

# Piezoelectric grain-size effects of BaTiO<sub>3</sub> ceramics under different sintering atmospheres

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**Abstract** Two groups of barium titanate (BaTiO<sub>3</sub>) ceramics with high piezoelectric coefficient ( $d_{33}$ ) have been successfully fabricated by the conventional solid-state reaction technique under different sintering atmospheres. The influences of sintering atmosphere on piezoelectric grain-size effects were systematically investigated. It was found that  $d_{33}$  first increases then decreases with the increase of grain size ( $g$ ) for both two groups of ceramics. However, the  $d_{33}$  value reaches the maxima (501 pC/N) at  $g = 1.13 \mu\text{m}$  for the samples sintered under the air sintering atmosphere (BaTiO<sub>3</sub>-Air). The samples sintered under the oxygen atmosphere (BaTiO<sub>3</sub>-O<sub>2</sub>) exhibit a large  $d_{33}$  (>450 pC/N) plateau at  $g$  from 0.98 to 7.30  $\mu\text{m}$ . The experimental results indicated that the piezoelectric grain-size effects of BaTiO<sub>3</sub> ceramics were strongly affected by the sintering atmosphere. Related mechanisms may be attributed to the variations of the domain configuration under different sintering atmospheres.

## 1 Introduction

BaTiO<sub>3</sub> ceramics are historically the first polycrystalline piezoelectric materials and extensively used as piezoelectric actuators, sensors, and transducers [1–4]. During past

several decades, BaTiO<sub>3</sub> ceramics have been believed to exhibit modest piezoelectric activity, with  $d_{33}$  values of approximately 191 pC/N, which were inferior to lead zirconate-titanate [5–7]. However, recent studies revealed that amazing high-performance BaTiO<sub>3</sub> ceramics can be obtained by means of optimizing raw materials, stoichiometry and processing technique. High  $d_{33}$  values (486 pC/N, 519 pC/N and 788 pC/N, respectively) have recently been obtained in BaTiO<sub>3</sub> ceramics prepared by solid-state reaction with ordinary BaCO<sub>3</sub> and TiO<sub>2</sub> raw powers, two-step sintering using hydrothermally synthesized BaTiO<sub>3</sub> fine power and template grain growth technique, respectively [9–12]. These steps forward bring great hope that BaTiO<sub>3</sub>-based ceramics might be revitalized as a popular lead-free piezoelectric material with the important advantage of being low in cost.

A systematic examination of the literature reveals the existence of a puzzling issue, wherein the reported behaviors of the BaTiO<sub>3</sub> ceramics are not unique but display a heterogeneous relationship between the piezoelectric properties and the microstructure [13–15]. Similarly to the well-known dielectric grain-size effects, piezoelectric grain-size effects have been studied by several investigators in the past few years, which the BaTiO<sub>3</sub> ceramics display an increase in  $d_{33}$  with a decreasing average  $g$ , passing through a maximum when  $g \sim 1.0 \mu\text{m}$  and then decreasing with a further reduction of  $g$  [16–22]. Nevertheless, in recent study, other BaTiO<sub>3</sub> ceramics display entirely different piezoelectric behaviors, where the change of  $d_{33}$  as a function of  $g$  does not obey the rule suggested by the piezoelectric grain-size effects [23]. Instead, relatively high  $d_{33}$  value are observed in coarse-grained BaTiO<sub>3</sub> ceramics with  $g$  values large than 10  $\mu\text{m}$  and up to several tens of micrometers [9, 12, 23–25]. These differences demonstrate that previous cognitive on piezoelectric grain-size effects of BaTiO<sub>3</sub> ceramics

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is insufficient [9, 20–24]. Further systematic investigations are necessary to clarify the underlying mechanism.

On the other hand, it is widely accepted that the preparation condition is one of the most important factors that affects the piezoelectric properties of BaTiO<sub>3</sub> ceramics, as it will introduce different defect levels into the ceramics, which could greatly affect the domain configurations and weaken the domain wall movement [12–18, 23]. Considering the point defects tend to migrate to the grain boundaries, the pinning effects may be sensitive to fabrication process [9, 24–28]. This may be an important reason for the different piezoelectric grain-size effects reported by different investigators [12, 26–32]. In previous reports, the effects of different preparing processes on the piezoelectric grain-size effects have been systematically studied [9, 16, 22–26]. However, as an important method to control defect levels of the ceramics, systematic investigations on the sintering atmospheres dependence of domain configurations and piezoelectric properties in BaTiO<sub>3</sub> ceramics are still rare. Therefore, in this work, we attempted to introduce different defect levels into BaTiO<sub>3</sub> ceramics by fabricating two groups of ceramics under air and oxygen sintering atmosphere by the conventional solid-state reaction. The relationships between piezoelectric properties and microstructures for the two groups of ceramics were systematically examined. Possible mechanisms that lead to the different piezoelectric grain-size effects were investigated.

## 2 Experimental procedure

BaTiO<sub>3</sub> powders were prepared by the conventional solid-state reaction technique, starting from properly choosing the raw materials of commercial BaCO<sub>3</sub> powder (purity ≥99.0%, Sinopharm Chemical Reagent Co. Ltd.) and TiO<sub>2</sub> powder (purity ≥99.8%, Xiantao Zhongxing Electronic Material Co. Ltd.). The preparation procedures are basically the same as those in previous studies [7, 13, 18, 23]. The raw materials were weighed according to the stoichiometric ratio and ball-milled in ethanol for 12 h on a planetary ball mill. The milled slurry mixture was dried and ground using an agate mortar and pestle. The powder mixture was calcined at 1050 °C for 4 h, followed by a second ball-milling in ethanol procedure for 12 h. This powder was mixed with a 0.5 wt% polyvinyl alcohol (PVA) binder, and pressed into small disks (15 mm in diameter and 1.5 mm in thickness) at 200 MPa. The PVA binder was then burned out at 650 °C for 0.5 h [13, 23]. Finally, BaTiO<sub>3</sub> ceramics were sintered at different temperatures (from 1190 to 1450 °C) and under different sintering atmospheres (air environment and oxygen environment, with oxygen rate is 6 ml/min) for 2 h.

The density of the ceramics was measured by the Archimedes method. For piezoelectric properties characterization, the ceramic specimens were coated with silver paint on the top and bottom surfaces and fired at 575 °C for 20 min. Poling was carried out at 80 °C in silicon oil under 5.0 kV/mm for 30 min. Measurements of the piezoelectric properties were taken out after 24 h. The  $d_{33}$  value was measured using a Berlucourt-type  $d_{33}$  meter (YE 2730 A). The microstructure and domain configuration of the BaTiO<sub>3</sub> ceramics were examined using a scanning electron microscope (SEM, JEOL JSM6460), based on which the average grain size ( $g$ ) and domain width ( $w$ ) were calculated.  $g$  and  $w$  were measured as follows: First, four straight lines connecting two diagonal lines; and two straight lines across midpoint were drawn in the micrograph. Second, the total length of the four straight lines was measured using the scale and the total grain number was calculated. Finally, the total length was divided by the total grain number to obtain the average  $g$ . Several graphs were plotted to improve the accuracy. For the microstructure and domain configuration characterization, the poled specimens were mirror-polished and chemically etched for 10 s in an aqueous solution of 5% HCl with a small amount of HF (3 drops of HF: 20 ml HCl solution).

## 3 Results and discussion

The relative density ( $\rho_0$ ) of the two groups of BaTiO<sub>3</sub> ceramics sintered under different sintering atmospheres and different temperature conditions are listed in Table 1. Relative density was calculated using the theoretical density of 6.017 g/cm<sup>3</sup> for the pure BaTiO<sub>3</sub> ceramics [15–17]. As shown, for the BaTiO<sub>3</sub> ceramics sintered at temperatures above 1230 °C, the  $\rho_0$  of both groups of specimens could reach nearly 98%. Further enhancing the

**Table 1** Room temperature physical properties of BaTiO<sub>3</sub> ceramics sintered different sintering atmospheres and different temperature conditions

Sintering temperature (°C)	BaTiO <sub>3</sub> -Air		BaTiO <sub>3</sub> -O <sub>2</sub>	
	$\rho_0$ (%)	$d_{33}$ (pC/N)	$\rho_0$ (%)	$d_{33}$ (pC/N)
1190	95.4	275	95.1	244
1210	97.9	501	96.0	465
1230	98.0	485	97.9	495
1250	97.9	465	97.9	499
1270	97.6	346	98.0	410
1300	97.5	318	97.7	356
1350	97.6	307	97.8	344
1400	97.7	292	97.8	313
1450	97.8	303	97.7	309

sintering temperature cannot improve the  $\rho_0$  value. However, the densification temperatures are different for each group specimens. The relative density of BaTiO<sub>3</sub>-Air specimens is higher than 96% when sintering temperature is above 1190 °C. While for BaTiO<sub>3</sub>-O<sub>2</sub> specimens, the sintering temperatures have to be increased to 1230 °C to get specimens with relative density higher than 96%.

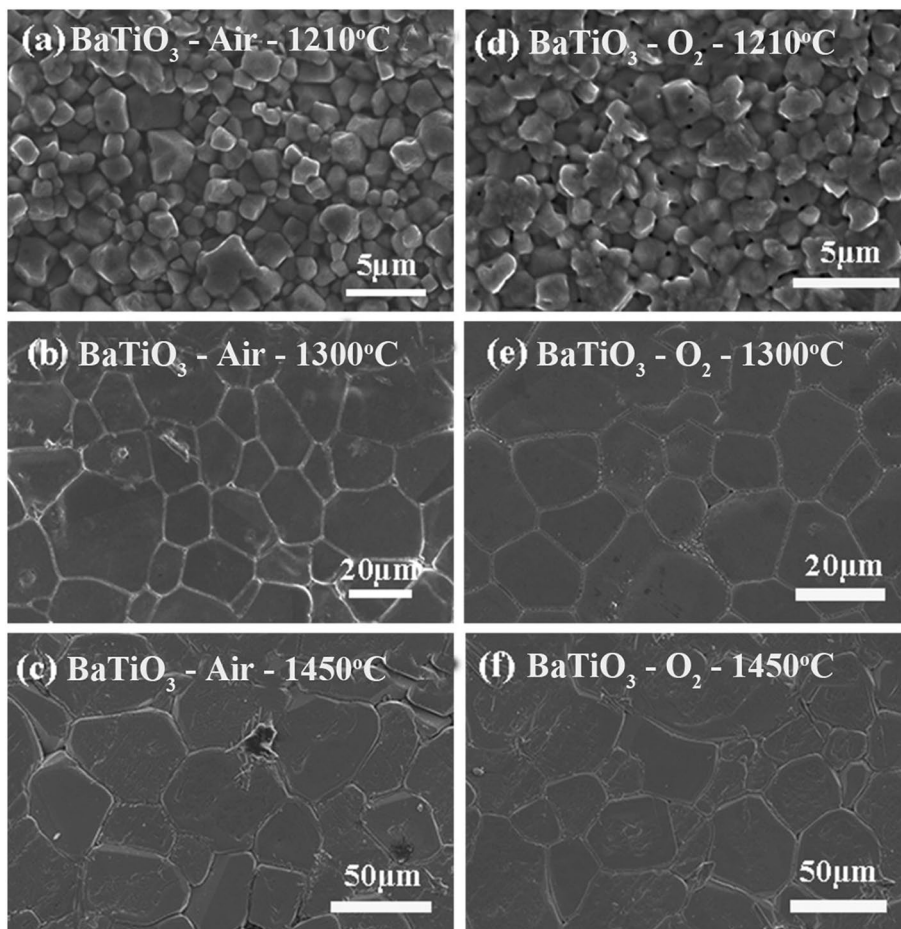
The dependence of the  $d_{33}$  value on the sintering temperature is also shown in Table 1. It could be found that for both groups of specimens, the  $d_{33}$  values firstly increase then decreases with the increase of sintering temperature. The  $d_{33}$  values increased significantly above 1190 °C for BaTiO<sub>3</sub>-Air and BaTiO<sub>3</sub>-O<sub>2</sub> atmosphere. The increase of relative density may be one important reason. High  $d_{33}$  value ( $\approx 500$  pC/N) can be obtained in both groups of BaTiO<sub>3</sub> ceramics. However, there are some differences in detail. For the BaTiO<sub>3</sub>-Air specimens, the  $d_{33}$  value reaches maximum values of 501 pC/N at 1210 °C. While for the BaTiO<sub>3</sub>-O<sub>2</sub> specimens, the highest  $d_{33}$  value of 499 pC/N is obtained at the sintering temperature of 1250 °C. In addition, below 1230 °C the BaTiO<sub>3</sub>-Air ceramics exhibit larger  $d_{33}$  values than BaTiO<sub>3</sub>-O<sub>2</sub> ceramics at the same sintered temperature.

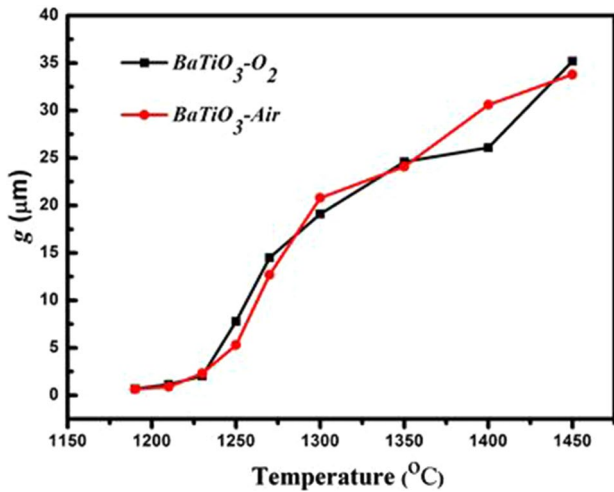
While above 1230 °C, BaTiO<sub>3</sub>-O<sub>2</sub> ceramics exhibit larger  $d_{33}$  values.

The piezoelectric properties are considered to be closely related to the microstructure of the BaTiO<sub>3</sub> ceramics in the previous study [4, 7, 18–20]. Figure 1 shows SEM images of two groups of various BaTiO<sub>3</sub> ceramics sintered under different temperature and different sintering atmosphere conditions. As shown, both groups of ceramics exhibit similar microstructure with uniform  $g$  distribution, although the ceramics sintered under different sintering atmospheres. The relationship between sintering temperature and  $g$  under different sintering environment is shown in Fig. 2. It can be seen that for all the two groups of BaTiO<sub>3</sub> ceramics, the  $g$  increases with the increase of sintering temperature. The  $g$  can be reach over 30  $\mu\text{m}$  at the highest sintering temperature of 1450 °C. At the same sintering temperature, both groups of BaTiO<sub>3</sub> ceramics exhibited similar  $g$ , which demonstrates that the sintering atmospheres have less influence on grain growth of BaTiO<sub>3</sub> ceramics.

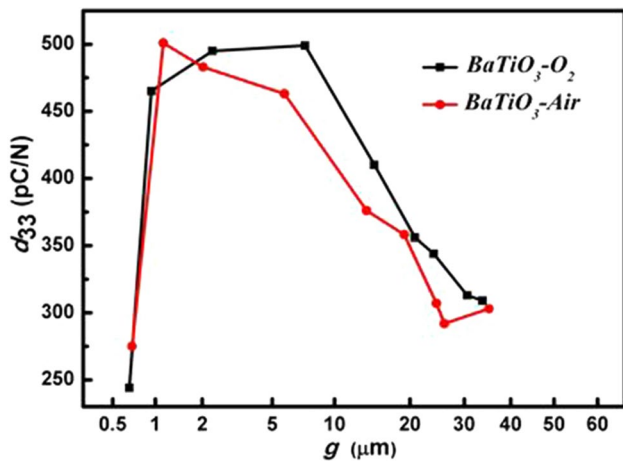
Figure 3 presents the change in  $d_{33}$  with  $g$  measured at room temperature in all the poled BaTiO<sub>3</sub> ceramics. It is clear that  $d_{33}$  value was strongly affected by  $g$ . As can be seen, both of the groups of the ceramics exhibit

**Fig. 1** SEM images of BaTiO<sub>3</sub> ceramics sintered under different temperature and different sintering atmosphere conditions





**Fig. 2** Temperature dependences of grain size of BaTiO<sub>3</sub> ceramics under different sintering atmospheres



**Fig. 3** Grain size dependences of  $d_{33}$  of BaTiO<sub>3</sub> ceramics under different sintering atmospheres

similar trends of  $d_{33}$  with  $g$ , the  $d_{33}$  value first increases then decreases with the increase of  $g$ . The result is generally consistent with the results obtained in previous investigations [6, 8–12]. However, differences could also be observed between the ceramics sintered under the different sintering atmospheres. Firstly, for the BaTiO<sub>3</sub>-Air ceramics, the largest  $d_{33}$  value of 501 pC/N obtained at  $g = 1.13 \mu\text{m}$ . While for the BaTiO<sub>3</sub>-O<sub>2</sub> ceramics, the maximum piezoelectric constant has been migrated in the direction of large grain. The maximum  $d_{33}$  value of 499 pC/N is obtained at  $g = 7.30 \mu\text{m}$ . Secondly, the  $g$  dependence of  $d_{33}$  exhibits a sharp peak for the BaTiO<sub>3</sub>-Air ceramics. While for the BaTiO<sub>3</sub>-O<sub>2</sub> ceramics, the ceramics exhibit a large  $d_{33}$  (>450 pC/N) plateau at  $g$  from 0.98 to 7.30  $\mu\text{m}$ . Furthermore, it should be noted that when  $g > 2 \mu\text{m}$ , the BaTiO<sub>3</sub>-O<sub>2</sub> ceramics

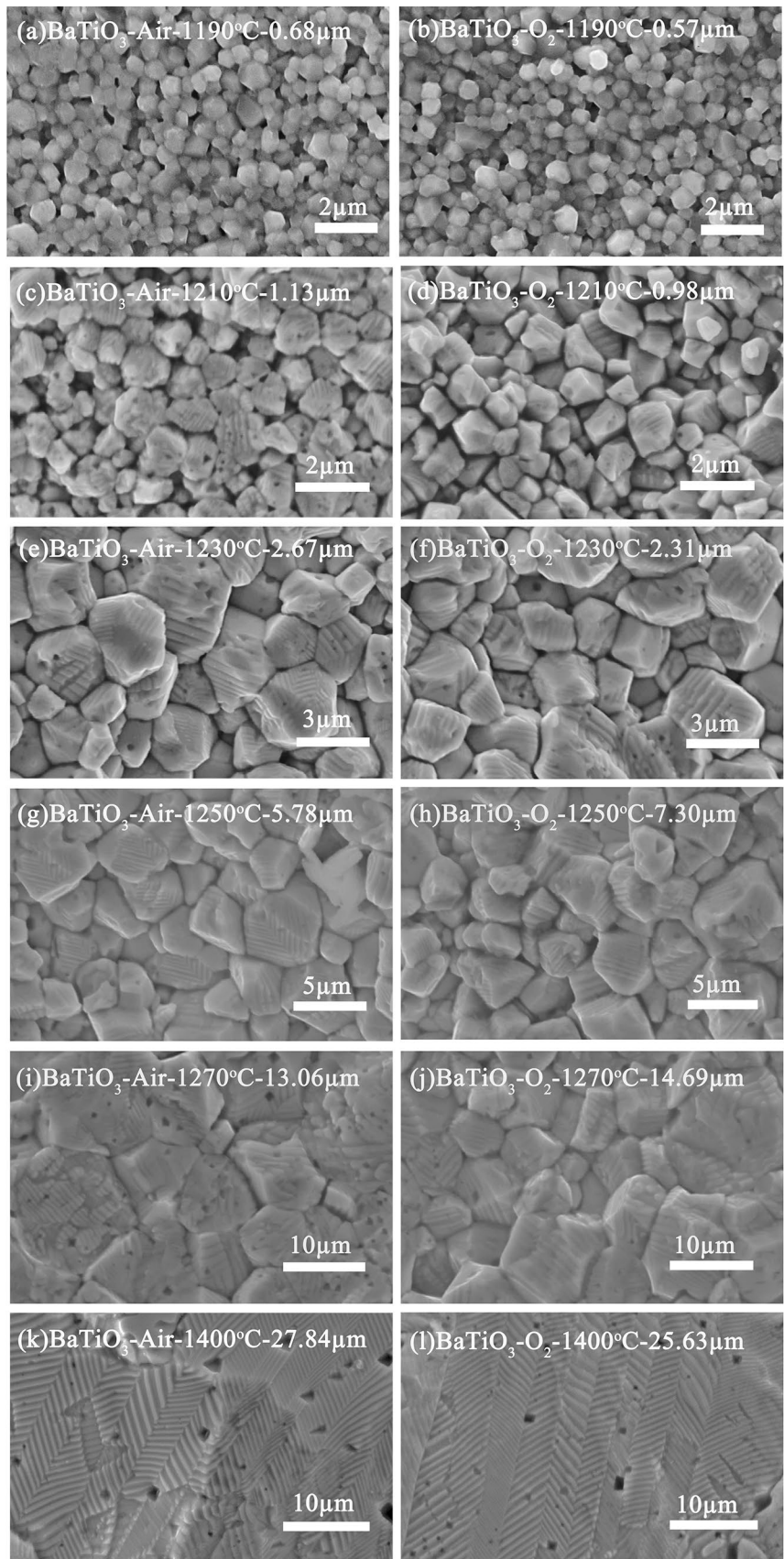
shows the higher  $d_{33}$  value than those BaTiO<sub>3</sub>-Air ceramics. The related mechanism will be discussed later. Below that, it is just reverse. The lower relative density may be responsible for that, as shown in Table 1. Generally, it is considered that the sintering atmosphere has greatly influence on the  $g$  dependence of piezoelectric properties.

It is known that the piezoelectric properties of a piezoelectric ceramics material could be generally resolved into intrinsic and extrinsic contributions. The former originates from the deformation of the unit cell under an external electric or mechanical field, while the latter is mainly due to domain wall movement [5, 6, 12–15]. Obviously, both the piezoelectric grain-size effects are closely related to the extrinsic contributions.

Figure 4 presents SEM images of domain structure observed in the poled BaTiO<sub>3</sub>-Air and BaTiO<sub>3</sub>-O<sub>2</sub> with different sintering temperature. The evolution of the microstructure and domain structure can be clearly seen from these figures. As shown, below 1210 °C, most of the grains are of single domain structure. This may be another reason for the great decrease of  $d_{33}$  values below 1210 °C for BaTiO<sub>3</sub>-Air and BaTiO<sub>3</sub>-O<sub>2</sub> atmosphere. The extrinsic contribution to  $d_{33}$  from the domain wall motion will reduce as the amount of domain walls decrease. Above 1210 °C, stripes and herringbone patterns are recognizable inside the grains. These have been reported to be typical features of the domain configuration of BaTiO<sub>3</sub> ceramics in the tetragonal phase [6, 16, 20–23]. The stripes correspond to the 90° domain patterns, where polarization vectors in adjacent domains adopt a head-to-tail arrangement across the domain boundaries. The physical origin of the formation of 90° domains is considered to be associated with the release of internal stress. The herringbone patterns are the consequence of the combination of two sets of alternating 90° domains [6, 10–12, 20]. Furthermore, it can be found that the domain configuration become more complex with the increase of the  $g$  in both groups of the BaTiO<sub>3</sub> ceramics. The domain patterns of the fine-grained BaTiO<sub>3</sub> ceramics are quite simple, being predominantly stripes. While, for coarse-grained BaTiO<sub>3</sub> ceramics, diverse and very complicated domain patterns are more frequently observed. However, the critical  $g$  for the appearance of the herringbone domain patterns is different. For the BaTiO<sub>3</sub>-Air ceramics, with the fine grain ( $g \approx 1 \mu\text{m}$ ), the domain patterns mainly consist of stripes patterns running across the whole grain, as shown in Fig. 4c. Small amount of herringbone domain patterns could be found with  $g$  larger than 2  $\mu\text{m}$ , shown in Fig. 4e. With increase the  $g$ , more and more herringbone domain patterns are frequently observed. However, for the BaTiO<sub>3</sub>-O<sub>2</sub> ceramics, nearly no herringbone domain patterns could be observed inside the grain until the  $g$  is larger than 7.3  $\mu\text{m}$ .

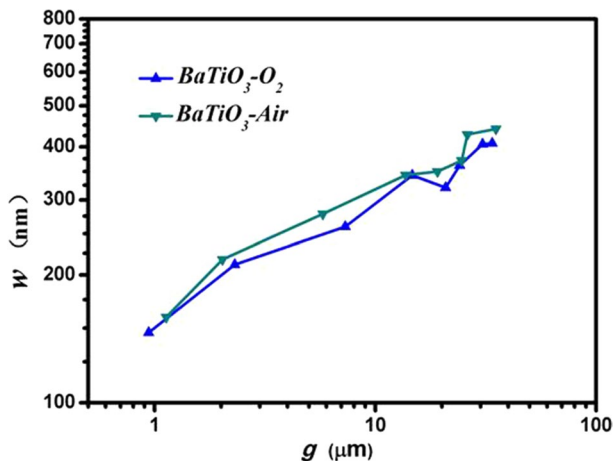


**Fig. 4** Domain structures of poled  $\text{BaTiO}_3$  ceramics under different sintering atmospheres with different sintering temperature



Domain width ( $w$ ) is considered to be an important reason for the piezoelectric grain-size effects of  $\text{BaTiO}_3$  ceramics [4, 6, 17–19]. Small  $w$  leads to high domain density are considered to account for the strong piezoelectric activities in the fine-grain  $\text{BaTiO}_3$  ceramics [9–13, 23]. Figure 5 illustrates the change in the average  $w$  with  $g$  for the various poled  $\text{BaTiO}_3$  ceramics of sintering under different atmospheres. The domain width was calculated by linear intercept method. Each line was vertical through a series of parallel domain. Then the total length of the lines was measured using the scale and the total grain number was counted. The domain width was statistically averaged in more than 150 grains at different locations for each specimen [5, 8, 9, 25–29]. As shown, the average  $w$  decreases with decreasing  $g$  for both groups of  $\text{BaTiO}_3$  ceramics. At the same  $g$ , the  $\text{BaTiO}_3\text{-O}_2$  ceramics exhibits smaller  $w$  than the  $\text{BaTiO}_3\text{-Air}$  ceramics. It may be the reason for the larger  $d_{33}$  values of the  $\text{BaTiO}_3\text{-O}_2$  ceramics compared with that of the  $\text{BaTiO}_3\text{-Air}$  ceramics with the larger  $g$  above  $2\ \mu\text{m}$ . However, the similar  $g$  dependence of  $w$  obviously cannot account for the different piezoelectric grain-size effects mentioned above. This phenomenon demonstrates that the  $w$  is not the only reason for the piezoelectric grain-size effects. Systematic studies of the domain structures are needed.

Interestingly, it seems like that the different piezoelectric grain-size effects under different sintering atmospheres are closely related to the critical  $g$  variations of appearance of herringbone domain patterns. For the  $\text{BaTiO}_3\text{-Air}$  samples, herringbone domain patterns gradually increase with the increase of  $g$  over  $1\ \mu\text{m}$ . At the same time, the  $d_{33}$  gradually decreases with the increase of  $g$  and exhibits a sharp peak at  $g$  near  $1\ \mu\text{m}$ . While for the  $\text{BaTiO}_3\text{-O}_2$  samples, nearly no herringbone domain patterns could be observed inside the grain until the  $g$  is larger than  $7.30\ \mu\text{m}$ . Simultaneously,



**Fig. 5** Grain-size dependences of domain width of  $\text{BaTiO}_3$  ceramics under different sintering atmospheres

the  $d_{33}$  value begins to decrease with the increasing  $g$ . It has been revealed that the herringbone domain patterns have greatly influences on the piezoelectric grain-size effects of  $\text{BaTiO}_3$  ceramics. The motion of a  $90^\circ$  domain wall might be inhibited by the interactions from the neighboring domain walls that are included in the complex and conjoined herringbone domain patterns [28–33]. In such a case, it might be more proper to consider the motion of domain walls as the joint behavior, which will increase the effective inertia mass for an individual domain wall [9, 23–27]. This will reduce the domain walls' response to the external electrical or stress signal, reduce the extrinsic contribution of domain wall motion to piezoelectric activities and lead to the lower  $d_{33}$  value [6, 9, 16–25]. Therefore, the herringbone domain patterns are considered to be the more important factor that decreases the piezoelectric activities in the coarse grains [13, 20]. The experiment results above indicate that the herringbone domain patterns may be also accountable for the decrease of piezoelectric activities in the fine grains.

Furthermore, the mentioned above experiment results also demonstrate the formations of the herringbone domain is closely related to the oxygen defects in the grain [26–32]. It can be easily understand as the oxygen defects will introduce large internal stress in the grain [14, 31–39]. Herringbone domains patterns forms as the stress could not be relieved by the 2-dimensions adjustment. In the fine-grained ceramics, oxygen defects inner the grain can be easily compensated in the oxygen sintering atmosphere due to the small  $g$  and low sintering temperature [32–35]. Therefore, the herringbone domain patterns are greatly decreased [26, 27]. But in the coarse-grained  $\text{BaTiO}_3$  ceramics, the compensation of inner oxygen defects is difficult because of the large  $g$  and high sintering temperature [35–38]. Correspondingly, the oxygen cannot inhibit the formation of herringbone domain patterns any more.

## 4 Conclusions

The influences of sintering atmosphere on piezoelectric grain-size effects were systematically studied in this paper. It is indicated that the appearance of herringbone domain patterns should be responsible for the decreases of the piezoelectric activities in both coarse grains and fine grains. Oxygen atmosphere can delay the formation of the herringbone domain by reducing the oxygen defects, which will decrease the inner stress of the samples. The variations of critical  $g$  for appearance of the herringbone domain patterns might be an important reason for the different piezoelectric grain-size effects under different sintering atmospheres.

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