

Plastic deformation behavior of ultrafine-grained Al–Mg–Sc alloy

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Abstract Ultrafine-grained (UFG) Al–Mg–Sc alloy was obtained by friction stir processing. The UFG alloy was subjected to uniaxial tensile testing to study the tensile deformation behavior of the alloy. An inhomogeneous yielding (Lüdering phenomenon) was observed in the stress–strain curves of UFG alloy. This deformation behavior was absent in the coarse-grained alloy. The Lüdering phenomenon in UFG alloy was attributed to the lack of dislocations in UFG microstructure. A strong dependence of uniform ductility on the average grain size was exhibited by the UFG alloy. Below a critical grain size (0.5 μm), ductility was very limited. Also, with the decrease in grain size, most of the plastic deformation was observed to be localized in necked region of the tensile samples. The negative strain rate sensitivity (SRS) observed for the UFG alloy was opposite of the SRS values reported for UFG alloys in the literature. Based on activation volume measurement, grain boundary mediated dislocation-based plasticity was concluded to be the micro-mechanism operative during plastic deformation of UFG Al–Mg–Sc alloy.

Introduction

Almost two decades of intensive research has gone into understanding the mechanical properties and deformation behavior of ultrafine grained (UFG) materials [1–3]. The scale of UFG microstructure, on the basis of grain size in polycrystalline materials, lies between 1 μm and 100 nm [4]. It is now well established that some of the mechanical properties of UFG materials are superior to, and the deformation behavior is different from their coarse-grained (CG) counterparts (grain size $>1 \mu\text{m}$) [5]. From mechanical properties point of view, the main motivation to refine grain size comes from the prediction made by Hall–Petch (HP) relationship [6, 7]. HP relationship relates yield strength (YS) and grain size (d) of a polycrystalline material as follows:

$$\sigma_y = \sigma_0 + k_y d^{-1/2} \quad (1)$$

where σ_y , σ_0 , and k_y are YS, friction stress, and HP coefficient, respectively. As per this relationship, the YS of a material goes up with a decrease in grain size. For example, the published literature shows that the YS of the CG 5XXX series Al alloys is limited upto 300 MPa. On grain refinement, UFG alloys have shown strength beyond 500 MPa [8–13]. Hence, grain refinement takes the strength level of 5XXX series Al alloys to the category of CG 2XXX and 7XXX Al alloys.

At present, there are various techniques available to obtain UFG microstructure in a wide variety of metals such as Al, Mg, Ti, Fe, etc. and their alloys [5, 14–19]. Among these, severe plastic deformation (SPD) techniques have been widely exploited because of their potential for commercialization in near future. Friction stir processing (FSP) is relatively new among all SPD techniques. Early studies

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on processing-microstructure-property relationship using FSP were limited to micron-size grain regime. Due to improved understanding of the processing, this technique is now being used to produce UFG microstructure [20–29]. The microstructural evolution during FSP has been studied very extensively. The continued research so far in this area has revealed that the microstructure evolved in the materials processed using FSP is distinctively different from those obtained by other SPD techniques. The grains in the processed region are equiaxed, homogeneous, and have relatively low dislocation density. For example, Su et al. [25] and recently, Ma et al. [26] and Kumar et al. [27–29] reported fraction of high angle grain boundaries (HAGB) to be >90 % in FSP UFG alloys. However, except a few studies concerning microstructure-property relationship in materials processed using FSP, there is a need to explore this relationship further in greater detail.

As mentioned before, UFG materials show very different mechanical properties and unique deformation behaviors. Apart from significant improvement in strength, UFG alloys exhibit enhanced strain rate sensitivity (SRS) [30–33]. Several fold increase in SRS values of UFG FCC materials compared to their CG counterparts have been observed. For example, Wei et al. [31] reported a SRS value of 0.02 for UFG Cu having mean grain size ~ 200 nm. The SRS of CG Cu is ~ 0.004 [34]. Hence, UFG Cu showed a five-fold increase in SRS. Although HP relationship has been shown to hold upto a grain size 10 nm in general, Valiev et al. [35] in a recent work have shown that extremely high YS of HPT processed UFG 7475Al and 1570Al cannot be explained on the basis of HP relationship. Another important difference shown by UFG metals and alloys is the presence of tension/compression asymmetry [36]. This has been attributed to an increase in free volume due to higher fraction of grain boundary per unit volume. Yield point phenomenon followed by Lüders band formation is another interesting feature of UFG alloys [37].

Hence, understanding of various properties in UFG regime is important both technologically and scientifically. In spite of such an extensive amount of work on UFG materials, processing of UFG alloy containing equiaxed and dislocation free grains with small distribution in grain size remains a challenge. Moreover, disappointingly low uniform elongation exhibited by UFG remains another handicap for any practical uses of this class of materials. Compilation of the literature data by Koch [38] and Mukai et al. [39] supports this observation.

Although there have been some attempts to understand the underlying deformation mechanisms of UFG alloys, it is still far from fully understood phenomenon. It, therefore, necessitates further research to establish a correlation between microstructure-properties of UFG materials. The present research deals with the plastic deformation

behaviors of UFG Al–Mg–Sc alloy. The strength, ductility, SRS, and work hardening rate have been explored for FSP UFG Al–Mg–Sc alloy. Special emphasis has been laid upon the ductility and necking instability. An optical microscope was used to study the neck formation in CG and UFG Al–Mg–Sc alloy. Work hardening rate has been evaluated in terms of grain boundary character and its spacing. Plastic deformation mechanism has been discussed on the basis of SRS measurement experiments.

Experimental details

Processing of the material

A ~ 3.75 -mm-thick twin-roll cast (TRC) Al–Mg–Sc alloy (nominal composition: Al-4Mg-0.8Sc-0.08 wt%Zr) was subjected to various thermo-mechanical processing (TMP) procedures to obtain the alloy in different microstructural conditions. The aging of the alloy was carried out at 563 K (290 °C) for 22 h. FSP was carried out in two different microstructural states: AR and AR+Aged. The FSP of AR and AR+Aged samples were carried out at two different tool rotation rates: 400 and 325 rpm while keeping other FSP parameters same. The details of FSP can be found elsewhere [29]. Table 1 summarizes all the processing conditions under which samples were subjected to quasi-static uniaxial tensile testing.

Uniaxial tensile testing

Samples in various TMP conditions were subjected to uniaxial tensile testing to evaluate the mechanical properties of the alloy. The microstructural state before FSP has an influence on the microstructure evolution during FSP. Different microstructural evolution paths may have its bearing on the mechanical properties. Aging heat treatment at 563 K (290 °C) for 22 h was given to TRC alloy before FSP, and it was followed by tensile testing to study this aspect of processing-property relation. The purpose of testing samples in different TMP conditions was to

Table 1 The thermomechanical conditions of the samples which were subjected to uniaxial tensile testing

Thermomechanical conditions	Uniaxial tensile testing
As-received (AR)	YES
AR+Aged (290 °C, 22 h)	YES
Friction stir processing (FSP)	YES
AR+Aged (290 °C, 22 h)+FSP	YES
AR+Aged (290 °C, 22 h)+FSP+Aged (290 °C, 22 h)	YES

compare mechanical properties of the samples containing different UFG microstructures. All the testings were carried out at room temperature (RT) at an initial strain rate ($\dot{\epsilon}$) of 10^{-3} s^{-1} . To determine the SRS value of UFG alloy, the samples were subjected to strain rate jump test. The gage length, width, and thickness of the mini-tensile samples for AR and AR+Aged conditions were 5.00, ~ 0.95 , and 0.95 mm, respectively, and for the rest of the conditions ~ 5.0 , ~ 1.2 , and ~ 1.0 mm, respectively. All tensile samples were polished using water-based polycrystalline diamond suspension from 15 to 1 μm grit size.

Results and discussion

Quasi-static mechanical properties

Stress–strain and strength–ductility relationships

The engineering stress–engineering strain curves for TRC Al–Mg–Sc alloy in various TMP conditions are shown in Fig. 1. This alloy in AR condition possessed a YS and UTS of 204 ± 4 and 293 ± 4 MPa, respectively. The elongation-to-failure (e_f) is $27.2 \pm 1.2 \%$ out of which $\sim 68 \%$ constituted the uniform elongation (e_u). On aging at 563 K (290 °C) for 22 h, the YS increased to 366 ± 8 MPa and UTS to 418 ± 4 MPa. As expected, a significant drop in e_f was observed which changed from $27.2 \pm 1.2 \%$ in AR condition to $11.1 \pm 3.6 \%$ —a drop of $\sim 60 \%$. Still, e_u in this condition was $\sim 61 \%$ of e_f . However, after FSP of the alloy in AR condition at 400 rpm (henceforth referred to as UFG-1), not only improvement in the YS and UTS was observed, but e_f was also very high (24.4 %). It should be noted that in spite of a considerable improvement in strength level for UFG-1, the ductility level (e_f) attained

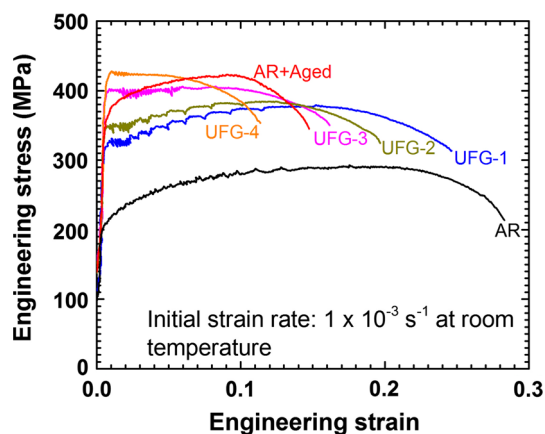


Fig. 1 Engineering stress–engineering strain curves of coarse-grained (CG) and ultrafine-grained (UFG) Al–Mg–Sc alloy (UFG-1: FSP (400 rpm), UFG-2: Aged+FSP (400 rpm), UFG-3: FSP (325 rpm), UFG-4: Aged+FSP (325 rpm))

was quite comparable to that exhibited in AR condition. The YS, UTS, e_f , e_u , and non-uniform elongation e_{nu} for TRC alloy processed under various conditions are summarized in Table 2. As can be noted, the Aged+FSP(325) (henceforth referred to as UFG-4; 325 in the bracket means 325 rpm) showed a strength level better than TRC+Aged condition with almost same level of e_f .

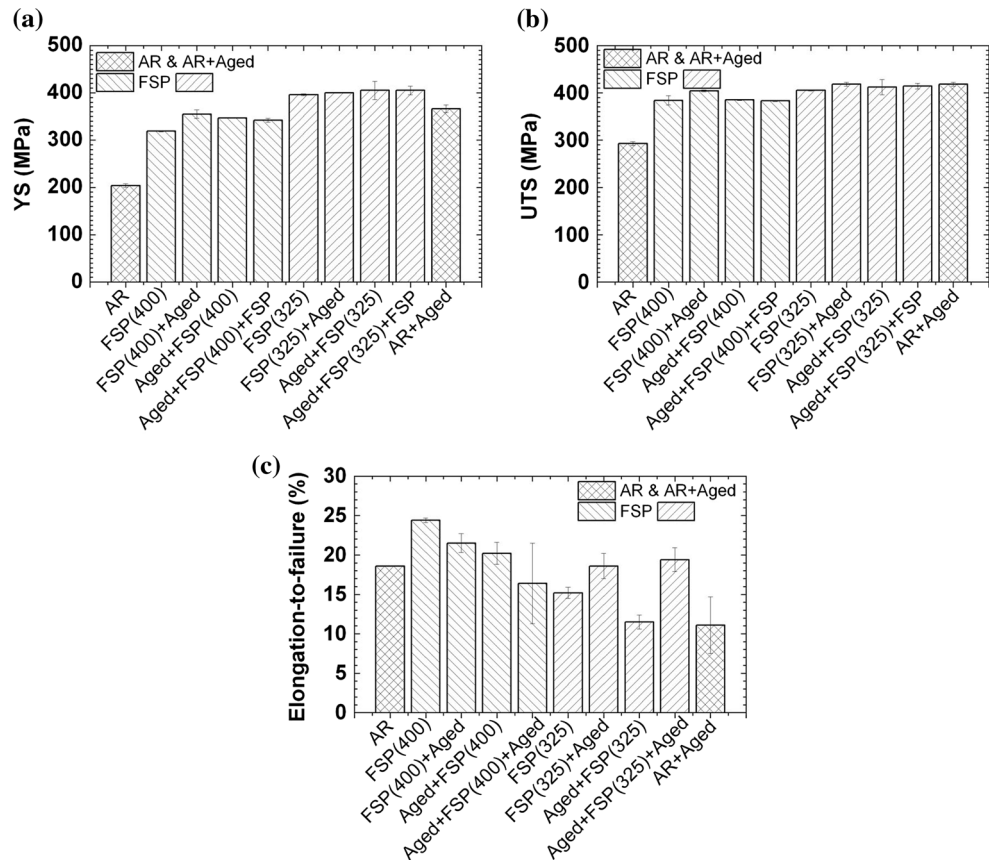
To understand the effect of post-FSP heat treatment, the FSP alloys were subjected to aging heat treatment at 563 K (290 °C) for 22 h. The effects of this aging heat treatment on tensile properties have been shown in the form of histograms in Fig. 2. Aging of UFG-1 showed improvement in YS and UTS, but there was no improvement in YS and UTS on aging of Aged+FSP(400) (henceforth referred to as UFG-2). Unlike UFG-1, FSP(325) (henceforth referred to as UFG-3) did not show any improvement in YS and showed very slight increase in UTS on aging. After aging of UFG-4, like UFG-2, no improvement in YS and UTS was observed. The TRC alloy processed at 400 rpm and 325 rpm with different microstructural conditions responded differently to post-FSP aging heat treatment as far as e_f of the processed alloy is concerned. As can be noted from Fig. 2c, ductility dropped for UFG-1 after aging. This is an expected behavior, because the strength of the TRC alloy in this condition increased after aging. It is well known that the ductility of the alloys decreases as strength increases. Although aging heat treatment did not cause any change in the YS and UTS for UFG-2, a drop in ductility can be observed. In case of aging of UFG-3 and UFG-4 (Aged+FSP(400)+Aged and Aged+FSP(325)+Aged) increase in ductility values are observed. The YS, UTS, and % e_f values of post-FSP samples are summarized in Table 3.

The strength–ductility of the present alloy is shown in Fig. 3 and a comparison has been made with various CG and UFG Al alloys reported in the literature [8–13, 41–45]. Figure 3a shows the variation of YS with e_f of presently investigated TRC CG and UFG Al–Mg–Sc alloy and was compared with 5XXX CG and UFG Al alloys reported in the literature [8–13]. The strength–ductility values for majority of the 5XXX series Al alloys in CG and UFG conditions fall into the band shown in Fig. 3a. However, as can be noted, FSP UFG alloy in some of the TMP conditions lies outside the band. Evidently, FSP resulted in a better combination of strength and ductility. Further comparison of the TRC CG and UFG Al–Mg–Sc alloy with precipitation strengthened 2XXX, 6XXX, and 7XXX Al alloys revealed that strength (YS and UTS) of the presently investigated alloy was better than most of the CG 6XXX Al alloys, and strength was comparable to some of 2XXX and 7XXX Al alloys. For the same strength level, the ductility (e_f) was observed to be better than all these alloys. The variation of YS with ductility for 2XXX, 6XXX, and 7XXX alloys and their comparison with currently investigated alloy are shown

Table 2 The results of uniaxial mini-tensile testing of TRC Al–Mg–Sc alloy in various thermo-mechanical conditions

	YS (MPa)	UTS (MPa)	% e_f	% e_u	% e_{nu}
TRC	204 ± 4	293 ± 4	27.2 ± 1.2	18.6 ± 0.0	8.6 ± 0.9
TRC+Aged	366 ± 8	418 ± 4	11.1 ± 3.6	6.8 ± 2.4	4.3 ± 1.2
FSP(400) (UFG-1)	319 ± 1	384 ± 10	24.4 ± 0.3	14.3 ± 0.2	10.1 ± 0.0
Aged+FSP(400) (UFG-2)	347 ± 1	385 ± 1	20.2 ± 1.4	11.6 ± 0.3	8.6 ± 1.1
FSP(325) (UFG-3)	396 ± 2	405 ± 1	15.2 ± 0.7	7.2 ± 0.6	8.0 ± 0.0
Aged+FSP(325) (UFG-4)	405 ± 19	412 ± 16	11.5 ± 0.9	3.4 ± 1.1	8.1 ± 0.2

Fig. 2 A comparison of the **a** YS, **b** UTS, and **c** ductility of FSP UFG Al–Mg–Sc alloy with AR and AR+Aged alloy. Included is the effect of pre- and post-FSP aging



in Fig. 3b. The mechanical properties of Al–Mg–Sc with or without Zr have been investigated in the past by many researchers [41–45]. A comparison of the present dataset with those in the literature on Al–Mg–Sc (Zr) showed a superior combination of strength and ductility as illustrated in Fig. 3c.

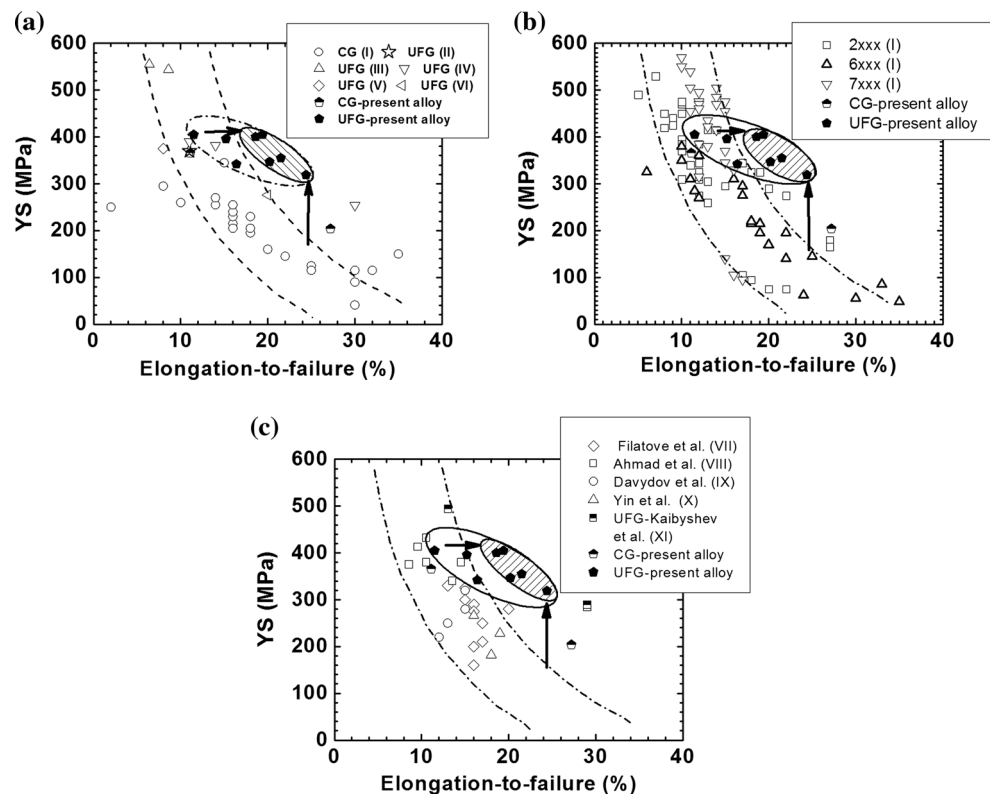
Ductility of UFG Al–Mg–Sc alloy

Extensive research on UFG alloys has been carried out in last two decades due to their scientific and technological importance [1, 2, 46]. The research carried out so far indicates a significantly different deformation behavior and mechanisms for UFG alloys in comparison with their CG counterparts. A disappointingly low uniform ductility (e_u)

shown by UFG alloys has been a bottleneck in the widespread use of these alloys. Compilation of the literature data by Koch [38] and Mukai [39] reveals that elongation (ductility) and grain size are proportionately related, i.e., ductility of the metallic materials decreases with decrease in grain size. To understand the relationship between grain size and ductility of the present UFG alloy, elongation versus grain size plot was created and is shown in Fig. 4a. It shows variation of e_f , e_u , and e_{nu} as a function of average grain size. AR and AR+Aged materials belong to CG regime. As noted by Koch [38] and Mukai [39], here also a wide variation in ductility in these two conditions can be observed. The trend line shown in Fig. 4a does not consider the elongation values of AR+Aged samples. As can be noted, there is a sharp decline in ductility in UFG regime

Table 3 The effect of post-FSP aging heat treatment on the uniaxial tensile mechanical properties of TRC Al–Mg–Sc alloy in various thermo-mechanical conditions

	YS (MPa)	UTS (MPa)	% e_f	% e_u	% e_{nu}
FSP(400)+Aged	355 ± 9	404 ± 2	21.5 ± 1.2	11.1 ± 1.7	10.4 ± 0.5
Aged+FSP(400)+Aged	342 ± 4	383 ± 7	16.4 ± 5.1	9.4 ± 0.4	7.0 ± 5.5
FSP(325)+Aged	400 ± 1	418 ± 4	18.6 ± 1.6	7.3 ± 1.1	11.3 ± 2.6
Aged+FSP(325)+Aged	405 ± 9	414 ± 6	19.4 ± 1.5	4.7 ± 0.0	11.4 ± 1.4

Fig. 3 Comparison of presently investigated Al–Mg–Sc alloys with those in the literature; **a** CG and UFG 5XXX series Al alloys (I–VI: [8–13]), **b** 2XXX, 6XXX, and 7XXX Al alloys (I: [8]), **c** CG and UFG Al–Mg–Sc (Zr) alloys (VII–XI: [41–45])

with decrease in grain size. The UFG-1 (grain size— $0.73 \pm 0.44 \mu\text{m}$) showed a considerably high level of elongation (both in terms of e_f and e_u). Although the total elongation exhibited by UFG-4 ($0.39 \pm 0.16 \mu\text{m}$) was little higher than 10 %, it showed a very small uniform elongation (<4 %). It, therefore, suggests that mere consideration of e_f gives a false impression about the true nature of UFG materials in terms of useful elongation available.

This dependence of uniform ductility on grain size was explained recently by Kumar et al. [27] on the basis of relationship between dislocation mean free path and grain size. It was shown that the dislocation mean free path was of the same order as grain size in UFG-4 material. Direct interaction with HAGB led to enhanced recovery rate. It resulted in lower work hardening capacity of the material and hence early onset of plastic instability. Total elongation,

e_f , and uniform elongation, e_u , both showed the same trend with change in grain size. However, with the change in grain size, non-uniform elongation (e_{nu}) part did not change much as evident from the horizontal trend line. It indicates that fraction of e_{nu} increased with the decrease in grain size. The variations in the fraction of e_u and e_{nu} are shown in Fig. 4b. Clearly, the fraction of e_{nu} increased with decrease in grain size, whereas a decrease in the fraction of e_u was observed with decrease in grain size. This increase in non-uniform elongation in UFG samples is reflected in the geometry of the fractured samples in uniaxial tensile testing as well.

UFG and necking phenomenon

In the analysis of work hardening rate of CG material, stress–strain curves upto UTS were considered. In CG material, load drop is generally associated with necking

Fig. 4 **a** The variation of elongation as a function of grain size and **b** variation of fraction of uniform and non-uniform elongation as a function of grain size

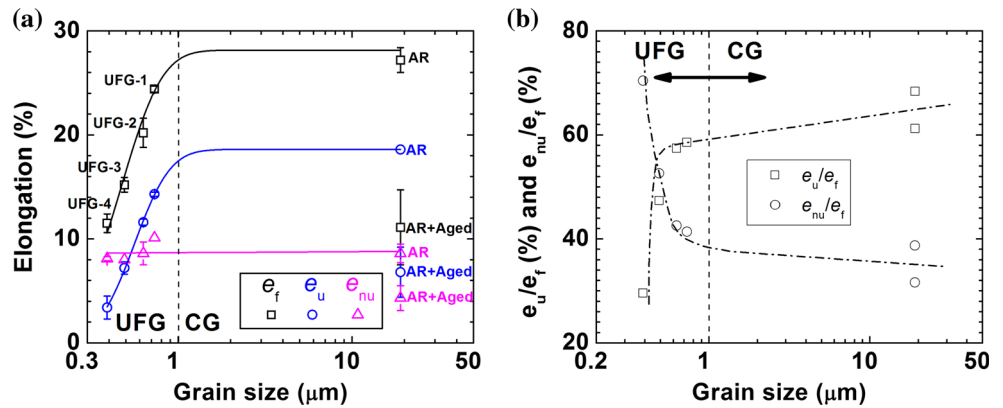
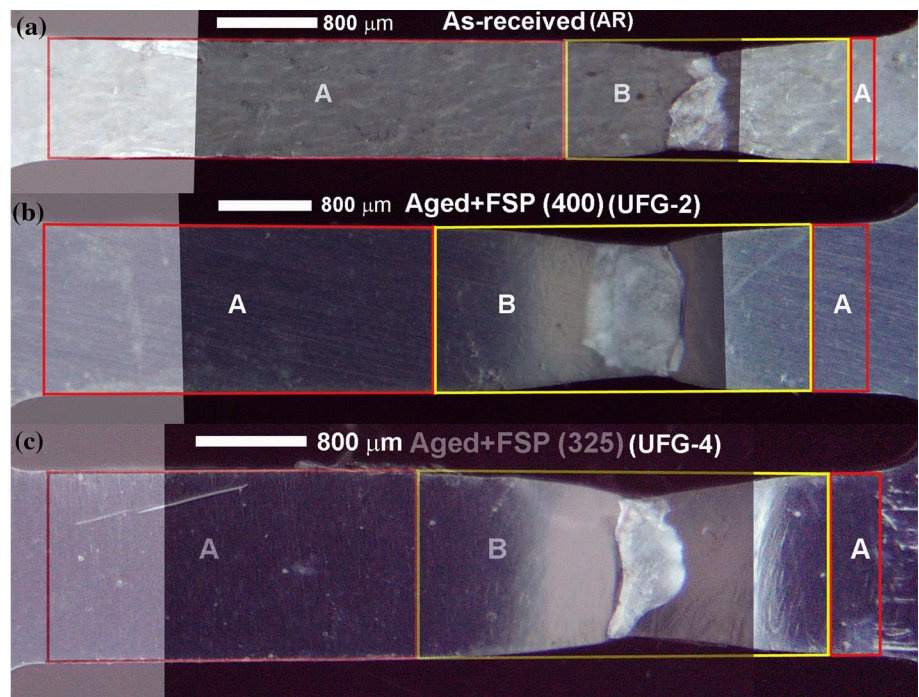


Fig. 5 Mini-tensile fractured sample showing uniformly elongated (A) and necked (B) regions for **a** AR, **b** UFG-2 and **c** UFG-4 samples



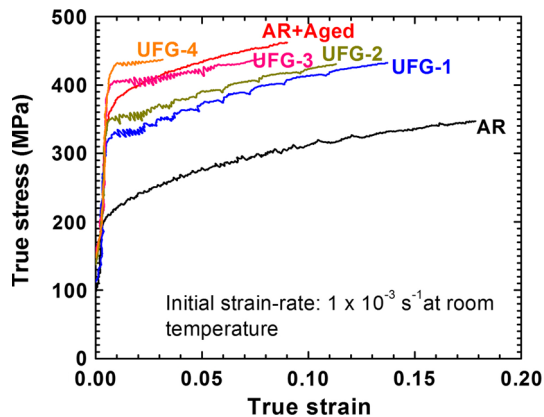
phenomenon when material is tested under uniaxial tensile loading condition. It may not be the case for UFG materials. Fractured mini-tensile samples related to CG and UFG materials in AR, UFG-2, and UFG-4 conditions were observed under optical microscope after uniaxial tensile testing. Both the parts of the fractured mini-tensile samples were joined in image analysis software Adobe Photoshop. These joined samples are shown in Fig. 5. The uniform elongation values were estimated from these fractured samples by measuring the change in width and thickness of regions designated as region A in Fig. 5 (here only top view of the fractured tensile samples is shown). The area marked B represents necked region. The results from this analysis are summarized in Table 4. It should be noted that measured elongation values from fractured samples are close to those obtained from stress–strain curves. The

measurement of e_u of UFG-4 was not possible from the optical images due to very small change in dimensions. It can be attributed to the resolution limit of the microscope used and measurement errors.

In recent literature, it has been discussed that necking is delayed in UFG materials due to enhanced SRS [47]. This may be the case where SRS values are very high, such as in the case of superplasticity phenomenon. However, the SRS values lie in the range of 0.01–0.04 for UFG Al alloys [40], and in alloys showing dynamic strain aging (DSA), (as is the case for the presently investigated CG and UFG Al–Mg–Sc alloy) even negative SRS has been reported (see “Strain rate sensitivity and activation volume” Section for a detailed discussion on it). For strain rate sensitive materials, neck instability phenomenon is described using Hart’s criterion of neck instability [48]. However, for such

Table 4 Comparison of elongation values measured using LVDT and on fractured samples

	Elongation values measured from fractured samples			Elongation values measured from stress–strain curves		
	e_f	e_u	e_{nu}	e_f	e_u	e_{nu}
AR	24.3 ± 1.0	13.0 ± 3.2	11.4 ± 2.2	27.2 ± 1.2	18.6 ± 0.0	8.6 ± 0.9
UFG-2	17.7 ± 3.3	7.3 ± 1.2	10.4 ± 2.1	20.2 ± 1.4	11.6 ± 0.3	8.6 ± 1.1
UFG-4	12.2 ± 1.2	0.0	12.2 ± 1.2	11.5 ± 0.9	3.4 ± 1.1	8.1 ± 0.2

**Fig. 6** True stress–strain curves of coarse-grained (CG) and ultrafine-grained (UFG) Al–Mg–Sc alloy (UFG-1: FSP (400 rpm), UFG-2: Aged+FSP (400 rpm), UFG-3: FSP (325 rpm), UFG-4: Aged+FSP (325 rpm))

small values of SRS (either positive or negative), neck formation criterion reduces to the formulation proposed by Considère [49]. Hence, for CG and UFG Al alloys, uniform ductility is mainly governed by strain hardening rate which is greatly influenced by the microstructural state of the material. Kapoor et al. [40] also have pointed out that this level of SRS values of UFG Al alloys might not be sufficient to cause delay in necking in UFG samples tested under tensile conditions. The present result from the measurement of e_u from optical images and from stress–strain curves indicates that necking might have started near UTS in UFG materials also.

Strain hardening rate

As discussed before, strain hardening and uniform ductility exhibited by materials are related. To study the strain hardening behavior of the UFG alloy, engineering stress–engineering strain curves upto UTS were converted into true stress (σ)–true strain (ε) curves (Fig. 6). Specimens AR, AR+Aged, UFG-1, and UFG-2 showed work hardening during deformation. However, UFG-3 exhibited significantly reduced strain hardening capacity, and UFG-4 showed almost a perfectly elasto-plastic behavior. These true stress–strain curves were further used to construct $d\sigma/d\varepsilon$

versus σ plot (Fig. 7). As can be noted, the initial part of the SHR curve corresponding to AR showed a linear decrease in the SHR. The later stage of the work hardening rate curve also showed a linear variation but at a slower rate than the initial stage. This is generally associated with the change in stage III hardening to stage IV hardening [50]. However, it should be emphasized that each stage of work hardening is characterized by characteristic microstructural development, and in the absence of microstructural information, it cannot be confirmed whether such a transition took place during deformation. Like AR material, the alloy in other conditions also showed similar trends in SHR variation. The linear regions of each curve can be approximated with an expression based on Voce law [50] which is given as

$$\frac{d\sigma}{d\varepsilon} = \frac{\alpha G b k_1}{2} - \frac{k_2 \sigma}{2} \quad (2)$$

where α , k_1 , and k_2 are a constant, a thermal dislocation storage, and recovery terms, respectively. Other symbols have their usual meaning. Linear curve fitting was carried out for upper and lower linear portions of the work hardening rate versus true stress curves and is shown in Fig. 7. In Eq. (2), first term on right-hand side (referred to as θ_0) represents maximum work hardening rate (where macroscopic yielding begins) and second term recovery. In the plot of $d\sigma/d\varepsilon$ versus σ , the slope of the curves represents $k_2/2$. Based on linear curve fitting, θ_0 (intercept) and $k_2/2$ (slope) are summarized in Table 5.

The slopes of the lower linear regions of the curves shown in Fig. 7 varied from 3.8 to 15 whereas intercept values from 620 to 1991 (Table 5). From the slope values of lower linear region (which represents rate of recovery) (Table 5), it can be stated that AR+Aged should show minimum uniform elongation whereas maximum value would be expected for UFG-4. However, Table 2 shows that UFG-4 showed minimum uniform elongation. This variation in slopes (3.8–15) can be treated as quite small and concluded that this alloy in different thermo-mechanical conditions exhibits similar rate of recovery in lower linear regime. No clear trend emerges between uniform elongation and intercept values (Table 5) of lower linear regime.

From the intercept values obtained based on the analysis of upper linear region, a clear trend appears to emerge

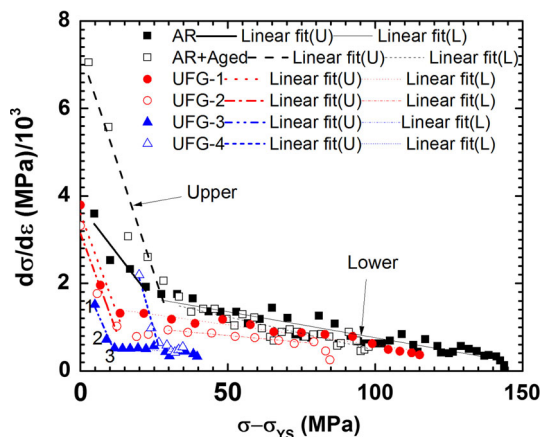


Fig. 7 The Kocks–Mecking (K–M) plot showing work hardening behavior of CG and UFG TRC Al–Mg–Sc alloy

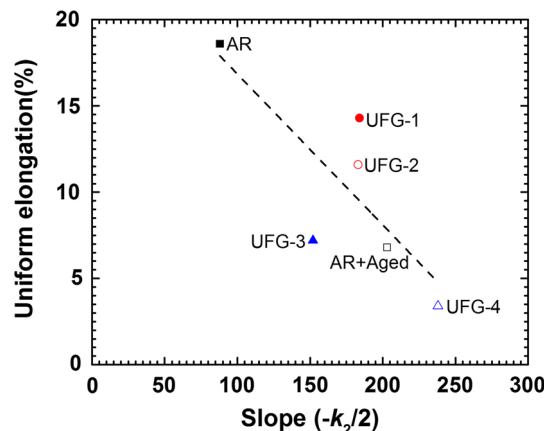


Fig. 8 The variation of uniform elongation as a function of slope of upper linear region of K–M plot in Fig. 7

Table 5 A summary of work hardening parameters obtained by linear curve fitting of work hardening rate curves shown in Fig. 7

Material condition	Upper linear region		Lower linear region	
	Slope ($-k_2/2$)	Intercept (θ_0)	Slope ($-k_2/2$)	Intercept (θ_0)
AR	88	3772	12	1945
AR+Aged	203	7288	15	1991
UFG-1	184	3597	9.3	1520
UFG-2	183	3142	6.2	1118
UFG-3 ^a	152 (199)	2210 (2491)	5.2	602
UFG-4	238	6867	3.8	620

^aRefer to text in “Strain hardening rate” section for the interpretation of values shown in brackets)

between uniform elongation and intercept of this material in different microstructural conditions. However, slope of upper linear region seems to have a better correlation with uniform elongation. The slope of the upper linear region for AR condition was the lowest, whereas the slope was the highest for UFG-4. Figure 8 establishes relationship between uniform elongation and slope of the upper linear region of curves shown in Fig. 7. Overall, uniform ductility appears to follow a linear relationship and decreases with increase in slope or rate of recovery. It should be pointed out here that UFG-3 showed a slope of 152 which was smaller than the slope values of UFG-1 and UFG-2. However, the uniform elongation corresponding to UFG-3 condition was also smaller than that of UFG-1 and UFG-2. It may be a result of insufficient data in the upper linear regime of UFG-3. If for linear curve fitting, only datum points 1 and 2 are considered (Fig. 7), the slope is 199 which is quite close to the slope obtained for AR+Aged (203). The uniform elongation values for UFG-3 and

AR+Aged conditions are quite close to each other. Despite such discrepancies, overall, there is a linear relationship between uniform elongation and rate of recovery as evident from Fig. 8.

In UFG materials, higher rate of recovery and hence lower strain hardening rate have been associated with early onset of plastic instability and consequently lower uniform ductility [37, 38, 51, 52]. Since, grain refinement causes flow stress to rise considerably in UFG materials, and at the same time, work hardening rate is impaired due to higher recovery rate; condition of plastic instability [48, 49] during uniaxial tensile testing is met very early resulting in lower uniform elongation. UFG-3 (based on slope calculation using points 1 and 2; Fig. 7) and UFG-4 not only showed a very high rate of recovery compared to others, but also the later part of curve had almost a constant SHR unlike other curves where a gradual decrease in SHR can be observed. It, therefore, appears that high work hardening rate and lower rate of recovery are two very important prerequisites for obtaining an acceptable level of uniform ductility in materials. In fact, Wang et al. [51] successfully induced very high work hardening capability by introducing bimodal grain size distribution using a suitable TMP treatment in nanostructured/UFG copper. The coarser grains in this material provided required work hardening to sustain uniform deformation during the deformation. In the absence of such microstructure, the UFG copper showed almost negligible uniform elongation.

Strain rate sensitivity and activation volume

SRS measurement provides an insight into the deformation mechanisms operative at that length scale. UFG alloys have shown to possess different deformation mechanisms from their CG counterparts. SRS studies on FCC materials have

shown that its values increase with decrease in grain size [10, 30, 31, 53, 54]. In the present study, UFG-2 was subjected to strain rate jump test to estimate the SRS of FSP UFG Al–Mg–Sc alloy. It was further used to calculate apparent activation volume. The analytical expression used to calculate SRS is given as

$$m = \frac{\partial \ln \sigma}{\partial \ln \dot{\epsilon}} \quad (3)$$

where m is SRS. The apparent activation volume, v , is calculated as follows:

$$v = \frac{Mk_B T}{\sigma m} \quad (4)$$

where M , k_B , and T are Taylor's factor equal to 3.06 for a polycrystalline FCC material having random texture, Boltzmann constant (J/K), and test temperature (K), respectively.

The result of the strain rate jump test on UFG-2 alloy is shown in Fig. 9a along with the literature data on SRS of FCC and BCC materials as a function of grain size (Fig. 9b). Overall, the trend for FCC materials is an increasing SRS with decreasing grain size. Figure 9a shows the true stress–true strain curves obtained during strain rate jump test. It shows two curves—one was obtained by changing the strain rate from lower (0.001 s^{-1}) to higher (0.01 s^{-1}) and other one from 0.01 to 0.0001 s^{-1} . In each case, the material was deformed at the changed strain rate for a pre-specified amount of strain before changing the strain rate back to the starting value. In the first case, the stress level dropped on raising the strain rate value. In the second case, the stress level increased on decreasing the strain rate from 0.01 to 0.0001 s^{-1} . Also, the changes in stress values are quite different in these two cases. The change in stress value is lower where strain rate

was changed from 0.001 to 0.01 s^{-1} compared to the case where strain rate was changed from 0.01 to 0.0001 s^{-1} . It was 10 and 18 MPa, respectively.

The m values calculated using Eq. (3) were quite close, and an average value of -0.011 is shown in Fig. 9b. Clearly, the present alloy showed *negative strain rate sensitivity* (nSRS). In CG Al–Mg alloys, the nSRS phenomenon is quite common [49, 55] and has been associated with DSA phenomenon [49]. Given the fact that FCC UFG Al and its alloys show enhanced SRS (see Fig. 9b for commercially pure Al), nSRS shown by UFG-2 condition is of interest. Careful observation of the stress–strain curves in Fig. 1 reveals that AR alloy shows serrations which are drastically reduced or get eliminated on aging (AR+Aged). However, UFG-1 and UFG-2 both showed pronounced serrations in the stress–strain curves. Hence, nSRS phenomenon observed for UFG Al–Mg–Sc alloy is not unexpected. Also, AR and AR+Aged should show either zero or very small nSRS values. The nSRS in UFG or nanostructured Al alloys has been reported by many other researchers also [56–58]. The nSRS values from the work of these researchers are included in Fig. 9b. Ahn et al. [57] observed a small positive SRS value of 0.0025 for 5083Al alloy having an average grain size of $140 \mu\text{m}$ which decreased to -0.0108 on refining the grain size to 252 nm . The observation of nSRS was rationalized on the basis of enhanced interaction of solutes and dislocations at grain boundaries by these authors. Solute concentration has been shown to increase with decrease in the grain size [59]. Also, in UFG materials, grain boundaries have been shown to be better source and sink of dislocations [10, 30, 31, 33, 53, 60, 61]. Hence, at lower strain rate, solutes get enough time to pin the dislocations at grain boundaries. It raises the stress level necessary to drive the dislocations and consequently results in nSRS behavior. However, in ECAP processed UFG Al–Mg alloys, nSRS was suppressed. For example, Kapoor et al. [62] reported that Al–Mg alloy exhibited nSRS in

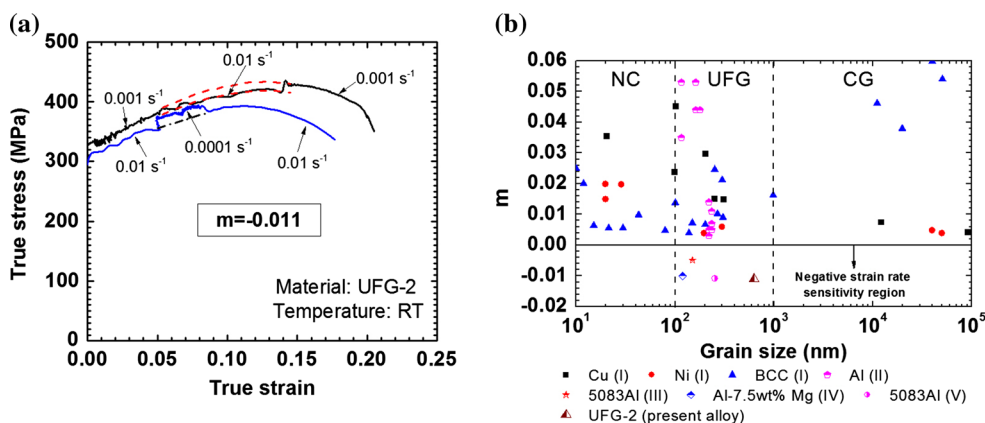


Fig. 9 Plot showing **a** strain rate jump test for UFG-2 alloy for the determination of strain rate sensitivity, and **b** the strain rate sensitivity of several FCC and BCC material along with presently investigated

alloy as a function of grain size ranging from CG to NC regime (I–III: [31], IV: [10], V: [56], VI: [58], VII: [57])

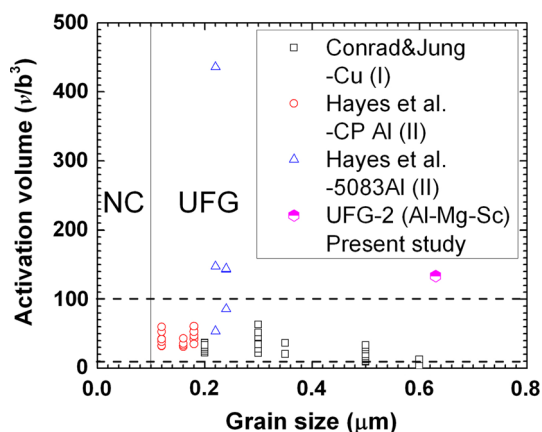


Fig. 10 Activation volume of UFG Al alloys along with the presently investigated FSP UFG alloy as a function of grain size (I, II: [10, 33])

annealed condition, whereas ECAP-12B_C showed a positive SRS. A similar observation was made in an earlier study by Muñoz-Morris et al. [63]. A positive SRS of ECAP processed Al–Mg alloy was rationalized on the basis of high dislocation density in ECAP processed materials causing high number of mobile dislocation and a small number of Mg atoms available per dislocations. It should be noted that FSP is a high temperature processing technique, and microstructure evolved during processing has very low dislocation density. Hence, Mg atoms per dislocation may be sufficient to introduce nSRS in UFG condition.

The apparent activation volume (*v*) calculated using Eq. (4) is shown in Fig. 10 [10, 33]. In the calculation of *v*, absolute value of *m* was used in Eq. (4). For comparison, the literature data on apparent activation volume are shown for UFG FCC materials in the same figure. Evidently, the *v* value of the UFG-2 alloy is very close to the reported literature data on apparent activation volume for UFG FCC materials. As mentioned before, the knowledge of the activation volume gives an insight into the operative deformation mechanism(s) during plastic deformation of materials. The smallest activation volume is obtained for those processes where vacancy-assisted diffusion processes are operative—for example, Coble creep, grain boundary shear, etc. In such cases, activation volume is expected to be 1–10b³ [54, 64]. As shown in Fig. 10, in the UFG regime, most of the reported values lie in the range of 10–100b³ with only a few values lying outside it [33, 53, 65–67]. Wei and Gao [54] have rationalized the activation volume of vacancy-assisted diffusion processes and dislocation-assisted deformation processes as follows:

$$v = \begin{cases} \sim V_a & \text{for vacancy assisted diffusion} \\ \alpha V_a d/b & \text{for dislocation based processes} \end{cases} \quad (5)$$

where *V_a* and *α* are atomic volume and a geometrical factor, respectively. For dislocation-based processes, if

only atoms associated with dislocation cores are considered, the length of the dislocations which would get activated should be proportional to the grain size. Hence, reduction in grain size would result in a decrease in activation volume. Wei et al. [31] also have considered grain size to be the obstacle spacing in UFG FCC materials in the development of a model to explain the decrease in activation volume with grain size. Conrad and Jung [33] have explained decrease in activation volume by a model based on grain boundary shear promoted by dislocation pile-up models. There may be differences in opinion among researchers about the details of exact mechanism operative during plastic deformation, but the role of grain boundaries as sources and sinks of dislocations has been accepted by many researchers for UFG materials [10, 30, 31, 33, 53, 60, 61]. Based on the activation volume value for UFG-2, it can be speculated that a dislocation-mediated plasticity might be at play, and grain boundaries are probably acting as a source for those dislocations.

Lüders band formation in UFG materials

As mentioned in the Introduction section of this paper, Lüders deformation is another interesting and unique feature of the UFG alloys. The Lüders band formation was observed in currently investigated FSP UFG Al–Mg–Sc alloy. The signature of its formation is embedded in the stress–strain curves in Fig. 1 for UFG-1 to UFG-4 alloys in the form of serrations just after yielding. Such deformation behavior was not exhibited by AR and AR+Aged Al–Mg–Sc alloy. Hence, observation of this phenomenon is not just a manifestation of dislocation-solute interaction, as commonly observed for substitutional and interstitial solid solutions, but also a reflection of complex interplays between dislocations and grain size.

The formation of Lüders deformation bands in fine grained Al and its alloys has been reported by Deep and Plumtree [68], Lloyd and Morris [69], and Wyrzykowski and Grabski [70] in the past and recently by Yu et al. [4], Hung et al. [71], and a few others in UFG Al. Deep and Plumtree [68] attributed occurrence of this phenomenon to the very fine recrystallized microstructure (grain size—0.5 μm to 2 μm) in which all the dislocations were expected to be immobile. Similarly, others also have attributed this deformation behavior to the lack of mobile dislocations [4, 69–71]. To test the hypothesis of lack of mobile dislocations as the origin for the appearance of Lüders deformation in UFG alloys, the present UFG-1 alloy was given 50 % thickness reduction by cold rolling to introduce mobile dislocations in the grain structure. It was followed by mini-tensile testing. In this microstructural condition, no Lüders deformation phenomenon was observed in the stress–strain curve (Fig. 11). Since lack of dislocations is the reason for the occurrence of

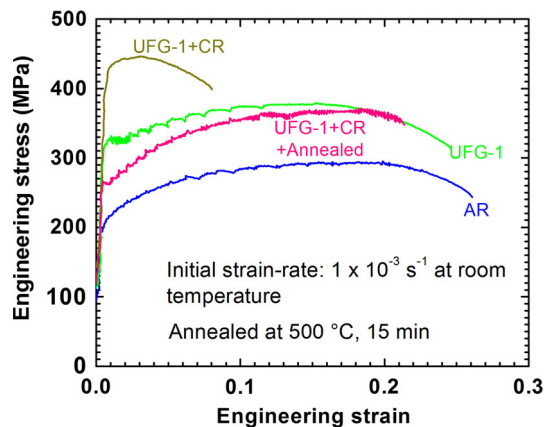


Fig. 11 Stress–strain curves illustrating the microstructural condition necessary for the formation of Lüders bands (UFG-1: AR+FSP (400 rpm))

this phenomenon, the removal of dislocations introduced during rolling should reintroduce the Lüders deformation in the stress–strain curve. The cold-rolled UFG-1 alloy was annealed at 773 K (500 °C) for 15 min and tested. The stress–strain curves indeed showed re-occurrence of this phenomenon (Fig. 11). Hence, annealing at 773 K (500 °C) caused recovery of dislocations thereby making the UFG material mobile dislocation deficient. It, therefore, indicates that the Lüders band formation observed in the present UFG alloy is in fact a result of lack of mobile dislocations.

Conclusions

- I. The FSP UFG Al–Mg–Sc alloy showed a discontinuous transition from elastic to plastic regime (Lüders deformation phenomenon). Below a critical grain size ($\sim 0.5 \mu\text{m}$) stress–strain curve showed elastic–perfectly plastic deformation behavior (UFG-4).
- II. Grain size and its distribution play an important role in the determination of the uniform ductility of UFG alloy. UFG-2 having average grain size of $0.63 \mu\text{m}$ and $\sim 10\%$ of the grains $>1 \mu\text{m}$ showed a moderately high uniform elongation (11.6 %) whereas UFG-4 having average grain size of $0.39 \mu\text{m}$ and all the grains $<1 \mu\text{m}$ showed disappointingly very low uniform elongation (3.4 %).
- III. The diminishing work hardening capacity of the UFG Al–Mg–Sc alloy can be attributed to reduced intragranular dislocation–dislocation interactions and enhanced dislocation recovery at grain boundaries.
- IV. As the average grain size decreases, the majority of the plastic deformation is concentrated in the necked region of the tensile samples.

- V. Very high negative strain rate sensitivity observed can be rationalized on the basis of enhanced grain boundary solutes and dislocation interaction at lower strain rate. The corresponding increase in apparent activation volume was similar to the values reported in the literature.
- VI. The formation of Lüders band can be attributed to the lack of mobile dislocations in FSP UFG alloy.

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