ORIGINAL RESEARCH

Monitoring the level of hypnosis using a hierarchical SVM system

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Abstract

Monitoring level of hypnosis is a major ongoing challenge for anesthetists to reduce anesthetic drug consumption, avoiding intraoperative awareness and prolonged recovery. This paper proposes a novel automated method for accurate assessing of the level of hypnosis with sevofurane in 17 patients using the electroencephalogram signal. In this method, a set of distinctive features and a hierarchical classifcation structure based on support vector machine (SVM) methods, is proposed to discriminate the four levels of anesthesia (awake, light, general and deep states). The frst stage of the hierarchical SVM structure identifes the awake state by extracting Shannon Permutation Entropy, Detrended Fluctuation Analysis and frequency features. Then deep state is identifed by extracting the sample entropy feature; and fnally light and general states are identifed by extracting the three mentioned features of the frst step. The accuracy of the proposed method of analyzing the brain activity during anesthesia is 94.11%; which was better than previous studies and also a commercial monitoring system (Response Entropy Index).

Keywords Depth of anesthesia · Electroencephalogram (EEG) · Hierarchical classifcation · Support vector machine

1 Introduction

The use of the electroencephalogram (EEG) to monitor level of hypnosis during surgery is highly desirable to prevent delayed recovery [[1\]](#page-6-0) and also minimize the possibility of the patient being aware or experiencing pain intraoperatively [\[2](#page-6-1), [3](#page-6-2)]. Currently, some commercial EEG devices such as the M-Entropy module (Datex-Ohmeda, Helsinki, Finland) [\[4](#page-6-3)],

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Bispectral index (BIS, Covidien) [[5\]](#page-6-4) and Narcotrend index monitor [[6](#page-6-5)] are widely used in clinical practice for the estimation of level of hypnosis with moderate success.

In the last decade, a large number of features from the EEG have been proposed to assess level of hypnosis with more precision; such as relative power in the classical frequency bands [[7,](#page-6-6) [8](#page-6-7)], largest Lyapunov exponent [[9](#page-6-8)], Lempel–Ziv complexity analysis [\[10\]](#page-6-9), Bayesian methods [[11](#page-6-10), [12\]](#page-6-11), phase-rectified signal averaging [[13\]](#page-6-12), distribution of auto-regressive moving average model parameters [[14](#page-6-13)], Hilbert–Huang transform $[15]$, recurrence analysis [[16](#page-6-15)], Detrended Fluctuation Analysis (DFA) [\[17,](#page-6-16) [18](#page-6-17)] and entropies [[19](#page-6-18)–[22](#page-6-19)]. These analyses provide information which describes the complexity of EEG signals. But, none of the above mentioned methods has been proved to be adequately reliable for measuring level of hypnosis in the clinical setting. Anesthetic drugs cause complicated neurophysiological changes during the transition from awake to deep anesthesia and a comprehensive set of features is required to adequately describe these processes. Therefore, some researchers have combined a number of features to extract most aspects of brain activity [[23](#page-6-20)[–27\]](#page-6-21). Moreover, diverse classifcation methods have been utilized for mapping a set of features to diferent states of hypnosis. For example, some researchers have used Artifcial Neural Network [[9](#page-6-8), [21\]](#page-6-22), and adaptive neuro-fuzzy inference system [\[28](#page-6-23)–[30](#page-6-24)]. These structures can successfully model systems with nonlinear relationships between inputs and outputs. However, there is the unsolved problem of the accurate classifcation of the overlapping states.

Recently in other biomedical research application, features and classifiers are combined in an efficient mannerusing a hierarchical structure—to determine the classifcation performance robustly in overlapping classes [\[31–](#page-6-25)[37](#page-7-0)]. Using the divide-and-conquer strategy [[38](#page-7-1)], hierarchical classifcation attempts to combine classes with similar characteristics in specifc features into one class, which can then be separated later at the succeeding steps with other features. The main idea behind this method is to separate the data into two classes (the 'specifc class' and other classes) at each level using specifc features. The data of other classes is then reclassifed at the next level using diferent features. This approach is shown to be very useful for biomedical applications, because using diferent feature set to classify diferent classes in a hierarchical structure is very efficient compared to using a single feature set for the whole dataset.

The main contribution of this paper is to identify a set of robust and discriminative features from EEG signal and develop a hierarchical classifcation structure based on a support vector machine (SVM) to distinguish the four levels of anesthesia (awake, light, general, and deep anesthetic states) effectively. The ability of this novel system to classify EEG into four anesthetic states is evaluated with a commercial monitoring system (Response entropy (RE) index), in 17 patients during sevofurane anesthesia.

2 Materials and methods

2.1 Subjects and data acquisition

Seventeen patients with age 18–63 years are used in this study. These patients were scheduled for orthopedic, gynecological or general surgery. The details have been previously published [\[39\]](#page-7-2). The GE electrode system was applied to the forehead of all the patients. EEG data is recorded with 100 sample per second and M-Entropy system was used to measure the RE Index (0.2/s). Based on the anesthesiologist's judgment, the EEG data of patients were classifed into awake, light anesthesia, general anesthesia and deep anesthesia. A 680 s (s) segment of EEG signal was extracted in each state for each patient. Then, for analysis, EEG data were separated into 10 s sections. As a result, each state comprised 68 test sections. Details of separating EEG signal in one of the four states of anesthesia based on the anesthesiologist's judgment have been previously published [\[40](#page-7-3)].

2.2 EEG‑derived parameter extraction

A comprehensive set of features is required to adequately quantify the complexity of EEG dynamic patterns during the transition from awake to deep anesthesia. We have extracted the following four features to do this.

2.2.1 Frequency‑index

Frequency-index is the logarithmic relative spectral energy of frequency bands in (30–47) Hz and (11–21) Hz respectively

$$
Beta_index = \log \frac{E(30 - 47)}{E(11 - 21)}
$$
 (1)

These frequencies are chosen based on other studies [[6,](#page-6-5) [7\]](#page-6-6).

2.2.2 Sample entropy (SampEn)

SampEn algorithms are described below [\[41](#page-7-4)]:

1. Suppose a time series X_N with *N* points, produces vectors of length *m* defned as:

$$
X_i = [x_i, x_{i+1}, \dots, x_{i+m-1}].1 \le i \le N-m
$$
\n(2)

2. Computing the distance between X_i and X_j , represented by $d(X_i.X_j)$ as:

$$
d(X_i.X_j) = \max(|x_{i+k} - x_{j+k}|), 0 \le k \le m - 1, j \ne i
$$
\n(3)

3. Calculating this possibility is shown below:

$$
P_i(m,r) = \frac{n_i(m,r)}{N-m-1}, \quad i-1, N-m
$$
 (4)

where $n_i(m.r)$ shows the number of vectors X_j which are analogous to X_i conditional on $d(X_i, X_j) \leq r$.

4. Evaluating

$$
A(m.r) = \frac{1}{N - m} \sum_{i=1}^{N - m} P_i(m.r)
$$
 (5)

- 5. Setting $m = m + 1$ and again repeating steps 1–4
- 6. Obtaining SampEn of X_N as:

$$
SampEn(XN, m, r) = -Ln \frac{A(m+1, r)}{A(m, r)}
$$
(6)

2.2.3 Shannon permutation entropy (SPE)

Numerical feature that describe EEG signal complexity is called SPE. The details of this algorithm have been previously published in [[42\]](#page-7-5).

2.2.4 Detrended fuctuation analysis (DFA)

The DFA has proven useful in revealing the extent of longrange correlations in time series especially in EEG signal. The details of this algorithm have been previously published in [[17,](#page-6-16) [18\]](#page-6-17).

2.3 Statistical analysis

The Database used for the whole project consist 272 data related to 68 diferent patients (four data derived from one individual). Due to the limited dataset, we have used a special case of K-fold Cross-Validation in which K is equal to one. In this method which is known as leave one out procedure, one data is considered as the test data and the remaining data are used for the training set at each trial. This is repeated until all data are evaluated as a test data for one time. By averaging the all results, we obtain an estimate of the evaluation performance. Therefore, the obtained result is fair and not dependent to the data division approach since the test and training data have no correlation in each step and all data participate in testing phase for one time. The schematic of how data is divided in leave one out method can be shown in Fig. [1.](#page-2-0)

2.4 SVM classifcation

SVMs are broadly applied in classifcation issues. Assume that a binary classifer is used to categorize the following data:

$$
\theta = \{ (x_1, y_1), (x_2, y_2), \dots, (x_l, y_l) \}
$$

$$
y_i = 1 \text{ or } -1
$$
 (7)

where x_i are sample data containing features and y_i are the corresponding class labels. The linear model of the separator function is given by:

$$
f(x) = \sum_{i=1}^{l} \omega_i x_i + b \tag{8}
$$

where w_i is the weight vector and b is constant. These parameters should be calculated in such a way that the margin between the hyperplane and nearest data becomes maximum. The resultant optimization problem can be described as follows:

$$
\min_{\omega, \zeta} \frac{1}{2} (\omega^T \omega) + C \sum_{i=1}^l \zeta_i
$$
\n
$$
subject to \begin{cases} y_i((\omega^T x_i) + b) \ge 1 - \zeta_i \\ \zeta_i \ge 0 \text{ for } i = 1 \dots l \end{cases} \tag{9}
$$

C is a positive constant which makes a balance between tolerance of deviations and fatness of the function. For example, larger C results overftting to the training data and less generalization. ζ_i for $i = 1, 2, ..., l$ are slack variables which allows a slight error for each data. The equivalent dual problem can be introduced by using Karush–Kuhn–Tucker theorem as follows [[43](#page-7-6)]:

Fig. 1 The schematic of data division in Leave one out cross validation methodology in SVM classifcation

minimize<sub>$$
\alpha_i
$$</sub> $G(\alpha) = -\sum_{i=1}^{l} \alpha_i + \frac{1}{2} \sum_{i,j=1}^{l} \omega_i \alpha_i \alpha_j y_i y_j K(x_i.x_j)$
subject to

$$
\begin{cases} 0 \le \alpha_i \le C & (10) \\ \sum_{i=1}^{l} \alpha_i y_i = 0. \end{cases}
$$

where α_i are Lagrangian multipliers and $K(x, y) = (\phi(x), \phi(y))$ is a kernel function. In advance classifcation problems, it is usually not practical to fnd a separable trajectory which can distinct the data especially when there exist overlapped features. In response to this situation, Support vector classifcation maps the feature space into a higher dimension space by using kernel function (ϕ : $x \in \mathbb{R}^n \to \mathbb{R}^m$) and construct an optimal discriminant hyperplane in that space. Common choices for the kernel function are quadratic, polynomial, and Radial Basis Function (RBF). The parameters are set in the optimization process which is known as training phase. With all the above modifications, the decision hyperplane can be rewritten as follows:

$$
f(x) = sign\left(\sum_{i=1}^{l} \alpha_i y_i K(x, x_i) + b\right)
$$
\n(11)

Each test data is fed to this function. If the resultant value of the function is positive, the data is labeled $+1$ and the data would be labeled -1 if the output is negative.

2.5 Hierarchical SVM classifcation structure

A hierarchical classifcation structure tries to overcome the overlapped states using the divide-and-conquer strategy so that states with similar characteristics for specifc features are combined into one state, which can be separated later at the succeeding steps with other features. This structure based on a sequence of SVM is designed to classify EEG data into different states during anesthesia. In the first step, we separate between awake and non-awake states (light, general and deep anesthetic). The SPE, DFA and Beta features extracted from EEG signal are used as input to SVM which classifes the input data into one of these two states. If the data is classifed as the awake state, the procedure is fnished. Otherwise, the data is classifed as non-awake state and move on to the next stage. In the second stage, we separate the non-awake data into deep and non-deep state (light and general anesthetic). The SampEn feature is used as input to SVM which classifes the non-awake data into one of these two states. If the data is classifed as the deep state, the procedure is fnished. Otherwise, the data is classifed as non-deep state and we pass on to the next stage. Finally, we separate non-deep data into light and general states. In this stage, the DFA, SPE, and Beta features are used as input to SVM which classifes the non-deep data into light or general anesthetic. The process chart of the hierarchical SVM classifcation structure which is composed of three stages is shown in Fig. [2](#page-3-0).

3 Results

Four features—Beta, SampEn, SPE, and DFA—are computed from each 10 s EEG segment. Figure [3](#page-4-0) shows box plots related to the distribution of each of four features for the entire data. $m = 6$ in SPE and $k = mr = 0.15$ in SampEn are calculated according to sampling frequency of EEG signal, trial and error and other studies [[19,](#page-6-18) [20](#page-6-26)]. Hierarchical SVM classifcation structure described in II.E is used to classify EEG data into diferent states during anesthesia in 17 patients. The frst-stage classifer is responsible for determining the awake state, the second stage classifer is for the deep state and fnally, third stage is for separation the light and general states. In all classifcation levels, RBF is selected as the kernel function of SVM. The sigma value (σ) which describes the diversity of RBF is optimized to have the minimum average classifcation error in each stage by try and error. The optimal σ for RBF kernel are 0.31, 0.90 and 0.80

Fig. 2 The process chart of the hierarchical SVM classifcation structure

Fig. 3 The box plot of SampEn ($k = 0.15$), SPE ($m = 6$), Beta index, DFA and RE index which describes the data distribution of each feature in the diferent states. Awake (I), light anesthetic (II), general anesthetic (III) and deep anesthetic (IV), respectively. The red line

indicates the median value; the rectangle lower and upper edges represent 25 and 75 percentiles of the values distribution; the whiskers represent the bounds of 99.7% of the data; and the red "+" symbol represents the data outliers

Table 1 Confusion matrices obtained from the frst, second and third stages of hierarchical SVM classifcation structure

| Stage | True labels | Estimated labels | |
|--------------|-------------|-------------------------|-----------|
| First stage | | Awake | Non-awake |
| | Awake | 64 | 3 |
| | Non-awake | 7 | 198 |
| Second stage | | Deep | Non-deep |
| | Deep | 65 | 1 |
| | Non-deep | 2 | 130 |
| Third stage | | Light | General |
| | Light | 60 | 2 |
| | General | 1 | 67 |

for frst, second and third stage of classifer, respectively. Table [1](#page-4-1) shows the confusion matrices obtained from the frst, second and third stages of hierarchical SVM classifcation structure, separately. The confusion matrix shows the diferences between the output of the proposed classifer and the real class label. The proposed structure separate between awake and non-awake data with 96.32% accuracy in the frst stage, deep and non-deep with 98.48% accuracy and between general and light with 97.69% accuracy in the fnal stage. When we get the results of the frst, second and third stages, the fnal classifcation result in detecting the four states is 94.11%. The accuracy obtained by the proposed method in every state of anesthesia is given in Table [2.](#page-4-2) As you see, the hierarchical classifcation structure can discriminate the four states of anesthesia efectively.

For comparison with other methods, Table [2](#page-4-2) shows the values of classifcation accuracy in every state of anesthesia using SVM classifer (RBF kernel) and MultiLayer Perceptron (MLP) using two hidden layers with three neurons when the four selected features are used as the inputs of the classifers. The parameters of these two classifers are optimized by the trial and error to obtain the best results. Clearly, it is demonstrated that, thanks to its multistage structure, the

proposed hierarchical structure signifcantly improves the classifcation performance in all states. For the test data, the prosed system was quicker to calculate. In Matlab on a laptop computer (CPU:i7-3.5 GHz, RAM:16 GB), the average time spent for the proposed system was 0.0019 s. Finally, the results of the proposed system was compared to a commercial monitoring system (RE Index) on the same database. The box plot related to the distribution of RE values from each 10 s EEG segment for all patients is constructed in Fig. [3](#page-4-0). Table [2](#page-4-2) represents the value of classifcation accuracy based on the RE index. Clearly, it is demonstrated that our new system attains higher classifcation accuracy in all anesthetic states, as compared to the RE Index.

4 Discussion

In this study, we propose a new automated system to assess level of hypnosis from EEG signal, based on a set of discriminative features (DFA, SPE, SampEn, and Beta features) and a hierarchical classifcation structure based on a SVM. This system could classify the EEG data into awake, light, general and deep states during anesthesia in 17 patients and yields an overall accuracy of 94.11%.

When the characteristics of the data distribution of four features for the entire data are observed (Fig. [3](#page-4-0)), it is determined that all states cannot be identifed fully by extracting any single feature because of overlapping brain states. The SPE feature has a unique ability to distinguish the awake state (I) from non-awake states and this capability is also partly available for the Beta and DFA features. After determining and removing the data from this state, SampEn feature was best at discriminating the deep anesthetic (IV) state from other states. Finally, after determining and removing the data from these two states, the SPE, DFA and Beta features are important features for discriminating the light (II), and general anesthetic (III) states. Consequently, it was observed that diferent feature sets represent diferent components for the four anesthetic states. For this reason, we decided to design a sequential hierarchical classifcation structure to obtain better performance in monitoring level of hypnosis. In this structure, at each level, diferent feature extraction methods are used to determine the specifc state. If the state of data is determined in each level, the procedure is fnished; otherwise, other feature extraction methods for another state are used. The speed of parameter learning, the small number of adjustable parameters, and the accuracy of classifcation in diferent states are the advantages of our structure compared to the other methods.

Describing the behavior of the EEG as a function of the depth of consciousness and properties of the signal processing algorithms assists to extract the relative features. In anesthetic-induced EEG; First, large waxing and waning 'spindle-like' waves appear whose frequencies are often related to the anesthesia drug concentration in the blood [\[3\]](#page-6-2). At low anesthetic concentrations, the frequency is in the beta spectral range (light anesthesia) and categorizes well with our Beta index, but with the increased drug concentration (general anesthesia), the frequency of signal slows down to about 8 Hz. This component can be distinguished more precisely using SPE features because it considers both overall signal variability characteristics, naturally related to spectral content and the signal's complexity [\[41\]](#page-7-4). As anesthesia gets deeper, large amplitude delta and sub-delta waves may be seen [[17](#page-6-16), [18\]](#page-6-17) which can be detected more accurately using DFA feature. Finally, the EEG signal changes into a burst suppression pattern (deep anesthesia) which is a pattern of high amplitude EEG signal, known as the bursts, separated by low amplitude activity normally under 10 µv peak-to-peak, named the suppressions. SampEn is robust in the description of this pattern [[20](#page-6-26), [21\]](#page-6-22) because it provides naturally regular interpretation of the suppression in so far as the threshold is higher than data points during suppression. These amplitudes of the burst waves help us achieve such high level of threshold. These justifcations support the selection of signal processing techniques in this research and rationalize why these kinds of properties of EEG signal can be evaluated properly by our methods.

The result of this paper was also compared to previous studies with the same database. In [\[20](#page-6-26)], MLP classifer and in [[21](#page-6-22)] ANFIS classifer are used for assessing level of hypnosis which result in 88% and 92% accuracy, respectively. In the present study, thanks to the proposed hierarchical classifcation method, we have attained the higher classifcation accuracy (94.11%) which is proven to have better performance than other methods. However, because of the high variability in response to anesthetic drugs, this work needs to be validated in large patient data sets.

5 Conclusions

A hierarchical classifcation structure based on a SVM is able to estimate real time level of hypnosis (using EEG data) into awake, light, general and deep anesthetic states. The proposed system combines three classifers with different features in a cascade manner in order to achieve good performance. SPE, DFA and Beta features are utilized to capture awake state in the frst stage, SampEn feature to capture deep anesthetic state in the second stage and fnally three mentioned features of frst step to capture light and general states.

Compliance with ethical standards

Conflict of interest We have no conficts of interest.

Ethical approval All procedures performed in studies involving human participants were in accordance with the ethical standards of the institutional and/or national research committee and with the 1964 Helsinki declaration and its later amendments or comparable ethical standards. This study received ethics committee approval at Waikato Hospital, New Zealand.

Informed consent Informed written consent was obtained from all patients included in the study.

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