ORIGINAL RESEARCH

Modeling acid–base balance during continuous kidney replacement therapy

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Abstract

Clinical studies have suggested that use of bicarbonate-containing substitution and dialysis fuids during continuous kidney replacement therapy may result in excessive increases in the carbon dioxide concentration of blood; however, the technical parameters governing such changes are unclear. The current work used a mathematical model of acid–base chemistry of blood to predict its composition within and exiting the extracorporeal circuit during continuous veno-venous hemofltration (CVVH) and continuous veno-venous hemodiafltration (CVVHDF). Model predictions showed that a total substitution fuid infusion rate of 2 L/h (33% predilution) with a bicarbonate concentration of 32 mEq/L during CVVH at a blood fow rate of 200 mL/min resulted in only modest increases in plasma bicarbonate concentration by 2.0 mEq/L and partial pressure of dissolved carbon dioxide by 4.4 mmHg in blood exiting the extracorporeal circuit. The relative increase in bicarbonate concentration (9.7%) was similar to that in partial pressure of dissolved carbon dioxide (8.2%), resulting in no signifcant change in plasma pH in the blood exiting the CVVH circuit. The changes in plasma acid–base levels were larger with a higher infusion rate of substitution fuid but smaller with a higher blood fow rate or use of substitution fuid with a lower bicarbonate concentration (22 mEq/L). Under comparable fow conditions and substitution fuid composition, model predicted changes in acid–base levels during CVVHDF were similar, but smaller, than those during CVVH. The described mathematical model can predict the efect of operating conditions on acid–base balance within and exiting the extracorporeal circuit during continuous kidney replacement therapy.

Keywords Acid–base of blood · Acute kidney injury · Bicarbonate · Carbon dioxide · Dialysis fuid · Kidney replacement therapy · Substitution fuid

1 Introduction

Patients with acute kidney injury (AKI) treated by continuous kidney replacement therapy (CKRT) require the use of fluids or solutions containing bicarbonate or other buffer bases to correct metabolic acidosis, and a large majority

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of these critically-ill patients also receive mechanical ventilatory support $[1, 2]$ $[1, 2]$ $[1, 2]$. The effect of the administration of large amounts of bicarbonate, either by using substitution (also called replacement) or dialysis fuids, on acid–base balance and overall clinical outcomes in these patients is however unclear. For instance, Kashani et al. [[3\]](#page-9-2) used propensity score matching in a retrospective analysis of AKI patients treated by continuous veno-venous hemofltration (CVVH) using regional citrate anticoagulation, in which over 80% also required mechanical ventilatory support, to show that patients treated with a substitution fuid containing a high concentration of bicarbonate (32 mEq/L versus 22 mEq/L) was associated with significantly higher inhospital and 90-day mortality. These investigators hypothesized that administration of large amounts of bicarbonate resulted in increased production of dissolved carbon dioxide potentially leading to cerebral acidosis or intracranial hypertension. A subsequent retrospective analysis by this same

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group [\[4\]](#page-9-3) showed that use of substitution fuid containing a high concentration of bicarbonate was also associated with hypotension during the frst hour of CKRT initiation. In contrast, Allegretti et al. [[5\]](#page-9-4) studied 19 mechanically-ventilated patients who were subsequently treated by CVVH with substitution fuids containing 32 mEq/L of bicarbonate. These investigators showed that arterial partial pressure of carbon dioxide ($pCO₂$) remained stable during the initial 96 h after initiation of CVVH. These two reports were limited to critically-ill AKI patients without signifcant hypercarbia.

The effect of bicarbonate-containing substitution fluids during CKRT on acid–base parameters in critically-ill patients with impaired respiratory function is also incompletely understood, although it is known that both mechanical ventilatory support and acute respiratory distress syndrome are associated with subsequent AKI [\[6](#page-9-5), [7\]](#page-9-6). Such patients are also administered large amounts of bicarbonate independent of whether the patients are treated by hemodialysis or CKRT, and the clinical consequences of such bicarbonate administration is unclear. For example, Nentwich et al. [[8\]](#page-9-7) recently reported that mechanically-ventilated patients with hypercapnic acidosis requiring kidney replacement therapy only achieved modest reductions in the arterial $pCO₂$ (even after applying extracorporeal carbon dioxide removal), presumably because of the loading of blood with $CO₂$ via use of bicarbonate-rich substitution fluids during CVVH. Better understanding of acid–base chemistry of blood during the administration of bicarbonate-containing substitution fuids in extracorporeal circuits will likely assist in developing new approaches to improve the outcome of AKI patients.

The current work describes a mathematical model of acid–base balance during CVVH and continuous venovenous hemodiafltration (CVVHDF) based on a model of acid–base chemistry of blood by Rees and Andreassen [\[9,](#page-9-8)

[10\]](#page-9-9). The main objective of this work is to predict changes in the acid–base composition of blood within a CKRT circuit as a result of using substitution and dialysis fuids containing high bicarbonate concentrations; as a frst step, this work is limited to predicting changes in blood chemistry within the extracorporeal circuit only.

2 Methods

2.1 Total carbon dioxide mass balance

CVVH and CVVHDF extracorporeal circuits are shown in Fig. [1](#page-1-0) where, for simplicity, it has been assumed that there is negligible net fuid removal from the patient, and only steady state conditions were considered. During CVVH, the total substitution fluid flow rate (Q_s) is thus equal to the ultrafiltration rate (Q_f) , and the fraction of substitution fuid that is infused preflter in predilution mode is denoted by the letter f. During CVVHDF, the sum of the predilution substitution fuid fow rate and dialysis fuid flow rate is equal to the total substitution fluid flow rate; as with CVVH, the fraction of the total substitution fuid infused preflter is denoted by the letter f. In both cases, the inlet and outlet blood fow rates to the extracorporeal circuit indicated by Q_{bi} are equal. Consideration here is restricted to conditions where the composition of all substitution and dialysis fuids during a given treatment are assumed to be the same.

Mass balance during both CVVH and CVVHDF requires that total carbon dioxide concentration in the blood inlet of the hemofilter (C_i) is modified from that in the patient's blood by the following relationship (see Appendix)

Fig. 1 Schematics of the fow of blood, substitution fuid and dialysis fuid in CVVH and CVVHDF circuits. The blood fow rate from the patient is denoted by Q_{bi} ; it contains a total carbon dioxide concentration of C_{bi} . The total substitution/dialysate fluid flow rate is denoted by Q_s ; it contains a total carbon dioxide concentration of C_s . The symbol f denotes the fraction of substitution fuid that is infused

before the flter (predilution). The total carbon dioxide concentration entering the filter is denoted by C_i (see Eq. [1](#page-2-0)). The total carbon dioxide concentration in the outfow dialysis fuid during CVVHDF is denoted by C_{se} ; in general, that concentration is not used in any model calculation

$$
C_{i} = \frac{C_{bi} + (fQ_{s}/Q_{bi})C_{s}}{1 + fQ_{s}/Q_{bi}}
$$

\n
$$
J = D\left(1 - Q_{f}/Q_{i}\right)(C_{s}/\alpha - C_{i}) - Q_{f}C_{i}
$$
\n(3)
\nwhere D denotes the dialysance, Q_f denotes the ultrafiltration

where C_{bi} and C_s denote total carbon dioxide concentrations in patient blood entering the extracorporeal CKRT circuit and in substitution fuid, respectively. During CVVH the relationship between the acid–base composition of blood entering and exiting the hemoflter is determined by the ultrafiltration rate and the overall sieving coefficient. Here, it was assumed that the overall sieving coefficient for total carbon dioxide is equal to unity; stated in other words, it is assumed that the concentration of total carbon dioxide in the ultrafltrate is equal to that in plasma. Under such conditions, the total carbon dioxide concentration in blood exiting the hemofilter (C_0) can be readily calculated since the acid–base composition of plasma and red blood cells does not change within the hemofilter; there is only a change in the hematocrit (see Supplementary Materials). The term overall sieving coefficient used here is unconventional but represents the combined effects of the true sieving coefficients for dissolved carbon dioxide and bicarbonate, the volume of protein occupied by plasma proteins, and electrostatic

$$
J = D\Big(1 - Q_f/\psi_{Q_i}\Big)(C_s/\alpha - C_i) - Q_f C_i \tag{3}
$$

rate, defned as positive in the blood-to-dialysate direction, α denotes the Donnan factor (1.05 for a monovalent anion) $[12]$ $[12]$, C_s denotes the total carbon dioxide concentration in the dialysis fluid, Q_i denotes the blood flow rate into the hemofilter $(Q_{bi} + fQ_s)$, and C_i denotes total carbon dioxide concentration in the blood entering the hemoflter as described in Eq. [\(1\)](#page-2-0). As the dialysate fow rate is relatively small compared with both the blood fow rate into the hemoflter and the dialysance, it will be assumed that the dialysance is equal to the inlet dialysate flow rate or $(1-f)Q_s$; under these assumptions therefore, Eq. [\(3](#page-2-1)) becomes

$$
J = (1 - f)Q_s \left(1 - \frac{fQ_s}{Q_i}\right) \left(C_s / \alpha - C_i\right) - fQ_s C_i \tag{4}
$$

This equation represents an upper bound to the actual transport rate; the latter will be less than that predicted by Eq. ([4](#page-2-2)).

Mass balance across the CVVHDF flter then allows the calculation of the total carbon dioxide concentration from the outlet of the extracorporeal circuit (C_{b_o}) as (see Appendix)

$$
C_{bo} = C_{bi} + \frac{fQ_s}{Q_{bi}}C_s + \frac{J}{Q_{bi}} = C_i + (1 - f)Q_s / Q_{bi} \left(1 - \frac{fQ_s}{Q_i}\right) (C_s / \alpha - C_i)
$$
\n(5)

forces from the Donnan effect. An improved description of the overall sieving coefficient requires one to identify the true sieving coefficients for a specific hemofilter. Likewise, the total carbon dioxide concentration in blood exiting the extracorporeal circuit (C_{b0}) after infusion of postdilution substitution fuid during CVVH can be expressed by the following (see Appendix)

$$
C_{bo} = C_o \Big(1 + (f - 1) \Big(Q_s /_{Q_{bi}} \Big) \Big) + (1 - f) \Big(Q_s /_{Q_{bi}} \Big) C_s \tag{2}
$$

Equations ([1\)](#page-2-0) and ([2](#page-2-3)) were used to determine the total carbon dioxide composition of blood at diferent positions within the extracorporeal CVVH circuit (for example, C_i , C_o and C_{bo}) using the mathematical model of acid–base chemistry of blood described below.

Equations describing mass balance of total carbon dioxide concentration during CVVHDF difer because there is both difusive and convective transport of solutes with this modality. We assumed the equation proposed by Sargent and Gotch [[11](#page-9-12)] describes difusive and convective transport of total carbon dioxide within the flter (J), defned as positive in the dialysate-to-blood direction, as follows (see Appendix).

where C_i is described in Eq. ([1\)](#page-2-0).

2.2 Non‑bicarbonate bufer and hematocrit mass balance

Albumin is the major non-bicarbonate buffer in plasma [[9,](#page-9-8) [13](#page-9-11)]. As albumin is not present in substitution fuids used during CKRT, it can be assumed that the concentration of non-bicarbonate bufer in substitution fuid is zero. Thus, in general, Eq. ([1](#page-2-0)) can be used to calculate the dilution of total non-bicarbonate bufer concentration in plasma entering the hemoflter (using the plasma, not the blood, flow rate) and the total non-bicarbonate buffer concentration exiting the extracorporeal circuit can be assumed to be equal to that entering the extracorporeal circuit as net fluid removal is zero and the hemofilter sieving coefficient of albumin is assumed equal to zero. A similar argument applies to changes in hematocrit; these changes in total nonbicarbonate buffer concentration and hematocrit assume that bicarbonate buffer tonicity is identical to that in plasma such that the substitution fuid does not enter red blood cells.

The total non-bicarbonate buffer concentration in plasma exiting the hemoflter was determined by assuming a sieving coefficient is equal to zero and realizing that ultrafiltration only removes plasma water. The hematocrit exiting the hemoflter was calculated by a cell balance analysis as described in Supplementary Materials. Specifc equations used for calculating the total non-bicarbonate bufer concentration in plasma and hematocrit within and exiting the extracorporeal circuit are specifed in Supplementary Materials.

2.3 Bufer base mass balance and base excess

The model of acid–base chemistry of blood described below requires that base excess be determined at each position within the extracorporeal circuit. The concept of base excess is only germane to blood and other body fuids; however, the bufer base (concentration) of any fuid is equal to the strong ion diference [[14](#page-9-13)], and base excess is a parameter that can be derived from the buffer base of a solution [\[9\]](#page-9-8). Substitution fuids typically contain only bicarbonate, dissolved carbon dioxide and various electrolytes; thus, the bufer base and strong ion diference of such solutions can be assumed to be equal to their bicarbonate concentration. Because mass balance considerations of buffer base are comparable to those for total carbon dioxide, we can use Eqs. $(1, 2, 3, 4 \text{ and } 5)$ to determine buffer base at positions within a CKRT extracorporeal circuit by using buffer base concentrations instead of total carbon dioxide concentrations. The determination of bufer base exiting the hemoflter is more complex since the sieving coefficient of the two main buffer base components, bicarbonate and albumin (or non-bicarbonate buffer), differ. The equations used to calculated the buffer base concentration of blood exiting the hemoflter are specifcally described in Supplementary Methods.

We then used the definition of base excess as the calculated bufer base of blood under the conditions within the extracorporeal circuit minus the buffer base of the same blood sample (i.e., the same hematocrit and total non-bicarbonate concentration in plasma) under normal conditions defined as full oxygenation, a $pCO₂$ of 40 mmHg and a pH equal to 7.4 [[9\]](#page-9-8). The latter can be also be calculated using the model of acid–base chemistry of blood under diferent applied conditions as described in Supplementary Materials.

2.4 Assumed clinical conditions

The purpose of this work is to use a mathematic model to predict acid–base balance within and exiting the extracorporeal circuit during CKRT for an assumed acid–base composition of blood entering the extracorporeal circuit. Current CKRT devices typically access venous, not arterial, blood; thus, venous blood composition will be selected to be representative. Blood fow rates during CKRT are typically 150–200 mL/min but under some conditions can be up to 400 mL/min. The volume of substitution fuid used is typically based on patient body weight but is generally about 2 L/h, although it may be increased to increase uremic toxin removal. Substitution fuid composition can vary signifcantly to control blood electrolyte composition (for example, serum potassium or phosphorus); however, many of the elements of blood do not infuence acid–base balance directly and will be neglected further here. The main components of substitution fuid considered will be the bicarbonate concentration of either 32 or 22 mEq/L; these concentrations of bicarbonate were chosen since they have been evaluated in previous clinical studies $[3, 4]$ $[3, 4]$ $[3, 4]$. As described above, these substitution fuids have a strong ion diference and bufer base of 32 or 22 mEq/L, respectively. These solutions also contain dissolved carbon dioxide at low but somewhat variable concentrations such that the pH of commercial solutions vary from 7.0 to 8.5. It will be assumed that the dissolved carbon dioxide concentration in these solutions is such that the pH is 7.4; based on that assumption and the Henderson-Hasselbalch equation [[9\]](#page-9-8), the substitution fluids with bicarbonate concentrations of 32 and 22 mEq/L will be assumed to have $pCO₂$ of 52.2 and 35.9 mmHg, respectively. The total carbon dioxide concentration in the substitution and dialysis fuids is then the sum of the bicarbonate and dissolved carbon dioxide concentrations.

2.5 Calculation of blood acid–base composition

We used the model described by Rees and Andreassen [[9,](#page-9-8) [10](#page-9-9)] to determine the acid–base chemistry of blood within the extracorporeal circuits of CVVH and CVVHDF. Once the concentrations of total carbon dioxide and base excess in whole blood and that of the total non-bicarbonate bufer in plasma are derived as above, the model can calculate the complete acid–base composition in plasma and red blood cells; these calculations are not detailed here but have been completely described elsewhere [[9](#page-9-8), [10\]](#page-9-9). In Supplementary Materials, we describe the equations used to determine the acid–base composition of blood based on this approach. Briefy, this model calculates the total carbon dioxide concentration in blood as the volume-weighted sum of that in plasma and red blood cells. The total carbon dioxide concentration in plasma is the sum of the concentrations of dissolved carbon dioxide and bicarbonate, and the total carbon dioxide concentration in red blood cells is the sum of the concentrations of dissolved carbon dioxide and bicarbonate within red blood cells plus that of carbamino hemoglobin (hemoglobin with bound carbon dioxide moieties). The total concentration of oxygen in blood is similarly quantifed; it includes concentrations of dissolved oxygen and oxygenated hemoglobin, the latter within red blood cells only. The concentration of total non-bicarbonate bufer in plasma is the sum of both the protonated and non-protonated forms of the buffer (or buffers) that are in equilibrium; the fraction of each are dependent on plasma pH. The whole blood base excess is the weighted sum of that in plasma and red blood cells as defned elsewhere [\[9](#page-9-8)]. All chemical reaction equilibrium constants and other parameters were assumed as previously described [[9](#page-9-8)] and are listed in Supplementary Materials. Throughout this work, the fraction of red blood cells (hematocrit) of whole blood was assumed to be 0.3, and the oxygen saturation of venous blood was assumed to be 0.7. The oxygen content of blood was assumed constant throughout the extracorporeal circuit.

Using the above equations, the acid–base composition of blood at any position in the extracorporeal circuit can be determined by simultaneously solving 19 equations according to the model of Rees and Andreassen [[9](#page-9-8), [10\]](#page-9-9). We performed these calculations using Matlab (Version R2018a, MathWorks, Natick, MA, USA).

3 Results

The acid–base composition of venous blood entering the extracorporeal circuit assumed a total carbon dioxide concentration of 19 mmol/L and a base excess of−8 mmol/L, comparable to that which occurs for a patient with metabolic acidosis with normocarbia in previously reported clinical studies $[3, 5]$ $[3, 5]$ $[3, 5]$ $[3, 5]$; the complete acid–base composition is detailed in Supplementary Materials. Figure [2](#page-4-0) shows the efect of blood fow rate and substitution fuid fow rate

during CVVH on the calculated values of plasma bicarbonate concentration and $pCO₂$ in blood entering the extracorporeal circuit, after infusion of predilution substitution fuid (i.e., entering the hemoflter), and at the outfow of the extracorporeal circuit. Here, results are shown for a substitution fluid with a bicarbonate concentration of 32 mEq/L, 33% infused in predilution mode; the venous blood composition was assumed the same in each. Plasma bicarbonate concentration and $pCO₂$ were only modestly higher after infusion of substitution fuid, both in blood entering the hemoflter and that exiting the extracorporeal circuit. These trends were accentuated when using higher rates of substitution fuid but lessened when the blood flow rate was higher. Additional model predictions regarding the effect of substitution flow rate on total carbon dioxide concentration in blood, base excess in blood, total non-bicarbonate bufer concentration in plasma and hematocrit at several positions within the extracorporeal circuit under these same conditions are listed in Table [1](#page-5-0). As expected, higher substitution fluid flow rates resulted in higher total carbon dioxide concentrations in blood and more positive base excess values in blood exiting the extracorporeal circuit.

Figure [3](#page-5-1) shows plasma bicarbonate concentration and pH under the same conditions as in Fig. [2](#page-4-0). Although plasma bicarbonate concentration increases after both predilution and postdilution infusion of substitution fuid, plasma pH is not substantially altered. The lack of a change in plasma pH resulted from approximately proportional increases in plasma bicarbonate concentration and $pCO₂$. At a blood flow rate of 200 mL/min and a substitution fow rate of 2 L/hr, for example, the relative increase at the exit of the CVVH circuit in plasma bicarbonate concentration was 9.7% and the

Fig. 2 Plasma concentration of bicarbonate ([bicarbonate]) and partial pressure of carbon dioxide $(pCO₂)$ in venous blood entering the CVVH circuit, after infusion of substitution fuid in predilution mode and in the outfow from CVVH circuit. Blood fow rate and substitution fuid fow rates were 200 mL/min and 2 L/h for black bars,

200 mL/min and 3 L/h for white bars and 400 mL/min and 2 L/h for gray bars. Results are shown in solid bars for [bicarbonate] and in dotted bars for $pCO₂$. The total carbon dioxide concentration and base excess in blood entering the CVVH circuit were assumed as 19 and −8 mmol/L, respectively

Table 1 Predicted values of total carbon dioxide concentration in blood $([tCO2]_b)$, base excess in blood (BE), total non-bicarbonate buffer concentration in plasma $([tNBB]_n)$, and hematocrit for diferent substitution fow rates at several positions in the extracorporeal CVVH circuit at a blood fow rate of 200 mL/ min with 33% predilution of substitution fuid containing 32 mEq/L bicarbonate

Fig. 3 Plasma concentration of bicarbonate ([bicarbonate]) and pH in blood entering the CVVH circuit, after infusion of substitution fuid in predilution mode and in the outfow from CVVH circuit. The fraction of substitution fuid infused predilution was 0.33. Blood fow rate and substitution fuid fow rates were 200 mL/min and 2 L/h for black

bars, 200 mL/min and 3 L/h for white bars and 400 mL/min and 2 L/h for gray bars. Results are shown in solid bars for [bicarbonate] and in dotted bars for pH. The total carbon dioxide concentration and base excess in blood entering the CVVH circuit were assumed as 19 and − 8 mmol/L, respectively

relative increase in $pCO₂$ was 8.2%, resulting in an unaltered plasma pH in blood exiting the CVVH circuit.

Figure [4](#page-6-0) compares the efect of the bicarbonate concentration in substitution fuid on plasma bicarbonate concentration and $pCO₂$ within the extracorporeal CVVH circuit. As expected, using a substitution fuid with a lower bicarbonate concentration of 22 mEq/L blunted increases in both plasma bicarbonate concentration and $pCO₂$ within and exiting the CVVH circuit. Indeed, there was virtually no increase in $pCO₂$ within and exiting the CVVH circuit with the lower bicarbonate concentration in the substitution fluid. Figure [5](#page-6-1) compares the effect of CVVHDF instead of CVVH on plasma bicarbonate concentration and $pCO₂$ with a substitution/dialysis fuid containing a bicarbonate concentration of 32 mEq/L, 33% infused into the blood in the predilution mode. Use of CVVHDF instead of CVVH using the same substitution/dialysis fuid composition had a minor

effect on plasma bicarbonate concentration and $pCO₂$ within and exiting the extracorporeal circuit. Smaller increases in plasma bicarbonate concentration during CVVHDF resulted from the lower rates of bicarbonate transfer to blood due to the Donnan effect, reducing the transfer rate of bicarbonate anions into blood. Figure [5](#page-6-1) also shows the efect of using 100%, instead of only a fraction, of the substitution fuid in the predilution mode. Infusion of all substitution fuid in the predilution mode resulted in similar, but slightly lower, plasma bicarbonate concentration and $pCO₂$ exiting the extracorporeal circuit.

The above results assumed only a single acid–base composition of venous blood entering the extracorporeal circuit; however, this may difer depending on the patient's underlying medical condition and may vary over days of treatment for a given patient. Figure [6](#page-7-0) shows the

Fig. 4 Plasma concentration of bicarbonate ([bicarbonate]) and partial pressure of carbon dioxide $(pCO₂)$ in venous blood entering the CVVH circuit, after infusion of substitution fuid in predilution mode and in the outfow from CVVH circuit. Blood fow rate and substitution fuid fow rates were 200 mL/min and 2 L/h with a bicarbo-

nate concentration of 32 mEq/L (black bars) and 22 mEq/L (white bars). Results are shown in solid bars for [bicarbonate] and in dotted bars for $pCO₂$. The total carbon dioxide concentration and base excess in blood entering the CVVH circuit were assumed as 19 and −8 mmol/L, respectively

Fig. 5 Plasma concentration of bicarbonate ([bicarbonate]) and partial pressure of carbon dioxide $(pCO₂)$ in venous blood entering the extracorporeal circuit, after infusion of substitution fuid in predilution mode and in the outfow from extracorporeal circuit. Blood fow rate and substitution fuid fow rates were 200 mL/min and 2 L/h during CVVH for black bars and during CVVHDF for white bars; the fraction of substitution fuid in the predilution mode was 0.33 for

both. Blood fow rate and substitution fuid fow rates were 200 mL/ min and 2 L/h during CVVH with all substitution fuid infused in the predilution mode for gray bars. Results are shown in solid bars for [bicarbonate] and in dotted bars for $pCO₂$. The total carbon dioxide concentration and base excess in blood entering the CVVH circuit were assumed as 19 and −8 mmol/L, respectively

efect of blood and substitution fuid fow rates during CVVH when venous blood contained a high $pCO₂$, representing a patient with potential lung dysfunction. This example assumed a total carbon dioxide concentration of 25 mmol/L and a base excess of -2 mmol/L in venous blood; the complete acid–base composition is detailed in Supplementary Materials. The model predictions in Fig. [6](#page-7-0) are qualitatively similar to those shown in Fig. [2.](#page-4-0) Similar calculated results were predicted when the assumed acid–base composition of blood during CVVHDF was as described in Fig. [6](#page-7-0) when compared to those in Fig. [5](#page-6-1) (results not shown).

4 Discussion

Several clinical studies have evaluated acid–base balance during CKRT but have focused primarily on comparing the advantages and disadvantages of bicarbonate versus lactate as the substitution fluid buffer base $[15-21]$ $[15-21]$ $[15-21]$. Virtually all such studies have been concerned with overall effects on whole body acid–base balance with little effort to understand the direct effects of buffer base administration on acid–base chemistry in the blood of the extracorporeal circuit per se. A recent study by Jonckheer et al.

Fig. 6 Plasma concentration of bicarbonate ([bicarbonate]) and partial pressure of carbon dioxide $(pCO₂)$ in blood entering the CVVH circuit, after infusion of substitution fuid in predilution mode and in the outfow from CVVH circuit. Blood fow rate and substitution fuid flow rates were 200 mL/min and 2 L/h for black bars, 200 mL/min and 3 L/h for white bars and 400 mL/min and 2 L/h for gray bars.

Results are shown in solid bars for [bicarbonate] and in dotted bars for $pCO₂$. These predictions are comparable to those in Fig. [2](#page-4-0) but for a diferent composition of venous blood entering the CVVH circuit. The total carbon dioxide concentration and base excess in blood entering the CVVH circuit were assumed as 25 and −2 mmol/L, respectively

[[22](#page-10-1)] reported blood acid–base and oxygen chemistry of blood at various positions within a CVVH extracorporeal circuit for the frst time. That work demonstrated a decrease in bicarbonate concentration and $pCO₂$ in blood within a CVVH circuit after the infusion of predilution substitution fuids that did not contain bicarbonate (citrate was the bufer base in this instance). Such fndings are not comparable to those studied in the current work, although the current model can apply to those conditions (results not shown). Empirical data to directly confrm the model predictions reported in this study are not currently available in the literature.

The mathematical model described herein predicts that the administration of bicarbonate via difusion or convection results in only a modest increase in plasma bicarbonate concentration and $pCO₂$ without a significant change in plasma pH in the blood exiting the extracorporeal circuit. This model prediction results from a conversion of bicarbonate to dissolved carbon dioxide and similar relative increases in bicarbonate concentration and $pCO₂$ in plasma. The addition of bicarbonate to blood during CKRT is akin to adding bicarbonate to blood in a so-called "closed system", where it has been previously suggested from in vitro experiments [[23](#page-10-2)] and theoretical arguments [[24\]](#page-10-3) that such bicarbonate additions to blood do not produce large changes in plasma pH. Although the current model predictions appear counter intuitive since administration of solutions containing bicarbonate to patients will, in time, result in an increase in plasma pH, they are consistent with expectations in a so-called "closed system" when bicarbonate is added to blood. It should be noted that the plasma pH in blood exiting an extracorporeal circuit during maintenance hemodialysis [[25,](#page-10-4) [26](#page-10-5)] is reduced when those patients are chronically treated with high dialysis fuid concentrations of bicarbonate and high dialysis fuid fow rates; such conditions result in substantially larger transfer rates of bicarbonate into blood. The current model of acid–base chemistry of blood does result in similar predictions of changes during maintenance hemodialysis as in those latter studies (Pietribiasi and Leypoldt, manuscript in review). The increase in whole body plasma pH after administration of bicarbonate solutions to patients is due to the "open system" conditions when accounting for the loss of dissolved $CO₂$ in the patient's lungs [[24](#page-10-3)].

Diferences in acid–base balance during CVVHDF versus CVVH therapies have not been directly evaluated in previous clinical studies although it has been proposed that metabolic acidosis would be more prevalent during CVVHDF than CVVH [\[27](#page-10-6)]; this is consistent with the model predictions in the current work. The only empirical comparison of acid–base balance during CVVH and CVVHDF in the literature is difficult to evaluate critically since the content of the substitution and dialysis solutions were diferent [[28\]](#page-10-7). Although the current model predictions show differences between CVVHDF and CVVH therapies regarding acid–base balance, these diferences are small and may not be clinically signifcant.

The mathematical model of acid–base chemistry used in this work is complex, but it cannot describe all chemical changes within blood during CKRT. For that purpose, more complex models would likely be required [[29,](#page-10-8) [30](#page-10-9)]. It is noteworthy however that the model of Rees and Andreassen [\[9](#page-9-8)] has been shown to be consistent with several physiological systems, in particular the mixing of blood with diferent compositions [\[31\]](#page-10-10). The mixing of diferent fuid streams in the extracorporeal CKRT circuit examined in this study is essentially akin to that of mixing two diferent types of blood, although in this instance blood is mixed with a cellfree, protein-free crystalloid solution.

Although this work makes novel predictions regarding acid–base chemistry in a CKRT extracorporeal circuit, there are several limitations that deserve mention, especially regarding the assumptions in the mathematical model that were necessary to make the calculations practical. For example, it has been assumed that the overall sieving coefficients of bicarbonate and dissolved carbon dioxide are equal to unity, that is the total carbon dioxide concentration in plasma and ultrafltrate are equal. Although measured true sieving coefficients for all small solutes are approximately equal to one [\[32\]](#page-10-11), ultrafltration occurs during CKRT only with the plasma water fraction of blood, not plasma itself. On the other hand, true sieving coefficients likely depend on the hemofilter employed; thus, further consideration of the efect of the true sieving coefficient and the effect of the volume of plasma proteins on model predictions using the current approach will require consideration of a hemoflter with specifc sieving properties. Second, it has been assumed that the dialysance of bicarbonate transfer during CVHDF is equal to the inlet dialysate fow rate; this assumption provides an upper bound for the dialysance; thus, our contention that acid–base balance during CVVHDF may be less efective than during CVVH is likely correct. A third limitation is the assumption that the non-bicarbonate bufer in plasma is composed solely of albumin. It is known however that plasma phosphate levels contribute to the bufering capacity of blood and that the phosphate level of patients treated by CKRT can have both higher or lower than normal levels of plasma phosphate; the efects of altered plasma phosphate concentration on the reported results require further study. Finally, we note that no consideration in the current work addressed the anticoagulant used during CKRT that could potentially infuence acid–base balance such as when using regional citrate anticoagulation. Thus, the current model predictions are only valid when using other anticoagulant strategies, such as when using heparin, the most widely used anticoagulant during CKRT according to Karkar and Ronco [[33](#page-10-12)].

In conclusion, a mathematical model of acid–base chemistry of blood can predict the efect of operating conditions on acid–base balance within the extracorporeal circuit during CKRT. Additional empirical measurements during CKRT are necessary to validate and potentially improve these model predictions.

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Author contributions JKL designed the study, wrote the original computer programs, and wrote the frst draft of the manuscript. MP assisted in writing the computer program; JE and KH assisted in designing the study and provided clinical input. All authors reviewed the manuscript, provided feedback on the frst draft, and approved the submission of the manuscript for publication.

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Data availability Portions of the computer code used in making model calculations are available if requested.

Compliance with ethical standards

Conflict of interest JKL is a consultant to Baxter International. JE and KH are full-time employees of Baxter International with ownership interests.

Ethical approval No studies involving patients were reported in this manuscript, thus, no ethics approval was necessary.

Research involving human and animal rights statements This manuscript does not involve research requiring human and animal rights statements.

Appendix

Equations [\(1](#page-2-0)) and [\(2](#page-2-3)) in Methods can be derived from mass balance considerations before and after the infusion of substitution fuids during CVVH. First, the mass fow rate of total carbon dioxide after predilution infusion of substitution fuid and entering the hemoflter (total carbon dioxide concentration times fluid flow rate or $C_i \times (Q_{bi} + fQ_s)$ must equal the mass fow rate of total carbon dioxide in blood entering the extracorporeal CVVH circuit or $C_{bi} \times Q_{bi}$ plus the mass fow rate of total carbon dioxide with infusion of substitution fluid or $C_s \times fQ_s$. Stated in mathematics, this requires

$$
C_i(Q_{bi} + fQ_s) = C_{bi}Q_{bi} + C_s fQ_s
$$
\n
$$
(6)
$$

After some algebra, this equation can be rearranged to Eq. ([1\)](#page-2-0) in Methods. Second, the mass fow rate of total carbon dioxide exiting the hemofilter or $C_0 \times \{Q_{bi} + (f-1)Q_s\}$ plus the mass fow rate of total carbon dioxide via the postdilution infusion of substitution fluid or $C_s \times (1-f)Q_s$ must equal the mass fow rate of total carbon dioxide exiting the extracorporeal circuit or $C_{bo} \times Q_{bi}$. Stated as an equation, this requires

$$
C_{i} \{ Q_{bi} + (1 - f)Q_{s} \} + C_{s} (1 - f)Q_{s} = C_{bo} Q_{bi}
$$
 (7)

This equation can be rearranged to Eq. ([2\)](#page-2-3) in Methods.

To assess mass or solute transport from blood to dialysate during hemodialysis with both difusive and convective solute transport, the following equation (in the terminology of the current work) was defined by Sargent and Gotch $[11]$ $[11]$ $[11]$ as

$$
J = D(C_i - C_s) + Q_s (C_i - \frac{D}{Q_i}(C_i - C_s))
$$
\n(8)

where D denotes the dialysance and Q_i denotes the blood flow rate into the hemofilter. In this equation both J, the overall solute transport rate, and Q_s , the ultrafiltration rate, were defned as positive in the blood-to-dialysate direction. As in Methods, C_i and C_s denote total carbon dioxide concentrations in blood and dialysis fuid, respectively. When it is noted that J in Methods is defned as positive in the opposite or dialysate-to-blood direction, Eq. [\(3\)](#page-2-1) is the result after some algebra if the dialysis fuid concentration is modifed by the Donnan efect as suggested by Sargent et al. [\[12](#page-9-10)]. Mass balance during CVVHDF requires that the mass fow rate of total carbon dioxide exiting the hemoflter or $C_{\rm bo} \times Q_{\rm bi}$ must equal the mass flow rate into the hemofilter or $C_i \times Q_i$ plus the mass transport rate of total carbon dioxide from dialysis fuid to blood or J. Stated as an equation, this requires

$$
C_{bo} \times Q_{bi} = C_i \times Q_i + J \tag{9}
$$

Algebraic rearrangement of this equation in conjunction with Eqs. (1) (1) (1) and (4) (4) yields Eq. (5) (5) in Methods.

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