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Understanding crack growth within the $γ'$ **Fe₄N layer in a nitrided low carbon steel during monotonic and cyclic tensile testing**

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ABSTRACT

Nitriding is a cost-efective method to realize simultaneous improvements in tensile and fatigue properties and resistance to abrasion and corrosion. Previous studies reported that nitriding pure Fe enhances tensile strength by ~ 70% and fatigue limit by \sim 200%. It is due to the increase in surface hardness caused by the formation of γ ′(Fe₄N) and ε(Fe₂₋₃N) nitrogen-containing intermetallic compound phases. However, the intermetallic compound layer is prone to brittle-like cracking. To beter design nitrided steels, it is crucial to identify the crack growth mechanisms via analysis of the microstructural crack growth paths within the \sim 4–6 μ m thick nitride layer. In the current work, we statistically evaluate the crack propagation behavior in the γ ^r Fe₄N layer during monotonic and cyclic tensile deformation in nitrided low-carbon steel (0.1 wt% C). Since nitriding typically results in the formation of columnar grains, the efect of morphology needs to be clarifed. To this end, the steel was shot-peened and subsequently nitrided to promote equiaxed nitride grains morphology (~ 16% increase). Crack growth paths were comparatively evaluated for multiple cracks, and no signifcant efect of nitride morphology was observed. $\{100\}_{\gamma'}$ is the predominant transgranular crack path in the monotonic tensile tested specimen, followed by $\{111\}_{\gamma}$. It is despite the elastic modulus of $\{111\}_{\gamma'}$ < $\{100\}_{\gamma'}$. This contrary behavior is explained by $\{100\}_{\gamma'}$ plane having the lowest surface energy (density functional theory calculations). In the cyclic tensile loaded specimen, experiments revealed that transgranular cracking along ${100}^{\prime}$ (cracking via symmetric dislocation emission) or {111} $_{\gamma'}$ (slip plane cracking) is equally likely.

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GRAPHICAL ABSTRACT

Crack growth paths within the y' Fe₄N layer of nitrided steels

Introduction

Surface hardness is crucial for material life associated with metal fatigue and abrasion [\[1](#page-11-0)-[3\]](#page-11-1). Fatigue life in steels is predominantly controlled by fatigue crack initiation at the surface and subsequent small crack growth in a microstructural scale (within 1 mm) [[3–](#page-11-1)[5\]](#page-11-2). Therefore, surface modifications by thermal and mechanical treatment have been atempted to improve the steel surface $[6-8]$ $[6-8]$. One of the most promising and cost-efective treatments is nitriding, which realizes simultaneous improvements in resistance to fatigue and abrasion owing to a signifcant increase in surface hardness [\[9,](#page-11-5) [10](#page-11-6)]. Earlier studies have reported that nitriding of pure Fe can enhance the ultimate tensile strength [\[11\]](#page-11-7) and fatigue limit [[12–](#page-11-8)[14](#page-11-9)] (failure strength of 10^7 cycles) by ~70% and ~200%, respectively. The increase in surface hardness is owing to the formations of γ' (Fe₄N) and ε (Fe₂₋₃N) nitrogen-containing intermetallic compound phases [\[15](#page-11-10), [16](#page-11-11)].

Yet, there are some challenges in nitrided steels. Britle-like tensile cracking occurs in the intermetallic compound layer or at its interface to the matrix when high stress is loaded [[17](#page-11-12), [18\]](#page-11-13). Furthermore, the pores arising from the degassing of nitrogen (due to

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the decomposition of iron-nitride phases into N_2 gas and Fe at higher temperatures) act as fatigue crack initiation sites [\[17](#page-11-12), [19](#page-12-0)]. Therefore, in addition to crack initiation, fatigue crack growth behavior must also be controlled to endow robust resistance to fatigue. In particular, the small fatigue crack growth behavior in the thin nitride layer with a thickness of around 4–6 µm must be well understood. A crucial feature of the small fatigue crack growth is the microstructural growth path [[20](#page-12-1)]. Specifcally, the crystallographic information enables the identifcation of the crack growth mechanisms [\[21\]](#page-12-2). For instance, when crack growth via symmetrical dislocation emission at the crack tip, the crack growth path is mid-plane of the two symmetrical slip planes [\[22](#page-12-3)[–25](#page-12-4)]. In addition, when a persistent slip at a crack tip causes crack growth, the crack growth path is the slip plane [[25–](#page-12-4)[27](#page-12-5)].

Previously, crack propagation behavior within the γ ['] Fe₄N intermetallic compound layer in nitrided ultralow carbon steel (0.008 wt% carbon) was reported [[17,](#page-11-12) [18\]](#page-11-13). ${100}^{\prime}$ and ${111}^{\prime}$ planes were identified as the predominant crack growth paths in the monotonic and cyclic tests, respectively [[17,](#page-11-12) [18](#page-11-13)]. While these are pioneering studies, the following critical aspects still

need to be understood, which is the aim of the current work:

- 1. Steels designed for engineering applications typically contain carbon concentration ≥ 0.1 wt%, hence, the corresponding crack propagation behavior needs to be studied.
- 2. Since crack propagation occurs with a mixture of multiple growth mechanisms, statistical data of crystallographic crack paths is required for a deep understanding of the small crack growth behavior.
- 3. During nitriding, grain orientations with the fastest growth rates will grow preferentially, resulting in a columnar morphology [[28](#page-12-6)]. The effect of such a morphology needs to be evaluated.
- 4. First-principles calculations by Takahashi et al. [[29](#page-12-7)] demonstrated that in γ' Fe₄N, the elastic modulus of $\langle 111 \rangle_{\gamma}$ is the lowest, and that of $\langle 001 \rangle_{\gamma}$ is the highest. It suggests that the $\{111\}_{\gamma'}$ plane must be cracked when a cleavage fracture occurs. On the contrary, Koga et al. [\[17](#page-11-12)] reported {100}_{γ′} cleavage during monotonic tensile testing in the nitrided ultra-low carbon steel. This paradox needs to be clarifed.

In this study, we aim to understand the crack propagation behavior in the $Fe₄N$ intermetallic compound layer of nitrided (N) low-carbon steel (0.1 wt% carbon). The statistical data of the crack growth paths induced by monotonic and cyclic tensile loading are comparatively examined through electron backscater difraction (EBSD) analysis for multiple cracks. To study the efect of nitride grain morphology on the crack growth mechanisms, shot peening and subsequent nitriding treatment (SN steel), which results in relatively fine grain size and equiaxed grain morphologies [[30](#page-12-8)[–33\]](#page-12-9), are performed on the same low-carbon steel. Then, identical analyses are conducted in the nitrided layer of SN steel and compared to the specimen without shot peening (N steel).

Methods and materials

Materials and processing

The chemical composition of the low-carbon steel used is presented in Table [1](#page-2-0). Both N and SN steels were annealed for 900 s at 1223 K. Annealing was followed by water quenching. Tensile specimens for monotonic and cyclic testing were cut along the rolling direction (RD). The tensile specimens have a gauge length of 30 mm, a width of 4 mm, and a thickness of 2 mm. Detailed sample dimensions have been provided elsewhere [\[17\]](#page-11-12). Shot peening was carried out in an air blast shot peening machine (Fuji Manufacturing). Soda-lime glass beads with 550 HV hardness and a mean diameter of 53 μ m were used. Shot peening was performed at an injection pressure of 0.4 MPa with 200% coverage. Subsequently, the specimens were subjected to gas nitriding at 843 K for 18 ks (5 h) in an atmosphere of NH_3 , N_2 , and H_2 . A nitriding potential (K_N) of 0.35 Pa^{-0.5} was chosen based on the Leher diagram [\[19\]](#page-12-0) to selectively generate the γ ' nitride layer. Post nitriding at 843 K, the specimens were air-cooled (\sim 19 K min⁻¹) to ambient conditions. The nitriding process is schematically depicted in Fig. [1.](#page-2-1)

Monotonic and cyclic tensile test

Both the monotonic and cyclic tensile loading experiments were conducted using a Shimadzu Autograph

Figure 1 Schematic of the nitriding process to selectively generate the γ' nitride layer.

AG-20KNIST machine. The tensile test was performed at a strain rate of 2.8×10^{-4} s⁻¹ (crosshead speed of 0.5 mm/min). Cyclic loading tests (force control) were performed with a triangular waveform under a stress rate of 1 kN s^{-1} and a stress ratio of 0.1. The maximum stress in the cyclic loading tests corresponds to the yield stress (measured from monotonic tensile stress) of N and SN steels, 563 MPa and 583 MPa, respectively. The cyclic tensile tests were interrupted after 10,000 cycles (no necking observed), and the microstructure was characterized.

Characterization

The cross-section (perpendicular to transverse direction-TD) was mechanically polished to perform EBSD and electron channeling contrast imaging (ECCI). The EBSD and ECCI studies were carried out in a Carl Zeiss Merlin feld emission scanning electron microscope (FE-SEM) equipped with an EDAX Digiview 5 EBSD detector. Typically, defects such as dislocations and stacking faults appear with bright contrast in ECCI (when the grain is in channeling condition) [\[34\]](#page-12-10). EBSD data was analyzed using OIM Analysis 7 software, and only data points with confidence index value ≥ 0.1 were considered. The grain size was estimated from EBSD data using the intercept length method (edge grain included as half grains) over a

 (a)

Figure 2 Slab models of Fe4N **a** (100), **b** (110), and **c** (111) surfaces. The purple spheres represent iron (Fe) atoms, while the blue spheres indicate nitrogen (N) atoms.

Side view

width of 200 μm and 248 μm for N steel and SN steel, respectively. To assess the morphology of the $Fe₄N$ grains, the grains are approximated to an ellipse; the grain is identifed as equiaxed if the ratio of the minor axis to the major axis (aspect ratio) is > 0.4 . Since the EBSD step size was 40 nm, only grains with grain size > 100 nm were considered for the aspect ratio analysis. No edge grains were considered for the aspect ratio analysis.

Density functional theory (DFT) calculations

The density functional theory (DFT) calculations were performed to obtain the surface energy of low-index planes in $γ'$ -Fe₄N. Three surfaces were analyzed: (100), (110), and (111) surfaces. The surface energy was calculated by the following equation:

$$
E_{\text{surface}} = \frac{E_{\text{slab}} - E_{\text{bulk}}}{2A}.
$$
\n(1)

where E_{surface} represents the surface energy per unit area. E_{slab} is the total energy of the slab model for a specific surface orientation, while E_{bulk} corresponds to the total energy of the $Fe₄N$ in its bulk phase. The term *A* denotes the surface area of the slab model. The calculation of surface state was performed with the slab model shown in Fig. [2.](#page-3-0) We employed the generalized

gradient approximation type Perdew–Burke–Ernzerho (GGA-PBE) exchange–correlation functional, along with the DNP basis set and efective core potentials. Brillouin zone integrations were performed with the k-point at a grid spacing of < 0.05 Å−1. All DFT calculations were performed with $DMol³$ [[35,](#page-12-11) [36](#page-12-12)].

Results and discussion

Initial microstructure: efect of shot peening

Table [2](#page-4-0) summarizes the grain size, thickness, and morphology (percentage of equiaxed grains) of the $Fe₄N$ layer in N and SN steels. The $Fe₄N$ compound layer thickness (averaged over 32 regions using secondary electron imaging) for N and SN steels is 5.40 μ m and 4.68 µm, respectively. This observation is contrary to the reports in the literature, wherein shot peening enhanced the nitride layer thickness owing to enhanced N difusion due to grain refnement and plastic deformation at the surface [[30](#page-12-8), [32,](#page-12-13) [37\]](#page-12-14). However, understanding this phenomenon is beyond the scope of the present work.

Table 2 Grain size and morphology of the Fe₄N layer in N and SN steels

		Grain size (um) Equiaxed grains Compound (intercept length) (area fraction $\%$) layer thickness	(μm)
N steel	0.412	60.7	$5.40 + 0.44$
SN steel 0.318		76.8	$4.68 + 0.67$

While negligible pores (or voids) were present in the compound layer in the N steel, a signifcant number of pores were observed close to the surface in the SN steel (Fig. [3\)](#page-4-1). This observation contradicts the results of Kikuchi and Komotori [\[38](#page-12-15)], wherein they observed that pre-treatment of fne particle peening (FPP) suppressed the formation of pores in the compound layer. It was atributed to the FPP-induced depletion of Cr in the compound layer [[38,](#page-12-15) [39](#page-12-16)]. However, the Cr concentration in the low-carbon steel investigated in the current work (Table [1](#page-2-0)) is signifcantly lower. Schwarz et al. [\[40](#page-12-17)] have observed that while pore formation was absent in single crystalline pure Fe, pores developed along grain boundaries in polycrystalline pure Fe and Fe-based binary alloys. Schwarz et al. [[40](#page-12-17)] atributed the pore formation to grain boundaries acting as nucleation agents for N_2 gas-filled pores. Thus, it is likely that in the absence of signifcant Cr content, the grain refnement caused by shot peening promotes pore nucleation.

To ensure statistical robustness, grain size and morphology information (summarized in Table [2\)](#page-4-0) of the nitride layer was extracted from 200 µm and 248 µm long EBSD scans for N and SN steel, respectively. Representative inverse pole fgure (IPF) map of the γ' -Fe₄N layer for N and SN steel is shown in Fig. [4a](#page-5-0), b, respectively. We observe two prominent efects of shot peening on the $Fe₄N$ layer: (i) reduction in grain size and (ii) increase in the fraction of equiaxed grains. The reduction in $Fe₄N$ grain size due to shot peening is consistent with earlier fndings [[32\]](#page-12-13). Previous studies demonstrated that for pure Fe, γ' Fe₄N_{1-x} initially nucleates at the Fe grain boundaries at the surface, subsequently growing laterally into the Fe grains [[28,](#page-12-6)

Figure 3 Enhanced void formation in the compound layer (close to the surface) of SN steel compared to N steel.

Figure 4 Representative inverse pole figure (IPF) maps of the γ' -Fe₄N layer for **a** N and **b** SN steel illustrating the decrease in grain size and increase in the formation of equiaxed grains in SN steel.

[41](#page-13-0)]. Since shot peening results in grain refnement [\[30](#page-12-8), [32,](#page-12-13) [37](#page-12-14)], the nucleation sites for γ' Fe₄N_{1-x} nitride would enhance, and the area available for lateral growth of the nucleated nitride would decrease. This results in both a reduction in grain size and the promotion of equiaxed morphology in the $Fe₄N$ layer [\[28](#page-12-6)]. Competitive growth between nitride nanograins of diferent orientations occurs during the thickening of the nitride layer [[28](#page-12-6), [42\]](#page-13-1). Grains with orientations corresponding to the fastest growth rates will grow preferentially, resulting in a mixed morphology of columnar and equiaxed $Fe₄N$ grains in the SN steel [[28](#page-12-6)].

Crack propagation during monotonic tensile testing

Microstructural observations within the homogeneous deformation region (outside necking) post monotonic tensile fracture are shown in Figs. [5](#page-5-1) and [6.](#page-6-0) ECC micrographs in Fig. [5a](#page-5-1), a' indicate the columnar $Fe₄N$ microstructure in N steel. Figures [5](#page-5-1)b, c and [6a](#page-6-0)–e show the EBSD analysis results of crack propagation paths during monotonic tensile testing in N and SN steels, respectively (evaluated from seven microcracks). We report the frequency of occurrence of each crystallographic crack path (Figs. [5](#page-5-1)c, [6e](#page-6-0)). Two

Figure 5 Microstructural observations in the homogeneous deformation region (outside necking) after monotonic tensile fracture. ECC micrographs illustrate the a columnar Fe₄N grains in the N steels, and **a'** the presence of dislocations and stacking

faults formed during monotonic tensile testing. **b** Phase map and **b'** corresponding inverse pole fgure (IPF) map around a microcrack formed in the N steel. **c** Frequency of occurrence of each crack path (seven microcracks were investigated).

Figure 6 a Image quality map, **b** Phase map, **c** Grain reference orientation deviation (GROD) angle map, and **d** IPF map of a representative microcrack in the $Fe₄N$ layer in the SN steel after monotonic loading. The white arrow indicates a crack propagat-

ing adjacent to the GB. **b** The frequency of occurrence of diferent crack paths (evaluated from EBSD studies on seven microcracks) .

transgranular $γ'$ -Fe₄N cleavage planes are considered, namely $\{100\}_{\gamma'}$ and $\{111\}_{\gamma'}$ [\[17\]](#page-11-12). 'Neither' refers to the scenario wherein the transgranular crack does not correspond to either of the two planes (likely caused by the voids). Since the indexing of the crack path is based on two-dimensional EBSD trace analysis, there exist occasional cases wherein the trace of the cleavage plane corresponds to either of {100} and {111} planes (for instance, when the crack path is along *<* 011 *>* ). Such instances are labeled as 'Either.

Grain boundary (GB) has not been considered as a crack pathway for monotonic specimens. This is to avoid the overestimation of intergranular cracking. The width of the majority of the cracks investigated in monotonic tensile samples is ≥ 1 µm (Fig. [5a](#page-5-1)). Occasionally, we observed fne cracks in the monotonic tensile specimen wherein the width was ≤ 100 nm (possibly caused by the voids). For instance, a crack propagating towards the surface is shown in Fig. [6](#page-6-0). A fine transgranular crack adjacent to a GB is highlighted with a white arrow in Fig. [6d](#page-6-0). When the crack width is ~ 1 μm, a similar transgranular crack adjacent to a GB can be mis-indexed as intergranular cracking, causing an overestimation of GB cracking. It is due to the (i) preferential material removal at the edge during

polishing and (ii) limited spatial resolution of EBSD (-30 nm) [\[43\]](#page-13-2).

We observed that for both N steel and SN steel, the predominant transgranular crack path for the monotonic tensile specimen is ${100}_{\gamma'}$ followed by ${111}_{\gamma'}$ plane. Previously, Koga et al. [[17](#page-11-12)] reported ${100}\gamma$ cleavage during monotonic tensile testing. Koga et al. [[17](#page-11-12)] noted that it contradicts the elastic anisotropy results by Takahashi et al. $[29]$ $[29]$ (E₁₁₁ $(lowest)$ < E_{110} < E_{001} , Table [3](#page-7-0)) that were obtained from first-principles calculations. Based on their experimental results, Koga et al. [\[17](#page-11-12)] concluded that E_{001} should be the lowest in γ′-Fe₄N and further inferred that the elastic modulus behavior of γ' -Fe₄N is identical to γ -Fe. In the current work, we propose an alternative explanation for ${100}_{\gamma'}$ cleavage that does not contradict the density functional theory (DFT) results of Takahashi et al. [[29\]](#page-12-7).

The fracture toughness (K_{IC}) of a brittle material in plane strain condition based on Griffith's theory is typically estimated by [\[46](#page-13-3), [47](#page-13-4)]:

$$
K_{IC} = \sqrt{\frac{2E\gamma_s}{1 - v^2}}\tag{2}
$$

wherein E is Young's modulus in the plane normal direction to the cleavage plane, γ_s is the fracture surface energy of the cleavage plane, and *v* the Poisson's ratio. *v* for γ-Fe and γ′-Fe₄N is taken to be 0.376 [\[45](#page-13-5)] and 0.36 [[29\]](#page-12-7), respectively. It has to be noted that the elastic anisotropy of FCC γ '-Fe₄N is contrary to that of FCC Fe [[29,](#page-12-7) [48](#page-13-6)]. The directional dependence of elastic modulus in Fe₄N and γ -Fe (FCC Fe–15 Cr–15 Ni) obtained from ab initio calculations by Takahashi et al. [\[29](#page-12-7)] is provided in Table [3](#page-7-0). The surface energy of lowindex surfaces in γ-Fe using DFT-based calculations was reported by Yu et al. [[44](#page-13-7)] as shown in Table [3](#page-7-0). However, similar data for the γ' -Fe₄N system was not available in the literature. To this end, we calculated the surface energies of low-index surfaces in γ' -Fe₄N using DFT ("[Density functional theory \(DFT\) calcu](#page-4-2)[lations"](#page-4-2) section). The surface energies follow γ_s^{100} < $\gamma_s^{110} < \gamma_s^{111}$. Based on Eq. [2](#page-6-1), fracture toughness exhibits the opposite trend with $K_{IC}^{111} < K_{IC}^{110} < K_{IC}^{100}$.

It is important to note that Eq. [2](#page-6-1) is only applicable for elastic materials that undergo brittle fracture. We observed the presence of dislocations and stacking faults in Fig. [5](#page-5-1)a' (which is consistent with previous report by Koga et al. [[18\]](#page-11-13)). Furthermore, the localized plastic deformation in the γ' -Fe₄N layer during crack propagation is evident from the grain reference orientation deviation (GROD) angle map [[49\]](#page-13-8), as shown in Fig. [6c](#page-6-0). This indicates that the assumption that plasticity is absent is incorrect. Linear elastic fracture mechanics (LEFM) approximation (Eq. [2\)](#page-6-1) is valid when the crack tip plastic zone is small compared to the crack length [[50](#page-13-9)]. However, in the present scenario maximum possible crack length is $\leq 6 \mu m$ (nitride layer thickness), further explaining the limitation of the LEFM approach. The preferred cleavage plane ${100}^{\prime}$ corresponds to the plane with lowest surface energy. Hence, it can be

inferred that the cleavage during monotonic tensile testing is predominantly determined by the plane with lowest surface energy. It can be noted that in addition to $\left\{ 100\right\} _{\gamma^{\prime}}$ cleavage, we also observe $\left\{ 111\right\} _{\gamma^{\prime}}$ cracking which can be attributed to the lowest K_{IC} .

Crack propagation during cyclic tensile testing

Fatigue crack initiation in nitrided steels can involve the following mechanisms:

- (i) Surface crack formation [[51,](#page-13-10) [52\]](#page-13-11).
- (ii) Crack initiation at the interface of the compound layer and the base material due to the local heterogeneity caused by the diference in elastic modulus, hardness, and plastic deformation behaviour [[53](#page-13-12), [54](#page-13-13)].
- (iii) Crack initiation at the pores/voids formed during nitriding [\[17](#page-11-12), [55](#page-13-14), [56](#page-13-15)].
- (iv) Formation of fresh cracks ahead of a crack tip [[57,](#page-13-16) [58\]](#page-13-17).
- (v) Sub-surface crack initiation at inclusions [\[59](#page-13-18), [60](#page-13-19)].

However, the detailed statistical understanding of the crack initiation mechanisms is beyond the scope of the current work and constitutes future work.

Figure [7a](#page-8-0)–c show a discontinuous crack propagating towards the surface within the γ' -Fe₄N layer in an SN steel subject to cyclic tensile tests. The GROD angle map of the crack tip region shown in Fig. [7d](#page-8-0) demonstrates that the fatigue crack propagation involves plasticity evolution. This observation is consistent with previous transmission electron microscopy investigations of the γ' -Fe₄N layer after cyclic tests, which showed the crack propagation mechanism involved plastic deformation at the crack tip [[18\]](#page-11-13). These results

Figure 7 a Secondary electron (SE) image, **b** IPF map, **c** Phase map, and **d** Grain reference orientation deviation (GROD) angle map of a discontinuous microcrack within the $Fe₄N$ layer in the

SN steel after cyclic loading. Black boxes in **a**, **b** correspond to the GROD angle map in **d**.

Figure 8 Schematic of fatigue crack propagation via **a** symmetrical dislocation emission at the crack tip and **b** slip plane cracking (adapted from Ju et al. $[23]$ $[23]$) in Fe₄N.

indicate that the crack propagation occurred via cyclic plasticity evolution at the crack tip.

When plasticity controls the fatigue crack growth, the crack growth is recognized to occur through two representative mechanisms. Figure [8](#page-8-1)a illustrates a schematic of fatigue crack propagation via symmetrical dislocation emission at the crack tip. The crack growth paths along ${110}_{\gamma'}$ and ${100}_{\gamma'}$ planes are the mid-plane of the two symmetrical $\{111\}_{\gamma'}$ slip planes [[22–](#page-12-3)[25](#page-12-4)]. The fatigue crack propagation on $\{111\}_{\gamma'}$ (Fig. [8](#page-8-1)b) is generally interpreted as slip plane cracking caused by persistent slip at a crack tip [[25](#page-12-4)[–27](#page-12-5)]. The crack propagation on the slip plane typically occurs when the crack length is smaller than the microstructure size, such as grain size.

The crack growth along ${110}_{\gamma'}$ and ${100}_{\gamma'}$ planes in Fig. [9a](#page-9-0), c occurs via the symmetrical dislocation emission at the crack tip (Fig. [8a](#page-8-1)) [[22](#page-12-3)[–25](#page-12-4)]. The fatigue crack propagation occurs on $\{111\}_{\gamma'}$ (Fig. [9a](#page-9-0), c) corresponds to the slip plane cracking mechanism (Fig. [8](#page-8-1)b) [[25–](#page-12-4)[27\]](#page-12-5). Figure [9d](#page-9-0), e show the frequency of occurrence of crack paths after cyclic tensile testing in N steel

Figure 9 a Representative IPF map of crack propagation in cyclic testing in the N steel. **b** ECC micrograph of a microcrack in SN steel after cyclic tensile testing. (b') ECC micrograph at a higher magnifcation revealing the presence of stacking faults and dislocations (black box in **b**).The red box corresponds to the representa-

and SN steel, respectively. It is based on EBSD investigations of ten microcracks for each N and SN steel. 'Either' is a label for instances wherein the crack path could correspond to either $\{100\}_{\gamma'}$ or $\{111\}_{\gamma'}$. If the crack plane did not correlate to either of ${100}\gamma$ or ${111}\gamma$ we then checked for ${110}_{\gamma'}$ cracking. 'Neither' refers to the cases wherein the transgranular crack path does not match with any of the three planes ({100}_{γ'}, {111} γ and ${110}_\gamma$). It is likely that a transgranular crack in the case of 'neither' is caused by the coalescence of discontinuous cracks and coalescence of cracks with pre-existing voids (due to localization of plasticity).

tive IPF map with various crack paths in **c**. **d** The frequency of occurrence of diferent crack paths in N steel after cyclic tensile loading (evaluated from EBSD studies on ten microcracks). **e** The frequency of occurrence of diferent crack paths in SN steel after cyclic loading (evaluated from EBSD studies on ten microcracks).

Further in-situ and quasi-in-situ experimental investigations are required to verify this hypothesis.

For both N and SN steels, we observe that transgranular cracking along $\{100\}_{\gamma'}$ or $\{111\}_{\gamma'}$ plane is equally likely (Fig. [9d](#page-9-0), e, Fig. [10\)](#page-10-0). Since the width of fatigue cracks for the N and SN steel is \leq 200 nm, we can index and report GB cracks with reasonable confdence (unlike monotonic testing). It can be noted that intergranular crack propagation is the predominant fatigue crack propagation pathway for both N and SN steels (Fig. [9](#page-9-0)d, e). As discussed in "[Initial microstruc-](#page-5-2)ture: effect of shot peening" section, Schwarz et al. [\[40\]](#page-12-17)

Figure 10 Summary of the statistical assessment of the cracking behavior in the γ' Fe₄N layer of N and SN steels during **a** monotonic and **b** cyclic tensile deformation.

reported that the grain boundaries act as nucleation sites for N_2 gas-filled pores. Thus, it is likely that such grain boundary void formation results in enhanced intergranular cracking. However, the effect of preexisting voids on the crack growth pathways cannot be clarifed via post-mortem investigations; it necessitates in-situ (or quasi-in-situ) studies and constitutes future work.

Conclusions

Figure [10](#page-10-0) summarizes the statistical assessment of the cracking behavior in the γ ' Fe₄N layer during monotonic and cyclic tensile deformation in a nitrided (N) and shot-peened and subsequently nitrided (SN) lowcarbon steel. Crack growth paths were comparatively evaluated through EBSD analysis for multiple cracks.

- 1. SN steel consisted of ~ 16% more equiaxed nitride grains when compared to N steel. Additionally, enhanced void formation within the compound layer (near the surface) was observed in the SN steels. Since no considerable diference exists in the crack paths between N and SN steels, it is likely that the effect of nitride morphology and pores within the compound layer on the crack growth paths is negligible.
- 2. Both elastic modulus and LEFM-based fracture toughness of $\{111\}_{\gamma'}$ are lower when compared to ${100\math}^{\prime}_{\gamma}$. However, ${100\math}^{\prime}_{\gamma}$ is the predominant trans-

granular crack path in the monotonic tensile tested specimen, followed by $\{111\}_{\gamma}$. This contrary behavior is explained by $\{100\}_{\gamma'}$ plane having the lowest surface energy (obtained from DFT calculations).

3. A predominant intergranular fracture was observed in the cyclic tensile loaded specimen. Experiments revealed that transgranular cracking along $\{100\}_{\gamma'}$ (cracking via symmetric dislocation emission) or ${111}\gamma$ ['] (slip plane cracking) is equally likely.

A material's fatigue performance is dependent on both crack initiation and growth. This study presents a comprehensive understanding of the crack growth pathways. In addition, a statistical understanding of the crack initiation mechanisms is necessary to design nitrided steels. To this end, in-situ or quasi-in-situ experiments can help elucidate the role of microstructure on crack initiation. It is a topic of future work.

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Declarations

Conflict of interest The authors declare that they have no known competing fnancial interests or personal relationships that could have appeared to infuence the work reported in this paper.

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