}_2$  content of 10 wt% (a), 30 wt% (b), 50 wt% (c), 70 wt% (d), 80 wt% (e), and 85 wt% (f)

PVDF. PVDF becomes exothermic over 450 centigrade, suggesting that the heat quantity originating from PVDF decomposed reaction was larger than that from PVDF melting.

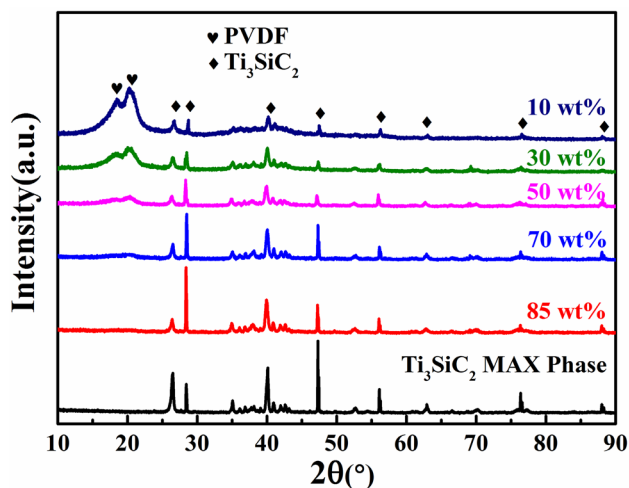
### 3.2 Conductivity Behavior

Figure 4 shows the frequency dependences of ac conductivity ( $\sigma_{ac}$ ) in  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  metacomposites with different  $\text{Ti}_3\text{SiC}_2$  content.  $\sigma_{ac}$  increased on frequency rising when  $\text{Ti}_3\text{SiC}_2$  contents were lower than that of 80 wt% in composites, while  $\sigma_{ac}$  decreased with frequency for composites at higher filling content. It is noteworthy that  $\sigma_{ac}$  sharply

increases ( $\epsilon'$  sharply decreases) when  $\text{Ti}_3\text{SiC}_2$  content range from 80 to 85 wt% as shown in Fig. 5d. Further to say, the different variation trends of  $\sigma_{ac}$  versus frequency indicated different conductive mechanisms. Percolation behavior occurred in  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites on raising  $\text{Ti}_3\text{SiC}_2$  content. The percolation threshold  $f_c$  was between 80 and 85 wt%, which was verified by the different conductive model. For composites below  $f_c$ , the  $\sigma_{ac}-f$  relationship can be expressed as:

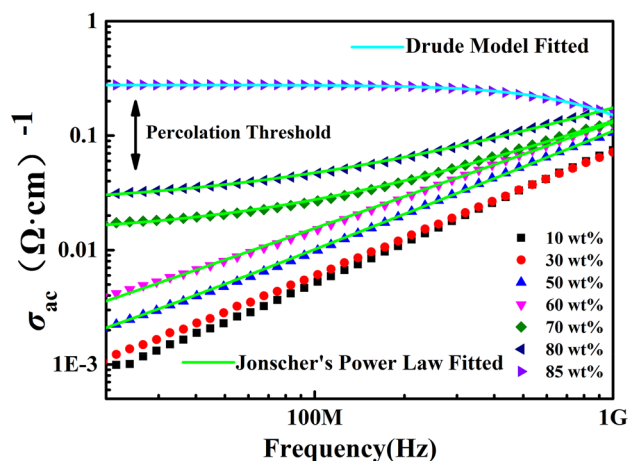
$$\sigma_{ac} = \sigma_{dc} + A(2\pi f)^n \quad (1)$$





**Fig. 2** XRD patterns of  $\text{Ti}_3\text{SiC}_2$  and  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites with different  $\text{Ti}_3\text{SiC}_2$  content

where  $\sigma_{dc}$  is direct current conductivity,  $f$  is the frequency,  $A$  is the pre-exponential factor and  $n$  is the fractional exponent ( $0 < n < 1$ ). For composites (10 wt%, 30 wt%, 50 wt% and 60 wt%), ac conductance was primary over whole test frequency as shown in Fig. 4. As increasing  $\text{Ti}_3\text{SiC}_2$  content to 70 wt% and 80 wt%, dc conductance dominated at low frequency region and ac conductance was primary at high frequency range. The fitting parameters were also confirmed the above analysis shown in Table S3. Experiencing an external electric field (especially high-frequency electric field), free electrons can “jump” across adjacent  $\text{Ti}_3\text{SiC}_2$  particles which was denoted as hopping conduction behavior. When the  $\text{Ti}_3\text{SiC}_2$  content exceeded  $f_c$ , the  $\text{Ti}_3\text{SiC}_2$  particles were interconnected to each other leading to the formation of 3D conductive networks throughout the composites. MAX phase presented metallic conduction (denoted as metal-like



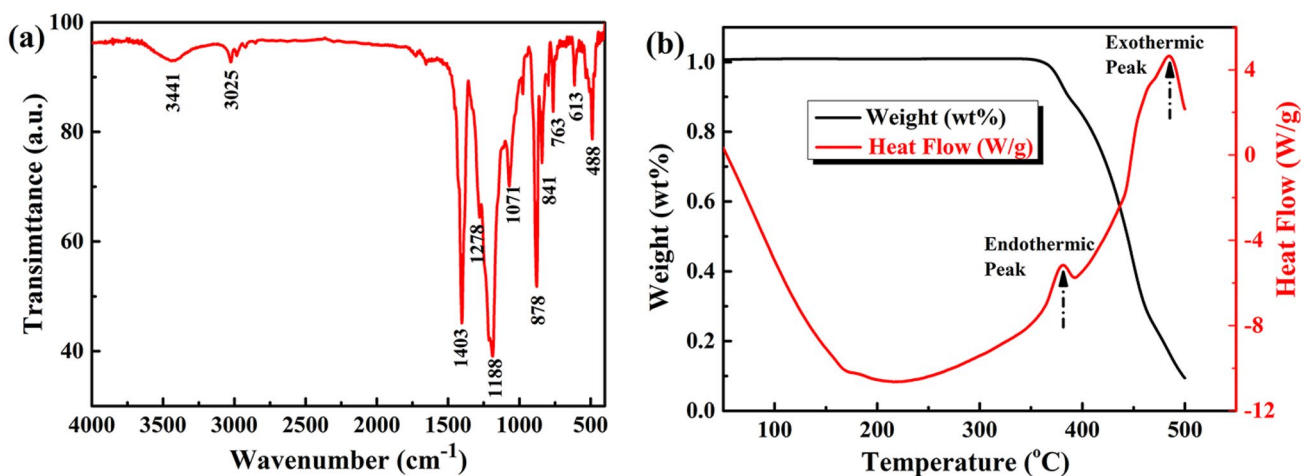
**Fig. 4** Frequency dispersions of ac conductivity for the  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites

conduction behavior), i.e.,  $\sigma_{ac}$  was almost independent of frequency at low frequencies while  $\sigma_{ac}$  decreased at high frequencies. Skin effect was applied to explain the metallic conduction. The skin depth was expressed as:

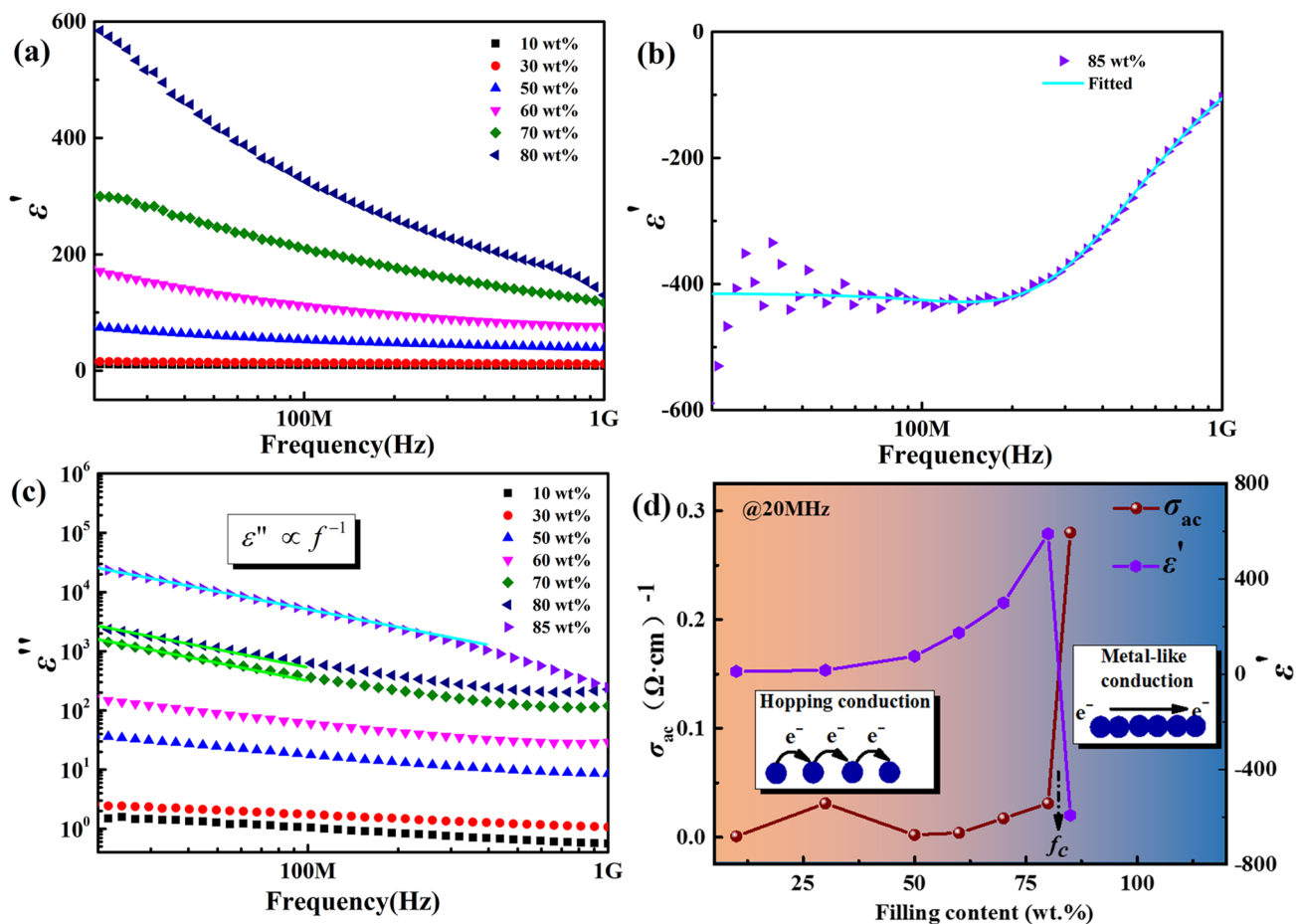
$$\delta = \left( \frac{2}{\omega \mu \sigma_{dc}} \right)^{\frac{1}{2}} \quad (2)$$

where  $\delta$  is the skin depth,  $\omega$  is the angular frequency,  $\sigma_{dc}$  is the dc conductivity, and  $\mu$  is the static permeability of the composites. The increasing frequency reduced the skin depth resulting in enhancement of the skin effects. The metal-like conductive behavior of composites with  $\text{Ti}_3\text{SiC}_2$  content of 85 wt% was explained by Drude model:

$$\sigma_{ac} = \frac{\sigma_{dc} \omega_{\tau}^2}{\omega^2 + \omega_{\tau}^2} \quad (3)$$



**Fig. 3** FT-IR curves of PVDF raw materials (a) and simultaneous DSC/TGA curves for PVDF raw materials (b)



**Fig. 5** Frequency dependences of real permittivity ( $\epsilon'$ ) for  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites (**a**, **b**). Frequency dispersions of the imaginary permittivity ( $\epsilon''$ ) (**c**). Variation trends of ac conductivity and real permittivity at 20 MHz with different  $\text{Ti}_3\text{SiC}_2$  filling content (**d**)

$$\sigma_{dc} = \frac{Ne^2\tau}{m} = \frac{\omega_p^2\tau}{4\pi} \quad (4)$$

where  $\sigma_{dc}$  is the dc limitation in conductivity,  $\omega_\tau$  ( $\omega_\tau = 1/\tau$ ) is the relaxation rate, and  $\omega_p$  describes the oscillator strength.

### 3.3 Negative Permittivity Behavior

Frequency dependences of the real permittivity ( $\epsilon'$ ) of  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  with different  $\text{Ti}_3\text{SiC}_2$  content were showed in Fig. 5a, b. For composites below the percolation threshold  $f_c$ , the values of  $\epsilon'$  were positive and enhanced with increasing  $\text{Ti}_3\text{SiC}_2$  content at 20 MHz–1 GHz region shown in Fig. 5a, d, which could be ascribed to increasing interface connection of isolated  $\text{Ti}_3\text{SiC}_2$  particles and PVDF matrix in the composites. Further, interfacial polarization in these micro-capacitors formed by  $\text{Ti}_3\text{SiC}_2$  particles and PVDF matrix, denoted as Maxwell–Wagner–Sillars effect, was responsible for the improvement of permittivity.

As analyzed above, negative permittivity behavior observed over  $f_c$  in composites, was ascribed to the formation of 3D interconnected  $\text{Ti}_3\text{SiC}_2$  networks.  $\text{Ti}_3\text{SiC}_2$  networks in composites with metallic conduction, generally presented low frequency plasmonic state leading to plasma-type negative permittivity behavior. The plasma-type negative permittivity behavior was theoretically described by Drude model as follows:

$$\epsilon^* = \epsilon' - i\epsilon'' = 1 - \frac{\omega_p^2}{\omega^2 + i\omega\Gamma_D} \quad (5)$$

$$\epsilon' = 1 - \frac{\omega_p^2}{\omega^2 + \Gamma_D^2} \quad (6)$$

$$\omega_p = \sqrt{\frac{n_{eff}e^2}{m_{eff}\epsilon_0}} \quad (7)$$

where,  $\Gamma_D$  is the damping constant,  $\omega_p = 2\pi f_p$  is plasmons angular frequency,  $n_{\text{eff}}$  is effective concentration of electron, and  $m_{\text{eff}}$  is effective weight of electron. However, as shown in Fig. S1, Drude model was not in agreement with the negative permittivity spectra at low frequency regions, suggesting that there should be another generation mechanism. Considering the combinative metallic and ceramic properties of MAX phase, there may be impactions of induced electric dipole at low frequency range. Thus, we combined Lorentz model with Drude model to explain negative permittivity behavior. The Lorentz model was expressed as:

$$\epsilon^* = \epsilon' - i\epsilon'' = 1 + \frac{\omega_p^2}{\omega_0^2 + \omega^2 + i\Gamma_L\omega} \quad (8)$$

$$\epsilon' = 1 + \frac{\omega_p^2(\omega_0^2 - \omega^2)}{(\omega_0^2 - \omega^2)^2 + \omega^2\Gamma_L^2} \quad (9)$$

where  $\omega$  ( $\omega = 2\pi f$ ) is the angular frequency,  $\omega_0$  ( $\omega_0 = 2\pi f_0$ ) is the characteristic frequency,  $\omega_p$  ( $\omega_p = 2\pi f_p$ ) is the angular plasma frequency, and  $\Gamma_L$  represents the damping constant. The Lorentz type dielectric resonance was resulted from the induced electric dipole in the isolated  $\text{Ti}_3\text{SiC}_2$  particles. As shown in Fig. 5b, negative permittivity spectra was fitted well by combination of Drude model and Lorentz model.

Dielectric loss in composites evaluated by imaginary permittivity ( $\epsilon''$ ) was an important performance when applied in electronic devices. In percolative composites, electric field frequency and concentration of conductive fillers were primary influencing factor to dielectric loss. Generally, dielectric loss mainly includes the conduction loss  $\epsilon''_C$ , polarization loss  $\epsilon''_P$  and dipole loss  $\epsilon''_D$ , which was expressed as:

$$\epsilon'' = \epsilon''_C + \epsilon''_D + \epsilon''_P \quad (10)$$

At 20 MHz–1 GHz region, the conduction loss and dipolar loss were primary loss.  $\epsilon''_C$  originating from leakage current among conductive fillers was expressed as:

$$\epsilon''_C = \frac{\sigma_{dc}}{2\pi f \epsilon_0} \quad (11)$$

where  $\sigma_{dc}$  is a constant. Thus,  $\epsilon''_C$  was inversely related to  $f$  ( $\epsilon''_C \propto f^{-1}$ ). Figure 5c presented frequency dependent  $\epsilon''$  for the  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites with different filling content.  $\epsilon''$  was evidently enhanced ascribing to the incorporation of conductive  $\text{Ti}_3\text{SiC}_2$  particles. For the composites below  $f_c$ ,  $\epsilon''$  spectra exhibited liner decrease trend in low frequency. With increasing frequency, relationship of  $\epsilon''$  versus  $f$  presented nonlinear increasing trend. In other words, the dominant role in dielectric loss changed from the  $\epsilon''_C$  to the  $\epsilon''_D$  with frequency rising.

### 3.4 Impedance and Equivalent Circuit Analysis

For  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites with positive permittivity, the reactance showed negative values at 20 MHz–1 GHz region (Fig. 6a). The relationship for different circuit elements was expressed as:

$$Z = \frac{\dot{U}}{\dot{I}} = R + i(X_L - X_C) = Z' + iZ'' \quad (12)$$

$$\varphi = \arctan \frac{\dot{U}_X}{\dot{U}_R} = \arctan \frac{\dot{U}_L - \dot{U}_C}{\dot{U}_R} \quad (13)$$

That is to say, for composites below  $f_c$ , capacitive reactance was stronger than inductive reactance ( $Z'' = X_L - X_C < 0$ ) indicating capacitive character. Equivalent

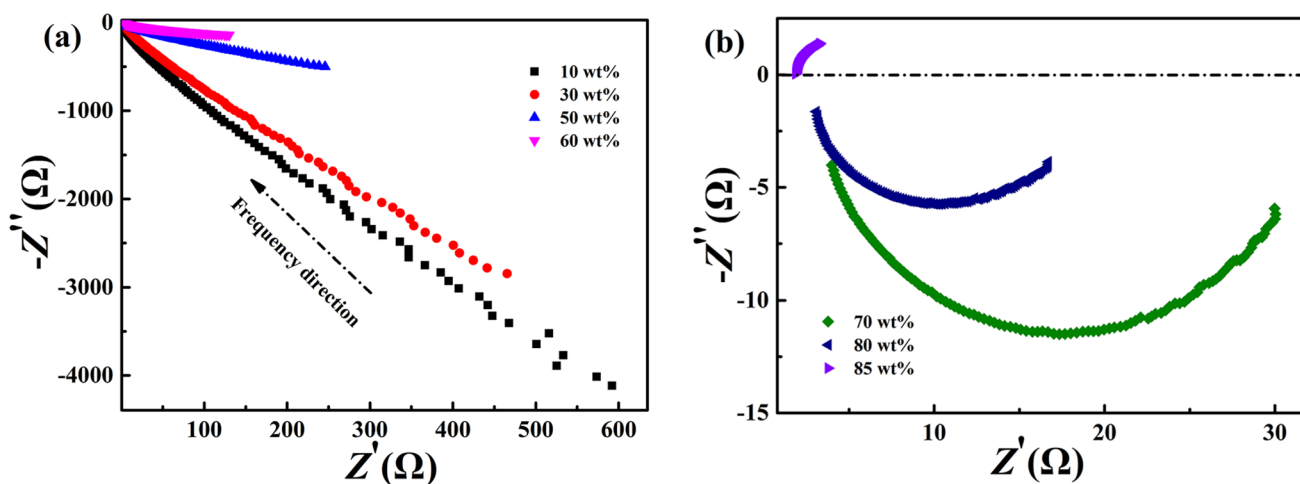
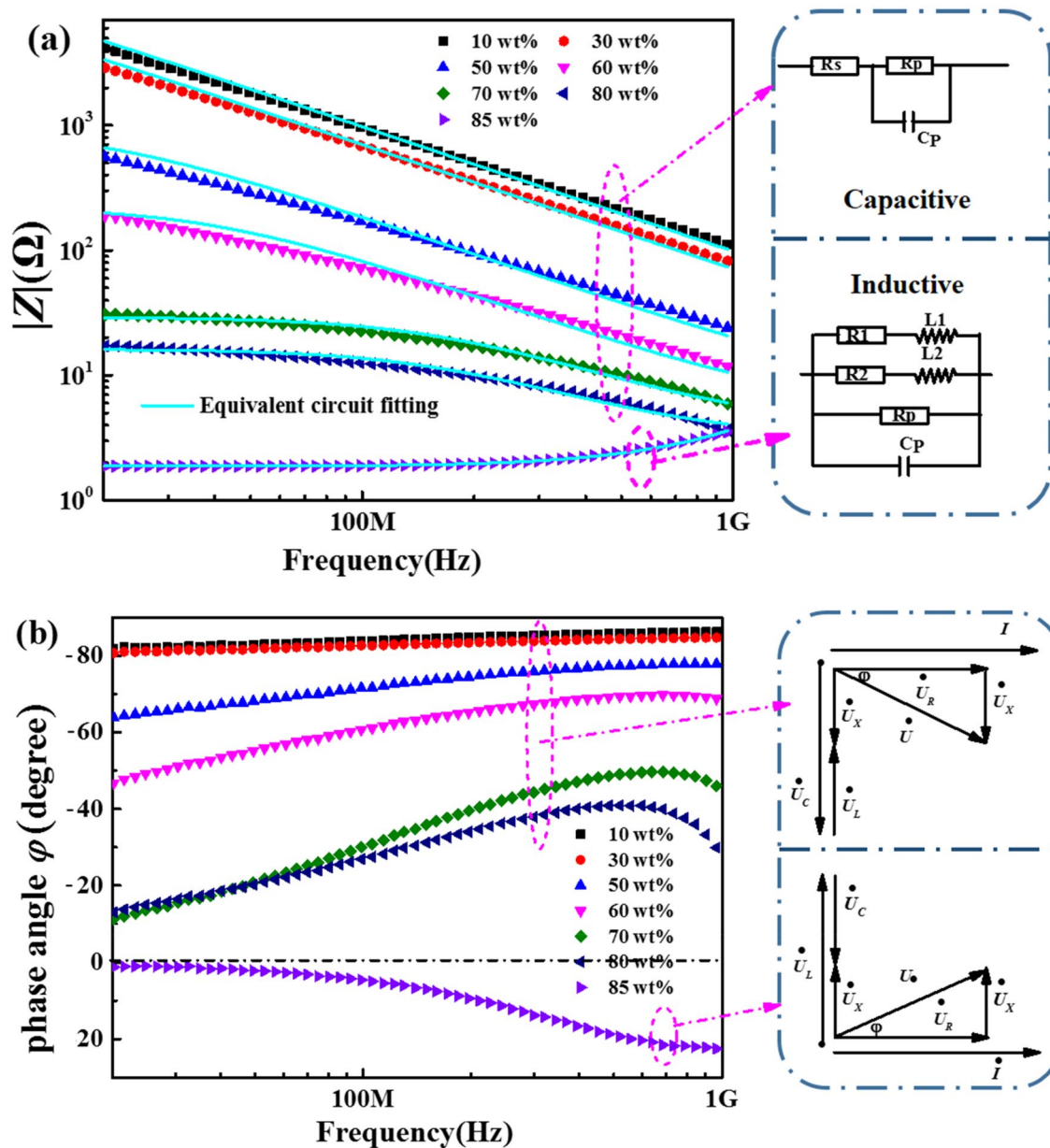


Fig. 6 Nyquist plots (a, b) for the  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites with different  $\text{Ti}_3\text{SiC}_2$  content

circuit models was applied to analyze impedance response of  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites. Equivalent circuit model of composites below  $f_c$  consists of a series resistor ( $R_s$ ) and a parallel connection of a resistor ( $R_p$ ) and a capacitor ( $C_p$ ) (inset of Fig. 7a).  $R_p$ , originating from the leakage current of composites, decreased with increasing conductive  $\text{Ti}_3\text{SiC}_2$  particles in PVDF matrix.  $C_p$ , mainly deriving from the micro-capacitors constructed by the  $\text{Ti}_3\text{SiC}_2$  and PVDF particles in composites, increased on increasing  $\text{Ti}_3\text{SiC}_2$  content. Noteworthy,  $C_p$  sharply increased near  $f_c$ . While capacitive reactance for composites above  $f_c$  was less than

inductive reactance ( $Z'' = X_L - X_C > 0$ ) leading to inductive character. Equivalent circuit model of composites above  $f_c$  consists of resistors ( $R_p$ ,  $R_1$  and  $R_2$ ), capacitor ( $C_p$ ), and inductors ( $L_1$  and  $L_2$ ) as shown in Fig. 7a. As illustrated in Fig. 8a, b, isolated  $\text{Ti}_3\text{SiC}_2$  particles distributed in PVDF matrix were equivalently forming to capacitors, while conductive paths of inductors in composites were formed by connective  $\text{Ti}_3\text{SiC}_2$  particles.

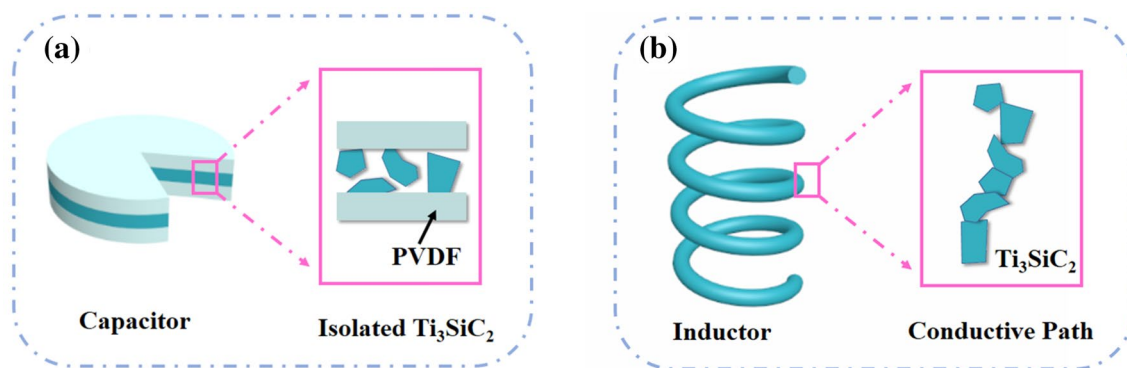
Figure 7b presented frequency dependent  $\varphi$  for  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites with different filling content. When composites experiencing ac electric field, the samples was



**Fig. 7** Frequency dependent impedance (a) and phase angle  $\varphi$  (b) for  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites. Phasor diagrams of voltage versus current were presented in b.  $U$ ,  $I$ ,  $U_R$ ,  $U_L$ ,  $U_X$  and  $U_C$  are voltage or current

phasor for different circuit elements,  $\varphi$  is the impedance angle,  $X_L$ ,  $X_C$  and  $X$  are reactance





**Fig. 8** Schematic evolution of the microstructure corresponding with variation of capacitor (a) and inductor (b)

considered as a typical *RLC* circuit consisting of capacitors (*C*), resistors (*R*) and/or inductors (*L*) shown in Fig. S3 in Supplementary Materials. When sample is pure resistor, the voltage and current is synchronous and  $\varphi = 0^\circ$ . Generally, when sample presents capacitive or inductive, the current and voltage is unsynchronized. Specifically, when the current and voltage flows through a capacitor, voltage lags current by  $90^\circ$  ( $\varphi = -90^\circ$ ). While, the current lags voltage by  $90^\circ$  ( $\varphi = 90^\circ$ ) as the current and voltage flows through an inductor. In  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  composites,  $\varphi$  shifts from negative to positive on increasing  $\text{Ti}_3\text{SiC}_2$  content, indicating transition of capacitive to inductive. For composite below  $f_c$ , the  $\varphi$  values are range from  $-90^\circ$  to  $0^\circ$ . Under this circumstance,  $U_L < U_C$ , thus  $U_X < 0$ , suggests that voltage phase falls

behind the current phase, capacitors dominate in the circuit and composite manifests capacitive character. Correspondingly, composites above  $f_c$  present inductive character when phase shift angle  $\varphi$  values range from  $0^\circ$  to  $90^\circ$ . Under this circumstance,  $U_L > U_C$ , thus  $U_X > 0$ , indicates that current phase lags behind voltage phase, inductors dominates in the circuit and composite manifests inductive character.

## 4 Conclusion

In conclusion,  $\text{Ti}_3\text{SiC}_2/\text{PVDF}$  percolative metacomposites towards negative permittivity were prepared. Conductive mechanism changes when increasing  $\text{Ti}_3\text{SiC}_2$  content over  $f_c$ . Negative permittivity behavior was explained by Lorentz and Drude model, suggesting the combinative contribution of induced electric dipole resonance and low-frequency plasmonic oscillation at radio-frequency region. Equivalent circuit analysis to impedance response of metacomposites manifested correspondence between capacitive-inductive characteristic change and positive–negative permittivity change. This work facilitates clarifying the generation

mechanism of negative permittivity which will greatly extend applications of MAX phase in metacomposites.

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## References

1. D.J. Bergman, D. Stroud, Physical properties of macroscopically inhomogeneous media. *Solid State Phys.* **46**, 147–269 (1992)
2. D.R. Smith, J.B. Pendry, M.C. Wiltshire, Metamaterials and negative refractive index. *Science* **305**, 788–792 (2004)
3. B. Wang, K.H. Teo, T. Nishino, W. Yezuanis, J. Barnwell, J. Zhang, Experiments on wireless power transfer with metamaterials. *Appl. Phys. Lett.* **98**, 254101–254103 (2011)
4. S. Jahani, Z. Jacob, All-dielectric metamaterials. *Nat. Nanotechnol.* **11**, 23–36 (2016)
5. N.K. Grady, J.E. Heyes, D.R. Chowdhury, Y. Zeng, M.T. Reiten, A.K. Azad, A.J. Taylor, D.A. Dalvit, H.T. Chen, Terahertz metamaterials for linear polarization conversion and anomalous refraction. *Science* **340**, 1304–1307 (2013)
6. W.J. Padilla, D.N. Basov, D.R. Smith, Negative refractive index metamaterials. *Mater. Today* **9**, 28–35 (2006)
7. S. Linden, C. Enkrich, M. Wegener, J. Zhou, T. Koschny, C.M. Soukoulis, Magnetic response of metamaterials at 100 terahertz. *Science* **306**, 1351–1353 (2004)
8. V.M. Shalaev, T.A. Klar, V.P. Drachev, A.V. Kildishev, Optical negative-index metamaterials: from low to no loss. *Nat. Photon.* **1**, 41–48 (2006)
9. D.R. Smith, J.B. Pendry, M.C.K. Wiltshire, Metamaterials and negative refractive index. *Science* **305**, 788–792 (2004)
10. X. Zhang, Metamaterials for perpetual cooling at large scales. *Science* **355**, 1023–1024 (2017)
11. M. Chen, X. Wang, Z. Zhang, K. Sun, C. Cheng, F. Dang, Negative permittivity behavior and magnetic properties of C/YIG composites at radio frequency. *Mater. Des.* **97**, 454–458 (2016)
12. N.D. Gavrilova, V.K. Novik, A.V. Vorobyev, I.A. Malyshkina, Negative dielectric permittivity of poly(acrylic acid) pressed pellets. *J. Non-Cryst. Solids* **452**, 1–8 (2016)



13. Z. Zhang, R. Fan, Z. Shi, S. Pan, K. Yan, K. Sun, J. Zhang, X. Liu, X.L. Wang, S.X. Dou, Tunable negative permittivity behavior and conductor–insulator transition in dual composites prepared by selective reduction reaction. *J. Mater. Chem. C* **1**, 79–85 (2013)
14. Z. Zhang, K. Sun, Y. Liu, Z. Kuang, S. Sun, X. Ji, The negative permittivity behavior and magnetic property of FeNi/Al<sub>2</sub>O<sub>3</sub> composites in radio frequency region. *Ceram. Int.* **42**, 19063–19065 (2016)
15. M. Chen, R.H. Fan, M. Gao, S.B. Pan, M.X. Yu, Z.D. Zhang, Negative permittivity behavior in Fe<sub>50</sub>Ni<sub>50</sub>/Al<sub>2</sub>O<sub>3</sub> magnetic composite near percolation threshold. *J. Magn. Magn. Mater.* **381**, 105–108 (2015)
16. M. Chen, M. Gao, F. Dang, N. Wang, B. Zhang, S. Pan, Tunable negative permittivity and permeability in FeNiMo/Al<sub>2</sub>O<sub>3</sub> composites prepared by hot-pressing sintering. *Ceram. Int.* **42**, 6444–6449 (2016)
17. Q. Hou, K.L. Yan, R.H. Fan, Z.D. Zhang, M. Chen, K. Sun, C.B. Cheng, Experimental realization of tunable negative permittivity in percolative Fe<sub>78</sub>Si<sub>9</sub>B<sub>13</sub>/epoxy composites. *RSC Adv.* **5**, 9472–9475 (2015)
18. X.A. Wang, Z.C. Shi, M. Chen, R.H. Fan, K.L. Yan, K. Sun, S.B. Pan, M.X. Yu, Tunable electromagnetic properties in Co/Al<sub>2</sub>O<sub>3</sub> cermets prepared by wet chemical method. *J. Am. Ceram. Soc.* **97**, 3223–3229 (2014)
19. M.A. Piechowiak, J. Henon, O. Durand-Panteix, G. Etchegoyen, V. Coudert, P. Marchet, F. Rossignol, Growth of dense Ti<sub>3</sub>SiC<sub>2</sub> MAX phase films elaborated at room temperature by aerosol deposition method. *J. Eur. Ceram. Soc.* **34**, 1063–1072 (2014)
20. L.L. Zheng, L.C. Sun, M.S. Li, Y.C. Zhou, Improving the high-temperature oxidation resistance of Ti<sub>3</sub>(SiAl)C<sub>2</sub> by Nb-doping. *J. Am. Ceram. Soc.* **94**, 3579–3586 (2011)
21. J.L. Smialek, Environmental resistance of a Ti<sub>2</sub>AlC-type MAX phase in a high pressure burner rig. *J. Eur. Ceram. Soc.* **37**, 23–34 (2017)
22. R. Yin, H. Wu, K. Sun et al., Fabrication of graphene network in alumina ceramics with adjustable negative permittivity by spark plasma sintering. *J. Phys. Chem. C* **122**, 1791–1799 (2018)
23. R. Yin, Y. Zhang, W. Zhao et al., Graphene platelets/aluminium nitride metacomposites with double percolation property of thermal and electrical conductivity. *J. Eur. Ceram. Soc.* **38**, 4701–4706 (2018)
24. H. Wu, R. Yin, Y. Zhang et al., Synergistic effects of carbon nanotubes on negative dielectric properties of graphene-phenolic resin composites. *J. Phys. Chem. C* **121**, 12037–12045 (2017)
25. H. Wu, R. Yin, L. Qian et al., Three-dimensional graphene network/phenolic resin composites towards tunable and weakly negative permittivity. *Mater. Des.* **117**, 18–23 (2017)
26. H. Wu, Y. Zhang, R. Yin et al., Magnetic negative permittivity with dielectric resonance in random Fe<sub>3</sub>O<sub>4</sub>@graphene-phenolic resin composites. *Adv. Compos. Hybrid Mater.* **1**, 168–176 (2018)
27. H. Wu, Y. Qi, Z. Wang et al., Low percolation threshold in flexible graphene/acrylic polyurethane composites with tunable negative permittivity. *Compos. Sci. Technol.* **151**, 79–84 (2017)
28. P. Xie, Z. Wang, Z. Zhang et al., Silica microspheres templated self-assembly of three-dimensional carbon network with stable radio-frequency negative permittivity and low dielectric loss. *J. Mater. Chem. C* **6**, 5239–5249 (2018)
29. P. Xie, K. Sun, Z. Wang et al., Negative permittivity adjusted by SiO<sub>2</sub>-coated metallic particles in percolative composites. *J. Alloy. Compd.* **725**, 1259–1263 (2017)
30. Z. Guo, P. Xie, F. Dang et al., Bio-gel derived nickel/carbon nanocomposites with enhanced microwave absorption. *J. Mater. Chem. C* **6**, 8812–8822 (2018)
31. P. Xie, W. Sun, Y. Liu et al., Carbon aerogels towards new candidates for double negative metamaterials of low density. *Carbon* **129**, 598–606 (2018)
32. Z. Zhao, R. Guan, J. Zhang, Z. Zhao, P. Bai, Effects of process parameters of semisolid stirring on microstructure of Mg-3Sn-1Mn-3SiC (wt%) strip processed by rheo-rolling. *Acta Metall. Sin.* **30**, 66–72 (2017)
33. Z. Zhao, P. Bai, R. Guan, V. Murugadoss, H. Liu, X. Wang, Z. Guo, Microstructural evolution and mechanical strengthening mechanism of Mg-3Sn-1Mn-1La alloy after heat treatments. *Mater. Sci. Eng. A* **734**, 200–209 (2018)
34. T. Su, Q. Shao, Z. Qin, Z. Guo, Z. Wu, Role of interfaces in two-dimensional photocatalyst for water splitting. *ACS Catal.* **8**, 2253–2276 (2018)
35. Z. Sun et al., Experimental and simulation understanding of morphology controlled barium titanate nanoparticles under co-adsorption of surfactants. *CrystEngComm* **19**, 3288–3298 (2017)
36. L. Zhang, W. Yu, C. Han, J. Guo, Q. Zhang, H. Xie, Q. Shao, Z. Sun, Z. Guo, Large scaled synthesis of heterostructured electrospun TiO<sub>2</sub>/SnO<sub>2</sub> nanofibers with an enhanced photocatalytic activity. *J. Electrochem. Soc.* **164**, H651–H656 (2017)
37. L. Zhang, M. Qin, W. Yu, Q. Zhang, H. Xie, Z. Sun, Q. Shao, X. Guo, L. Hao, Y. Zheng, Z. Guo, Heterostructured TiO<sub>2</sub>/WO<sub>3</sub> nanocomposites for photocatalytic degradation of toluene under visible light. *J. Electrochem. Soc.* **164**, H1086–H1090 (2017)
38. Y. Zhang, L. Qian, W. Zhao, X. Li, X. Huang, X. Mai, Z. Wang, Q. Shao, X. Yan, Z. Guo, Highly efficient Fe-N-C nanoparticles modified porous graphene composites for oxygen reduction reaction. *J. Electrochem. Soc.* **165**, H510–H516 (2018)
39. B. Song, T. Wang, H. Sun, Q. Shao, J. Zhao, K. Song, L. Hao, L. Wang, Z. Guo, Two-step hydrothermally synthesized carbon nanodots/WO<sub>3</sub> photocatalysts with enhanced photocatalytic performance. *Dalton Trans.* **46**, 15769–15777 (2017)
40. X. Lou, C. Lin, Q. Luo, J. Zhao, B. Wang, J. Li, Q. Shao, X. Guo, N. Wang, Z. Guo, Crystal-structure modification enhanced FeNb<sub>11</sub>O<sub>29</sub> anodes for lithium-ion batteries. *ChemElectroChem* **4**, 3171–3180 (2017)
41. C. Lin, H. Hu, C. Cheng, K. Sun, X. Guo, Q. Shao, J. Li, N. Wang, Z. Guo, Nano-TiNb<sub>2</sub>O<sub>7</sub>/carbon nanotubes composite anode for enhanced lithium-ion storage. *Electrochim. Acta* **260**, 65–72 (2018)
42. Q. Hou, J. Ren, H. Chen, P. Yang, Q. Shao, M. Zhao, X. Zhao, H. He, N. Wang, Q. Luo, Z. Guo, Synergistic hematite-fullerene electron extracting layers for improved efficiency and stability in perovskite solar cells. *ChemElectroChem* **5**, 726–731 (2018)
43. Y. Li, T. Jing, G. Xu, J. Tian, M. Dong, Q. Shao, B. Wang, Z. Wang, Y. Zheng, C. Yang, Z. Guo, 3-D magnetic graphene oxide-magnetite poly(vinyl alcohol) nanocomposite substrates for immobilizing enzyme. *Polymer* **149**, 13–22 (2018)
44. C. Wang, M. Zhao, J. Li, J. Yu, S. Sun, S. Ge, X. Guo, F. Xie, B. Jiang, E. Wujcik, Y. Huang, N. Wang, Z. Guo, Silver nanoparticles/graphene oxide decorated carbon fiber synergistic reinforcement in epoxy-based composites. *Polymer* **131**, 263–271 (2017)
45. J. Zhao, L. Wu, C. Zhan, Q. Shao, Z. Guo, L. Zhang, Overview of polymer nanocomposites: computer simulation understanding of physical properties. *Polymer* **133**, 272–287 (2017)
46. X. Cui, G. Zhu, Y. Pan, Q. Shao, C. Zhao, M. Dong, Y. Zhang, Z. Guo, Polydimethylsiloxane-titania nanocomposite coating: fabrication and corrosion resistance. *Polymer* **138**, 203–210 (2018)
47. C. Wang, B. Mo, Z. He, C.X. Zhao, L. Zhang, Q. Shao, X. Guo, E. Wujcik, Z. Guo, Hydroxide ions transportation in polynorborene anion exchange membrane. *Polymer* **138**, 363–368 (2018)
48. Y. He, S. Yang, H. Liu et al., Reinforced carbon fiber laminates with oriented carbon nanotube epoxy nanocomposites: magnetic field assisted alignment and cryogenic temperature mechanical properties. *J. Colloid Interface Sci.* **517**, 40–51 (2018)
49. Z. Wu, S. Gao, L. Chen, D. Jiang, Q. Shao, B. Zhang, Z. Zhai, C. Wang, M. Zhao, Y. Ma, X. Zhang, L. Weng, M. Zhang, Z. Guo, Electrically insulated epoxy nanocomposites reinforced

- with synergistic core-shell SiO<sub>2</sub>@MWCNTs and montmorillonite bifillers. *Macromol. Chem. Phys.* **218**, 1700357 (2017)
50. Y. Zheng, Y. Zheng, S. Yang, Z. Guo, T. Zhang, H. Song, Q. Shao, Esterification synthesis of ethyl oleate catalyzed by Brønsted acid-surfactant-combined ionic liquid. *Green Chem. Lett. Rev.* **10**, 202 (2017)
51. Y. Zheng, Y. Zheng, Z. Wang, Y. Cao, Q. Shao, Z. Guo, Sodium dodecyl benzene sulfonate-catalyzed reaction for aromatic aldehydes with 1-phenyl-3-methyl-5-pyrazolone in aqueous media. *Green Chem. Lett. Rev.* **11**, 217–223 (2018)