

Leveraging prior strain rates efect during stress relaxation of Sn–1.7Ag–0.7Cu lead‑free alloys with microalloying of Te and Co for microelectronics applications

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Abstract

Prior strain rate history during stress relaxation (SR) behavior is one of the fundamental issues adapting the design of solder joints. In this paper, the SR tests were performed on Sn–1.7Ag–0.7Cu (SAC177) solder with Te and Co addition at the elastic region. The SR of SAC177 solders occurred at high prior deformation history could induce unexpected relaxation resistance depending on the qualified proportions of Te and Co microalloying. The global strain rate ϵ_p of three solders was found to follow the power-law with stress-sensitivity *n* of 5.8–7.6. The activation energies *Q* of 58.15–78.23 kJ mol−1 were achieved from SR results at initial stress σ_0 of 10 MPa. An evolved SR model based on logarithmic single barrier model is intended in the present study to predict and confrms the SR mechanism. Microstructure assessment shows that the SR behaviors are controlled by pipe difusion assisted with dislocation climb. According to the proposed relaxation model, the extent of SR and SR rate of SAC177 solder were found to be decreased markedly with increasing prior strain rate, *Q* value and Te/Co addition. Moreover, signifcant enrichment in the elastic compliance of SAC177 solders was noticed after Te/Co addition due to increasing the ductility, which has good predictions for electronics applications.

1 Introduction

Solders are a kind of metallic materials that can be used in all electronics industry since the growing of electronics era. The eutectic or near-eutectic Sn–Pb solder were used for assembling electronics owing to its high reliability, appropriate solderability, manufacturability and low pricing [\[1](#page-9-0)]. Because of the intrinsic toxicity of Pb-based solders, extensive attempts have been implicated to design innovative Sn-based lead-free solders for electronic interconnection. The Sn–Ag–Cu(SAC) alloy family is one of the highest promising alternative to Sn–Pb solders that could apply in fip-chip electronic interconnections, ball grid arrays (BGA) and other multiple electronic packages in modern electronic technology [\[2](#page-9-1)]. Recently, the low Ag-content SAC solders system has been developed by microalloying of metallic elements such as, Zn, Bi, Sb, Ni, nanoparticles, etc. [\[3,](#page-9-2) [4](#page-9-3)]. It is recognized that the shrinking of volume fraction of large platelet Ag3Sn phase in these low-Ag SAC solders could improve their mechanical properties and enrich their reliability $[4-6]$ $[4-6]$ $[4-6]$. For instance, Zn can refine Ag₃Sn IMC particles of SAC103 solders and formed the $(Cu, Ag)_{5}Zn_{8}$ IMC particles that enhance the yield strength (YS) with largest ductility [\[7](#page-9-5), [8\]](#page-9-6). Bi particles addition to SAC157 solder leads to substantial increase in ultimate tensile strength (UTS), YS and Young's modulus, while the ductility was sustained at the SAC157 level [[9\]](#page-9-7).

Since the solder joints operate at elevated homologous temperatures ($T/T_{\text{m}} \approx 0.4{\text{-}}0.8$, T_{m} is the eutectic temperature), the microstructural instability and the variation in coefficients of thermal expansion (CTE) at the substrate are of great concern [\[10\]](#page-9-8). These severe process conditions could deteriorate the electrical connector, which intended to encounter the most performance requests at end of suitable life of components. Therefore, the annihilation of initial bonding force with time at substrate is one of the foremost topics in the design of solder joints. The annihilation of initial bonding force gives rise to an open circuit. For this reason, the SR test is a reliable method for assessment the contact force and its deformation mechanism [[11\]](#page-9-9). Despite the

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other aspects, such as alloy components, time, temperature, initial stress and grain size, the prior deformation history of strain rate on SR behavior is the vital aspect affecting the solder joints. For instance, the σ_0 levels imposed before SR in eutectic Sn–40Pb, Sn–4Ag, and Sn–2.5Ag–0.8Cu–0.5Sb at 23 °C were found to depend on the prior strain rates, i.e. high SR could result in higher cyclic deformation histories of strain rates [[12\]](#page-10-0). However, since it is hard to design solder joints with defnite amount of normal stress at the contact interface, the designed force must be improved to verify the end-of-suitable life force. For this reason, the prior deformation history could enhance the designed force to verify the end-of-suitable life force. Until this work, no systematic study has been reported on the efect of prior deformation history on stress relaxation behavior of low-Ag SAC177 solder. In this study, the infuence of prior strain rate on SR behavior of SAC177 solder has been investigated at diferent processing conditions of temperatures. At the same time, microalloying of Te and Co elements were added to enhance the microstructure and modifying the design of SAC177 solder joints. The efects of Te and Co microalloying on the growth rate of Ag_3Sn and Cu_6Sn_5 IMCs and SR behavior have been discussed in this paper. SR tests were carried out to evaluate the controlling deformation mechanisms at different temperature conditions for SAC177 solders.

2 Experimental procedures

The low-Ag content SAC177, SAC177-0.2Te and SAC177-0.5Co alloys with the chemical compositions of Sn–1.7Ag–0.7Cu, Sn–1.7Ag–0.7Cu–0.2Te and Sn–1.7Ag–0.7Cu–0.5Co (wt%) were used for the study. The alloys were prepared from metal ingots of Sn (99.9%), Ag (99.999%), Cu, Co and Te (99.99%). The metal ingots were melted at 800 °C for \sim 1 h in a quartz tube under a KCl + LiCl (1.3:1) atmosphere in an induction furnace. The ingots melts were mechanically stirred to verify master alloy dissolution. The ingots were cast into a steel mold and left to cool at cooling rate of 6–8 °C/s, so as to construct microstructures typically create in small solder joints in electronic industries. In order to attain the surface quality demanded for scanning electron microscope (SEM) and EDS assessments, the samples were polished and etched with a solution of 3% HCl, 2% and HNO₃ in 95% ethyl alcohol for a few seconds. The prepared specimens were analyzed by XRD analysis to identify the precipitated phases in the solidifed alloys. Then, tensile tests were done to measure the stress–strain and stress-time relations using computerized tensile testing system described previously [\[13](#page-10-1)]. A number of shaped rods for each of three alloys, having nominal gage diameters of 1.2×10^{-3} m with a gage length of 4×10^{-2} m, were prepared for tensile tests. Stress–strain tests were carried out frst for a small time to achieve the initial stress of 10 MPa at the elastic region. The tensile tests were performed at prior strain rates of $6.6 \times 10^{-5} - 3.5 \times 10^{-3}$ s⁻¹ and temperature range of 25–110 \degree C. And then, SR tests were performed immediately after each tensile test. The created imposed strain for each sample corresponding to the desired initial stress was then held constant to permit the initial stress of 10 MPa to relax for a sufficient relaxation time t_{SR} of 5000 s. However, the SR test was repeated three times for the entire alloy samples.

3 Results and discussion

3.1 Solidifcation microstructure of SAC177 based‑alloys

To identify the primary phases in the solders, the as-cast microstructures are examined by XRD. As shown in Fig. [1,](#page-1-0) the Sn, Ag₃Sn and Cu₆Sn₅ phases are existed in SAC177, SAC177-0.2Te and SAC177-0.5Co alloy samples. It is also notable that Te- and Co-microalloying are efectively suppressed the difraction peak intensity of Sn phase. This indicates that the crystallinity of three phases is refned with Te- and Co-microalloying. However, the affinity of Te into Sn to leads to formation of SnTe IMC particles in SAC177-0.2Te solder, while the high affinity of Co into Cu leads to formation of $(Cu, Co)₆Sn₅$ IMC precipitates in the SAC177-0.5Co solder. Based on the XRD results of Fig. [1,](#page-1-0) our current understanding of modifcation by Te/Co additions to SAC177 solder alloy can be advanced. As shown in Fig. [2](#page-2-0)a, the as-solidifed SAC177 alloy involves a fully eutectic structure of Ag₃Sn needles and Cu₆Sn₅ IMCs with

Fig. 1 XRD profles of as-solidifed SAC177, SAC177-0.2Te and SAC177-0.5Co alloys

Fig. 2 Low and high magnifcation FE-SEM image of SAC177 solder and their corresponding EPMA elemental mappings of Sn, Ag and Cu, showing the microstructure of $Cu₆Sn₅$ and Ag3Sn IMCs

haphazard distribution inside the β-Sn matrix. The average size of needle-like Ag_3Sn is approximately 7–30 μ m, while for irregularly shaped $Cu₆Sn₅$ IMCs is about 4–7 µm. The dual-phase mixture is consistent with earlier work of SAC alloys [[14\]](#page-10-2). The SEM-EPMA elemental map of SAC alloy microstructure in Fig. [2](#page-2-0)b–f shows that the starting microelectronic joint solder involves Sn, Cu and Ag. The microstructure of SAC177 is basically composed of Ag₃Sn and Cu₆Sn₅ phases inside β-Sn matrix. As a result, both the $Cu₆Sn₅$ and Ag₃Sn are at equilibrium in molten SAC177 alloy before nucleating the β-Sn phase. Compared with the basic SAC177 solder, the change in composition of IMC particles is detected with Te-microalloying as seen in Fig. [3](#page-3-0)a; Firstly, minor Te-microalloying (-0.2 wt\%) can introduce new hexagonal SnTe particles (with an average size of $\leq 10 \mu m$) within the eutectic and dendritic regions during the solidifcation process. Since the grain size of SnTe particles lies in the range of superplastic alloy materials, it will not induce micro-cracks. Therefore, these new IMC particles could be one of the causes that enhance the SR resistance of SAC177-0.2Te solder. Secondly, the growth of primary β-Sn grains with the appropriate volume fraction of fine eutectic $Cu₆Sn₅$ and Ag₃Sn particles could promote the mechanical property of SAC177-0.2Te solder. Figure [3b](#page-3-0), c estimates detailed views of FE-SEM micrograph and corresponding EDS analysis of SnTe IMC particles. However, the effective refinement of $Cu₆Sn₅$ and Ag₃Sn IMC particles contributed by minor amount of Te can be ascribed to its higher affinity. The higher affinity of Te to Sn atoms could reduce the activity of Sn, which reduces the driving force for $Cu₆Sn₅$ and Ag₃Sn IMC formation. Besides, SnTe particles can assist as an extra nucleation sites to promote the solidifcation process and retard the growth of IMCs. With Co addition, microstructure of SAC177 solder is signifcantly changed. Figure [4a](#page-4-0) shows the morphology progress of SAC177-0.5Co alloy. Clearly, 0.5wt% addition of Co into SAC177 solder leads to significant change in $Ag₃Sn$ morphology from coarse needle-like (Fig. [2](#page-2-0)a) into small volume fraction of fne needle-shaped (Fig. [4](#page-4-0)a). The presence of fne IMC particles can positively afect the mechanical **Fig. 3** Low and high magnifcation FE-SEM image of SAC177-0.2Te alloy and corresponding EDS analysis of SnTe IMC particles

reliability of solder when this alloy solder applied on novel green microelectronic devices. However, the small $Cu₆Sn₅$ particles were found to be regularly distributed at the β-Sn phase. As well, the dissolved Co and Cu elements are reacted with β-Sn phase to form an excessive amount of long stripshaped $(Cu, Co)₆Sn₅$ IMC particles in solder matrix. As seen in Fig. [4](#page-4-0)b–g, the mapping of elements identifed by EPMA shows the color mapping of Ag, Cu, Co and Sn elements. The β-Sn-matrix plays the utmost detection for fne particles (violet-green-pink-red) spread softly over the view sample. It seems that the content of Sn was minor only at areas attendant with $(Cu, Co)_6Sn_5$ and Ag₃Sn IMCs.

3.2 Strength and ductility

Drop impact reliability of solder joints has become one of vital topic for enhancing inventive portable electronics. To empathize this issue, a typical stress–strain tests for three SAC177, SAC177-0.2Te and SAC177-0.5Co alloys were conducted at strain rate of 5.8×10^{-4} s⁻¹ and T=25 °C. The results were presented in Fig. [5](#page-4-1) and the yield stress YS, ultimate tensile stress UTS and elongation are summarized in the corresponding histogram. It is noted that the tensile behaviors of three alloys refect the attendance of large plateau rejoins thanks to the relative equilibrium of dynamic recovery with work hardening processes during deformation. However, the Te and Co microalloying is markedly enriched the drop impact reliability of SAC177 alloy. The additions of Te and Co are slightly increased YS and UTS of SAC177 solder, whereas the ductility is signifcantly increased due to refne the microstructure along with the grew of fine SnTe and $Co₃Sn$ IMCs. The highest YS (28.0 MPa) and UTS (29.92 MPa) as well as elongation of 50.41% were observed for Co-containing solder. The Te and Co microalloying acknowledge the deformation to be ''spread out'' over the whole phases as well. The high stress and strain values of Co-containing solder could result in greater elastic compliance than that of SAC177 solder for innovative green microelectronic industry.

3.3 Stress relaxation dependence of prior strain rate

Figure [6](#page-5-0)a–c shows the SR behavior of three solders at different prior strain rates in terms of the decrease in yielding stress versus relaxation time. In all testing conditions, the amount of initial stress σ_0 was held constant at 10 MPa in the elastic region (lower than the YS point) at $T=25$ °C. For better comparison of results, the SR responses are superimposed to explicate the infuence of prior strain rates. As

Fig. 4 FE-SEM image of SAC177-0.5Co alloy and corresponding EDS analysis of $(Cu, Co)_6$ Sn₅ IMC particles

noticed from the curves, the rate of stress relaxation is accelerated in the primary stage of relaxation at initial time of 1000–1500 s, followed by a slight rate decrease at extended times up to 5000 s. The drastic drop of SR is detected at ~ 2.36 MPa with prior strain rate of 6.6×10^{-5} s⁻¹ for plain SAC177 solder, indicating the highest amount of relaxation $\Delta \sigma$ (*t*) [$\Delta \sigma = \sigma_o - \sigma(t)$] and SR rate *σ*^{*·*} [*σ*^{*=*} =d($\Delta \sigma/d$ ln(*t*)] among all solders, as shown in Table [1.](#page-5-1) The slowing down of SR may develop as a result of hardening following the plastic deformation and the lessening in mobile dislocation density [\[15\]](#page-10-3). Although the entire SR curves in Fig. [6](#page-5-0) show comparable trends, the fnal relaxed stress in three solders after 5000 s shows diferent SR behavior, depending on the initial imposed strain ε_0 or strain rate and alloy composition. For instance, at time of 5000 s, the total $\Delta \sigma$ is about 4.37, 4.02, 3.76 MPa, respectively, for SAC177, SAC177-0.2Te and SAC177-0.5Co solder samples at strain rate of 3.5 × 10^{-3} s⁻¹, as seen in Table [1.](#page-5-1) The low SR rate σ for Te- and Co-containing solders is largely ascribed to dislocation interaction with SnTe and $Co₃Sn$ IMCs that playing significant role in adapting deformation behavior despite the traditional dislocation–dislocation intersection. The dislocation loops accumulated nearby the IMC particles could generate internal stresses in the solder matrix, which leads to oppose the dislocation motion and hence could develop the strain hardening ability of Te- and Co-containing solders. However, the improvement in ε_0 values with prior strain rate during SR tests was the best for Co microalloying, as shown in Fig. [6d](#page-5-0). Even so, the higher ε_0 values of 0.002–0.013 observed at all prior strain rates for three alloys confrm that plasticity has occurred below the YS point. The occurrence of plasticity could ascribe to the high fraction of β-Sn grain boundaries and fne IMCs that acting as main sources of dislocations. Remarkably, the more plasticity is detected with SAC177- 0.5Co solder, followed by SAC177-0.2Te and SAC177

Fig. 5 Tensile stress–strain curves of SAC177, SAC177-0.2Te and SAC177-0.5Co alloys and corresponding histogram of yield stress YS, ultimate tensile stress UTS and elongation

Fig. 6 Experimental stress relaxation curves of SAC177, SAC177-0.2Te and SAC177-0.5Co alloys at 25 °C at diferent strain rates and prior strain rate dependence of imposed strain

solders (Table [1\)](#page-5-1). This was an unexpected result that elucidates the short-term SR history dependence established by these solder alloys. This phenomenon is in good agreement with previous observation on SR test for copper wires [[15,](#page-10-3) [16](#page-10-4)]. Nonetheless, this occurrence contrasts to that reported by Woodmansee and Neu [\[12\]](#page-10-0), where the cyclic prior deformation rates result in larger amount of stress relaxation and smaller relaxed stress for Sn–2.5Ag–0.8Cu–0.5Sb, Sn–4Ag and Sn–40Pb samples. They attributed this behavior to the decrease in the ratio of back stress/total stress. Majors and Krempl [\[17\]](#page-10-5), Yaguchi and Takahashi [[18](#page-10-6)] also proposed that the cyclic response dependent phenomena is unique and emphasize the non-linear relation between strain rate and relaxation stress. That means, increasing the cyclic strain rate causes less increase in the relaxation stress.

3.4 Stress exponent

In the present study, diferent SR behaviors of SAC177 based-solders have been conducted with initial stress σ_0 of 10 PMa in the elastic region and the corresponding deformation mechanisms will be assessed in this section. During the SR process, the total imposed strain ε_0 of specimen is kept constant. At any time t during SR test, SR occurs because of a part of ε_0 is converted into plastic strain ε_p . Hence, the total imposed strain ε_0 can be directly expressed as:

$$
\varepsilon_{o} = \varepsilon_{e} + \varepsilon_{p} = \text{Const.}
$$
 (1)

Since ε_0 is held constant, then the rate of change of $\varepsilon_0 = 0$. Equation (1) (1) can be by rewritten as:

$$
d\varepsilon_p/dt = -d\varepsilon_e/dt = -d(\sigma/E)/dt
$$
\n(2)

where ε_e is the elastic strain, σ is the current stress at any time *t* and $E = \sigma/\varepsilon_e$ is the elastic modulus. The elastic modulus *E* is determined as 28.6, 29.0 and 29.5 GPa for SAC177, SAC177-0.2Te and SAC177-0.5Co solders, respectively. Therefore, $d \epsilon_p/dt$ is considered as the creep strain rate from SR test. The relationship between strain rate *ε*· and stress *σ* for the three solders at 25 °C can be attained from Eq. [2](#page-6-1) and plotted in Fig. [7](#page-6-2)a. Besides, the efect of temperature on *ε°* versus σ curves for SAC177 solder is illustrated in Fig. [7b](#page-6-2). It is interesting to note that the three curves are coincident in first stage of relaxation below \sim 5 MPa, although they are separated in second the stage above 5 MPa. This result indicates that SR tests are not respond to applied stresses lower than the 5 MPa level, even if the SR tests were conducted at higher temperatures. Additionally, Fig. [7a](#page-6-2) shows that the relaxation strain rate of SAC177 is greater than that of SAC177-0.2Te and SAC177-0.5Co in the secondary stage of SR. That means, Te and Co microalloying enhanced the creep resistance of SAC177 solder. Also, in the 2nd SR stage, a certain stress and temperature could yield diferent SR rates for three samples. This suggests that SR rate is afected by the transient stress in the 1st stage and processing temperature. In this case, dislocation motion could grow quickly as the critical stress of 5 MPa can be merely overcome. Based on the power-law equation, the global strain rate ε ^{*i*}**p** is *correlated with relaxing stress σ by the following relation [*[19](#page-10-7)*]:*

$$
\varepsilon_{\mathbf{p}} = A\sigma^{\mathbf{n}} \tag{3}
$$

For assessing the stress exponent *n*, the natural logarithm of Eq. [3](#page-6-3) is rearranged as:

$$
\ln \epsilon_{\mathbf{p}} = \ln A + n \ln \sigma \tag{4}
$$

Figure [8](#page-7-0) shows the steady strain rate versus stress curves of entire alloys in log–log from SR tests. The *n* values were determined from the slop of ln ε_p – ln σ . It can be seem that *n* values are increased respectively, from 5.8 to 6.8 and 7.6 with Te and Co microalloying at constant $\epsilon = 3.5 \times 10^{-3} \text{s}^{-1}$ and $T=25$ °C. However, the variations of *n* values with increasing strain rate are listed in Table [1,](#page-5-1) while the

Fig. 7 Global stress dependence of strain rate for of SAC177, SAC177-0.2Te and SAC177-0.5Co alloys at 25 °C

Fig. 8 Global strain rate dependence of stress for SAC177, SAC177-0.2Te and SAC177-0.5Co alloys at 25 °C derived from SRT at diferent prior strain rates

variations of *n* with temperatures for three alloys are summarized in Table [2](#page-7-1). Interestingly, the *n*-value for power-law creep was found to depend on the imposed strain or strain rate, wherein it can decrease with increasing strain rate and/ or deformation temperature, as shown in Fig. [9](#page-8-0). Besides, the higher *n* values were observed with Te and Co microalloying. The slight drop of *n* value with increasing temperature for Te- and Co-containing solders indicates the higher stability of its microstructure, and could be attributed to the high dissipation ability of heat by the new SnTe and $(Cu, Co)_6$ Sn₅ IMCs that developed in the alloy matrix and impeding the dislocation motion, which restrains the SR process. However, stress exponent refects the deformation mechanism in a sense. Generally, the *n* values which approach 4–7 indicate climbing of dislocations [\[7](#page-9-5)–[9\]](#page-9-7).

3.5 Activation energy during hot deformation

Generally, the deformation process of alloy materials is controlled by diffusion mechanism [[7,](#page-9-5) [8](#page-9-6)]. The

Table 2 Activation energy (*Q*), stress exponent (*n*) values for SAC(177), SAC(177)-0.2Te and SAC(177)-0.5Co solder alloys at different temperature and constant strain rate $\varepsilon = 3.5 \times 10^{-3} \text{s}^{-1}$

Alloys	Tempera- ture $(^{\circ}c)$	N	Q_{exp} . (kJ/mol)	$Q_{Theorritical}$ (kJ/mol)
SAC 177	25	5.8	58.15	63.06
	70	4.5		
	90	4.3		
	110	4.2		
SAC 177-0.2Te	25	6.8	71.10	69.77
	70	5.5		
	90	5.3		
	110	5.1		
SAC 177-0.5Co	25	7.6	78.23	75.48
	70	6.7		
	90	6.5		
	110	6.1		

Fig. 9 Imposed strain dependence of stress exponent *n* derived from SRT at 25, 70 and 110 °C for SAC177, SAC177-0.2Te and SAC177-0.5Co alloys

development of the global strain rate $\varepsilon_{\rm p}$ *during SR tests as a function of relaxing stress σ and deformation temperature T can be mathematically appointed with the Arrhenius power-law equation [*[19](#page-10-7)*] as:*

$$
\varepsilon_{\rm p} = A\sigma^{\rm n} \exp\left(-\mathcal{Q}/RT\right) \tag{5}
$$

where *Q* is the activation energy, *R* is the gas constant, *A* is the creep constant and *n* is the stress exponent. The *Q* values can be evaluated from:

$$
Q = Rn \left[\frac{d \ln \sigma}{d \left(\frac{1}{T} \right)} \right] \epsilon
$$
 (6)

The logarithmic relationship between relaxation stress ln σ and 1000/T (K⁻¹) at strain rate of 3.5 × 10⁻³ s⁻¹ is presented in Fig. [10](#page-8-1). By linear ftting, the *Q* values of 58.15, 71.10 and 78.23 kJ mol⁻¹ for SAC177, SAC177-0.2Te and SAC177-0.5Co solder alloys, respectively; can be matched well with the grain boundary difusion mechanism [[7–](#page-9-5)[9](#page-9-7), [18](#page-10-6)]. These *Q* values indicate that the activation energy of SAC177 based-solders varies with the relaxation

Fig. 10 The activation energy (Q) values of SAC177, SAC177-0.2Te and SAC177-0.5Co alloys at constant strain rate 3.5×10^{-4} s⁻¹

stress, stress exponent and testing temperature according to Eq. (6) (6) (6) .

In an attempt to establish the mechanism of stress relaxation, a quantitative analysis has been carried out on the experimental results based on single barrier model of loga-rithmic SR [\[15](#page-10-3)]. The SR rate σ in this model has been represented as a function of activation energy *Q*, initial stress $σ_o$ of relaxation and temperature *T* by the relation:

$$
\sigma = [kT\sigma_0/(Q - mkT)] \tag{7}
$$

where *k* is Boltzmann constant and the constant $m = 25$. By differentiating Eq. [7](#page-9-10) with regard to σ_0 , one can obtain the *Q* values of three solders, as:

$$
(\mathrm{d}\sigma'/\mathrm{d}\sigma_0) = [kT/(Q - mkT)] \tag{8}
$$

$$
Q = kT[m + (d\sigma_0/d\sigma')] \tag{9}
$$

The unit of *Q* values designed from Eq. [\(9](#page-9-11)) is eV. However, Eq. ([9\)](#page-9-11) can be reserved. Here, as is striking, we replace the constant *m* by stress exponent *n* values and the Boltzmann constant *k* by gas constant *R*. Thus one has:

$$
Q = RT\left[n + \left(\mathrm{d}\sigma_{\mathrm{o}}/\mathrm{d}\sigma\right)\right]
$$
 (10)

The unit of *Q* values designed from Eq. ([10](#page-9-12)) is kJ mol⁻¹. The attained *Q* values of the relaxation process from the empirical formula in Eq. [\(10\)](#page-9-12) at room temperature are; 63.06, 69.77 and 75.48 kJ mol−1 for SAC177, SAC177-0.2Te and SAC177-0.5Co solder alloys, respectively. These *Q* values are close to that obtained from Eq. [\(6](#page-8-2)), as seen in Table [2.](#page-7-1) The numerical *Q* value results illustrate that the developed relaxation model can describe the inelastic deformation of SAC177, SAC177-0.2Te and SAC177-0.5Co alloys with good accuracy. Moreover, the *Q* values are in the order of magnitude of grain boundary difusion mechanism. They are somewhat small to be associated with the lattice difusion mechanism (90–120 kJ mol⁻¹) [\[7](#page-9-5), [8,](#page-9-6) [20](#page-10-8)]. Interestingly, the calculated *Q* values from the modifed relaxation model are in good agreement with *Q* values from the present experimental results. Alternatively, Eq. ([10](#page-9-12)) also implies that the modifed relaxation model could better confrm the SR rate σ· dependence of kinetic parameters, wherein σ· is decreased with increasing *Q* values, and hence with Te/Co addition to SAC177 solders (as seen in Fig. [6](#page-5-0)). This could ascribed to the amount of unrelaxed dislocation pile-ups that growing at the interface boundaries of SnTe and $(Cu, Co)_6$ Sn₅ IMCs in the path of an elastic relaxation. These accumulated dislocation pile-ups could induce incessant reduction in the movement of further dislocations arriving from inside the crystal lattice. And could result in an associated reduction in the SR level and SR rate of SAC177-0.2Te and SAC177- 0.5Co alloys; the greater the interface boundaries of IMCs, the better the hindering efect, and hence the minimum the amounts of SR and SR rate. Similar behavior was observed for Cu–42.2Zn–0.6Pb alloys [\[16](#page-10-4)]. The variations in solidifcation mode and its structural efects, such as the SR level and SR rate, suggest that a single barrier model is not suffcient to explain increasing *Q* values appertaining to the

relaxation stress, since the *n* values are changed with varying deformation temperature.

4 Conclusions

- (1) Te and Co microalloying enhanced both the strength and ductility of SAC177 alloy. This is a signifcant issue, which develops the elastic compliance and impact resistance of solder joints assembled in SAC177 alloys.
- (2) The achieved strength improvement is activated by precipitation hardening effects of $SnTe$ and $Co₃Sn$ IMCs in the respective alloys, while the enriched ductility of Te- and Co-containing alloys can be ascribed to structural refnement caused by the microalloying.
- (3) According to the modifed single barrier model of logarithmic stress-relaxation, the amount of SR and SR rate of SAC177 solder were signifcantly decreased with increasing prior strain rate, *Q* value and Te/Co addition.
- (4) The structural relaxation of SAC177 solders occurred at high prior deformation history could induce unexpected relaxation resistance that depends on the qualifed proportions of Te and Co microalloying, high prior deformation results in both low SR levels and SR rates.
- (5) According to the obtained *n* and *Q* values, the dominant deformation mechanism in of SAC177 and Te-containing alloys is dislocation climb with pipe difusion over the entire temperature range examined. The *Q* values obtained from the modifed relaxation model are consistent with the experimental results.

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