ORIGINAL ARTICLE



# Red Emitting Coumarin—Azo Dyes : Synthesis, Characterization, Linear and Non-linear Optical Properties-Experimental and Computational Approach

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Abstract The coumarin molecules with 7-(N,Ndiethylamino) substitution and aryl azo (Ar–N=N-) at 3 position were synthesized, by reacting diazonium salt of substituted amines and 7-(N, N-diethylamino)-4-hydroxy coumarin under basic conditions. They were found to be fluorescent despite the presence of azo group. The azo group rotation was blocked by complexing with  $-BF_2$ , so as to get a red shift in absorption. The azo molecules show charge transfer, whereas  $BF_2$ -complexes do not. The dipole moment ratios between the ground and excited states calculated suggest highly polar excited state and an intra-molecular charge transfer at the excited state in the case of azo dyes. The NLO properties were calculated by solvatochromic method and computationally. Second order hyperpolarizability was found to be 46 to 1083 times more than urea. DFT and TDTDF calculations were performed to understand the electronic properties of the molecules at the ground as well as excited states.

Keywords Azo dye . Coumarin . Red emitting . DFT . TDDFT . NLO properties

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## Introduction

Many of the known coumarins are fluorescent molecules and they are known to have good quantum yield [[1](#page-13-0), [2](#page-13-0)] and high photostability [[3,](#page-13-0) [4\]](#page-13-0). Most of the them are colorless but substitutions at various positions bring about a red shift in absorption and emission, and are used in the applications such as laser dyes [[5](#page-13-0)], textile dyes [\[6](#page-13-0)] and sensors [\[7\]](#page-13-0). Coumarins have also been used as optical brighteners [\[8\]](#page-13-0), non-linear optical (NLO) materials [[9\]](#page-13-0) and in biological labelling [\[10,](#page-13-0) [11\]](#page-13-0). The compounds with azo functionality are less fluorescent to non-fluorescent in nature. Azo functional group at the 3-position of 4-hydroxy coumarin molecule was first reported by Yazdanbaksh et al. [\[12\]](#page-13-0). In the later studies on these molecules UV–vis absorption, fluorescence and acid dissociation constants were reported [[12,](#page-13-0) [13](#page-13-0)]. The substituent at 7-position plays an important role in the photophysical properties of coumarins [[14](#page-13-0), [15\]](#page-13-0) and imparts a red shift in absorption if the 7-substituent happens to be electron releasing. Here we report the synthesis of four 7-(N,N-diethylamino)-3-azo coumarin dyes with different substitutions at the 4-position of the phenylazo core (Fig. [2\)](#page-1-0). The properties like absorption, emission and quantum yield are studied. The dominant tautomer among the azo and hydrazine (Fig. [2\)](#page-1-0) form is established by DFT. The effect of rigidization of azo functional with  $BF_2$ -complexation is also studied in comparison with the parent molecules. The rigidization of the azo group is known with N-B-N=N kind of bridge [[16,](#page-13-0) [17](#page-13-0)] and no much information is given on O-B-N=N type of bridge particularly in an azo coumarin system. This happens to be the first study of this kind. The N-B-N=N bridge has introduced the red shifts in the absorption characteristics of the molecules [\[17](#page-13-0)] (Fig. [1](#page-1-0)). The red shift in the molecule was attributed to the azo rigidization and the resulting π-resonance effect (Fig. [2](#page-1-0)).

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<span id="page-1-0"></span>

The photophysical behavior of these molecules was probed for sensitivity towards solvent polarity. DFT calculations were used to get insights into the photophysical properties.

#### Experimental

#### Materials and Equipments

All the commercial reagents were procured from SD Fine Chemicals (Mumbai) and were used without further purification. Laboratory reagent grade solvents were purchased from Rankem, Mumbai. The reactions were monitored by TLC using 0.25 mm E-Merck silica gel 60  $F_{254}$  precoated plates, which were visualized with UV light (254 and 344 nm). Melting points were measured on standard melting point apparatus from Sunder Industrial products Mumbai and are uncorrected. <sup>1</sup>HNMR spectra were recorded on Bruker 400 MHz and Agilent 500 MHz instruments using TMS as an internal

Fig. 2 7-(N,N-diethylamino) 3 azo coumarin dyes (azo and hydrazone form) and their  $BF<sub>2</sub>$ -Complexes

standard. Mass spectra were recorded on FINNIGAN LCQ ADVANTAGE MAX instrument from Thermo Electron Corporation (USA). The absorption spectra of the compounds were recorded on a Perkin Elmer Lambda 25 UV-Visible spectrophotometer; Emission spectra were recorded on Varian Inc. Cary Eclipse spectrofluorometer.

The ground state  $(S_0)$  geometries of the tautomers of the compounds 3a-3d were optimized in the gas phase using Density Functional Theory (DFT) [[18\]](#page-13-0). The popular hybrid functional B3LYP was used, which combines Becke's three parameter exchange functional (B3) [[19](#page-13-0)] with the nonlocal correlation functional by Lee, Yang, and Parr (LYP) [[20](#page-13-0)]. All the atoms were treated with 6– 31 G(d) basis set, which deems to be sufficient for the type of molecules involved [[21](#page-13-0)–[23](#page-13-0)]. The validity of the structures as local minima on potential energy surface was verified with vibrational analysis and confirmed that they are with no imaginary frequencies. Time Dependent Density Functional Theory (TD-DFT) with the same hybrid functional and basis set was used to estimate vertical excitations and oscillator strengths . The lowest singlet excited state  $(S_1)$  was relaxed using TD-DFT to get optimised geometry of the excited state. The vertical emissions were computed by using the optimized relaxed singlet first excited state  $(S_1)$ . Frequency computations were carried out on the optimized geometry of the lowlying vibronically relaxed first excited state of the conformers. All the computations in solvents were carried out using the Polarizable Continuum Model (PCM) [\[24](#page-13-0)].



Gaussian 09 program [\[25](#page-13-0)] was used for all the DFT and TDDFT computations and the results were visualized with Gauss View 5.0 [[26\]](#page-13-0).

## Synthesis and Characterization

The compound 1 was synthesized by the method reported [\[27\]](#page-13-0) from bis(2,4-dichlorophenyl) malonate and 3-(diethylamino)phenol. The product obtained was sufficiently pure to be used for the further steps.

#### General Procedure for Diazotization and Coupling

Substituted aniline (2.5 mmol) was dissolved in 11 N hydrochloric acid (3 mL) and was cooled externally to −5 °C in ice-salt mixture. A solution of sodium nitrite (0.22 g, 3.1 mmol) in 1 ml water was added to the above dropwise with stirring. The solution thus formed was then stirred for 1 h at the same temperature. Excess nitrous acid was quenched with the addition of urea (1.5 mmol) to this solution. In an another flask 7-(diethylamino)-4-hydroxy-2H-chromen-2-one (0.5 g, 2.1 mmol) was dissolved in pre-cooled 5 % NaOH solution (5 mL) which was then placed in an ice-salt bath, and the diazonium salt prepared in the first flask was slowly added maintaining the pH 8–9 with the addition of solid sodium carbonate. After complete addition the reaction mixture was stirred for a period of 1 h and then neutralized with dilute hydrochloric acid. The yellow to brick red precipitate formed was then filtered, washed with water and dried under vacuum to give the product in good yield (Fig. 3).

## 7-(Diethylamino)-4-hydroxy-3-(phenyldiazenyl)-2Hchromen-2-one (3a)

Yield: 80 %

M.P.: 190 $\degree$ C

**HNMR** (CDCl<sub>3</sub>, 400 MHz) :  $\delta$  1.24 (t, J=7.2Hz, 6H), 3.45 (q, J= 7.2Hz, 4H), 6.35 (s, 1H), 6.57 (m, 1H), 7.23 (s, 1H), 7.42 (t,  $J = 8$ Hz, 2H), 7.59 (d,  $J = 8$ Hz, 2H), 7.85 (d,  $J = 8$ Hz, 2H).

Fig. 3 Synthesis of 7-(N,Ndiethylamino)-4-hydroxy 3-azo coumarin dyes

**HRMS**: 338.1480 (M+1) (Calculated for  $C_{19}H_{20}N_3O_3$ : 338.1426)

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): δ 12.9, 44.7, 97.3, 109.4, 114.18, 118.3, 125.81, 128.36, 144.5, 156.3, 158.5, 162.21, 164.3.

7-(Diethylamino)-4-hydroxy-3-((4 nitrophenyl)diazenyl)-2H-chromen-2-one (3b)

**Yield: 85 %** 

M.P.: 260 $\degree$ C

**HNMR** (CDCl<sub>3</sub>, 400 MHz) : $\delta$  1.26 (t, J=7.2Hz, 6H), 3.48 (q,  $J = 7.2$ Hz, 4H), 6.36 (d,  $J = 2.4$ Hz, 1H), 6.60 (dd,  $J=6.4 \& 2.4 \text{Hz}$ , 1H), 7.67 (d,  $J=9.2 \text{Hz}$ , 2H), 7.86 (d,  $J=6.4$  Hz, 1H), 8.31 (d,  $J=9.2$ Hz, 2H)

HRMS: 383.1319 (M+1) (Calculated for  $C_{19}H_{19}N_4O_5$ : 383.1355)

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): 12.9, 51.6, 96.9, 109.5, 117.4, 122.5, 126.3, 128.7, 130.1, 154.0, 156.7, 159.1.

4-((7-(Diethylamino)-4-hydroxy-2-oxo-2H-chromen-3 yl)diazenyl)benzoic acid (3c).

After acidifying the solution remained clear and was saturated with sodium chloride to give brick red coloured precipitate.

Yield: 68 %

**M.P.:**  $>300 °C$ 

**HNMR** (CDCl<sub>3</sub>, 400 MHz) :  $\delta$  1.25 (t, J=7.2Hz, 6H), 3.45(q, 6H), 6.34(s, 1H), 6.58(d,  $J=6$ Hz, 1H), 7.63(d,  $J=8.6$ Hz, 2H), 7.88 (d,  $J=6$ Hz, 1H), 8.14 (d,  $J=8.6$ Hz, 2H).

**HRMS** : 382.1375 (M+1) (Calculated for  $C_{20}H_{20}N_{3}O_{5}$ : 382.1403)

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): δ 12.7, 44.4, 97.3, 109.7, 116.906, 123.9, 128.4, 131.2, 154.0, 156.3, 158.8, 167.1, 176.8.

7-(Diethylamino)-4-hydroxy-3-((4 methoxyphenyl)diazenyl)-2H-chromen-2-one (3d)

Yield: 82 %

M.P.: 205  $^{\circ}$ C

**HNMR** (CDCl<sub>3</sub>, 400 MHz) :  $\delta$  1.24(t, 6H), 3.45(q, 4H), 3.89(s, 3H),  $6.37(d, J=2.4Hz, 1H)$ ,  $6.58(dd, J=6.4&2.4Hz$ , 1H),  $6.96(d, J=8.8Hz, 2H)$ ,  $7.56(d, J=8.8Hz, 2H)$ ,  $7.85(d,$  $J = 6.4$ Hz, 1H)



**HRMS:** 368.1590 (M+1) (Calculated for  $C_{20}H_{22}N_{3}O_{4}$ : 368.1610)

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): δ 11.9, 44.4, 54.5, 96.9, 108.0, 114.9, 119.0, 121.8, 123.2, 129.1, 134.6, 153.9, 156.3, 159.467, 176.1

#### General Procedure for  $BF_2$ -complexation

The azo compound (3a-3d) (1 mmol) was dissolved in 20 mL of dry acetonitrile. To this solution,  $BF_3-Et_2O$  solution (45– 50 % solution, 2 mL) was added dropwise. The resultant solution was stirred and refluxed under nitrogen environment. After completion of the reaction, the mixture was cooled and the dark colored precipitate formed was filtered, washed with diethyl ether (20 mL) and dried under vacuum (Fig. 4).

8-(Diethylamino)-2,2-difluoro-5-oxo-3-phenyl-2,5 dihydrochromeno[3,4-e][1,3,4,2]oxadiaza borinin-3-ium-2-uide (4a)

Yield: 70 %

M.P.: 272 °C

**HNMR** (CDCl<sub>3</sub>, 500 MHz) :  $\delta$  1.30(t, 3H), 3.54(q, 4H), 6.46(s, 1H), 6.71(d,  $J=10$ Hz, 1H), 7.45(m, 3H), 7.96(t,  $J = 8.5$ Hz, 3H).

HRMS: 386.1464 (M+1) (Calculated for  $C_{19}H_{19}BF_{2}N_{3}O_{3}$ : 386.1488)

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): δ 12.5, 45.7, 97.35, 110.93, 122.0, 129.2, 129.5, 129.7, 155.9, 157.7, 159.8.

8-(Diethylamino)-2,2-difluoro-3-(4-nitrophenyl)-5-oxo-2,5-dihydrochromeno[3,4-e][1,3,4,2] oxadiazaborinin-3 ium-2-uide (4b)

Yield: 82 %

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M.P.: 270 (dec.)^{\circ}C
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**HNMR** (CDCl<sub>3</sub>, 500 MHz):  $\delta$  1.33(t, J=7.5Hz, 6H), 3.59(q,  $J = 7.5$ Hz, 4H), 6.47(d,  $J = 2.5$ Hz, 1H), 6.74(d,d,  $J=2.5,5.5Hz$ , 1H), 7.98(d,  $J=10Hz$ , 1H), 8.12(d, J = 10Hz, 2H),  $8.31(d, J=9.5Hz, 2H)$ .

HRMS: 431.1318 (M+1) (Calculated for  $C_{19}H_{18}BF_2N_4O_5:431.1338$ 

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): δ 12.6, 46.1, 97.7, 111.6, 122.0, 124.8, 125.7, 130.3, 156.7, 159.24.

Fig. 4  $BF_2$ -Complexation of 7-(N,N-diethylamino)-4-hydroxy 3 azo coumarin dyes

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Yield: 50%
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M.P.: 200 $\degree$ C

**HNMR** (CDCl<sub>3</sub>, 500 MHz) :  $\delta$  0.90(t, J=7.5Hz, 6H),  $3.24(q, J=7.5Hz, 4H), 6.16(d, J=2.5Hz, 1H), 6.44(q,$  $J = 4$ Hz, 1H), 7.48(d,  $J = 4$ Hz, 1H), 7.59(q,  $J = 3.5$ Hz),  $7.74(d,d, J=5Hz, 3.5Hz, 2H).$ 

HRMS: 430.1355 (M+1) (Calculated for  $C_{20}H_{19}BF_{2}N_{3}O_{5}$ : 430.1386)

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): δ 176.1, 167.1, 158.5, 156.3, 153.9, 144.3, 130.1, 129.7, 128.3, 127.65, 123.6, 120.8, 117.0, 109.7, 108.3, 101.4, 97.6, 96.6, 44.4, 12.9.

8-(Diethylamino)-2,2-difluoro-3-(4-methoxyphenyl)-5 oxo-2,5-dihydrochromeno[3,4-e][1,3,4,2] oxadiazaborinin-3-ium-2-uide (4d)

Yield: 85 %

M.P.: 205  $^{\circ}$ C

**HNMR** (CDCl<sub>3</sub>, 500 MHz) :  $\delta$  1.30(t, J=7.5Hz, 6H), 3.53(q,  $J = 7.5$ Hz, 4H), 3.88(s, 3H), 6.45(d,  $J = 10$ Hz, 1H), 6.69(q,  $J = 5$ Hz, 1H), 6.97(q,  $J = 10$ Hz, 1H), 7.93(d,  $J = 5$ Hz, 1H), 7.96(m, 3H).

HRMS: 416.1585 (M+1) (Calculated for  $C_{20}H_{21}BF_{2}N_{3}O_{4}$ : 416.1593)

<sup>13</sup>CNMR (DMSO- $d_6$ , 125 MHz): δ 12.5, 45.6, 55.6, 97.3, 110.7, 110.7, 114.4, 114.9, 123.6, 128.3, 129.12, 155.5, 158.4, 161.1.

## Result and Discussion

## Structural Properties of Compound 3a-3d and 4a-4d

The geometries of the compounds 3a-3d were optimised in solvent environments using DFT. These kind of dyes are known to exhibit azo-hydrazone tautomerism [[28](#page-13-0)–[30](#page-13-0)]. Therefore both the forms i.e. azo and hydrazone tautomers (Fig. [2](#page-1-0)) were optimised with DFT-B3LYP/6-31 g(d). The comparison of the energy values of azo (enol form) and hydrazone (keto form) has revealed that the latter is more



Table 1 Photophysical properties of compound 3a-3d and comparison with theoretical

values

<span id="page-4-0"></span>stable in terms of total energy of the optimised structures (Supporting information). The hydrazone structure is used for further optimizations and calculation of the electronic properties. The energy values also has revealed that the substituent effect is also important to the stabilisation energy as the  $-NO<sub>2</sub>$  substituted compound 3b is the most stable and the unsubstituted one i.e. compound 3a is the least stabilised. The stabilities of the compounds 3c and 3d is intermediate. Among these the electron withdrawing group –COOH in the compound 3c has enhanced the molecular stability as compared the  $-OCH<sub>3</sub>$  of the compound 3d. The bond length and dihedral angle analysis suggests that, O-atom of keto functional group in hydrazone form in the compounds 3a-3d shows H-bonding with the hydrogen on the =N-N-H. This suggests that the molecules may be in tautomeric equilibrium in solutions.

#### Linear Optical Properties

The compounds were studied for their photophysical properties in solvents of various polarity and nature. The absorption properties of the compounds 3a-3d are summarised in Table 1.

The absorption properties in terms of absorption wavelength are not much sensitive towards solvent polarity. The



 $a$ TD-B3LYP/6-31G(d)

FWHM (Full width at half maximum) values for all the dyes 3a-3d are higher in polar aprotic solvents like N,Ndimethylformamide (DMF) and dimethylsulphoxide (DMSO) indicating broadening of the spectra in dipolar aprotic solvents. For the compound 3b the values are higher in polar protic solvents also. The other molecules 3a, 3c-3d show lower FWHM values for the protic solvents. The polar aprotic solvents also shows higher integrated absorption coefficients (IAC) in all the dyes except in 3b. The values for the IAC falls in the range of  $0.3357-1.7028 \times 10^8$ . The molar extinction co-efficient at  $\lambda^{\text{max}}$  is the highest for the chlorinated non polar solvent dichloromethane (DCM). The observation is consistent with all the substituents. The absorption crosssection is also the highest in DCM, and has reached up to  $2.01 \times 10^{-19}$  cm<sup>-2</sup> for the compound 3d.

In an analogous manner the compounds 4a-4d are less sensitive to the polarity but has different features in various solvents (Supporting Information). An increase of the FWHM is observed here for the polar protic solvents i.e. methanol and ethanol. Also there is two-fold increase in the molar absorptivity ( $\varepsilon^{\text{max}}$ ) of the compounds 4a-4d when compared with their counterparts in the compounds 3a-3d. This is due to the lowering of HOMO-LUMO gap (longer wavelength absorption) and apparent increase in the concentration of the absorbing species. The IAC values are also higher than the values of the compounds  $3a-3d$ . Amongst all the BF<sub>2</sub>-

complexes 3a and 3d show an increase in absorption cross section. The oscillator strengths  $(f)$  are not sensitive to the polarities of the solvents and shows no clear correlation.

The compounds 4a-4d are red shifted as against their parent azo compounds 3a-3d. The FWHM values are also higher and a broader absorption is indicated. The molar extinction co-efficients of the azo-BF2 complexes are improved over the azo compounds. Absorption cross section values are in the range of  $0.93-2.91 \times 10^{-19}$  cm<sup>-2</sup> in all the solvents.

## Absorption and Solvatochromism

The compounds 3a-3d were studied for their solvatochromic properties in various solvents of different polarities. The absorption wavelengths were insensitive to solvent polarity (Table [1](#page-4-0)). The dyes 3a-3d show the highest molar extinction coefficient in the solvent dichloromethane (DCM) (Table [1\)](#page-4-0).

However there is no clear correlation between the solvent polarities and the molar extinction coefficients, in general polar solvents show lower values. As expected, the compound 3a has blue shifted absorption at 468 nm in DCM as compared to 3b at 490 nm in DCM (Fig. 5). The dye 3b has  $-NO<sub>2</sub>$  group which is electron withdrawing and exhibits a red shifted absorption as it assists the azo group in pulling electrons and eventually shifts the absorption to the red region, whereas



compound 3a-3d in various solvents

the compound 3c with a –COOH group at *para*-position shows a red shift of 17 nm which is lower compared to the dye 3a. Though the dye 3d possesses an electron donating group  $(-OCH_3)$ , it also has exhibited a red shift of 14 nm in absorption. The presence of electron withdrawing or donating group has induced a red shift in these compounds. The azo group (-N=N-), being an electron withdrawing can be involved in the charge transfer from both sides and hence enhances the red shifted absorption. This is also evident from FMO diagrams given in Table [5.](#page-11-0) The electron density at LUMO is mostly present on the azo group.

Though the absorption wavelengths of the dyes 3a-3d are not solvent dependent, their fluorescence shows a greater impact of solvents. The emissions of all the dyes 3a-3d ranges between 538 and 646 nm. The Stokes shift values are higher and are in the range of  $2460-5662$  cm<sup>-1</sup> (68 to 166 nm) across the compounds in various solvents. The Stokes shifts are higher in polar solvents. The quantum yield values are on the lower side which are in the range of 0.0005 to 0.0210 (Table [1\)](#page-4-0). The quantum yields are not uniform and are higher in non-polar solvents like toluene, dichloromethane and ethyl acetate (EtOAc) due to the lesser interaction with fluorophores as compared to the polar solvents. The order of the emission wavelength is dichloromethane>ethyl acetate>toluene amongst the non-polar solvents. The compounds have shown an unusual high Stokes shift, and may be attributed to the flexibility of the  $-N=N-Ar$  group at the 3-position which may be involved in vibrational relaxation at in the excited state lowering the energy of the emissive state (Fig. 6).

The dyes  $4a-4d$ , which are the BF<sub>2</sub>-complex derivatives of the dyes 3a-3d absorb at a longer wavelength  $(-50-60)$  nm). The differences between the two kind chromophores are the rigidization of azo group and the presence of an electron deficient  $BF<sub>2</sub>$ -core which has formed a more efficient acceptor in the case of dyes 4a-4d. Though there is no significant effect of polarity on absorption wavelength but still has a marginal red shift in polar solvents  $(\sim 15-20 \text{ nm})$ . Among all, the dye 4b is the most red shifted by  $\sim$ 20–40 nm as the nitro group is a strong withdrawer. The order of the substituents exhibiting longer wavelength is  $-H < -OCH_3 < -COOH < -NO_2$ . The fluorescence emission of 4a-4d exceeds 600 nm in all the solvents tested except for toluene in which their emission maxima is slightly lower than 600 nm. The fluorescence quantum yield has drastically improved in azo-BF2 complexes over the azo compounds, the order of the increase in quantum yield is about 10–100 folds. The quantum yields are the lowest in the  $-NO<sub>2</sub>$  substituted derivatives (3b and 4b) in their respective series (Figs. [7](#page-7-0) and [8](#page-7-0)).



solvents

<span id="page-7-0"></span>Fig. 7 Absorption spectra of compound 4a-4d in various



Fig. 8 Fluorescence emission spectra of compound 4a-4d in various solvents



<span id="page-8-0"></span>Table 2 Photophysical properties of compounds 4a-4d and comparison with theoretical values



A comparison of the computed and experimental absorption and emission wavelengths for the dyes 3a-3d and 4a-4d are given in Tables [1](#page-4-0) and 2 respectively. The deviations are higher for the compounds 4a-4d with deviations ranging between 1.0 and 13.6 % in absorption, compared to 0.2 to 11.6 % deviation shown by the compounds 3a-3d in absorption. A similar trend is followed in the emission calculations. The compounds 4a-4b, which have a strong acceptor in the form of  $-BF_2$  complex, makes the system different in its charge separation. The trends in solvatochromism exhibited by the molecules in the present study has been clearly demonstrated by the chosen computational method (Tables [1](#page-4-0) and 2).

#### Solvent Polarity Function Plots

The solvatochromic behaviour of the dyes 3a-3d and 4a-4d was studied with the help of Lippert [[31](#page-13-0)], Weller [\[32](#page-13-0)] and Rettig [[32](#page-13-0)] plots. A complete account of the Lippert Mataga, Weller and Rettig equations are given in the supporting information.

The azo dye series 3a-3d showed linear relation of Stokes shift with respect to the orientation polarizability function  $f_1(\varepsilon, n)$  given by Lippert (Supporting information) plot and the correlation factors range between 0.43 and 0.86. while the corresponding boron complexes do not show any appreciable correlation (Supporting info). The linearity in the photophysical behaviour of the dyes 3a-3d suggest that the local excitation of the molecules is affected by the solvent polarity and the trend is more linear in polar aprotic and non-polar solvents. The molecules in polar protic solvents have shown more randomness in their photophysical properties, and is backed by the fact that H-bonding interactions of the protic solvents is not considered in this polarity function. The Weller's plot for the azo dyes (3a-3d) is linear leading to the inference that there is intra molecular charge transfer (ICT) affected by the solvent polarity. The flexibility around the azo group makes the ICT possible, and the molecule relaxes to a lower emissive state. This has been reflected in the higher stokes shifts of these molecules (Table [1](#page-4-0))

On the other hand, the  $BF_2$ -complexes of the azo dyes i.e. 4a-4d do not show any correlation with the solvent polarity. The plots of Stokes shift in  $cm^{-1}$  versus solvent polarity parameter  $f_1(\varepsilon, n)$  (Lippert plot), emission in cm<sup>-1</sup> versus solvent polarity parameter  $f_2(\varepsilon, n)$  (Weller plot) and emission in cm<sup>-1</sup> versus solvent polarity parameter  $f_3(\varepsilon, n)$  (Rettig plot) were with very low regression coefficients. This implies that in the boron complexes due to rigidity the emissive state is not an ICT state but a local relaxed excited state. The lower (as compared to compound 3a-3d) Stokes shift exhibited by the dyes in all the solvents adds to the justification. (Plots are given in supporting information.)

#### Dipole moment Ratio

The dyes 3a-3d responds well to the solvent polarity functions  $f(\varepsilon, n)$ , the similar equations are introduced by Bilot-Kawski [\[33\]](#page-13-0), Bakhshiev [\[34](#page-13-0)] and Liptay [\[35\]](#page-13-0) for the estimation of the ratio of the excited state dipole moment and ground state dipole moment i.e.  $\frac{\mu_e}{\mu_g}$ . The equations are given in supporting information.

The dipole moments calculated with the above equations is tabulated in Table 3.

All the compounds show higher  $\frac{\mu_e}{\mu_g}$  ratio suggesting a highly polar excited state. This leads to a positive solvatochromism. This observation is also supported by the red shifted absorption and emission spectrum in polar solvents. The Bilot-Kawski equation has consistently estimated lower  $\frac{\mu_e}{\mu_g}$  ratio as compared to the Bakhshiev and Liptay Equations.

Table 3 Dipole moment ratio of compound 3a-3d by various methods

3b	3c	3d
4.372	5.317	4.519
4.871	6.267	5.026
5.034	6.583	5.284
	4.297 4.629 4.633	

#### Transition Dipole Moment

In addition to the difference in dipole moments between the excited and ground states, the charge transfer character of the fluorophore can be understood from the oscillator strength  $(f)$ (Given in Tables [1](#page-4-0) and [2](#page-8-0) and transition dipole moment of the dyes ( $\mu_{\rho\sigma}$ ). The effective number of electrons transition from the ground to excited state is usually described by the oscillator strength, which provides the absorption area in the electronic spectrum. The oscillator strength  $(f)$  can be calculated using the literature method [\[36](#page-14-0)]. Transition dipole moments for absorption  $(\mu_{eg})$  which is a measure of the probability of radiative transitions have been calculated for the dyes in different solvent environments [\[37](#page-14-0)]. The values of transition dipole moment  $(\mu_{eg})$  for the dyes in each solvent is given in Table 4.

The transition dipole moments calculated for all the dyes shows that higher transition dipole moment is observed for the BF<sub>2</sub>-complexed azo dyes as compared to their azo anologues. The trend in solvent environment is not clear but broadly a higher transition dipole moment is observed in the polar solvents.

## Frontier Molecular Orbitals

The FMO (Frontier Molecular Orbitals) involved in the electronic transition from  $S_0 \rightarrow S_1$  are HOMO $\rightarrow$ LUMO in the dyes 3a-3d. The electron density on the HOMO is located on the donor 7-N,N-diethylamino group and moves towards –N-NH-Ar group in the LUMO, and thus sets up a clear acceptor and donor relationship. The –nitro group in 3b possess electron density in LUMO, and shows a higher degree of charge transfer resulting in a red shift in absorption.

The compounds 4a-4d have similar donor (i.e. N, Ndiethylamino group), but the LUMO shows electron density located on the  $BF_2$ -complexed core.

**Table 4** Transition dipole moments  $(\mu_{eg})$  obtained from absorption properties of compound 3a-3d and 4a-4d in various solvents

Solvent	3a	3b	3c	3d	4a	4b	4c	4d
<b>ACN</b>	7.1	7.0	5.2	8.0	9.2	6.6	9.3	10.7
<b>DCM</b>	4.8	7.1	3.8	8.4	7.4	7.6	9.2	8.7
DMF	8.5	6.8	7.8	7.8	7.4	7.2	8.6	9.5
<b>DMSO</b>	6.8	5.8	7.0	5.4	9.3	5.6	8.3	10.2
EtOAc	6.4	6.9	6.0	7.6	9.3	6.1	8.3	8.4
EtOH	4.7	6.7	6.3	6.9	7.7	6.3	8.0	10.1
MeOH	4.9	7.1	6.8	8.4	7.3	6.9	7.7	9.4
Tol	5.8	7.0	5.1	7.4	9.1	7.0	7.6	9.5

Values expressed in Debye

#### NLO Properties

There are quite a few reports on the hyperpolarizability estimation of the coumarin molecules as they can be a good candidate for such applications [\[38](#page-14-0)–[40](#page-14-0)]. The higher ratio of the excited state dipole moment and ground state dipole moment also suggests a higher charge transfer.

#### Calculation of  $\alpha_{CT}$  from the Solvatochromic Data

The linear polarizability  $\alpha_{CT}$  was evaluated experimentally for synthesized extended styryls. These values are obtained by two-level model using UV–vis absorption/emission spectroscopy. The solvatochromic method can also be utilized in the determination of dipole moment of the lowest lying charge transfer excited state [\[41\]](#page-14-0). All  $\alpha_{CT}$  values are calculated for azo coumarins, which are compared with theoretically obtained  $\alpha_{CT}$ or $\alpha_{xx}$  (Supporting information).

The dyes are expected to show good non-linear properties. There are various experimental and theoretical methods reported to evaluate  $\beta$  value. Theoretical methods to evaluate  $\beta$  value are based on the time-dependent perturbation theory [\[42,](#page-14-0) [43\]](#page-14-0). The common experimental methods used to obtain  $\beta$  values are the electric field induced second harmonic generation (EFISH) [\[44\]](#page-14-0) and the hyper Rayleigh scattering (HRS) [\[45\]](#page-14-0).

The methods described above lack the cost effectiveness and it demands a more elaborate experimental set up. The solvatochromic method is simple and cost effective and serves as an effective a priori approach in understanding the nonlinear optical behaviour of dyes.

The two level microscopic model to determine solvent dependent hyperpolarizability is based on Oudar equation [[46,](#page-14-0) [47\]](#page-14-0) which in modified form can be presented as,

$$
\beta_{xxx} = \beta_{CT} = \frac{3}{2h^2c^2} \frac{v_{eg}^2 \mu_{eg}^2 \Delta \mu_{CT}}{\left(v_{eg}^2 - v_L^2\right)\left(v_{eg}^2 - 4v_L^2\right)}
$$
(1)

where x is the is the direction of charge transfer,  $h$  is Planck's constant (in erg  $\times$  s), c is speed of light in vacuum (in cm s<sup>-1</sup>),  $\mu_{eg}$  is the transition dipole moment,  $v_L$  is the frequency of the reference incident radiation to which the  $\beta$  value would be referred,  $v_{eg}$  is the transition frequency and  $\Delta \mu_{CT}$  is the difference between excited state and ground state dipole moment, the hyperpolarizability obtained by this equitation is the dominant component of the hyperpolarizability tensor  $\beta_{xxx}$  [\[48\]](#page-14-0) and as the formula refers to charge transfer transition the hyperpolarizability obtained often indicated as  $\beta_{CT}$  (charge transfer). The  $\Delta\mu_{CT}$  is obtained on the basis of McRae's theory [\[49,](#page-14-0) [50](#page-14-0)]

$$
\overline{\vartheta}_{abs} - \overline{\vartheta}_{emn} = (\delta_{abs} + \delta_{emn}) + \frac{2\Delta\mu_{CT}^2}{hca^3} \left(\frac{\varepsilon - 1}{\varepsilon + 2} - \frac{n^2 - 1}{n^2 + 2}\right) \tag{2}
$$

where  $\overline{\vartheta}_{abs} - \overline{\vartheta}_{emn}$  is the Stokes shift (in cm<sup>-1</sup>),  $\delta_{abs}$  and  $\delta_{\text{emm}}$  are the differences in the vibrational energy (in cm<sup>-1</sup>) of the molecule in the excited and ground state for absorption and emission, respectively, a is the cavity radius within Onsager's model (in cm), ε is the relative dielectric constant and  $n^2$  the static refractive index of the solvent. a was calculated by integration of the solvent accessible surface using density functional theory optimized geometry Eq. 2 can be written as,

$$
\overline{\vartheta}_{abs} - \overline{\vartheta}_{emn} = \frac{2\Delta\mu_{CT}^2}{hca^3} \left( \frac{\varepsilon - 1}{\varepsilon + 2} - \frac{n^2 - 1}{n^2 + 2} \right) + (\delta_{abs} + \delta_{emn}) \tag{3}
$$

Treating this Eq. 3 as,

$$
y = mx + c \tag{4}
$$

where,  $y = \overline{\vartheta}_{abs} - \overline{\vartheta}_{emn}$ ,  $m = m = \frac{2\Delta\mu_{CT}^2}{hca^3}$ ,  $x = \left(\frac{\varepsilon - 1}{\varepsilon + 2} - \frac{n^2 - 1}{n^2 + 2}\right)$  $\left(\frac{\varepsilon-1}{n^2-1}\right)$ and  $c = (\delta_{abs} + \delta_{emm})$ 

Using the value of slope m,  $\Delta \mu_{CT}$  was then derived, and the transition dipole moment  $\mu_{eg}^2$  is related to the oscillator strength  $f$  (Equation given in supporting information).

where, m is mass of electron, f is oscillator strength,  $\overline{\vartheta}_{eg}$  is the absorption frequency in cm−<sup>1</sup> , e is charge on electron. The oscillator strength can be obtained by integrated absorption coefficient of the absorption band.

The value of first hyperpolarizability obtained using the solvatochromic method is based on several assumptions and thus allow only approximate estimate of dominant tensor of total hyperpolarizability along the direction of charge transfer which is the major contributor to the total hyperpolarizability. Though the values are approximate it is possible to understand the trend in the hyperpolarizability values in a series of molecules (Table [5\)](#page-11-0).

The  $BF_2$ -complexed molecules do not show prominent solvatochromism while the azo dyes (3a-3d) show. The experimental and calculated values of  $\beta_{xxx}$  for compounds 3a-3d are given in Table [6.](#page-12-0)

The experimental and computed values of  $\beta_{xxx}$  for the dyes 3a and 3d are in good agreement. The compounds 3b and 3c having stronger electron withdrawing groups show appreciable difference between the experimental computational values of  $\beta_{\text{rrr}}$ .

The value of  $\beta_0$  or total first order hyperpolarizability of the molecule gives an estimate of the NLO properties of the organic molecules. The computed values were compared with the values obtained for urea. The comparison of the values is given below in Table [7.](#page-12-0)

The total hyperpolarizability calculated is 46 to 1083 times greater than that of urea. The electron donating group (i.e.–  $OCH<sub>3</sub>$ ) in the dye 3d contributes to the least total hyperpolarizability of the molecule. On the other hand the



<span id="page-11-0"></span>Table 5 FMO (Frontier molecular orbital) for compound 3a-3d and 4a-4d

dye 3b with electron withdrawing group shows 1083 times more value of hyperpolarizability than urea.

The second order hyperpolarizability  $\langle \gamma \rangle$ SD at molecular level originating from the electronic polarization in the nonresonant region can be treated by a three-level model [\[51](#page-14-0)–[55\]](#page-14-0). The quasi-two-level model in place of three level model using the density matrix formalism leads to a simpler Eq. 5 [\[56](#page-14-0), [57\]](#page-14-0).

$$
\langle \gamma \rangle \propto \frac{1}{E_{eg}^3} \mu_{eg}^2 \left( \Delta \mu^2 - \Delta \mu_{eg}^2 \right) \tag{5}
$$

The value  $\frac{1}{E_{eg}^3} \mu_{eg}^2 \left( \Delta \mu^2 - \Delta \mu_{eg}^2 \right)$  is indicative of the value of second order hyperpolarizability and can be considered to be the "solvatochromic descriptor of second order hyperpolarizability" and the values calculated are given in supporting information.

The solvatochromic descriptor  $\langle \gamma \rangle$  of the second order hyperpolarizability of the compounds show higher values in the case of the dye 3d with a strong donor i.e. –OCH3. The value for the dye 3b remains to be the second highest. The electron flow enhancement in the azo core seems to be

<span id="page-12-0"></span>**Table 6** Linear polarizability  $\alpha_{CT}$  calculated by solvatochromic method and computed  $\alpha_{CT}$  for compound 3a-3d

	3а		3 <sub>b</sub>		3c		3d	
				$E\alpha_{rr}$ $C\alpha_{rr}$ $E\alpha_{rr}$ $C\alpha_{rr}$ $E\alpha_{rr}$ $C\alpha_{rr}$ $E\alpha_{rr}$				$C\alpha_{rr}$
<b>ACN</b>	1.73	4.07	1.78	2.29	0.96	2.27	2.31	4.43
<b>DCM</b>	0.74	3.88	1.72	2.18	0.50	2.16	2.39	4.23
<b>DMF</b>	2.34	4.07	1.54	2.29	2.03	2.27	2.04	4.43
<b>DMSO</b>	1.46	4.08	1.10	2.30	1.58	2.28	0.95	4.45
EA	1.39	3.77	1.65	2.12	1.25	2.11	2.00	4.12
EtOH	0.75	4.04	1.62	2.27	1.40	2.25	1.68	4.39
MeOH	0.84	4.06	1.82	2.28	0.52	2.27	2.54	4.42
Tol	1.05	3.42	1.60	1.94	0.81	1.94	1.75	3.73

 $E \alpha_{xx}$  = Experimental  $C \alpha_{xx}$  = Computational

Values are in the order of  $\times 10^{-30}$  esu

enhancing the third order hyperpolarizability descriptor  $\langle \gamma \rangle$ . The solvent effect is also evident on this parameter. Higher the polarity of the solvent, higher is the second order hyperpolarizability.

# Computational  $\gamma$  Value (Second Order Static Hyperpolarizability)

The individual components of the second order static hyperpolarizability  $\gamma$  were obtained computationally. The values are considered to be proportional to the solvatochromic descriptor  $\langle \gamma \rangle$  of the second order hyperpolarizability. The values obtained are given in supporting information (Tables 8 and 9).

The values has a trend where higher polarity solvents show higher values of  $\gamma$ , but the similar trend is not followed by the solvatochromically obtained values.

Table 7 Expermental and computed  $\beta_{xxx}$  values for compound 3a-3d in various solvents

Solvent 3a			3b		3c		3d	
		$E\beta_{xxx}$ $C\beta_{xxx}$ $E\beta_{xxx}$ $C\beta_{xxx}$ $E\beta_{xx}$ $C\beta_{xx}$ $C\beta_{xx}$ $E\beta_{xx}$ $C\beta_{xx}$						
<b>ACN</b>	3.69	4.56	5.28	0.41	2.21	0.47	3.13	2.01
<b>DCM</b>	1.58	3.83	5.14	0.35	1.13	0.40	3.42	2.03
<b>DMF</b>	5.07	4.57	4.21	0.41	4.42	0.47	2.82	2.01
<b>DMSO</b>	3.14	4.63	3.04	0.41	3.67	0.47	1.35	2.01
EA	2.88	3.45	4.79	0.32	2.88	0.36	2.74	2.01
EtOH	1.62	4.44	4.68	0.40	3.10	0.45	2.38	2.02
MeOH	1.82	4.53	5.17	0.40	1.18	0.46	3.56	2.01
Tol	2.25	2.31	4.71	0.23	1.84	0.26	2.43	1.76

 $E \beta_{xxx}$  = Experimental  $C \beta_{xxx}$  = Computed

Values are in the order of  $\times 10^{-30}$  esu

Table 8 Total first order hyperpolarizability calculated with B3LYP/6-31G (d) for compound 3a-3d

	3a $\beta_o \times 10^{-30}$	3 <sub>b</sub>	3c	3d
ACN	134.88	447.01	254.14	20.12
<b>DCM</b>	115.27	384.05	220.90	14.03
DMF	135.19	447.99	254.65	20.22
<b>DMSO</b>	136.68	452.70	257.13	20.73
EA	104.83	350.05	202.86	11.34
EtOH	131.70	436.86	248.79	19.05
MeOH	134.18	444.78	252.97	19.88
Tol	72.02	240.86	144.05	11.12
Average	120.59	400.54	229.44	17.06
Ratio with urea (Urea: Compound)	326	1083	620	46

# Conclusion

In conclusion, we have reported the fluorescent 3-azo coumarin compounds (3a-3d) with solvatochromism. The molecules were confirmed by spectral analysis like <sup>1</sup>HNMR, <sup>13</sup>CNMR, and mass spectra. A careful analysis of solvent polarity function and photophysical properties shows that there is presence of intra molecular charge transfer state (ICT) involved in the photo-excitation and emission of the molecules. There is a good linearity observed for dielectric constant and refractive index based solvent polarity functions like Lippert, Weller and Rettig functions. The dipole moment ratio calculated with different equations have revealed that there is a highly polar excited state involved in photoexcitations. The positive solvatochromism shown is attributed to this. On the other hand, the respective  $BF_2$ -complexes (4a-4d) which are the rigidized versions of the azocoumarins (3a-3d) do not show any linear relations with the solvent polarity parameters based on dielectric constant and refractive index. The locking of the flexible azo-group has restricted the ICT process and stokes shift is lowered, however there is a red shift observed in absorption as compared to the compound 3a-3d. The overall hyperpolarizability compared with urea has 46 to 1083 times





<span id="page-13-0"></span>greater hyperpolarizability, and can be very good candidates as NLO materials. The second order static hyperpolarizability was found to be solvent dependent and reiterates the utility of these molecules as NLO materials.

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