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# **Improved thermoelectric properties of n-type Bi<sub>2</sub>Te<sub>3</sub> alloy deriving from two-phased heterostructure by the reduction of CuI with Sn**

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Received: 24 October 2018 / Accepted: 15 November 2018 / Published online: 28 November 2018 © Springer Science+Business Media, LLC, part of Springer Nature 2018

#### **Abstract**

In this report, CuI and Sn co-doped n-type  $Bi_2Te_3$  samples have been prepared by a high-temperature solid-state reaction, and the effect of co-doping on the thermoelectric properties was investigated from room temperature to 525 K. Sn single-doped and undoped  $Bi_2Te_3$  were prepared for comparison. Detailed charge transport data including electrical conductivity, Seebeck coefficient, Hall coefficient, and thermal conductivity are presented. Microscopic observation of CuI/Sn co-doped samples revealed that numerous distinctive microstructures such as nanoprecipitates of the Cu and SnI-rich phase were generated in the matrix. The lattice thermal conductivity of CuI/Sn co-doped  $Bi_2Te_3$  was substantially reduced compared to those of undoped and single doped  $Bi_2Te_3$ . Benefiting from the improved electrical transport properties by doping and the reduced lattice thermal conductivity by numerous microstructures, the ZT value of the  $Bi_2Te_3$  doped with 1 at.% CuI/Sn is distinctly enhanced to 1.24 at 425 K. The average ZT value ( $ZT_{ave} \sim 1.02$ ) at 300–525 K was clearly higher than those of Sn-doped  $Bi_2Te_3$  ( $ZT_{ave}$  ~ 0.54) and CuI-doped  $Bi_2Te_3$  ( $ZT_{ave}$  ~ 0.98). This work indicates that the average ZT can be improved over a broad temperature range using a co-doping approach.

# **1 Introduction**

Thermoelectric materials, which can enable direct transformation of waste heat to electric energy, provide an alternative solution to energy and environmental issues. Thus, exploring high-efficiency thermoelectric materials have attracted ever-increasing attention both from the viewpoint of an academic research and industrial applications [[1,](#page-8-0) [2](#page-8-1)]. The efficiency of a thermoelectric device is directly related to the material's thermoelectric performance, which is determined by a dimensionless figure of merit (ZT), defined as  $ZT = (S^2 \sigma/\kappa)T$ , where S,  $\sigma$ ,  $\kappa$  and T denote the Seebeck coefficient, electrical conductivity, thermal conductivity and working temperature in Kelvin, respectively [\[3](#page-8-2)].

Bismuth telluride  $(Bi<sub>2</sub>Te<sub>3</sub>)$  and its alloys are regarded as some of the most promising materials for solid-state refrigeration applications, and they operate in a temperature range between 200 and 400 K [\[4](#page-8-3)]. A series of p- and n-type semiconductor pairs are needed to fabricate the thermoelec-tric cooling devices [[5\]](#page-8-4). A high ZT of  $> 1.86$  at 320 K was achieved in p-type  $Bi_2Te_3$ -based TE materials [\[6](#page-8-5)]. However, the ZT value of n-type  $Bi_2Te_3$  is still relatively lower than that of its p-type counterpart [\[7](#page-8-6)[–9\]](#page-9-0). Therefore, there is still a great need for developing new n-type  $Bi_2Te_3$  with a high ZT that can match well with p-type counterparts. So far, considerable efforts have been made to enhance the thermoelectric properties of n-type  $Bi<sub>2</sub>Te<sub>3</sub>$  by changing its composition by chemical doping/alloying [[10–](#page-9-1)[13](#page-9-2)], and microstructural modification by introducing defects/nanostructures [\[7](#page-8-6), [14,](#page-9-3) [15](#page-9-4)]. Bi<sub>2</sub>Te<sub>3</sub> can be p-type by doping with extrinsic atoms such as Bi, Se, Ge, Sn, Pb, and rare earth elements or n-type with In, Cl, I, CuI, and  $SbI_3$  [[16\]](#page-9-5). The resonant level formed by Sn doping strongly enhances the thermoelectric power of  $Bi_2Te_3$  at room temperature [[17\]](#page-9-6). Intercalation of metal between the weak van der Waals gap in the  $Bi_2Te_3$  structure has been realized one of the effective strategy to improve the ZT value and stability of  $Bi_2Te_3$  materials  $[18–20]$  $[18–20]$ . However, it is very difficult to achieve high levels of intercalation due to the formation of secondary phases or substitution instead of intercalation by interactions between intercalant species and the matrix. Combining the effects of substitution and intercalation has also been reported previously to improve the thermoelectric properties [[21\]](#page-9-9). The co-doping of Cu and I in  $Bi<sub>2</sub>Te<sub>3</sub>$  enhances the power factor, thus increasing the ZT of  $(Cul)_{0.01}$  Bi<sub>2</sub>Te<sub>3</sub> (ZT∼1.16 at 368 K). In addition to

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the high peak ZT, thermoelectric materials should also have high average performance within the working temperature range.

Herein, we report new progress in tuning the thermoelectric properties of n-type  $Bi_2Te_3$  by employing CuI as a co-dopant with Sn. The experiment was conducted in two stages. We first studied the effect of the concentration of the alloyed Sn atoms on the thermoelectric properties of  $Bi<sub>2</sub>Te<sub>3</sub>$ . After this, we carried out experiments on co-doping; more specifically, we studied the variation of the thermoelectric properties of  $Bi_2Te_3$  doped with both Sn and CuI.

# **2 Materials and methods**

#### **2.1 Synthesis**

All reagents were purchased from Sigma-Aldrich and were used as obtained including: Bi chunks (99.999%), Te chunks (99.999%), CuI powder (99.999%), and granular Sn (99.5%). A series of CuI/Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$  samples with a chemical formula of  $(CuI+1/2Sn)_xBi_{2-x}Te_3$  (x = 0.01, 0.03, 0.05, 0.07, 0.1; namely CuI/Sn-substituted  $Bi_2Te_3$ ) and  $(CuI+1/2Sn)_{x}Bi_{2}Te_{3}$  (x = 0.01, 0.03, 0.05, 0.07, 0.1; namely CuI/Sn-added  $Bi_2Te_3$ ) were prepared by means of the conventional high-temperature solid-state reaction method.  $Bi<sub>2</sub>Te<sub>3</sub>$  samples doped by Sn alone with the chemical formulas  $Sn_xBi_{2-x}Te_3$  (x = 0.01, 0.03, 0.05; namely Sn-added  $Bi_2Te_3$ ) and  $Bi_{2-x}(Sn)_xTe_3$  (x = 0.01, 0.03, 0.05; namely Snsubstituted  $Bi<sub>2</sub>Te<sub>3</sub>$ ) were prepared under identical experimental conditions to allow for a meaningful comparison. We also prepared undoped  $Bi<sub>2</sub>Te<sub>3</sub>$  as a pristine material. A series of doped  $Bi<sub>2</sub>Te<sub>3</sub>$  samples with masses of ~30 g were melted in evacuated quartz tubes ( $\sim 10^{-3}$  Torr) using a rocking furnace at 1273 K for 24 h; then, the samples were cooled to room temperature at a rate of 80  $^{\circ}$ C h<sup>-1</sup>. The resulting ingots were crushed into fine powders using a ball mill (8000D; SPEX, USA) for 40 min. Then, the samples were densified by a spark plasma sintering (SPS) method (SPS-211LX, Fuji Electronic Industrial Co., Ltd.) at 723 K for 5 min in a 12.7 mm diameter graphite die under an axial compressive stress of 50 MPa in vacuum. Highly densified  $(>98\%$  of theoretical density) disk-shaped pellets were obtained.

## **2.2 Characterization of materials**

The main paragraph text follows directly on here. Powder diffraction patterns were obtained with Cu K $\alpha$  ( $\lambda$  = 1.5418 Å) radiation in a reflection geometry on a diffractometer operating at 40 KV and 30 mA equipped with a position sensitive detector. The lattice parameters were obtained by a least squares refinement of the data in the 2θ range of 10°–70° with the assistance of a Rietveld refinement program [\[22](#page-9-10)].

Room temperature Hall coefficients  $(R_H)$  were measured using a Hall effect measurement system (HT-Hall, ResiTest 8300, Toyo Corporation). Carrier density  $(n<sub>H</sub>)$  was obtained by  $n_H = I/(eR_H)$ , and carrier mobility ( $\mu$ <sub>H</sub>) was calculated using the relationship  $\mu_H = \sigma R_H$ , where  $\sigma$  is the electrical conductivity obtained from ZEM-3 instrument and *e* is the free electron charge. Microstructures were investigated by transmission electron microscopy (HRTEM, JEM-2100F).

#### **2.3 Characterization of TE properties**

The obtained spark plasma sintering (SPS) processed pellets were cut into bars with dimensions of  $12 \times 3 \times 3$  mm<sup>3</sup> for the simultaneous measurement of the Seebeck coefficient and electrical conductivity using an Ulvac Riko ZEM-3 instrument under a low-pressure inert gas (He) atmosphere from room temperature to 520 K. The uncertainties in the Seebeck coefficient and electrical conductivity measurement were  $\pm 8\%$  and  $\pm 10\%$ , respectively. The SPSed pellets were cut and polished into a round shape of  $\Phi$  15 mm  $\times$  2 mm for thermal diffusivity (*D*) and specific heat capacity  $(C_p)$ measurements in a Netzsch LFA457 MicroFlash™ instrument. The samples were coated with a thin layer of graphite to minimize errors from the emissivity method. The density (ρ) was determined using the dimensions and mass of the sample. Thermal conductivity  $(\kappa_{tot})$  can be derived from the relationship  $\kappa_{tot} = D \times C_{p \times \rho}$ . The uncertainty in the thermal conductivity was estimated to be about  $\pm 10\%$ , considering all the uncertainties from *D*,  $\rho$  and  $C_p$ . The combined uncertainty for all measurements involved in the calculation of ZT was less than 15%. Unless otherwise noted, all the properties described in this study were measured perpendicular to the sintering pressure direction.

#### **3 Results and discussion**

Figure [1](#page-2-0) shows the XRD patterns of single Sn-doped and CuI/Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$ . All the main peaks of the samples can be well indexed to the phase of  $Bi<sub>2</sub>Te<sub>3</sub>$  (JCPDS ICDD 2002 #89-2009) [\[23\]](#page-9-11), and no obvious impurity phases were observed. No significant peak shifts were observed within the composition range for either the Sn or CuI/Sn doped samples. The lattice parameter  $a(4.37(1)$  Å) was almost the same for all compounds, while the lattice parameter *c* was 30.48(1) Å for the pristine compound, 30.49(1) Å for 1 at.% Sn-added, 30.48 (1) Å for 1 at.% Sn-substituted, 30.45(1) Å for 1 at.% CuI/Sn-added and 30.34(1) Å for 1 at.% CuI/Snsubstituted  $Bi<sub>2</sub>Te<sub>3</sub>$ . These values slightly decreased with CuI /Sn co-doping.

According to the Lotgering method [\[24\]](#page-9-12), the relative peak intensity ratio of the (006)–(015) peaks,  $I_{(006)}/I_{(015)}$ , was about∼0.18 for the Sn-doped Bi<sub>2</sub>Te<sub>3</sub> sample and~0.10



<span id="page-2-0"></span>**Fig. 1 a** Powder XRD patterns for Sn<sub>x</sub>Bi<sub>2</sub>Te<sub>3</sub>and Bi<sub>2−x</sub>Sn<sub>x</sub>Te<sub>3</sub> ( $x=0.0$ , 0.01, 0.03). **b** Powder XRD patterns for (CuI+1/2Sn)*xBi*<sub>2</sub>Te<sub>3</sub> and Bi<sub>2−*x*</sub>(CuI+1/2Sn)<sub>*x*</sub>Te<sub>3</sub> ( $x$  = 0.0, 0.01, 0.03), **c** lattice parameter *a*, **d** lattice parameter *c* 

for CuI/Sn co-doped  $Bi_2Te_3$ , indicating no obvious preferred orientation in these samples. All the samples showed a dense structure (the relative density reached 98%), thus we paid little attention to the porosity and anisotropy when analyzing the thermoelectric properties.

Hall measurements were carried out at room temperature to estimate the carrier concentration of different doping types and content in  $Bi<sub>2</sub>Te<sub>3</sub>$ . The resulting carrier concentration  $n_H$  and mobility  $\mu_H$  are listed in Table [1](#page-2-1). First of all, we noted that the carrier concentration in the undoped  $Bi<sub>2</sub>Te<sub>3</sub>$ samples was approximately  $n \approx 1.2 \times 10^{19}$  cm<sup>-3</sup>. When doping with CuI, the carrier concentration slightly increased because parts of the Cu and I atoms dissolved into the matrix as the electron donors ( $n \approx 5.9 \times 10^{19}$  cm<sup>-3</sup>). Generally, Sn is known to act as an electron acceptor by the substitution of divalent  $\text{Sn}^{2+}$  for trivalent  $\text{Bi}^{3+}$  in  $\text{Bi}^{3-}$ , thus compensating for the electron carriers. The concentration of holes from Sn doping surpassed that of majority carriers in pristine  $Bi_2Te_3$  by increasing the amount of Sn to 3 at.%, and noticeable changes in the conduction type were detected. The 3 at.% Sn-doped samples (both substituted and intercalated Bi<sub>2</sub>Te<sub>3</sub>) show *p*-type conduction ( $p \approx 2 \times 10^{19}$  cm<sup>-3</sup>for  $Sn_{0.03}Bi_2Te_3$ , and  $p \approx 3 \times 10^{19}$  cm<sup>-3</sup> for  $Sn_{0.03}Bi_{1.97}Te_3$ ). The samples with low Sn contents showed complicated behavior.

<span id="page-2-1"></span>**Table 1** Properties of Sn-doped, CuI-doped and CuI/Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$  at 300 K compared with pristine  $Bi<sub>2</sub>Te<sub>3</sub>$ 

| Sample  | Type        | Carrier concen-<br>tration<br>$(10^{19} \text{ cm}^{-3})$ | Mobility<br>$\rm (cm^2 V^{-1} s^{-1})$ |
|---|-------------|---|--|
| $Bi_2Te_3(CuI)_xBi_2Te_3$                             | n           | 1.2   | 355                                    |
| $x = 0.01$  | n           | 5.9   | 84.7                                   |
| $(Sn)_x Bi_{2-x}Te_3:Sn-added$                        |             |   |  |
| $x = 0.01$  | n           | 3.9   | 94.2                                   |
| $x = 0.03$  | p           | 2.4   | 102.4                                  |
| $(Sn)$ <sub>x</sub> $Bi_{2-x}Te_3$ : Sn-substituted   |             |   |  |
| $x = 0.01$  | n           | 1.1   | 171.7                                  |
| $x = 0.03$  | p           | 3.0   | 29.4                                   |
| $(Cul + 1/2Sn)$ <sub>x</sub> $Bi_2Te_3$ :CuI/Sn-added |             |   |  |
| $x = 0.01$  | n           | 5.3   | 175.7                                  |
| $x = 0.03$  | n           | 9.6   | 90.5                                   |
| $x = 0.05$  | $\mathbf n$ | 16.7  | 60.8                                   |
| $(CuI + 1/2Sn)_{y}Bi_{2-y}Te_{3}:CuI/Sn-substituted$  |             |   |  |
| $x = 0.01$  | n           | 9.2   | 129.2                                  |
| $x = 0.03$  | n           | 13.2  | 81.4                                   |
| $x = 0.05$  | n           | 21.8  | 75.2                                   |

This behavior may be related to a decrease in the amount of electrically active defects presented in the sample upon doping with Sn. The 1 at.% Sn-added sample increased its carrier concentration, indicating that Sn acts as a donor  $(n \approx 3.9 \times 10^{19} \text{ cm}^{-3}$  for Sn<sub>0.01</sub>Bi<sub>2</sub>Te<sub>3</sub>). However, the 1 at.% Sn-substituted sample had little effect on the net carrier concentration ( $n \approx 1.1 \times 10^{19}$  cm<sup>-3</sup> for Sn<sub>0.01</sub>Bi<sub>1.99</sub>Te<sub>3</sub>), and therefore the physical properties. For CuI/Sn co-doped samples, the carrier concentration increases steadily by increasing the amount of CuI/Sn dopant from  $5.3 \times 10^{19}$  cm<sup>-3</sup> to  $16.7 \times 10^{19}$  cm<sup>-3</sup> for the CuI/Sn-added sample, and from  $9.2 \times 10^{19}$  cm<sup>-3</sup> to  $21.8 \times 10^{19}$  cm<sup>-3</sup> for the CuI/Sn-substituted samples. The mobility  $\mu_H$  for CuI/Sn co-doped samples systematically decreased due to the increased scattering between carriers.

We selected Sn due to its unusual effect on the electrophysical properties of  $Bi<sub>2</sub>Te<sub>3</sub>$  due to the formation of a resonance state in the allowed valence band [[17\]](#page-9-6). Another reason for selecting Sn is to promote precipitation of Cu. Since the standard reduction potential of the  $Sn/Sn^{2+}$  couple (0.14 V) is less than that of the  $Cu^+/Cu^0$  couple (0.52 V) [\[25](#page-9-13)], Sn can reduce  $Cu<sup>+</sup>$  ions to  $Cu<sup>0</sup>$  as follows:

 $2Cu^{+} + Sn^{0} \rightarrow 2Cu^{0} + Sn^{2+}$ 

The overall reaction can be written as

 $2CuI + Sn \rightarrow 2Cu + SnI<sub>2</sub>$ 

Therefore, Cu and SnI<sub>2</sub> precipitates form from the reduction of CuI with Sn in a high-temperature solid-state reaction, and the embedded precipitates can act as scattering centers in the CuI/Sn co-doped  $Bi_2Te_3$  system.

The microstructures of the  $(CuI/Sn)_{0.01}Bi_2Te_3$  samples were investigated by HRTEM. As shown in Fig. [2,](#page-3-0) the 1 at.% CuI/Sn co-doped  $Bi_2Te_3$  was heavily nanostructured with various kinds of nanoprecipitates and lattice distortions dispersed throughout the  $Bi<sub>2</sub>Te<sub>3</sub>$  matrix. HRTEM images (Fig. [2](#page-3-0)a, b) show coherently embedded nanoparticles of about 2–5 nm in the bulk matrix. The SAED pattern (Fig. [2](#page-3-0)b inset) taken along the [0001] direction indicates that the matrix possesses a  $Bi<sub>2</sub>Te<sub>3</sub>$  type rhombohedral crystalline structure, and the precipitate regions showed extra atomic ordering (as indicated with open circles). In addition, CuI–Sn co-doped samples can readily identify abundant lattice defects, including dislocations and lattice distortion (Fig. [2c](#page-3-0)). An inverse fast Fourier transform (IFFT) image corresponding to Fig. [2](#page-3-0)d is presented in Fig. [2e](#page-3-0), and it can be used to readily identify abundant dislocations and lattice distortions. The strain introduced by these dislocations is quantitatively analyzed using the geometrical phase analysis (GPA) method. The strain fields are represented by strain



<span id="page-3-0"></span>**Fig. 2 a** TEM images of CuI/Sn co-doped  $Bi_2Te_3$ . **b** HRTEM images depicting nanoprecipitates embedded in the  $Bi<sub>2</sub>Te<sub>3</sub>$  matrix. The inset includes selected area electron diffraction (SAED) performed on vari-

ous areas. **c** HRTEM micrographs of CuI/Sn co-doped Bi<sub>2</sub>Te<sub>3</sub> **d** lattice defects, **e** an IFFT image corresponding to **d**, and **f** strain mapping corresponding to **d**

tensor components  $\varepsilon_{yy}$  as shown in Fig. [2f](#page-3-0). The compressive and tensile stress is observed around the lattice distortion, which is thought to be caused by the co-doping of CuI and Sn elements.

The BF-TEM images of CuI/Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$  are presented in Fig. [3,](#page-4-0) which more clearly shows the presence of two different phases of nanoprecipitates with bright and dark contrast in the  $Bi_2Te_3$  matrix (marked with yellow and red circles). Although it was difficult to determine the actual composition of the nanoprecipitates using energy dispersive X-ray spectroscopy, we speculate that the nanoprecipitates are indeed Sn-I rich phases (marked by yellow circles) and Cu rich phases (marked by red circles). The addition of Cu and SnI<sub>2</sub> as nanoinclusions may introduce a carrier energy filtering effect as observed in other metallic nanoinclusions containing  $Bi_2Te_3$ -based materials [\[18](#page-9-7), [26\]](#page-9-14). These nanosized precipitates in bulk  $Bi<sub>2</sub>Te<sub>3</sub>$  will affect the electrical and thermal transport properties.

Figure [4](#page-5-0) shows the temperature dependence of the thermoelectric properties for Sn-doped and CuI/Sn codoped  $Bi_2Te_3$ . A pristine  $Bi_2Te_3$  sample was also measured to examine the effect of doping on the electronic transport properties. The electrical conductivity at 300 K for  $Bi_2Te_3$  was ~ 307 S cm<sup>-1</sup>. The effect of Sn doping on the electrical conductivity of  $Bi<sub>2</sub>Te<sub>3</sub>$  is more complex, as shown in Fig. [4](#page-5-0)a. Both the substitution of 1 at.% Sn for  $Bi^{3+}$  and addition of 1 at.% Sn in  $Bi_2Te_3$  increased the electrical conductivity, while the electrical conductivity significantly decreased as the content of Sn increased to 3 at.%. These results suggest that Sn acts as a scattering center that disturbs electron conduction. With identical doping amounts, the singly Sn-substituted samples have much higher electrical conductivities than Sn-added samples. In the 1 at.% Sn-substituted sample, the electrical conductivity decreases with increasing temperature  $(\delta \sigma / \sigma)$ δT < 0), following a power law of  $\sigma \propto T^{-3/2}$ . In contrast, the Sn-substituted sample with  $x = 0.03$  and all cases of Sn-added samples displayed non-metallic behavior (δσ/  $\delta$ T > 0). Electrical conductivity decreased following a power law of  $\sigma \propto T^{3/2}$ , indicating that the carriers were predominantly scattered by ionized impurities (alloy disorder). The temperature dependence of the electrical conductivity for (CuI/Sn) co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$  samples is shown in Fig. [4b](#page-5-0). All samples showed typical degenerated semiconductor-like behavior ( $δσ/δT < 0$ ). Electrical conductivity decreased following a power law of  $\sigma \propto T^{-3/2}$ , indicating that the carriers were predominantly scattered by acoustic phonon scattering. No obvious bipolar conduction was observed. The electrical conductivity at room temperature for (CuI/Sn)-added  $Bi<sub>2</sub>Te<sub>3</sub>$  samples showed a slight decrease with increasing (CuI/Sn) fraction. The electrical conductivity values ranged from 2193 to 2079 S cm−1at 300 K. The electrical conductivity at room temperature for (CuI/Sn)-substituted  $Bi<sub>2</sub>Te<sub>3</sub>$  samples showed an increase with increasing (CuI/Sn) content from 1 to 5 at.% and ranged from 2348 to 3797 S  $cm^{-1}$ . The values of electrical conductivity for (CuI/Sn)-substituted samples were larger than those of (CuI/Sn)-added samples. Here,  $\sigma$  is known to depend on the carrier concentration and mobility as shown in the relationship  $\sigma =$  nue, where e is the carrier charge, n is the carrier concentration and  $\sigma$  is the mobility. As shown in Table [1](#page-2-1), the carrier concentration

<span id="page-4-0"></span>**Fig. 3** BF-TEM images of CuI/ Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$  showing two different phases of nanoprecipitate with bright and dark contrast in the  $Bi<sub>2</sub>Te<sub>3</sub>$  matrix (marked with yellow and red circles). (Color figure online)



> Bright contrast : Snl rich precipitate





<span id="page-5-0"></span>**Fig. 4** Thermoelectric properties as a function of temperature for Sndoped  $Bi<sub>2</sub>Te<sub>3</sub>$  and CuI/Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$  a and **b** electrical conductivity (σ), **c** and **d** Seebeck coefficient (*S*), **e** and **f** power factor. Here,

*x*% Sn-A means Sn<sub>x</sub>Bi<sub>2</sub>Te<sub>3</sub>, *x*% Sn-S is Sn<sub>x</sub>Bi<sub>2−*x*</sub>Te<sub>3</sub>, *x*% CuI-Sn-A indicates the  $(CuI + 1/2Sn)_xBi_2Te_3$  sample, and  $x\%$  CuI–Sn–S indicates the  $(CuI + 1/2Sn)$ <sub>*x*</sub>Bi<sub>2−*x*</sub>Te<sub>3</sub> sample

increased greatly as CuI/Sn content increased from 0 to 5 at.%. Figure [4](#page-5-0) c and d show the temperature dependence of the Seebeck coefficients for Sn-doped and CuI/ Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$ , respectively. The observed Seebeck coefficient values of Sn-doped specimens were negative for  $x = 0.01$ . They become positive for  $x = 0.03$ , which is consistent with the signs of the Hall measurements. This may be associated with the onset of the intrinsic behavior of Sn as a hole donor. According to conventional theory, the larger carrier concentration will lead to a smaller Seebeck coefficient. The magnitude of the Seebeck coefficient of the Sn-substituted sample decreased with increasing Sn content, whereas that of the Sn-added sample increased. These results are consistent with the trends of the Hall measurements. The Seebeck coefficients for CuI/Sn-codoped samples were all negative for all the samples over the whole temperature range, indicating *n*-type conductors. This result is consistent with the negative values of the Hall measurement. As the (CuI/Sn)-co-doped amount increased from 1 to 3 at.%, the values of the Seebeck coefficients decreased due to the increased carrier concentration. As mentioned above, the carrier concentration increased significantly as the CuI/Sn co-doping content increased, thus causing a decrease in the Seebeck coefficient. All the samples showed similar temperature dependence of the Seebeck coefficient. The Seebeck coefficient values of all CuI/Sn co-doped samples exhibited a moderate decrease with increasing temperature. The temperature-dependent power factors  $(S^2\sigma)$  as a function of temperature for Sn-doped and CuI/Sn co-doped  $Bi_2Te_3$ are shown in Fig. [4e](#page-5-0) and f, respectively. The power factor of the Sn-doped samples decreased with increasing doped Sn amount except around room temperature. The highest power factors of ~ 27.56 and ~ 26.11  $\mu$ W cm<sup>-1</sup> K<sup>-2</sup> at 325 K were achieved for 1 at.% Sn-substituted and 1 at.% Sn-added  $Bi<sub>2</sub>Te<sub>3</sub>$ , respectively. The power factor for the CuI/Sn co-doped  $Bi<sub>2</sub>Te<sub>3</sub>$  samples decreased with increasing doping content. A maximum power factor of  $\sim$  35.4  $\mu$ W cm<sup>-1</sup> K<sup>-2</sup> at 300 K was achieved for the 1 at.% CuI/ Sn-added sample. This value is  $\sim$  50% larger than that of

the pristine Bi<sub>2</sub>Te<sub>3</sub> ( ~ 22.4 µW cm<sup>-1</sup> K<sup>-2</sup> at 300 K) and the 1 at.% CuI/Sn-substituted  $Bi_2Te_3$  sample ( ~ 22.1 µW cm<sup>-1</sup>  $K^{-2}$  at 300 K).

To understand the effect of co-dopants, we compared the room-temperature Seebeck coefficient versus carrier concentration with the theoretical Pisarenko line  $[20, 27]$  $[20, 27]$  $[20, 27]$  $[20, 27]$ . The data point for pristine  $Bi_2Te_3$  fell on the Pisarenko line, demonstrating the validity of the adopted physical model. Except for the Sn-added samples, all samples showed higher Seebeck values than predicted by the Pisarenko line. As show in Fig. [5](#page-6-0)a, the Sn-substituted  $Bi<sub>2</sub>Te<sub>3</sub>$  samples had much higher Seebeck coefficients than predicted by the Pisarenko relation, which was reported to arise from the resonant levels inside the valence band introduced by the Sn dopant [\[17,](#page-9-6) [28](#page-9-16)]. The Seebeck coefficients of Sn-substituted  $Bi_2Te_3$  were very similar to previous values [[17](#page-9-6)]. It was also revealed that CuI and Sn co-doped  $Bi_2Te_3$  have slightly higher Seebeck coefficients at room temperature than predicted by the Pisarenko plot. If Sn or CuI is only a charge carrier regulator (pure dopant) in CuI/Sn co-doped  $Bi_2Te_3$ , then (CuI/ Sn)-added and (CuI/Sn)-substituted  $Bi_2Te_3$  should have the same Seebeck coefficients. However, this is not the case for the experimentally obtained results as shown in Fig. [5a](#page-6-0). The Seebeck coefficients for the CuI and CuI/Sn-containing samples are high, as shown in Fig. [5a](#page-6-0), indicating a higher effective mass, which is beneficial for the thermoelectric performance. We simply plotted the room-temperature power factor as a function of electron concentration, as shown in Fig. [5](#page-6-0)b. It is apparent that the CuI/Sn-containing samples showed significantly increased power factors, and the maximum values reached ~43  $\mu$ W cm<sup>-1</sup> K<sup>-2</sup> for the *x* = 0.01 sample. The optimal electron concentrations for the power factor ranged from  $5 \times 10^{19}$  cm<sup>-3</sup> to  $6 \times 10^{19}$  cm<sup>-3</sup>.

A comparison of the temperature dependent thermoelectric properties for different dopants (CuI-doping, Sn-doping, and CuI/Sn co-doping) with 1 at.% doping concentration in  $Bi<sub>2</sub>Te<sub>3</sub>$  is shown in Fig. [6.](#page-7-0) At identical doping fractions, the co-doping of CuI and Sn resulted in a higher improvement in the electrical conductivities due to the high carrier mobility and carrier concentration.

<span id="page-6-0"></span>**Fig. 5** Room-temperature **a** Seebeck coefficients (S) and **b** power factors as a function of carrier concentration (n) for  $Bi<sub>2</sub>Te<sub>3</sub>$  with different dopants. The solid lines represent the Pisarenko relationships with different effective masses





<span id="page-7-0"></span>**Fig. 6** The temperature dependence of **a** electrical conductivity (σ), **b** Seebeck coefficient (*S*), **c** power factor, and **d** thermal conductivity of *x*% CuI/Sn co-doped Bi<sub>2</sub>Te<sub>3</sub> ( $x=0.01, 0.03, 0.05, 0.07,$  and 0.10) including that for pristine Bi<sub>2</sub>Te<sub>3</sub>

Compared to pristine  $Bi_2Te_3$ , CuI-doping showed a donor effect and led to a substantial increase in the carrier concentration, thus increasing the electrical conductivity. As can be seen in Fig. [6b](#page-7-0), the Seebeck coefficient showed a trend opposite to that of the electrical conductivity, which is strongly related to the carrier concentration. All samples with 1 at.% dopant concentration showed negative Seebeck coefficients, indicating that the samples were *n*-type semiconductors. The co-doped sample showed a room temperature Seebeck coefficient of  $-127.13 \mu V K^{-1}$ , which is lower than that of the CuIdoped sample  $(S \sim -138.07 \mu V K^{-1})$ . The temperaturedependent power factors  $(S^2\sigma)$  are shown in Fig. [6](#page-7-0)c as a function of temperature for Sn-doped, CuI-doped, and CuI/Sn co-doped samples. One can see that at the same doping level ( $\sim$  1 at.%), the power factors of CuI/Sn codoped  $Bi<sub>2</sub>Te<sub>3</sub>$  increased relative to single dopant doped  $Bi<sub>2</sub>Te<sub>3</sub>$  and pristine  $Bi<sub>2</sub>Te<sub>3</sub>$  over a very wide temperature range from 300 to 525 K. We evaluated the temperature dependences of the total ( $\kappa_{\text{tot}}$ ) and lattice ( $\kappa_{\text{latt}}$ ) thermal

conductivity for Sn-doped, CuI-doped, and CuI/Sn codoped  $Bi<sub>2</sub>Te<sub>3</sub>$ , as shown in Fig. [6d](#page-7-0). As seen in Fig. [6](#page-7-0)d, the  $\kappa_{\text{tot}}$  for all doped samples is lower than that of the pristine sample. The  $\kappa_{\text{tot}}$  for pristine and Sn-doped Bi<sub>2</sub>Te<sub>3</sub> gradually increased with increasing temperature. In the case of CuI-doped and CuI/Sn co-doped compounds, a slight upward curvature of  $\kappa_{tot}$  with temperature was observed at higher temperatures over 400 K. This behavior generally occurs in materials where *n*-and *p*-type carriers coexist [[29](#page-9-17)]. The electronic contribution to the thermal transport is expected to be higher in the CuI/Sn co-doped sample due to the relatively high electrical conductivity values observed in the CuI/Sn co-doped compounds. However, the  $\kappa_{\text{tot}}$  of CuI/Sn co-doped sample was lower than that of single CuI-doped Bi<sub>2</sub>Te<sub>3</sub> ( $\kappa_{\text{tot}}$  ~ 1.44 W m<sup>-1</sup> K<sup>-1</sup> for  $(CuI + 1/2Sn)_{0.01}Bi_2Te_3$  and  $\kappa_{tot} \sim 1.34$  W m<sup>-1</sup> K<sup>-1</sup> for  $(CuI)_{0.01}Bi_2Te_3$ ). The reduction in the  $\kappa_{tot}$  for the CuI/Sn co-doped samples was mainly ascribed to the decreased lattice thermal conductivity. The total thermal conductivity ( $\kappa_{\text{tot}}$ ) can be expressed as the sum of the lattice ( $\kappa_{\text{latt}}$ )



<span id="page-8-7"></span>**Fig. 7** Figure of merit of the  $Bi_2Te_3$  with different dopants as a function of measurement temperature

and electrical thermal conductivity ( $\kappa_{elec}$ ).  $\kappa_{elec}$  is proportional to the electrical conductivity according to the Wiedemann–Franz law ( $\kappa_{\text{elec}} = L_{\sigma}T$ , where L is the Lorenz number ( $L = 1.54 \times 10^{-8}$  V<sup>2</sup> K<sup>-2</sup>) [[30](#page-9-18)], σ is the electrical conductivity and T is absolute temperature). As seen from Fig. [6d](#page-7-0),  $\kappa_{\text{latt}}$  of Sn-doped Bi<sub>2</sub>Te<sub>3</sub> decreased by ~ 50% over the whole measured temperature range (300 K–525 K) compared to pristine Bi<sub>2</sub>Te<sub>3</sub> ( $\kappa_{\text{latt}}$  ~ 1.44 W m<sup>-</sup>1 K<sup>-1</sup> at 300 K). A further decrease in lattice thermal conductivity of CuI/Sn co-doped samples was observed, which may originate from an increase in point defect scattering after doping, as shown in the TEM analysis.

Figure [7](#page-8-7) presents the temperature dependence of the dimensionless figure of merit (ZT) calculated from the combination of the electrical and thermal transport properties. The ZT values of all doped samples were significantly enhanced compared to pristine  $Bi_2Te_3$  (ZT ~ 0.42 at room temperature). The ZT values of doped samples at room temperature were slightly changed by the added dopants. However, Sn-doping significantly increased the ZTs of  $Bi<sub>2</sub>Te<sub>3</sub>$  in the low-temperature range ( $>325$  K), while the enhancement is marginal at elevated temperature. Compared to Sn-doped  $Bi<sub>2</sub>Te<sub>3</sub>$ , the ZT values of CuI-doped and CuI/Sn co-doped samples showed moderate temperature dependence over a wide temperature range (300 K–525 K). The maximum ZT value  $\sim$  1.23 at 418 K was higher than that of Sn-doped  $Bi_2Te_3$  ( ~ 0.88) and CuI-doped  $Bi_2Te_3$  $(-1.12)$ . As shown in Fig. [7](#page-8-7), co-doping of Sn and CuI causes an increase in the ZT in the mid temperature regions, which is probably due to the synergistic action of CuI and Sn. Our results suggest that further efforts to use co-dopant as an additive in bismuth telluride-based alloys would be promising for the development of highperformance *n*-type thermoelectric materials.

## **4 Conclusions**

Co-doping effects of CuI and Sn on the thermoelectric properties of the  $Bi<sub>2</sub>Te<sub>3</sub>$  matrix were investigated. Nanoprecipitates of the Cu and SnI-rich phase were generated by the reduction of CuI with Sn in the  $Bi<sub>2</sub>Te<sub>3</sub>$  matrix. Numerous distinctive microstructures were revealed by TEM observation for the CuI/Sn co-doped samples, suggesting that such a bulk nanocomposite structure would be highly effective for reducing the thermal conductivity while maintaining high electrical conductivity. CuI/Sn co-doped  $Bi_2Te_3$  showed a distinctly enhanced ZT value of 1.24 at 425 K, and the average ZT value ( $ZT_{\text{ave}} \sim 1.02$ ) at 300–525 K was clearly higher than that in Sn-doped  $Bi_2Te_3$  ( $ZT_{ave}$  ~ 0.54) and CuI-doped  $Bi_2Te_3$  ( $ZT_{ave}$  ~ 0.98). Overall, we showed that significant progress in the thermoelectric performance of n-type  $Bi<sub>2</sub>Te<sub>3</sub>$ can be achieved by employing a third element as a co-dopant with CuI to promote the precipitation of nanoinclusions.

**Acknowledgements** This research was supported by Nano Material Technology Development Program through the National Research Foundation of Korea (NRF) funded by the Ministry of Education, Science and Technology (NRF-2011-0030147). M.K.H. was supported by RP-Grant 2016 of Ewha Womans University.

#### **Compliance with ethical standards**

**Conflict of interest** There are no conflicts to declare.

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