

Solidification microstructures in Ag₃Sn–Cu₃Sn pseudo-binary alloys

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ABSTRACT

The solidification microstructures in three alloys from the Ag₃Sn–Cu₃Sn pseudo-binary section in the Ag–Cu–Sn system have been studied using a combination of X-ray diffraction, electron microscopy, differential scanning calorimetry, and quenching experiments. The three alloys have Ag:Cu ratios of 50:50, 40:60, and 30:70. In each case, the as-cast structures exhibit the equilibrium phases θ -Ag₃Sn and ε_1 -Cu₃Sn, with a little η -Cu₆Sn₅. There is no evidence of the metastable high-temperature phases that are so prevalent in as-cast structures of the corresponding binary alloys. The differential scanning calorimetry data obtained on heating the alloy samples are consistent with the transformations expected on the basis of the published ternary Ag–Cu–Sn diagrams. It is proposed that the solidification microstructures observed experimentally in such alloys must correspond to the nucleation of the high-temperature phases being kinetically limited upon cooling for these compositions. This leads to the direct formation of the equilibrium low-temperature phases by eutectic-type co-operative growth.

Introduction

The Ag–Cu–Sn system has attracted a great deal of attention, largely because Sn-rich alloys in this system are good candidates for Pb-free solders [[1,](#page-12-0) [2](#page-12-0)]. There are no ternary intermetallic phases formed in the Ag–Cu– Sn system [\[3](#page-12-0)], but the diversity of binary phases leads to complex phase equilibria for some ternary compositions. There is an Sn-rich ternary eutectic that forms the basis of most solder formulations: this occurs at around 218 °C with a composition of 3.5 % Ag, 1.1 % Cu and 95.4 % Sn (atomic percent) [[4\]](#page-12-0). Upon

[[5\]](#page-12-0)). These latter phases are the most Sn-rich intermetallics in the corresponding binary systems. In the binary Ag-Sn system, there is also a close-packed hexagonal phase ε_2 -Ag₅Sn. In the binary Cu-Sn system, there is one other low-temperature intermetallic phase, ε_1 -Cu₃Sn, and three high-temperature phases (β -Cu₁₃Sn₃, γ -Cu₄Sn, and δ -Cu₄₁Sn₁₁). The phases θ -Ag₃Sn and ε_1 -Cu₃Sn are iso-structural and exhibit the geometrically close-packed

solidification, a three-phase mixture is formed comprising: β -Sn, θ -Ag₃Sn and η -Cu₆Sn₅ (phases are designated following the notation adopted by Chang et al.

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orthorhombic Cu₃Ti-type structure $(DO_a, space group)$ *Cmcm*) $[6-8]$, although non-stoichiometric ε_1 -Cu₃Sn can deviate from the ideal $D0_a$ structure due to displacive lattice modulations or periodic faulting [[9,](#page-12-0) [10](#page-12-0)]. Both phases play an important role in microelectronic applications utilizing lead-free solders, where they can be present as minority strengthening phases in the solder alloy and can form as reaction products at solder/substrate interfaces [\[11–14\]](#page-12-0). Thin interfacial films of these phases can promote the formation of a good metallurgical bond at the solder joint, but coarsened interfacial phases can lead to embrittlement and to thermal fatigue or creep failures $[15-17]$. These DQ_a compounds are also of interest because they are found in dental amalgams as part of complex phase mixtures [\[6](#page-12-0), [18,](#page-12-0) [19](#page-12-0)].

Studying the properties of these $D\theta_a$ phases is challenging because the phase equilibria make the production of good quality single-phase samples very difficult. In the binary Ag-Sn system, the θ -Ag₃Sn phase forms via a rather sluggish peritectic reaction between Sn-rich liquid and the ε_2 -Ag₅Sn phase [[20](#page-12-0)]. In binary Cu-Sn alloys, ε_1 -Cu₃Sn forms via congruent ordering from the cubic BiF₃-type γ -Cu₄Sn phase, which is itself a peritectic reaction product [\[21\]](#page-12-0). There has been some success in producing bulk single-phase θ -Ag₃Sn and ε_1 -Cu₃Sn samples by casting followed by long-term annealing [[22\]](#page-12-0). These samples were used to measure the elastic properties, hardness, and indentation fracture toughness of the phases, but concerns remain about segregation and/or oxidation effects on measurements from material produced via this route.

In the present study, we selected three alloys with compositions that lie on the Ag₃Sn–Cu₃Sn pseudobinary and examined the solidification microstructures to evaluate the extent to which the complex phase equilibria can be avoided. X-ray diffraction (XRD) and scanning electron microscopy (SEM) data from as-cast samples of the three alloys gave the unexpected result that the θ -Ag₃Sn and ϵ_1 -Cu₃Sn phases can form directly from the melt via a eutectictype solidification process. Differential scanning calorimetry (DSC), heat-treatment/quenching, and transmission electron microscopy (TEM) experiments were then used to investigate the discrepancy between the observed microstructures and those expected on the basis of the published ternary Ag– Cu-Sn phase diagram. It is inferred from these data that the nucleation of intermediate phases such as ε_2 -Ag5Sn in the melt is suppressed even at very modest

cooling rates, leading to the formation of the phase mixtures observed experimentally.

Materials and experimental methods

Three $(Ag,Cu)_{3}Sn$ alloy compositions were selected for this study as shown in Table 1. These are referred to as the 50:50, 40:60, and 30:70 alloy samples, where the designations refer to the ratio of the atomic percentages of Ag and Cu in the respective alloys. Cylindrical ingots, 25 mm in diameter, were produced by ACI Alloys, Inc. (San Jose, CA) for each of the alloys from high-purity elemental starting materials by arc-melting and casting under argon gas.

Samples for XRD and SEM analyses were obtained by slicing disks of about 2 mm in thickness from the cylindrical ingots. These samples were ground using successively finer grades of SiC abrasive papers, and were then polished using colloidal alumina suspension. The XRD studies were performed on the polished surfaces using a Bruker AXS D2 Phaser diffractometer equipped with a 30 kV Cu K α source and a Lynxeye detector. The data were obtained by scanning over a 2θ range of $20-60^\circ$ at a scan speed of 0.02° /s for a total time of 2.5 h. These data were analyzed by comparison with standard International Centre for Diffraction Data (ICDD) files. Backscattered electron (BSE) SEM images and energy-dispersive X-ray spectrometry (EDXS) data were obtained from the polished sample surfaces in a FEI Teneo LoVac SEM equipped with an EDAX Octane silicon drift detector (SDD) EDXS system.

Small pieces were broken from each alloy, and samples with an approximate weight of 10 mg were used for DSC analyses. The initial analyses were performed in a TA Instruments SDT Q600 under a purified argon atmosphere using a heating rate of 10 °C/min. To identify the processes occurring at each significant event in the DSC signatures, parallel heating and quenching experiments were performed in a TA Instruments DSC 2920, which allows for

Table 1 Nominal compositions of the three alloys

Alloy $#$		Composition $(at.^{\%})$		Composition $(wt\%)$			
	Αg	Cu	Sn	Αg	Сu	Sn	
50:50	37.5	37.5	25.0	43.0	25.4	31.6	
40:60	30.0	45.0	25.0	35.7	31.6	32.7	
30:70	22.5	52.5	25.0	27.8	38.2	34.0	

samples to be removed rapidly from the apparatus. The heating conditions were matched to those of the initial DSC analyses, i.e., 10-mg samples were heated at 10 $\mathrm{C/min}$ under purified argon to the required temperatures. The samples were then removed and immediately quenched in water at room temperature. The quenched samples were mounted in cold-setting epoxy resin loaded with a conductive filler of Ni powder, ground and polished to a mirror finish, and the microstructures were examined using BSE imaging and EDXS analyses in the SEM.

For selected samples, analyses of microstructural details were performed by TEM. The TEM specimens were prepared by focused ion beam (FIB) milling techniques from polished sample surfaces using an FEI Helios Nanolab G3 dual-beam FIB instrument, which is equipped with a flip-stage and a scanning transmission electron microscopy (STEM) detector for improved final thinning. A 3 -µm-thick Pt layer was deposited onto the polished surfaces in situ to protect the surface of the TEM specimen during ion milling. This deposition was accomplished in two steps: the first $1 \mu m$ of Pt was deposited using the electron beam to crack the organometallic Pt precursor, and the remaining $2 \mu m$ of Pt was deposited using the ion beam. In the initial stages of the milling process, the accelerating voltage used for the ion column was 30 kV and the ion beam currents were reduced iteratively to a value of 28 pA. During the final milling process, the accelerating voltage for the ion column was reduced to 5 kV and the ion beam current used was reduced to 15 pA to avoid excessive $Ga⁺$ implantation and beam damage. The FIB-cut slices were mounted onto Mo grids and attached at one edge to avoid the re-deposition of the grid materials onto the sample surface during final thinning. The TEM specimens were examined in an FEI Tecnai T12 TEM and in an FEI Talos F200X S/TEM operating at accelerating voltages of 120 and 200 kV, respectively. The latter instrument is equipped with a Super-X SDD EDXS system, which allows for rapid acquisition of spectrum images for elemental mapping.

Results

Microstructure of the as-cast alloys

Producing fine powders from these alloys proved to be particularly challenging, and so XRD data were

obtained in Bragg-Bretano geometry from the polished surfaces of disks cut from the ingots. Representative examples of the data obtained from the three alloys are shown in Fig. [1,](#page-3-0) where the counts are plotted on a logarithmic scale to better show the low intensity peaks. We note that the relative intensities of the peaks (but not the peak positions) varied from scan to scan for each sample indicating that there are pronounced effects from the grain size and/or preferred grain orientations in these ingots. The majority of the XRD peaks correspond to those expected for the $D0_a$ phases θ -Ag₃Sn $(a_0 = 0.597 \text{ nm}, b_0 = 0.478 \text{ nm}, c_0 = 0.518 \text{ nm}$ [[6\]](#page-12-0)) and ε_1 -Cu₃Sn ($a_0 = 0.549$ nm, $b_0 = 0.432$ nm, $c_0 =$ 0.474 nm [\[7](#page-12-0)]). There are also minor peaks corresponding to the long-period superstructure polymorph of Cu₃Sn ($a_0 = 0.553$ nm, $b_0 = 4.775$ nm, $c_0 = 0.432$ nm, space group Cmcm [[9](#page-12-0)]¹) in the XRD data from the 50:50 alloy. This long-period polymorph of $Cu₃Sn$ is now widely accepted as the equilibrium form, but requires extended annealing to develop fully (e.g., [\[23](#page-12-0)]). We note that the absence of such peaks in the data from the 40:60 and 30:70 alloys does not necessarily demonstrate that this polymorph is not present in these alloys since most of the peaks from this polymorph of $Cu₃Sn$ overlap with those from the $D\theta_a$ ε_1 structure. Minor peaks from the hexagonal η -Cu₆Sn₅ phase ($a_0 = 0.419$ nm, $c_0 =$ 0.509 nm, space group $P6_3/mmc$ [\[24](#page-12-0)]) were observed in each of the alloys, although here again some of the peaks from this phase overlap with those from the phases ε_1 -Cu₃Sn and θ -Ag₃Sn.

The microstructures of the as-cast alloys were investigated using BSE imaging and EDXS analysis on metallographic sections in the SEM. Examples of typical BSE SEM images from the three alloys are presented in Fig. [2.](#page-3-0) There is strong compositional contrast in such images, and EDXS point analyses were used to confirm that the light and dark regions correspond to the main Ag $_3$ Sn and Cu $_3$ Sn phases, respectively. There are also occasional small gray regions corresponding to the $Cu₆Sn₅$ phase, and examples of these are shown in the insets to each micrograph. In each case, it was found that these phases are not pure stoichiometric compounds, but instead there is some solubility of Cu in Ag₃Sn, and of Ag in Cu₃Sn and Cu₆Sn₅. The mean compositions

 $^{\rm 1}$ It is important to note that the conventions used to define the axes in the D0a and long-period polymorphs are different. Thus, the b axis of the long-period structure lies parallel to c in the conventional description of the $D\theta$ _a structure, and b_0 (superstructure) $\approx 10 c_0$ (D0_a).

Figure 1 XRD data obtained from as-cast samples of the alloys: a 50:50; b 40:60; c 30:70.

for these majority phases as measured by EDXS are given in Table 2. These values were obtained from the raw Ag L, Cu K, and Sn L signals using library standards with e-ZAF corrections. It can be seen that the phase compositions are rather similar in the three alloys and thus the main effect of the differences in alloy composition is a difference in the volume fractions of the phases. Image analysis was performed on BSE images such as those shown in Fig. 2 and the mean volume fractions of Cu₃Sn obtained were 42, 52, and 64 % for the 50:50, 40:60, and 30:70 alloys, respectively. Since the volume fraction of the $Cu₆Sn₅$ phase is less than 2 % in each case, the Ag₃Sn phase constitutes most of the remainder of the as-cast microstructures. There is also a transition in the morphology of the phases. In the 50:50 alloy, there is a bimodal size distribution for the $Cu₃Sn$ phase with larger features (several µm across) resembling dendrite arms, and regions of much more finely divided features $(<1 \mu m)$ that are reminiscent of eutectic micro-constituents. In the 40:60 and 30:70 alloys, the

Figure 2 Representative BSE SEM images obtained from as-cast samples of the alloys: **a** 50:50; **b** 40:60; **c** 30:70.

Table 2 Compositions of the phases in the as-cast alloys measured using EDXS in the SEM

				Alloy # Ag ₃ Sn (at.%) Cu ₃ Sn (at.%) Cu ₆ Sn ₅ (at.%)					
						Ag Cu Sn Ag Cu Sn Ag Cu Sn			
50:50						68.1 4.8 27.1 3.2 73.4 23.4 1.2 55.6 43.2			
40:60						68.0 5.2 26.8 3.2 73.6 23.2 1.1 55.9 43.0			
30:70						66.1 7.0 26.9 2.7 73.9 23.4 * * *			

* The regions of $Cu₆Sn₅$ phase in the 30:70 alloy were too small to measure accurately by EDXS

majority phases adopt a more uniform blocky morphology, although in both cases there are still occasional regions that show a more finely divided structure.

These data suggest that the mixture of θ -Ag₃Sn and ε_1 -Cu₃Sn phases may form directly from the melt, rather than via reactions involving high-temperature phases such as ε_2 -Ag₅Sn or γ -Cu₄Sn. There was no evidence for such intermediate phases, or indeed any compositional gradients within the major phases, and both of these effects might have been expected if the phases were formed via the transformation paths that occur in the binary systems. Moreover, as explained in the Discussion section, this is not what one would expect on the basis of the published ternary phase diagram. The DSC and heat-treatment/quenching studies described below were performed to investigate these phenomena.

DSC analyses

The thermal characteristics of these alloys were determined by heating 10 mg samples of the as-cast materials from room temperature to 750 \degree C at 10 \degree C/ min. In each case, the alloys underwent a series of endothermic processes between 350 and 650 $^{\circ}$ C, and representative DSC data for the temperature range 300–700 C are shown in Fig. 3. All three alloys exhibit a small endothermic trough at 355° C, and much larger sharp troughs at 482 and 531 $^{\circ}$ C. The alloys also exhibit a fourth, somewhat broader

Figure 3 Plots of DSC heat flow data obtained from as-cast alloy samples at a heating rate of 10 \degree C/min.

trough. The temperature for this fourth trough varies with composition from 561 to 593 and 618 \degree C for the 50:50, 40:60, and 30:70 alloys, respectively. These data were repeatable with scans on duplicate samples exhibiting essentially identical trough temperatures and shapes. Furthermore, all of the processes associated with these troughs were found to be reversible. Samples of each alloy were heated from room temperature to $750 \degree C$, cooled to room temperature in the DSC apparatus, and then heated to $750 \degree C$ again. The troughs observed upon re-heating showed no significant differences from those in the original scans. For the 50:50 alloy, additional experiments were performed in which samples were heated from room temperature to 400, 500, and 545 \degree C (i.e., just past the first, second and third troughs, respectively), cooled to room temperature in the DSC apparatus, and then re-heated to the end-point temperature. In each case, the data obtained on re-heating were indistinguishable from those obtained in the initial heating scan. Thus, the thermal events observed in the DSC scans are reversible, both individually and in sequence.

To identify the transformations associated with these processes, additional 10-mg samples of each alloy were heated from room temperature to setpoints of 400, 500, 545, and 600 $^{\circ}$ C in a separate DSC apparatus. Upon reaching the set-point, the samples were removed rapidly from the apparatus and quenched into water. The set-points of 400 and 500 °C lie between the invariant troughs at 355, 482, and 531 °C in each sample. The set-point of 545 °C lies between the invariant trough at 531 \degree C and the fourth trough, whose temperature varies from one sample to another. The set-point of 600 °C is the maximum temperature achievable in this apparatus and lies above the fourth trough for the 50:50 and 40:60 alloys, but below this trough for the 30:70 alloy. The microstructural data obtained from these quenched specimens are described in the sections below.

Microstructures of the quenched 50:50 alloy samples

Examples of BSE SEM images from the quenched 50:50 alloy samples are presented in Fig. [4](#page-5-0). The sample quenched from $400 \degree C$ (Fig. [4a](#page-5-0)) exhibits a very similar morphology to that observed in the ascast 50:50 alloy (Fig. [2](#page-3-0)a). The only significant difference is the disappearance of the $Cu₆Sn₅$ phases. The microstructure in the sample quenched from 500 °C

Figure 4 Representative BSE SEM images obtained from 50:50 alloy samples quenched to room temperature from: a 400 °C; b 500 °C; c 545 °C; d 600 °C.

was rather different (Fig. 4b) with somewhat coarser Ag₃Sn and Cu₃Sn grains surrounded by a complex phase mixture. The morphology of this mixture is shown at higher magnification in the inset to the figure. The mean volume fractions of the micro-constituents were measured from such images as 40.4 % Ag₃Sn, 37.3 % Cu₃Sn, and 22.3 % of the phase mixture. For the samples quenched from 545 and 600 $^{\circ}$ C, however, there are only two micro-constituents present: $Cu₃Sn$ grains and a finely divided phase mixture. In both cases, the volume fraction of the $Cu₃Sn$ phase is similar (22.6 and 24.1 vol.%, respectively), but the phase morphologies and sizes are very different. In the sample quenched from $545 \degree C$, the Cu₃Sn is coarser (up to 50 μ m across) and more angular. In the sample quenched from $600 °C$, the Cu₃Sn is much finer (up to 5μ m across) and more globular. Mean compositions measured by EDXS analysis from the micro-constituents in the four quenched 50:50 alloy samples are presented in Table 3. The compositions of the Ag₃Sn and Cu₃Sn phases are fairly consistent throughout, although there is some minor variation in the Cu and Ag contents of these phases, respectively. The most

Table 3 Compositions (in at.%) measured using EDXS in the SEM from the microstructural constituents in the 50:50 alloy samples quenched from set-point temperatures, T

	$T({}^{\circ}C)$ Ag ₃ Sn			Cu ₃ Sn			Phase Mixture		
								Ag Cu Sn Ag Cu Sn Ag Cu	Sn
400					67.1 6.4 26.5 1.5 75.4 23.1 $-$				
500								69.4 8.2 22.4 2.7 74.1 23.2 37.0 27.3 35.7	
545								2.7 74.0 23.3 43.1 29.6 27.3	
600								3.3 73.2 23.5 43.8 28.9 27.3	

dramatic differences are in the composition of the phase mixture. The mixture in the sample quenched from 500 °C contains significantly less Ag and more Sn than that in the samples quenched from 545 and 600 °C. In these latter two samples, the EDXS data are very similar suggesting that the phase mixture present is the same.

The details of the phase mixtures were investigated by S/TEM analysis on FIB-cut TEM specimens from these micro-constituents in the samples quenched from 500, 545, and 600 \degree C. A set of data from one such experiment on the sample quenched from

Figure 5 S/TEM data obtained from the complex phase mixture in the 50:50 alloy sample quenched from 500 °C: a BF STEM image; b–d compositional maps obtained from the region in (a) showing the distribution of Ag, Cu, and Sn, respectively;

e SADP from region 1 in (a); (f–i) microdiffraction patterns from regions 2, 3, 4, and 5 in (a), respectively. The patterns in $(e-i)$ are presented at the same camera length.

500 °C is shown in Fig. 5. The bright field (BF) STEM image in Fig. 5a shows a large Ag₃Sn grain at the top left (labeled 1) with smaller grains from the complex phase mixture across the rest of the field of view. The compositional variation was revealed by spectrum imaging in which full spectra were collected at each point in the scan, and these were analyzed by performing a standard-less quantification using the Ag L, Cu K, and Sn L peaks at each point. Thus, the maps shown in Fig. 5b–d are compositional maps (rather than raw X-ray maps) and the intensities in these maps are proportional to the Ag, Cu, and Sn contents, respectively. Based upon these data, four different phases were detected in the mixture and an example of each is labeled (2-5) in Fig. 5a. The phases were identified by tilting the sample until zone axis patterns were obtained from a grain of each phase. Examples of the diffraction data are shown in Fig. 5e–i. The selected-area diffraction pattern $(SADP)$ in Fig. 5e was obtained from the large Ag₃Sn grain at 1 in Fig. 5a; this corresponds to a $\overline{[342]}$ zone axis pattern (ZAP) from the θ -Ag₃Sn phase. The grains in the phase mixture were too small to give clear SADPs, so instead micro-diffraction patterns were obtained with a convergent probe and a small condenser aperture. Examples of micro-diffraction

ZAPs from the grains labeled 2–5 in Fig. 5a are shown in Figs. 5f–i, respectively. These are indexed as the [100] ZAP for ε_1 -Cu₃Sn, the [1213] ZAP for η -Cu₆Sn₅, the [1213] ZAP for the hexagonal ε_2 -Ag₅Sn phase $(a_0 = 0.29658 \text{ nm}, c_0 = 0.47842 \text{ nm}, \text{ space}$ group $P6_3/mmc$ [[20\]](#page-12-0)), and the [311] ZAP for the tetragonal β-Sn phase ($a₀ = 0.582$ nm, $c₀ = 0.318$ nm, space group $I4_1$ /amd [\[25](#page-13-0)]). We note that while these patterns are presented at the same scale (effective camera length), they were obtained at different sample orientations and no conclusions could be drawn about the presence, or otherwise, of any orientation relationships between the phases.

Similar experiments on FIB-cut TEM specimens from the samples quenched from 545 and 600 $^{\circ}$ C revealed much simpler phase mixtures comprising alternating lamellae of the θ -Ag₃Sn and ε_1 -Cu₃Sn phases. An example of a data set obtained from the sample quenched from $600 \degree C$ $600 \degree C$ is shown in Fig. 6. A BF STEM image and the corresponding Ag, Cu and Sn maps are given in Figs. [6](#page-7-0)a–d, respectively. The SADP in Fig. [6e](#page-7-0) was obtained from the area shown in Fig. [6](#page-7-0)a, and Fig. [6f](#page-7-0) is an indexed schematic of this pattern. The pattern corresponds to overlay of the [142] ZAPs from the θ -Ag₃Sn and ε_1 -Cu₃Sn phases in the orientation relationship:

Figure 6 S/TEM data obtained from the eutectic micro-constituent in the 50:50 alloy sample quenched from 600 °C: a BF STEM image; b–d compositional maps obtained from the region

 $\left[\overline{1}\overline{4}\overline{2}\right]\theta$ -Ag₃Sn // [142] \mathcal{E}_1 -Cu₃Sn

in (a) showing the distribution of Ag, Cu, and Sn, respectively; e SADP obtained from the region shown in (a); f indexed schematic of the SADP in (e).

 $\left[\overline{142}\right]$ Ag₃Sn // [142] Cu₃Sn

 $(201)Ag₃Sn$ // $(201)Cu₃Sn$

 $(2\bar{2}3)Ag_3Sn$ // $(\bar{2}2\bar{3})Cu_3Sn$

Since the SADP in Fig. 6e includes contributions from several Ag₃Sn and Cu₃Sn lamellae, the phases must be arranged in colonies with well-defined orientations between the layers. Such characteristics are typical of eutectic solidification of phases mixtures with similar structures and modest differences in lattice parameters. We note that similar data were obtained from the phase mixtures in the sample quenched from 545 °C. Further work is underway in an attempt to understand the reasons for the adoption of this orientation relationship in the phase mixture.

Microstructures of the quenched 40:60 and 30:70 alloy samples

A representative selection of BSE SEM images obtained from the 40:60 and 30:70 alloy samples quenched from 500, 545, and 600 \degree C is shown in Fig. [7.](#page-8-0) The mean compositions of the micro-constituents in the quenched samples were measured using EDXS in the SEM and these data are summarized in Table [4.](#page-8-0) We note that, as for the 50:50 alloy, quenching from 400 °C produced no significant microstructural changes other than the disappearance of the $Cu₆Sn₅$ phases, and only very minor changes in the compositions of the $Ag₃Sn$ and $Cu₃Sn$ phases. The images from these samples are not included in Fig. [7.](#page-8-0)

The phase distribution in the 40:60 and 30:70 alloy samples quenched from 500 \degree C (Figs. [7](#page-8-0)a, b, respectively) is similar to that in the corresponding 50:50 alloy sample (Fig. [4](#page-5-0)b). There are coarse $Ag₃Sn$ and $Cu₃Sn$ grains plus regions of a complex phase mixture, which are shown at higher magnification in the insets to the figures. The volume fractions of the phase mixtures are significantly lower than that in the 50:50 alloy, at around 8 and 3 % in the 40:60 and 30:70 alloy samples, respectively. The mean compositions of these regions were also different in each alloy, and indeed from region to region in the same sample, suggesting that the compositions and/or proportions of the phases present in such regions vary somewhat.

For the 40:60 and 30:70 alloy samples quenched from $545 \,^{\circ}\text{C}$, only two micro-constituents are observed in the BSE SEM images (Fig. [7c](#page-8-0), d, respectively): coarse $Cu₃Sn$ grains and a fine phase mixture that resembles a eutectic. This is very similar to the microstructure observed for the 50:50 alloy quenched from this temperature (Fig. [4c](#page-5-0)). In contrast to the

Figure 7 Representative BSE SEM images obtained from the 40:60 (a, c, e) and 30:70 alloy (b, d, f) samples quenched from: a,b 500 °C; c,d 545 °C; e,f 600 °C.

Table 4

[001] \mathcal{E}_1 -Cu₃Sn - 1

[001] θ -Ag₃Sn - 2

[2110] η -Cu_cSn_s - 3

Figure 8 S/TEM data obtained from the phase mixture in the 40:60 alloy sample quenched from 600 °C: a BF STEM image; b d compositional maps obtained from the region in (a) showing the distribution of Ag, Cu, and Sn, respectively; e,f SADPs from

regions 1 and 2 in (a), respectively; (g) micro-diffraction pattern from region 3 in (a); h SADP obtained from an area including regions 1 and 2 in (a). The patterns in (e–h) are presented at the camera length.

samples quenched from 500 °C, the compositions of the micro-constituents in these samples were very consistent from region to region. Moreover, as can be seen from the values in Tables [3](#page-5-0) and [4,](#page-8-0) the compositions of these regions are extremely close to one another in the 50:50, 40:60, and 30:70 alloy. This is consistent with the phase mixture in the 40:60 and 30:70 alloy samples being the same combination of θ -Ag₃Sn and ε_1 -Cu₃Sn observed in the 50:50 alloy. Under these circumstances, the differences in the overall alloy composition must be accommodated by differences in the volume fractions of the microconstituents. The mean volume fractions of the $Cu₃Sn$ micro-constituent (as opposed to the total volume fractions of the Cu₃Sn phase including the Cu₃Sn in the phase mixture) measured for the 50:50, 40:60, and 30:70 alloy samples quenched from 545 $^{\circ}$ C were 22.6, 36.6, and 49.8 %, respectively.

The 40:60 alloy sample quenched from 600 \degree C exhibited a microstructure consisting of a homogeneously distributed phase mixture (Fig. [7](#page-8-0)e), which is significantly coarser than the mixtures in the samples quenched from 500 and 545 $°C$ (Fig. [7](#page-8-0)a, c, respectively). The morphology of this phase mixture is also different from those observed upon quenching from

these lower temperatures; in this case there are dark "feathery" dendritic structures with finer bright features between the dendrite arms. As expected, the composition of the mixture measured by EDXS corresponds closely to the nominal composition of the alloy. For the 30:70 alloy sample quenched from 600 °C , two micro-constituents are observed in the BSE SEM images (Fig. [7](#page-8-0)f): coarse Cu₃Sn grains and a phase mixture with a similar composition and morphology to, albeit somewhat finer than, that in the corresponding 40:60 alloy sample.

Although the phases mixtures in the 40:60 and 30:70 alloy samples quenched from 500 and 545 $^{\circ}$ C resemble those in the corresponding 50:50 alloy samples, the feathery dendritic mixtures in the samples quenched from 600 °C are clearly different. Here again, the characters of the phases in these mixtures were investigated by S/TEM analysis on FIB-cut TEM specimens, and a set of data from one such experiment on the 40:60 alloy sample quenched from 600 °C is shown in Fig. 8. The BF STEM image in Fig. 8a reveals a lobe from a dendrite (region 1) surrounded by a mixture of finer grains. The corresponding Ag, Cu, and Sn maps (Figs. 8b–d) and the $[00\bar{1}]$ SADP from region 1 (Fig. 8e) show that the

dendrite is composed of the ε_1 -Cu₃Sn phase. Most of the grains in the surrounding mixture are θ -Ag₃Sn, and an example of a [001] SADP from this phase is shown in Fig. [8](#page-9-0)f. There are some finer η -Cu₆Sn₅ grains, such as region 3 from which the $[2110]$ microdiffraction pattern in Fig. [8](#page-9-0)g was obtained. There are also some Sn-rich pockets, such as region 4, that are too small to give clear ZAPs, but are presumably β -Sn phase. We note that some of the θ -Ag₃Sn regions adjacent to the ε_1 -Cu₃Sn dendrites appeared to exhibit a simple low-index orientation relationship:

- $[00\bar{1}]$ Ag₃Sn // $[00\bar{1}]$ Cu₃Sn
- (010) Ag₃Sn $// (010)$ Cu₃Sn
- (100) Ag₃Sn $// (100)$ Cu₃Sn

Regions 1 and 2 in Fig. [8a](#page-9-0) are an example of this, as demonstrated in and the SADP obtained with the field limiting aperture surrounding these regions (Fig. [8](#page-9-0)h). The differences between the $[00\bar{1}]$ ZAPs for these isostructural compounds arise because the 110 and 200-type reflections in the $D0_a$ structure are chemically sensitive. These reflections are extremely weak in Ag₃Sn because the atomic scattering factors for Ag and Sn are very similar, as one might expect for elements with an atomic number difference of only 3. For $Cu₃Sn$, however, these reflections are fairly strong due to large differences in the atomic scattering factors. This is why the 110- and 200-type reflections from $Cu₃Sn$ are visible in Fig. [8](#page-9-0)h, but those from Ag3Sn are not.

Discussion

The phase equilibria in the Ag–Cu–Sn system have been described by Hari Kumar and Kubaschewski [\[26](#page-13-0), [27](#page-13-0)]. While recent attention has upon the Sn-rich corner of this system, the understanding of the transformations for alloys with the Sn-lean compositions considered here is based upon the earlier work of Gebhardt and Petzow [\[28](#page-13-0)] and Fedorov et al. [\[29](#page-13-0)] who produced isothermal sections and isopleths at 5– 25 wt% Sn. On this basis, one would expect the following transformation sequence upon cooling:

 $L \rightarrow L + \epsilon_1 \rightarrow L + \epsilon_1 + \epsilon_2 \rightarrow L + \epsilon_1 + \theta$ $\rightarrow \epsilon_1 + \theta + \eta$

Thus, the phases present in the as-cast structure correspond to those predicted by the equilibrium

phase diagram (i.e., mainly ε_1 -Cu₃Sn and θ -Ag₃Sn, with a little η -Cu₆Sn₅). Moreover, the DSC troughs observed upon heating can be reconciled with the processes expected from the phase diagram. The small invariant trough at 355 \degree C corresponds to the peritectic reaction:

$$
\eta \rightarrow \epsilon_1 + L
$$

As such, the η -Cu₆Sn₅ phase is absent from the microstructures in samples quenched from 400° C (e.g., Figure [4](#page-5-0)a). The larger invariant trough at 482 °C corresponds to the peritectic reaction:

 $\theta \rightarrow \epsilon_2 + L$

This results in more complex microstructures in samples quenched from 500 \degree C (Figs. [4b](#page-5-0), [7](#page-8-0)a, b). There are large grains of untransformed ε_1 -Cu₃Sn and θ -Ag₃Sn, plus a complex phase mixture of ε_2 -Ag₅Sn with ϵ_1 -Cu₃Sn, η -Cu₆Sn₅, and β -Sn, which form when the Cu- and Sn-rich liquid freezes around the ε_2 transformation product. Clearly, the presence of large regions of untransformed θ -Ag₃Sn indicates that the peritectic reaction is kinetically limited at these temperatures and heating rates. The second large invariant trough at 531 $°C$ corresponds to the congruent melting:

 $\epsilon_1 + \epsilon_2 \rightarrow L$

As such, in samples heated to $545 °C$, there is only liquid plus rather blocky ε_1 -Cu₃Sn phase present. Upon quenching from 545 $°C$, a fine eutectic mixture of ε_1 -Cu₃Sn and θ -Ag₃Sn forms (Figs. [4](#page-5-0)b, [7](#page-8-0)a, b).

Lastly, there is a broad trough whose temperature depends on the alloy composition. This lies at 561, 593, and 618 °C for the 50:50, 40:60, and 30:70 alloys, respectively. The trough corresponds to the melting of the ε_1 -Cu₃Sn phase, and therefore the temperatures at which these troughs occur are approximately those for the liquidus surface at these compositions. The samples quenched from $600 \degree C$ exhibit rather different microstructures. For the 50:50 alloy, the alloy is fully liquid at this temperature and quenching produces a refined microstructure (Fig. [4](#page-5-0)d) with primary ε_1 -Cu₃Sn and the same $\varepsilon_1 + \theta$ eutectic as in the samples quenched from 545 °C. For the 40:60 alloy, 600 \degree C is just beyond the trough and it is not clear whether a homogeneous liquid would be produced. Upon quenching from $600 \degree C$, we observe a mixture of feathery ε_1 -Cu₃Sn dendrites surrounded by grains of θ -Ag₃Sn, plus smaller grains of η -Cu₆Sn₅ and yet

smaller pockets of β -Sn (Fig. [7e](#page-8-0)). For the 30:70 alloy, $600 \degree$ C is below the trough and one would expect liquid plus coarse ε_1 -Cu₃Sn phase to be present. Upon quenching from $600 \,^{\circ}\text{C}$, the liquid solidifies into a phase mixture with a similar composition and morphology (if somewhat finer) to that for the 40:60 alloy (Fig. [7](#page-8-0)f).

While the transformations that occur upon heating are consistent with the published ternary phase diagrams, most of the solidification microstructures (both in as-cast and in quenched samples) do not correspond to what one might expect on this basis or based upon previous work on binary alloys (e.g., [\[22](#page-12-0)]). In the latter case, extended annealing was required to eliminate segregation effects and regions of high-temperature phases such as ε_2 -Ag₅Sn and γ -Cu₄Sn when producing samples of θ -Ag₃Sn and ε_1 -Cu₃Sn, respectively. No such effects were observed in the samples considered here. The ε_2 -Ag₅Sn phase was only observed in samples heated through the peritectic point at $482 °C$ and then quenched-in before this phase melts into a eutectic liquid at 531 °C. In all other samples, the phases present are θ -Ag₃Sn, ε_1 -Cu₃Sn, and in some cases η -Cu₆Sn₅ plus a little β -Sn. The most likely explanation for this is that the *nucleation* of the ε_2 -Ag₅Sn phase upon cooling is kinetically limited, and that the formation of this phase is suppressed in favor of the formation of the low-temperature equilibrium phases. It is difficult to prove this for the as-cast samples since the thermal history is not known accurately. As such, it is possible (although rather unlikely) that the ϵ_2 -Ag₅Sn phase forms and is then eliminated completely from the microstructure during slow cooling of the alloy ingots. For the samples quenched from $545 \degree C$, however, there is clearly insufficient time for such processes. The undercooling required to bypass the region of thermodynamic stability for the ε_2 -Ag₅Sn phase is only \approx 50 °C at these compositions, and so it seems reasonable that one should obtain a eutectic θ -Ag₃Sn + ε_1 -Cu₃Sn mixture around the remaining primary ε_1 -Cu₃Sn upon cooling. For the samples quenched from $600 \degree C$, the microstructures are different for the three alloys. In the 50:50 alloy the microstructure looks similar to those in the samples quenched from 545 °C with primary ε_1 -Cu₃Sn and eutectic θ -Ag₃Sn + ε_1 -Cu₃Sn. In the 40:60 alloy a different phase morphology is produced with feathery ε_1 -Cu₃Sn dendrites and an inter-dendritic mixture of θ -Ag₃Sn, η -Cu₆Sn₅ and β -Sn. The dendritic morphology and the orientation relationship between the dendrites and some of the adjacent θ -Ag₃Sn grains confirm that the ε_1 -Cu₃Sn forms first, rather than co-operatively as in the θ -Ag₃Sn + ε_1 -Cu₃Sn eutectic. The driving force for the formation of the ε_1 - $Cu₃Sn$ dendrites is presumably the concentration of Cu in the liquid, which is far higher than that at which the eutectic forms. The formation of a phase mixture with a similar composition and morphology in the 30:70 alloy quenched from 600 $^{\circ}$ C is consistent with this argument.

What is clear is that alloys with these compositions offer an interesting opportunity to study the characteristics and properties of the θ -Ag₃Sn and ε_1 -Cu₃Sn phases without needing to perform long-term annealing to eliminate metastable high-temperature phases. The only caveat to such studies would be that the effects of Cu in solid solution in θ -Ag₃Sn, and Ag in ε_1 -Cu₃Sn, would need to be taken into account.

Conclusions

The solidification microstructures and phase transformations in (Ag,Cu) ₃Sn alloys with Ag:Cu ratios of 50:50, 40:60, and 30:70 have been studied using XRD, electron microscopy, and DSC techniques. The main findings of this work are

- (1) The as-cast microstructures contain mainly the θ -Ag₃Sn and ε_1 -Cu₃Sn phases with a little η -Cu₆Sn₅. No metastable high-temperature phases or segregation was observed.
- (2) The DSC data obtained upon heating at 10 \degree C/ min revealed three invariant processes: one at 355 °C corresponding to $\eta \rightarrow \varepsilon_1$ + liquid; one at 482 °C corresponding to $\theta \rightarrow \epsilon_2$ -Ag₅Sn + liquid; and one at 531 \degree C corresponding to congruent melting of $\varepsilon_1 + \varepsilon_2$. A compositiondependent fourth process corresponding to melting of primary ε_1 .
- (3) Samples quenched from 400 \degree C contained θ and ε_1 grains but no η phase.
- (4) Samples quenched from $500 °C$ contained coarse θ and ε_1 grains plus a complex phase mixture of ε_1 , ε_2 , η , and β -Sn.
- (5) Samples quenched from 545° C contained coarse angular ε_1 grains plus a fine eutectic mixture of θ and ε_1 .
- (6) Samples quenched from 600 $^{\circ}$ C exhibited more diverse microstructures. The 50:50 alloy sample

contained fine ε_1 grains plus a eutectic mixture of θ and ε_1 . The 40:60 alloy sample contained fine feathery ε_1 grains with interdendritic θ , η , and β grains. The 30:70 alloy sample contained coarse ε_1 grains plus a refined version of the phase mixture in the 40:60 alloy sample.

The absence of the ε_2 phase in all but the samples quenched from 500 \degree C was accounted for on the basis of the nucleation of this phase being suppressed upon cooling giving instead eutectic θ and ε_1 , and other phase mixtures. These θ and ε_1 phases are thus formed far more readily than in the corresponding binary alloys, making these ternary compositions good model systems for studying the phases.

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Compliance with ethical standards

Conflict of Interest The authors declare that they have no conflict of interest.

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